

Review about fundamental diagrams of pedestrian streams

Oct. 2nd 2015 | Armin Seyfried

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Overview

Motivation

Experiments and measurement methods

Unidirectional streams

- Common consent
 - Trends
 - Specific flow
- Transitions
- External influences

Comparison of pedestrians, bicycles and cars in a 1d-system

Motivation



Chowpatty-beach, Mumbai, Indien

Foto: J. Sorabjee, Urban Design Res. Inst.

Motivation



Dortmund Central Station, Germany

Foto: Jeroen van den Heuvel, Railway Netherlands

Motivation

Viewpoint of an engineer

Aims

- Transport infrastructures
(stations, airports, trains, ...)
- Design of escape routes
(stadiums, theater, schools, ...)
- Safety at big events
- ...

Tools and methods

- Legal regulations
- Guidelines and handbooks
- Computer simulations



Quantitative description of crowd movement necessary!

General aim: Prevent congestions for movement under orderly conditions!

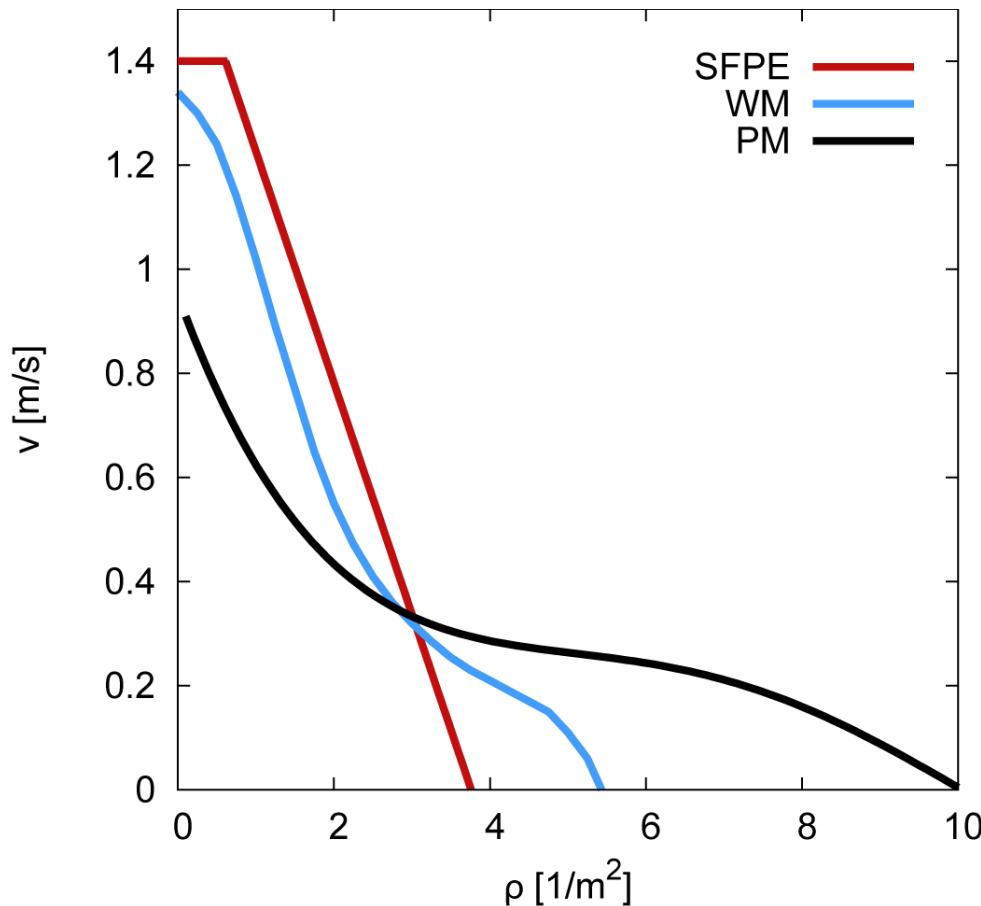
How to describe the movement of 'many' pedestrians?

- If many people are involved density, speed and flow are useful concepts
- Speed, density and flow are helpful to rate e. g.
 - Performance of pedestrian facilities (flow)
 - Level of service (density)
 - Travel or waiting times (speed)
- Speed, density and flow are related (Fundamental diagram)



Photo: Sebastião Salgado

Motivation



- SFPE P. J. DiNenno (2002) *SFPE Handbook ...*
PM V. M. Predtechenskii and Milinskii (1978)
WM U. Weidmann (1993) *Transporttechnik ...*

Motivation

Research groups studying systems with ‘many’ pedestrian (>20) by laboratory experiments and with determination of trajectories

- Univ. Milano-Bicocca, Italy: Vizari, Bandini et al.
- University of Tokio, Japan: Nishinari, Yanagisawa, Tadaki, et al.
- TU Delft, Netherlands: W. Daamen, S. Hoogendoorn, et al.
- PEDIGREE project, France: Jelić, Appert-Rolland, Pettré, et al.
- TU Berlin, Germany: Plaue, Baerwolf, et al.
- University of Hefei, China: W. Song, J. Ma, et al.
- Monash University, Australia: M. Sarvi, et al.
- TU Denmark, Denmark: J. Starke, et al.
- SL Rasch, Germany, R. Löhner, et al.
- University of Pamplona, Spain: A. Garcimartin, I. Zurigel et al.
- ...
- Univ. Cologne, Univ. Wuppertal and Research Centre Jülich, A. Schadschneider, M. Boltes, J. Zhang, ...

Experiments

Date	Place	# Pers.	Capturing	Aim
Mar. 2005	Jülich	34	manual	v(p) corridor
Nov. 2005	Jülich	60	manual	bottleneck width J(b)
Nov. 2006	Bergische Kaserne D-dorf	200	autom.	- v(p) corridor - bottleneck width J(b) - bottleneck length J(l), ...
Feb. 2008	Indien	64	manual	v(p) corridor
July 2008	Wuppertal	50	manual	v(p) corridor, motivation
Apr. 2009	ESPRIT Arena /	400	autom.	- stands (exits, stairs), stairs, ... - corridor, corners, junctions, ... - field studies on stairs J(p)
June 2013	Messe Düsseldorf	1000	autom.	development of congestions
Jan. 2015	Schools	200	Autom.	- v(p) corridor, heterogeneity - bottlenecks, groups

Video streams, trajectories,.... <http://www.fz-juelich.de/ias/jsc/cst>

Experiments

BaSiGo experiments

- Founded by the BMBF
- Fairground Düsseldorf, Hall 14



Experiments

BaSiGo experiments

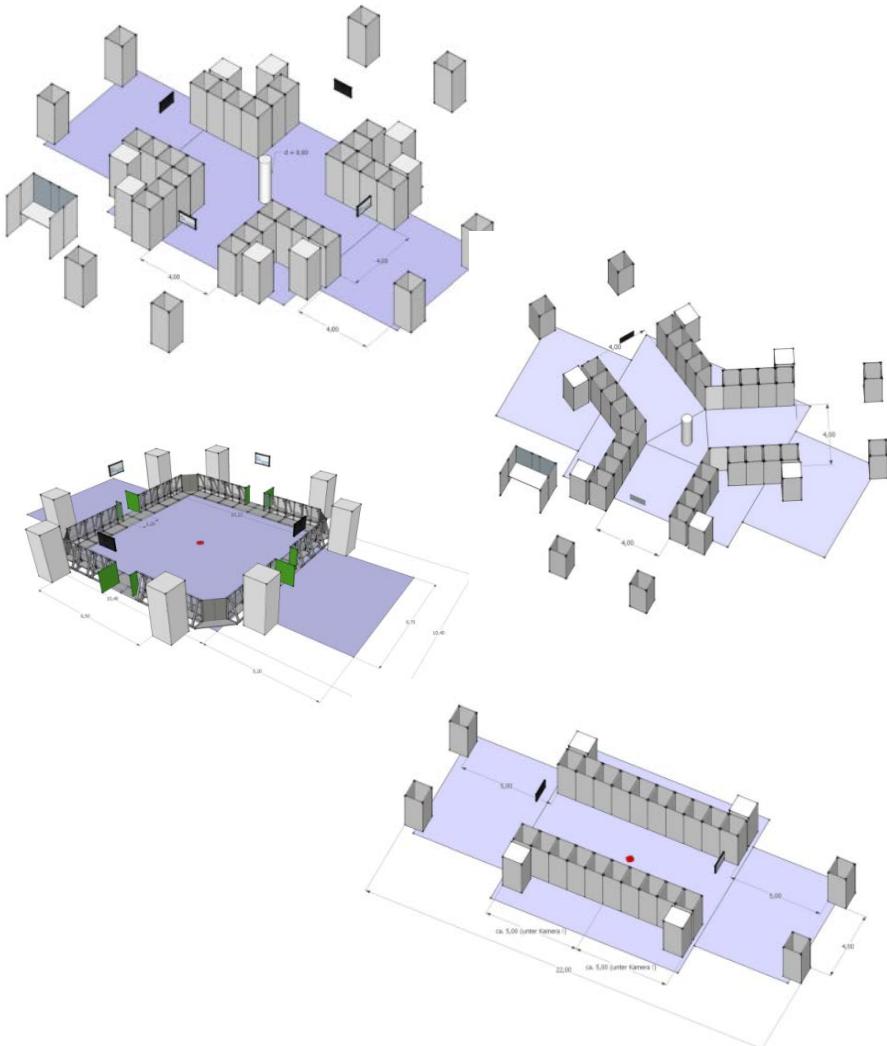
- Founded by the BMBF
- Fairground Düsseldorf, Hall 14
- Cooperation:
 - Univ. Siegen
 - IBIT GmbH
 - University of Essex ([Talk N. Bode](#))
- Around 50 staff and supporters



Experiments

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- 5 days, 31 experiments, 200 runs



Experiments

BaSiGo experiments

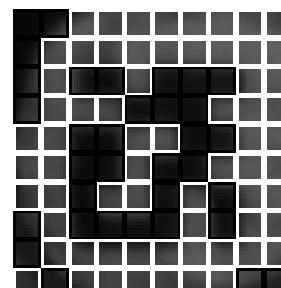
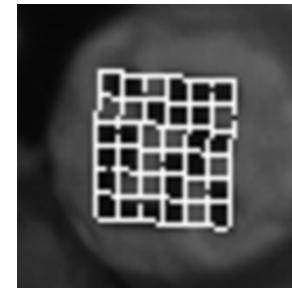
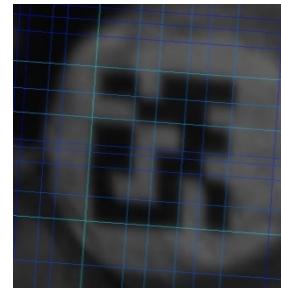
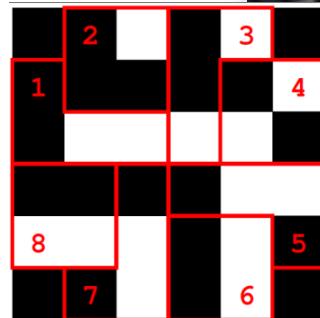
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- Grid with 28 industrial cameras, additional HD-, Stereo-, GoPro and spectacle cameras



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- Individual tracking



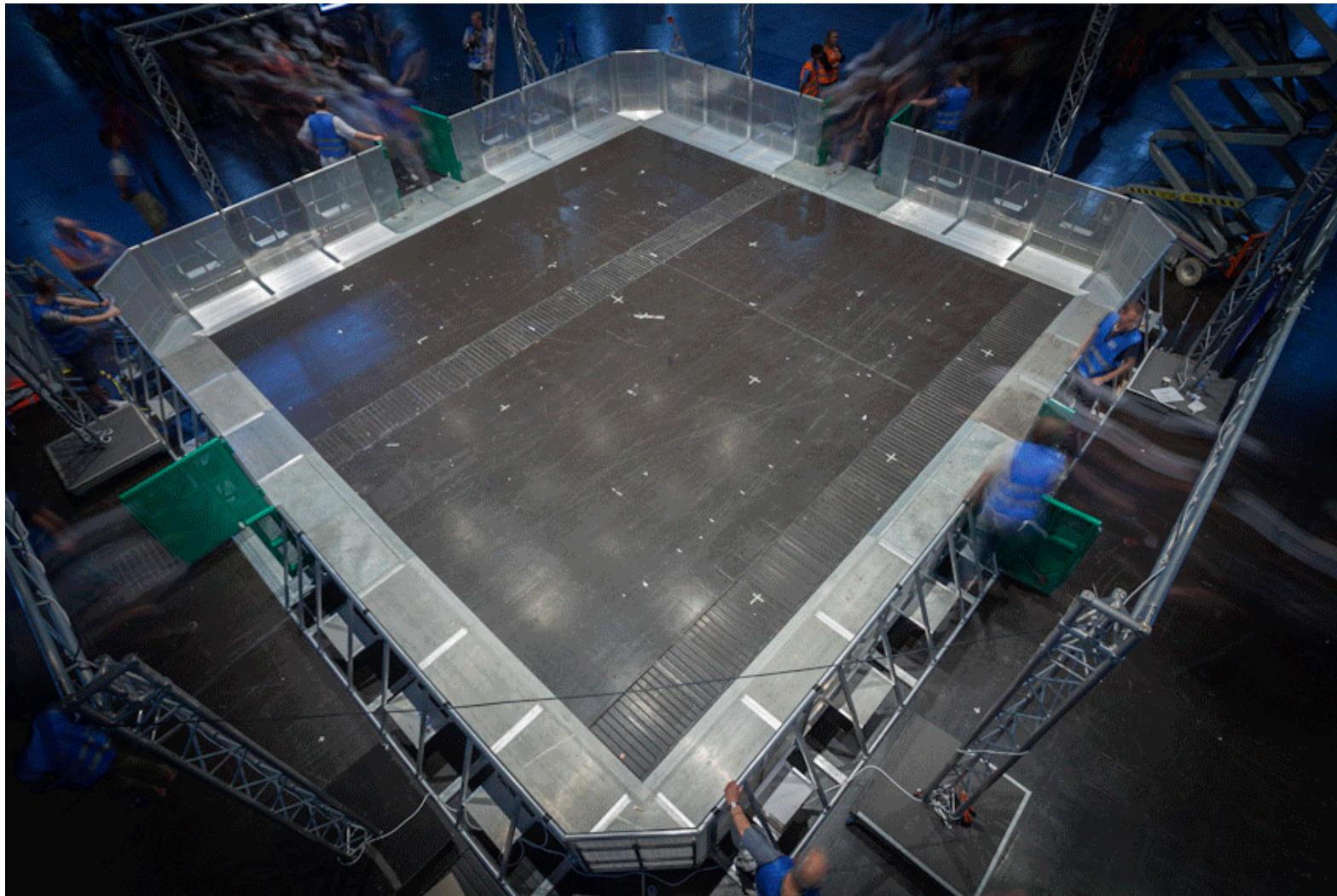
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BaSiGo experiments

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- Around 50 staff and supporters
- 5 days, 31 experiments, 200 runs
- Grid with 28 industrial cameras,
additional HD-, Stereo-, GoPro
and spectacle cameras
- Individual tracking
- 2200 participants in total,
max. 950 on one day



Experiments BaSiGo



Experiments BaSiGo: Crossing streams

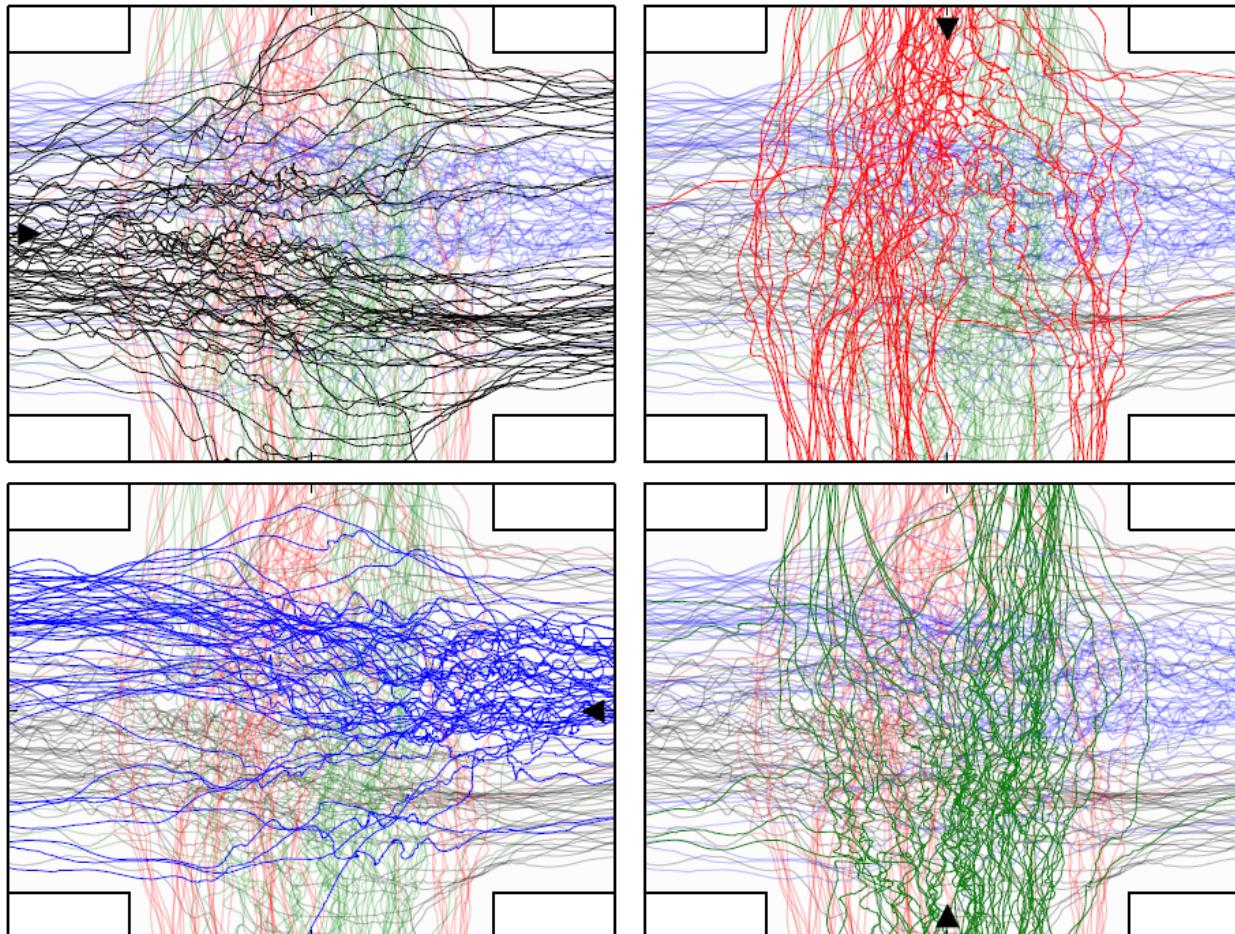


Experiments BaSiGo: Crossing streams



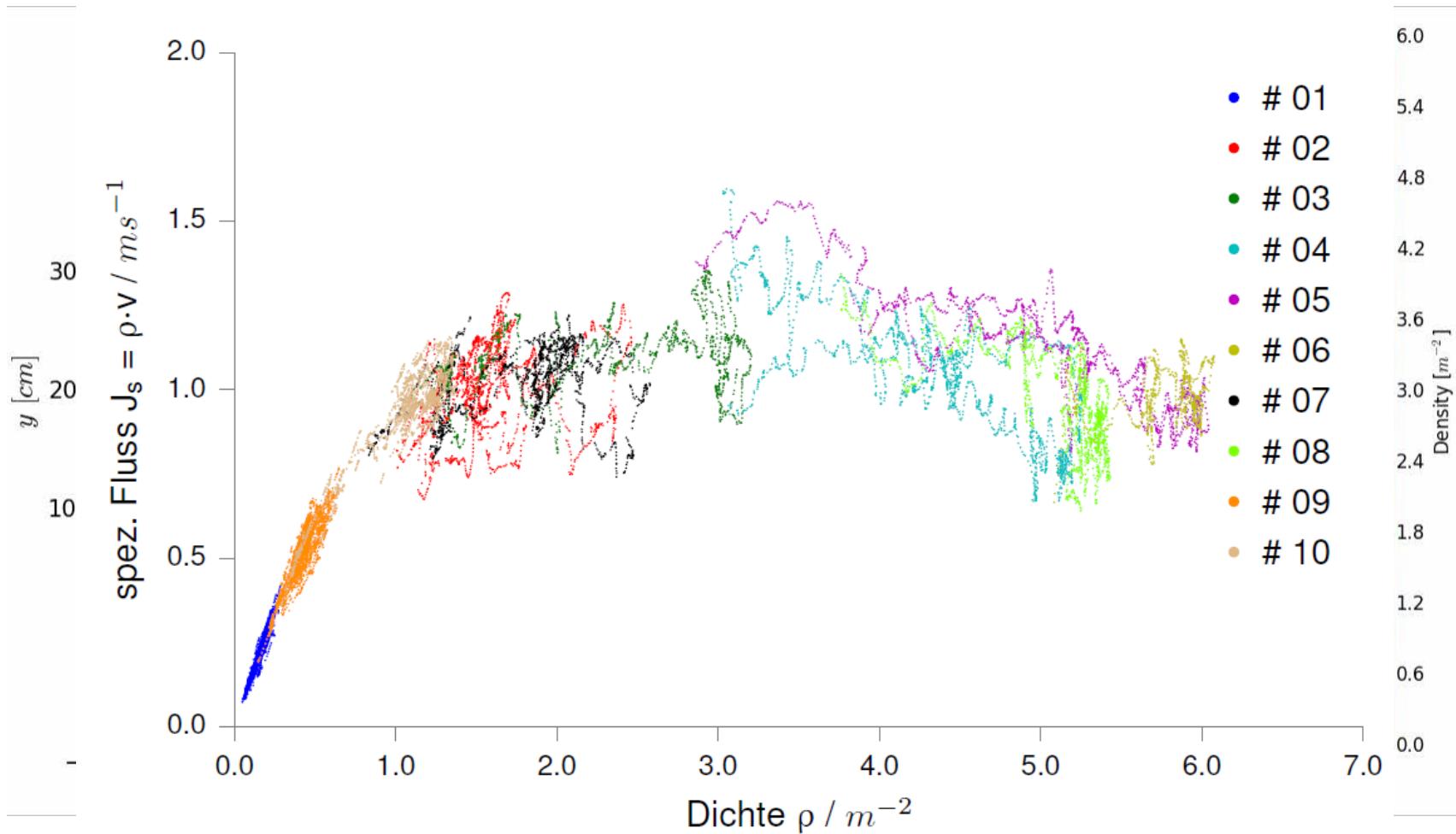
Experiments BaSiGo: Crossing streams

Trajektorien*



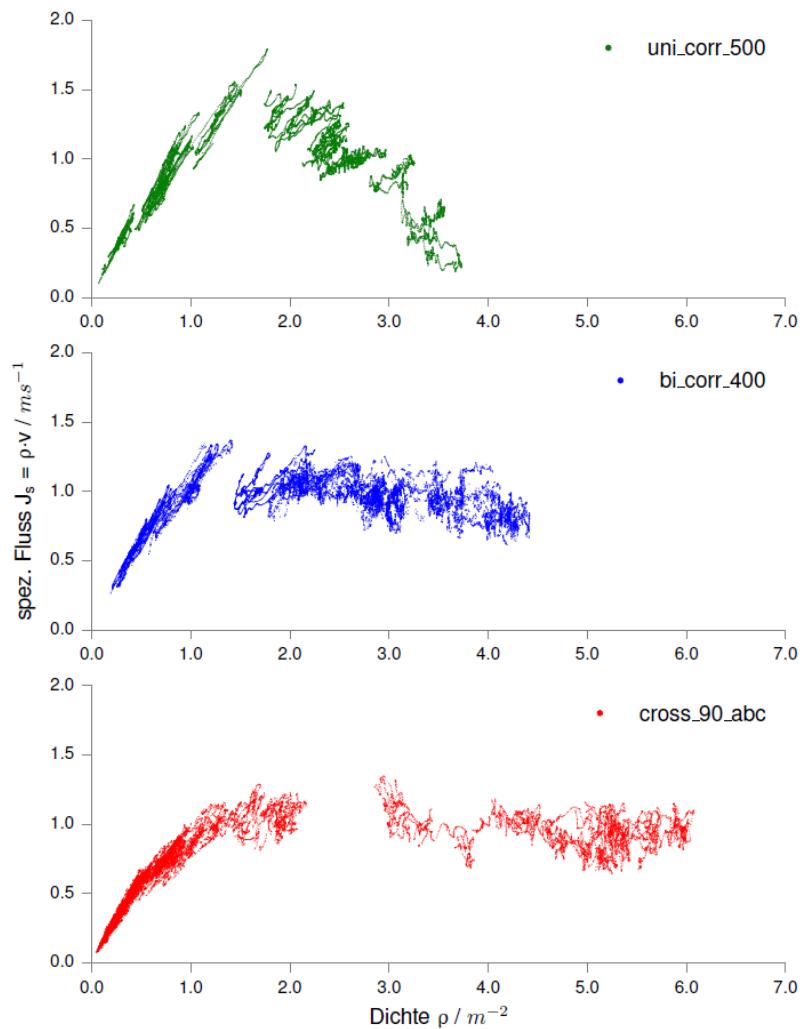
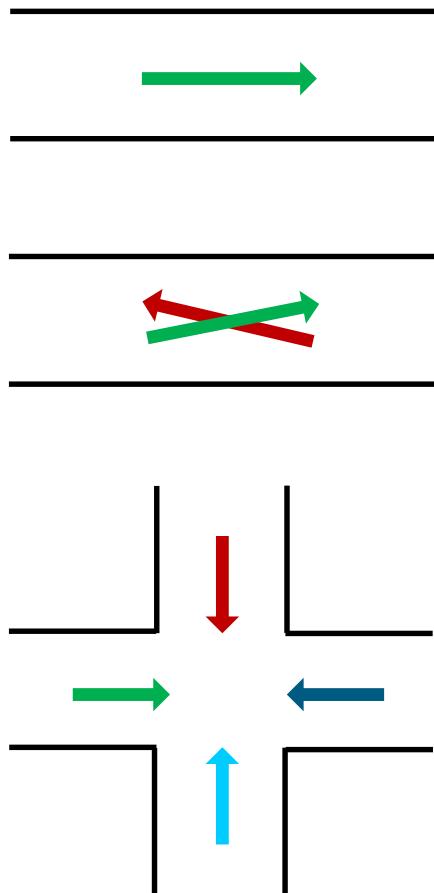
* Masterthesis, David Bodenstein, Mai 2015

Experiments BaSiGo: Crossing streams



Experiments BaSiGo: Crossing streams

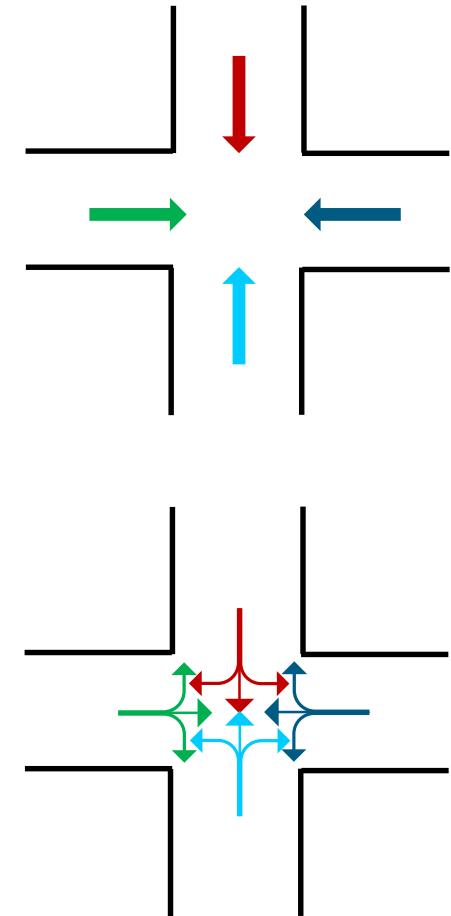
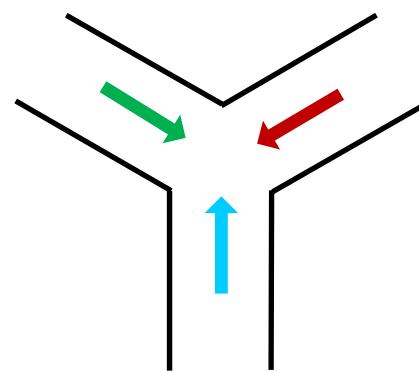
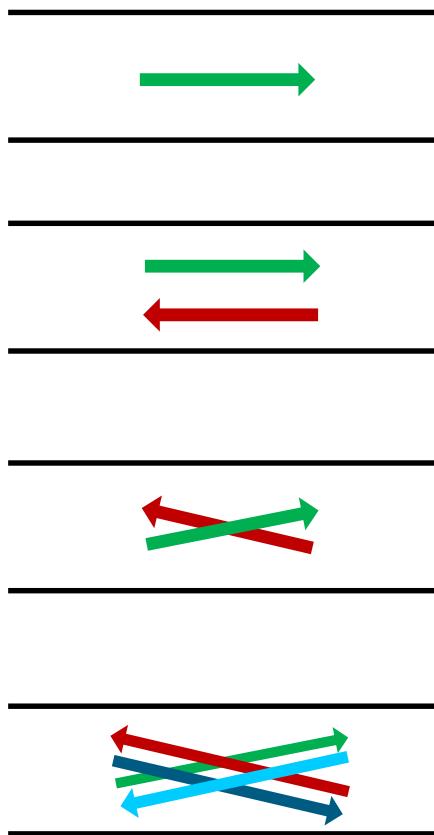
Fundamental diagrams



* Masterthesis, David Bodenstein, May 2015

Introduction

Uni- and multidirectional streams at different types of facilities



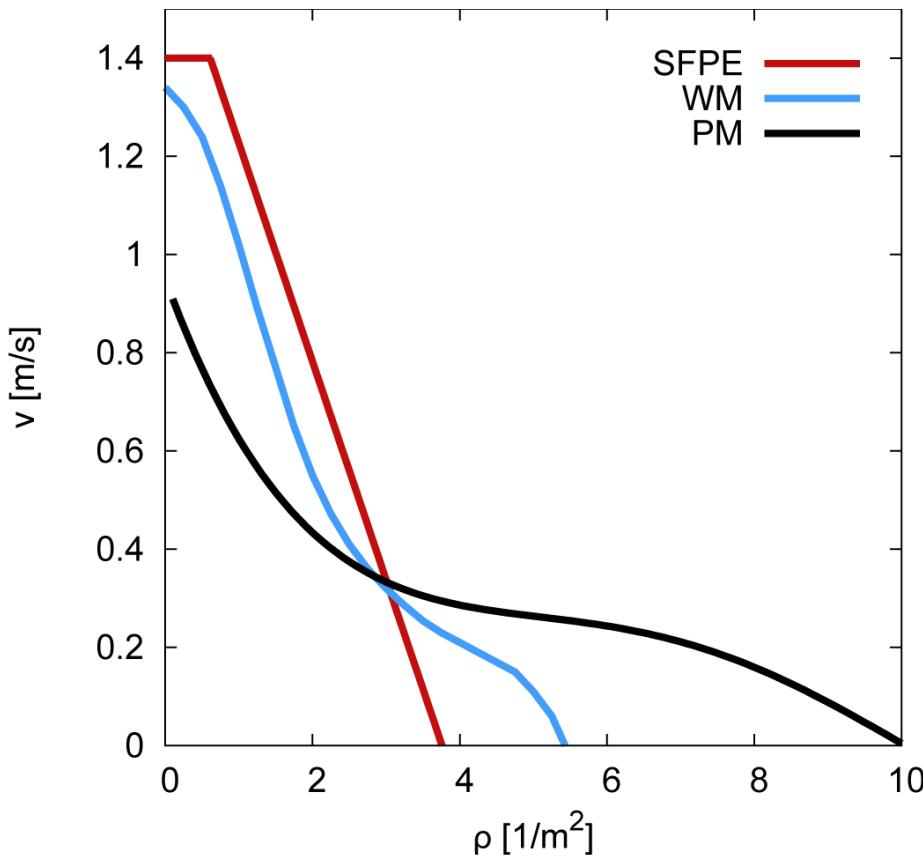
NOT INCLUDED: Bottlenecks, doors, ramps, stairs or mixtures

Unidirectional flow - Common consent

Now:

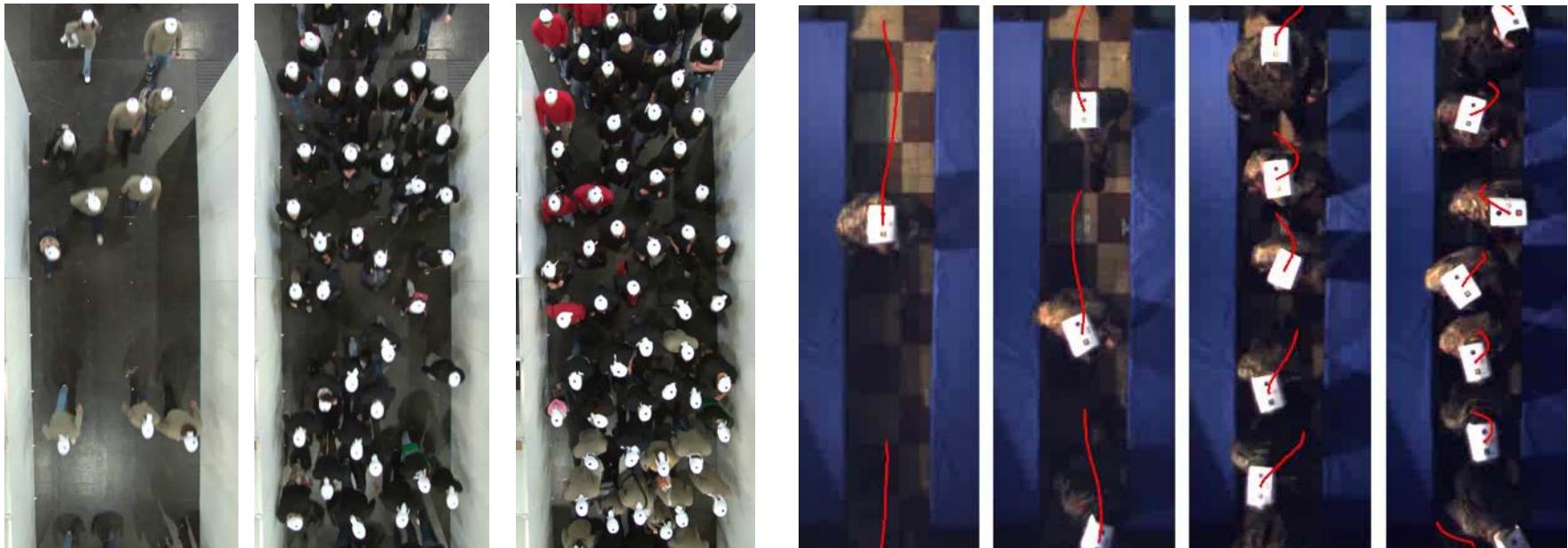


Unidirectional flow - Common consent

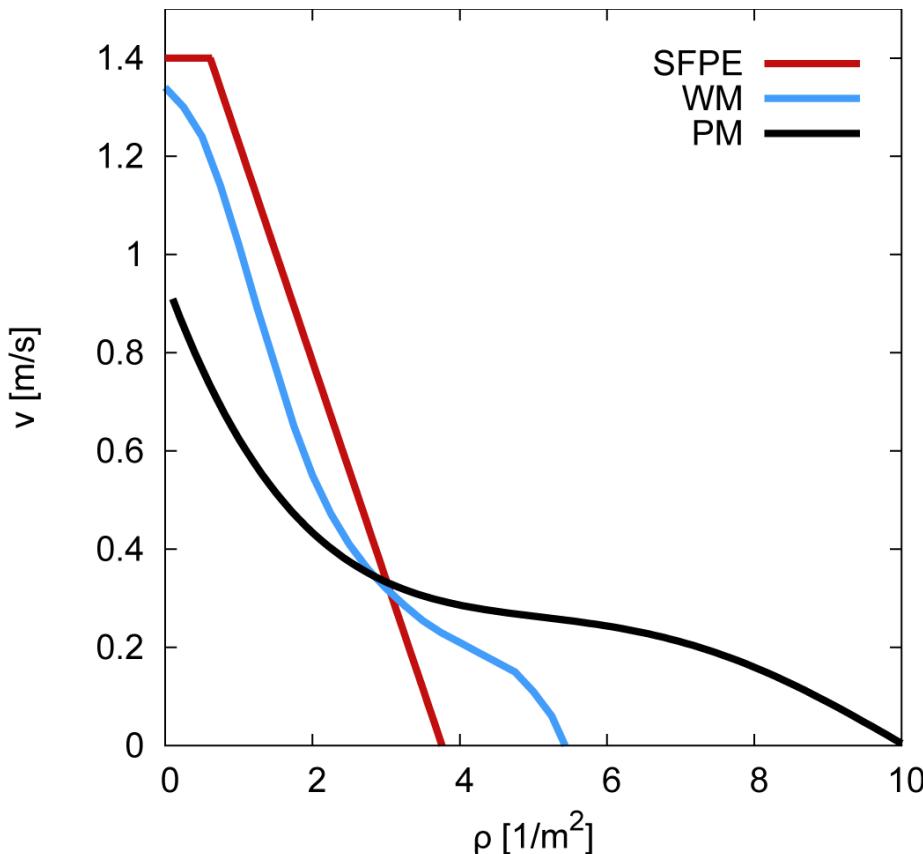


- SFPE P. J. DiNenno (2002) *SFPE Handbook ...*
PM V. M. Predtechenskii and Milinskii (1978)
WM U. Weidmann (1993) *Transporttechnik ...*

Unidirectional flow - Common consent

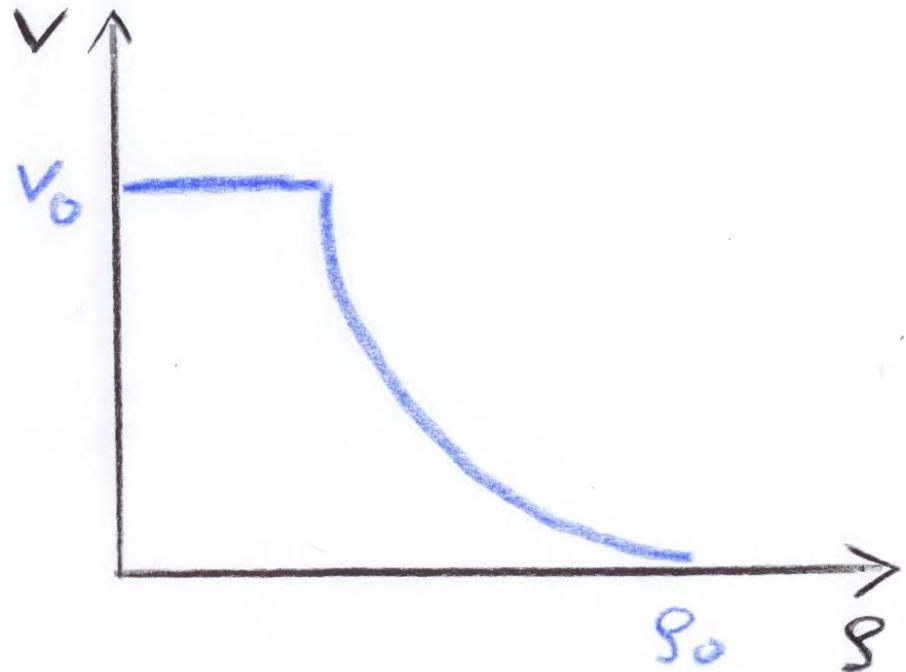
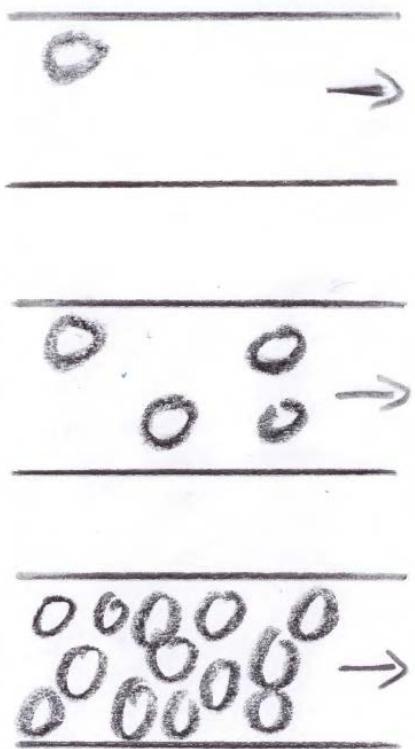


Unidirectional flow - Common consent



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Unidirectional flow - Common consent

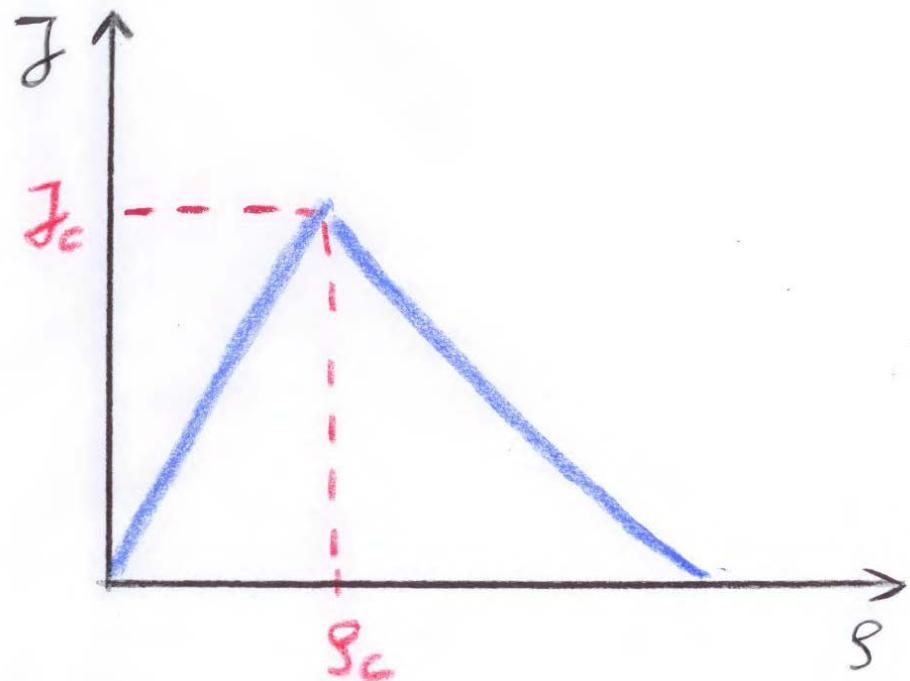
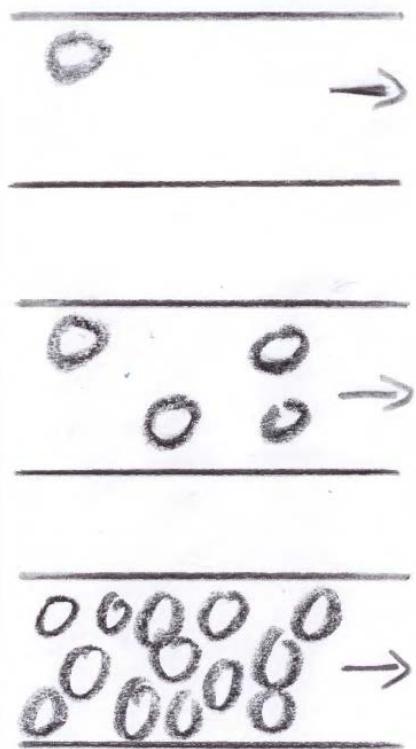


ρ small $\rightarrow v_0$ free flow speed

ρ high $\rightarrow v$ decreases

ρ_0 $\rightarrow v = 0$ (jamming)

Unidirectional flow - Common consent

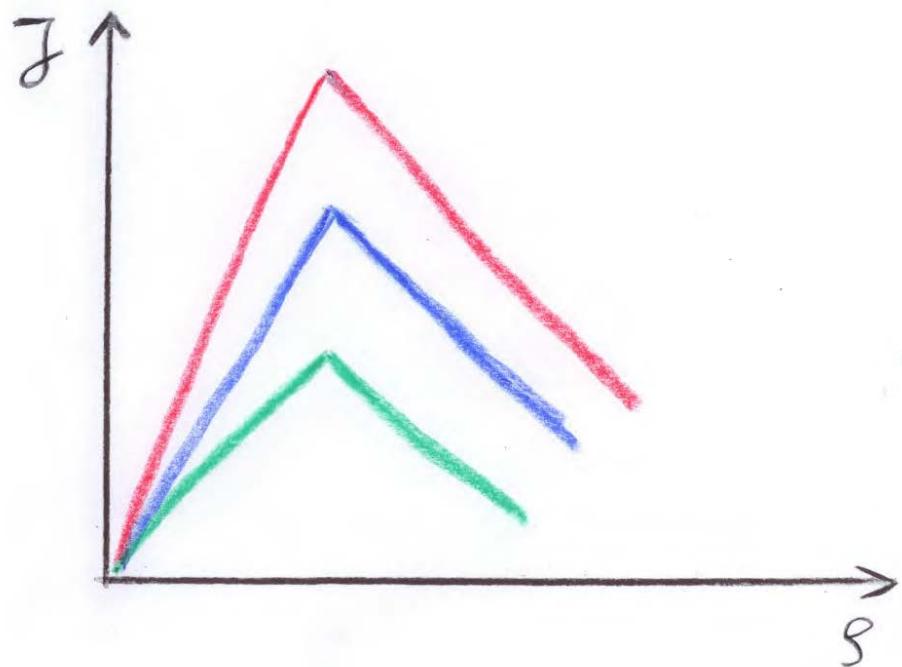
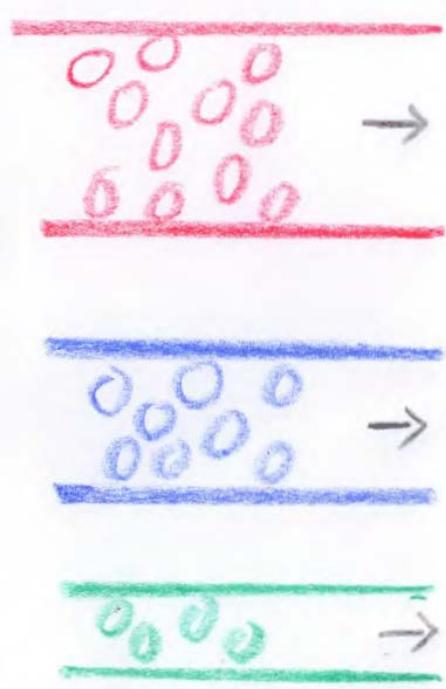


$\rho < \rho_c \rightarrow J$ increases: Free flow state

$\rho = \rho_c \rightarrow J_c$ maximum: Capacity

$\rho > \rho_c \rightarrow J$ decreases: Congested state

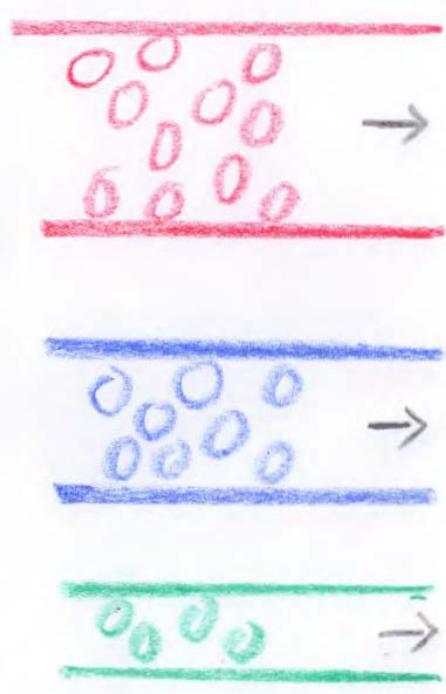
Unidirectional flow – Specific flow



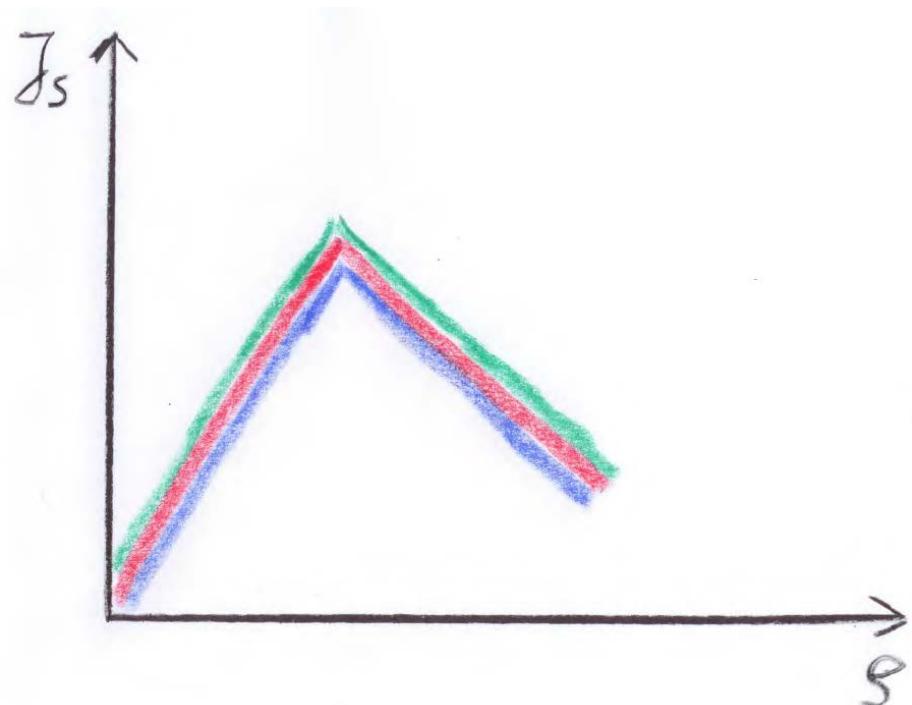
$b_1 > b_2 > b_3$ width increases → flow increases

Zhang et al., 2011, Transitions in pedestrian fundamental diagrams of straight corridors and T-junctions, J Stat Mech, P06004

Unidirectional flow – Specific flow



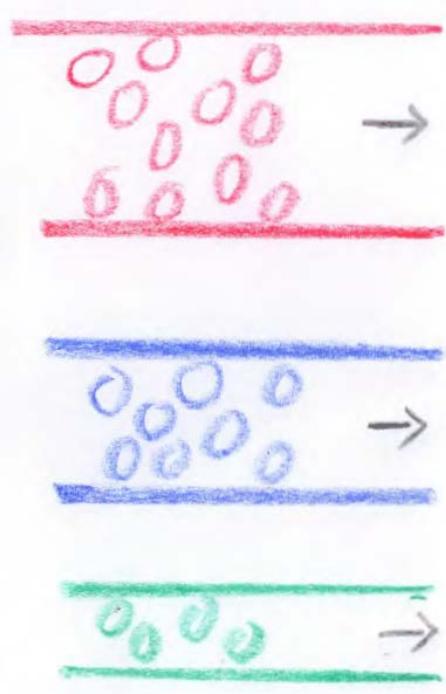
$$J_s = J/b$$



J_s : Fd's for \mathbf{b}_1 , \mathbf{b}_2 , \mathbf{b}_3 lie upon each other

Zhang et al., 2011, Transitions in pedestrian fundamental diagrams of straight corridors and T-junctions, J Stat Mech, P06004

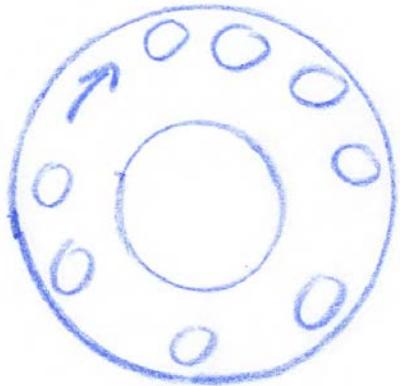
Unidirectional flow – Specific flow



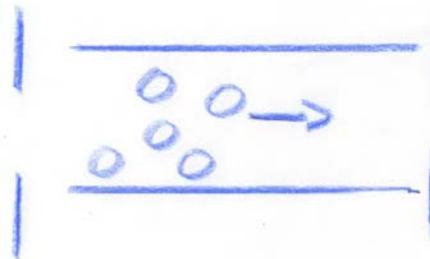
No data for high densities!

Zhang et al., 2011, Transitions in pedestrian fundamental diagrams of straight corridors and T-junctions, J Stat Mech, P06004

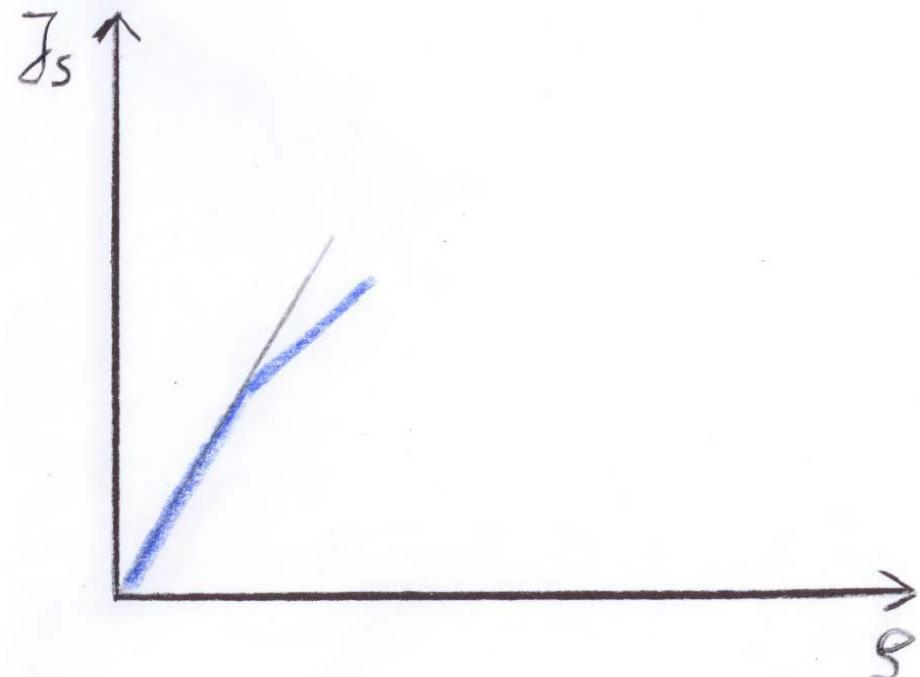
Fd: Transitions (free flow regime)



1)



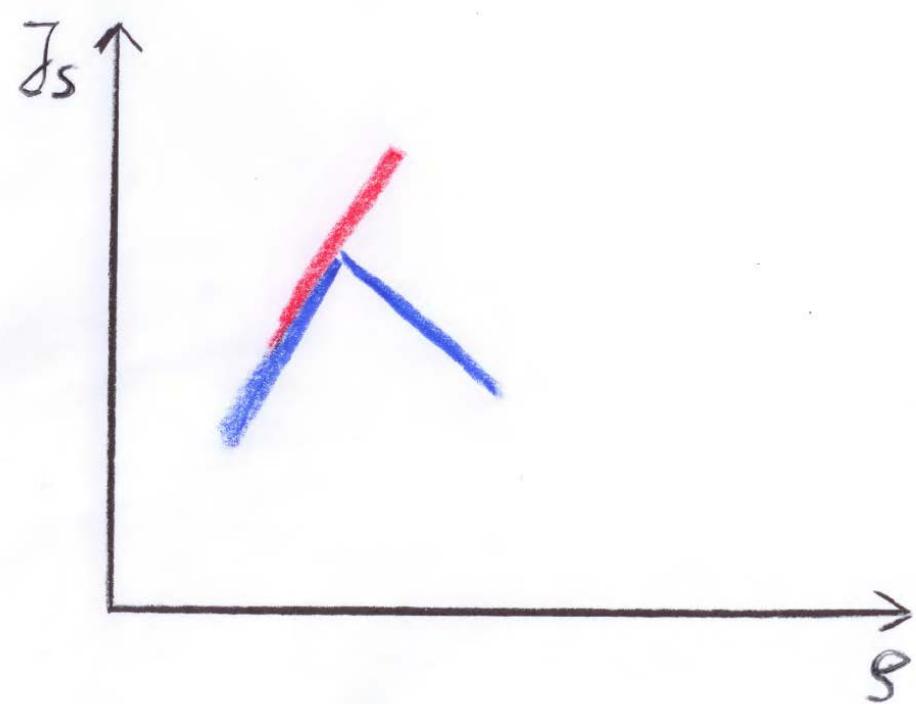
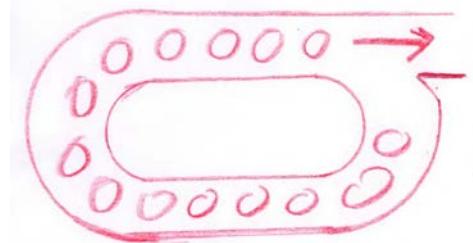
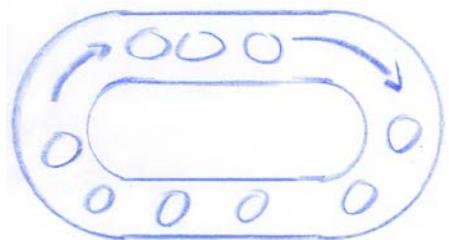
2)



1) Jelic et al., 2012, Properties of pedestrians walking in line: Fundamental diagrams, Phys Rev E 85, 036111

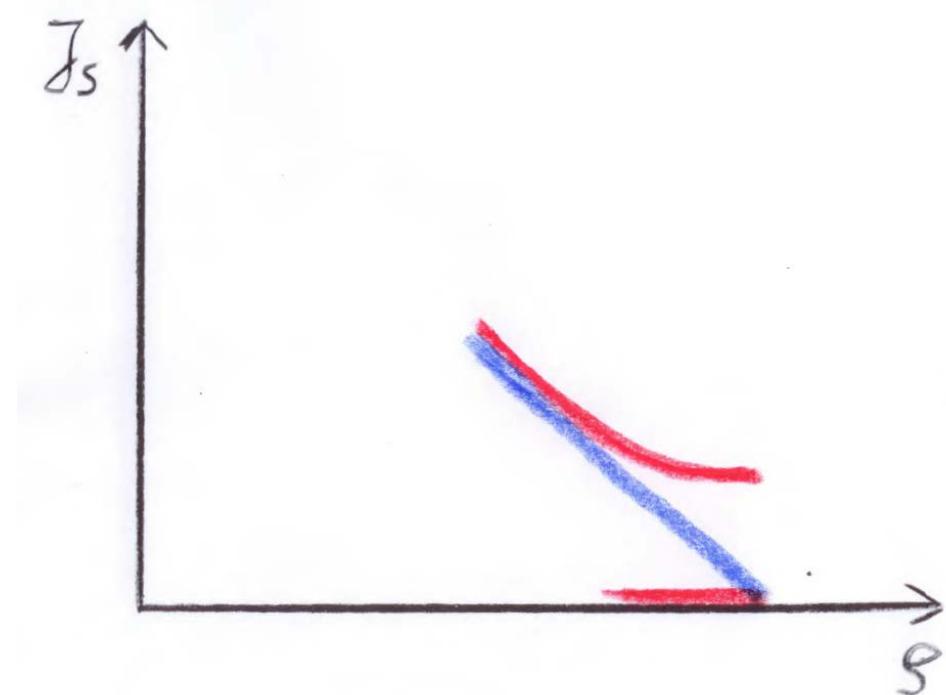
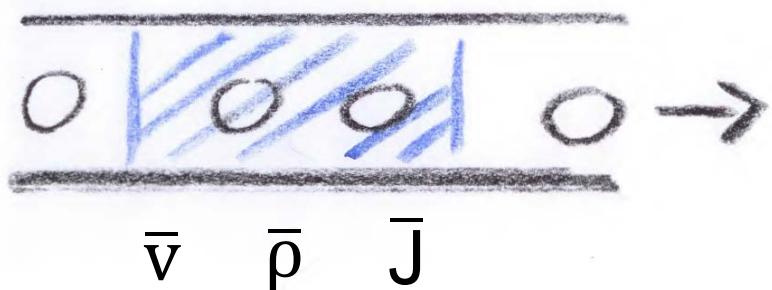
2) Zhang et al., 2011, Transitions in pedestrian fundamental diagrams of straight corridors and T-junctions, J Stat Mech, P06004

Fd: Transitions (at the capacity)



Zhang et al., 2014, Effects of Boundary Conditions on Single-File Pedestrian Flow, ACRI, Lecture Notes in Computer Science (LNCS), to appear

Fd: Transitions (stop and go waves)

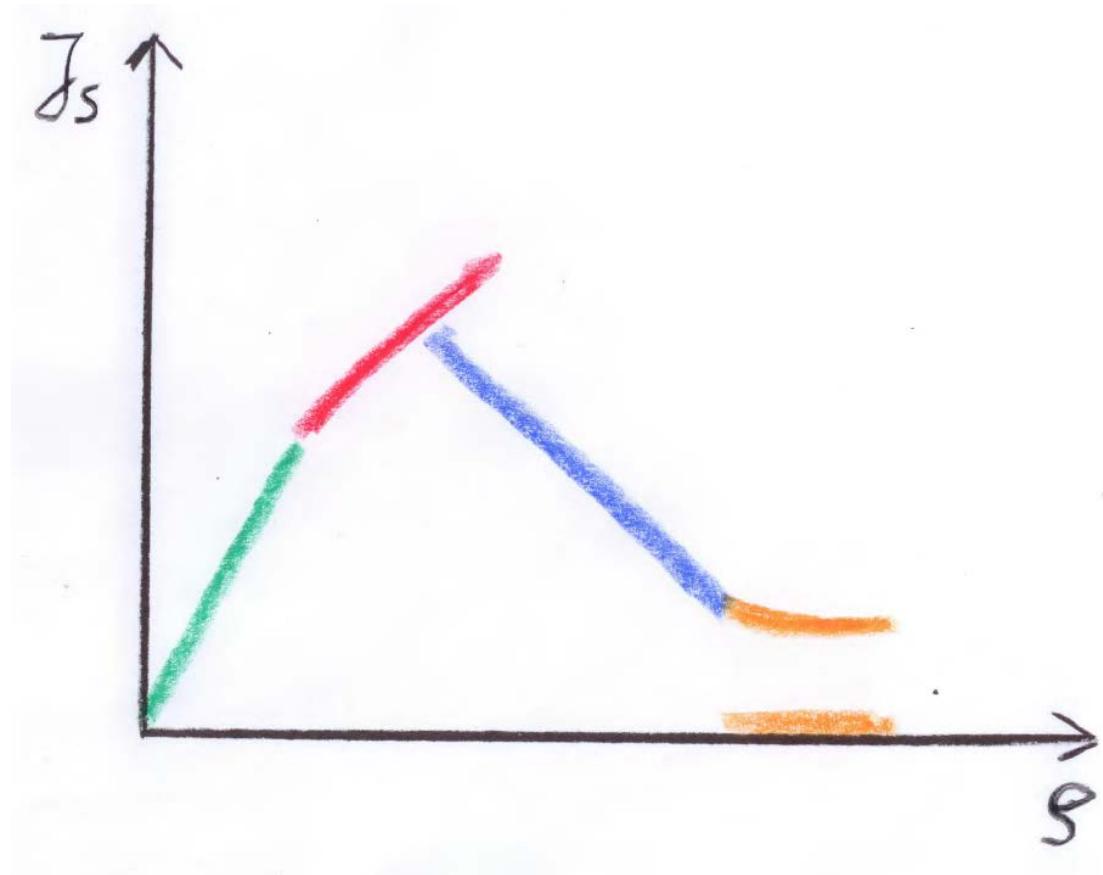


Portz, A. et al. (2011) Analyzing Stop-and-Go Waves by Experiment and Modeling
Pedestrian and Evacuation Dynamics 2010, Springer, S. 577-586

Fundamental diagram: Summary

Regimes of the Fd

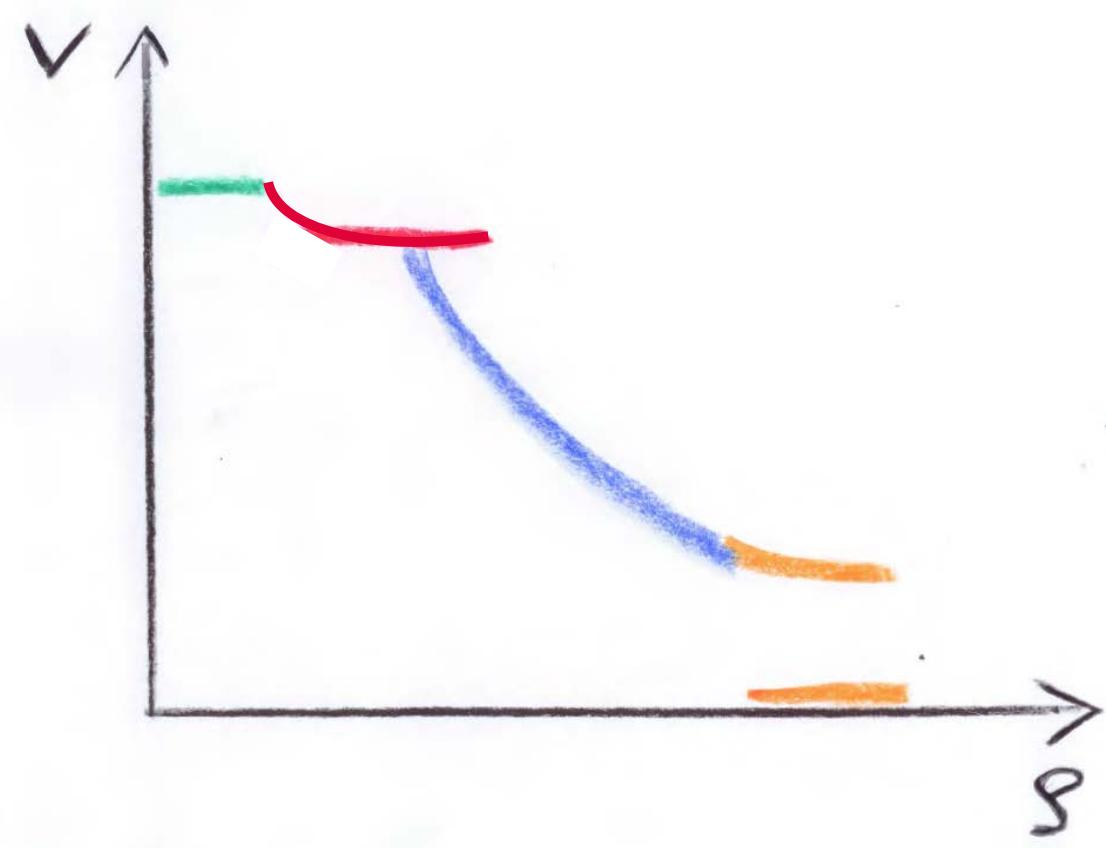
- Free flow regime 1
- Free flow regime 2
- Congested state 1
- Congested state 2
with STOP and GO



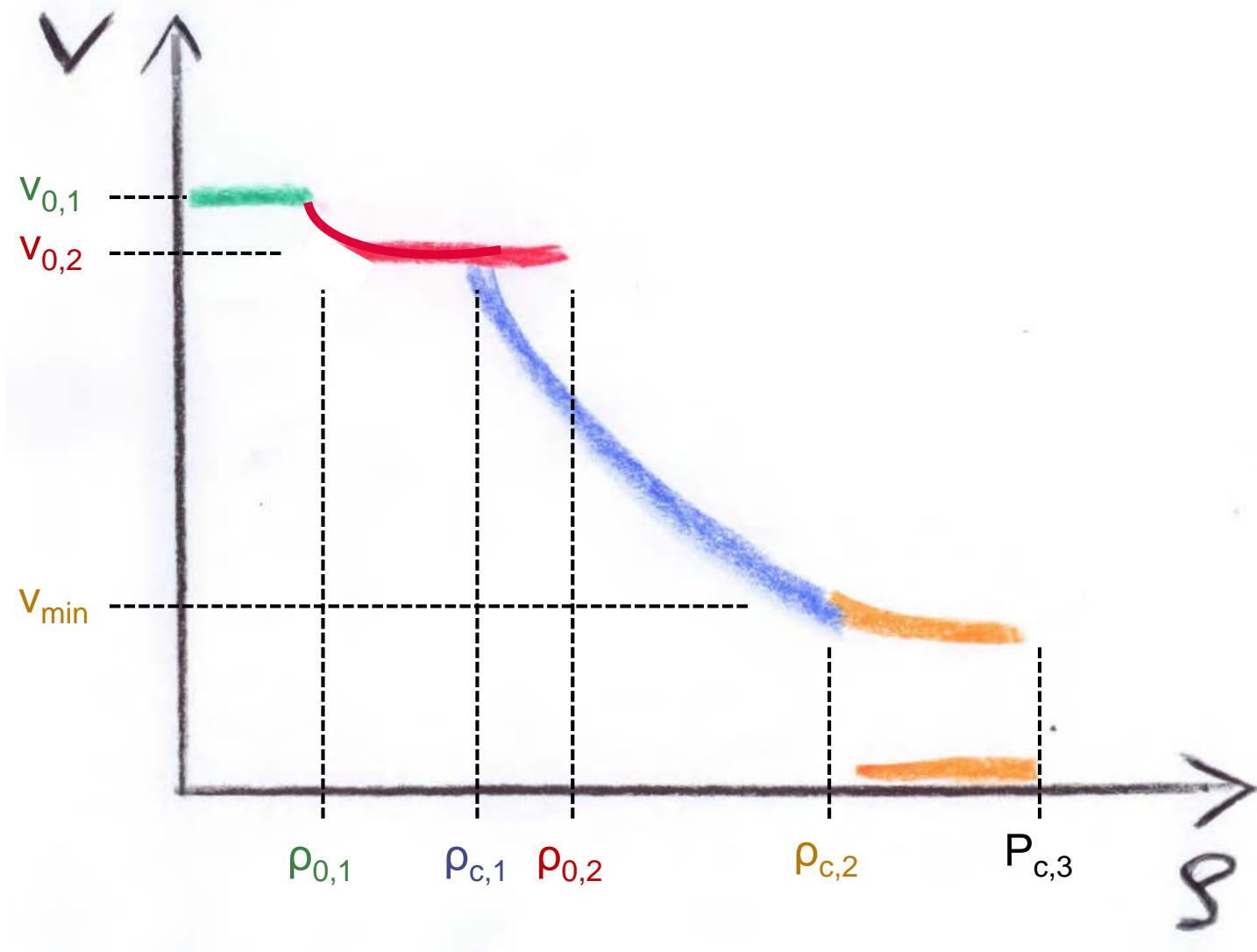
Fundamental diagram: Summary

Regimes of the Fd

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Fundamental diagram: Summary



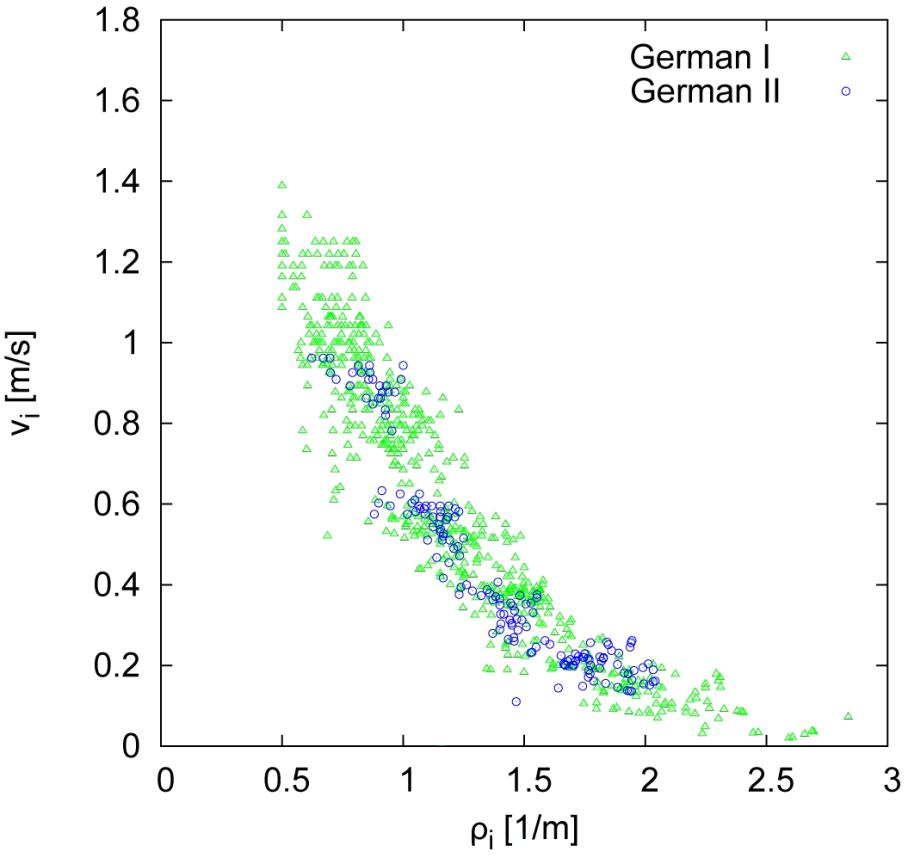
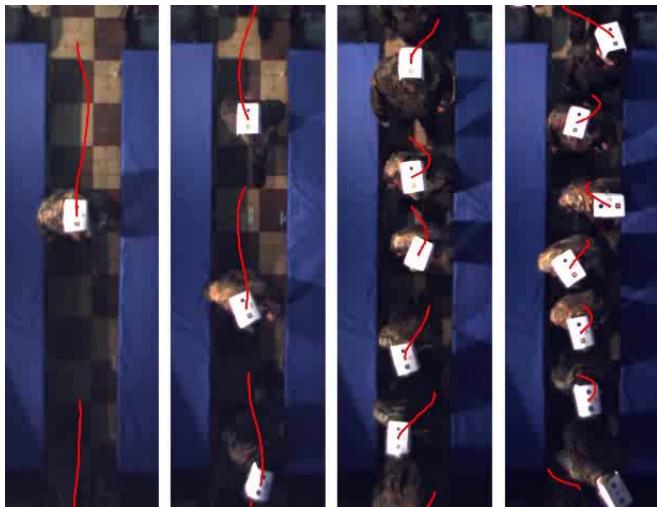
Comparison of 1d-FD for different pedestrians and environments

Yanagisawa, D.; Tomoeda, A. & Nishinari, K., *Improvement of pedestrian flow by slow rhythm*, Phys. Rev. E, American Physical Society, 2012, 85, 016111

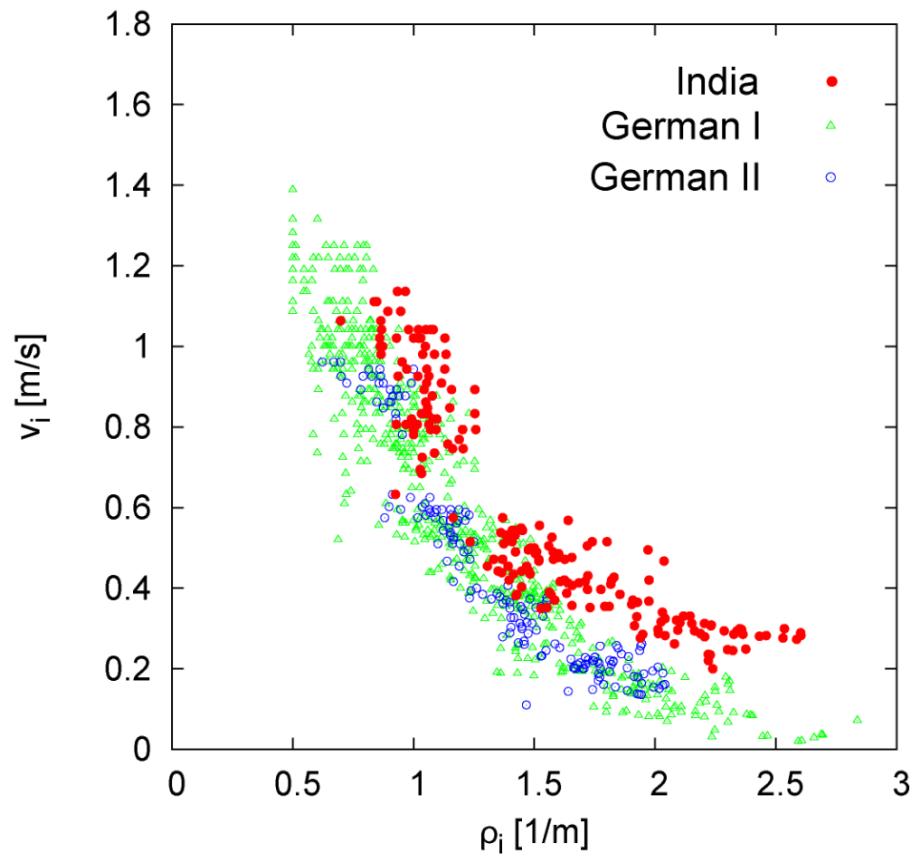
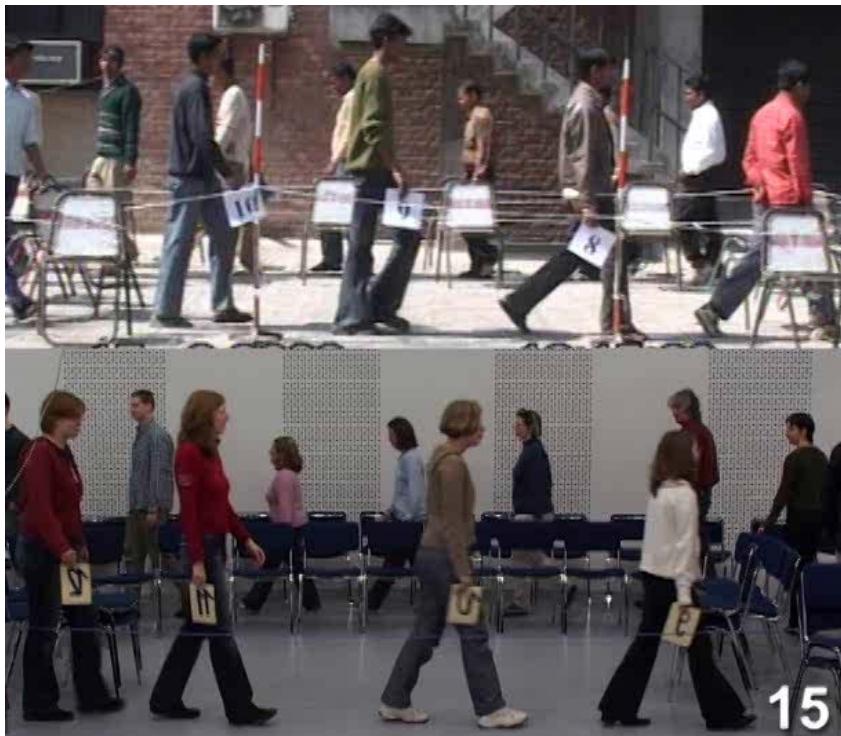
U. Chattaraj et al., Advances in Complex Systems 12(3), 393-405, 2009

J. Lukowski, Masterthesis, Univ. Wuppertal (2009)

Soldiers versus students

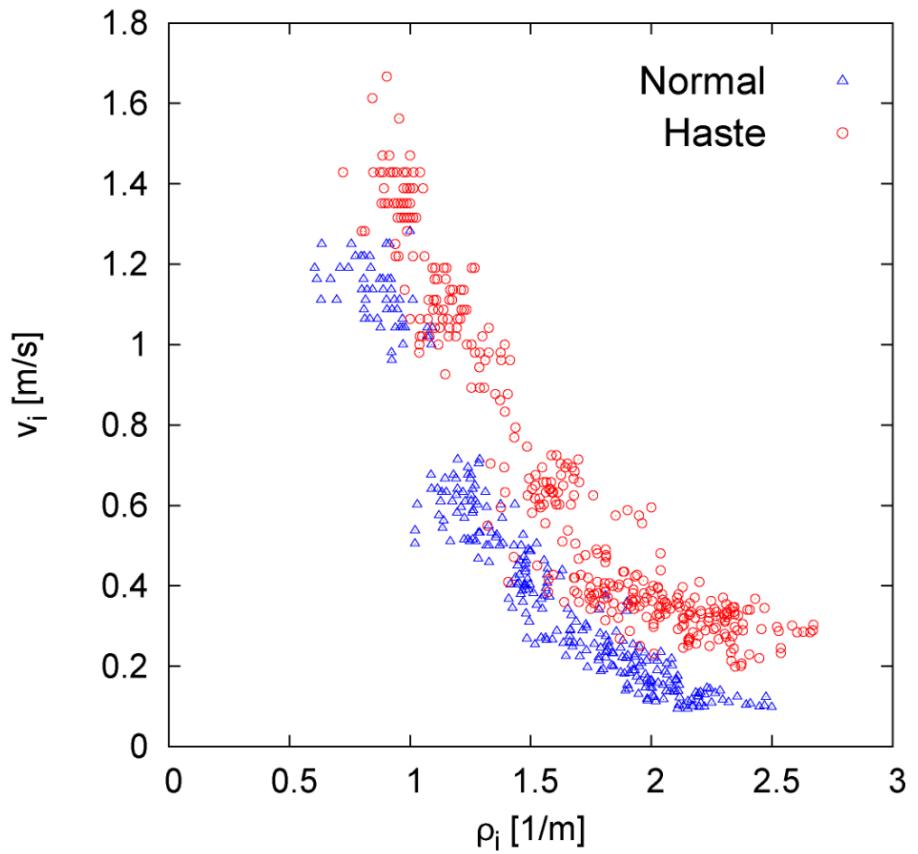


India (male) versus German I and II



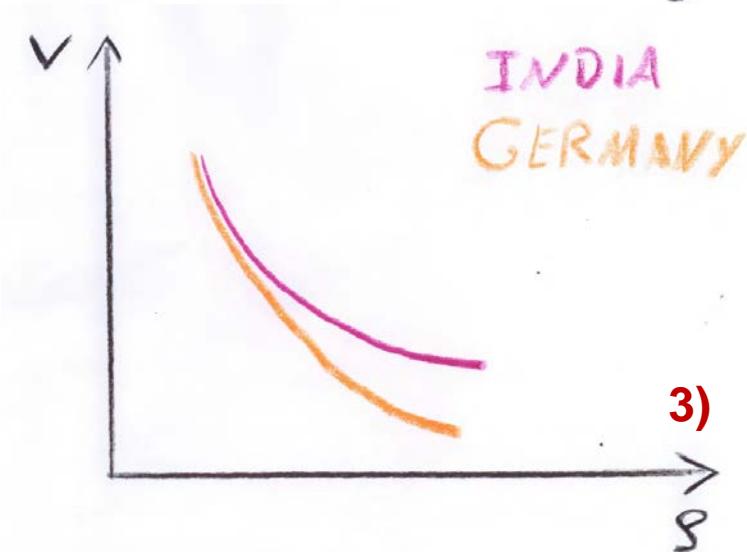
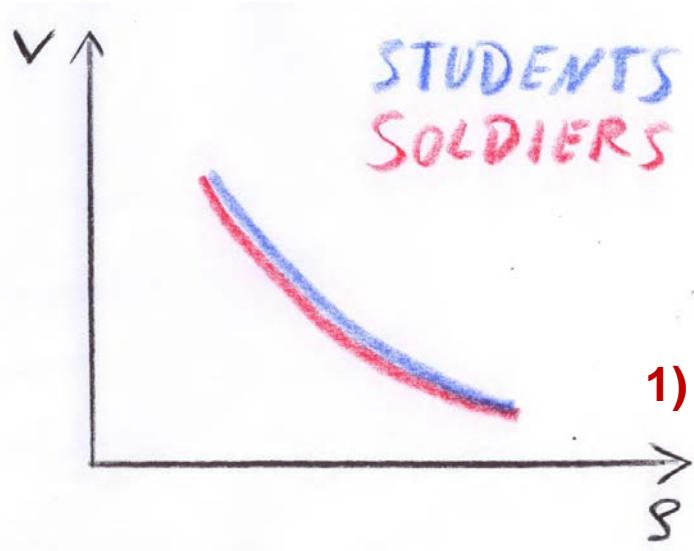
*U. Chattaraj et al., Advances in Complex Systems 12(3), 393-405, 2009

Influence of motivation*



*J. Lukowski, Masterthesis, Univ. Wuppertal (2009)

FD: Potential influences

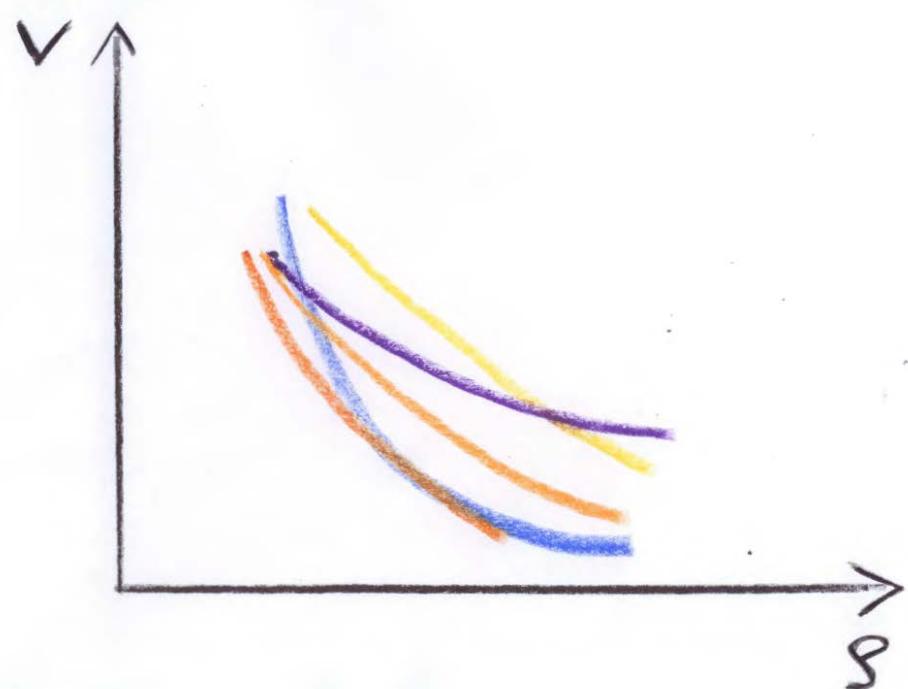


- 1) Portz, et al. (2011) PED 2010
- 2) Lukovski (2008) Masterthesis Wuppertal
- 3) Chattaraj (2009) Adv Comp Sys 12(3), 393
- 4) Nishinari, Tokyo, Japan
- 5) Delft
- 6) Hefei
- 7) SL-Rasch, ...

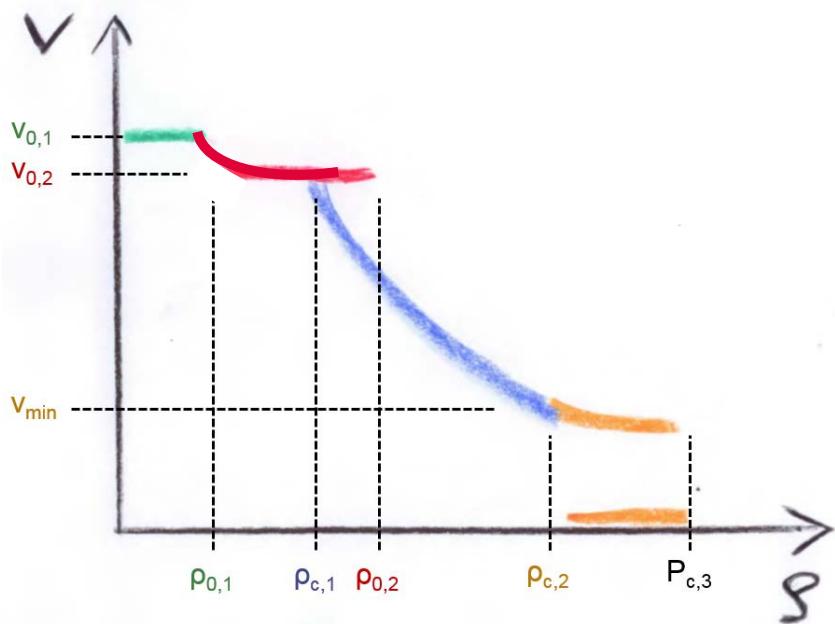
FD: Potential influences

Other potential influences

- Age
- Gender
- Social relations (groups)
- Fitness
- Size
- Weight
- Weather
- Motivation
- Attention
- Trip purpose
- Lighting
- Season
- Ground
- Indoor or outdoor
- Daytime
- Living space
- Distractions, ...

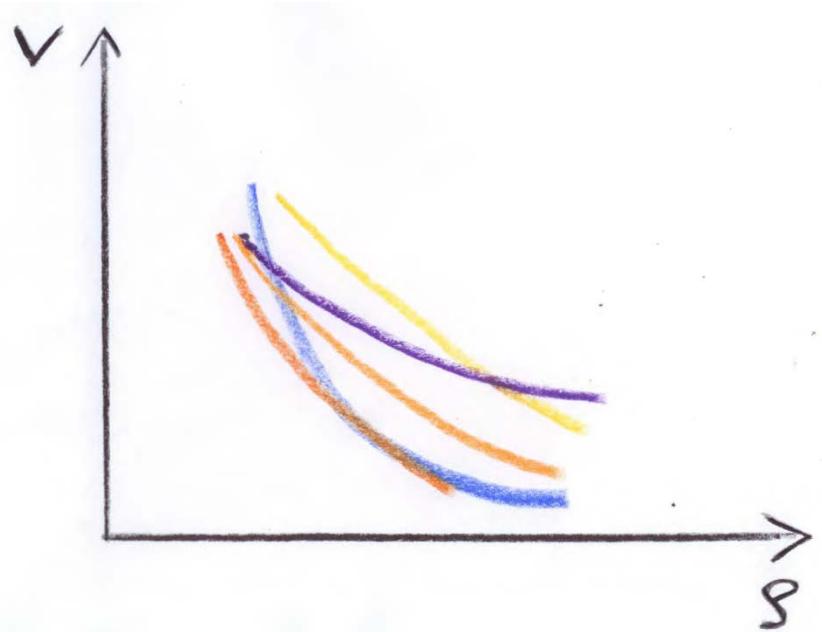


Fundamental diagram: summary



Regimes of the Fd

- Free flow regime I ($\rho_{0,1}, v_{0,1}$)
- Free flow regime II ($\rho_{0,2}, v_{0,2}$)
- Congested state I ($\rho_{c,1}, v_{0,2}$)
- Congested state II ($\rho_{c,2}, v_{\min}, \rho_{c,3}$)
with STOP and GO



Potential influences on $\rho_{i,j}, v_{i,j}$

- Age
- Gender
- Training
- Weather
- Motivation
- Attention
- Lighting, ...

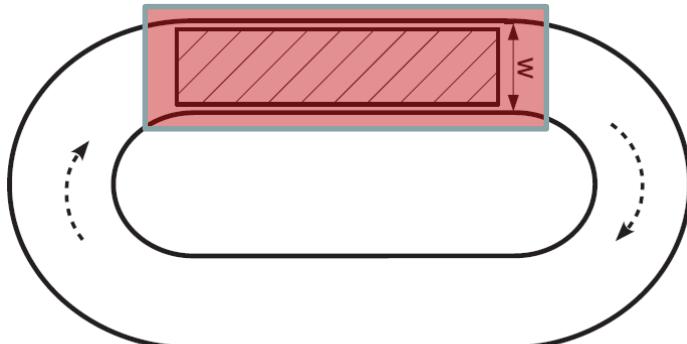
Comparison of 1d-FD of cars, bicycles and pedestrians

Zhang, Mehner, Holl, Boltes, Andresen, Schadschneider and Seyfried
Universal flow-density relation of single-file bicycle, pedestrian and car motion
Physics Letters A 378 (2014) 3274–3277

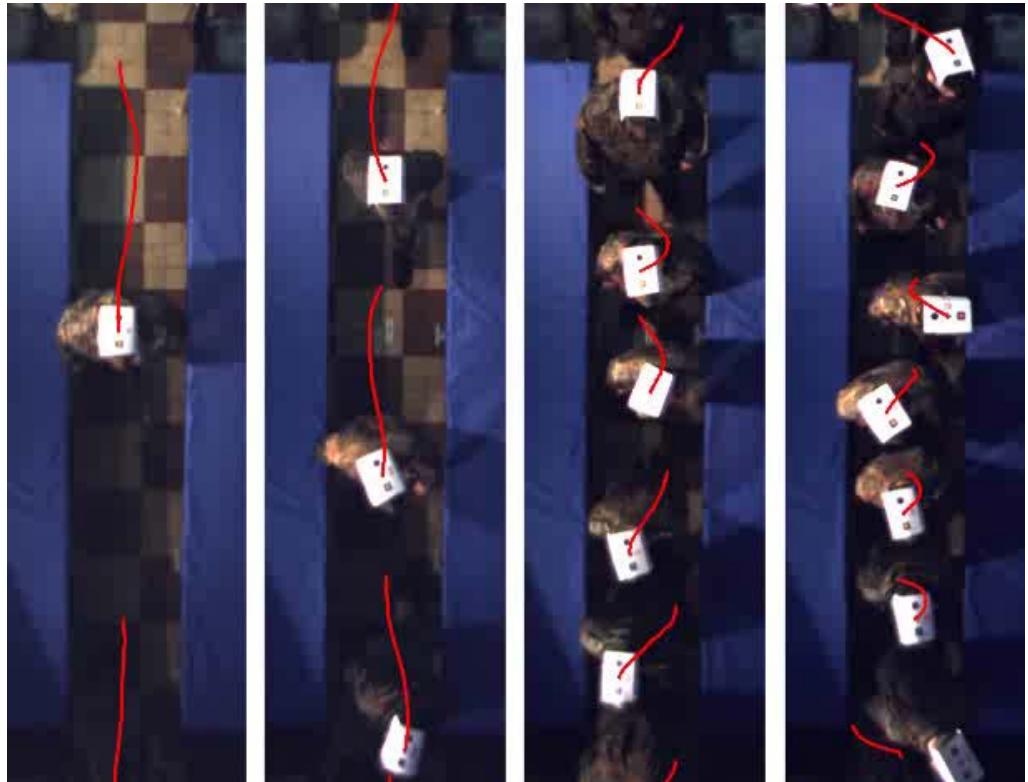
Pedestrians

Setup details

- Closed system
- Oval shape circuit with length
 $L = 26 \text{ m}$



- Number of pedestrians
 $N = 14, 17, 20, 22,$
 $25, 28, 34, 39,$
 $45, 54, 62, 70$



N=14

N=25

N=39

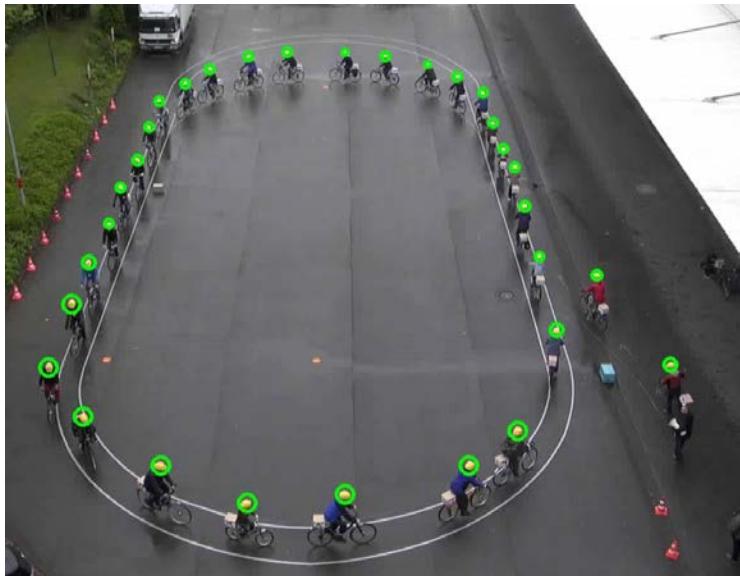
N=56

Seyfried et al., 2010, PED 2008

Bicycles

Setup details

- Oval shape circuit with length
 $L = 86 \text{ m}$
- 6 runs with number of bicycles
 $N = 5, 10, 15,$
 $18, 20, 33$

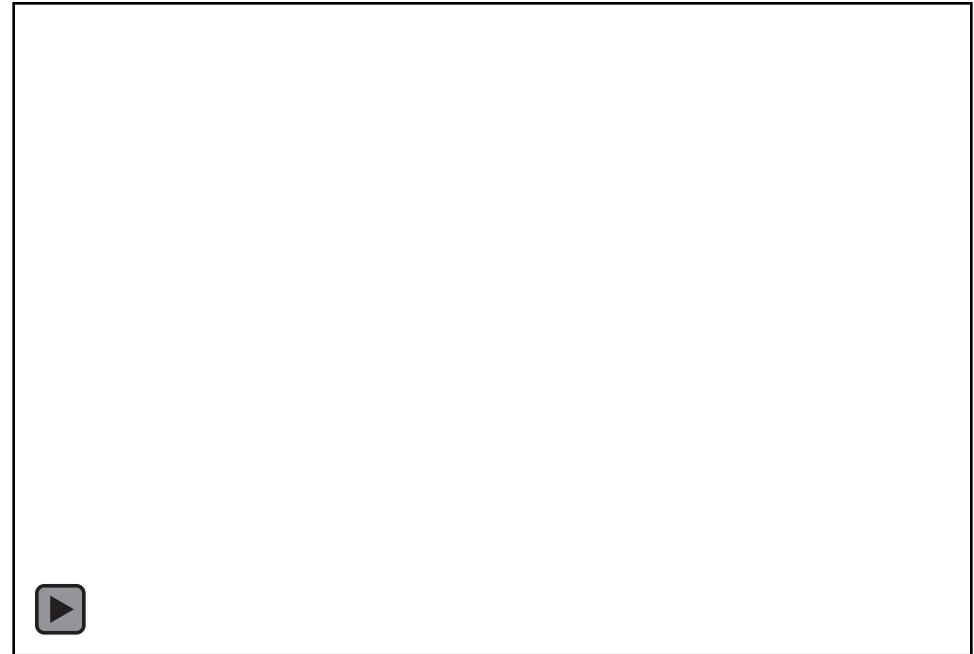
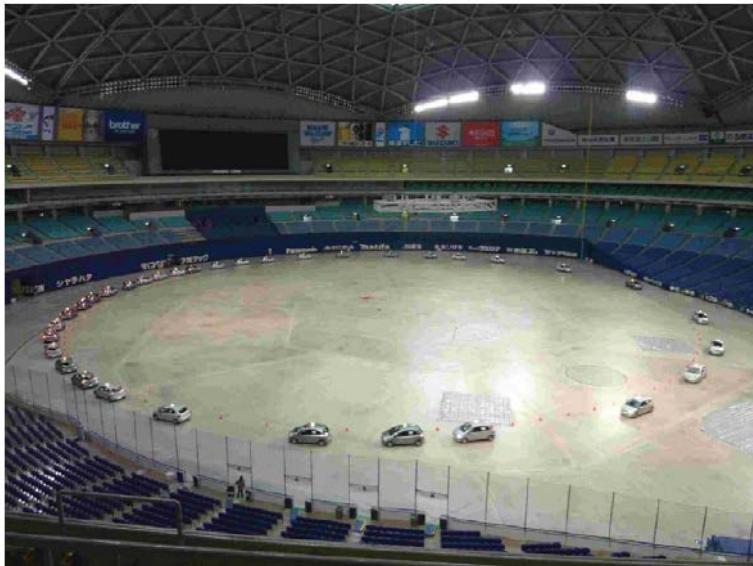


Andresen et al. 2013 1st SUMO user conference 2013, LNCS, to appear

Cars

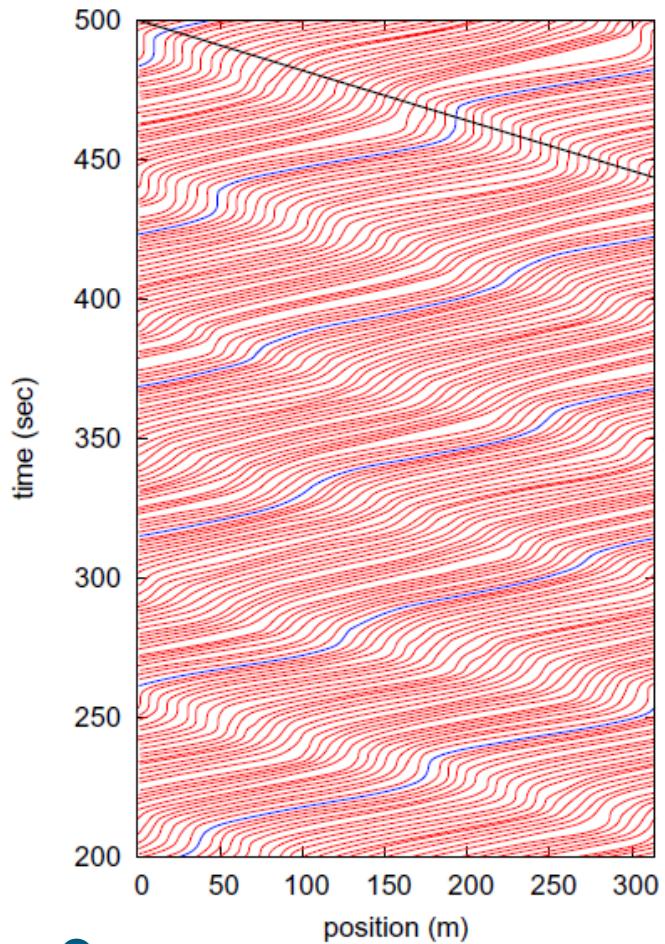
Setup details

- Circuit shape of length
 $L = 230 \text{ m}$ and 312 m
- 21 runs with numbers
 $N_{230} = 22, 23$
 $N_{312} = 10 - 40$ (19 runs)

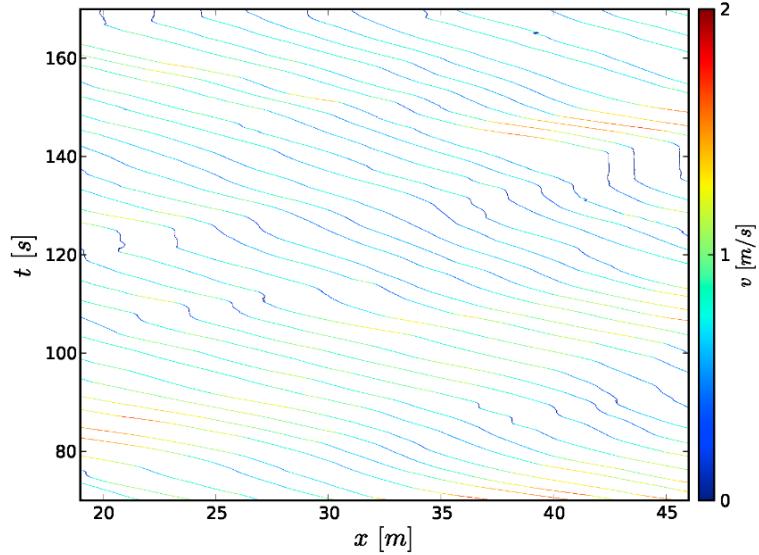


Sugiyama et al., 2008, *New Jour. Phys.* **10**, 1-7
Tadaki et al. 2013, *New Jour. Phys.* **15**, 103034

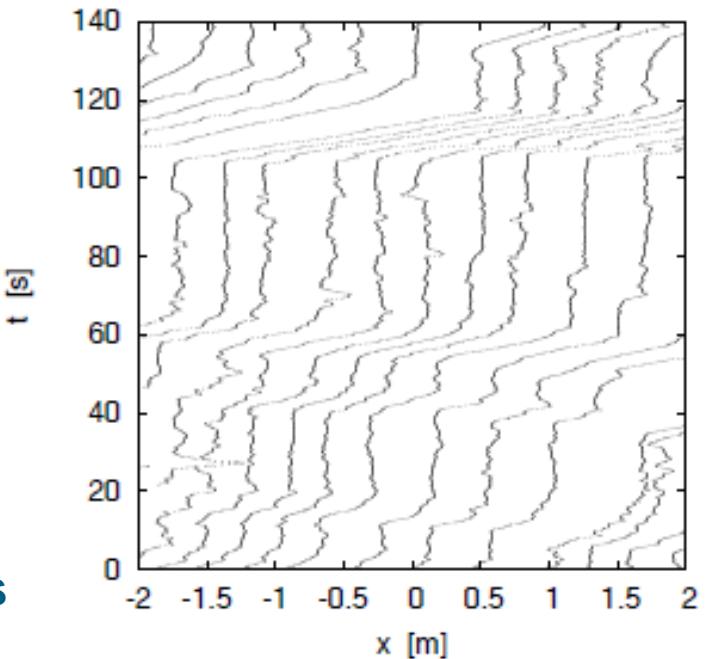
Instabilities (stop and go waves)



Cars

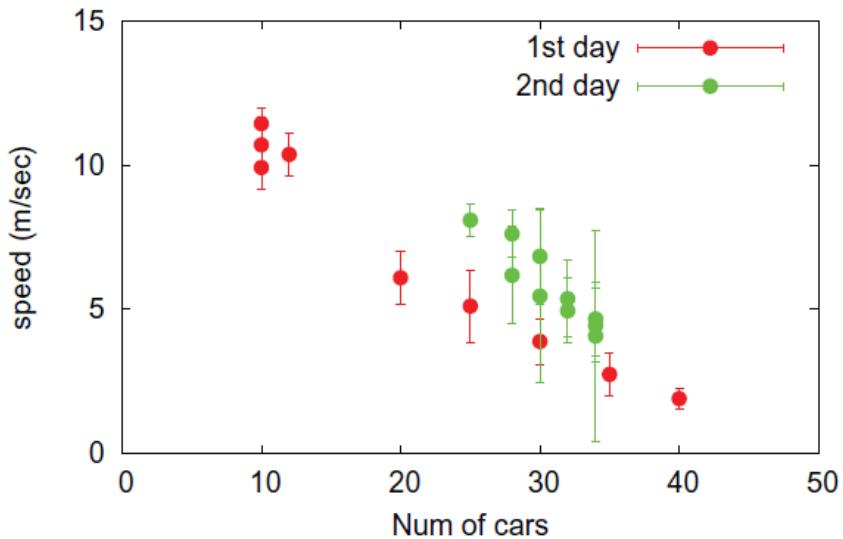


Bicycles

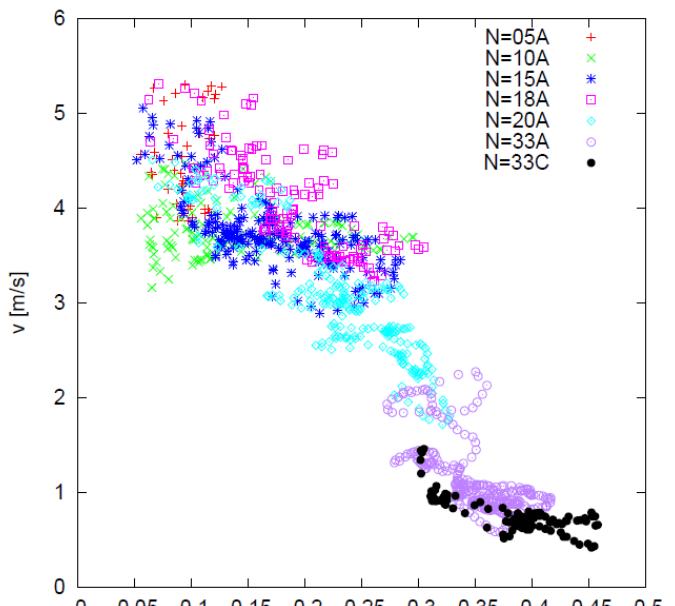


Pedestrians

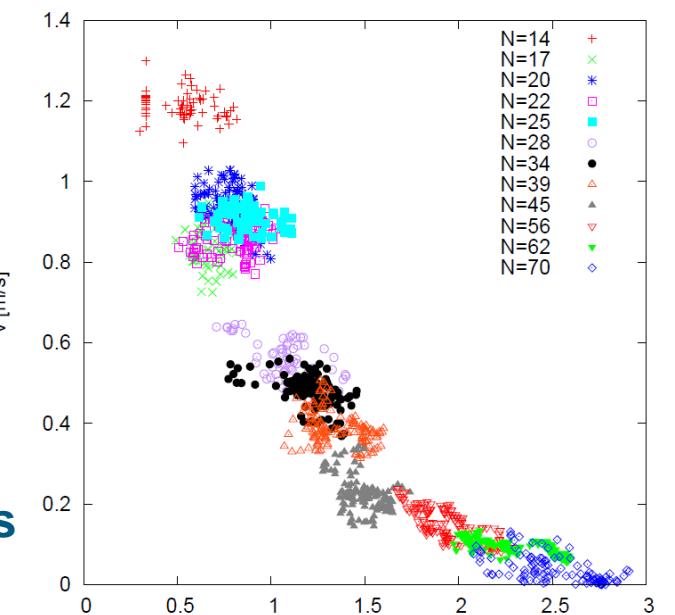
Speed-density relations



Cars



Bicycles



Pedestrians

Comparison and scaling

Scaling factors

Density $\rho \rightarrow \rho/\rho_0 = \rho L_0$

Ped: $L_0 = 0,40 \text{ m}$

Bicy: $L_0 = 1,73 \text{ m}$

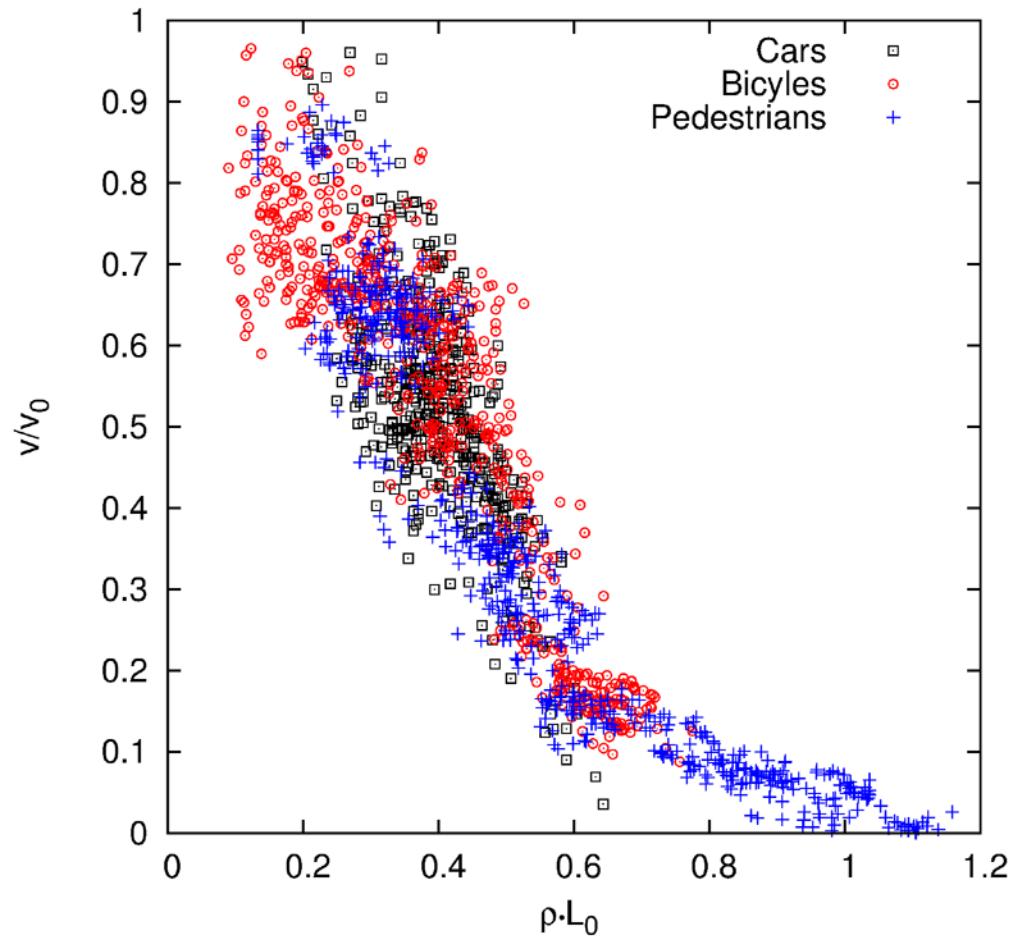
Cars: $L_0 = 3,90 \text{ m}$

Speed $v \rightarrow v/v_0$

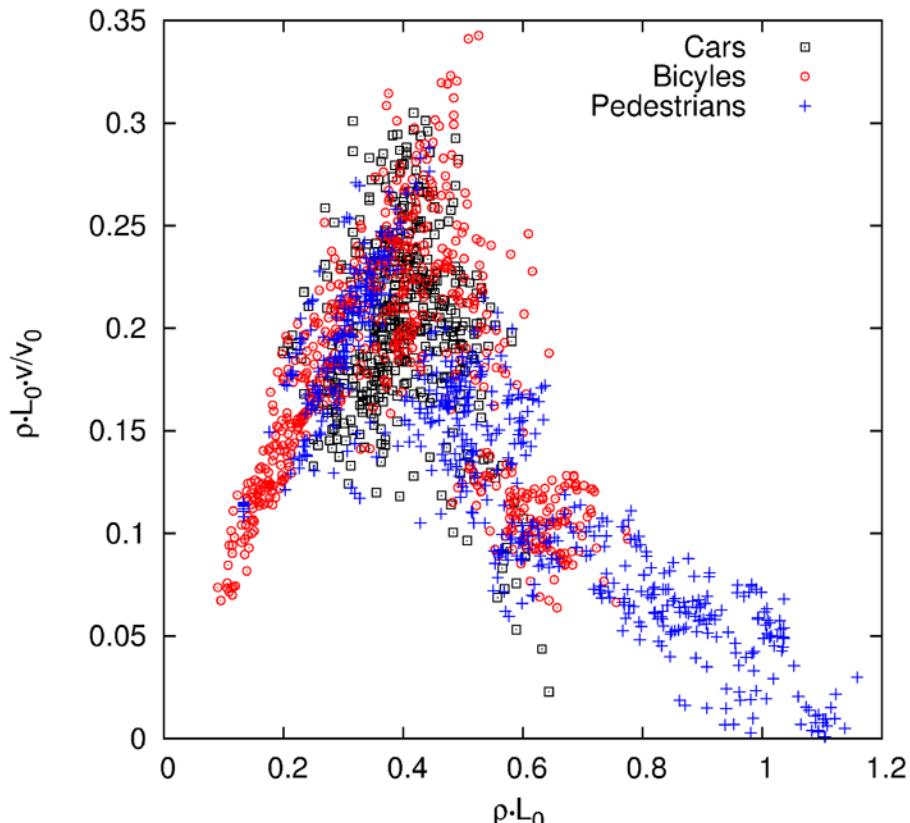
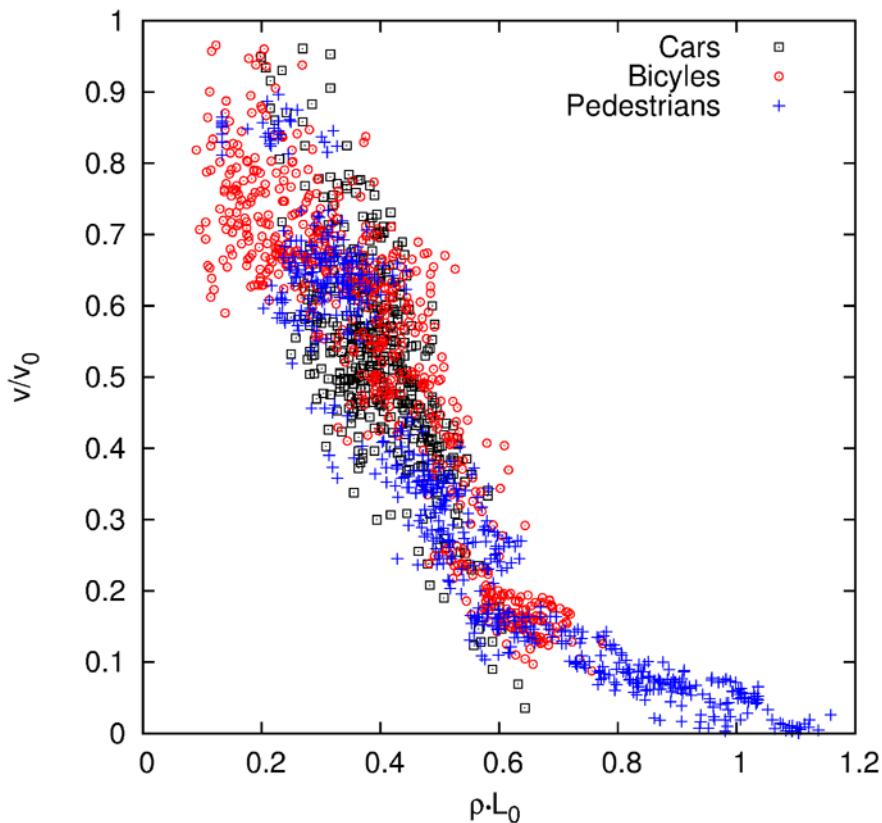
Ped: $v_0 = 1.4 \text{ m/s}$

Bicy: $v_0 = 5.5 \text{ m/s}$

Cars: $v_0 = 11.1 \text{ m/s}$



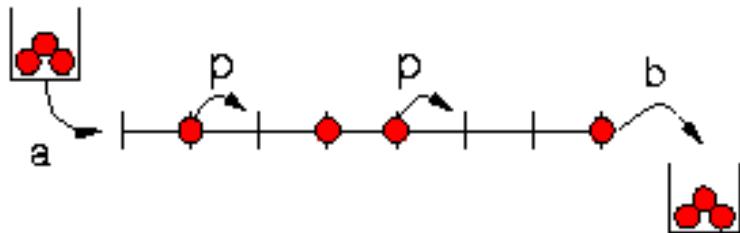
Comparison of scaled relations



Massage

Simplest model reproducing such a shape?

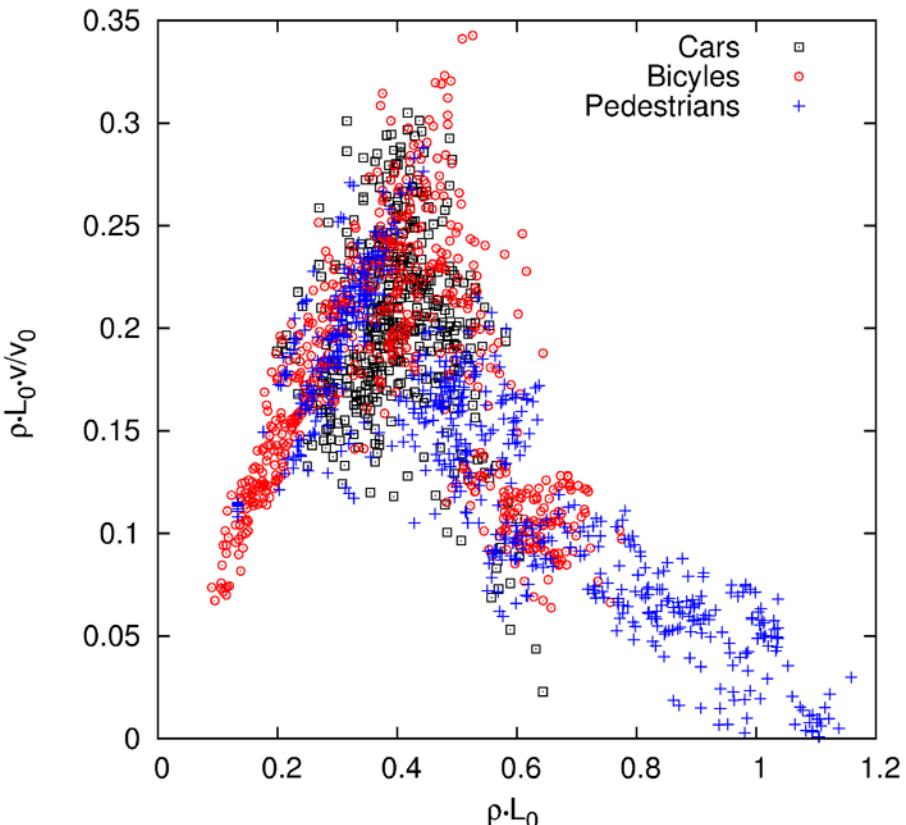
Asymmetric exclusion process



- Particles hopping with a probability p from cell to cell

Ingredients

- Particles prefer a direction
- **Volume exclusion** (Two particles in one cell are forbidden)



Summary

Experiments

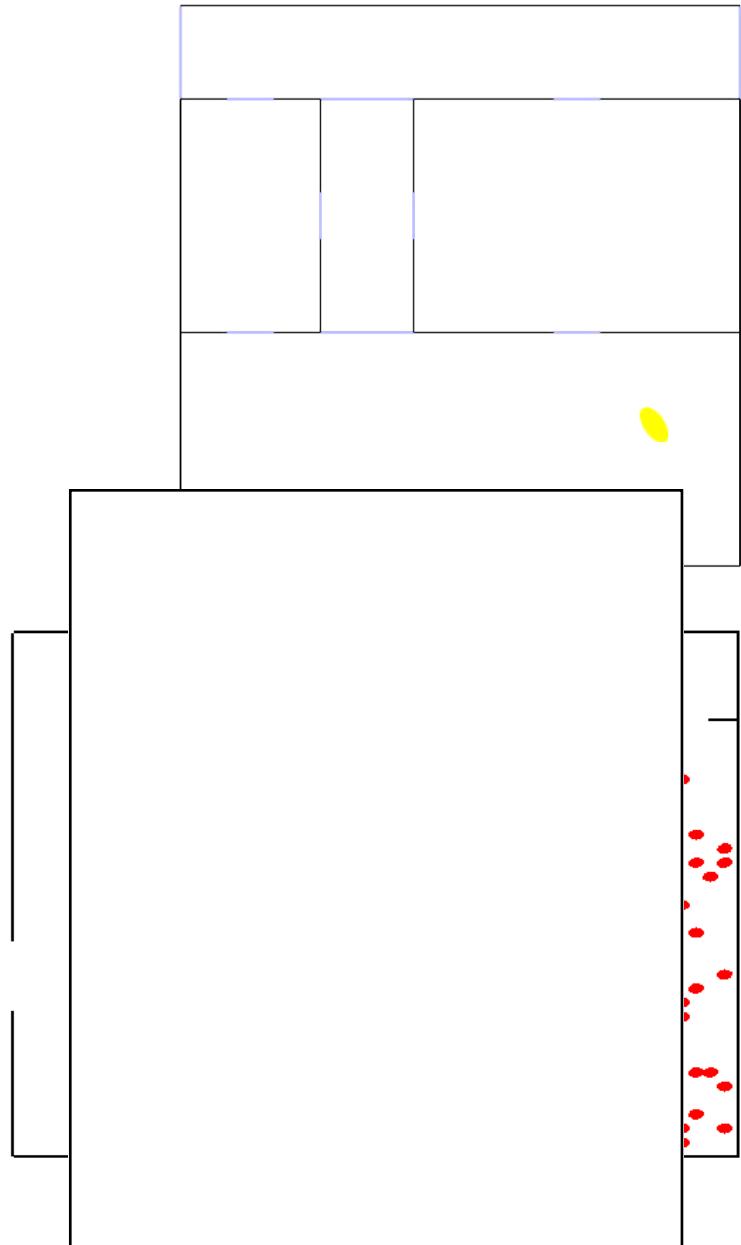
- Open source database including video recordings, trajectories, ...

<http://www.fz-juelich.de/ias/jsc/cst>

Modeling – Open source project



- JPScore: computing trajectories
- JPSvis: visualizing trajectories.
- JPSreport: analyzing trajectories and validating the model
- JPSed: editing geometry and model parameters



Thank you

Density measurement with Voronoi-diagrams

Steffen, B. und Seyfried, A.

Methods for measuring pedestrian density, flow, speed and direction with minimal scatter
Physica A, 2010, 389, 1902-1910

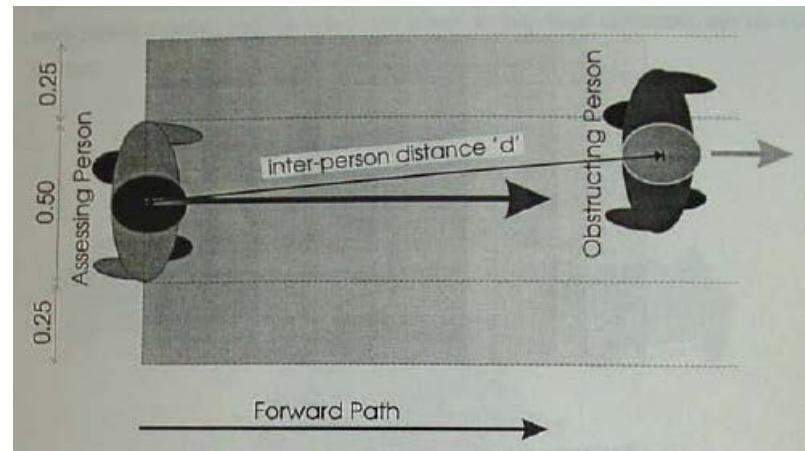
Definitions for the density

Different definitions

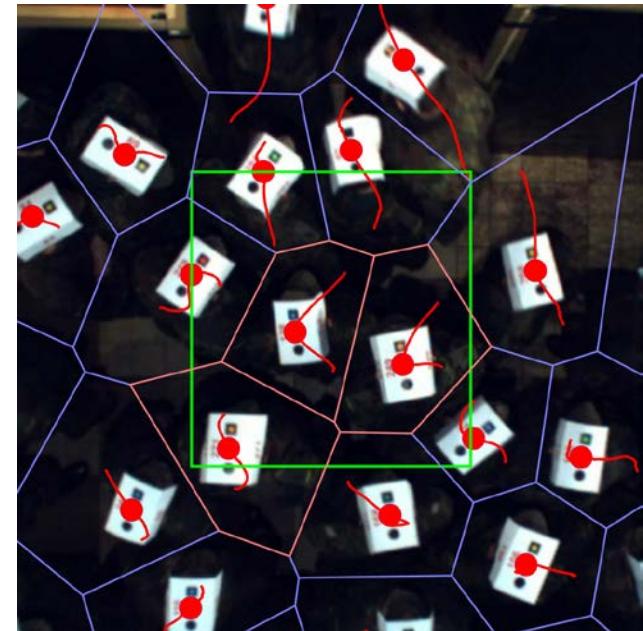
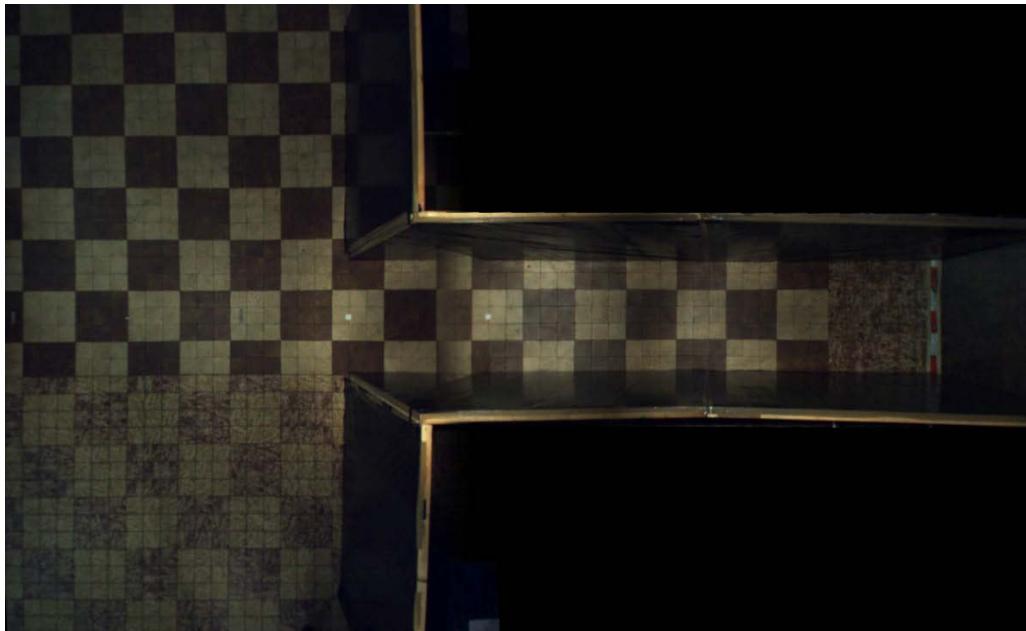
- Classical
- Pedestrian area module M (Fruin)
 - computed by the classical density
- Interperson distance (Thompson)
 - not unique
 - ...

$$\rho_{\text{class}} = \frac{N}{|A|}$$

$$M = \frac{1}{\rho_{\text{class}}}$$



Problems of the classical density definition

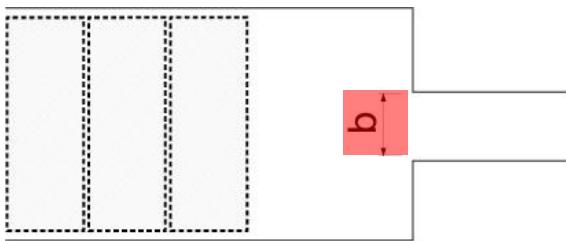


Problems

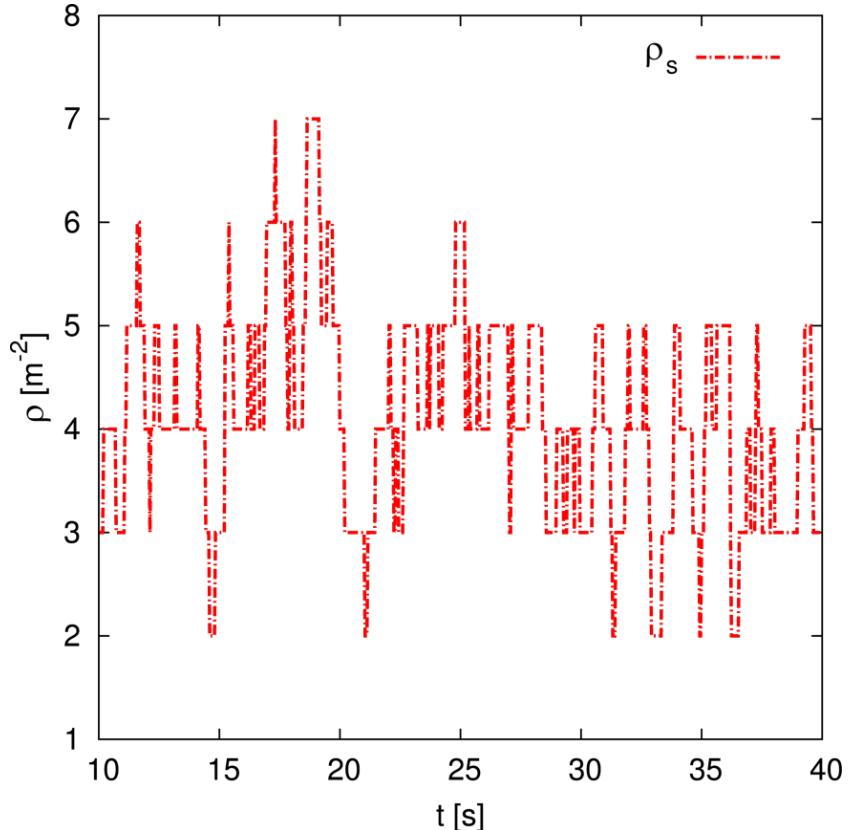
- Size of facilities normally restricted to 1 -10 m
- Number of pedestrians in the measurement area is small
- Mean value and fluctuations have same order of magnitude
- Proportion between of particle number and measurement area problematic

Problems of the classical density definition

Local density in front of the bottleneck

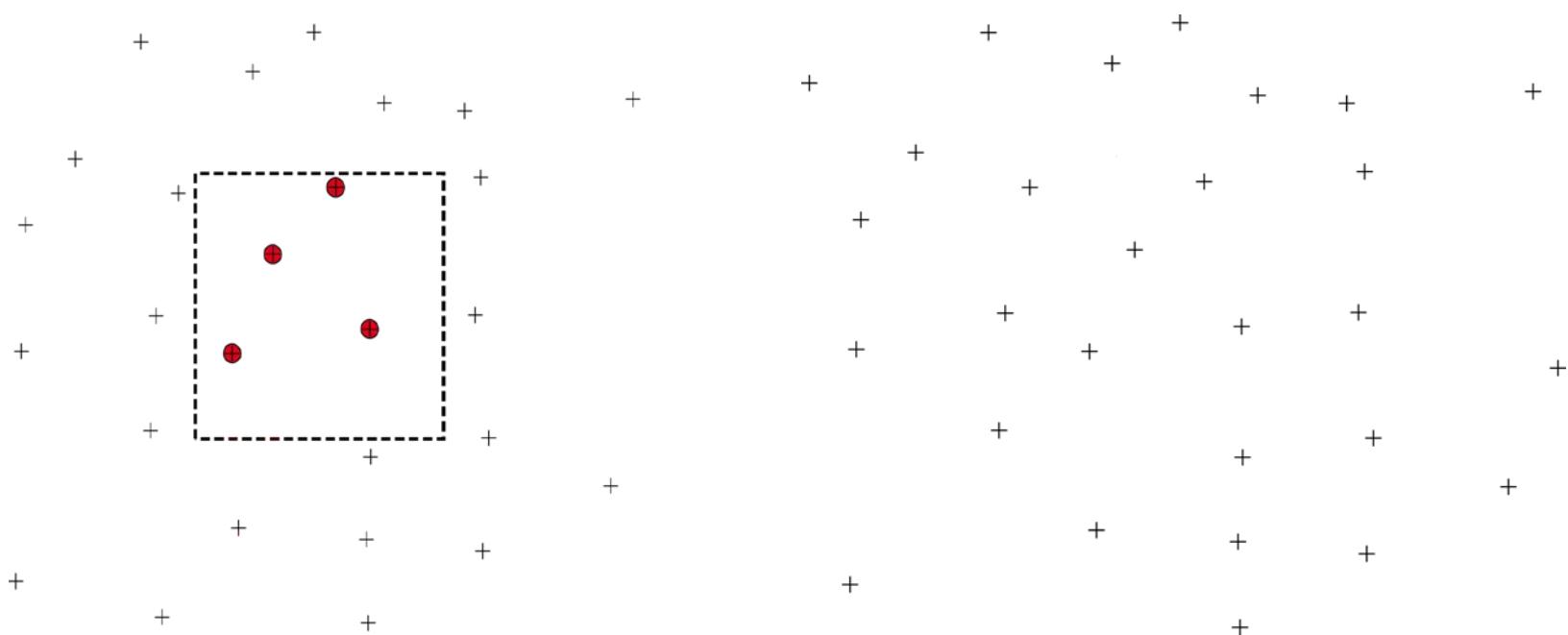


- Large fluctuations
 - Stationary state?
 - Mean value?
- $\rho_{\min} = 2 \text{ m}^{-2}$ to $\rho_{\max} = 7 \text{ m}^{-2}$



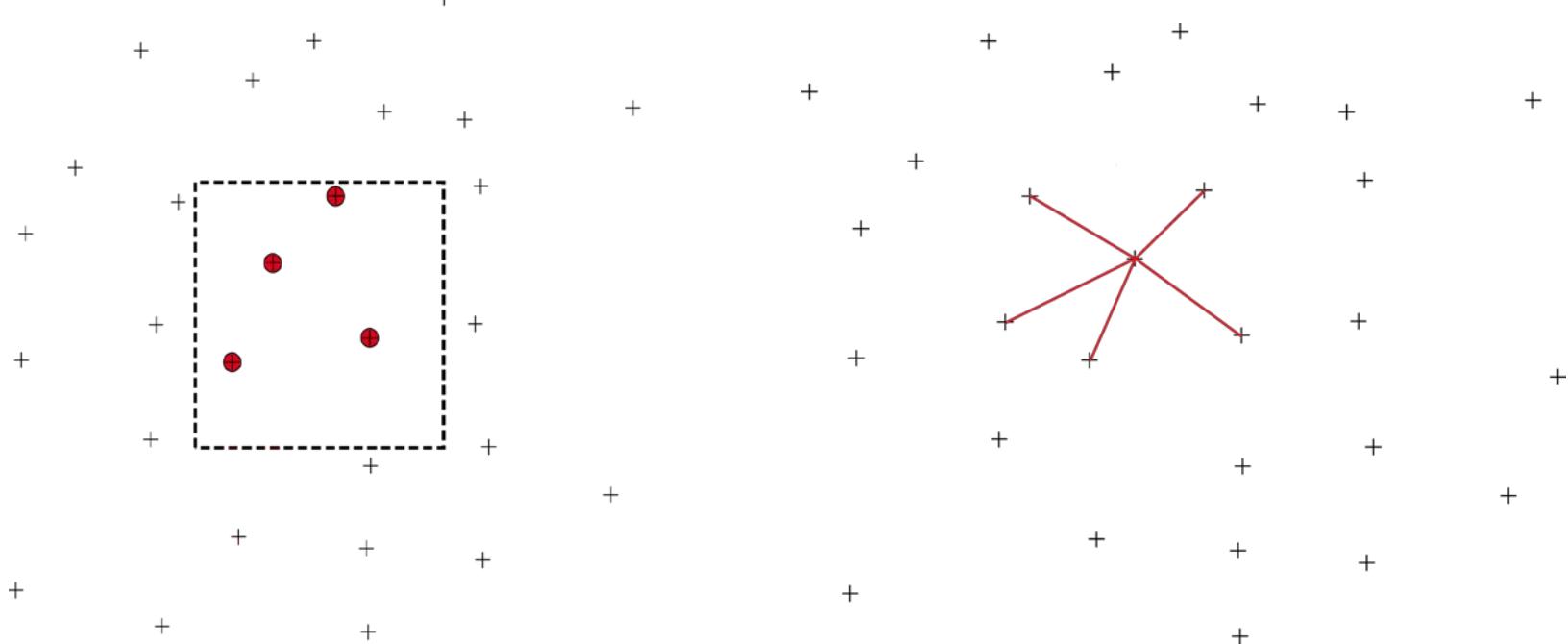
Voronoi - Density

$$\rho_{\text{class}} = \frac{N}{|A|}$$



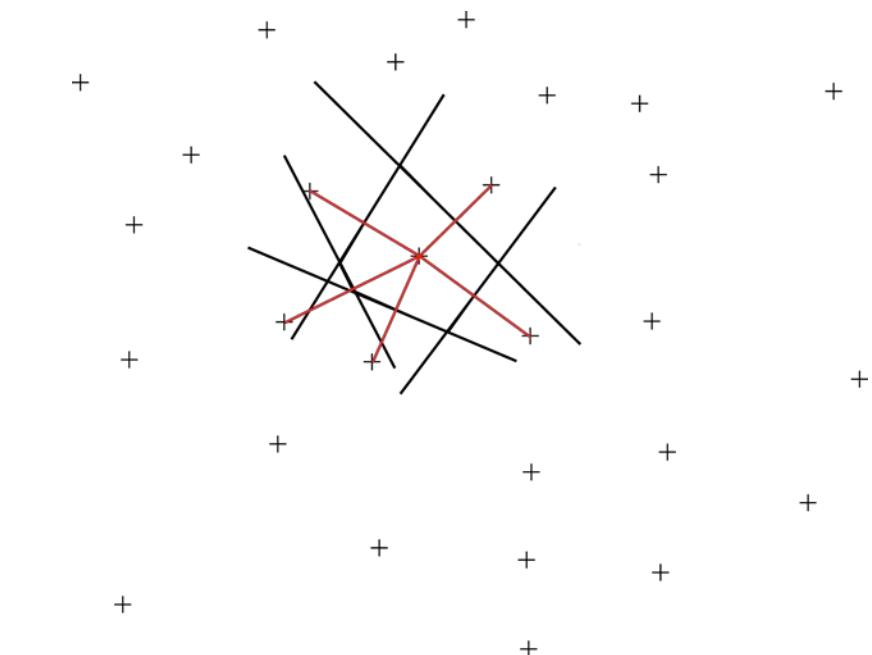
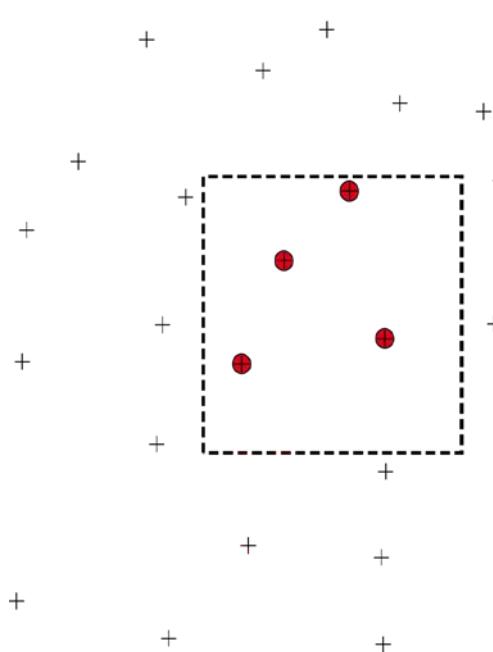
Voronoi - Density

$$\rho_{\text{class}} = \frac{N}{|A|}$$



Voronoi - Density

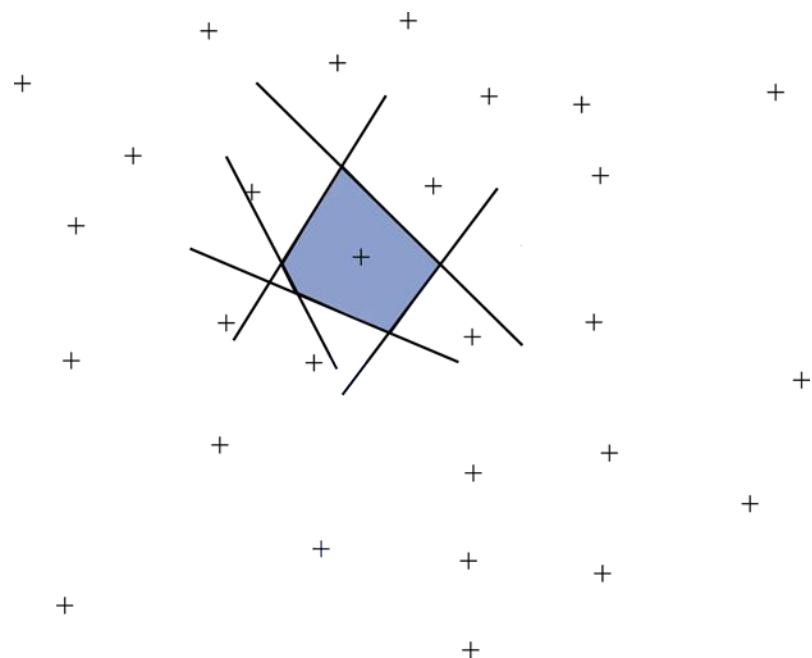
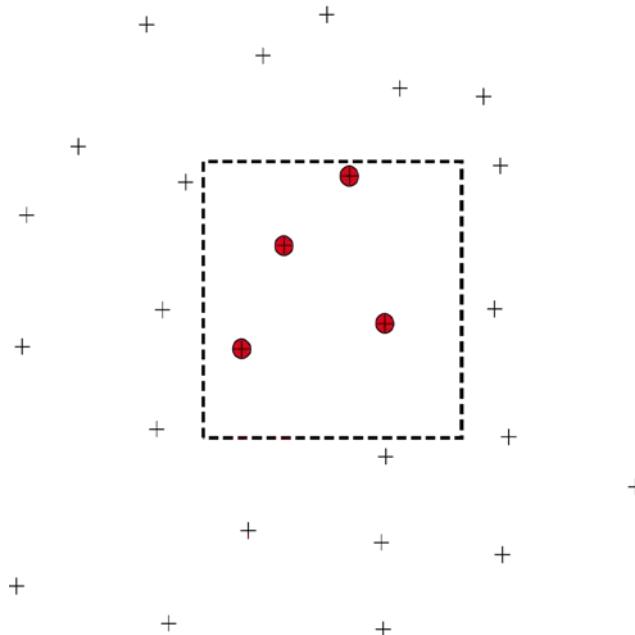
$$\rho_{\text{class}} = \frac{N}{|A|}$$



Voronoi - Density

$$\rho_{\text{class}} = \frac{N}{|A|}$$

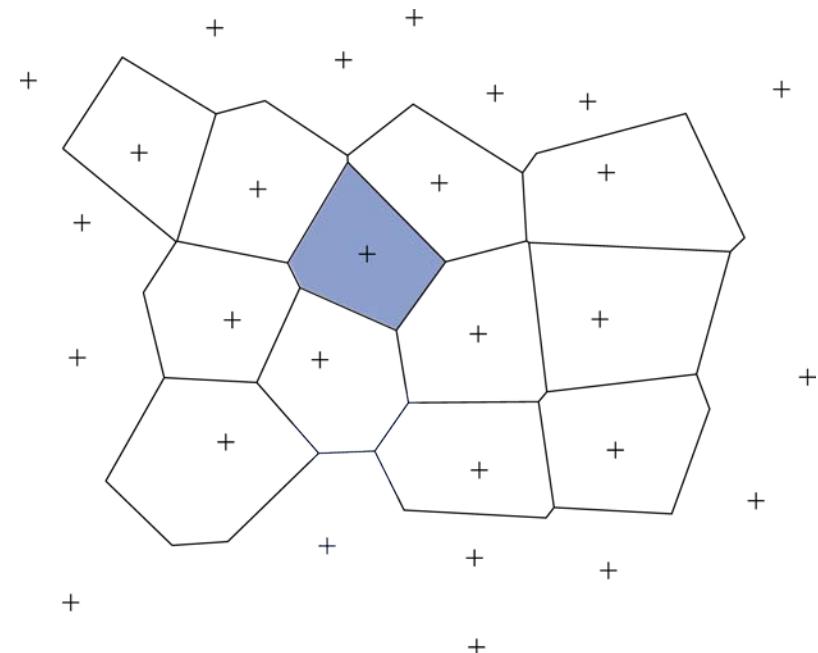
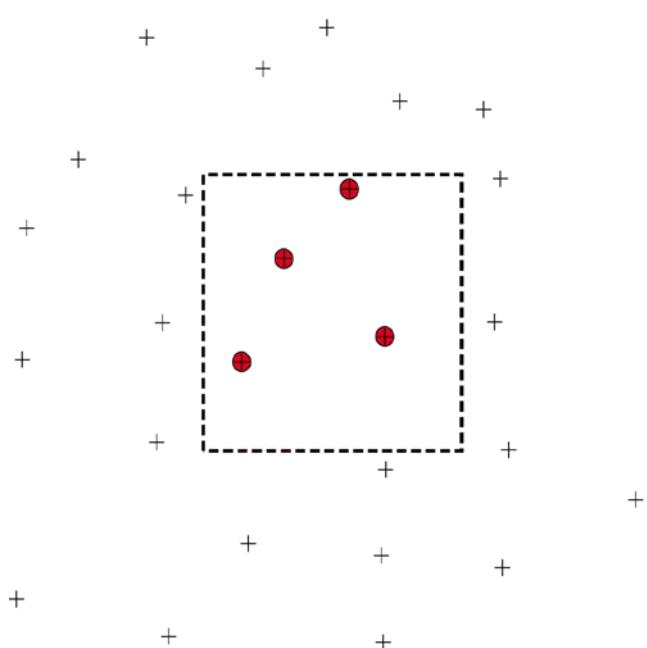
Voronoi - Cell: A_i



Voronoi - Density

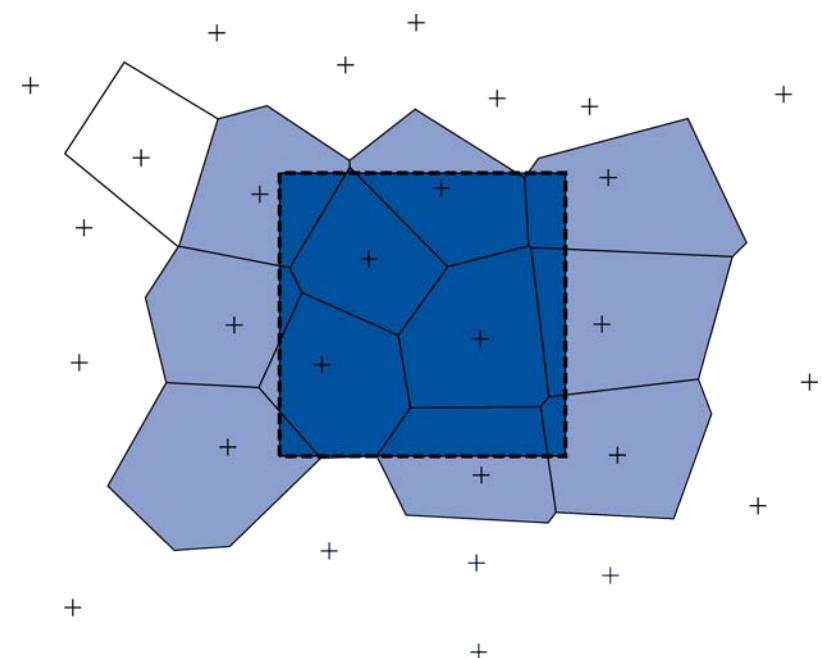
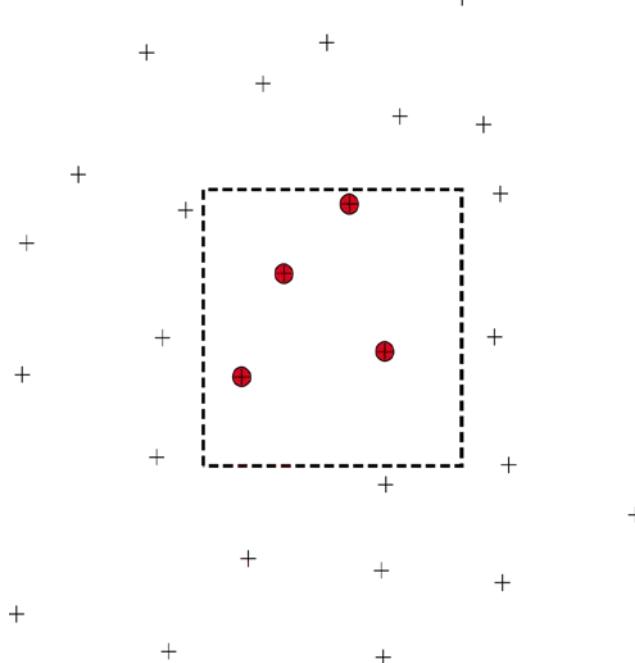
$$\rho_{\text{class}} = \frac{N}{|A|}$$

$$p(\vec{x}) = \begin{cases} \frac{1}{|A_i|} & : \vec{x} \in A_i \\ 0 & : \text{else} \end{cases}$$



Voronoi - Density

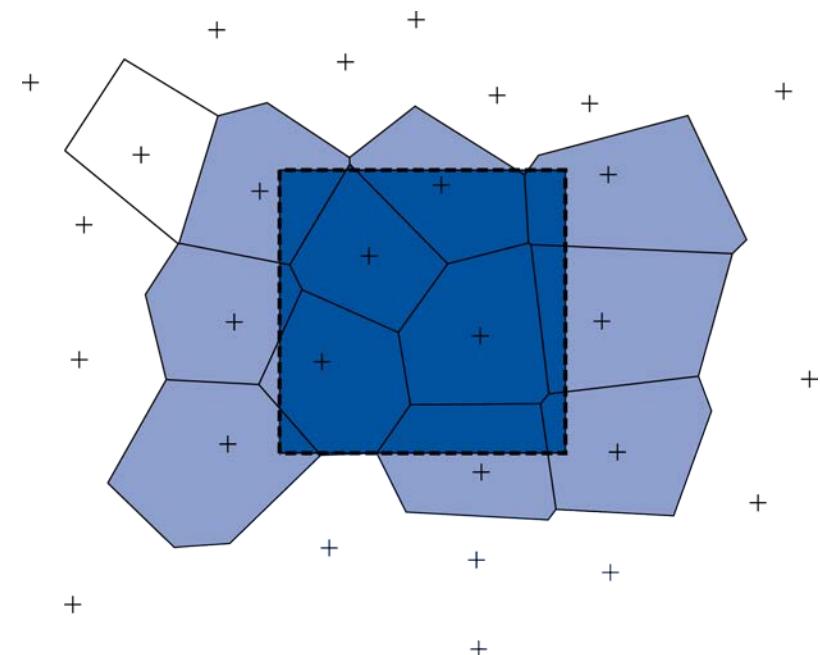
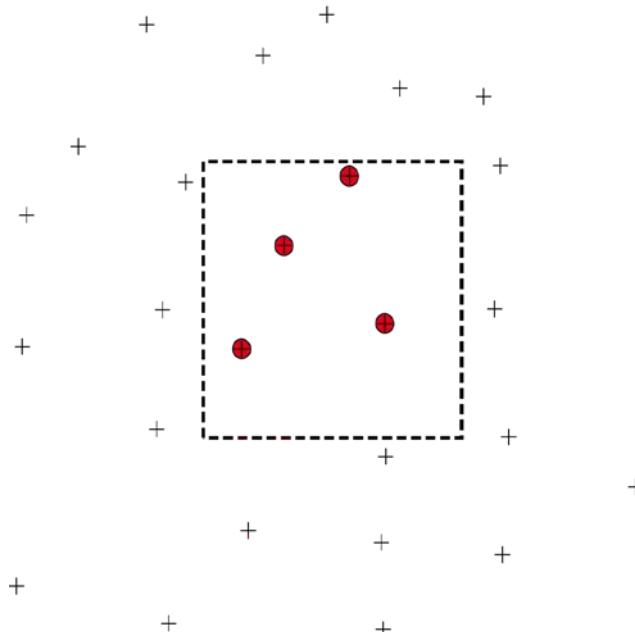
$$\rho_{\text{Voronoi}} = \frac{\int_A p(\vec{x}) d\vec{x}}{|A|} \quad \text{mit} \quad p(\vec{x}) = \begin{cases} \frac{1}{A_i} & : \vec{x} \in A_i \\ 0 & : \text{else} \end{cases}$$



Voronoi - Density

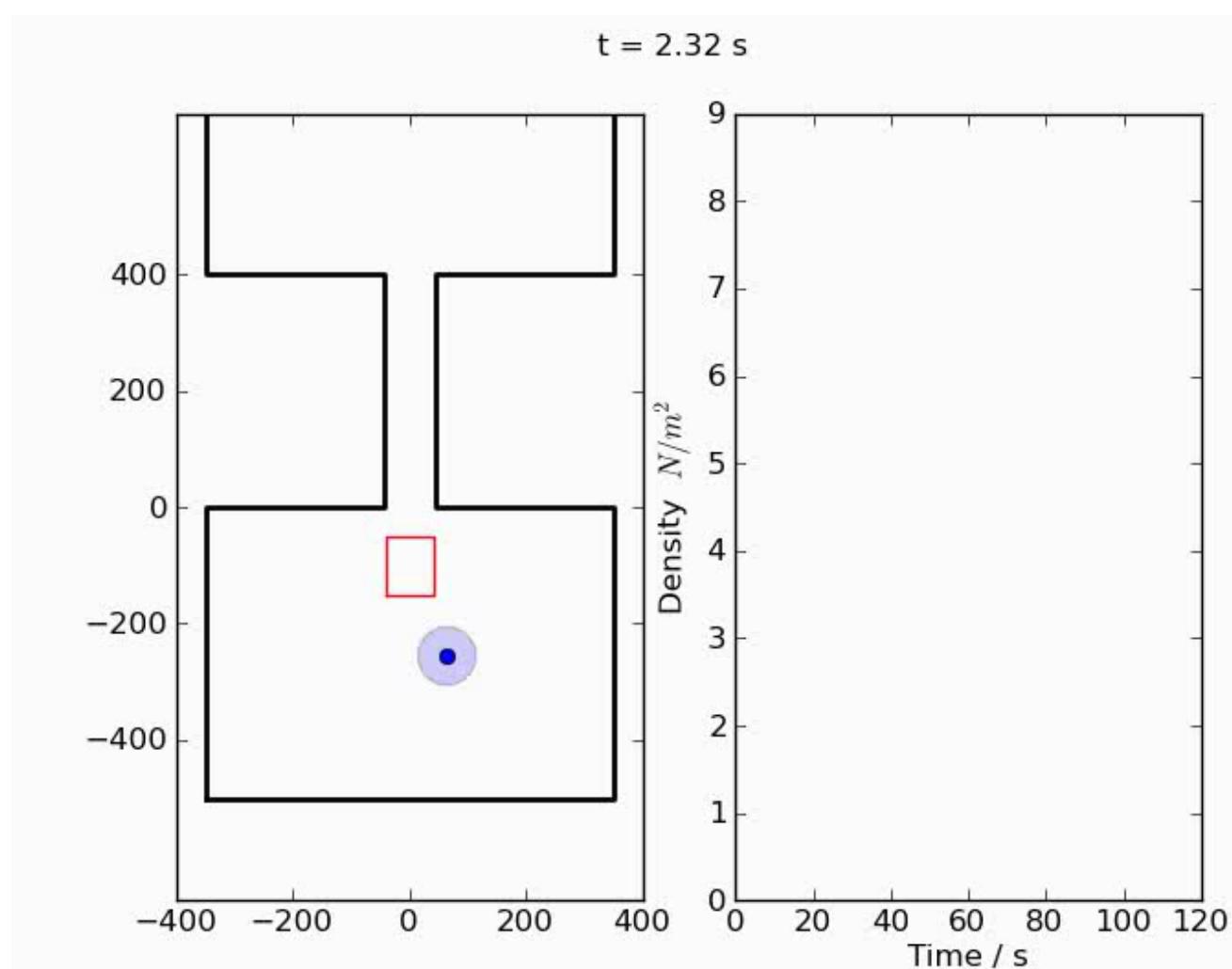
$$\rho_{\text{Class}} = \frac{N}{|A|}$$

$$\rho_{\text{Voronoi}} = \frac{\int_A p(\vec{x}) d\vec{x}}{|A|}, \quad p(\vec{x}) = \begin{cases} 1/A_i & : \vec{x} \in A_i \\ 0 & : \text{else} \end{cases}$$



¹B. Steffen and A. Seyfried, *Physica A*, **2010**, 389, 1902-1910

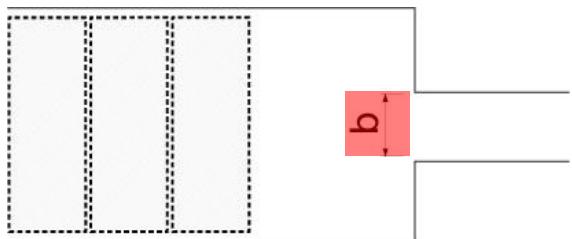
Voronoi - Density



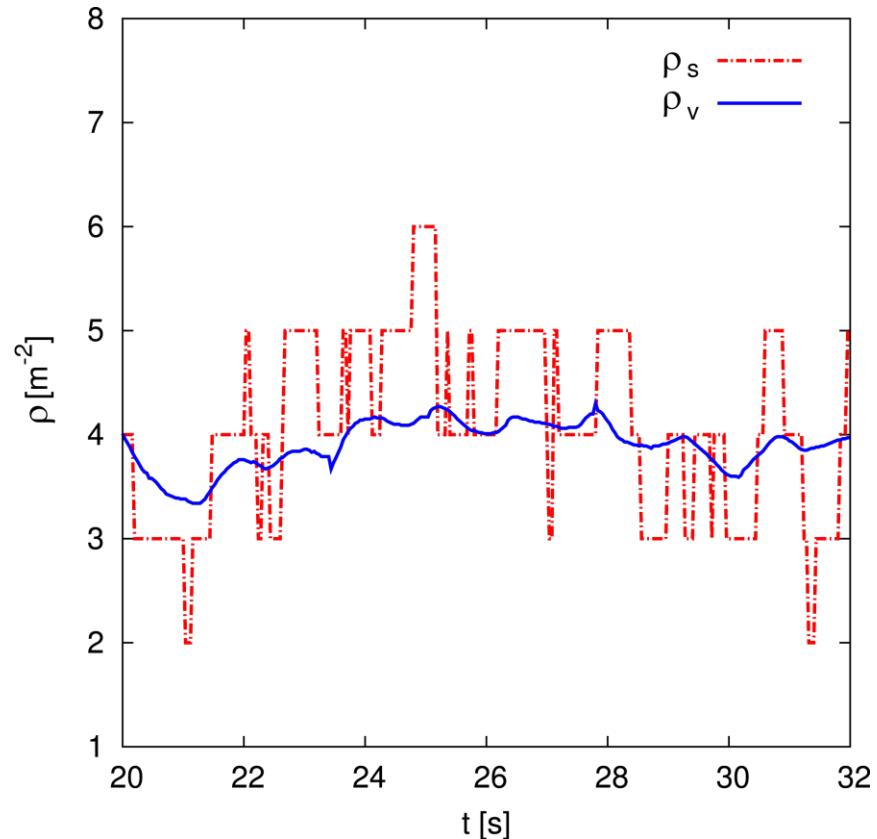
Credits: J. Liddle

Voronoi - Density

Comparison

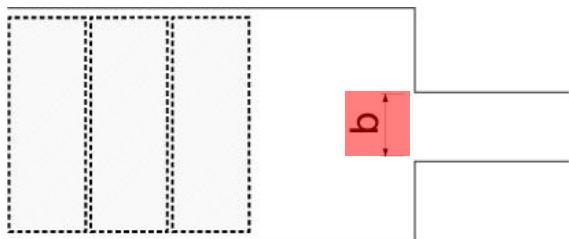


Typ	Mean [1/m ²]	Std. dev. [1/m ²]
ρ_{Class}	4.06	0.88
ρ_{Voronoi}	3.90	0.23

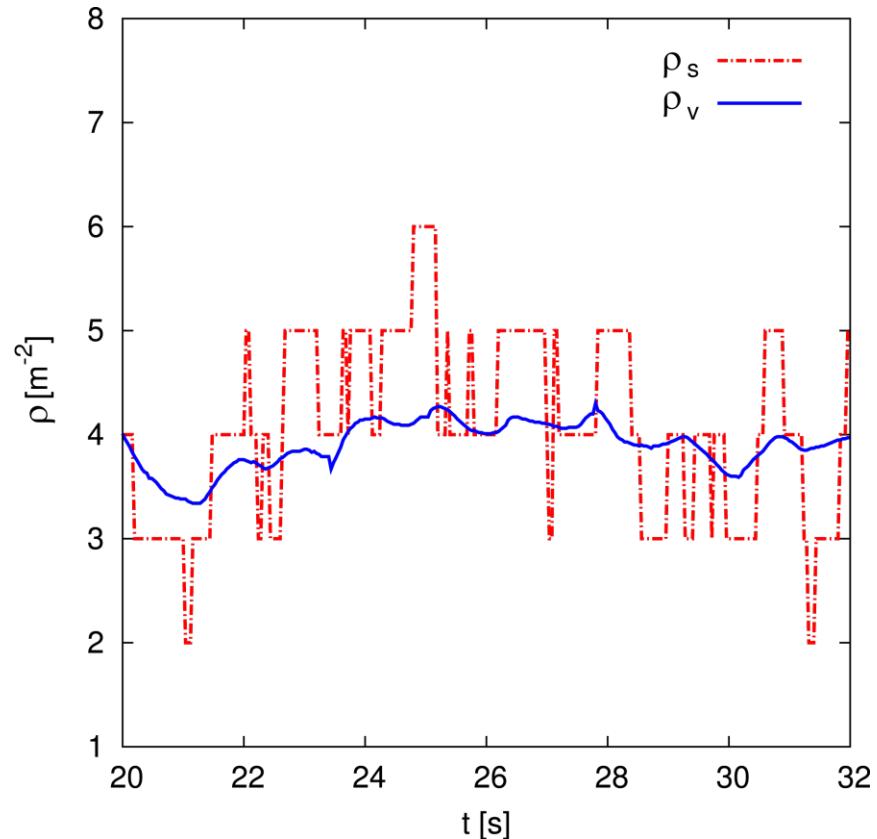


Voronoi - Dichte

Vergleich

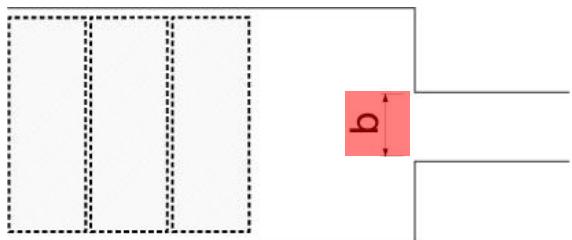


Typ	Mean [1/m ²]	Std. dev. [1/m ²]
ρ_{Class}	4.06	0.88
$\langle \rho \rangle_{\text{Space}}$	4.33	0.40
$\langle \rho \rangle_{\text{Time}}$	4.07	0.62
ρ_{Voronoi}	3.90	0.23

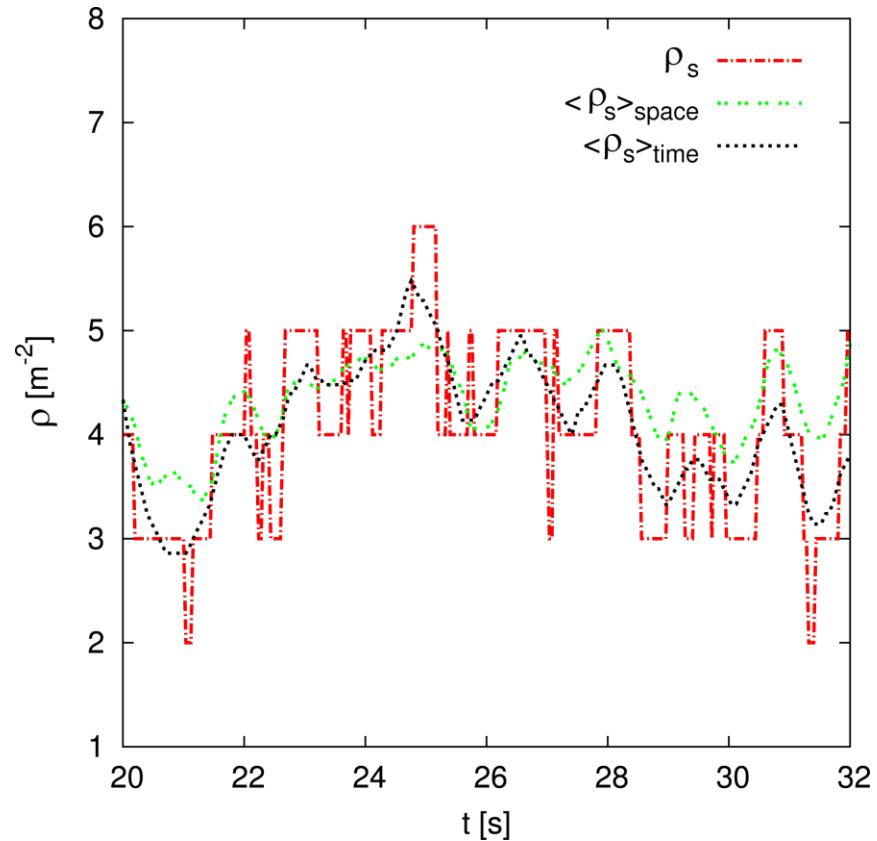


Voronoi - Dichte

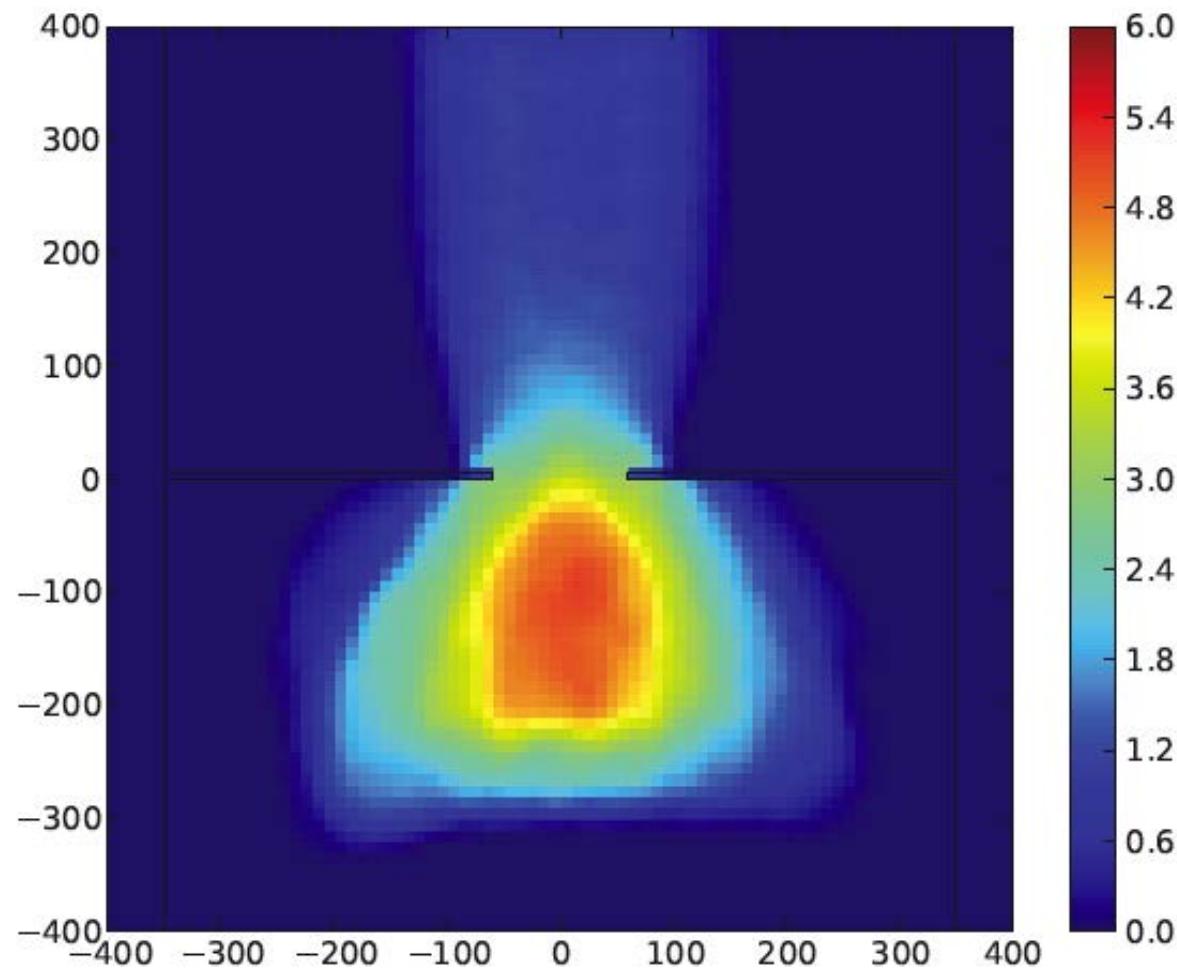
Vergleich



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Voronoi - Density



J. Liddle, et al., *arXiv:1105.1532*

Fundamental diagram for single file movement

-Microscopic measurement and phase separation -

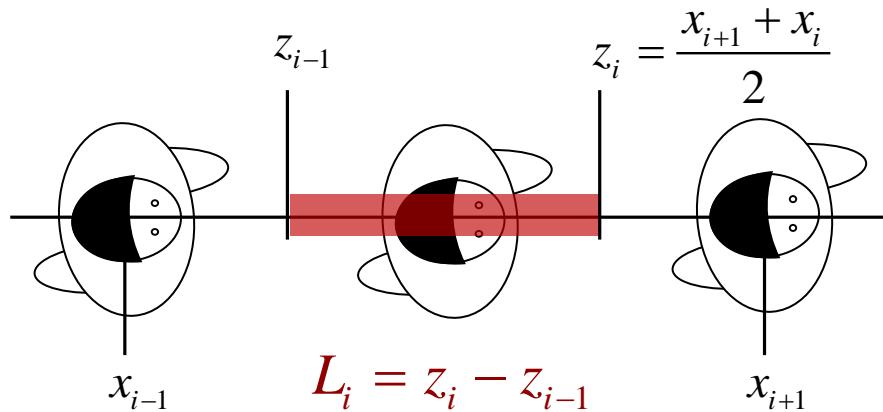
Seyfried, A.; Portz, A. & Schadschneider, A.

Phase Coexistence in Congested States of Pedestrian Dynamics

Cellular Automata, Springer, **2010**, 6350, 496-505

'Microscopic' Measurement

Density measurement with
Voronoi diagrams¹.

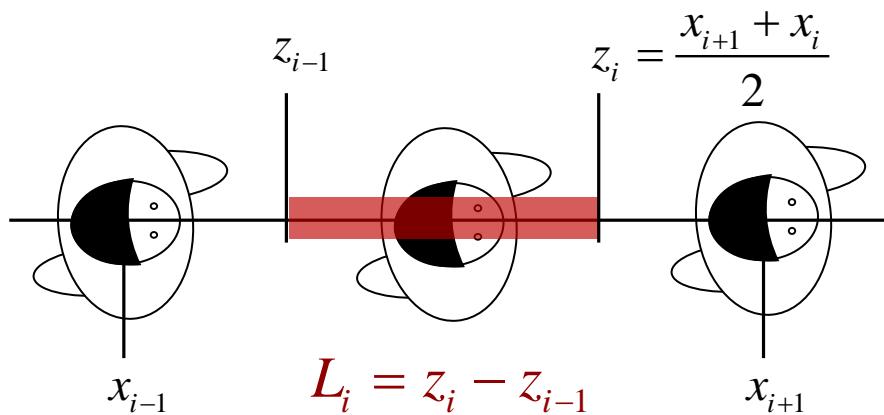


$$\rho_i(x) = \begin{cases} \frac{1}{L_i}, & x \in [z_{i-1}, z_i[\\ 0, & \text{otherwise} \end{cases}.$$

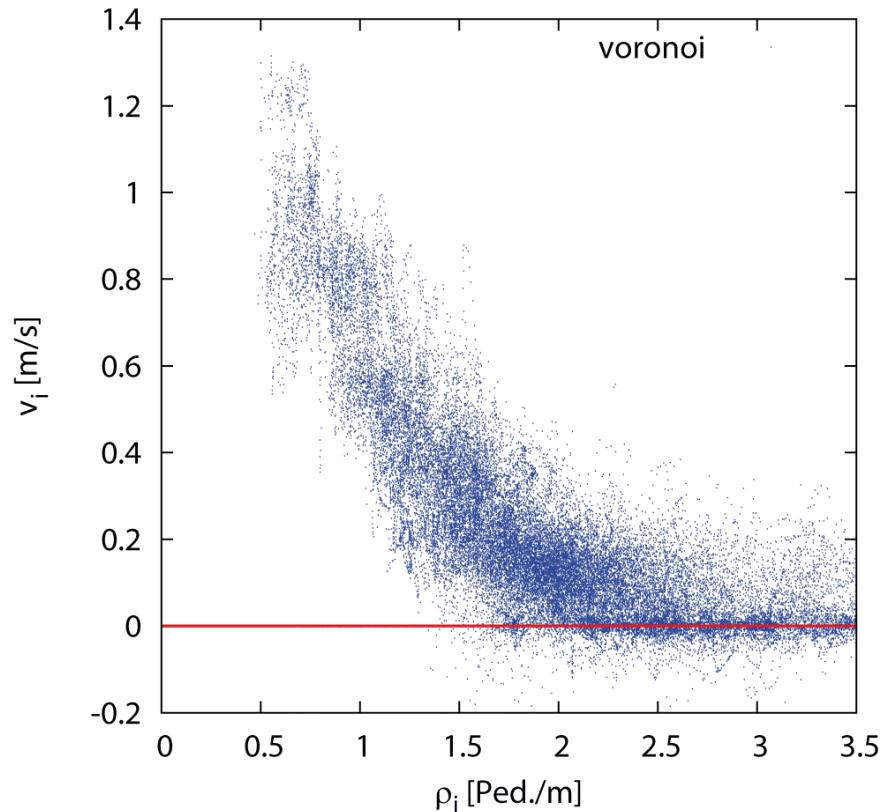
¹B. Steffen and A. Seyfried, *Physica A*, **2010**, 389, 1902-1910

'Microscopic' Measurement

Density measurement with Voronoi diagrams¹.

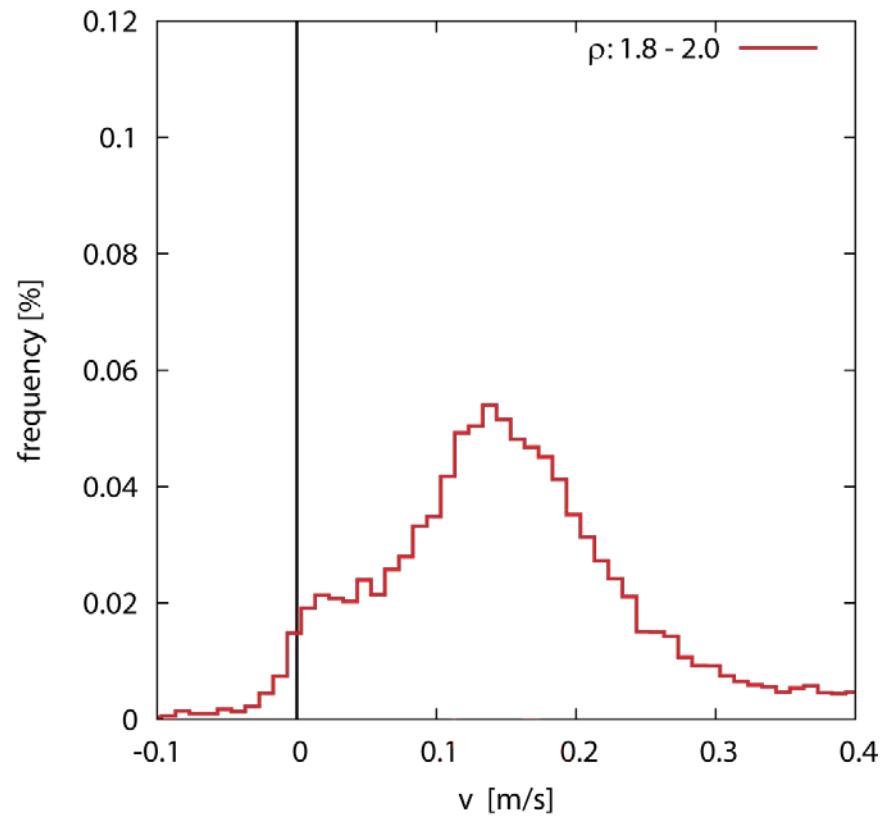
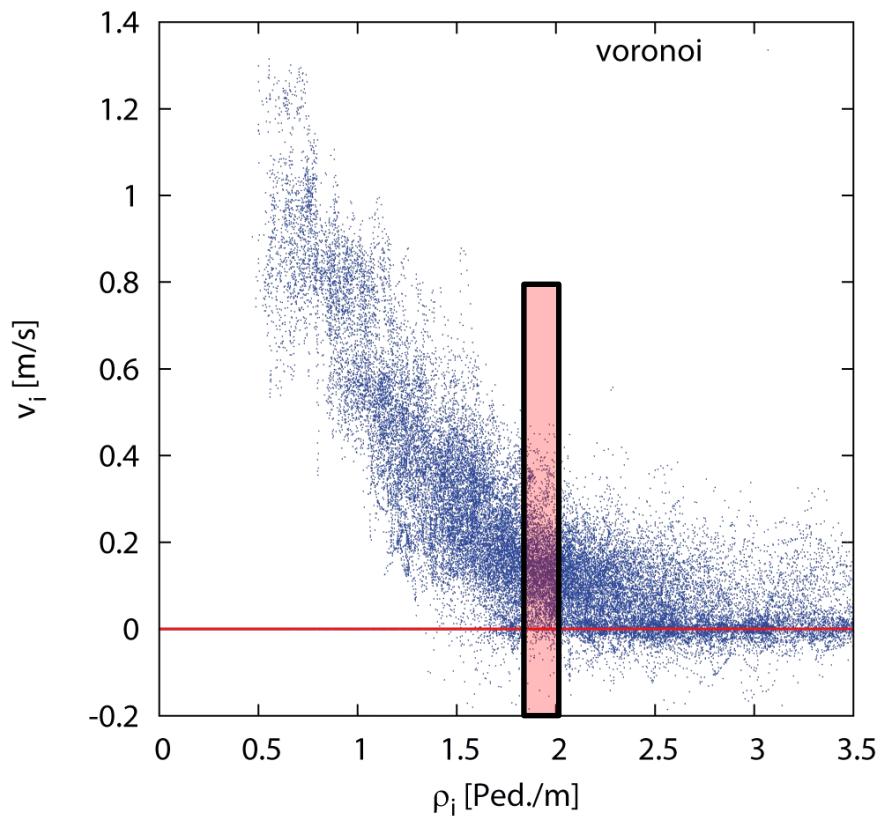


$$\rho_i(x) = \begin{cases} \frac{1}{L_i}, & x \in [z_{i-1}, z_i[\\ 0, & \text{otherwise} \end{cases}.$$

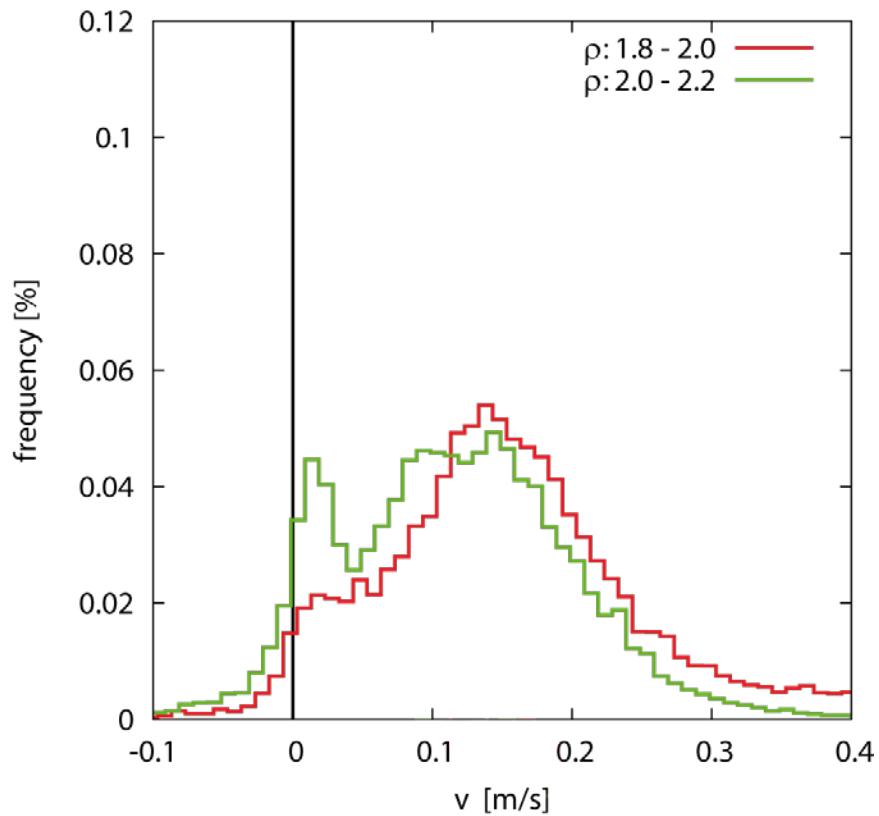
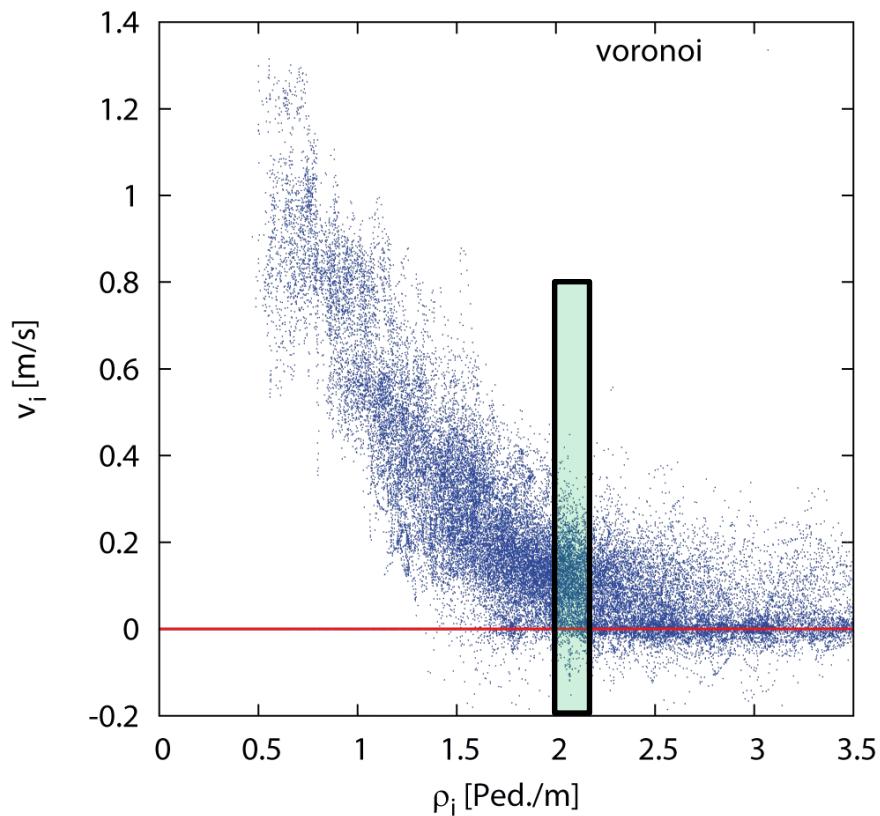


¹B. Steffen and A. Seyfried, *Physica A*, **2010**, 389, 1902-1910

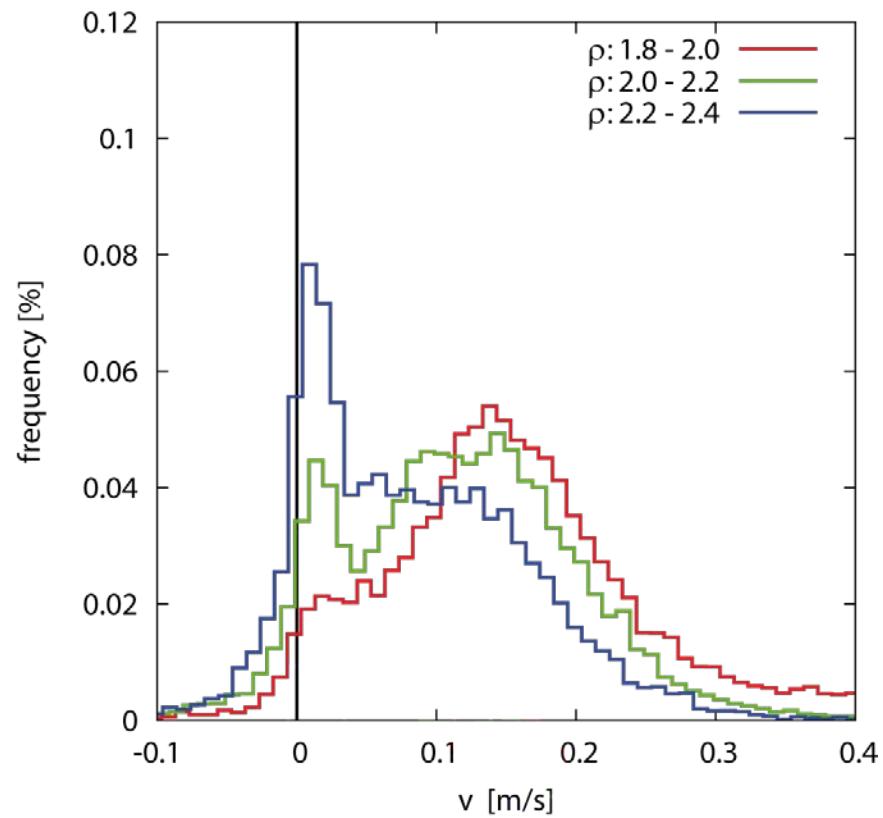
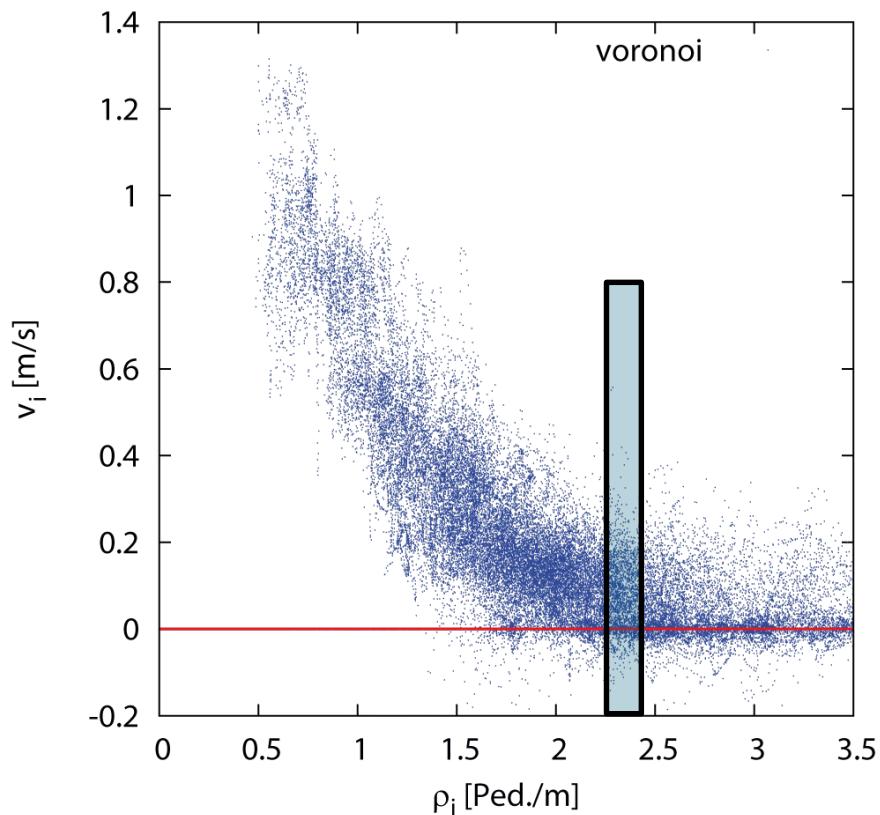
Velocity distribution



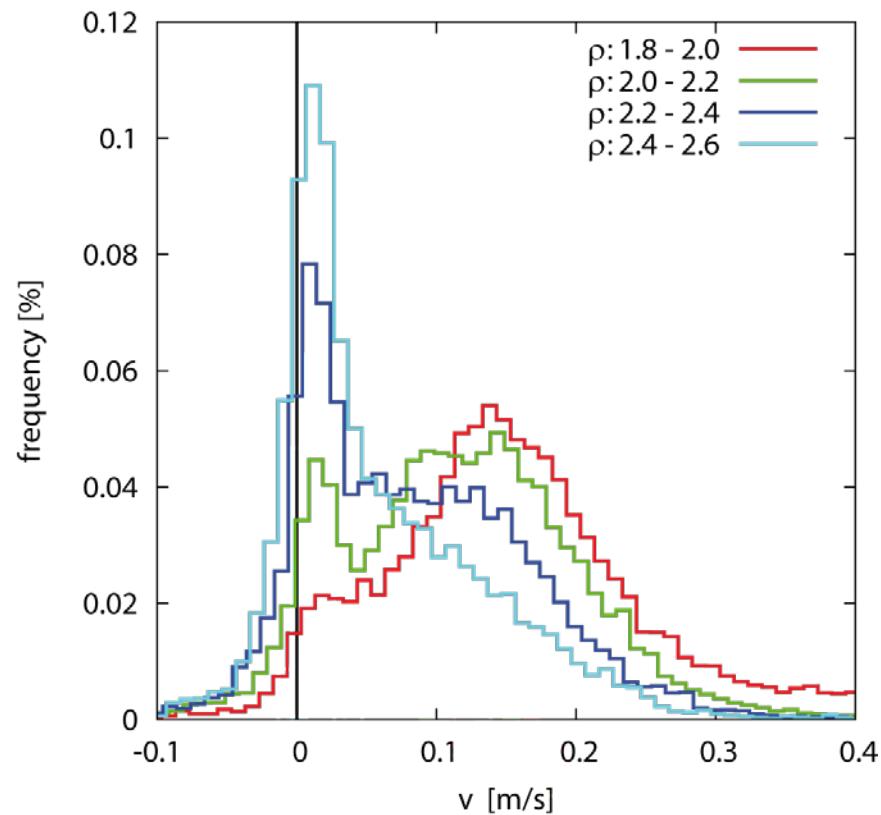
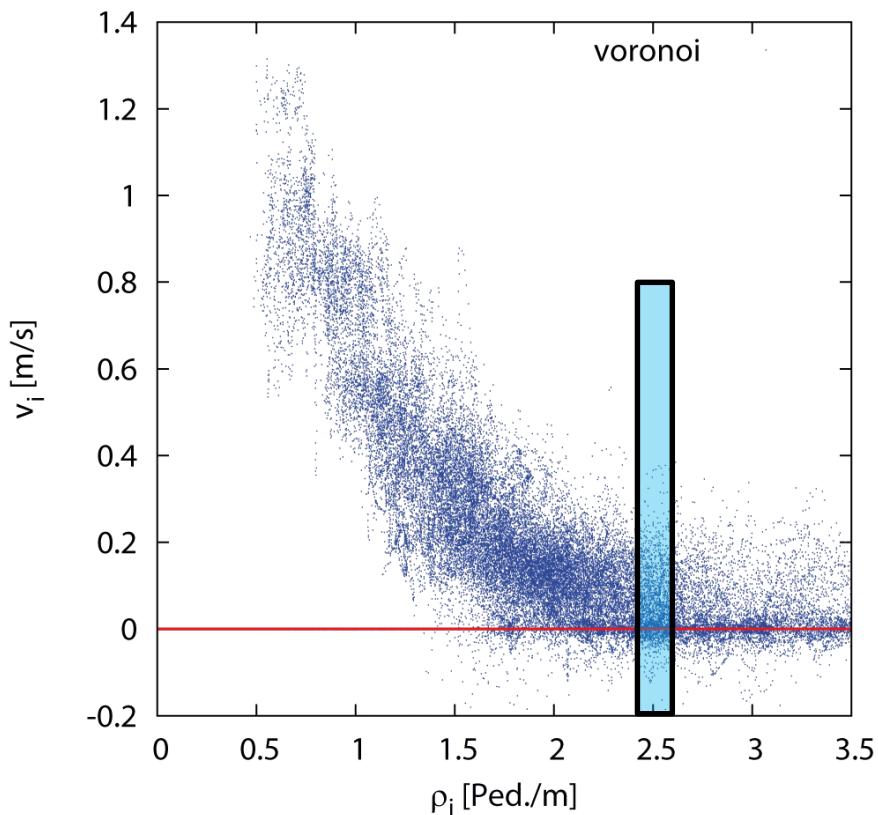
Velocity distribution



Velocity distribution



Velocity distribution



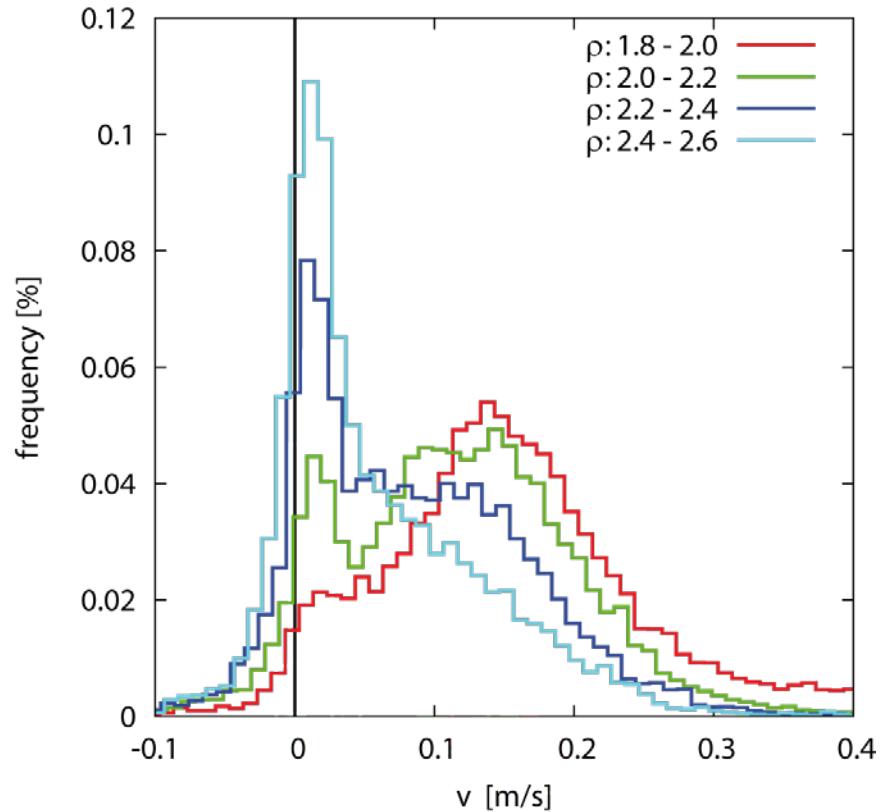
Velocity distribution

Coexistence of two states
at one density

Continuous transition from
Go to Stop - phase

First peak at $v = 0$ m/s

Second peak at $v = 0.15$ m/s



Thank you