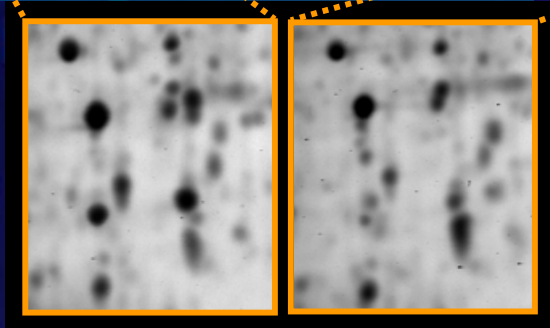
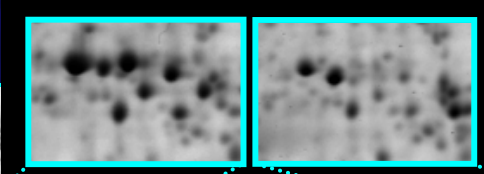
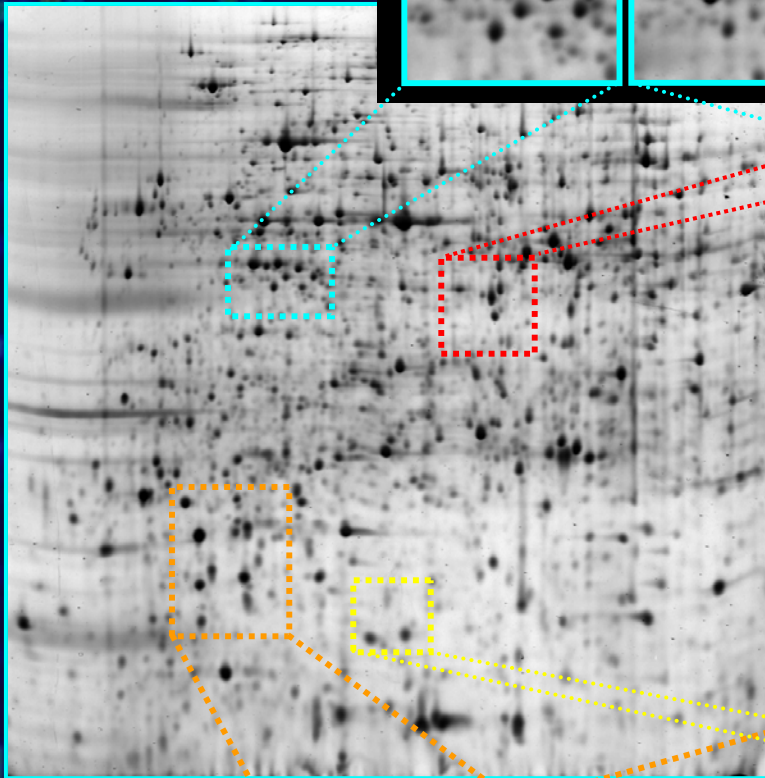


**Proteomics and the Antemortem
Diagnosis of Neurodegenerative Disease
(and a vignette)**

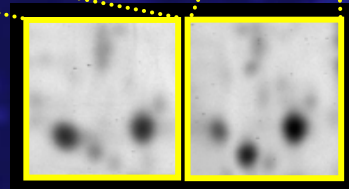
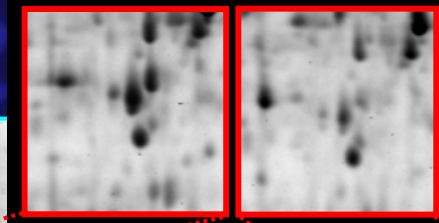
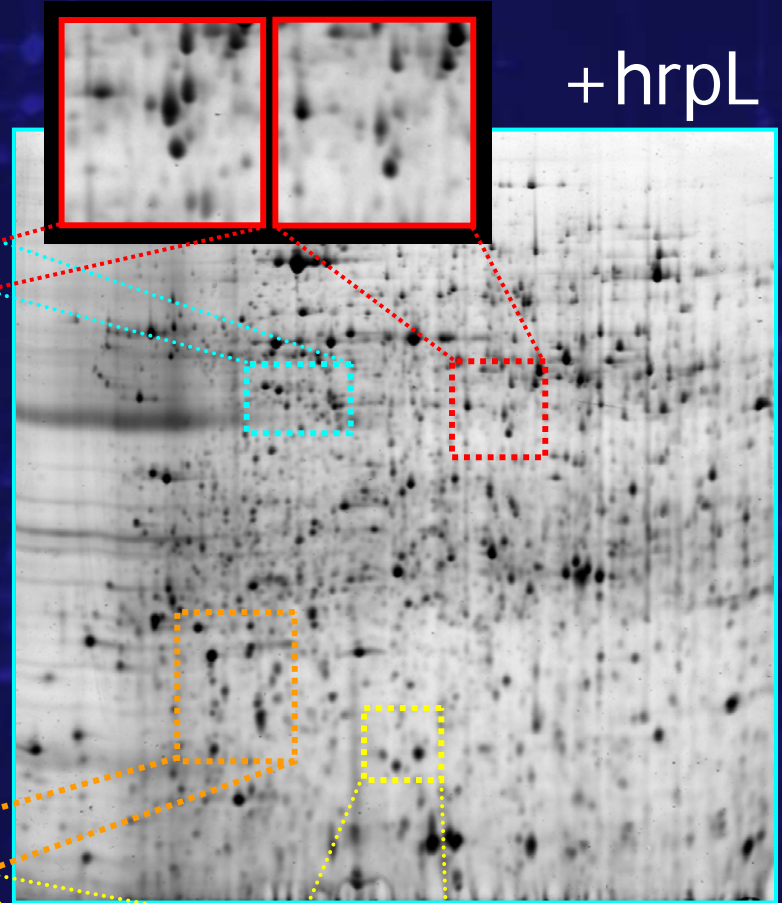
Kelvin H. Lee

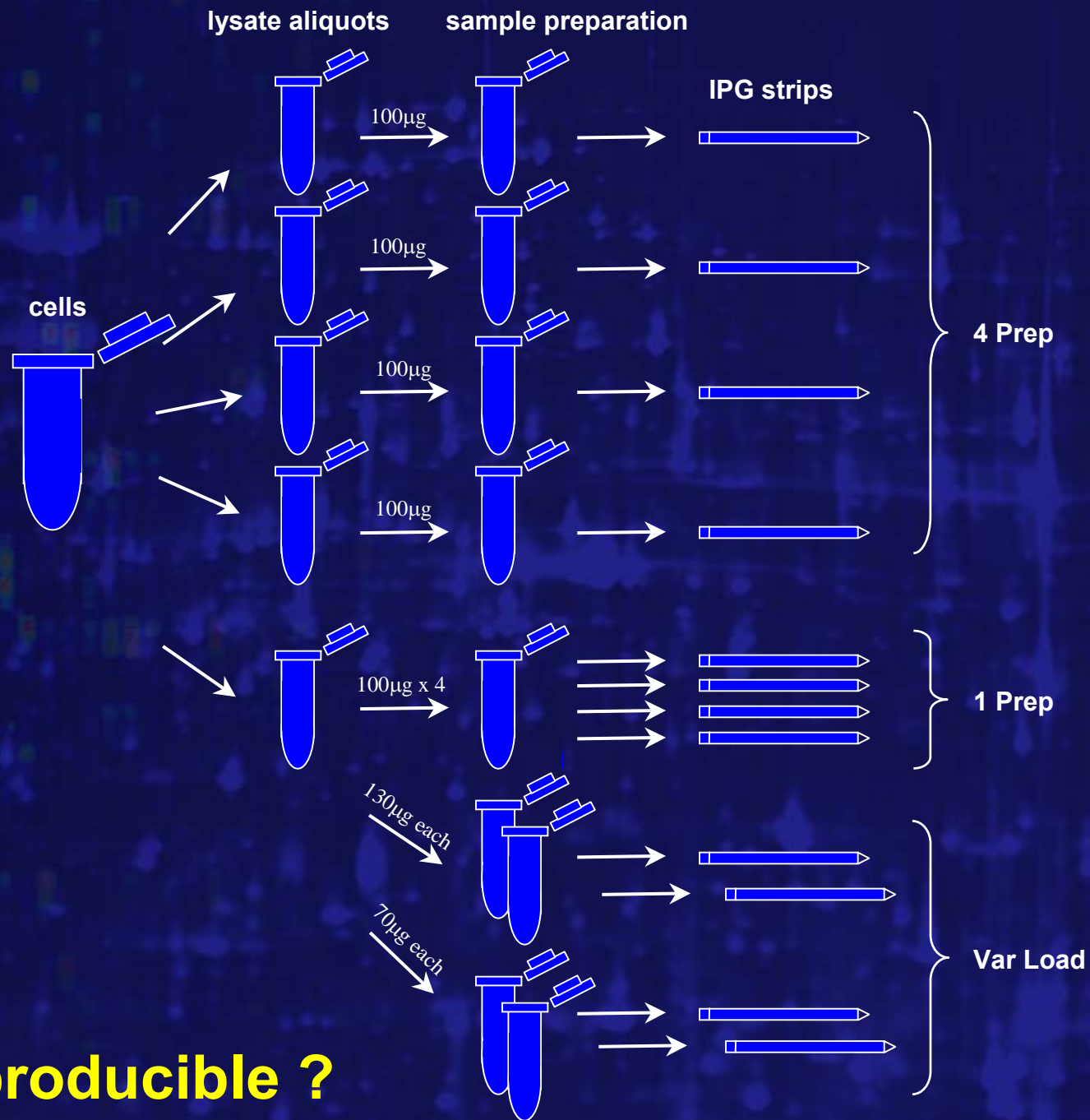
**Chemical and Biomolecular Engineering
Cornell Proteomics Program
Cornell University**

Δ hrp/hrc



+hrpL





But is it reproducible ?

Melanie 3 Analysis

Spots Matched in 2 out of 4 gels

Expt	#spots	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
1 Prep	815	76%	88%	94%	97%	99%	99%	100%	100%
4 Prep	842	65%	79%	90%	96%	98%	99%	100%	100%
Var Load	919	72%	85%	92%	97%	98%	99%	100%	100%

Spots Matched in 3 out of 4 gels

Expt	#spots	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
1 Prep	793	76%	88%	94%	97%	99%	99%	99%	100%
4 Prep	757	65%	79%	90%	96%	99%	99%	100%	100%
Var Load	879	73%	85%	93%	97%	99%	99%	100%	100%

Spots Matched in 4 out of 4 gels

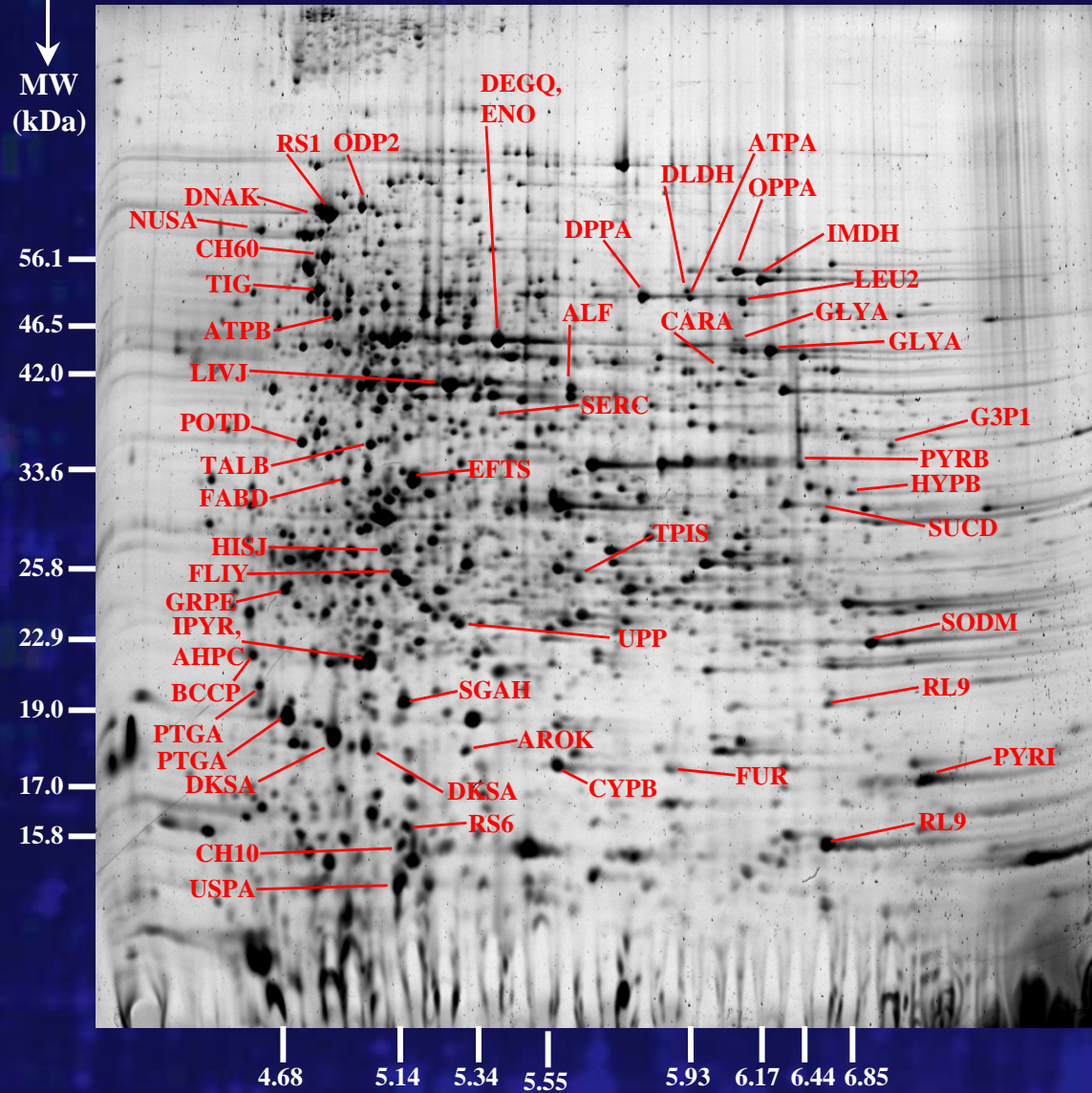
Expt	#spots	CV=0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
1 Prep	771	76%	88%	94%	97%	99%	99%	99%	100%
4 Prep	641	65%	79%	90%	96%	99%	100%	100%	100%
Var Load	824	74%	86%	93%	97%	99%	99%	100%	100%

Expt	Qual CV
1 Prep	0.03
4 Prep	0.14
Var Load	0.05

**Bottom line (with various caveats) :
95% of the spots exhibit a CV < 0.52.**

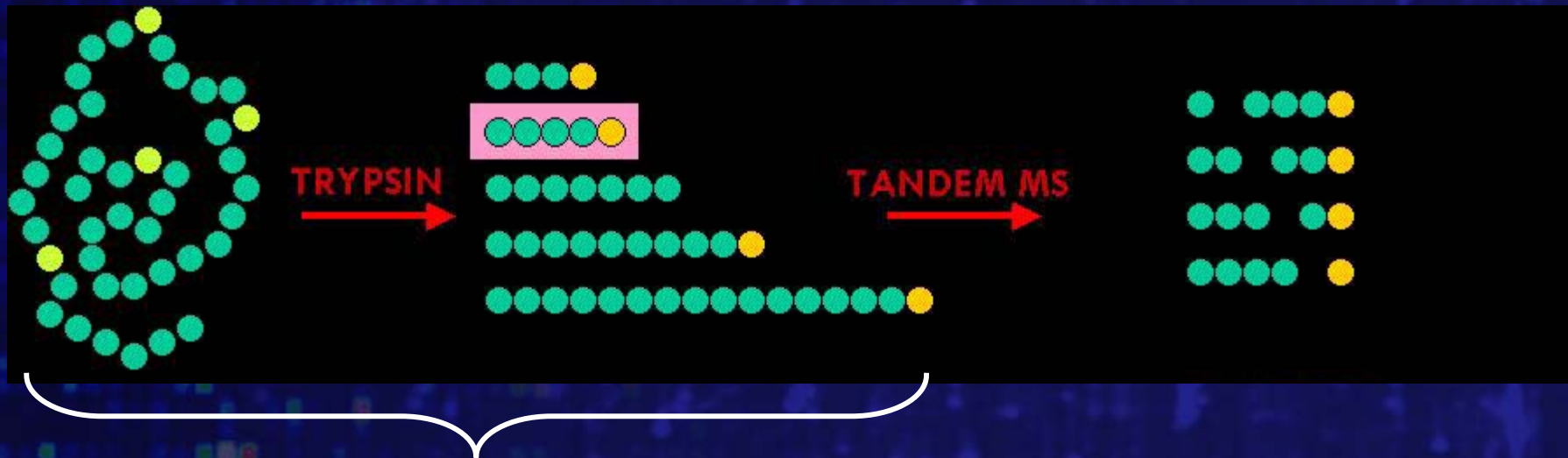
SYPRO Ruby stained gels

MW (kDa) → pI



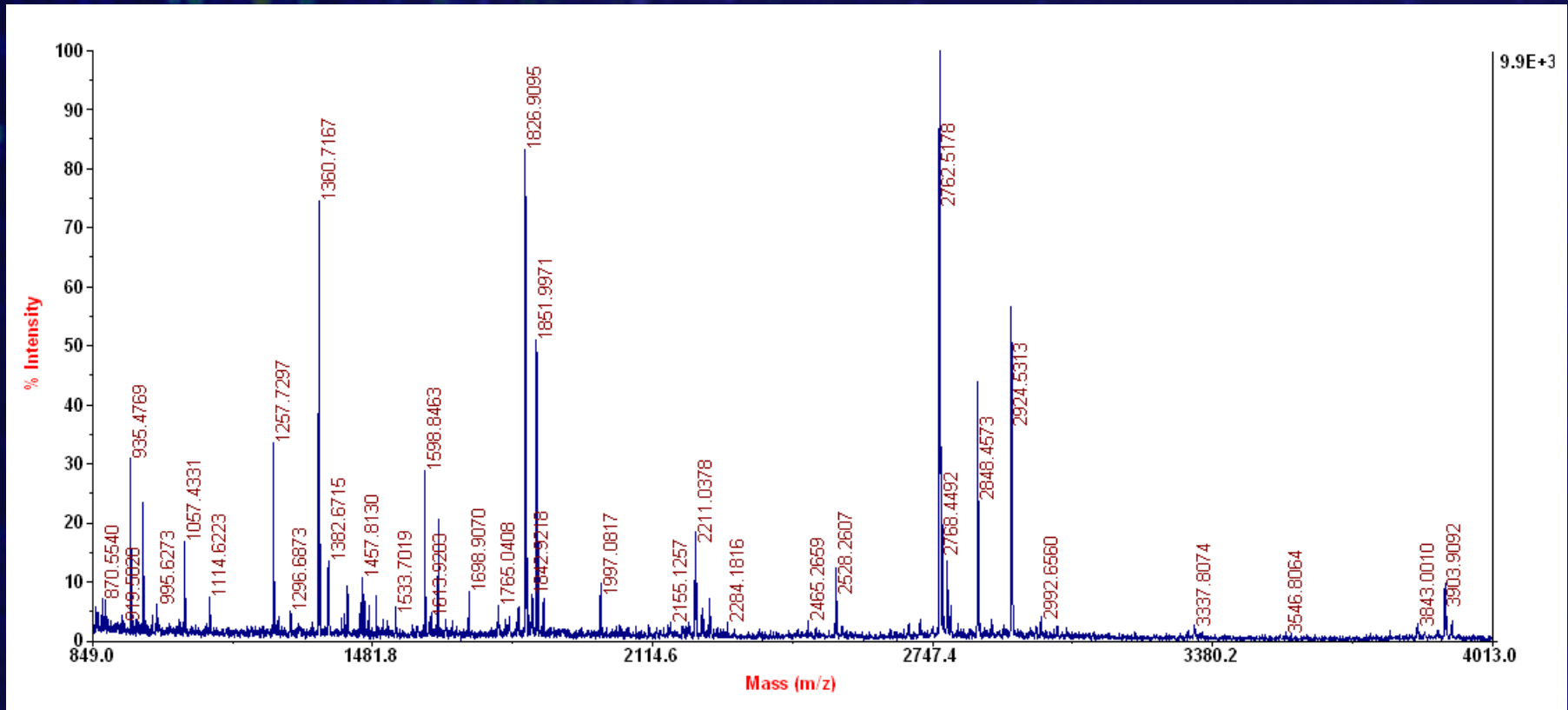
Characterization

Mass spectrometer measures mass of biomolecules with high accuracy.



Accurate mass measurement (ppm) of resulting tryptic peptides can be compared to *in silico* tryptic digests of sequence databases - Peptide Mass Fingerprinting.

Peptide Mass Fingerprinting Enabled by Availability of DNA Sequence Information



Works well for prokaryotes. Less so for eukaryotes.

Characterization

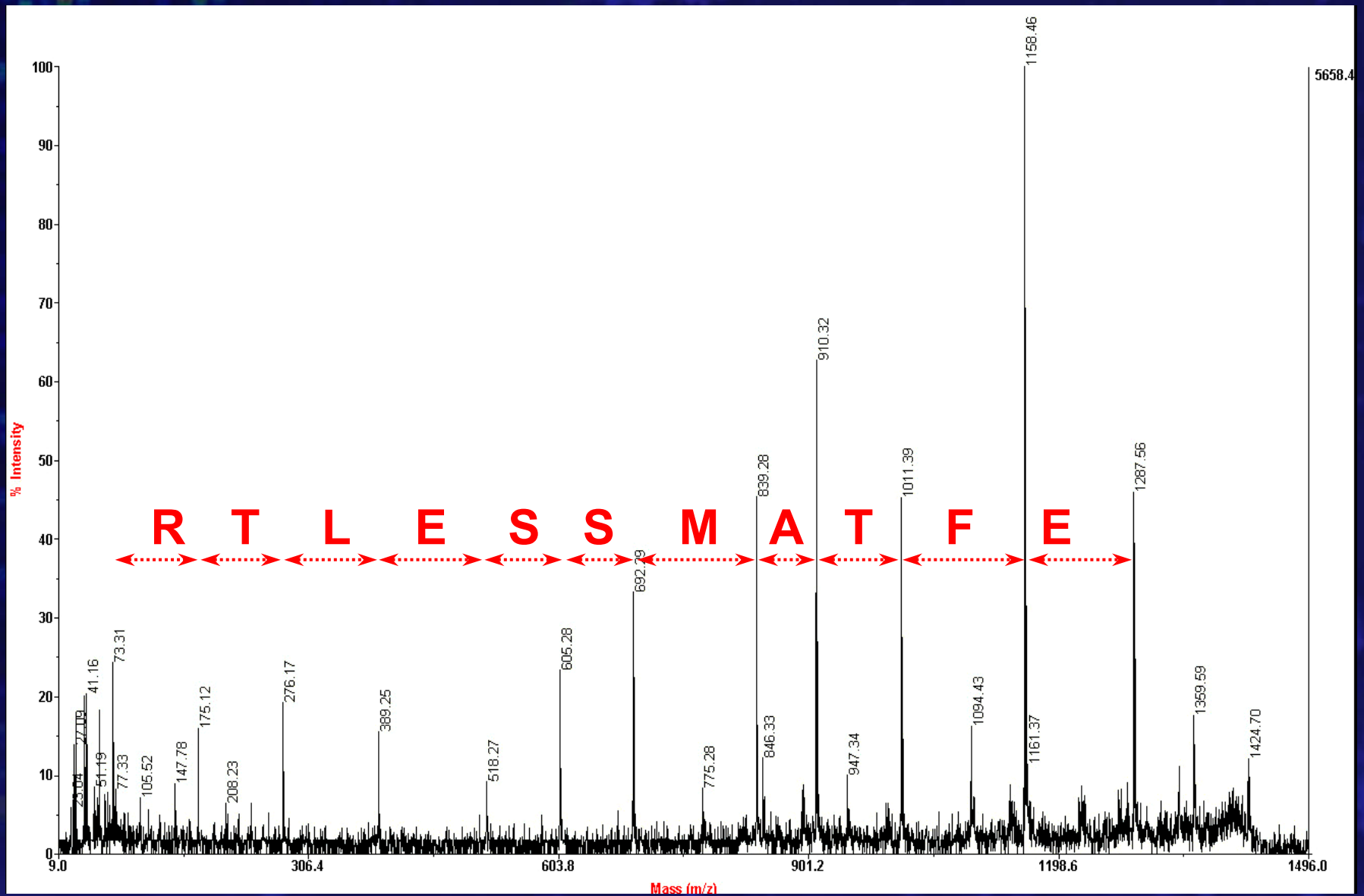
Mass spectrometer measures mass of biomolecules with high accuracy.



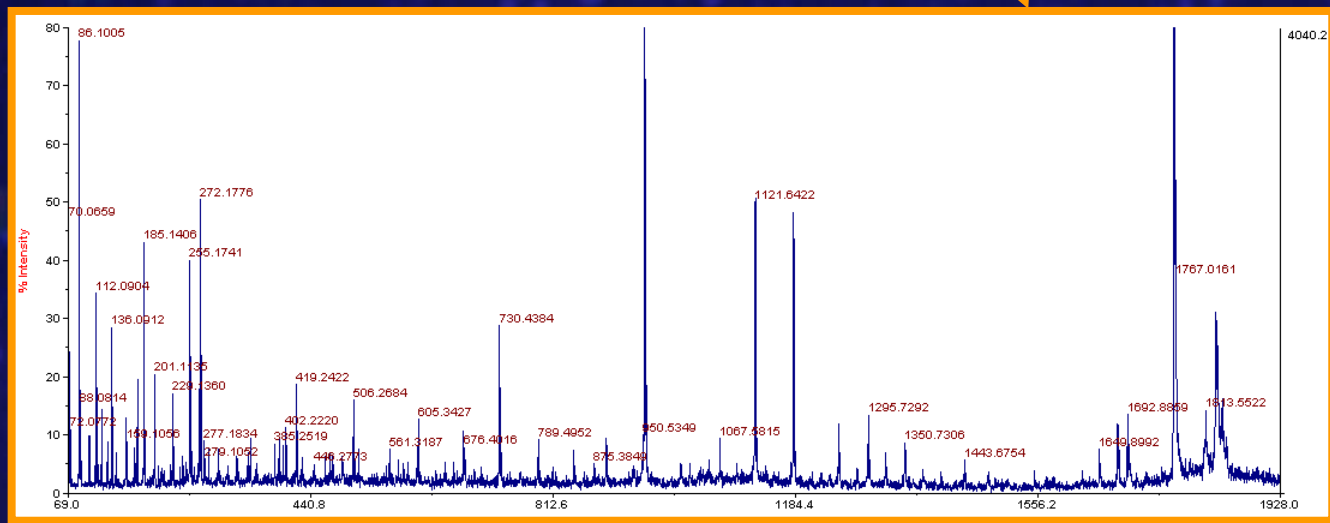
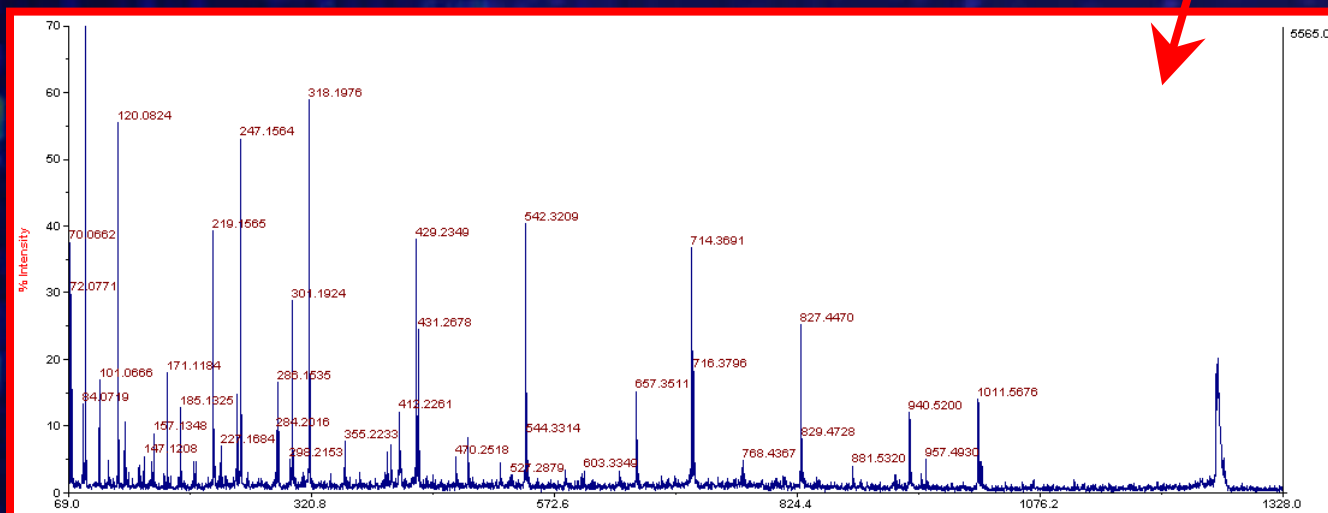
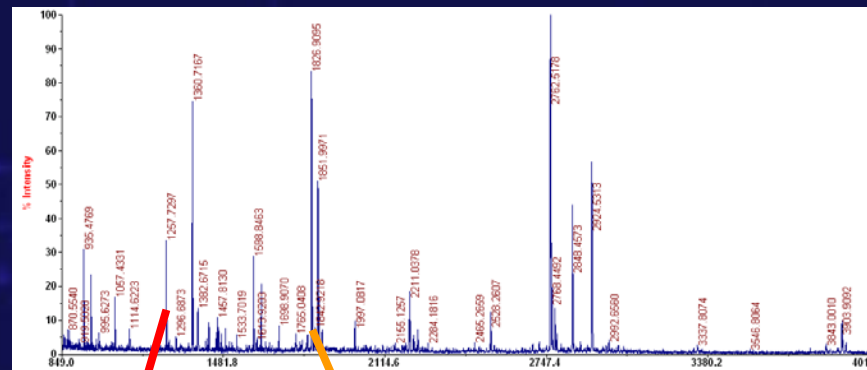
Peptide Mass Fingerprinting.

Individual peptides can be selected automatically by certain mass spectrometers for a tandem MS experiment.

MS/MS Analysis of $\text{HO}_2\text{C-R-T-L-E-S-S-M-A-T-F-E-NH}_2$



Tandem MS enables sequencing & high confidence characterization. MALDI facilitates simplicity.



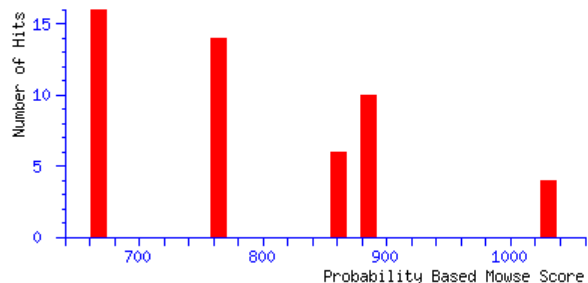
MASCOT Mascot Search Results

Pseudomonas syringae TOF-TOF Example

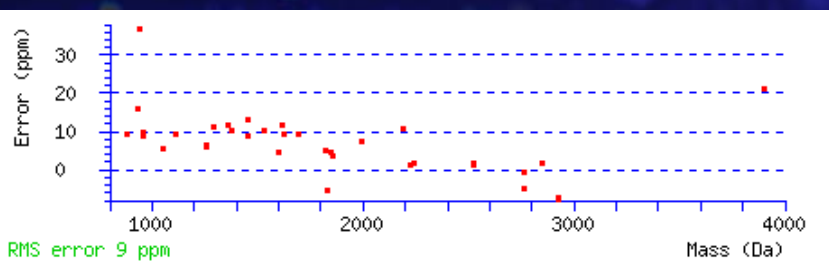
Search title : SampleSetID: 2022, AnalysisID: 4593, MalDiWellID: 58508, S
 Database : syringae6frame new (1836856 sequences; 298367028 residues)
 Taxonomy : Bacteria (Eubacteria) (1836856 sequences)
 Timestamp : 3 Oct 2003 at 17:57:19 GMT
 Top Score : 1030 for **16853.00116675**, 4887162..4888607

Probability Based Mowse Score

Score is $-10 * \log(P)$, where P is the probability that the observed match is a random event.
 Protein scores greater than 75 are significant ($p < 0.05$).



MOWSE scores represent probability of random match
1030 \Rightarrow $P = 1.85 \times 10^{-43}$



Match to: **16853.00116675**; Score: 1030
 4887162..4888607

Nominal mass (M_0): 51882; Calculated pI value: 6.35
 NCBI BLAST search of **16853.00116675** against nr

Variable modifications: Carbamidomethyl (C), Oxidation (M), Propionamide (C)
 Cleavage by Trypsin: cuts C-term side of KR unless next residue is P
 Sequence Coverage: 82%

Matched peptides shown in **Bold Red**

```

1 TVRRTRKIVAT LGPASNSPEV IEQLILSGLD VARLNFSGHT PDEHKARAKL
51 IREIAARHGR FVALLGDLQG PKIRIAKFTD KRIELKVGDK FTFSTAHLPT
101 SGNQQIVGID YPDLVKCGV GDELLDDGR VVMFVDITQA HELHCTVLIG
151 GPLSDHKGIN RRGGLTAPA LTEKDRQDIK LAEMDLDTL AVSFPRDAAD
201 MEYARQLRDE SGGTAWLVAK IERAEAVAND EVLDALIRAS DAVMVARGDL
251 GVEIGDAELV GVQKRIILHA RRHNKAVIVA TQMMESMISS PMPTRAEVSD
301 VANAVLDYTD AVMLSAESAA GSYPEAVQA MARIQVGAEK HPITGKTSRHR
351 IGHSFTRCDE SIALAAMYTA NHFPQVKALI ALTESGYTL DMSRIRSSVP
401 IYAFSPHRGT QARAAMFRGV YTVFPDPGAL PPGQVSQAAV DELLKRGVLV
451 QGDWVILTK DSYHTIGTGN GKILHVGDP LV
    
```

Start - End	Observed	Mr(expt)	Mr(calc)	Delta	Miss	Sequence
7 - 33	2762.52	2761.51	2761.52	-0.01	0	IVATLGPASNSPEVIEQLILSGLDVAR (Ions score 136)
7 - 33	2762.52	2761.51	2761.52	-0.01	0	IVATLGPASNSPEVIEQLILSGLDVAR (No match)
34 - 45	1381.66	1380.66	1380.64	0.01	0	LNFSHGTPDEHK (No match)
50 - 57	941.62	940.62	940.58	0.03	1	LIREIAAR (No match)
61 - 72	1257.73	1256.72	1256.71	0.01	0	FVALLGDLQGPK (Ions score 96)
61 - 72	1257.73	1256.72	1256.71	0.01	0	FVALLGDLQGPK (No match)
91 - 116	2848.46	2847.45	2847.44	0.00	0	FTFSTAHLTSGNQTIVGIDYPPDLVK (Ions score 71)
91 - 116	2848.46	2847.45	2847.44	0.00	0	FTFSTAHLTSGNQTIVGIDYPPDLVK (No match)
117 - 130	1533.70	1532.69	1532.68	0.02	0	DCGVGDELLDDGR Carbamidomethyl (C) (No match)
135 - 157	2528.26	2527.25	2527.25	0.00	0	VDYTAHELHCTVLIGGPLSDHK Carbamidomethyl (C) (Ions score 45)
163 - 174	1114.62	1113.61	1113.60	0.01	0	GGGLTAPALTEK (No match)
181 - 196	1826.91	1825.90	1825.89	0.01	0	LAEMDLDTLAVSFPR Oxidation (M) (Ions score 79)
181 - 196	1826.91	1825.90	1825.89	0.01	0	LAEMDLDTLAVSFPR Oxidation (M) (No match)
197 - 205	1057.43	1056.42	1056.42	0.01	0	DAADMETAR Oxidation (M) (No match)
197 - 205	1057.43	1056.42	1056.42	0.01	0	DAADMETAR Oxidation (M) (Ions score 5)
221 - 238	1997.08	1996.07	1996.06	0.01	1	TERAEAVANDEVLDALIR (No match)
221 - 238	1997.08	1996.07	1996.06	0.01	1	TERAEAVANDEVLDALIR (Ions score 10)
224 - 238	1598.85	1597.84	1597.83	0.01	0	AEAVANDEVLDALIR (Ions score 36)
224 - 238	1598.85	1597.84	1597.83	0.01	0	AEAVANDEVLDALIR (No match)
239 - 247	935.48	934.47	934.45	0.01	0	ASDAVMVAR Oxidation (M) (No match)
248 - 264	1698.91	1697.90	1697.88	0.02	0	GDLVGEIGDAELVGVQK (Ions score 35)
248 - 264	1698.91	1697.90	1697.88	0.02	0	GDLVGEIGDAELVGVQK (No match)
248 - 265	1855.00	1853.99	1853.98	0.01	1	GDLVGEIGDAELVGVQKR (No match)
266 - 272	878.58	877.57	877.56	0.01	1	LILHARR (No match)
276 - 295	2228.05	2227.04	2227.04	0.00	0	AVIVATQMMESMISSPMPTR 3 Oxidation (M) (No match)
276 - 295	2244.04	2243.03	2243.03	0.00	0	AVIVATQMMESMISSPMPTR 4 Oxidation (M) (No match)
296 - 333	3903.91	3902.90	3902.82	0.08	0	AEVSDVANAVLDYTDVAVMLSAESAAGSYPEAVQAHAR 2 Oxidation (M) (No match)
334 - 345	1296.69	1295.68	1295.67	0.01	1	ICVGAERKPTGK Carbamidomethyl (C) (No match)
358 - 377	2195.05	2194.04	2194.02	0.02	0	CDESIALAAMYTAHFPGVK Carbamidomethyl (C) (No match)
378 - 394	1835.98	1834.98	1834.99	-0.01	0	ALIALTESGYTLIMSR (No match)
378 - 394	1852.00	1850.99	1850.98	0.01	0	ALIALTESGYTLIMSR Oxidation (M) (No match)
378 - 394	1852.00	1850.99	1850.98	0.01	0	ALIALTESGYTLIMSR Oxidation (M) (Ions score 18)
395 - 408	1629.90	1628.89	1628.88	0.02	1	IRSSVPIYAFSPHR (No match)
395 - 408	1629.90	1628.89	1628.88	0.02	1	IRSSVPIYAFSPHR (Ions score 16)
397 - 408	1360.72	1359.71	1359.69	0.02	0	SSVPIYAFSPHR (Ions score 59)
397 - 408	1360.72	1359.71	1359.69	0.02	0	SSVPIYAFSPHR (No match)
419 - 445	2768.45	2767.44	2767.44	-0.00	0	GVYTVFPDPGALPPGQVSQAAVDLELLK (No match)
419 - 446	2924.53	2923.52	2923.54	-0.02	1	GVYTVFPDPGALPPGQVSQAAVDLELLKR (Ions score 53)
419 - 446	2924.53	2923.52	2923.54	-0.02	1	GVYTVFPDPGALPPGQVSQAAVDLELLKR (Ions score 53)
419 - 446	2924.53	2923.52	2923.54	-0.02	1	GVYTVFPDPGALPPGQVSQAAVDLELLKR (Ions score 108)
446 - 459	1613.92	1612.91	1612.89	0.02	1	RLVGEIGDWWILTK (No match)
447 - 459	1457.81	1456.81	1456.79	0.01	0	GLVGEIGDWWILTK (No match)
460 - 473	1453.66	1452.65	1452.63	0.02	0	GD SYHTIGTNGAK Oxidation (M) (No match)
474 - 482	962.58	961.57	961.56	0.01	0	ILHVGDPPLV (No match)
474 - 482	962.58	961.57	961.56	0.01	0	ILHVGDPPLV (Ions score 42)

Cerebrospinal Spinal Fluid (CSF) Proteins as Central Nervous System Disease Markers



Lumbar
CSF

Analysis

Normal

Different

disease specific
disease stage (early/late)
symptom specific
pathology specific
severity
response to therapy
sample specific

Are there any dementia biomarkers in CSF ?

Vascular dementia - none

Dementia with Lewy bodies - none

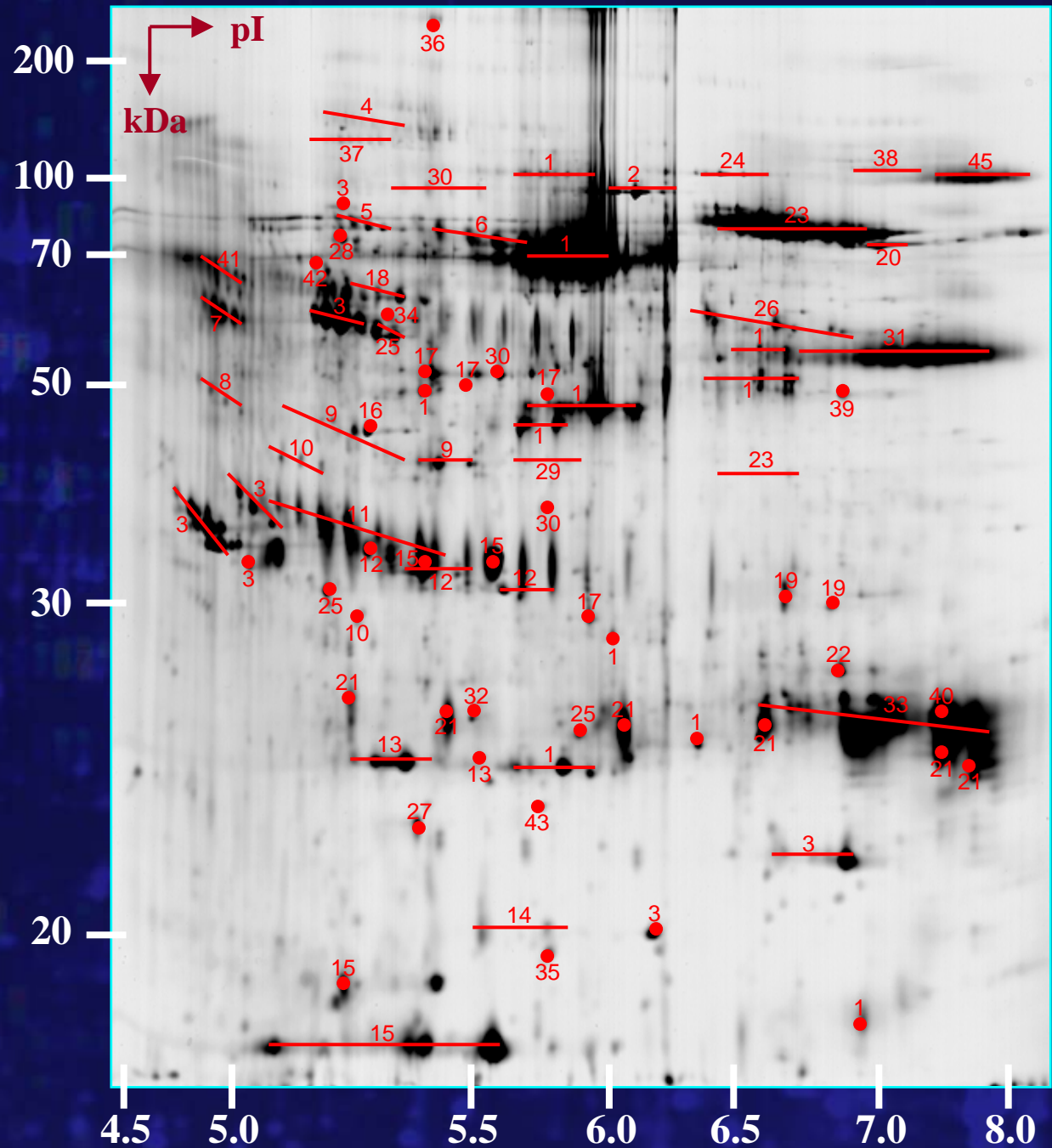
Frontotemporal dementia - none

Alzheimer's disease - $A\beta_{1-42}$, Tau, AD7C-NTP

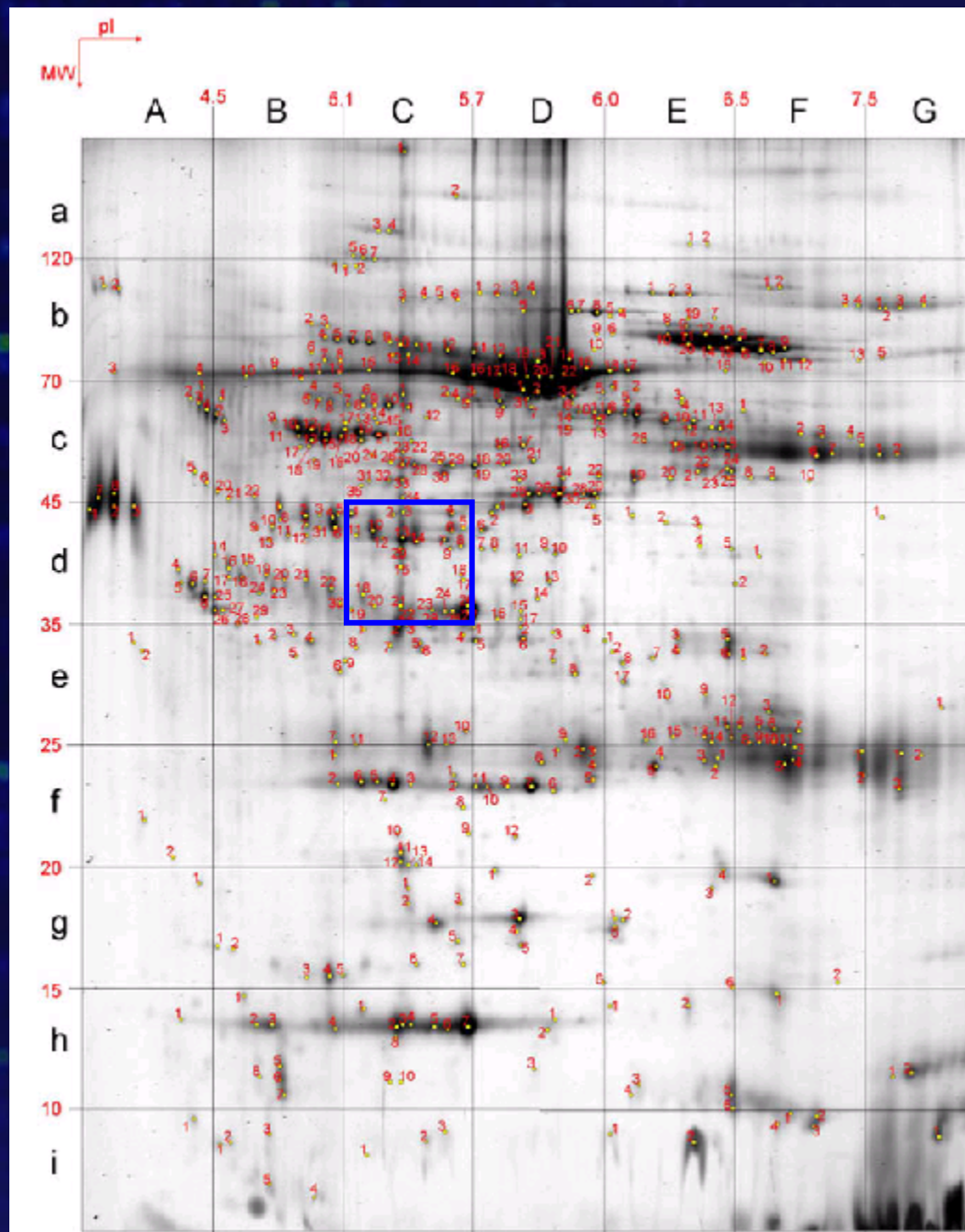
$A\beta_{1-42}$	83% sens, 82% spec
Tau	88% sens, 92% spec
$A\beta_{1-42}$ + Tau	85% sens, 87% spec
AD7C-NTP	70% sens, 87% spec

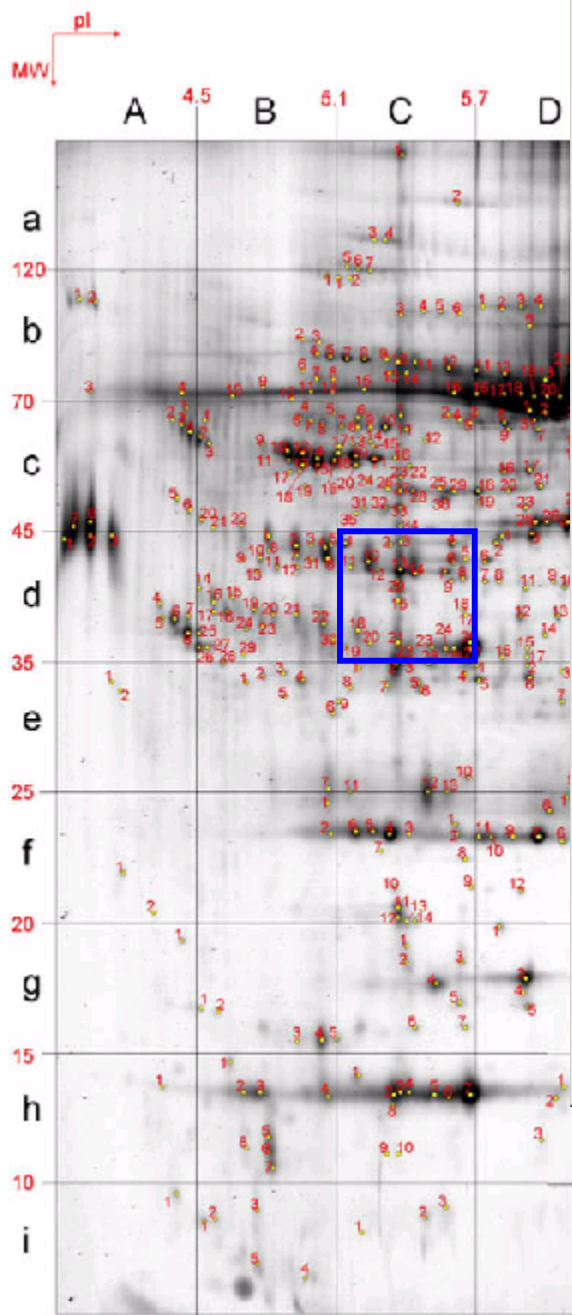
Sensitivity - true positive
Specificity - true negative

- 1 Albumin
- 2 Gelsolin
- 3 α -1-antitrypsin
- 4 Ceruloplasmin
- 5 α -1-B glycoprotein
- 6 Hemopexin
- 7 α 2-HS glycoprotein
- 8 Leucine-rich α -2-glycoprotein
- 9 Haptoglobin
- 10 Zinc- α -2-glycoprotein
- 11 Apolipoprotein J
- 12 Apolipoprotein E
- 13 Apolipoprotein A-I
- 14 Hp2- α -haptoglobin
- 15 Transthyretin
- 16 Apolipoprotein A-IV
- 17 EPC-1
- 18 Antithrombin III
- 19 Complement component 4A
- 20 Complement component 3
- 21 Prostaglandin D2 synthase
- 22 Kallikrein 6
- 23 Transferrin
- 24 Complement factor B
- 25 Vitamin D binding protein
- 26 β -2-glycoprotein
- 27 Retinal binding protein
- 28 Collagenase type IV
- 29 Fibrinogen beta
- 30 Fibrinogen gamma
- 31 Ig heavy chain
- 32 Serum amyloid P
- 33 Ig light chain
- 34 Angiotensinogen
- 35 Cu/Zn superoxide dismutase
- 36 Fibronectin
- 37 Inter- α -trypsin inhibitor heavy chain
- 38 Plasminogen
- 39 Complement factor H
- 40 Glutathione S-transferase
- 41 α -1-antichymotrypsin
- 42 kininogen
- 43 Perlecan

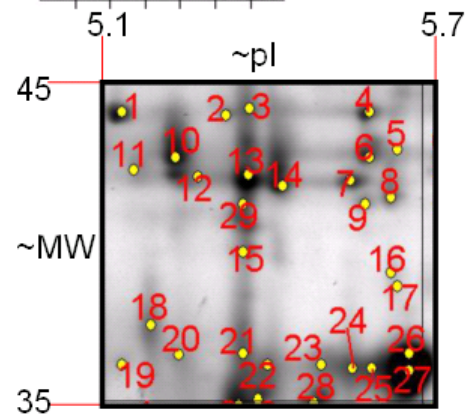
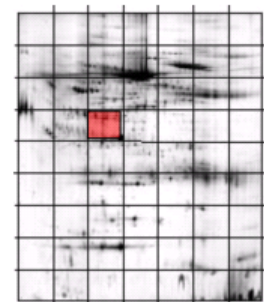


www.leelab.org/csfmap





Cd



Spot	Identification	gi#	score	CI	Link
Cd1	Apolipoprotein AIV	178779	199	100	●
Cd2	β-actin	14250401	167	100	●
Cd3	Serum albumin	113576	63	99	●
Cd4	Serum albumin	113576	67	99.9	●
Cd5	Serum albumin	113576	73	99.9	●
Cd6	Serum albumin	113576	152	100	●
Cd7	Serum albumin	113576	141	100	●
Cd8	Haptoglobin 1	123507	99	100	●
Cd8	Serum albumin	113576	51	96	●
Cd9	Serum albumin	113576	60	99.6	●
Cd11	α-1-antitrypsin	1942629	92	100	●
Cd12	Cathepsin L	4503155	25i	99	●
Cd13	Haptoglobin 1	123507	154	100	●
Cd13	Serum albumin	113576	87	99.9	●
Cd14	Haptoglobin 1	123507	80	99.9	●
Cd14	Serum albumin	113576	114	100	●
Cd15	Haptoglobin 1	123507	22i	97	●
Cd16	Haptoglobin 1	123507	27i	99.7	●
Cd17	Apolipoprotein J	178855	20i	95	●
Cd18	Apolipoprotein J	178855	149	100	●
Cd19	Apolipoprotein E	178563	113	100	●
Cd20	Apolipoprotein E	178563	56	98	●
Cd21	Apolipoprotein J	178855	172	100	●
Cd22	Apolipoprotein E	178563	104	100	●
Cd23	Apolipoprotein E	178563	111	100	●
Cd24	Apolipoprotein E	178563	119	100	●
Cd25	Apolipoprotein J	178855	61	99.6	●
Cd25	Transferrin	339685	154	100	●
Cd26	Transferrin	339685	273	100	●
Cd27	Transferrin	339685	212	100	●
Cd28	Apolipoprotein E	178563	232	100	●
Cd29	Serum albumin	113576	70	99.9	●

Transmissible Spongiform Encephalopathy (TSE)

In humans:

Creutzfeldt–Jakob disease (CJD)

New variant CJD

Kuru

others

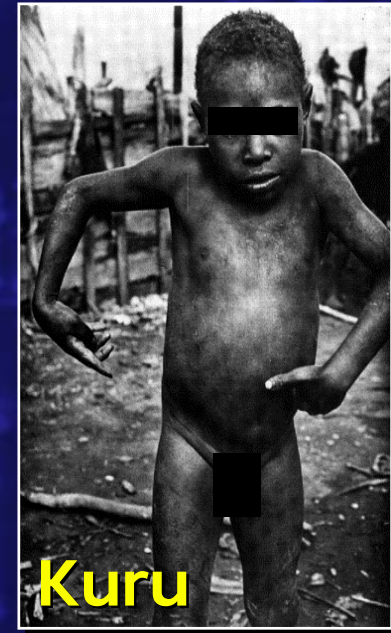
In animals:

Scrapie (sheep)

Bovine spongiform encephalopathy (BSE)

Transmissible mink encephalopathy (TME)

others



Molecular Pathology - An Enigma



- Normal prion protein (PrP) has unknown function.
- In TSEs, PrP is “misfolded” (PrP $\xrightarrow{\text{PrP}^{\text{res}}}$ PrP^{res}) and amplified.
- BUT, one cannot reconstitute the disease with this pure PrP^{res} and different strains of PrP^{res} appear to exist.
- Heat, denaturants and proteases do not eliminate transmissibility.

Unifying Characteristics of TSEs

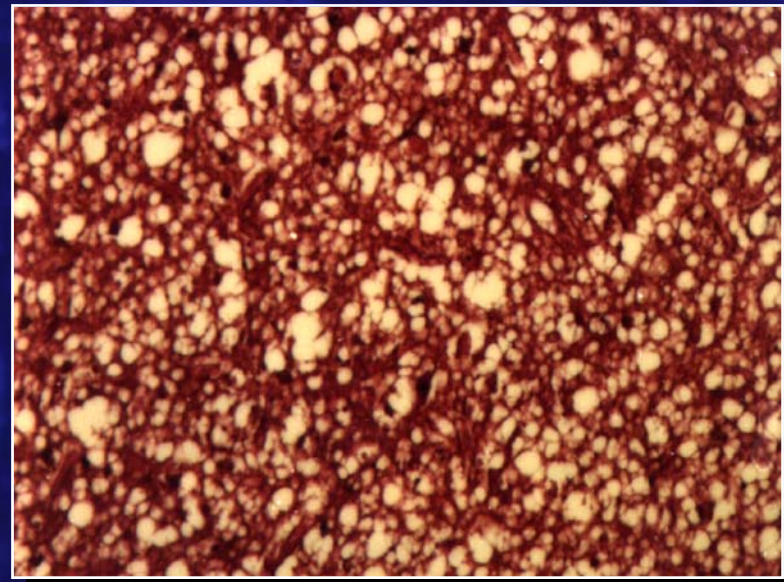
Transmissible (inter and intraspecies) - agent is very resistant to decontamination

Prion - no inflammatory response

Exposure, long incubation, onset of symptoms

Fatal

Spongiform pathology



Transmissible Spongiform Encephalopathy (TSE)

In humans:

Sporadic CJD

many years

New variant CJD

since 1996

others

In animals:

Scrapie (sheep)



"Mad Cow disease" (BSE)

many years

since 1986

others

**Slaughter of all UK cattle > 30 months old
has a significant economic impact.**

Commercially - Available, Postmortem Screening Tools for BSE in Cattle

Several antibody-based tests with 100% sensitivity

Tests not validated for use on humans

A need to classify vCJD vs spCJD

No antemortem tests available

CJD in UK (since 1993)

	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003
spCJD	38	51	35	40	59	63	62	49	55	73	57
iatrogenic CJD	4	1	4	4	6	3	6	1	3	0	4
other CJD	4	7	5	6	5	5	2	3	4	5	4
prob vCJD (alive)	0	0	0	0	0	0	0	0	0	0	0
vCJD (pending PM)	0	0	0	0	0	0	0	0	0	0	0
vCJD (confirmed)	0	0	3	10	10	18	15	28	20	17	18
Total	46	59	47	60	80	89	84	81	82	95	83

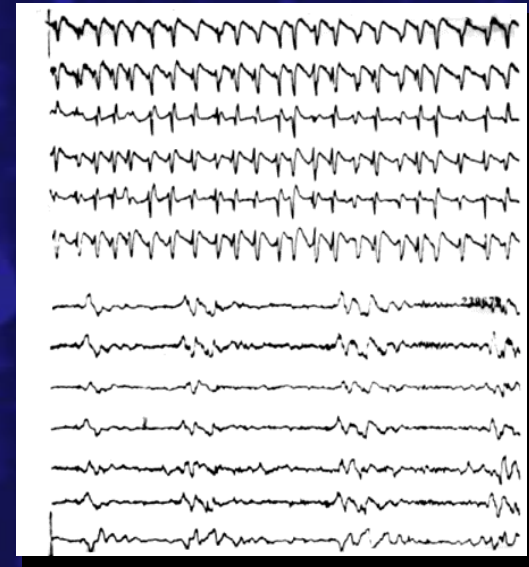
Total def & pr vCJD = 139 in UK

Differential Diagnosis: Alzheimer's, AIDS dementia, multi-infarct dementia, etc.

Antemortem Diagnosis - Humans

Clinical Diagnosis

- Atypical, subacute dementia
- Startle myoclonus
- "At risk" populations
- Brain biopsy
- Characteristic EEG

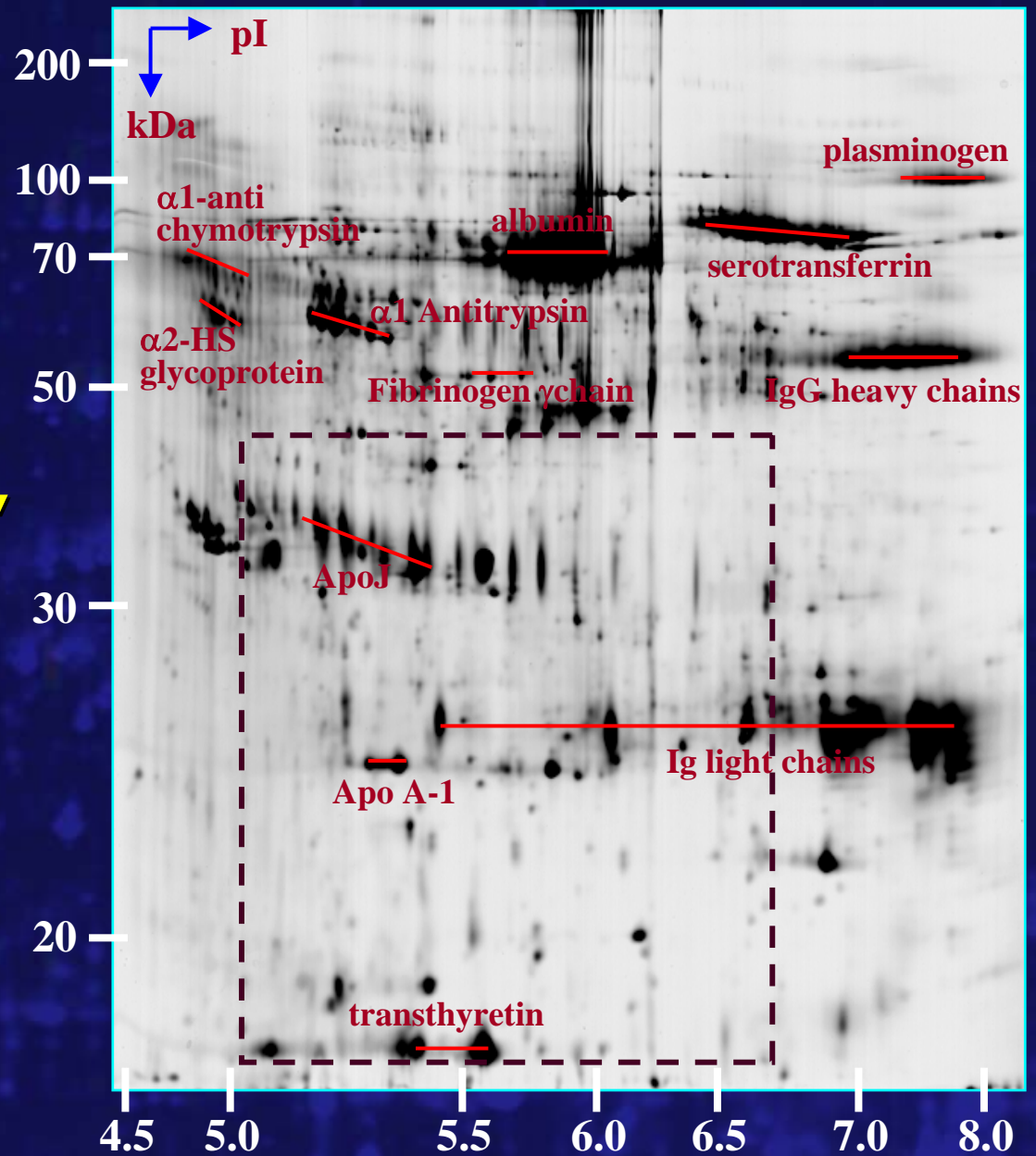


→ Iatrogenic transmission and may miss site of pathology

→ Not for atypical cases like vCJD

(Misdiagnosis of BSE and of animal TSEs)

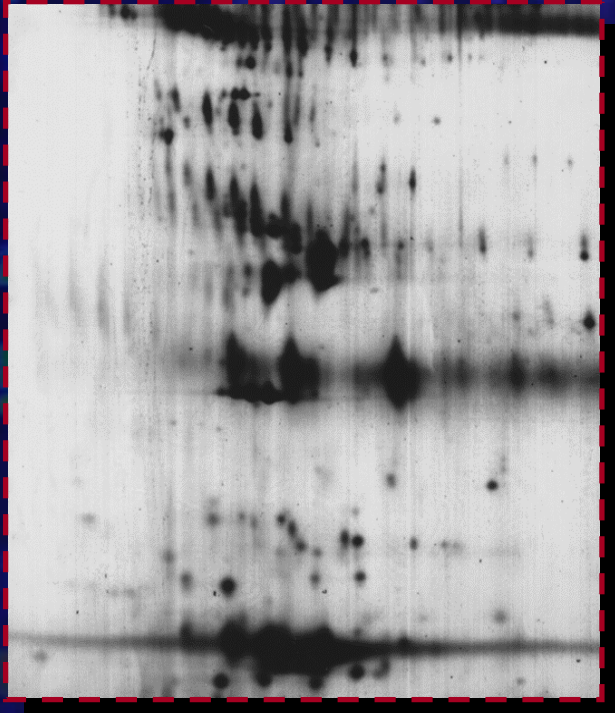
**Silver Stain
2DE-Separated
Proteins in
Cerebrospinal
Fluid
from a "Normal"
Volunteer**



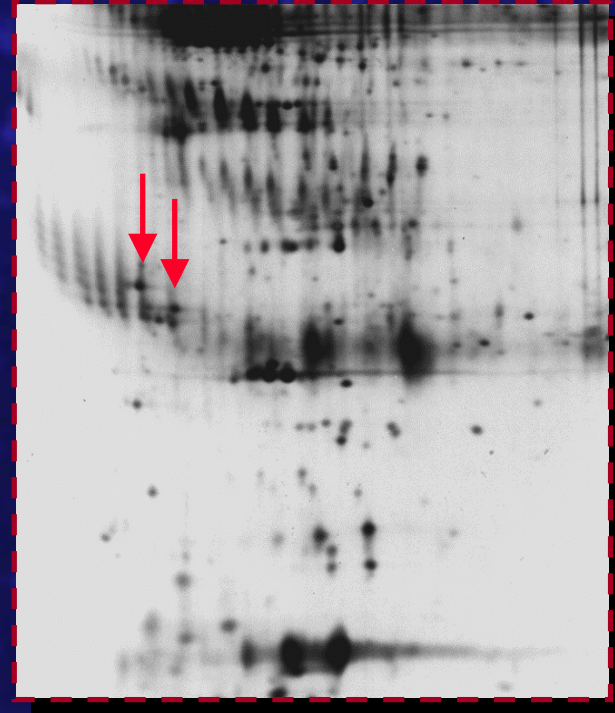
Proteomics Identifies Two Creutzfeldt–Jakob Disease Associated Proteins

131 (5.1, 29 kD)

130 (5.2, 26 kD)



Normal CSF



CJD CSF

Results with the 130/131 Assay in the Differential Diagnosis of Demented Patients

69 of 70 (>98%)

CJD patients were positive

297 of 298 (>99%)*

control patients were negative

*primary CNS lymphoma

Proteomics as a Discovery Tool in Assay Development

2D Gels

Complicated technology
Not automated
Too slow for the clinic
Lower throughput

Immunoassay

Simple technology
Automated
Fast
High throughput

How can we purify enough material for sequencing?

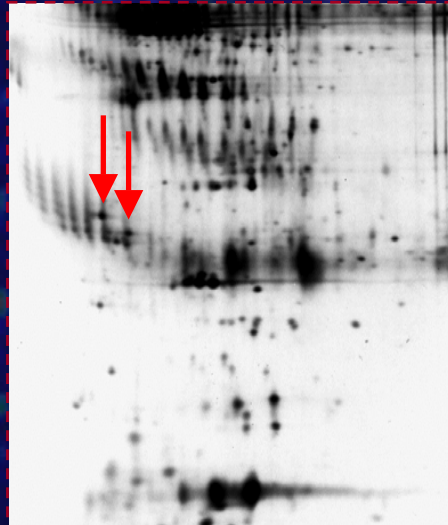
Hypothesis:

The appearance of 130/131 in CSF of CJD patients is a result of spongiform pathology. As neurons are destroyed their protein content leaks into the CSF.

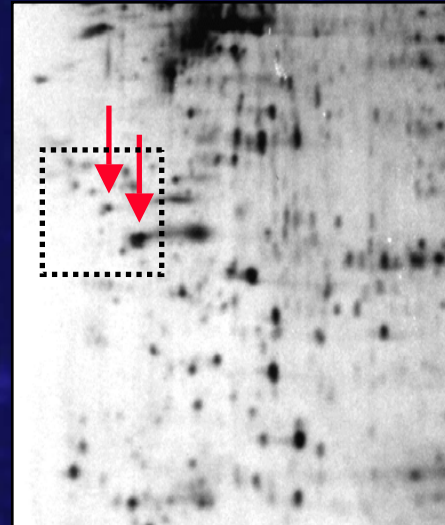
Can we find 130/131 in brain extract from normal individuals?

Identification of CSF Proteins 130/131 in Normal Brain Extract

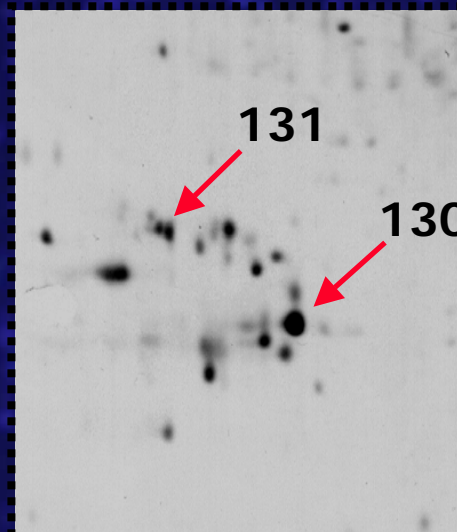
CJD
CSF



Normal
Brain



Normal
Brain



Characterization of Spot 130

Brain spot corresponding to CSF 130 pooled from 10 blots
LysC digestion
4 sequences obtained (initial yield 4 ± 2 pmol):

VTELNEPLXNEDXNLLSVA

DYYXYLAEVATGEK

NVVXARRSSXRVISSIEQ

YSEAXEIS



human 14-3-3 γ †

† Sequence information from A. Aitken

14-3-3 Family of Proteins

Seven isoforms

Highly conserved sequence

Variety of functions:

signal transduction

cell cycle control

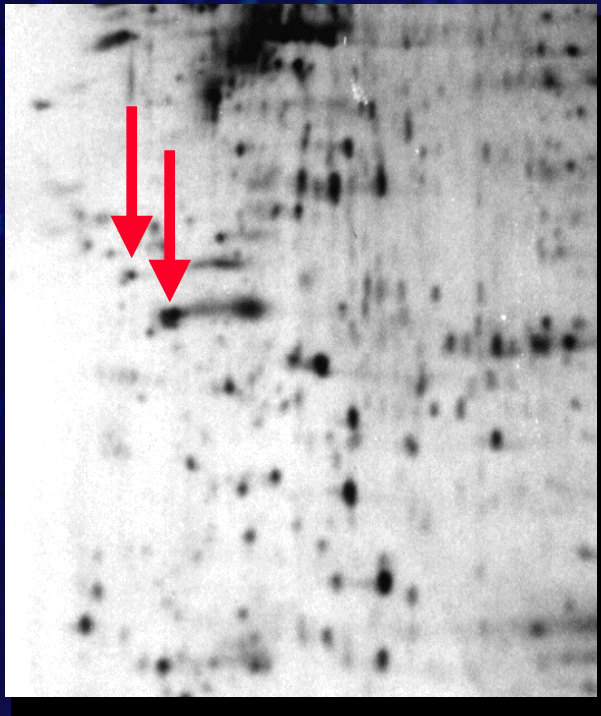
exocytosis

melatonin biosynthesis

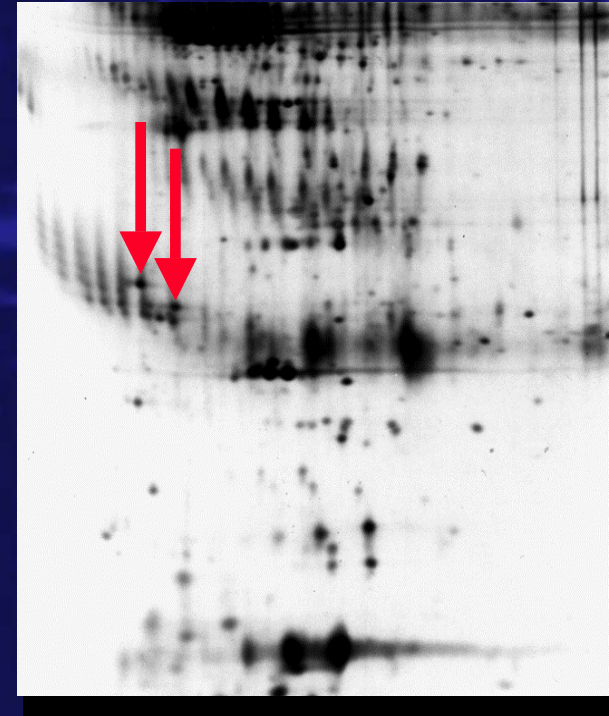
Identification of CSF 130/131 Proteins in Brain

sequence → antibody

brain



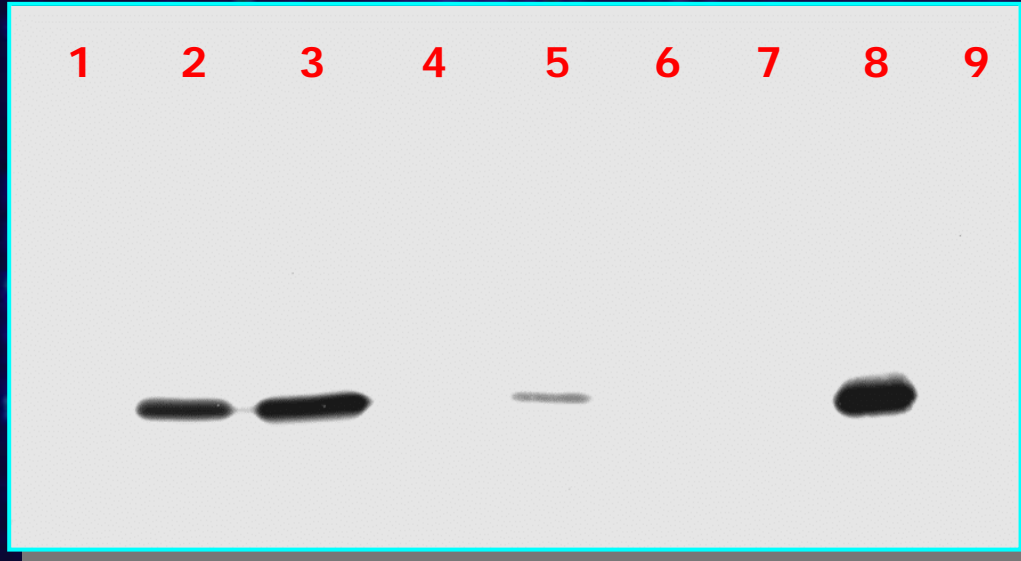
CSF



Anti-14-3-3 antibodies recognize both 130 and 131
on 2DE immunoblots of CJD CSF and brain extract.

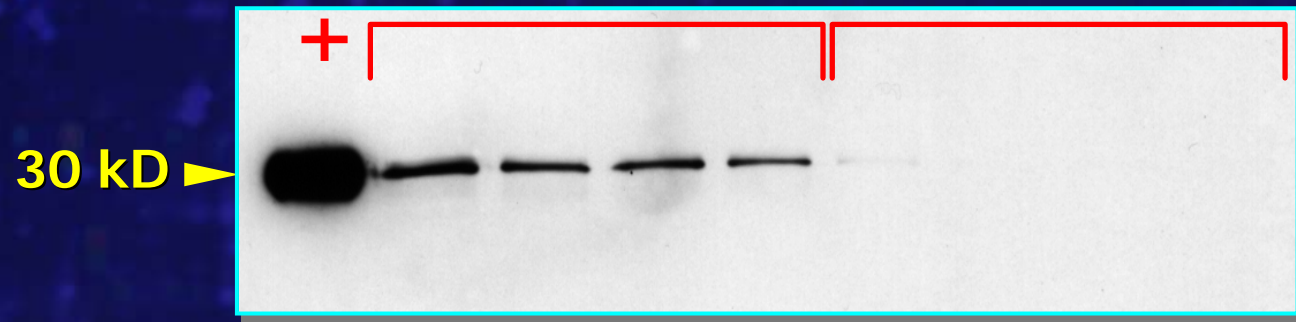
1D Assay for TSEs including BSE

- 1: Alzheimer's
- 2 & 3: CJD
- 4: normal cow
- 5: experimental TME in cow
- 6: normal human serum
- 7: CJD serum
- 8: normal human brain
- 9: PrP-pur. brain extract – CJD



BSE

control



ANIMALS	TOTAL SAMPLES	POSITIVE SAMPLES
Cattle: induced TME		
+ pathology	5	3
– pathology	1*	1*
Cattle: induced scrapie	4	3
Cattle: normal controls	15	0
Cattle: BSE	10	10
Cattle: BSE normal controls	6	1
Sheep: scrapie	6	5
Sheep: normal controls	1	0
Chimps: induced TSE	15	15
Chimps: normal controls	77	0
Total animals with + path	40	36
Total animals with – path	100	2

*This cow had clinical symptoms of TSE but normal histopathology

Effectiveness of Assays for TSE

2DE - Human

Overall Sensitivity > 98 % (69/70)

Overall Specificity > 99 % (297/298)

1D - Human

Overall Sensitivity > 96 % (68/71)

Overall Specificity > 99 % (90/91)

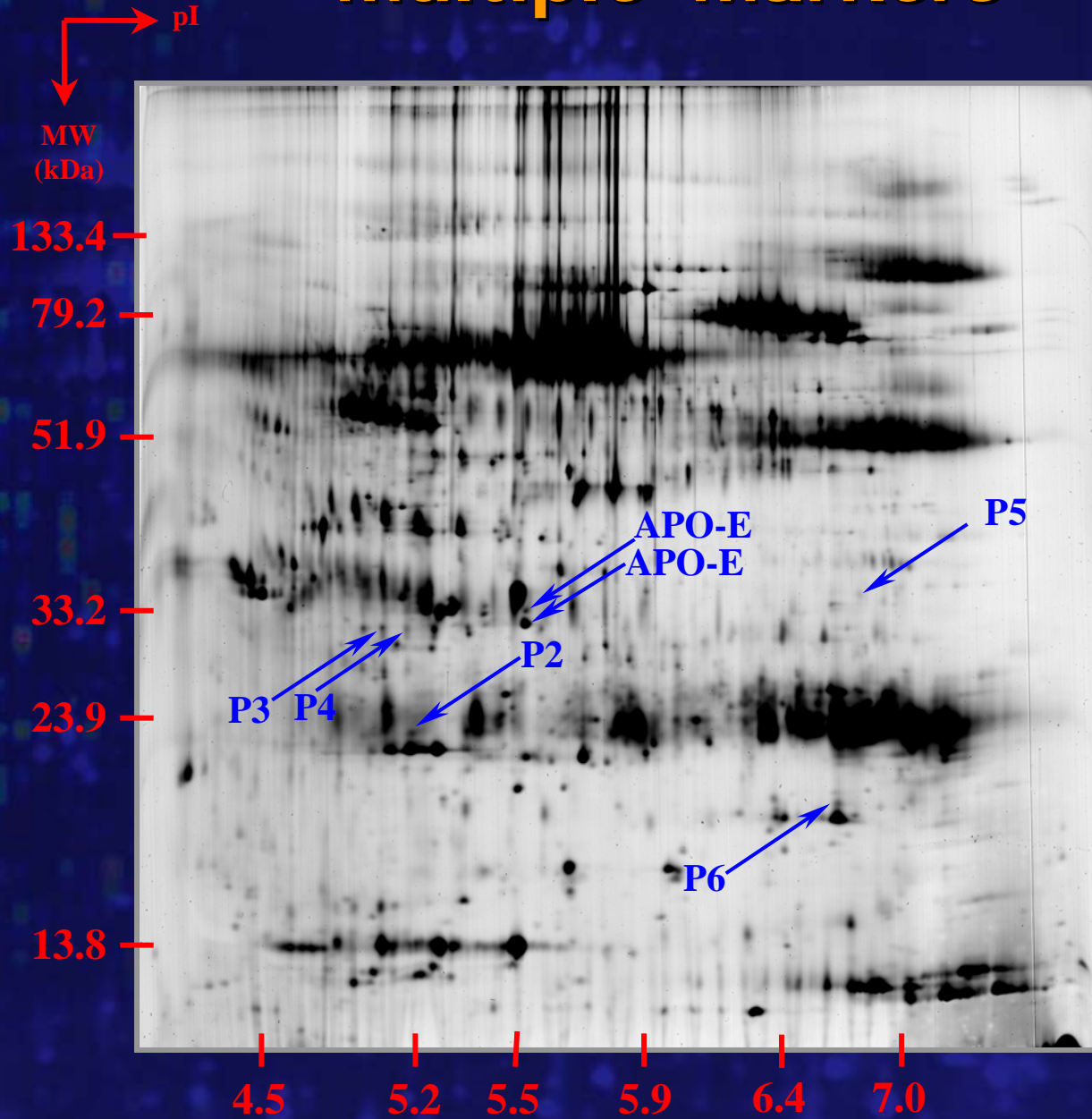
1D - Animal

Overall Sensitivity 90 % (36/40)

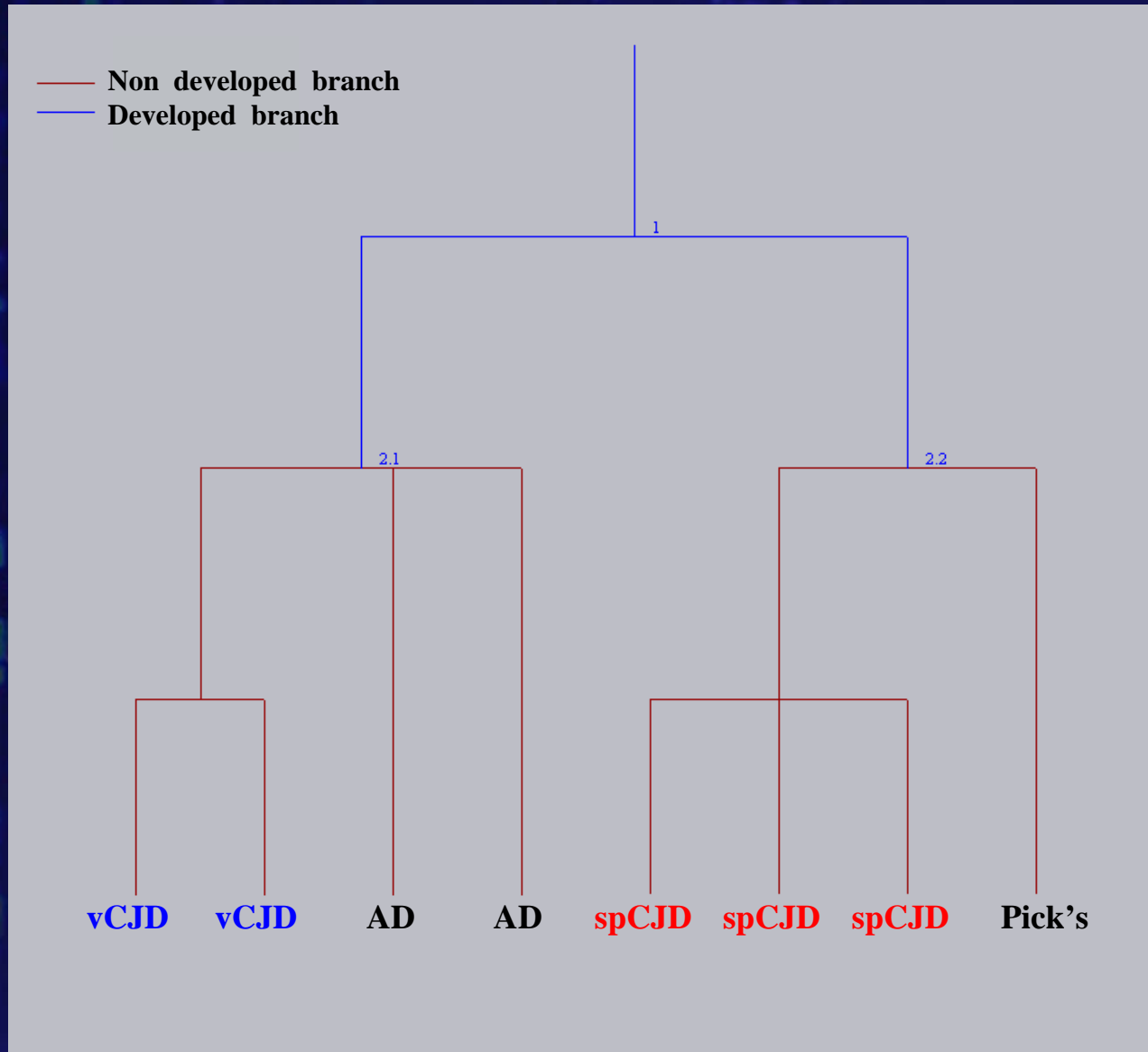
Overall Specificity 98 % (98/100)

vCJD
VS
spCJD
VS
other

Multiple Markers



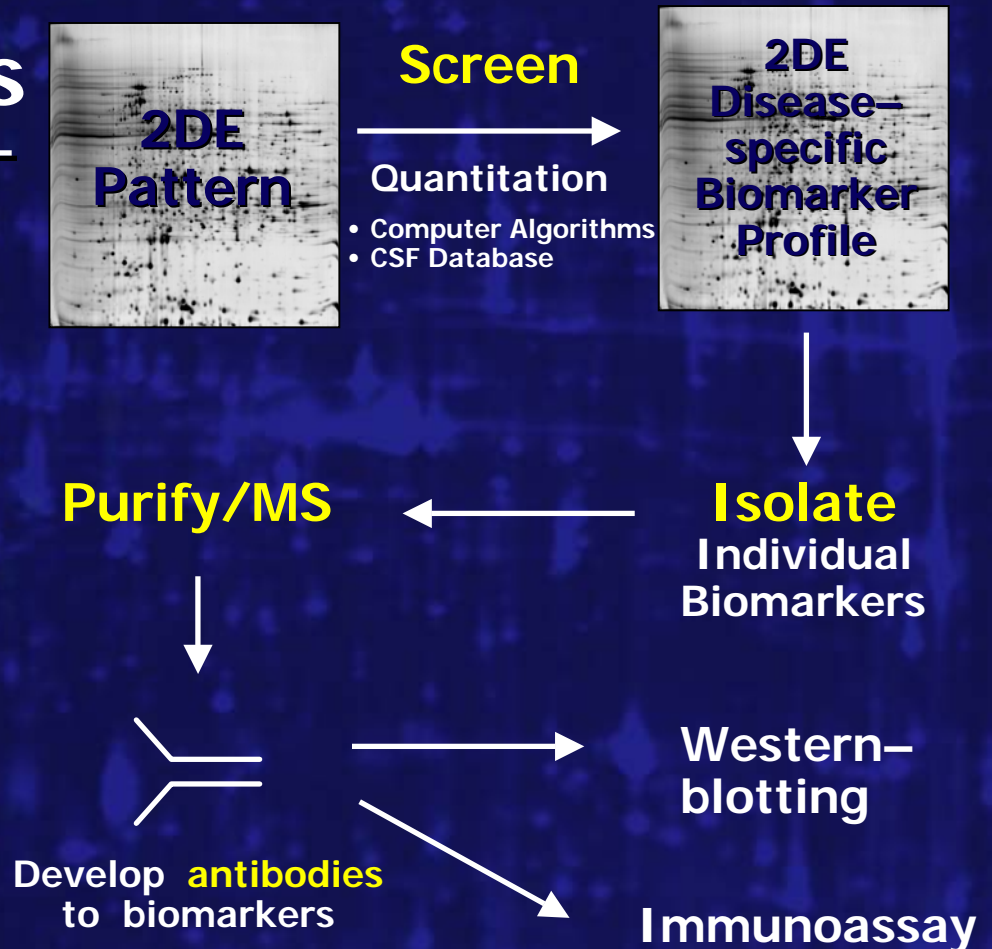
Heuristic Clustering – Class Level 2



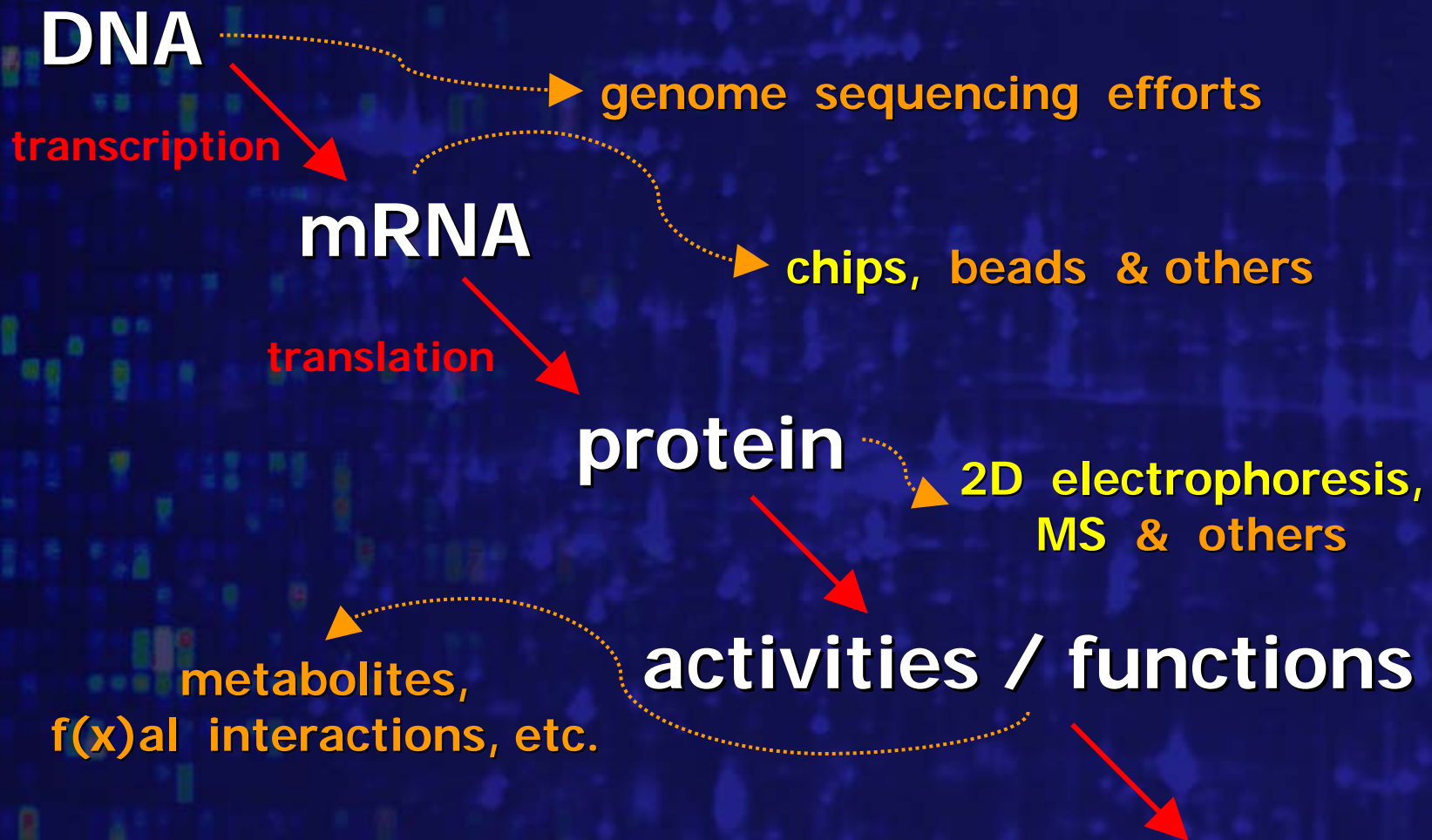
Developing Disease Bar Codes

Biomarker Profiles

Multiple sclerosis
Schizophrenia
Parkinson's disease
Alzheimer's disease
CJD (BSE in cattle,
scrapie in sheep)
Animal diseases



The "Central Dogma" (?)

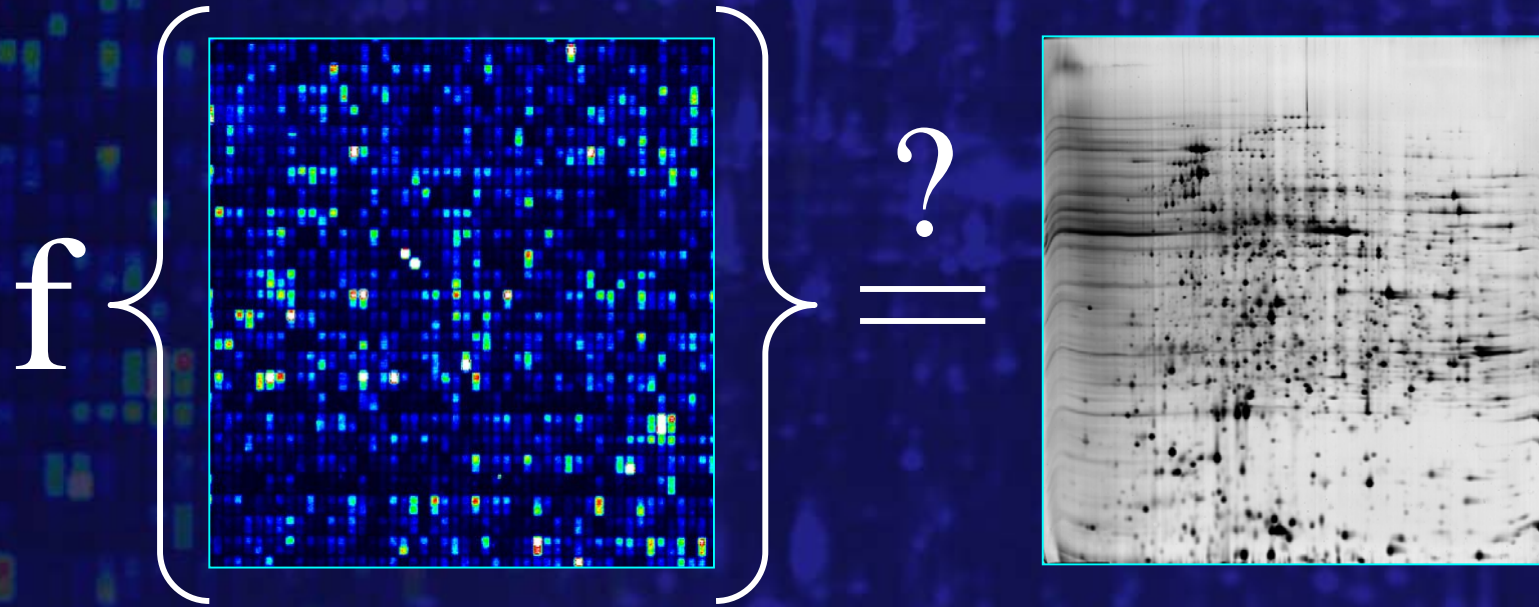


The machine does not isolate us from the great problems of nature but plunges us more deeply into them.

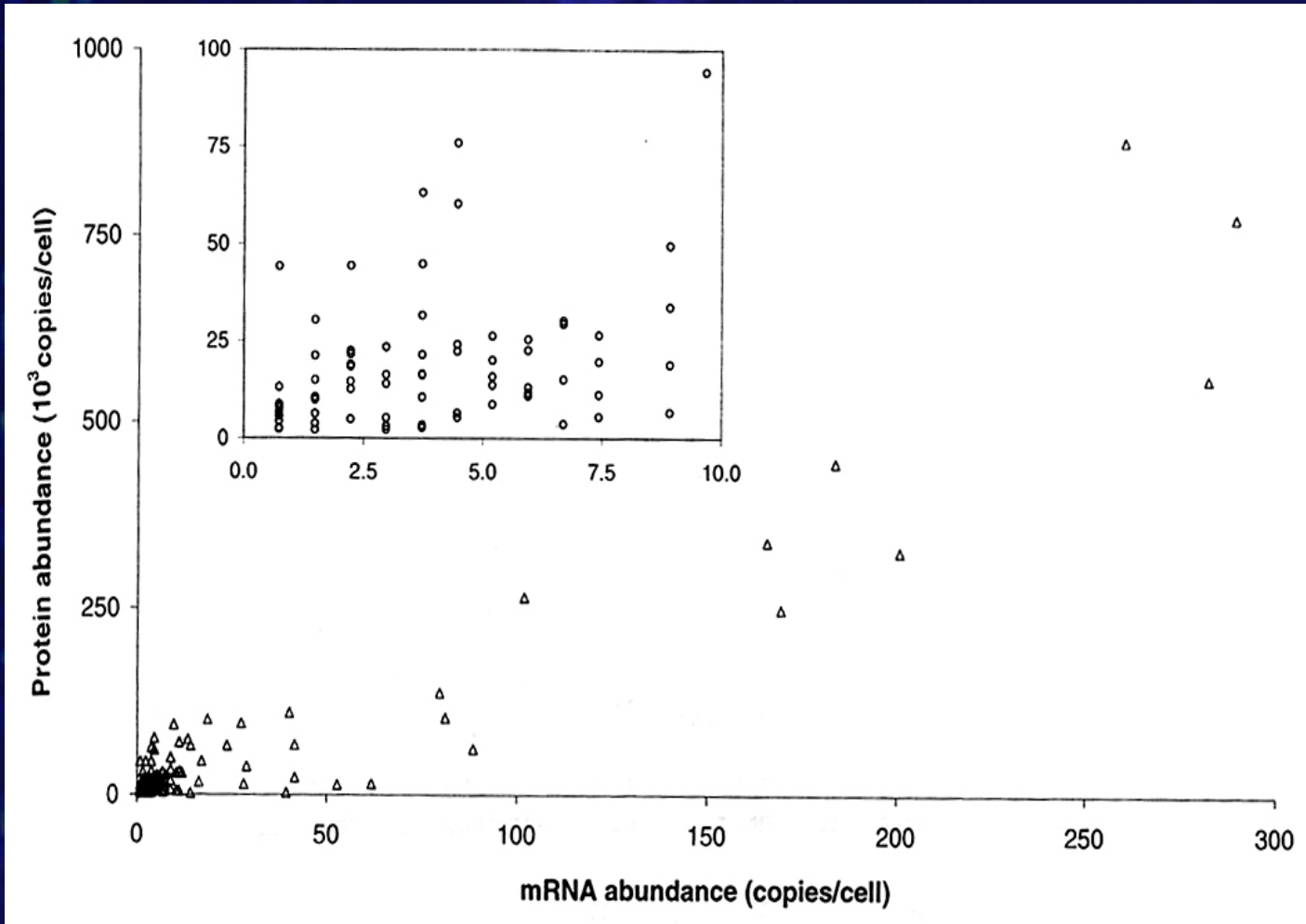
The Wind, Sand and Stars, Antoine de Saint-Exupéry, 1939

A second story

Chip to Gel Mapping



Yeast



Gygi *et al* 1999

$$f_j^m \equiv \frac{M_{T,j}}{M_{T,j,0}} \stackrel{?}{\approx} f_j^p \equiv \frac{P_j}{P_{j,0}}$$

"mRNA amplification factor"

"protein amplification factor"

If mRNA for gene X increases 2-fold when the system is perturbed, how much does the protein for gene X increase by?

SOLVING THE SYSTEM : A KEY RESULT

effective ribosome binding constant

$$f_i^p = \frac{Mr_o + r_o \cdot \tilde{k}_i \cdot Qs_o}{r_o} \cdot \left(\frac{r}{\frac{Mr_o}{f^{R_T}} + r \cdot \tilde{k}_i \cdot Qs_o} \right) \cdot f_i^m$$

free ribosomes

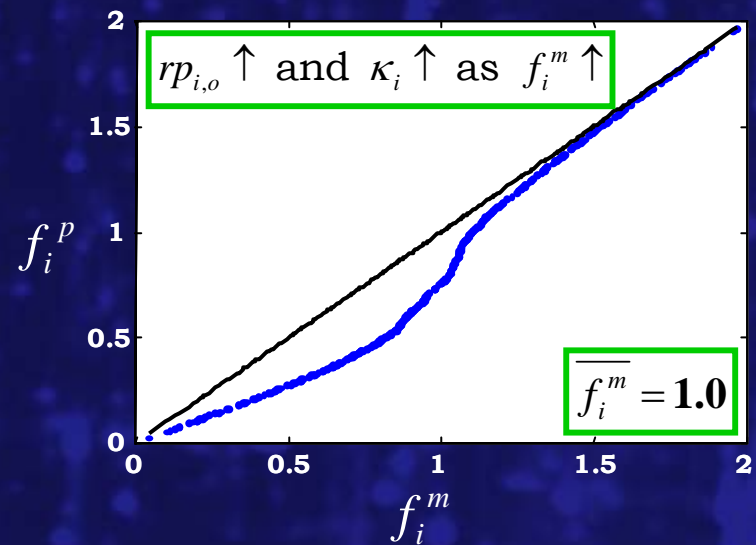
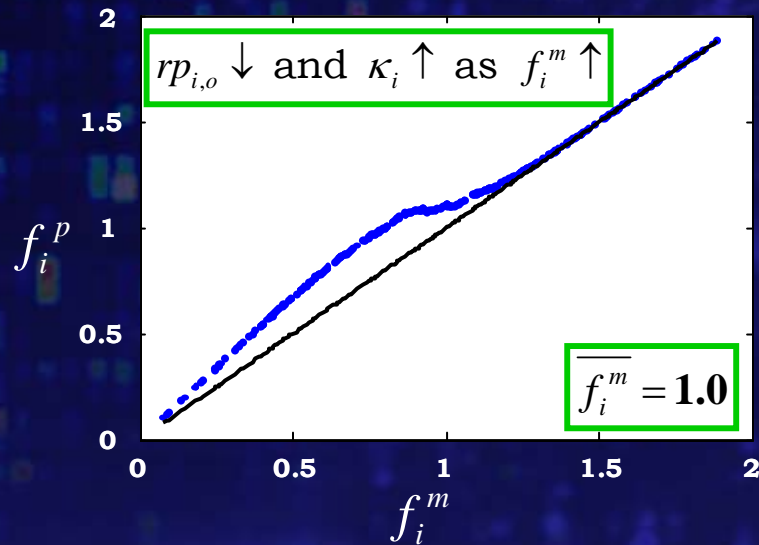
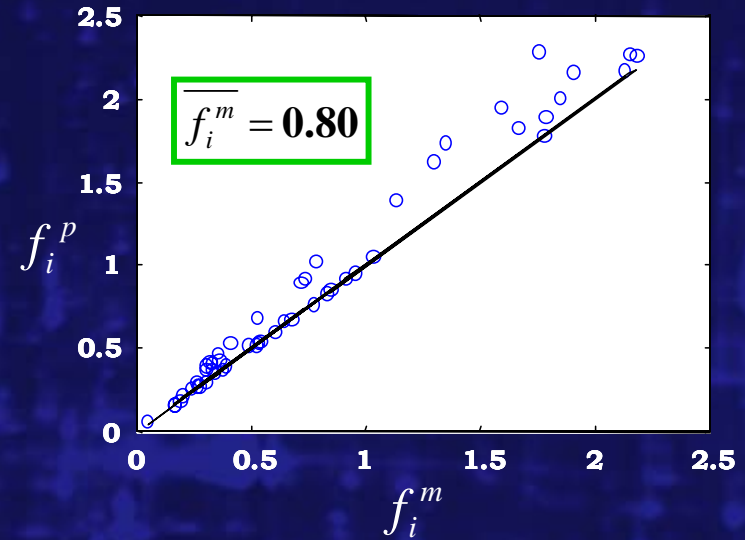
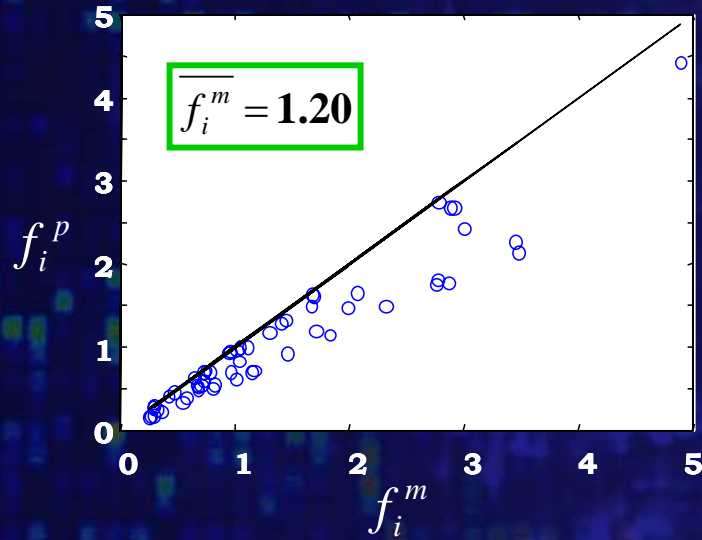
protein amplification factor

mRNA amplification factor

where $f^{R_T} \equiv \frac{R_T}{R_{T,0}}$ ratio of total # ribosomes

COMPUTATIONAL STUDIES

$\overline{f_i^m}$ total mRNA in the cell



Experimental Results - *E. coli*

- Induction of parallel cultures with 0, 0.1, 1.0 mM IPTG.
- Comparison of Hly super-secreting mutant vs controls.
- Studies on the effect of Fis expression level.
- mRNA analysis by Affymetrix Genechips - 3 metrics.
- Protein measurements by 2DE/MS & ICAT - 4 metrics.
- Biological Replicates

uxaC - uronate isomerase
present

yghQ - hypo. protein
present

perf. match
mismatch

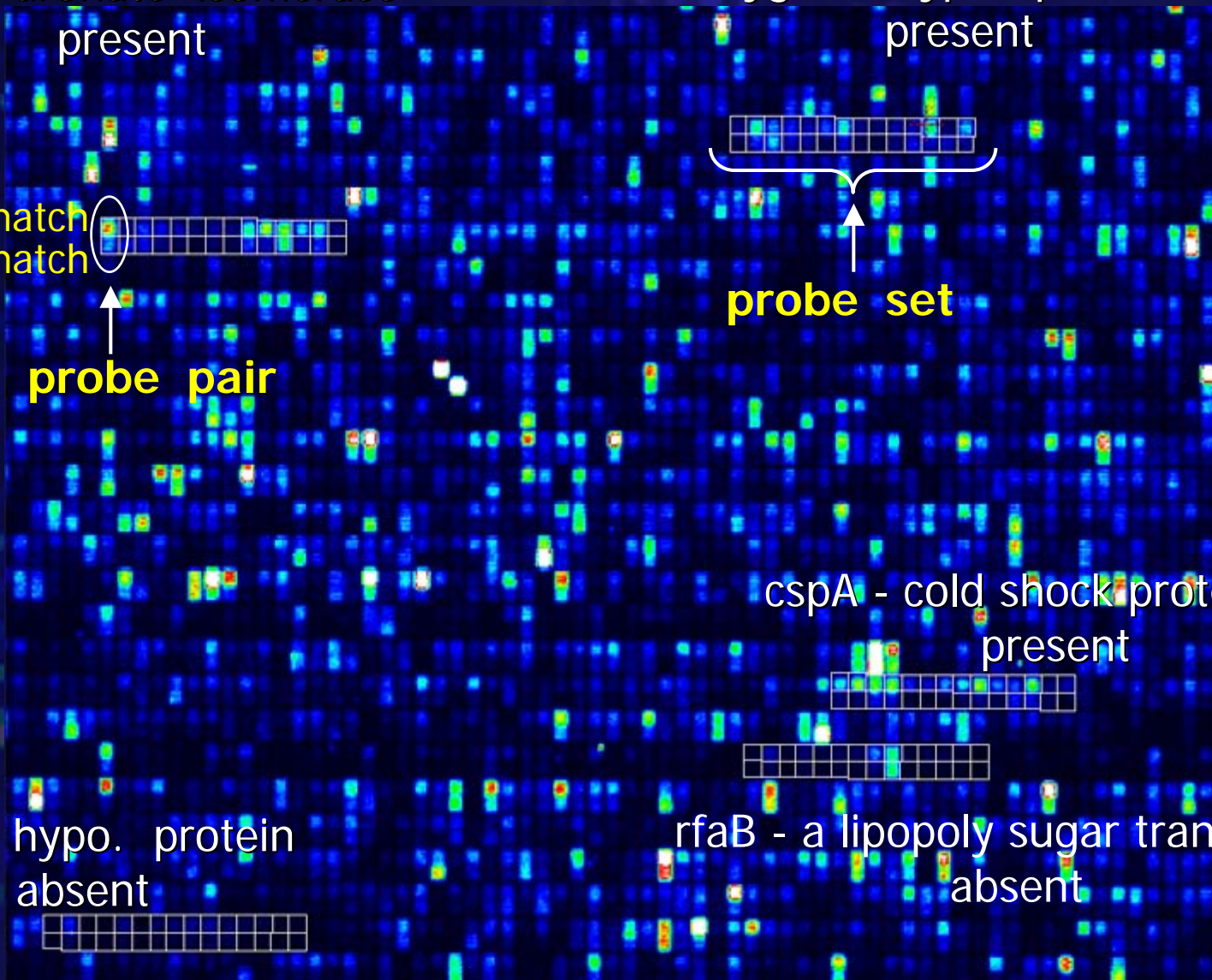
probe pair

probe set

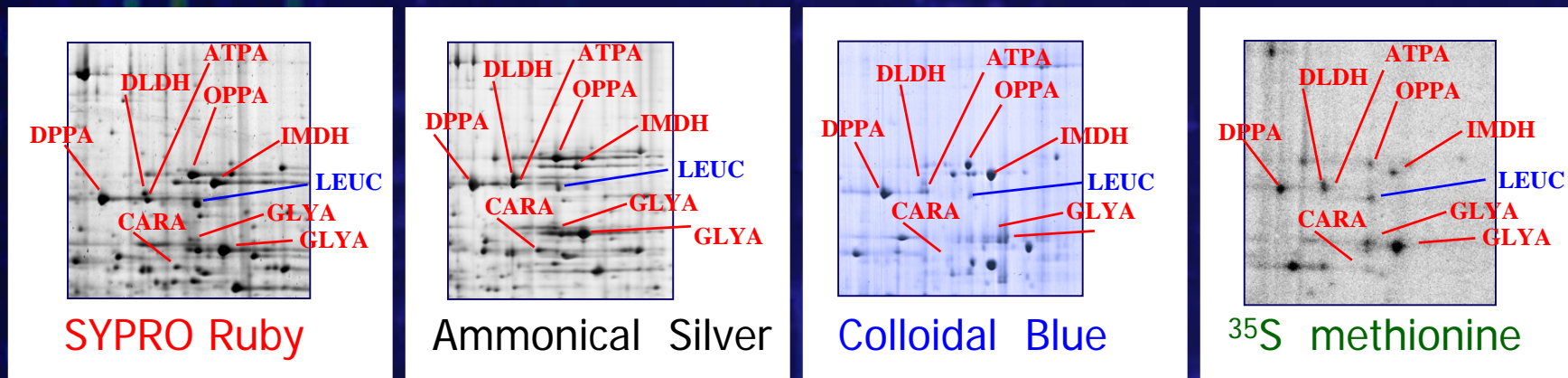
cspA - cold shock protein 7.4
present

yig F - hypo. protein
absent

rfaB - a lipopoly sugar transferase
absent



leuC (P30127; B0072)



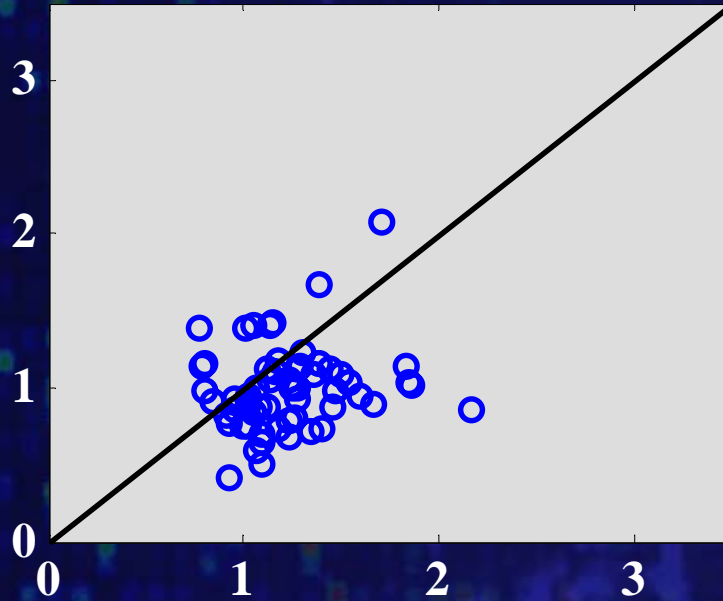
Fold change (f_p)	(low)	(high)
Ruby (%vol)	1.14	0.88
Silver (%vol)	1.99	1.75
Blue (%vol)	0.97	0.58
S35 (vol/stds)	0.76	0.35

leuC protein is downregulated (~25% for the culture) for shift from 0 mM IPTG to 0.1 mM IPTG to 1.0 mM IPTG.

$f_p \uparrow$
 $f_m \rightarrow$

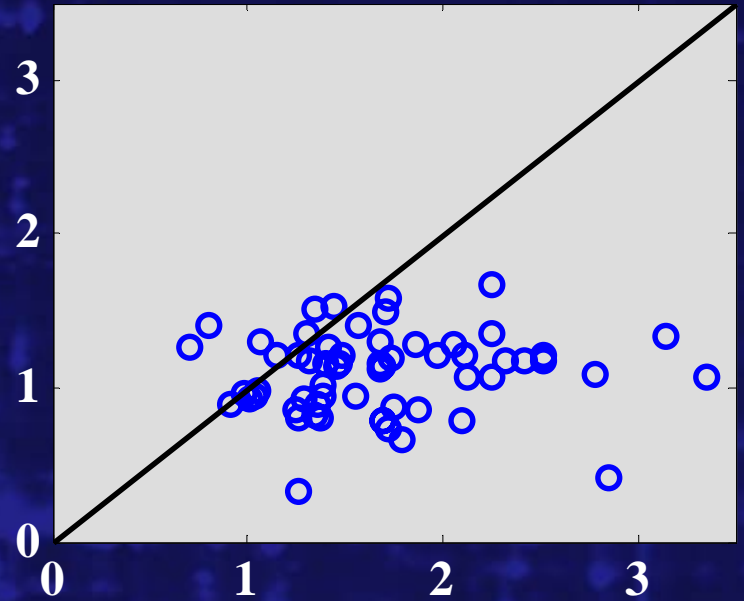
shift from 0 mM to 0.1 mM IPTG

expt



X: mRNA_i 0.1 / mRNA_i 0.0
Y: prot_i 0.1 / prot_i 0.0

shift from 0 mM to 1 mM IPTG



X: mRNA_i 1.0 / mRNA_i 0.0
Y: prot_i 1.0 / prot_i 0.0

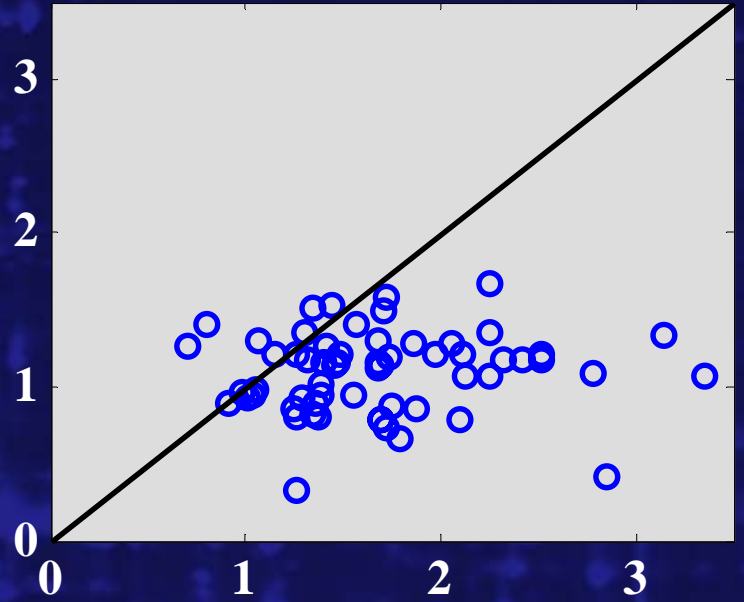
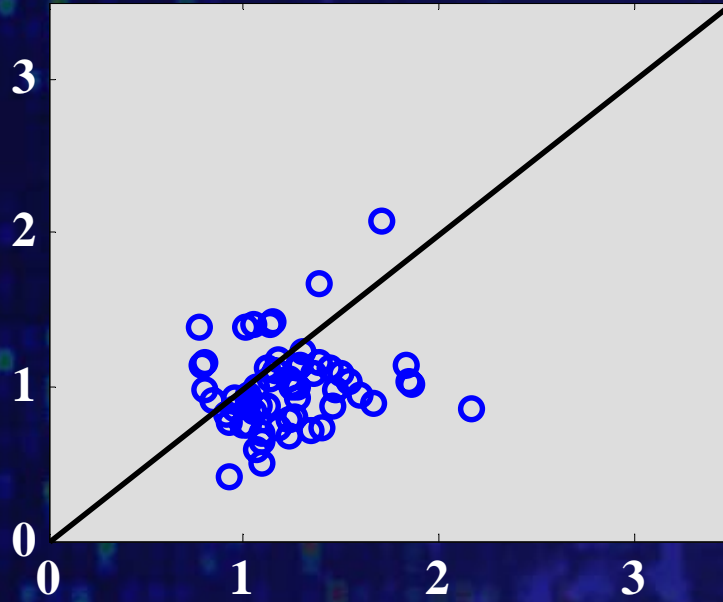
Relationship clearly nonlinear.

$f_p \uparrow$
 $f_m \rightarrow$

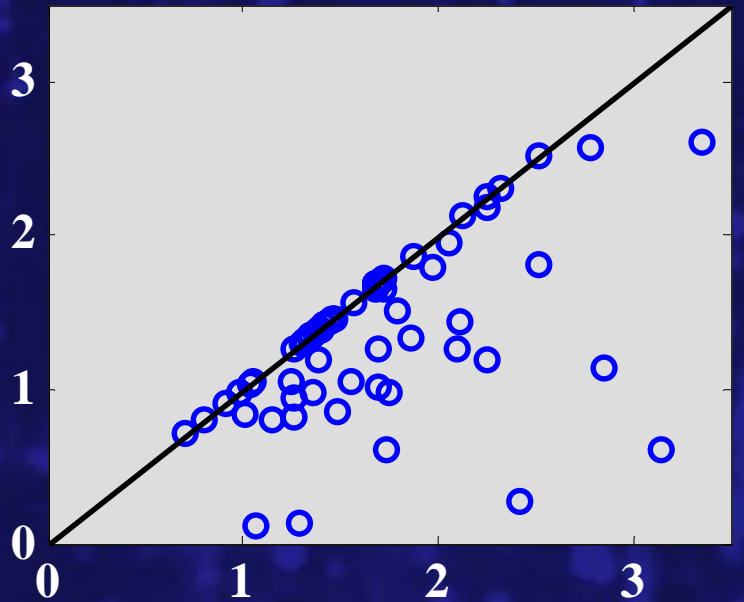
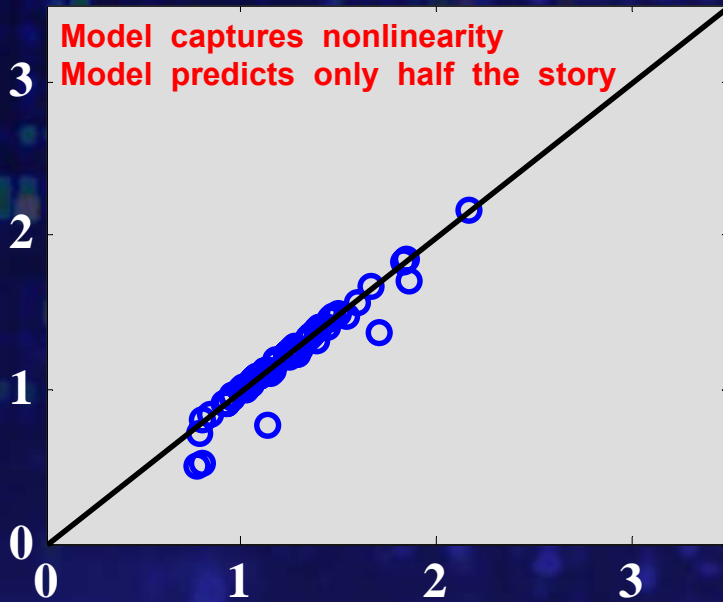
shift from 0 mM to 0.1 mM IPTG

shift from 0 mM to 1 mM IPTG

expt



model



$$\bar{f}_i^m < 1 \Rightarrow r > r_0 \Rightarrow f_i^p > f_i^m$$

$$\bar{f}_i^m > 1 \Rightarrow r < r_0 \Rightarrow f_i^p < f_i^m$$

A perturbation (0.1 to 1) could lead to, e.g., increased \bar{f}_i^m which model suggests by scaling arguments should result in a shift in the data further below the 1 to 1 line.

Scaling arguments suggest that if the total mRNA in the cell increases, then the ratio of any reasonable subset of observed data should reflect fewer proteins than mRNA - data migrates further below 1:1 line.

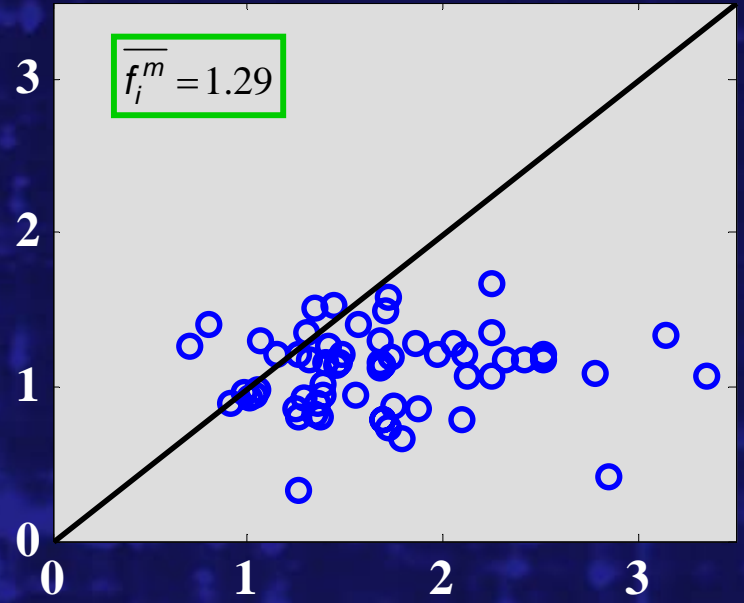
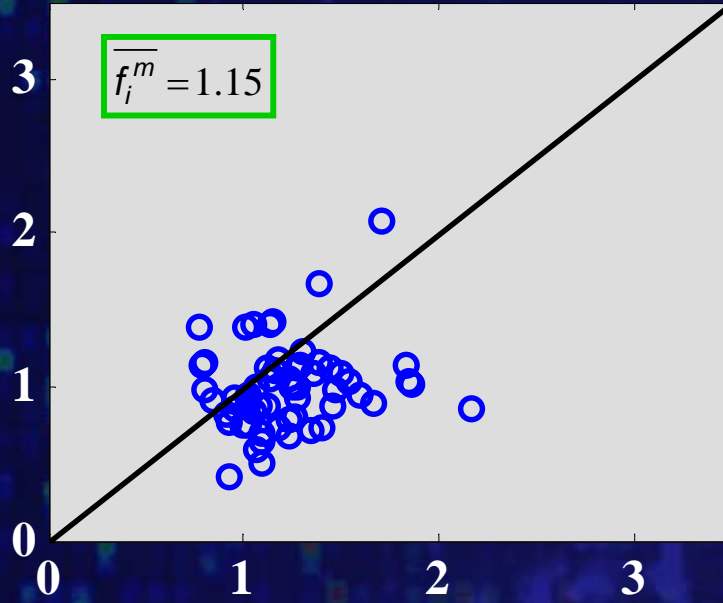
(Free ribosome availability becomes limiting).

$f_p \uparrow$
 $f_m \rightarrow$

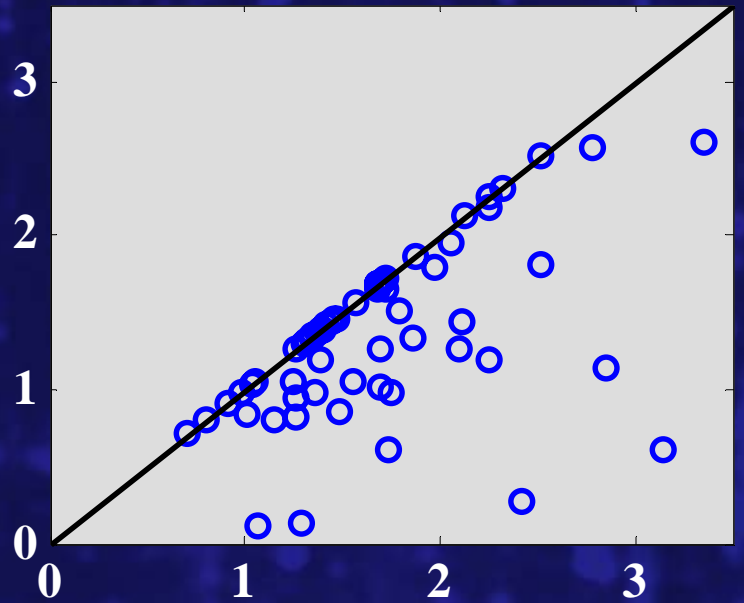
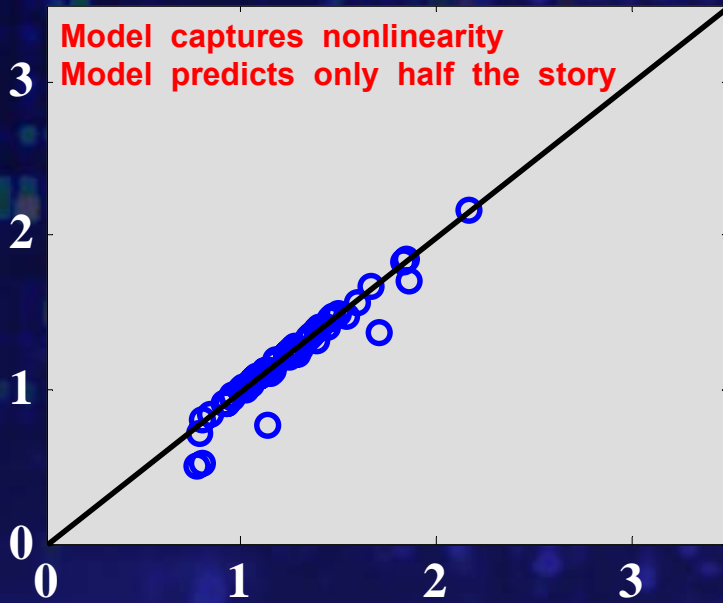
shift from 0 mM to 0.1 mM IPTG

shift from 0 mM to 1 mM IPTG

expt



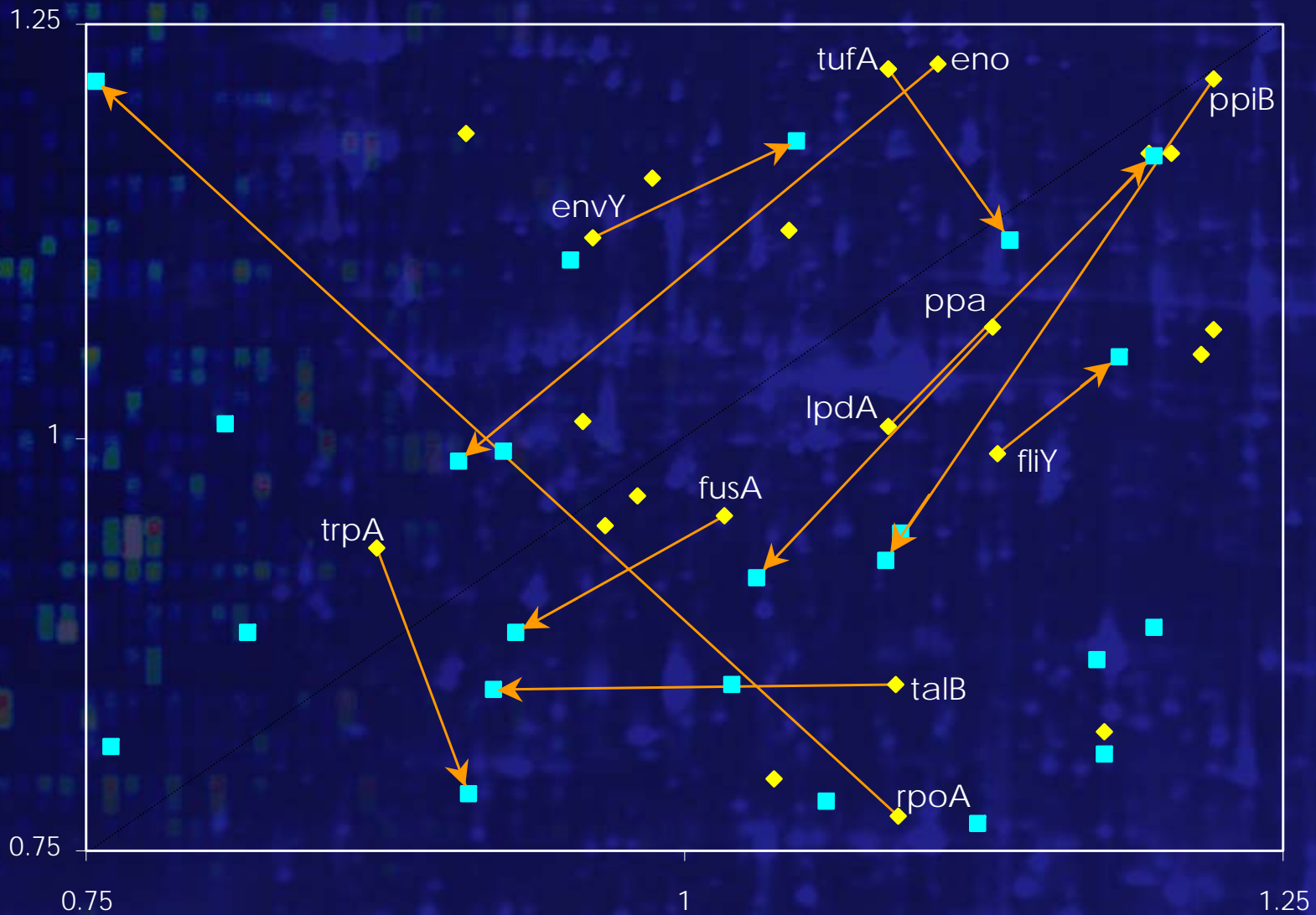
model



- The framework captures qualitatively the shift in the $f_p : f_m$ relationship when $\overline{f_i^m}$ increases.
- Can the framework be used to predict changes in gene expression for individual genes ?

Use the experimental data to identify the effective ribosome binding constants that capture the relative responses of the $f_p : f_m$ relationship in the experiments.

As culture conditions change (0.1mM/0mM to 1mM/0mM),
the relative fp:fm ratio will shift.
Can the framework predict this shift for individual genes?



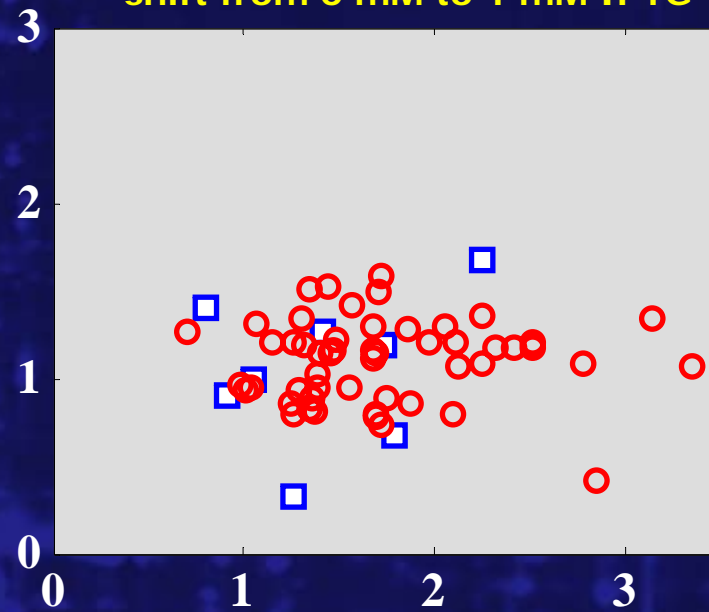
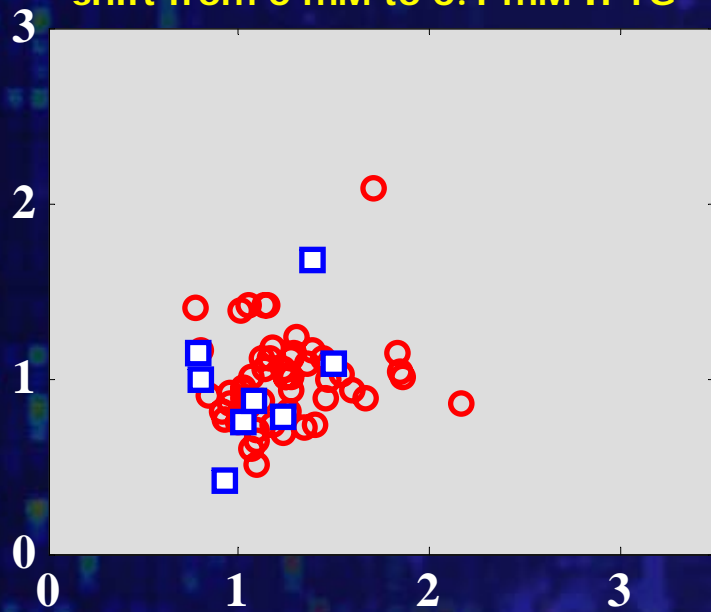
$f_p \uparrow$
 $f_m \rightarrow$

52 of 60 (87%) observed genes agree

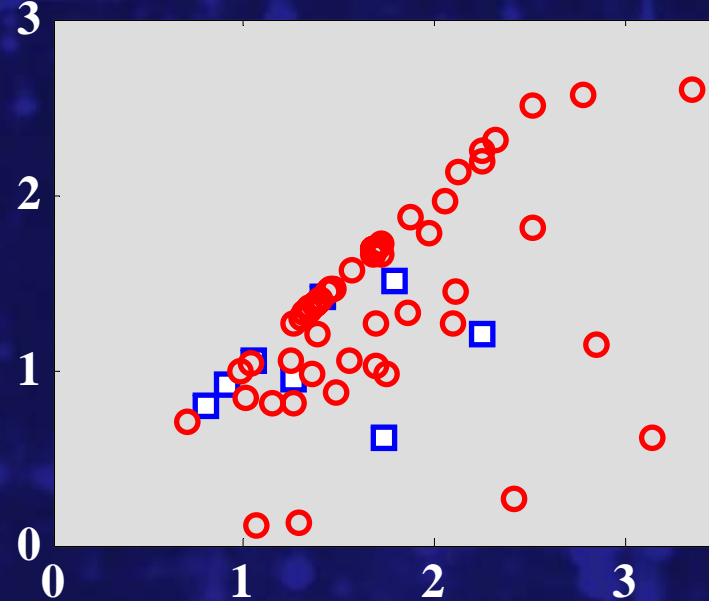
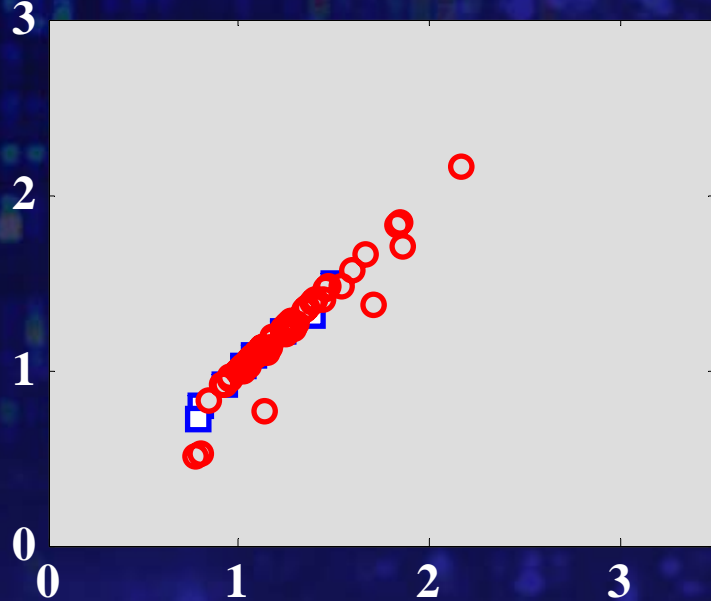
shift from 0 mM to 0.1 mM IPTG

shift from 0 mM to 1 mM IPTG

expt

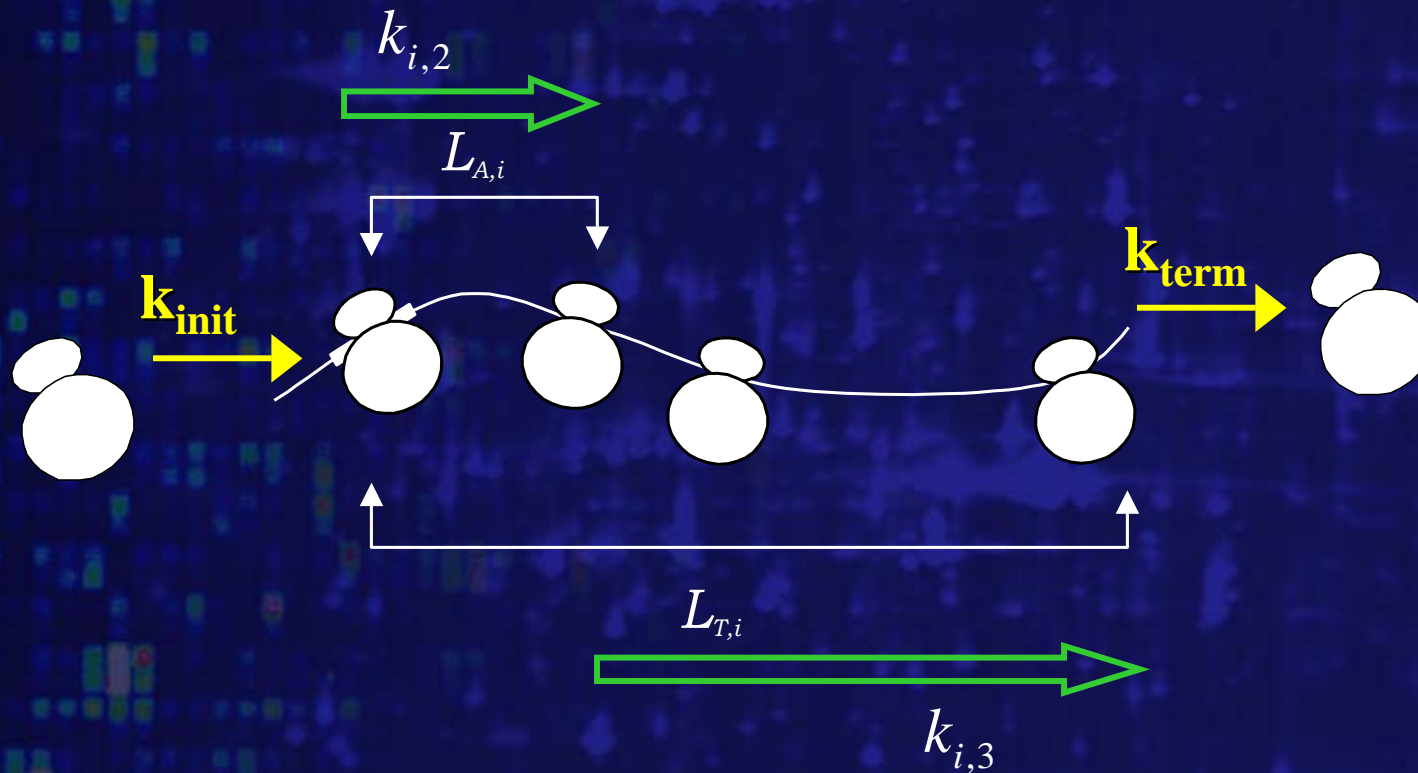


model



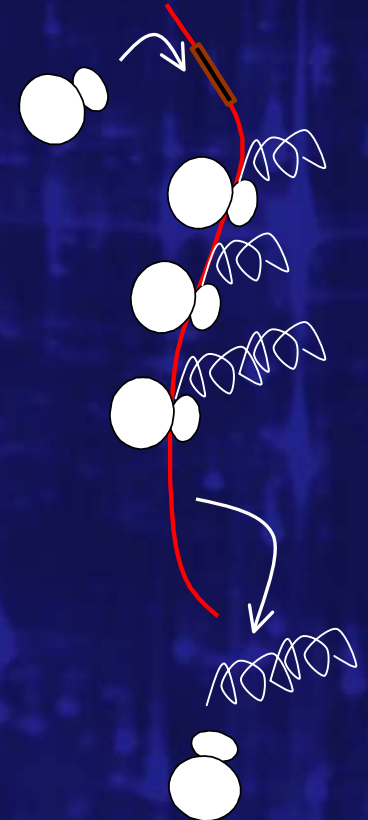
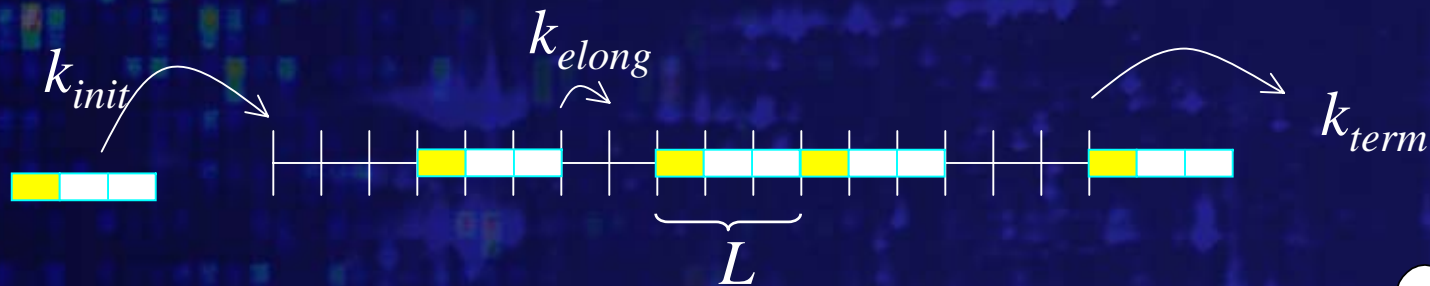
We just saw impact of ribosome competition and binding constants.

Translation Depends on the Codon Usage



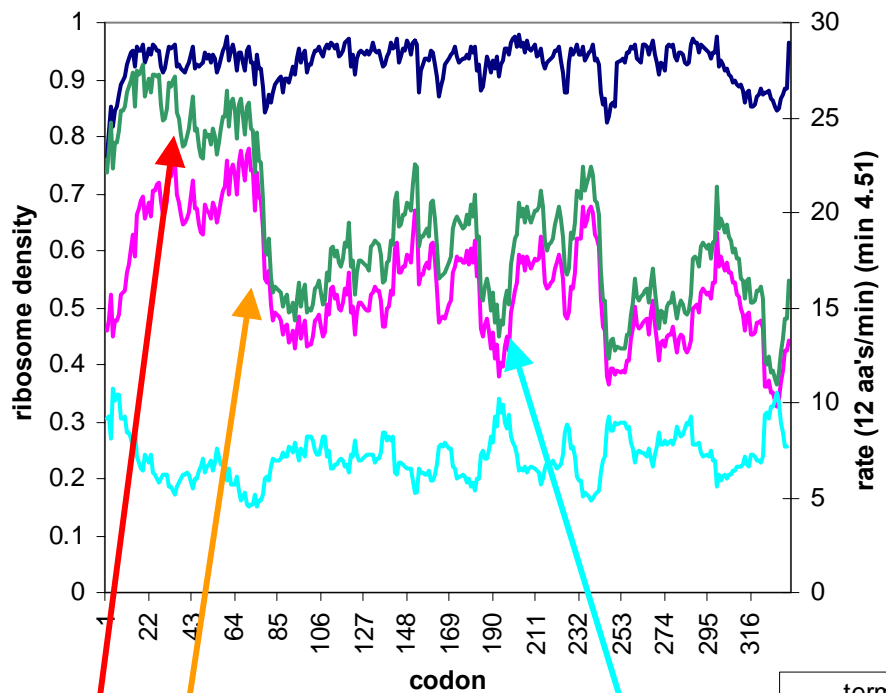
We know sequence / codon usage, [aa-tRNA].
Assume 100 copies compete for 4500 ribosomes.
Continuous time Monte Carlo simulations ...

Single lattice model

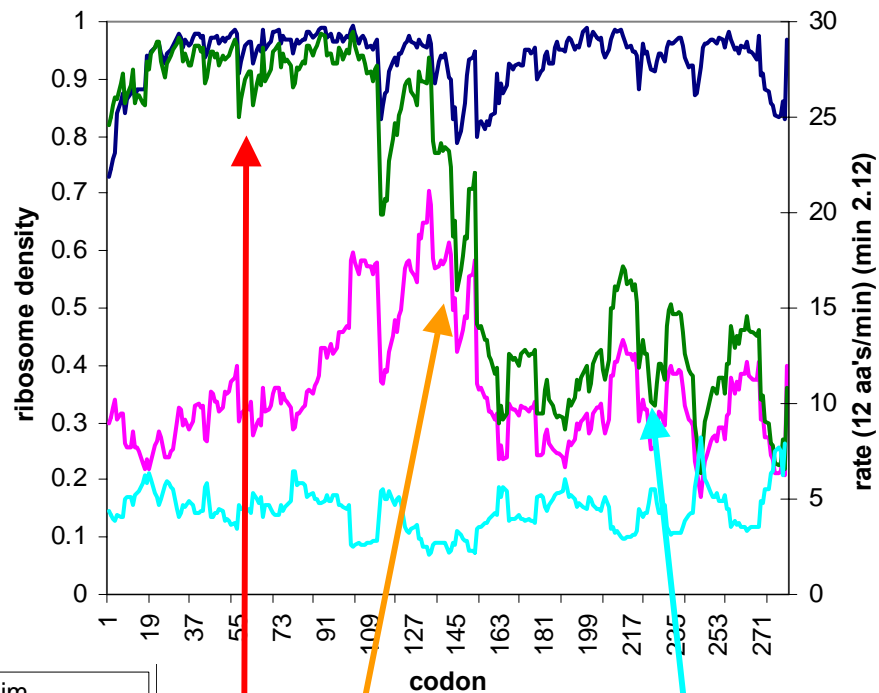


- mRNA modeled as a lattice
- ribosomes have steric hindrance
- parameters
 - ribosome length $L (=12)$
 - Initiation rate $k_{init} = k \times [\text{free ribosomes}]$
 - Elongation rates $k_{elong} = k \times [\text{free aa-tRNA}]$
 - termination rate k_{term}

ompA (abundant), max current 3.52/min



araC (rare), max current 1.59/min



— term lim
— init lim
— elong lim
— rate for 12 codons

Higher density of ribosomes

Fewer ribosomes

A slow site

Higher density

Lower density

A slow site

The mRNA - Protein Relationship Depends on the DNA sequence.

Ribosome binding affinity

Length of message

Ribosome velocity

Codon usage and frequency

mRNA secondary structure