

Quantitative 3D+4D Seismic imaging, inversion and monitoring inside the earth

Prof. David Lumley

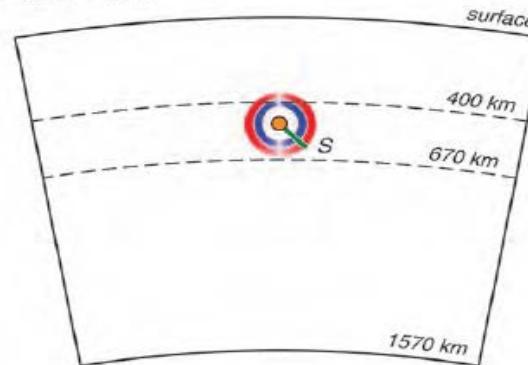
Green Chair in Geophysics, Research Center Director, UT Dallas
Adjunct Professor, Physics & Astrophysics, University of Western Australia



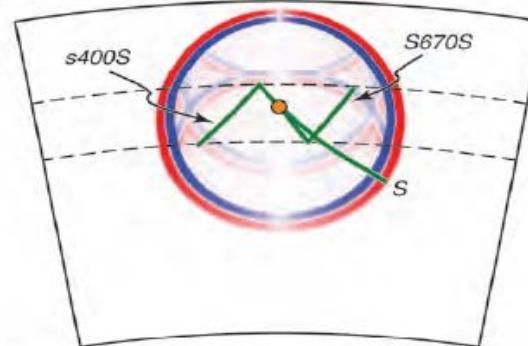
Introduction

Seismology...

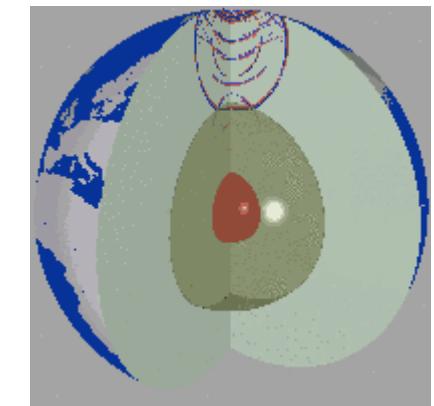
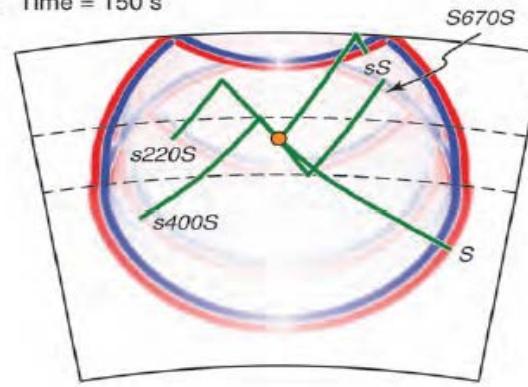
(a) Time = 30 s



(b) Time = 100 s

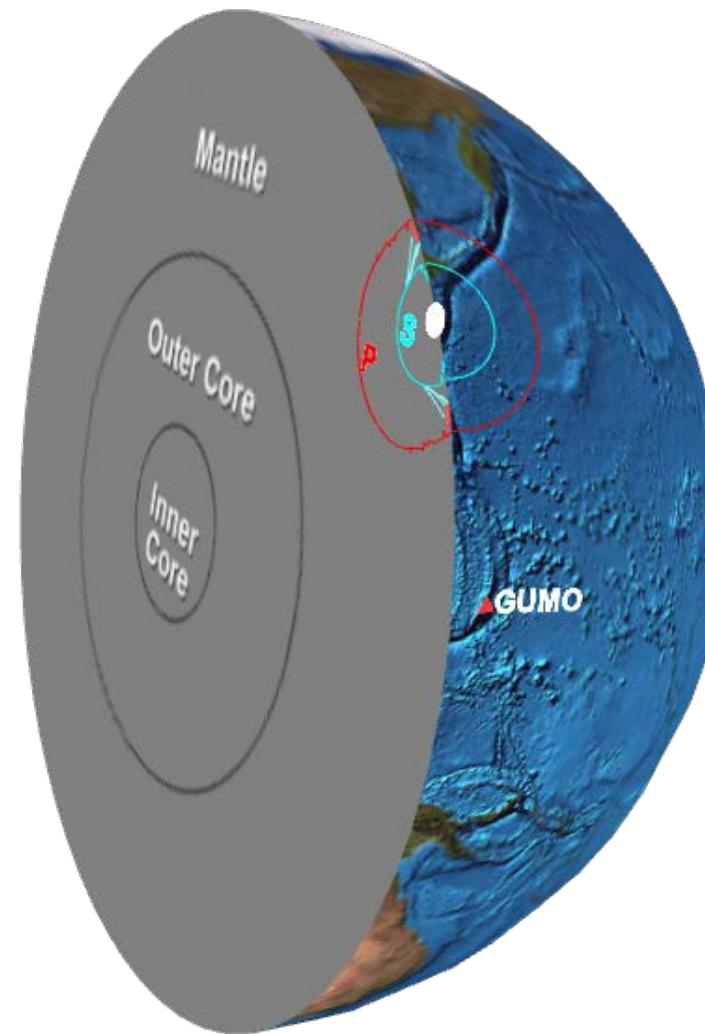


(c) Time = 150 s

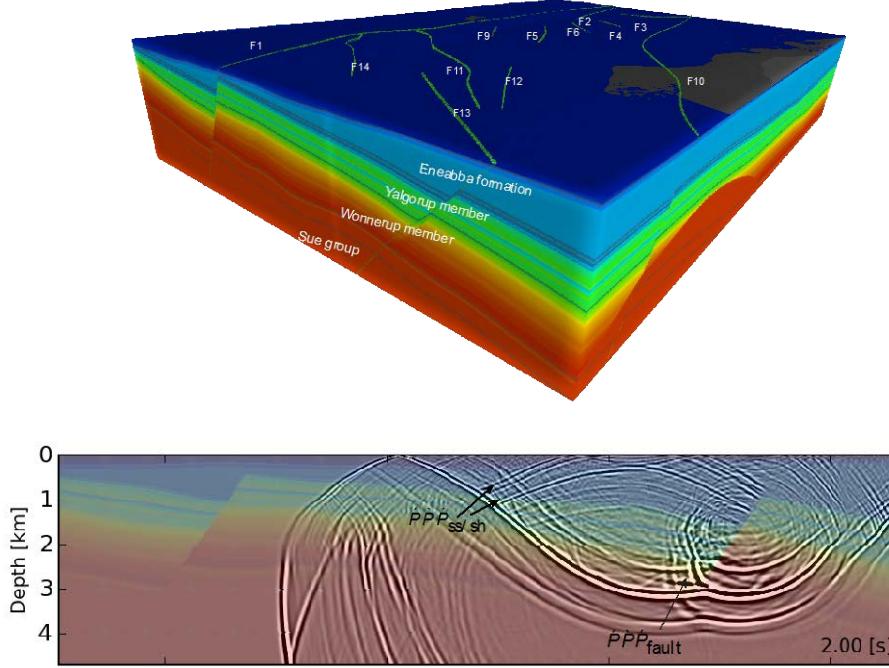


Thorne et al., SRL 2013

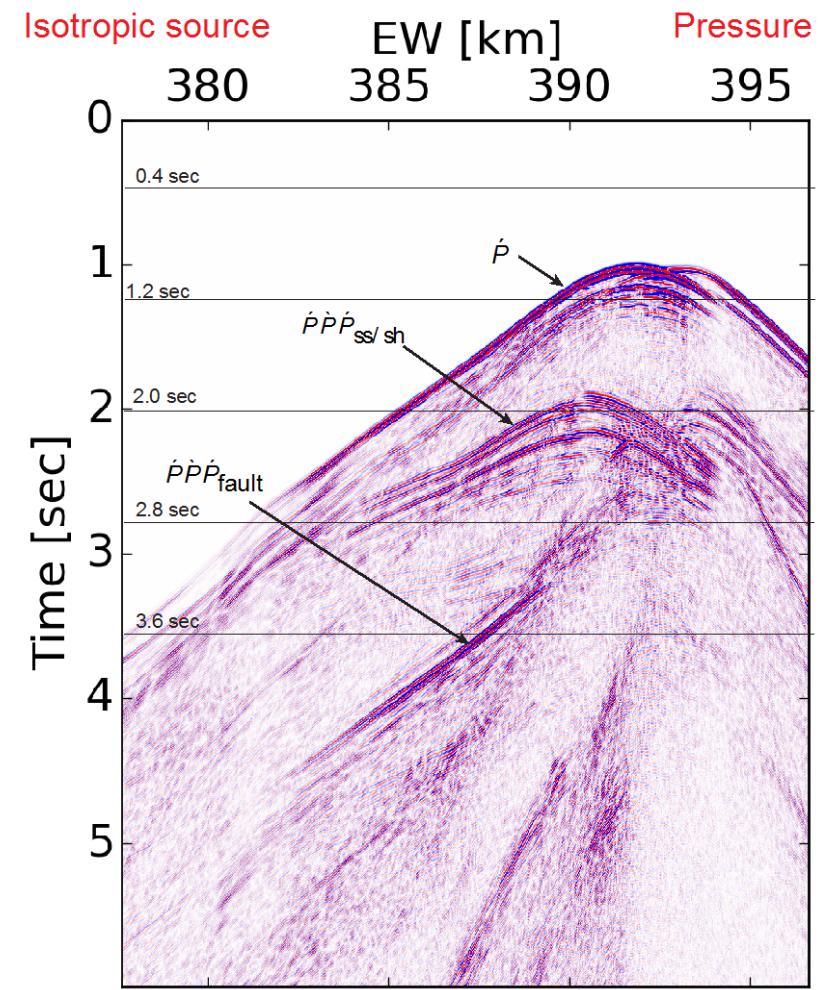
2011 Tohoku earthquake



3D Elastic wavefield modeling...

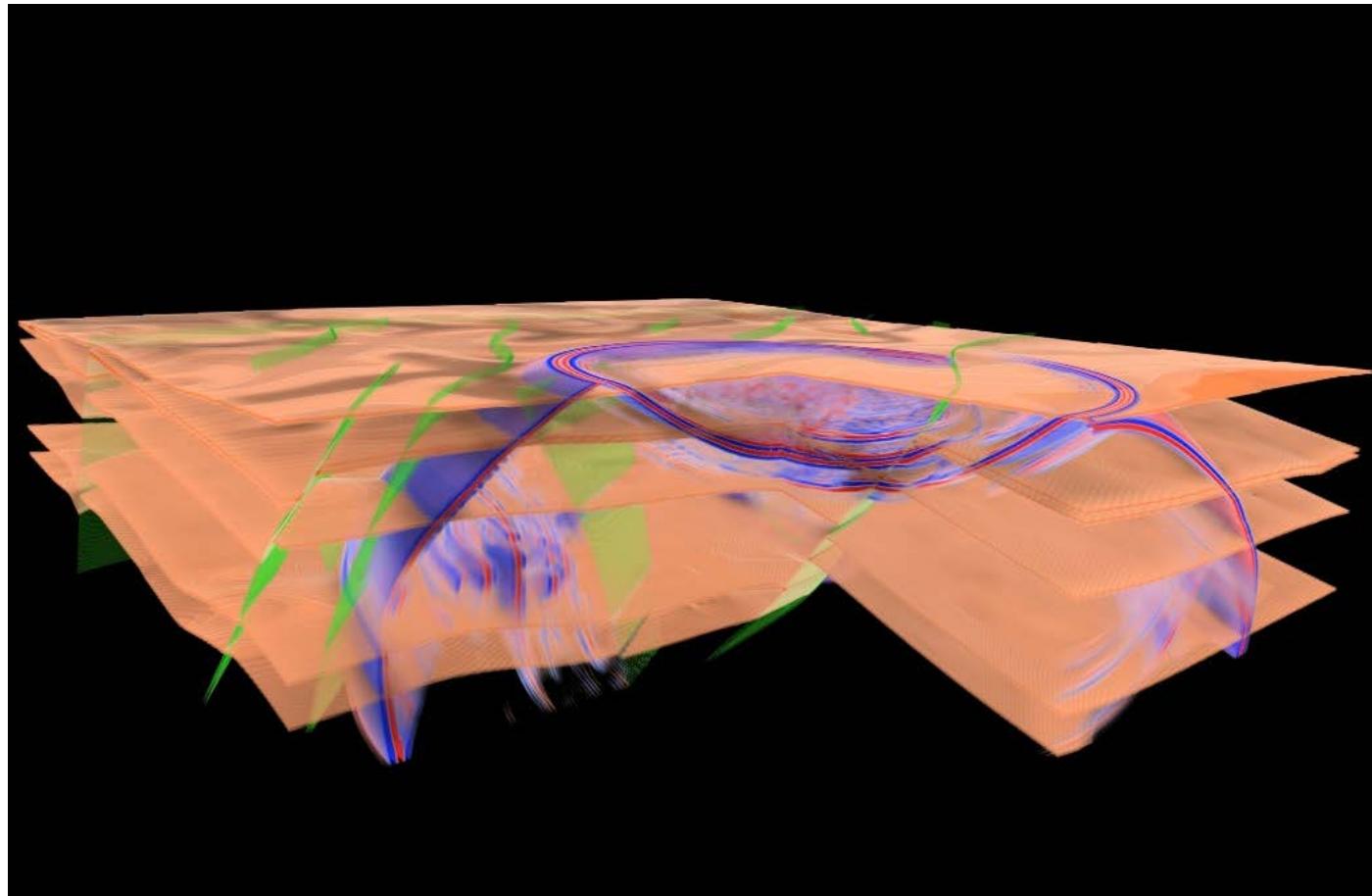


- **Large-scale 3D elastic modelling**
 - >5.2 billion grid points
 - Highly optimized parallel computation



Lumley et al., ANLEC 2016

3D Elastic wavefield modeling...



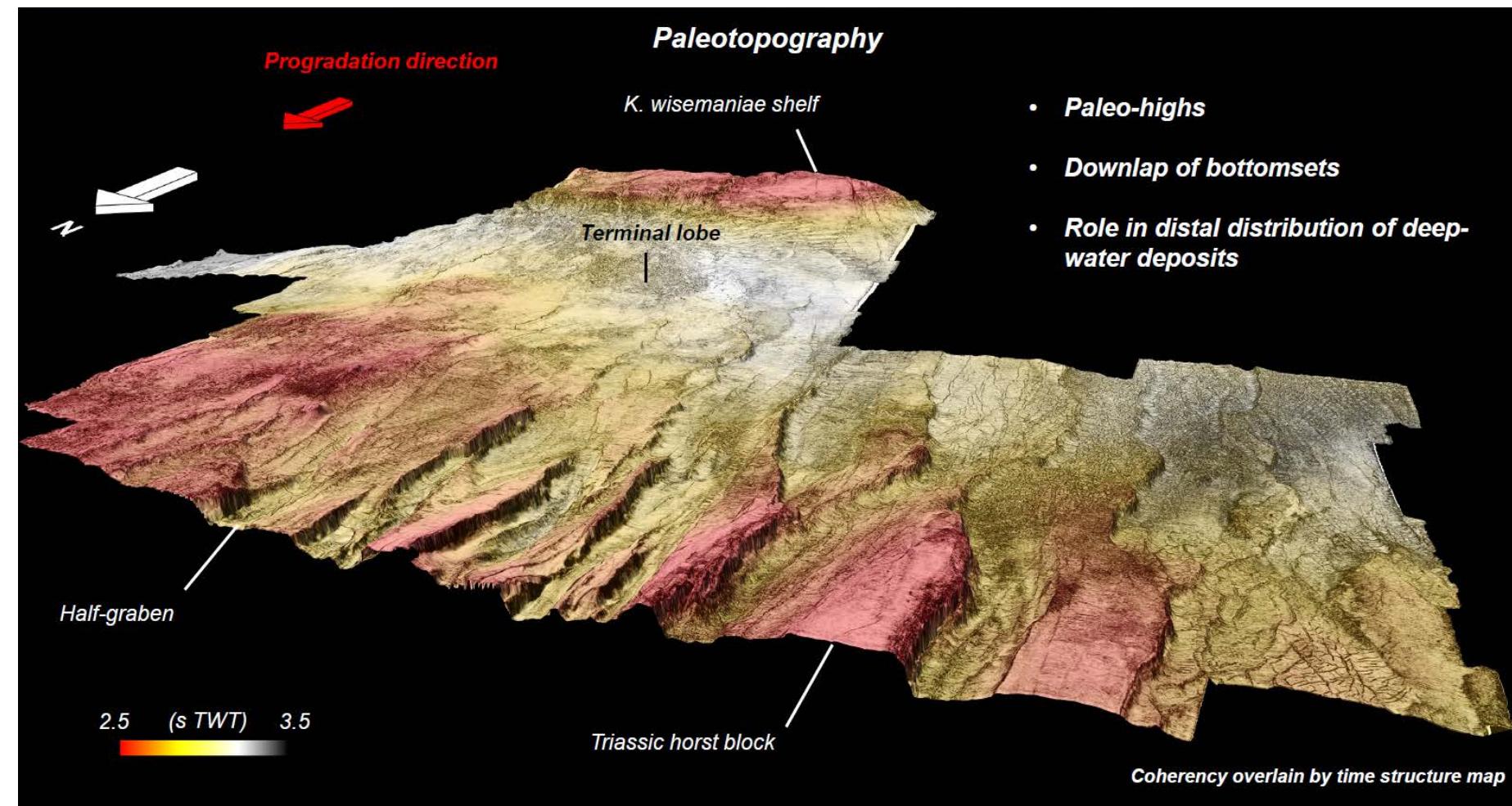
Miyoshi et al., 2016

Imaging... objects + patterns

source, energy, sensors

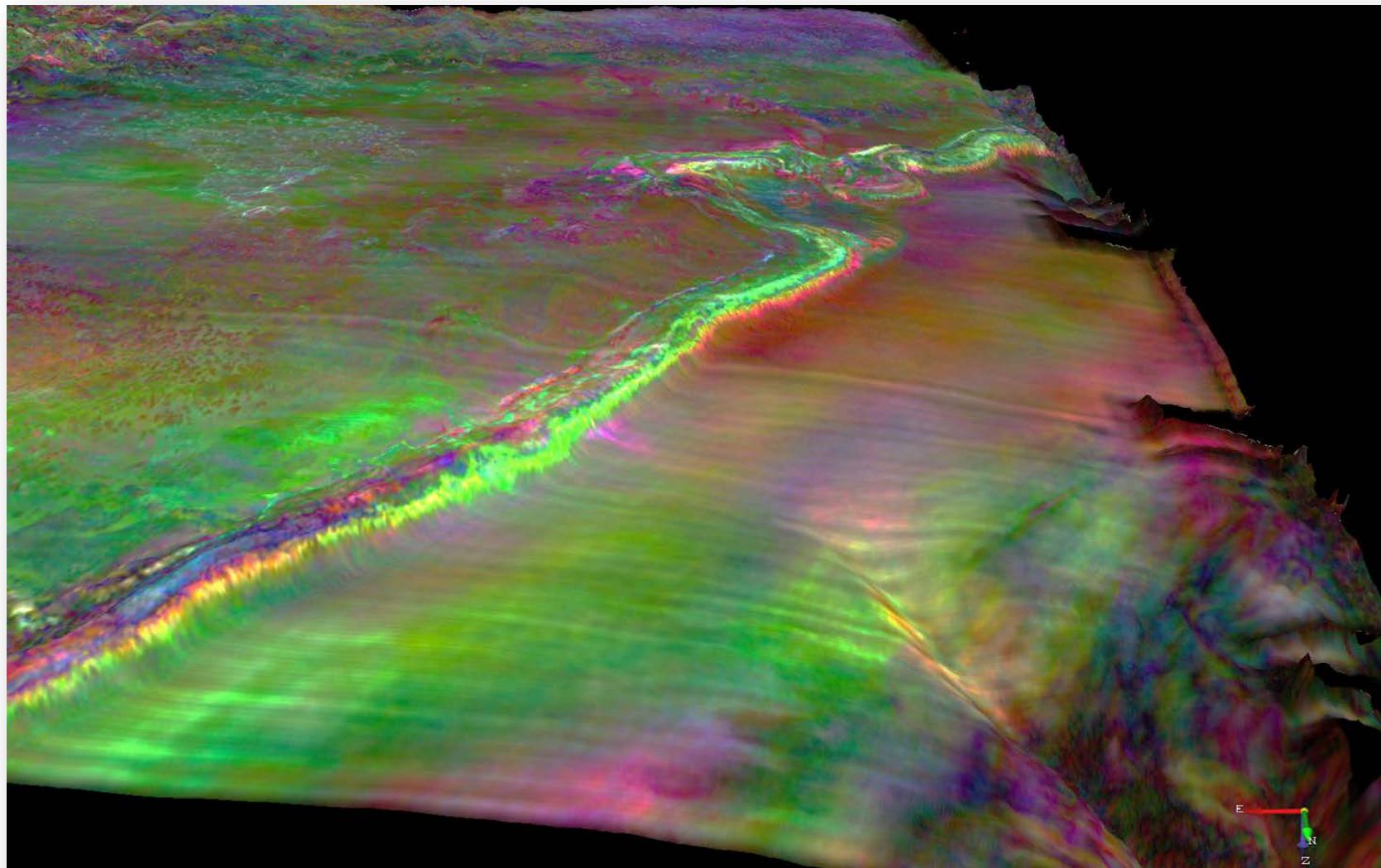


3D Seismic imaging...



Paumard et al., 2015

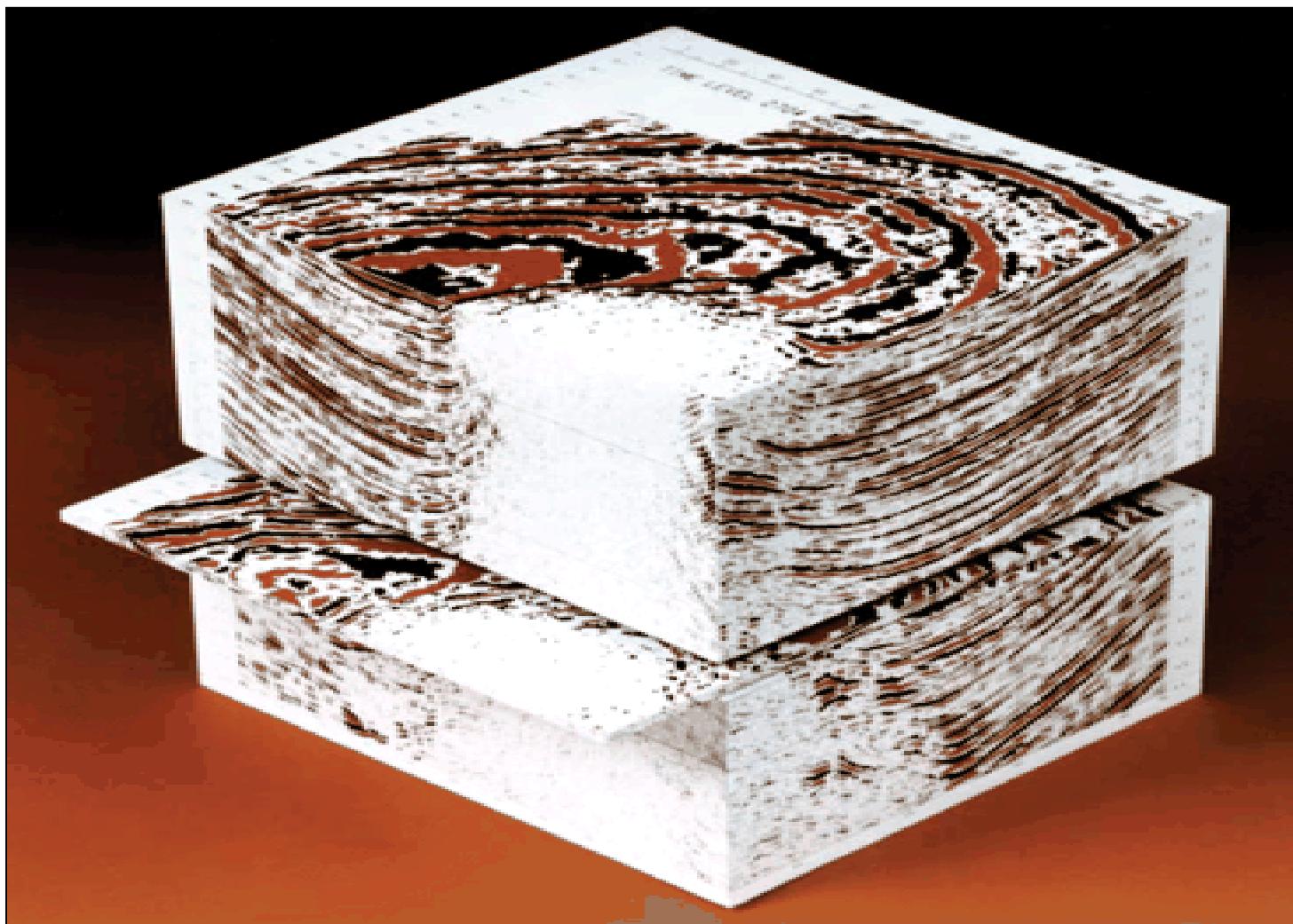
3D Seismic imaging...



Bourget et al., 2014

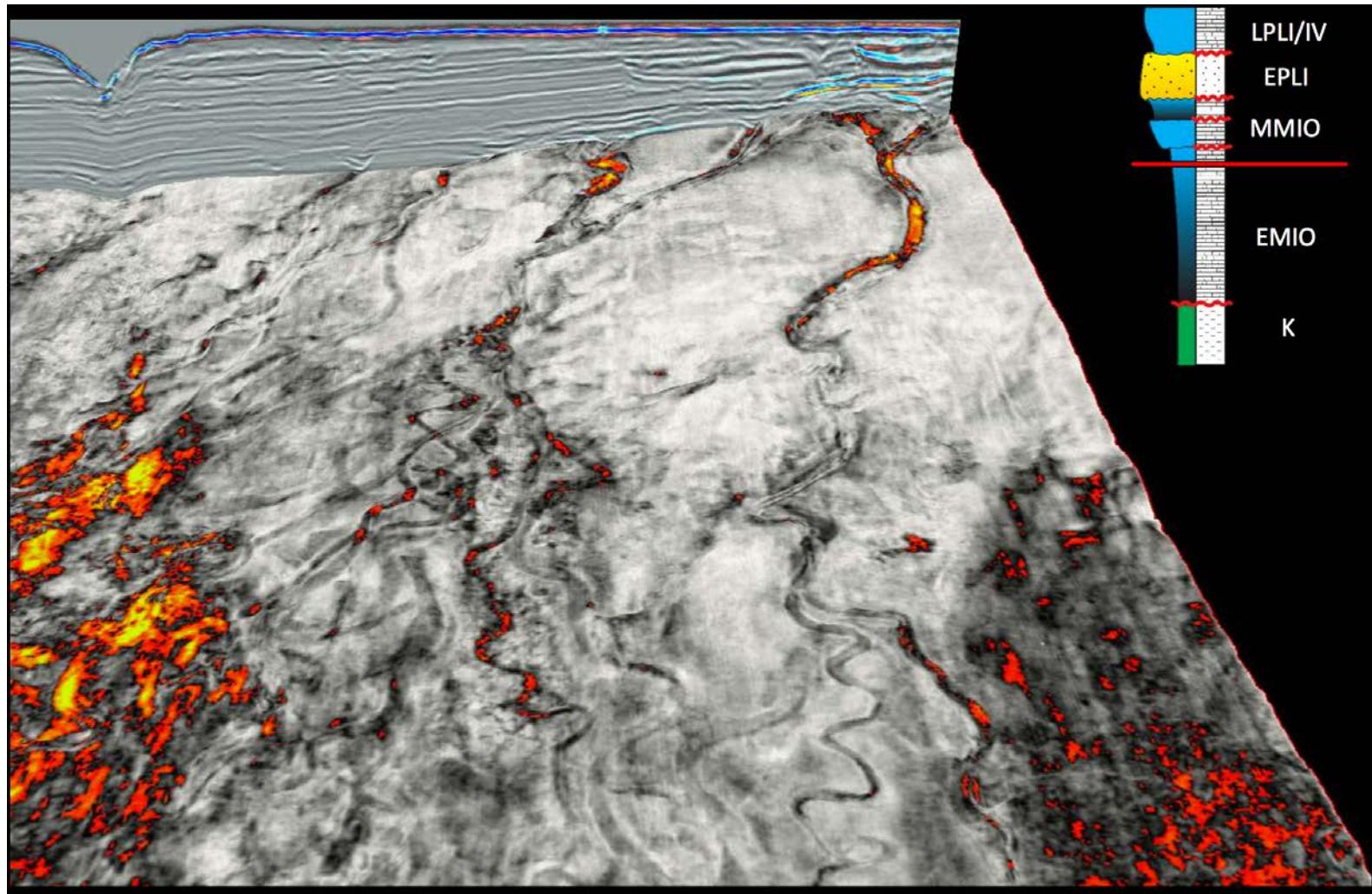
david.lumley@utdallas.edu

3D Seismic imaging...



Dragoset, TLE 2005

3D Seismic imaging...



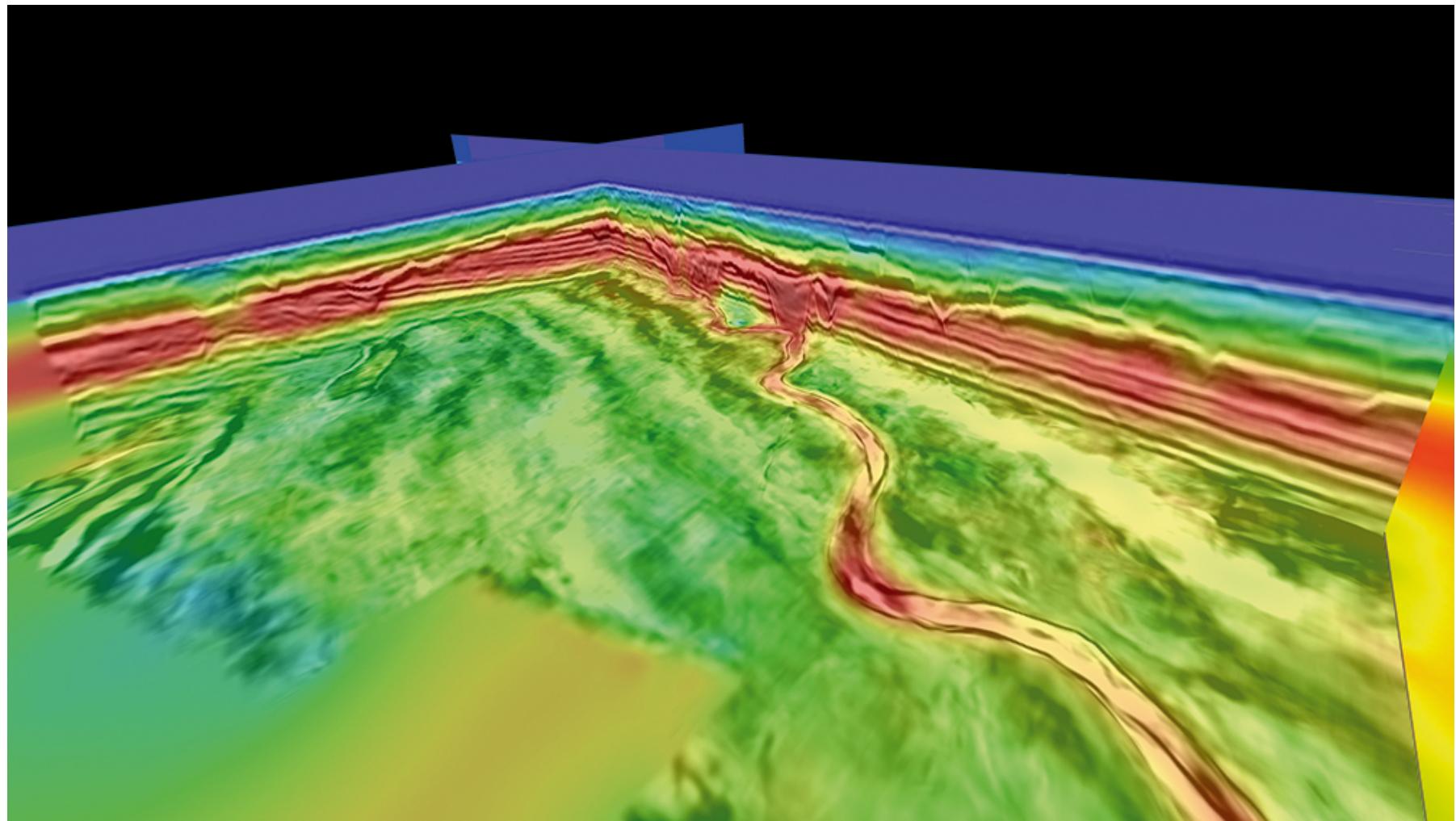
Bourget *et al.*, 2014

david.lumley@utdallas.edu

Inversion... physical properties

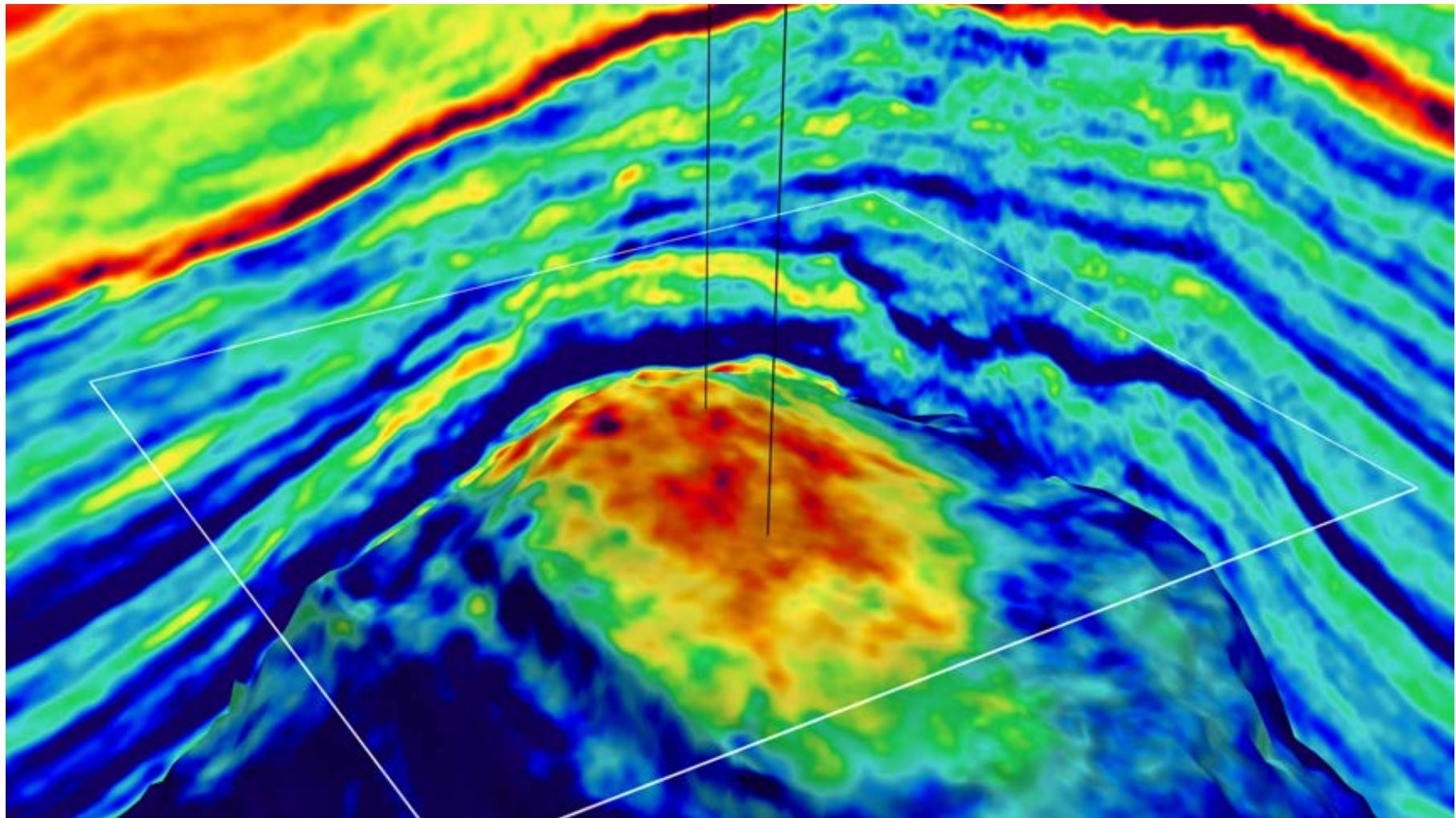


Full waveform inversion



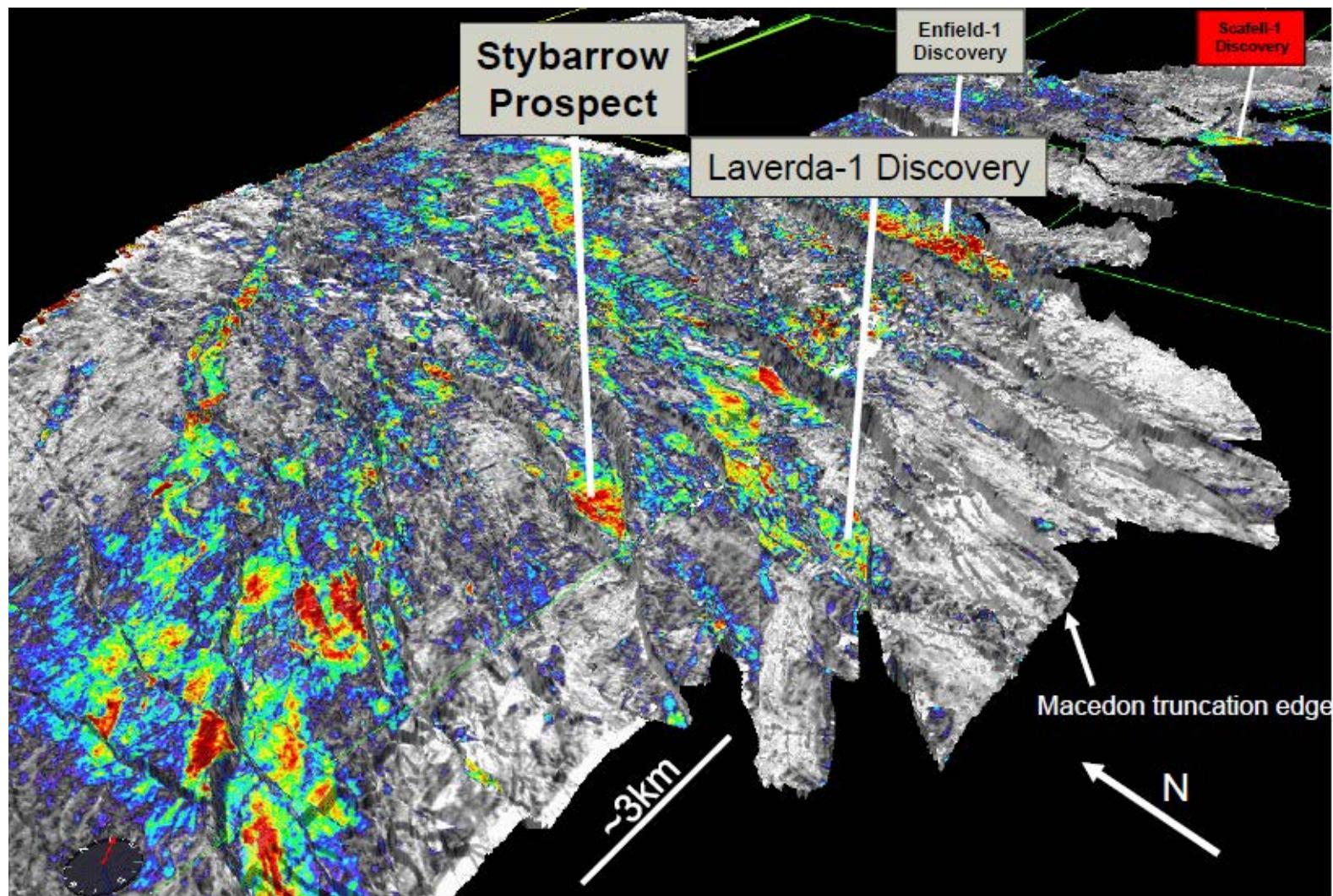
PGS

Full waveform inversion

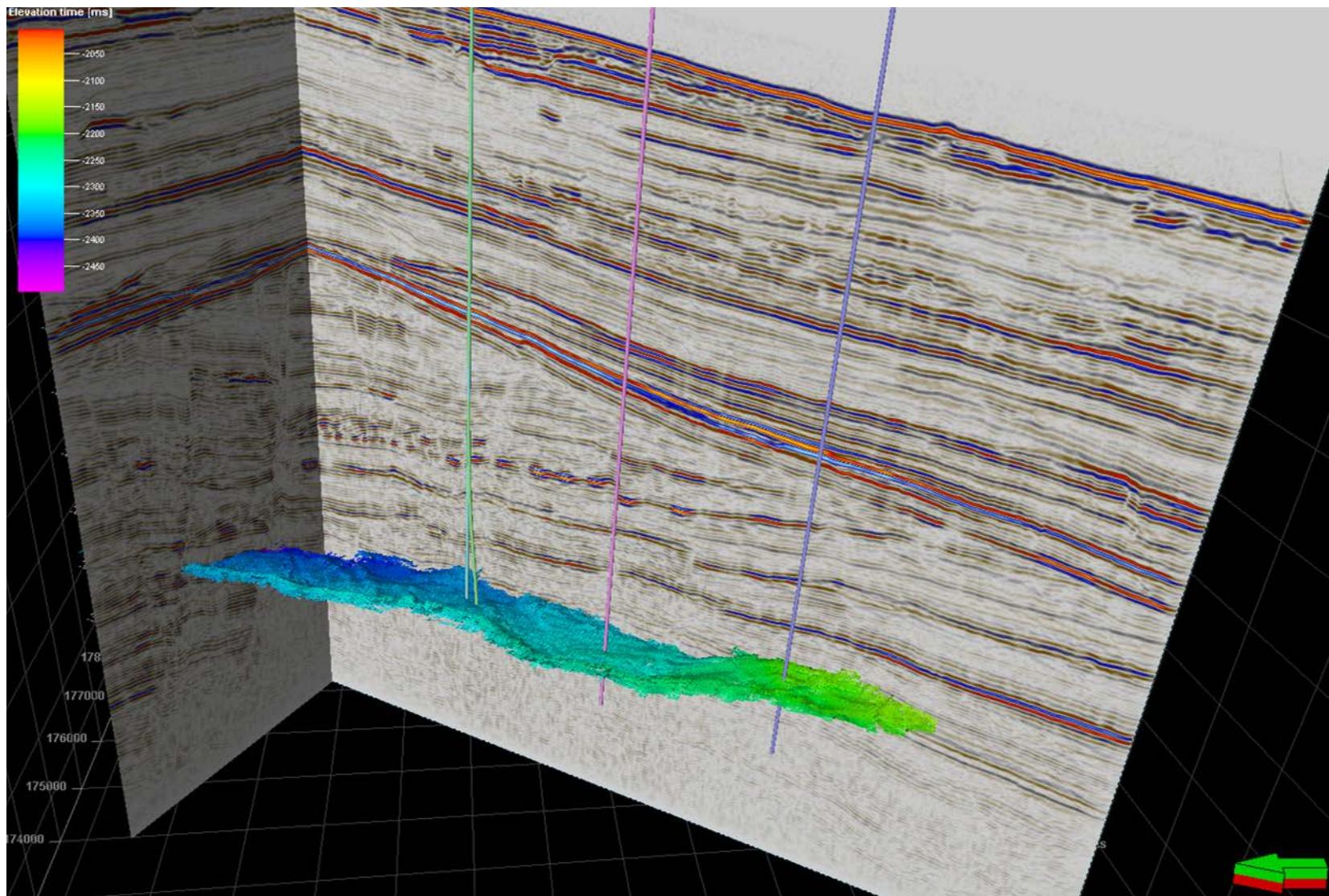


PGS

3D Exploration Seismology

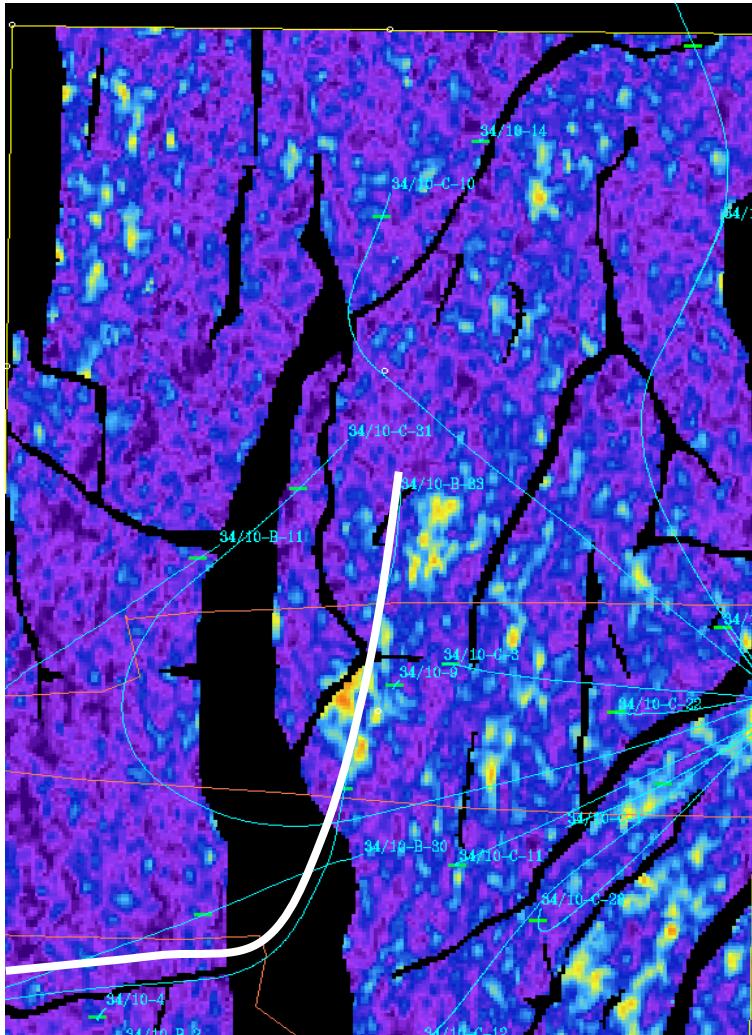


3D+4D Seismic Reservoir Analysis

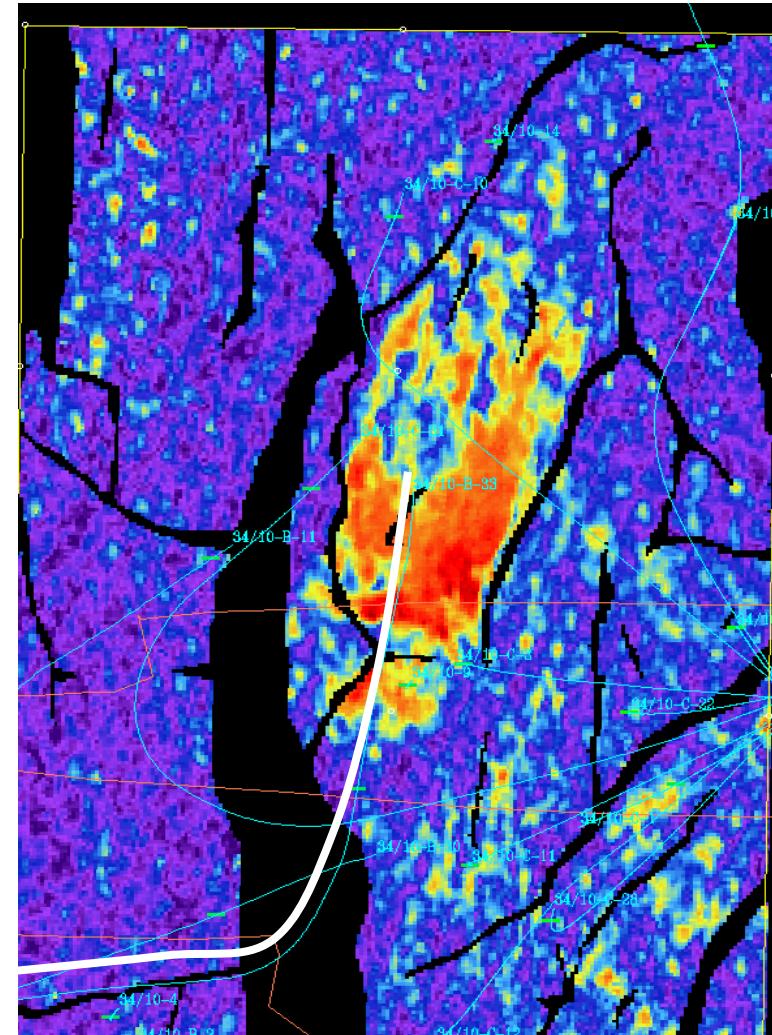


Time-lapse 4D Seismic Monitoring

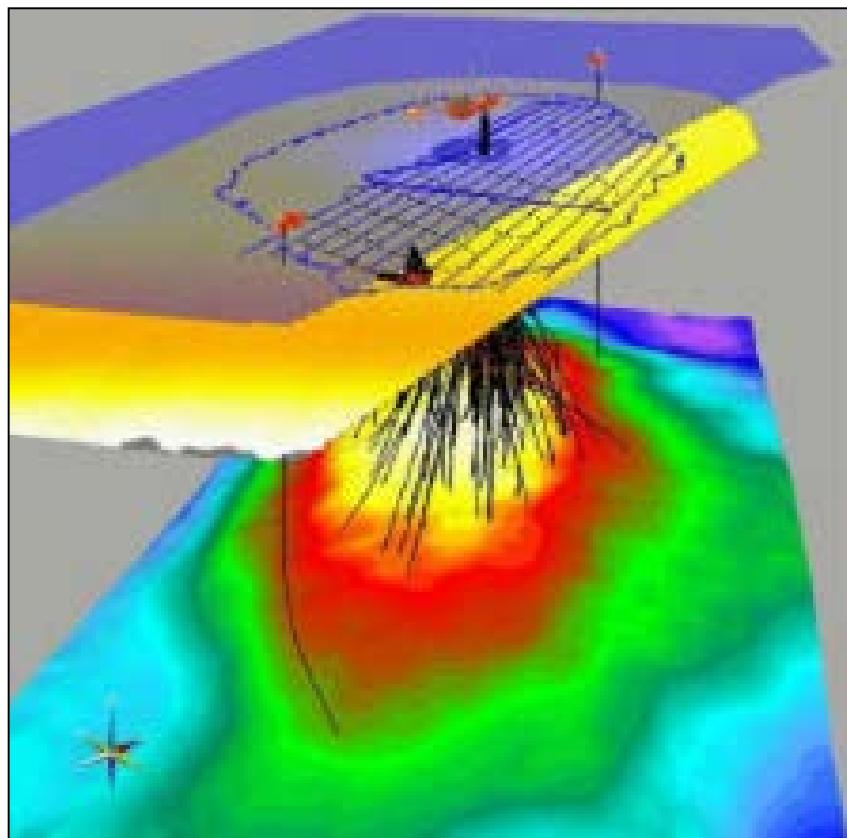
Before



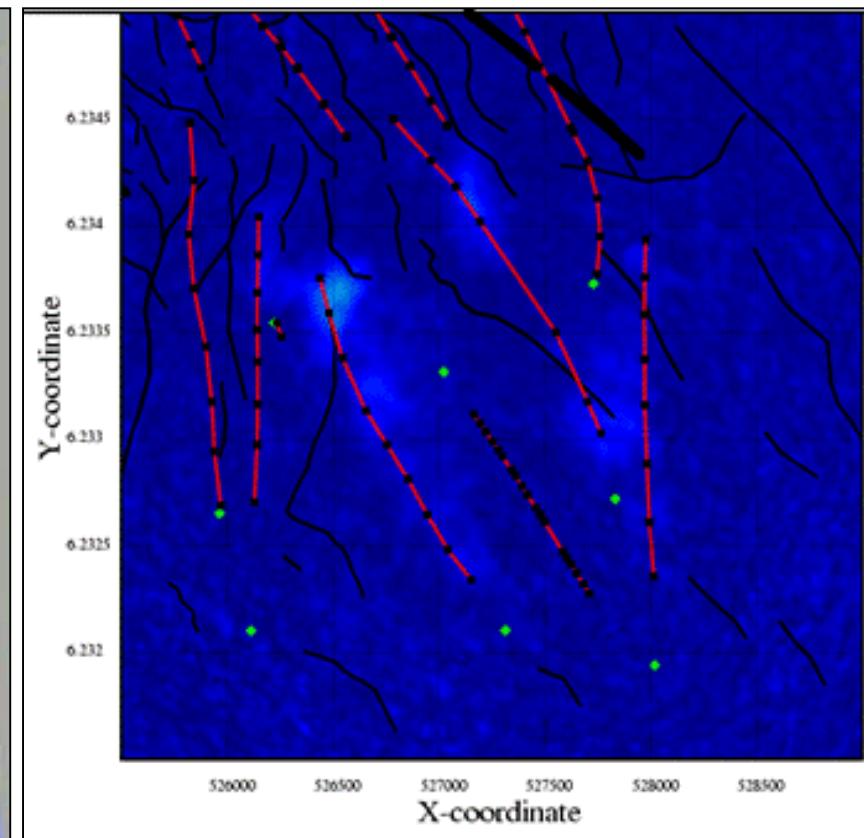
After



Valhall permanent seafloor array



Barkved et al., 2004



courtesy BP

Elastic Wave Equation

Elastic wave equation



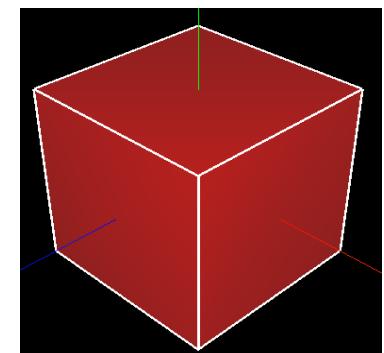
<http://blog.gaborit-d.com/les-icones-gif-3d-moran-goldstein/>

Newton's 2nd Law

$$\mathbf{F}_{total} = \mathbf{F}_{volume} + \mathbf{F}_{surface} = m\ddot{\mathbf{a}}$$

Body force: $f_i = F_i/V$

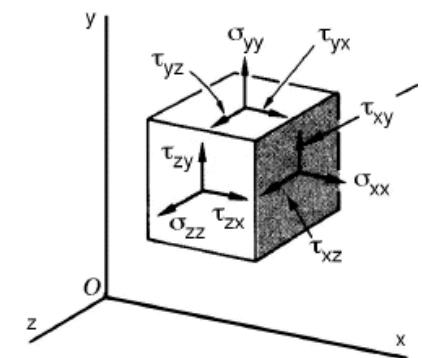
Surface force (Traction): $T_i = F_i/A$



$$\mathbf{F}_{total} = \int_V f_i + \int_S T_i = m\ddot{\mathbf{a}}$$

Stress: $T_i = \sigma_{ij} n_j$; $\sigma_{ij} = T_i x_j$

$$\mathbf{F}_{total} = \int_V f_i + \int_S \sigma_{ij} n_j = m\ddot{\mathbf{a}}$$

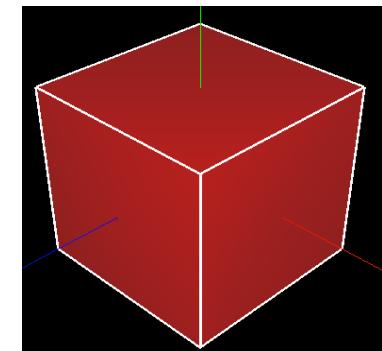


General elastic wave equation

$$\mathbf{F}_{total} = \int_V \mathbf{f}_i + \int_S \sigma_{ij} \mathbf{n}_j = m\ddot{\mathbf{u}}$$

Gauss Divergence Theorem

$$\int_S \mathbf{F} \cdot \mathbf{n} = \int_V \nabla \cdot \mathbf{F}$$



$$\mathbf{F}_{total} = \int_V \mathbf{f}_i + \int_V \partial_i \sigma_{ij} = \int_V \rho \ddot{\mathbf{u}}$$

$$\rho \ddot{\mathbf{u}}_i - \partial_i \sigma_{ij} = \mathbf{f}_i \quad \text{Elastic Weqn #1}$$

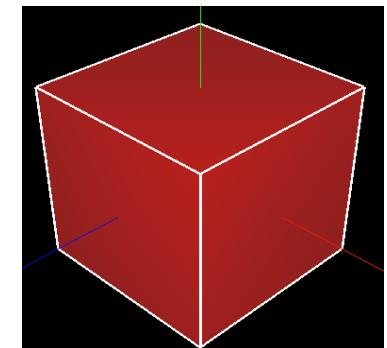
$$\rho \partial_t v_i - \partial_i \sigma_{ij} = f_i$$

"velocity-stress FD/FEM method"

Linear Stress and Strain

Strain: $e_{kl} = \frac{1}{2} (\partial_k u_l + \partial_l u_k)$

Normal: $k = l$ *Shear: $k \neq l$*



Generalized Hooke's Law (linear stress-strain)

$$\sigma_{ij} = c_{ijkl} e_{kl}$$

c_{ijkl} : elastic stiffness tensor

$\rho \ddot{u}_i - \partial_i c_{ijkl} e_{kl} = f_i$

Elastic Wgn #2

Elastic Stiffness Tensor ϵ_{ijkl}

- 81 coefficients in general, but due to symmetry etc.
 - Reduces to 21 independent coefficients
- ϵ_{ijkl} can be written in compact 6x6 Voigt notation as ϵ_{ii}

$$\begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{23} \\ \sigma_{13} \\ \sigma_{12} \end{bmatrix} = \begin{bmatrix} C_{1111} & C_{1122} & C_{1133} & C_{1123} & C_{1113} & C_{1112} \\ & C_{2222} & C_{2233} & C_{2223} & C_{2213} & C_{2212} \\ & & C_{3333} & C_{3323} & C_{3313} & C_{3312} \\ & & & C_{2323} & C_{2313} & C_{2312} \\ & & & & C_{1313} & C_{1312} \\ & & & & & C_{1212} \end{bmatrix} \begin{bmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ 2\epsilon_{23} \\ 2\epsilon_{13} \\ 2\epsilon_{12} \end{bmatrix}$$

symm

www.web.mit.edu

Voigt Elastic Stiffness Tensor ϵ_{ij}

- σ_{ijkl} can be written in compact 6x6 Voigt notation as ϵ_{ij}

$$\begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{23} \\ \sigma_{13} \\ \sigma_{12} \end{bmatrix} = \begin{bmatrix} C_{1111} & C_{1122} & C_{1133} & C_{1123} & C_{1113} & C_{1112} \\ & C_{2222} & C_{2233} & C_{2223} & C_{2213} & C_{2212} \\ & & C_{3333} & C_{3323} & C_{3313} & C_{3312} \\ & & & C_{2323} & C_{2313} & C_{2312} \\ & & & & C_{1313} & C_{1312} \\ & & & & & C_{1212} \end{bmatrix} \begin{bmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ 2\epsilon_{23} \\ 2\epsilon_{13} \\ 2\epsilon_{12} \end{bmatrix}$$

symm

$$\begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \sigma_3 \\ \sigma_4 \\ \sigma_5 \\ \sigma_6 \end{bmatrix} = \begin{bmatrix} C_{11} & C_{12} & C_{13} & C_{14} & C_{15} & C_{16} \\ & C_{22} & C_{23} & C_{24} & C_{25} & C_{26} \\ & & C_{33} & C_{34} & C_{35} & C_{36} \\ & & & C_{44} & C_{45} & C_{46} \\ & & & & C_{55} & C_{56} \\ & & & & & C_{66} \end{bmatrix} \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \epsilon_3 \\ \epsilon_4 \\ \epsilon_5 \\ \epsilon_6 \end{bmatrix}$$

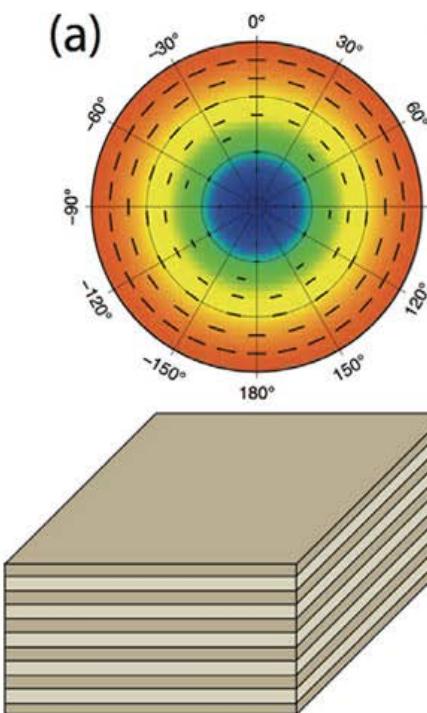
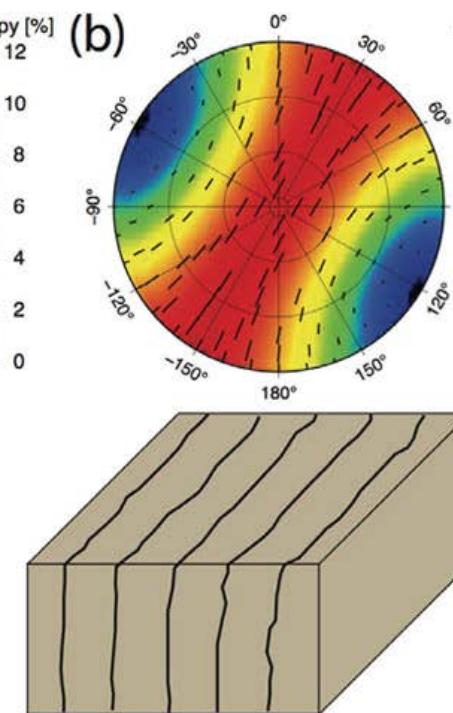
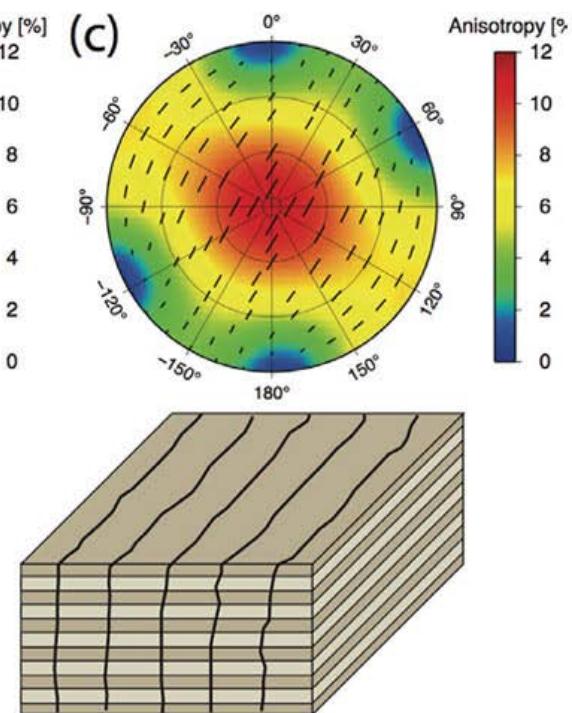
symm

Elastic Stiffness Tensor c_{ijkl}

- Isotropic
 - 2 independent coefficients... λ and μ ... “*Lamé parameters*”

$$\{c_{ij}\} = \begin{pmatrix} \lambda + 2\mu & \lambda & \lambda & 0 & 0 & 0 \\ \lambda & \lambda + 2\mu & \lambda & 0 & 0 & 0 \\ \lambda & \lambda & \lambda + 2\mu & 0 & 0 & 0 \\ 0 & 0 & 0 & 2\mu & 0 & 0 \\ 0 & 0 & 0 & 0 & 2\mu & 0 \\ 0 & 0 & 0 & 0 & 0 & 2\mu \end{pmatrix}.$$

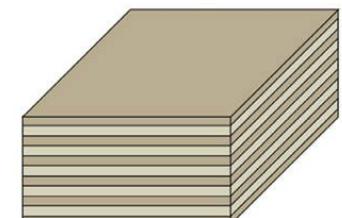
Seismic Anisotropy

VTI**HTI****Ortho**

after Kendall et al., CSEGR 2014

Elastic Stiffness Tensor C_{ijkl}

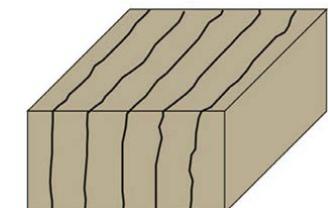
- VTI (polar) anisotropy
 - 5 independent coefficients $*C_{12} = C_{11} - 2C_{66}$



$$C_{\text{VTI}} = \begin{bmatrix} c_{11} & c_{12}^* & c_{13} & 0 & 0 & 0 \\ c_{12}^* & c_{11} & c_{13} & 0 & 0 & 0 \\ c_{13} & c_{13} & c_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & c_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & c_{44} & 0 \\ 0 & 0 & 0 & 0 & 0 & c_{66} \end{bmatrix}$$

Elastic Stiffness Tensor c_{ijkl}

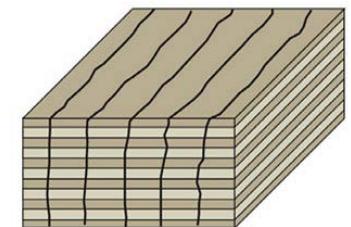
- HTI (azimuthal) anisotropy
 - 5 independent coefficients



$$\mathbf{c}^{(HTI)} = \begin{bmatrix} c_{11} & c_{13} & c_{13} & 0 & 0 & 0 \\ c_{13} & c_{33} & c_{33} - 2c_{44} & 0 & 0 & 0 \\ c_{13} & c_{33} - 2c_{44} & c_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & c_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & c_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & c_{55} \end{bmatrix}$$

Elastic Stiffness Tensor c_{ijkl}

- Orthorhombic anisotropy
 - 9 independent coefficients



$$\mathbf{C} = \begin{pmatrix} C_{11} & C_{12} & C_{13} & 0 & 0 & 0 \\ C_{12} & C_{22} & C_{23} & 0 & 0 & 0 \\ C_{13} & C_{23} & C_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & C_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & C_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & C_{66} \end{pmatrix}.$$

Elastic Stiffness Tensor c_{ijkl}

- Monoclinic anisotropy
 - 13 independent coefficients

$$\mathbf{C}' = \begin{bmatrix} c'_{11} & c'_{12} & c'_{13} & 0 & 0 & c'_{16} \\ c'_{12} & c'_{22} & c'_{23} & 0 & 0 & c'_{26} \\ c'_{13} & c'_{23} & c'_{33} & 0 & 0 & c'_{36} \\ 0 & 0 & 0 & c'_{44} & c'_{45} & 0 \\ 0 & 0 & 0 & c'_{45} & c'_{55} & 0 \\ c'_{16} & c'_{26} & c'_{36} & 0 & 0 & c'_{66} \end{bmatrix}$$

Isotropic elastic wave equation

$$\rho \ddot{\mathbf{u}}_i - \partial_i \mathcal{C}_{ijkl} \mathbf{e}_{kl} = f_i \quad \text{Weqn#2}$$

$$\rho \ddot{\underline{\mathbf{u}}} - \nabla \cdot \underline{\mathcal{C}} : (\nabla \underline{\mathbf{u}} + \nabla \underline{\mathbf{u}}^T)/2 = \underline{f}$$

substitute $\underline{\mathcal{C}}_{iso}$: assume ~homogeneous: $\partial\lambda, \partial\mu \sim 0$

$$\rho \ddot{\underline{\mathbf{u}}} = \underline{f} + \rho Vp^2 \nabla(\nabla \cdot \underline{\mathbf{u}}) - \rho Vs^2 \nabla \times (\nabla \times \underline{\mathbf{u}}) \quad \text{#3}$$

P-wave velocity: $Vp^2 = (\lambda + 2\mu) / \rho$

S-wave velocity: $Vs^2 = \mu / \rho$

P-wave scalar wave equation (iso)

$$\rho \ddot{\underline{u}} = f + \rho V p^2 \nabla (\nabla \cdot \underline{u}) - \rho V s^2 \nabla \times (\nabla \times \underline{u}) \quad \#3$$

Take Divergence of Eqn #3... let $\mathcal{P} = \nabla \cdot \underline{u}$

$$(\partial_{tt} - V p^2 \nabla^2) \mathcal{P}(\underline{x}, t) = \delta_p(\underline{x}, t) \quad \text{Eqn #4}$$

P-wave velocity: $V p^2 = (\lambda + 2\mu) / \rho$

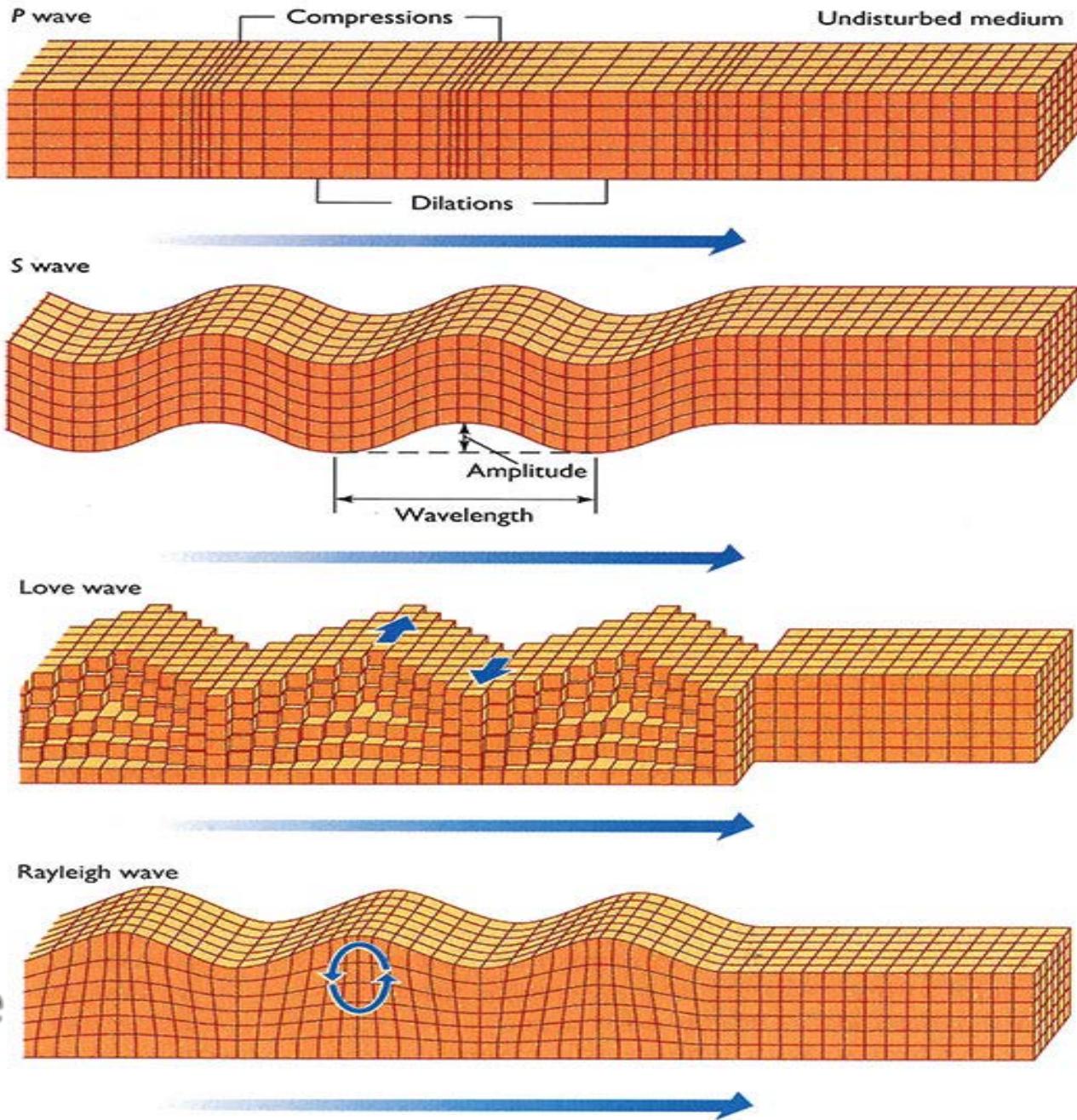
S-wave vector wave equation (iso)

$$\rho \ddot{\underline{u}} = f + \rho V p^2 \nabla (\nabla \cdot \underline{u}) - \rho V s^2 \nabla \times (\nabla \times \underline{u}) \quad \#3$$

Take curl of Eqn #3... let $\underline{Q} = \nabla \times \underline{u}$

$$(\partial_{tt} - V s^2 \nabla^2) \underline{Q}(\underline{x}, t) = \underline{\delta}_s(\underline{x}, t) \quad \text{Weqn #5}$$

S-wave velocity: $V s^2 = \mu / \rho$



P wave

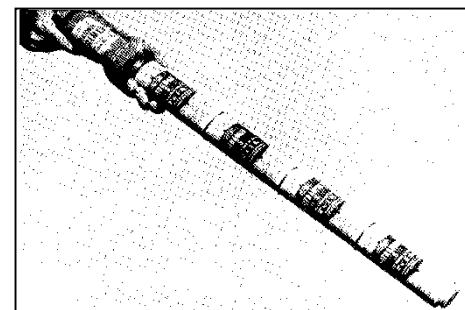
S wave

Love wave

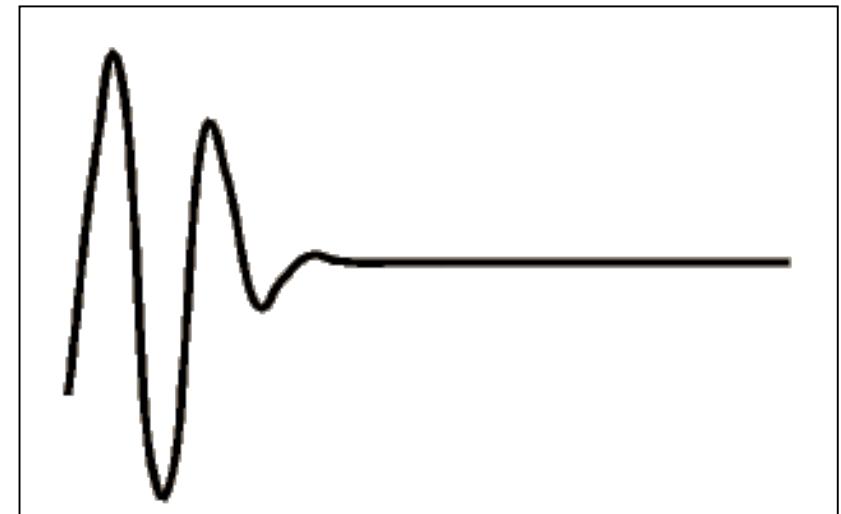
Rayleigh wave

Sources, Sensors, Acquisition geometry

land sources - dynamite



“impulsive” signal



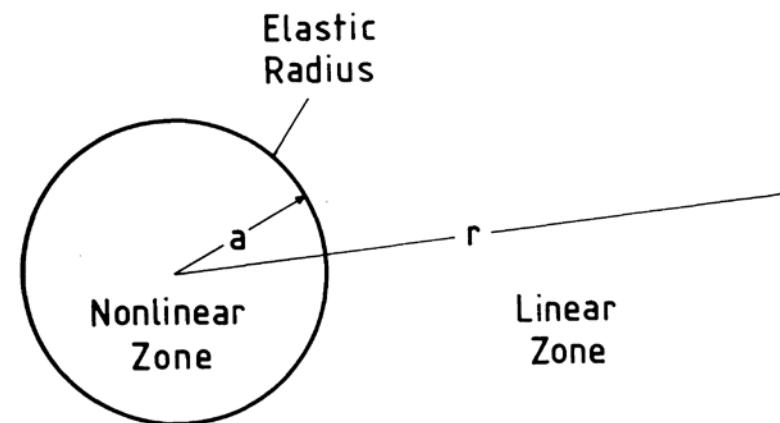
$$s(t) = \sin(\omega t) e^{-at}$$

land sources - dynamite

$$u(r, t) = \frac{1}{r^2} F\left(t - \frac{r}{v}\right) + \frac{1}{r v} F'\left(t - \frac{r}{v}\right); \quad t \geq r/v; \quad r > a$$

near field
 $r < 1 \text{ wavelength}$

far field
 $r >> 1 \text{ wavelength}$



land sources - vibroseis

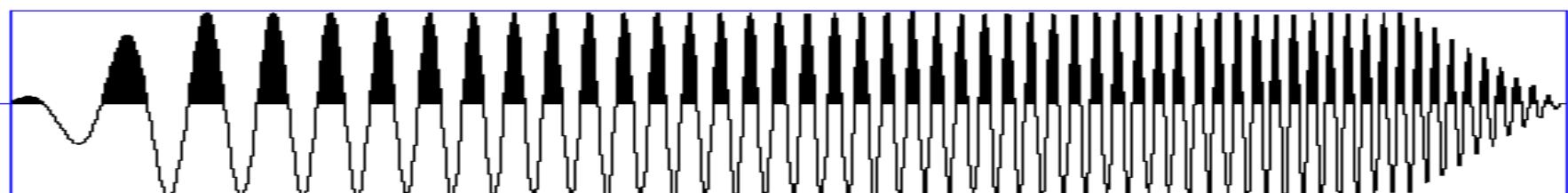


$$s(t) = \sin(2\pi f_0 t + \pi k t^2)$$

f_0 = starting frequency
 $k = (f_1 - f_0)/t_1$ = chirp rate

“chirp” signal

Conoco



land source array



Geokinetics

marine sources - airgun



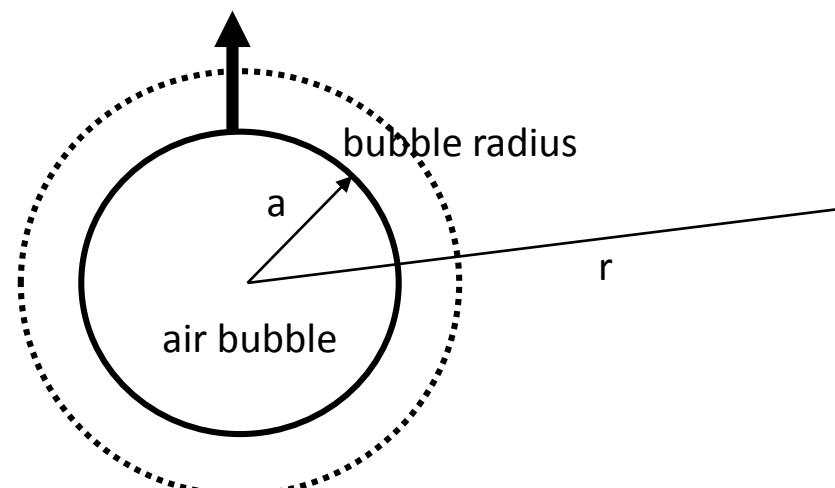
Bolt Technologies

marine sources - airgun

$$u(r, t) = \frac{1}{r^2} F\left(t - \frac{r}{v}\right) + \frac{1}{r v} F'\left(t - \frac{r}{v}\right); \quad t \geq r/v; \quad r > a$$

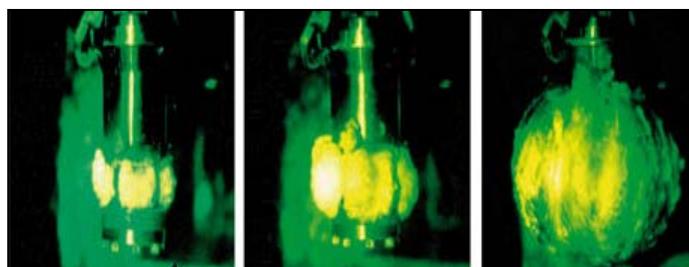
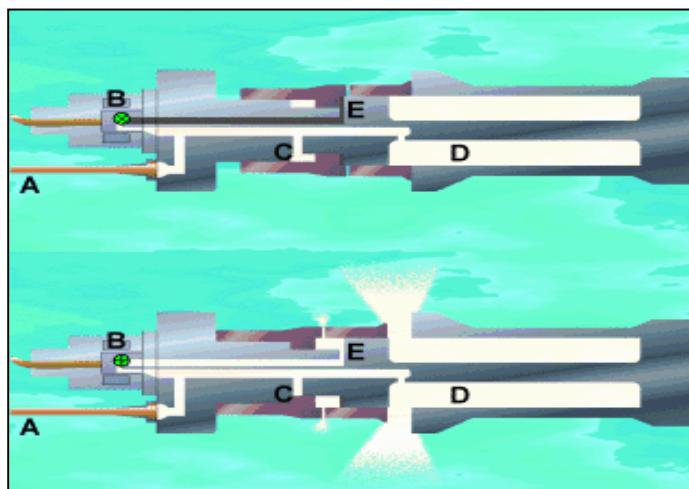
near field
 $r < 1 \text{ wavelength}$

far field
 $r >> 1 \text{ wavelength}$



marine sources - airgun

“impulsive” signal



GeoExpro

air gun array

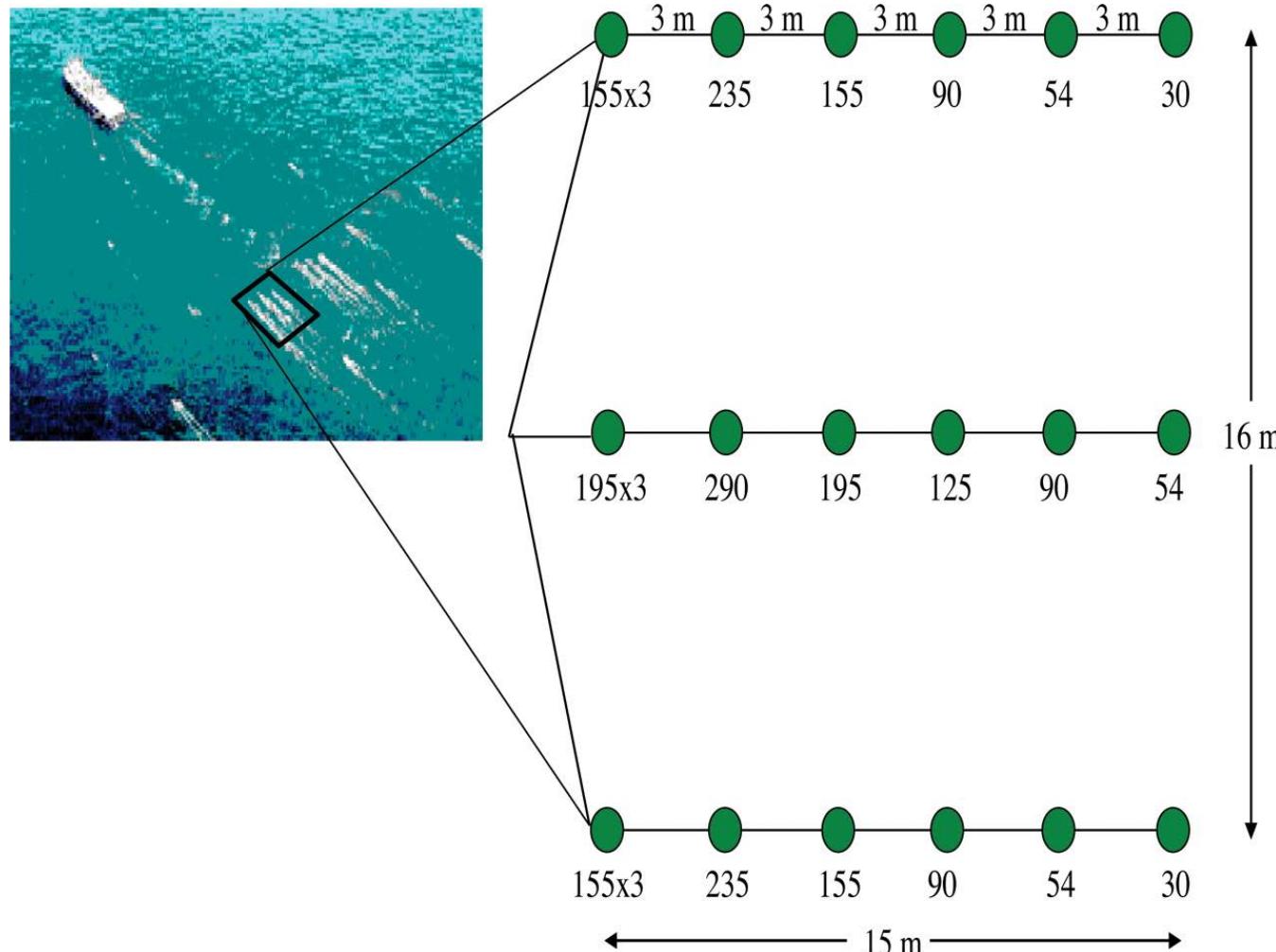


marine airgun array



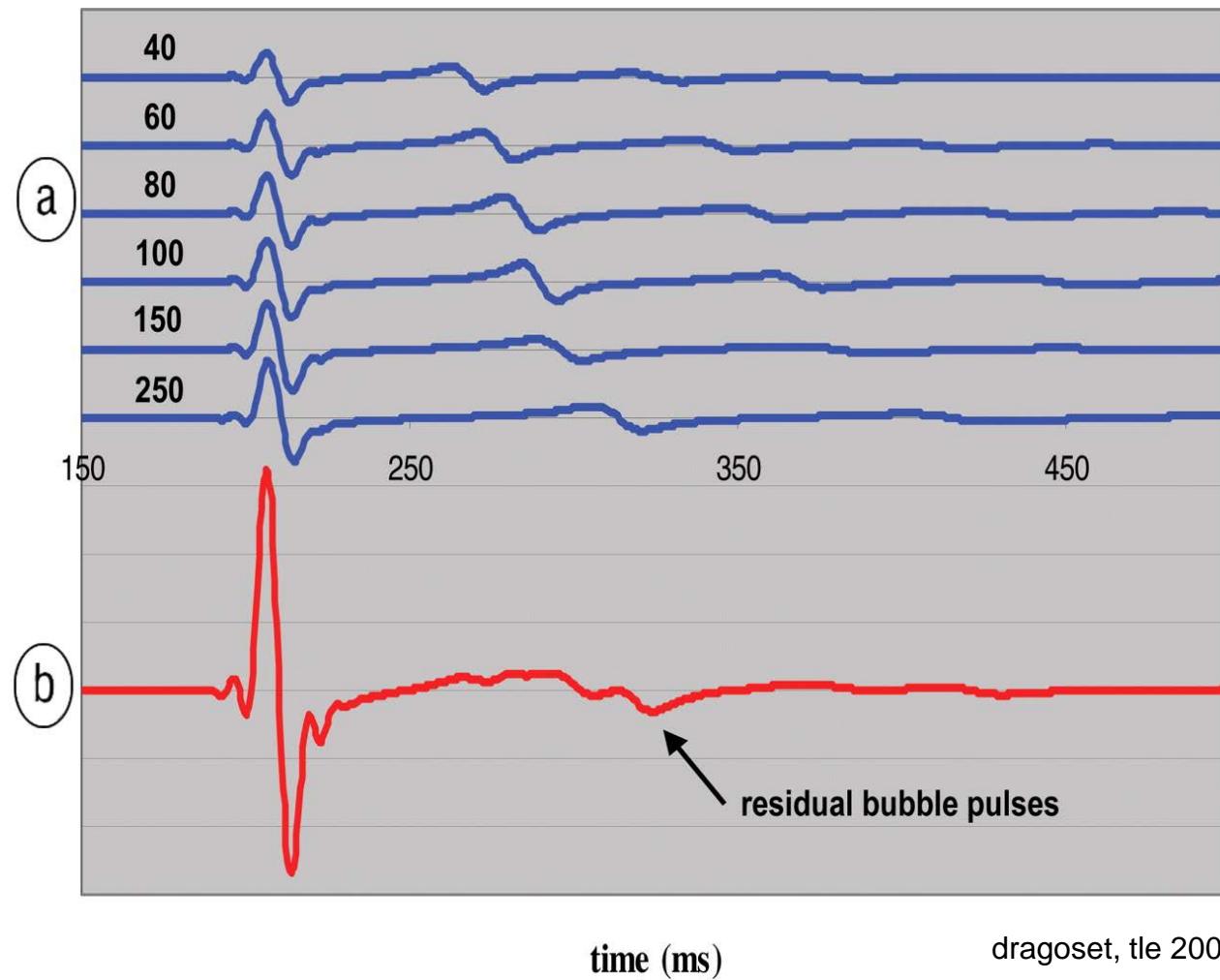
fugro

marine airgun array

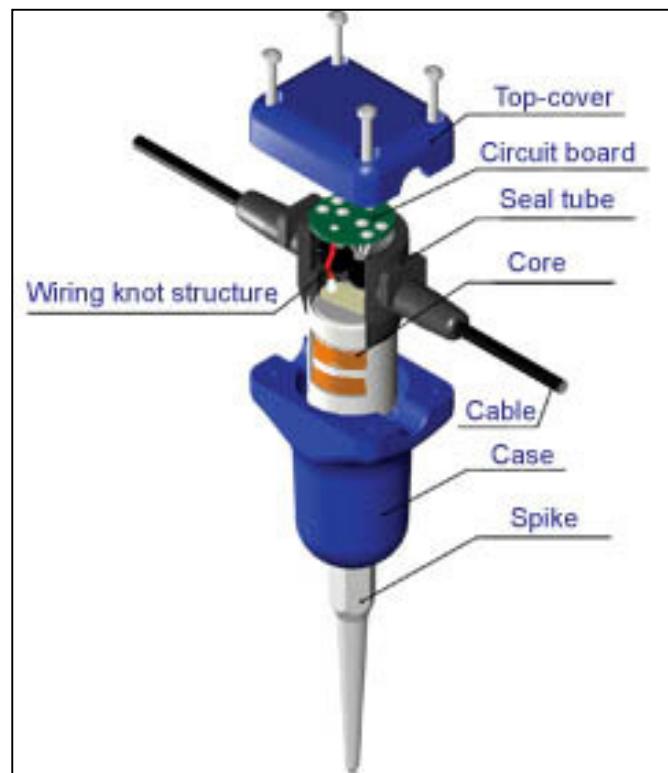


dragoset, TLE, 2000

marine airgun array



land receivers - geophone



output

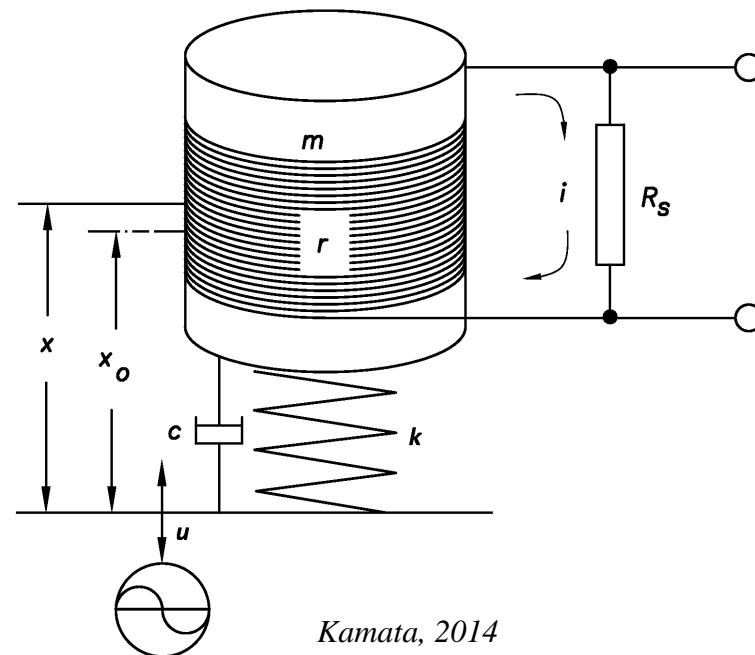


spring-mounted magnet
moving in a coil = voltage
~ particle velocity



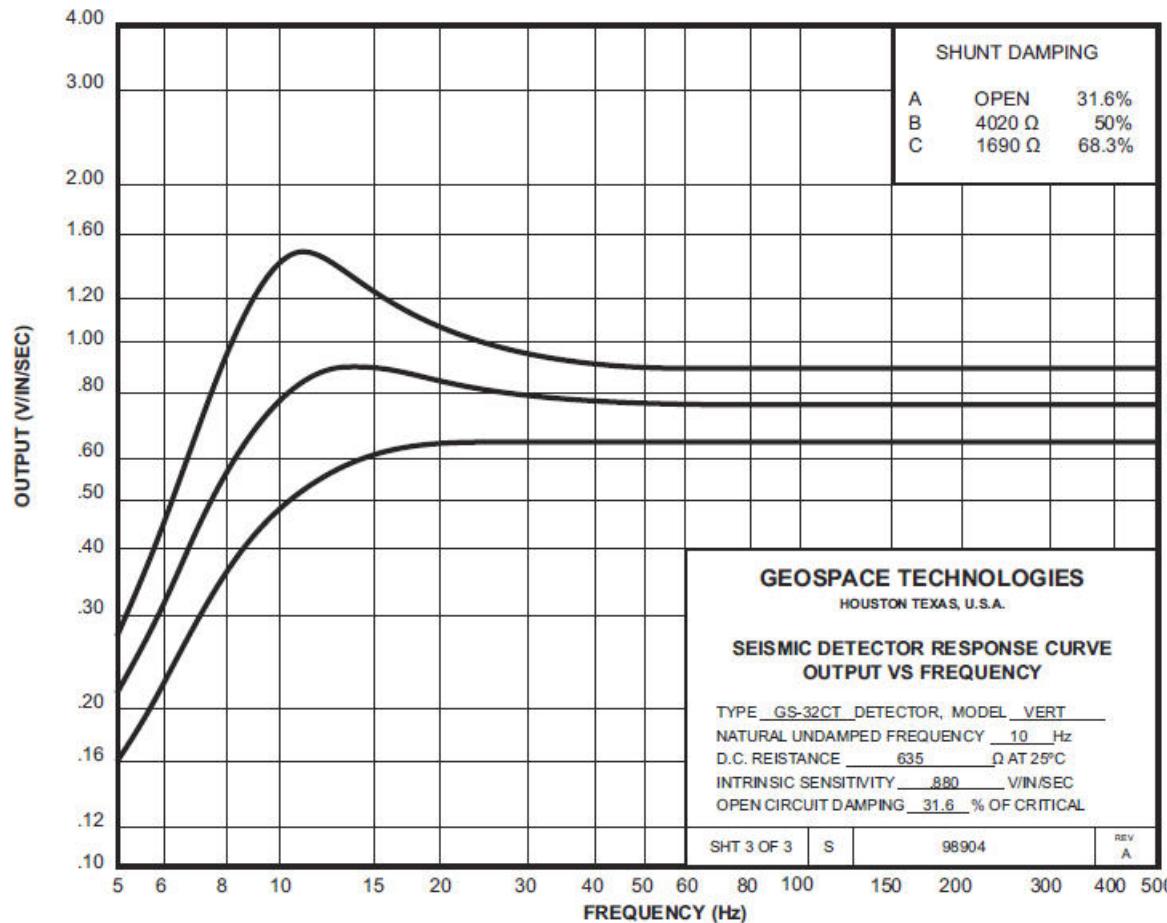
land receivers - geophone

$$e(t) = K/\omega \ e^{-\sigma(t-t_0)} \sin(\omega(t-t_0)) \ H(t-t_0) \text{ volts}$$



Kamata, 2014

geophone response

*Geospace*

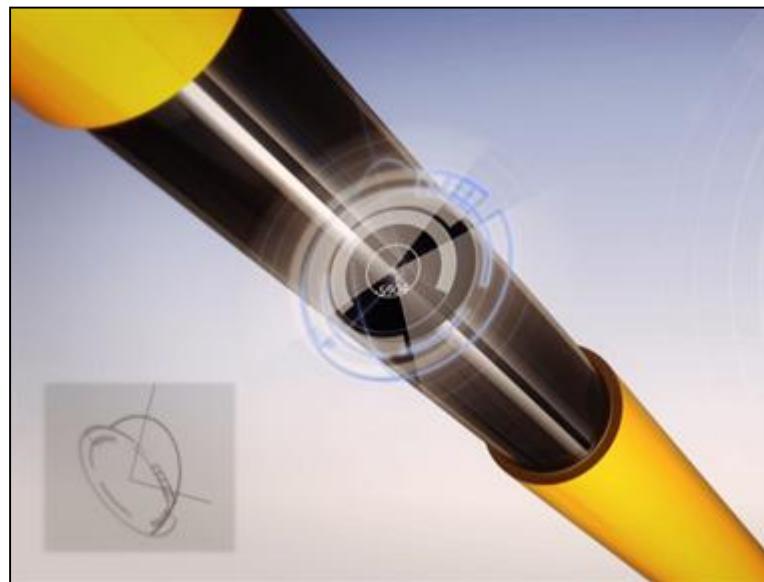
land receiver array



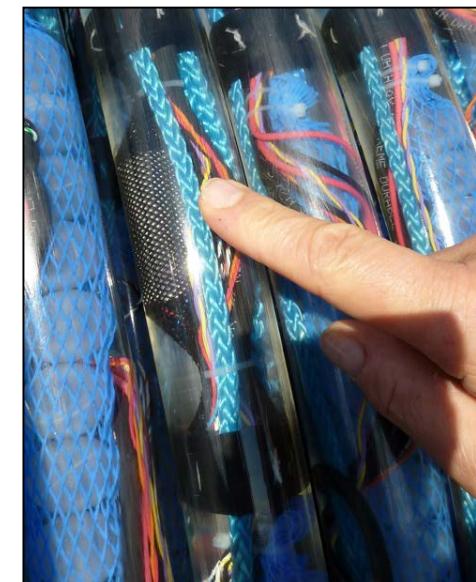
Lumley et al., 2005

marine receivers - hydrophone

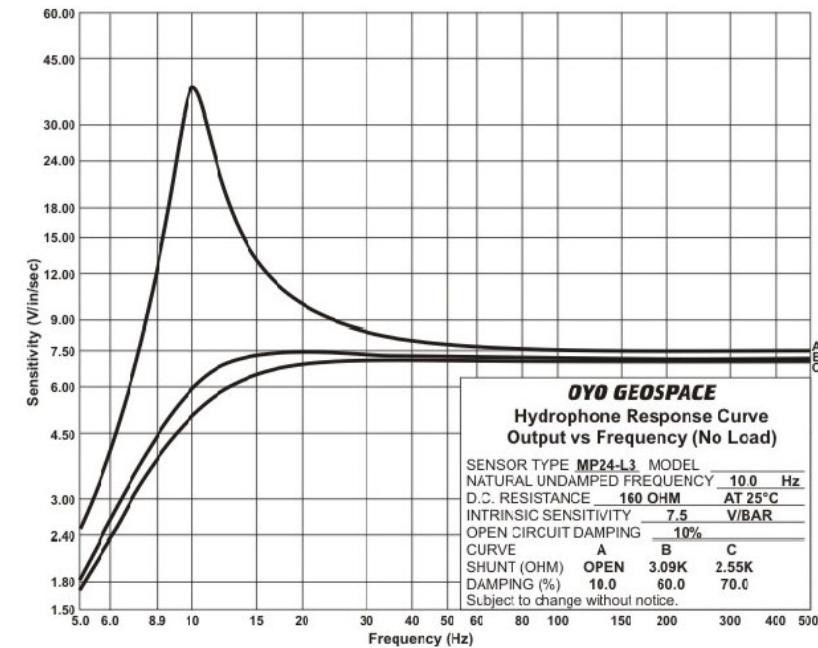
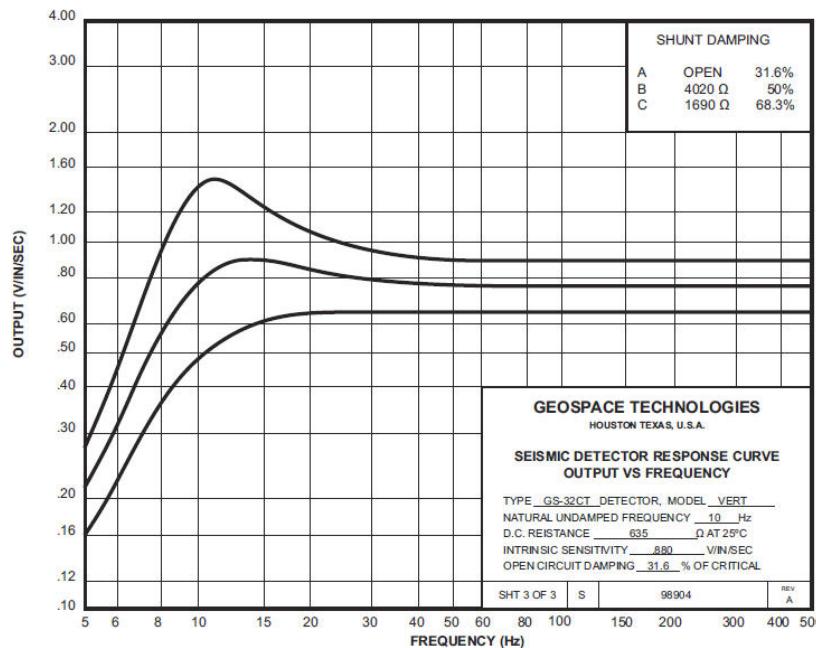
piezoelectric material
generates a voltage when stressed/strained
~ pressure



Sercel

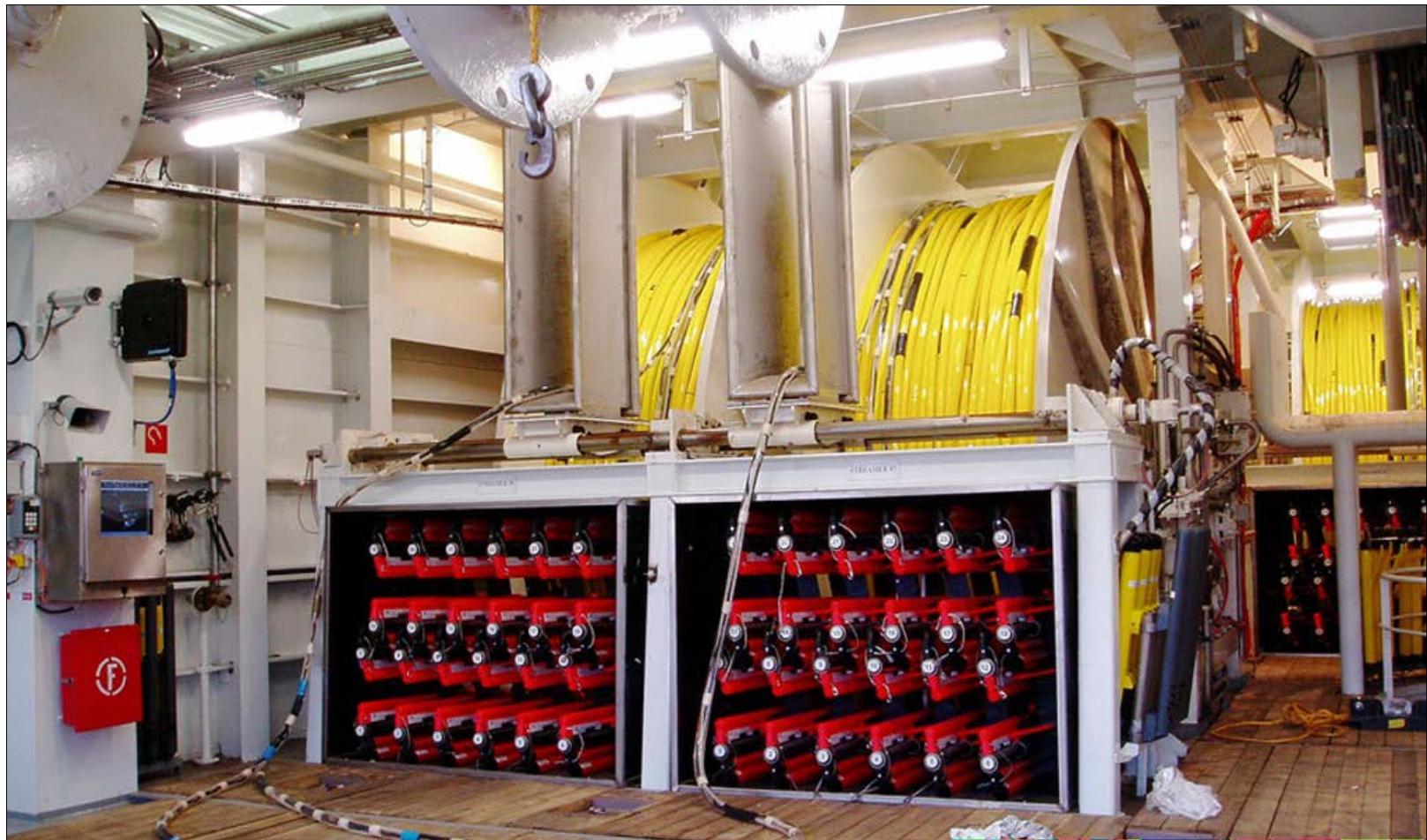


geophone + hydrophone response



Geospace

seismic boat – streamer deck



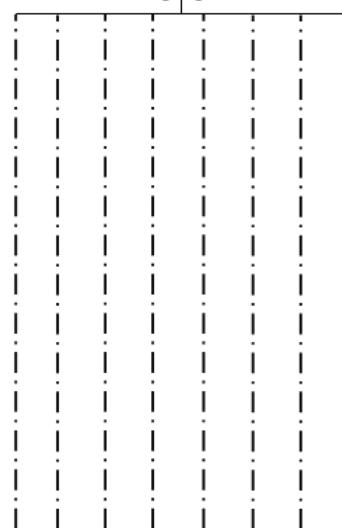
fugro

Seismic vessel;
arrow indicates
the direction of
vessel's motion

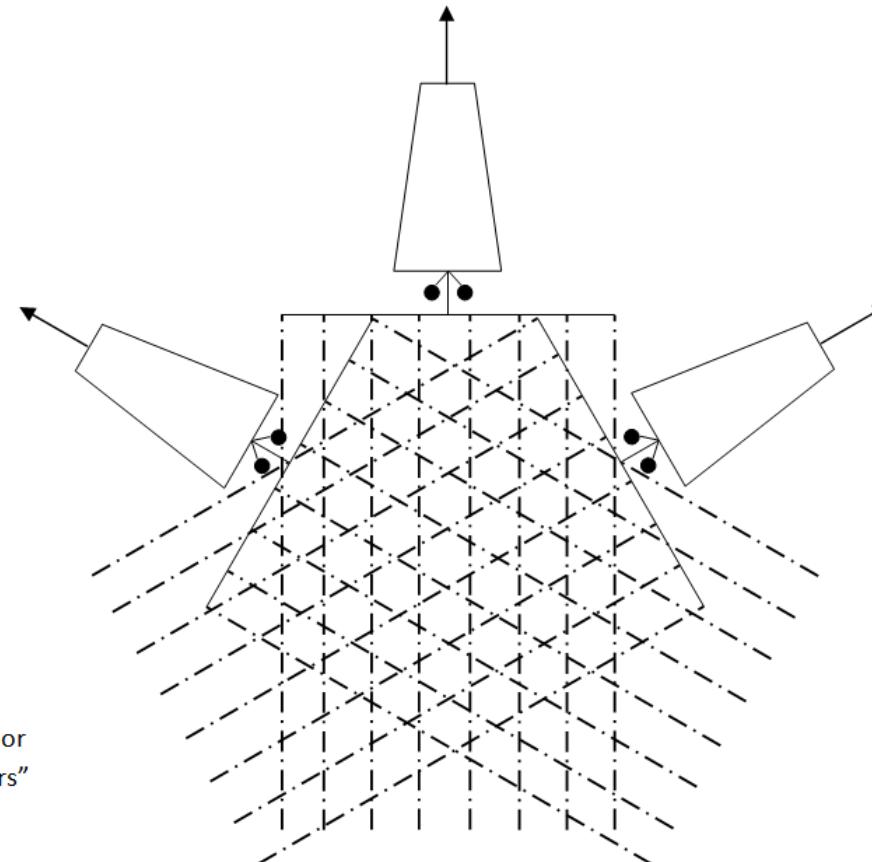


Seismic sources
(airguns)

Lines of
receivers or
"streamers"

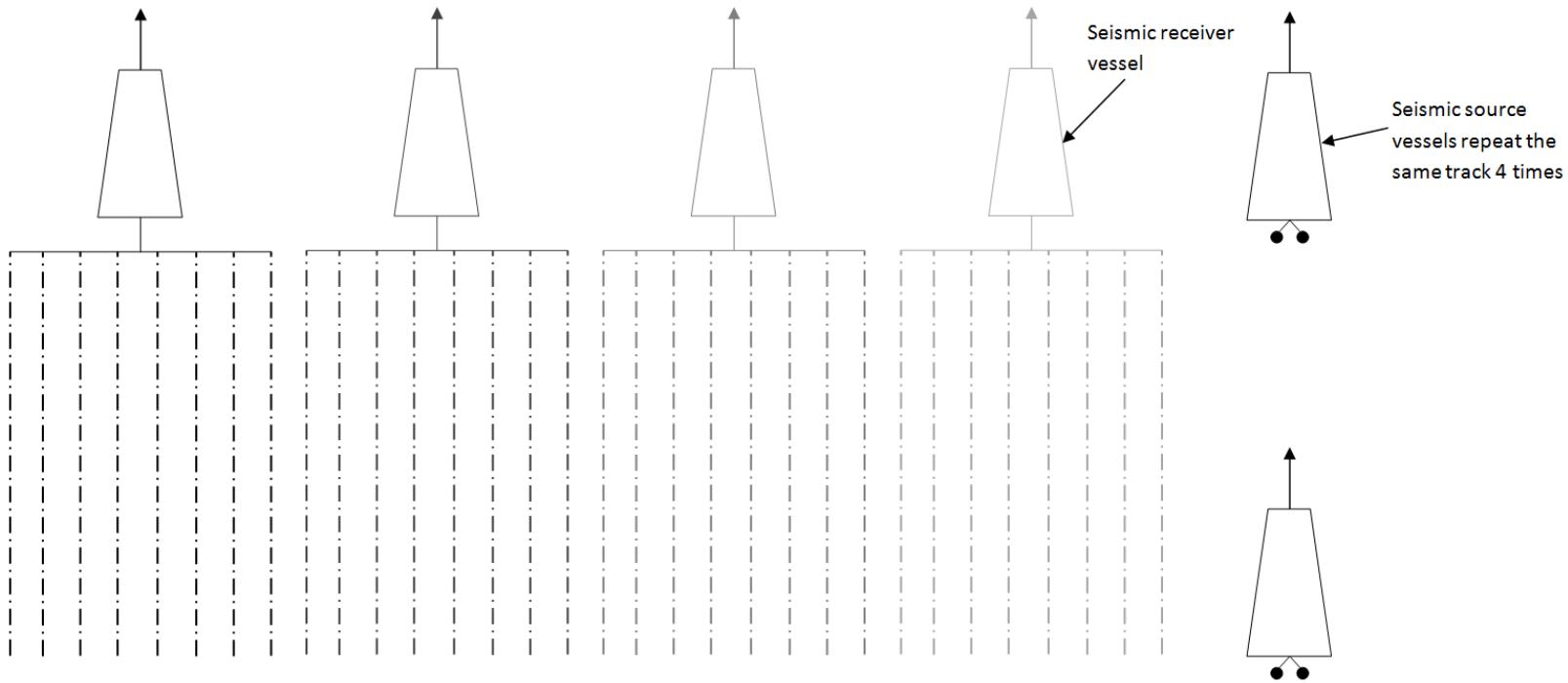


Narrow Azimuth Towed Streamer



Multi-Azimuth Towed Streamer

Wikipedia

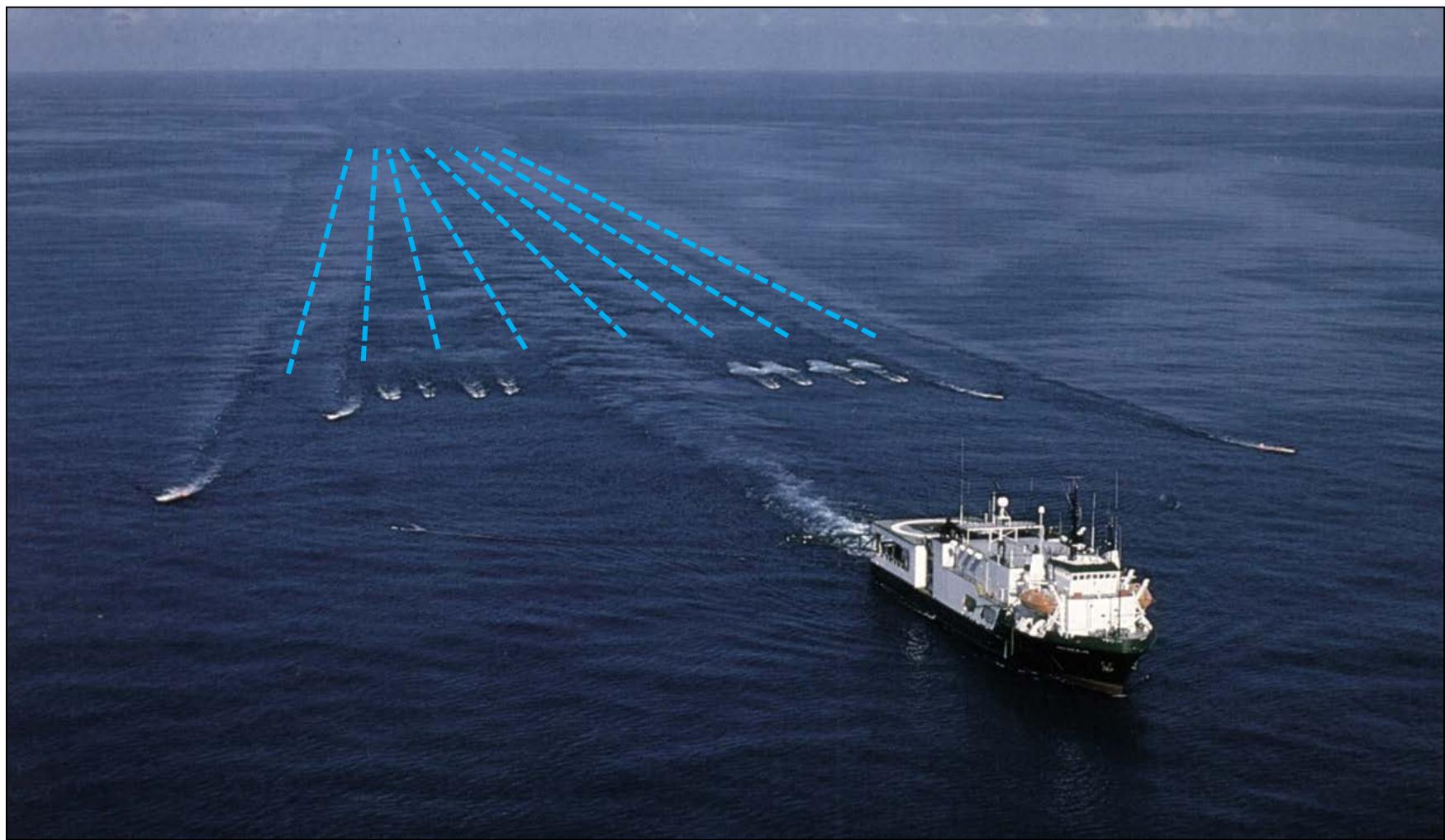


Wide Azimuth Towed Streamer

Seismic receiver vessel repeats 4 parallel tracks to give the effect of a survey with 4 x as many receivers; arrows indicates the direction of each vessel's motion

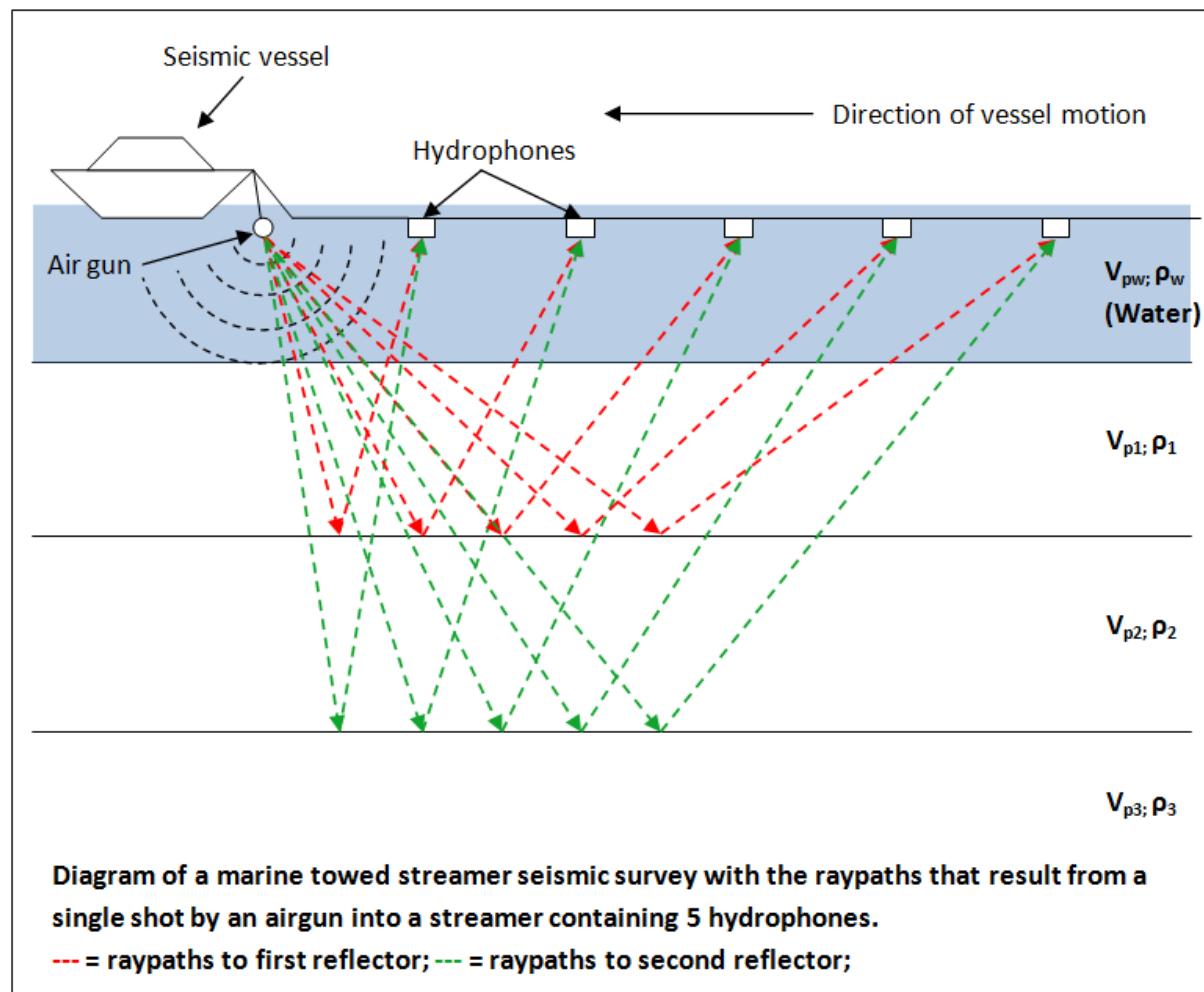
Wikipedia

marine receiver array

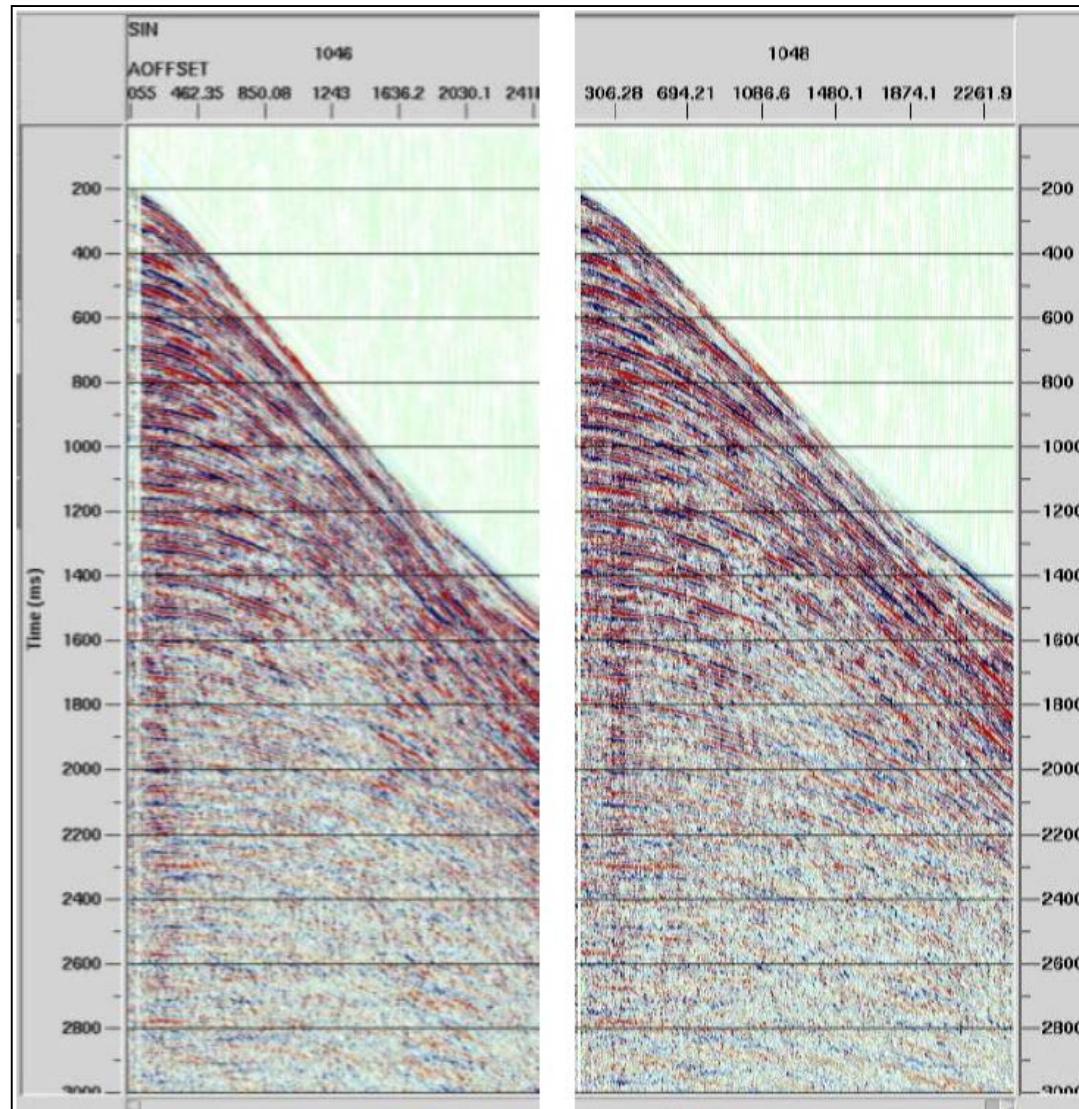


after Dragoset, TLE, 2005

Marine seismic acquisition



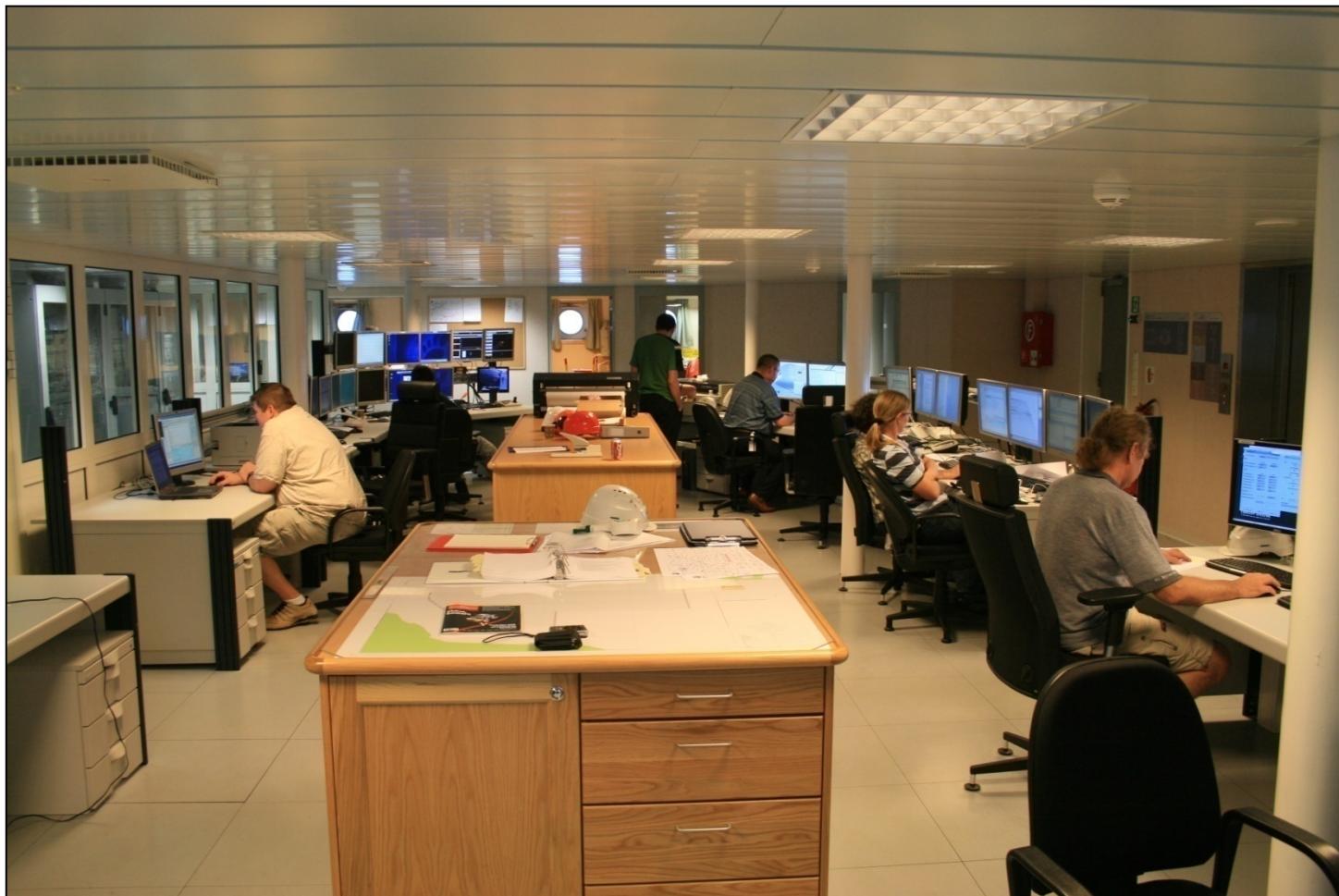
real shot gathers



lumley

david.lumley@utdallas.edu

marine vessel processing room

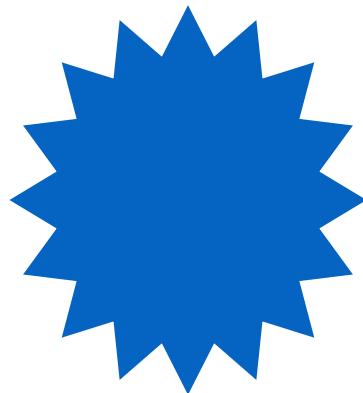


lindsey sharp, fugro

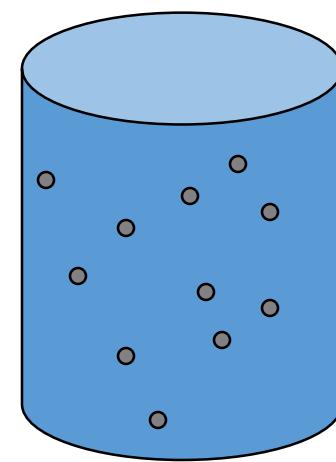


Rock and Fluid Physics

sponge



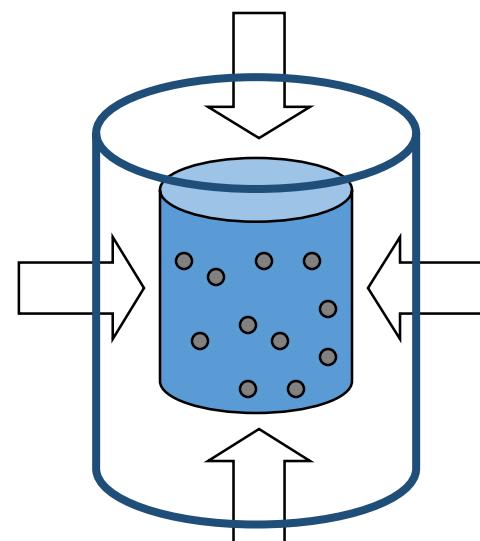
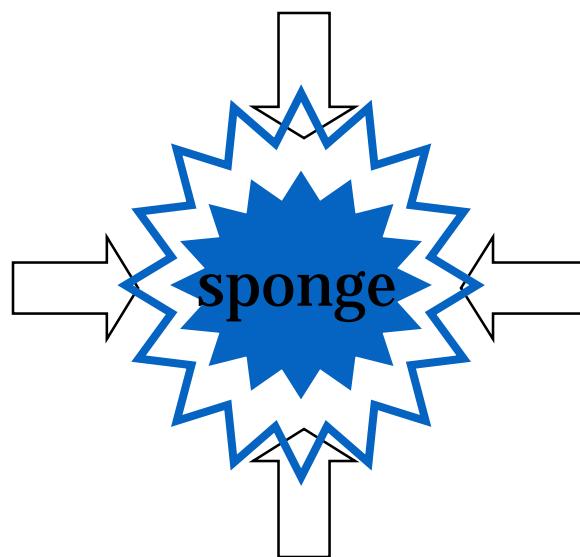
porous rock



Lumley

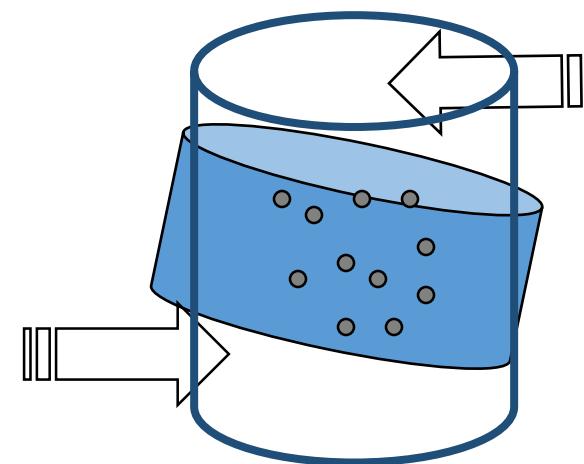
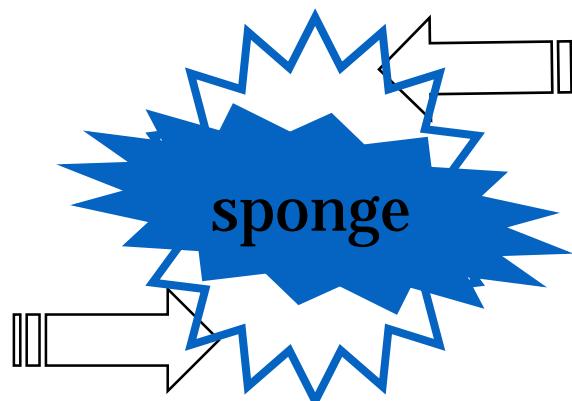
compression

- sensitive to rock compressibility
- sensitive to both pore fluids & pressure



shear

- sensitive to rock shear strength
- sensitive to pore pressure but not fluids



seismic velocity and impedance

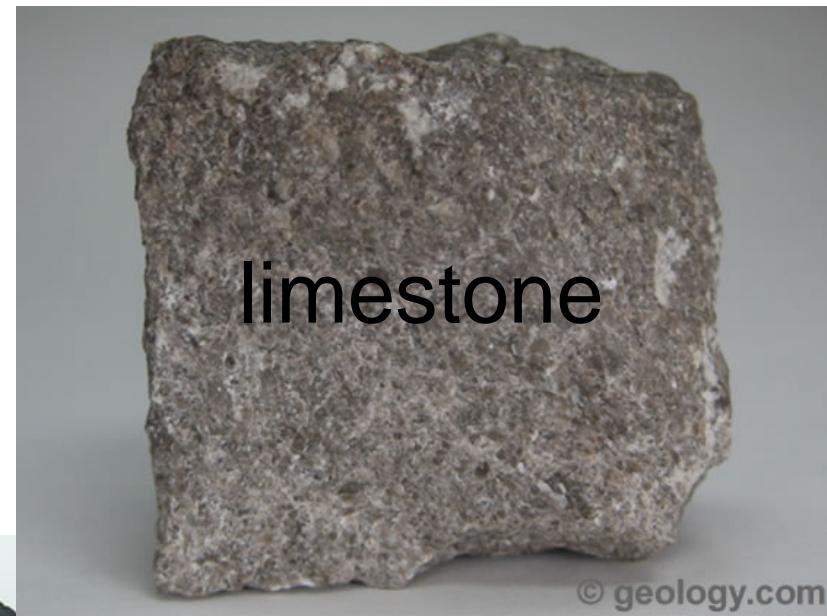
- Two types of velocity: v_p and v_s

- P-waves $v_p = \alpha = \sqrt{ (K + 4G/3)/\rho }$
- S-waves $v_s = \beta = \sqrt{ G/\rho }$

- $Z = \text{impedance} = \text{velocity} * \text{density} = v * \rho$

- $K = \text{bulk modulus (stiffness)} = \lambda + 2\mu/3$
- $G = \text{shear modulus (shear strength)} = \mu$
- $\rho = \text{density}$

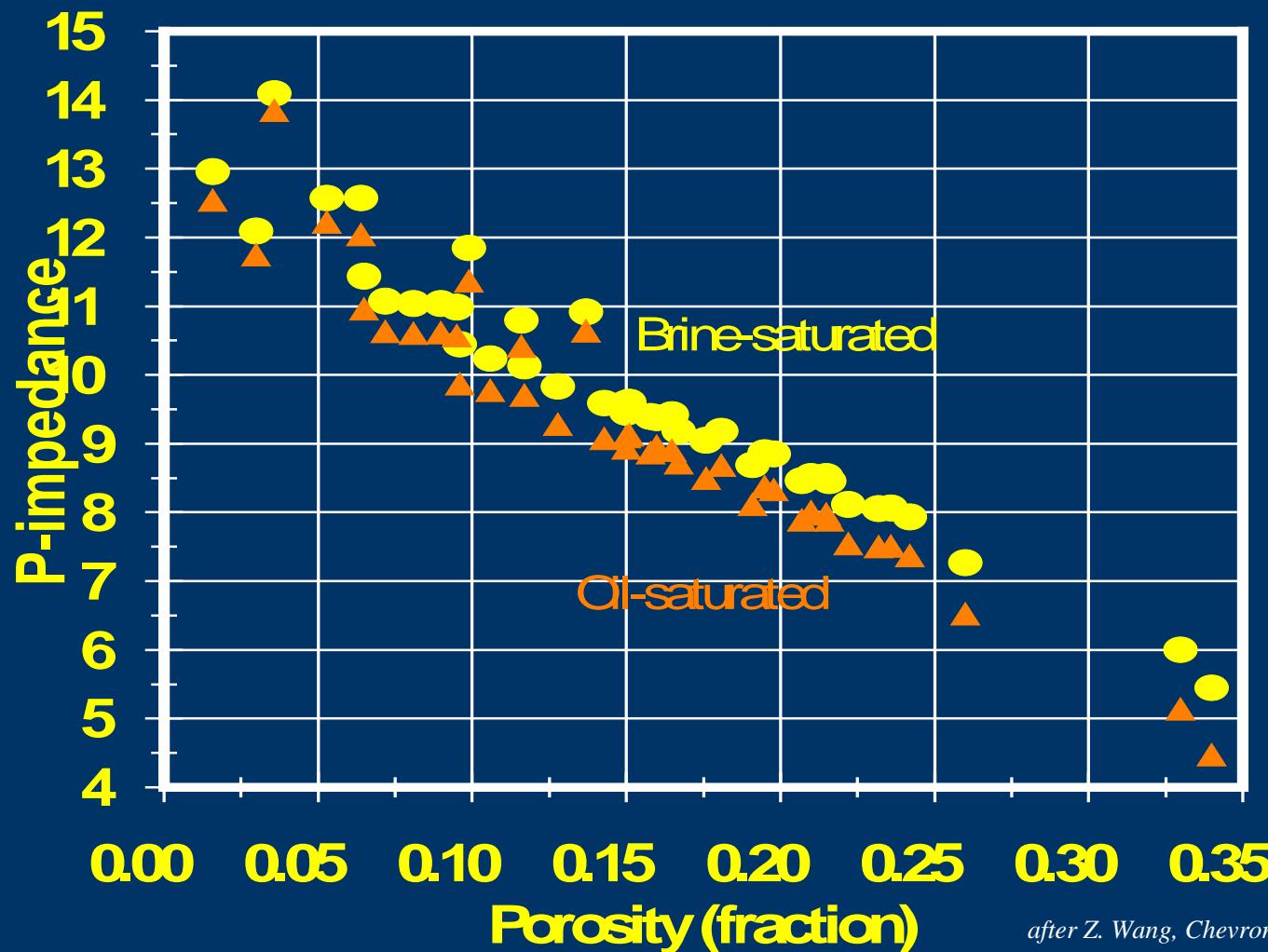
sedimentary rocks



hydrocarbon reservoirs

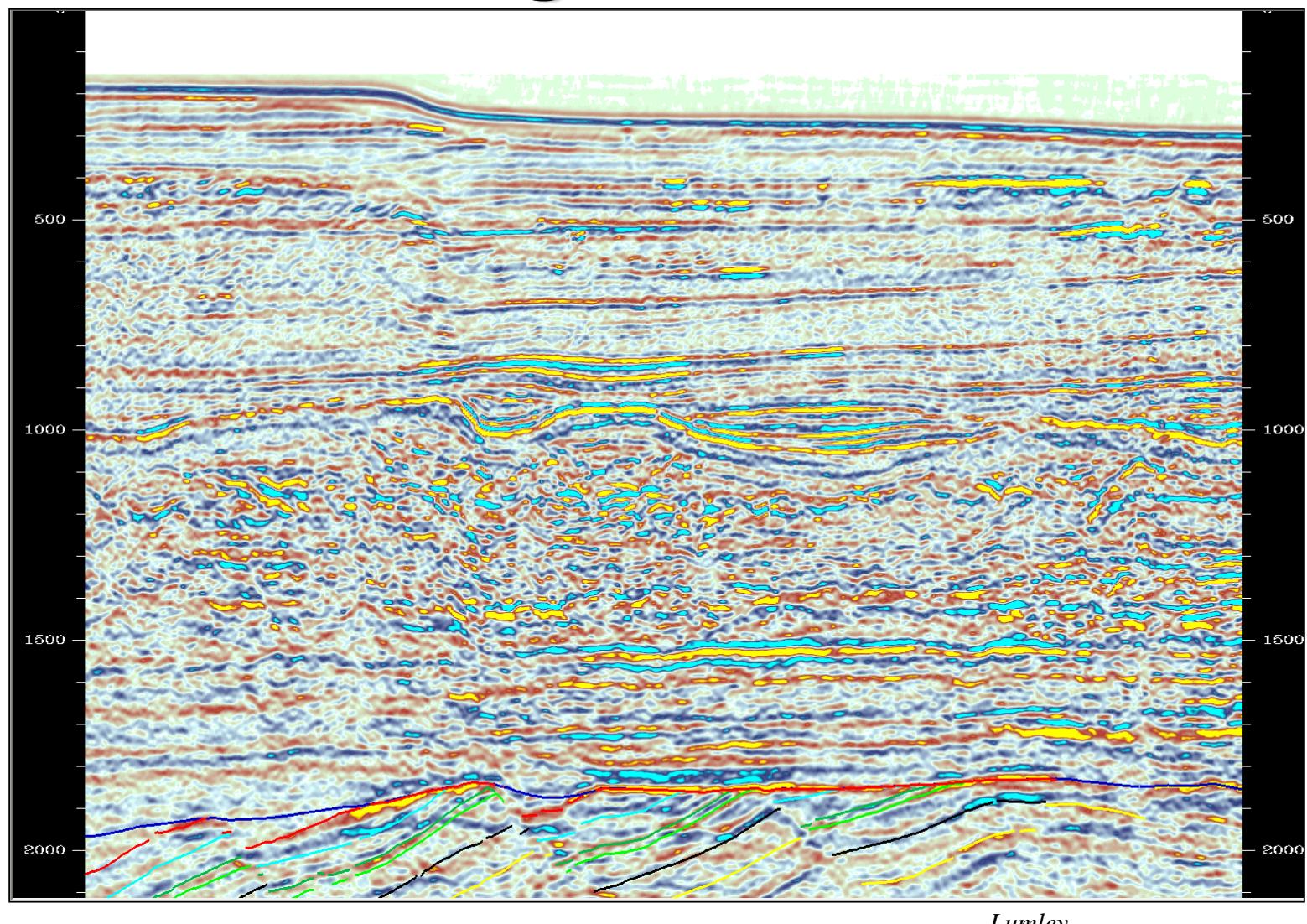
- sediments deposited into oceans
- sediments contain organic material (plant matter)
- buried, compressed and cooked in earth
 - **coal** *formed at low P, low T*
 - **oil** *formed at med P, med T, ie. the “oil window”*
 - **gas** *formed under various P,T conditions*
- rock pores contain fluids (**water**, **oil**, **gas**...)

Gulf Coast and Alaska Sand Samples

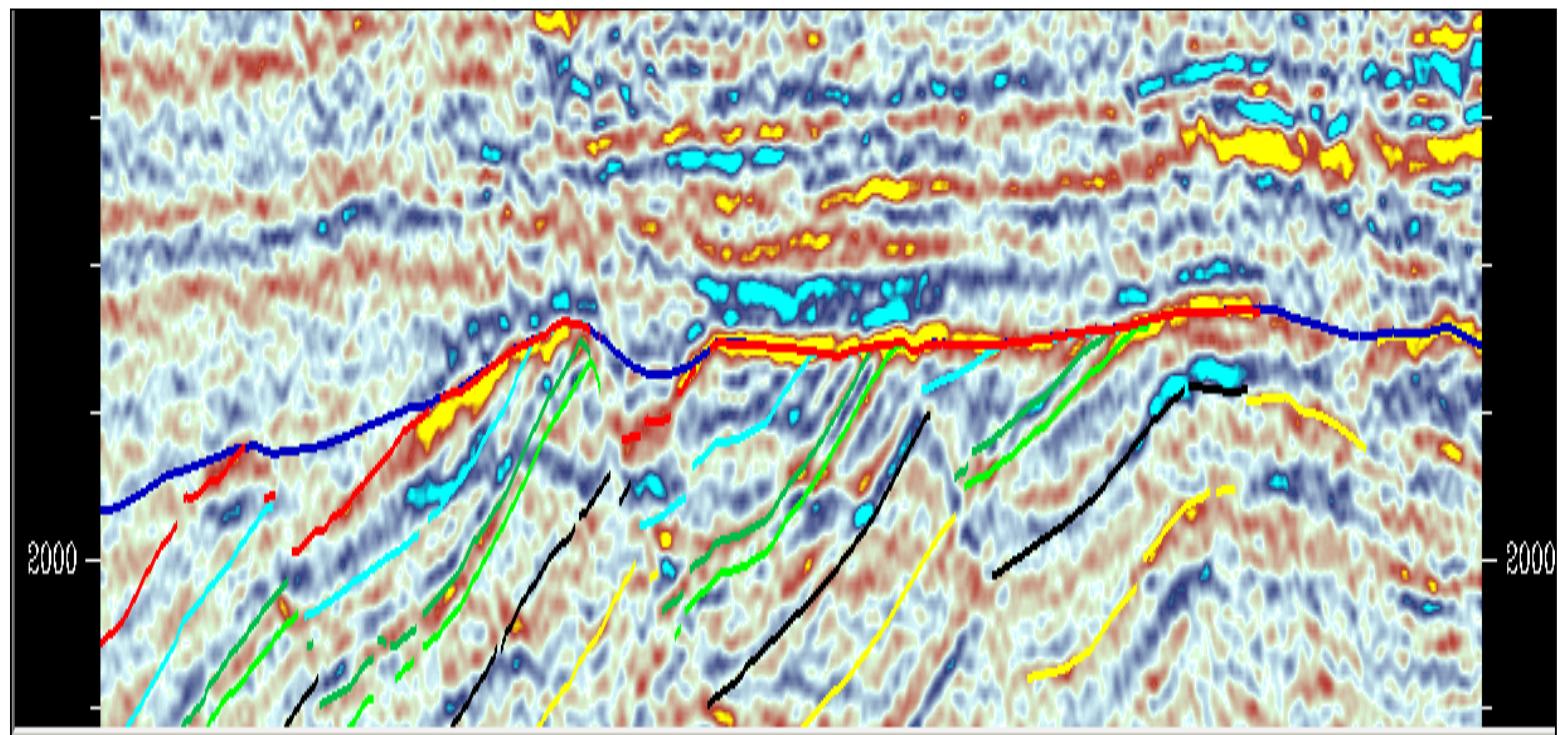


after Z. Wang, Chevron

Seismic Image – 2D cross-section

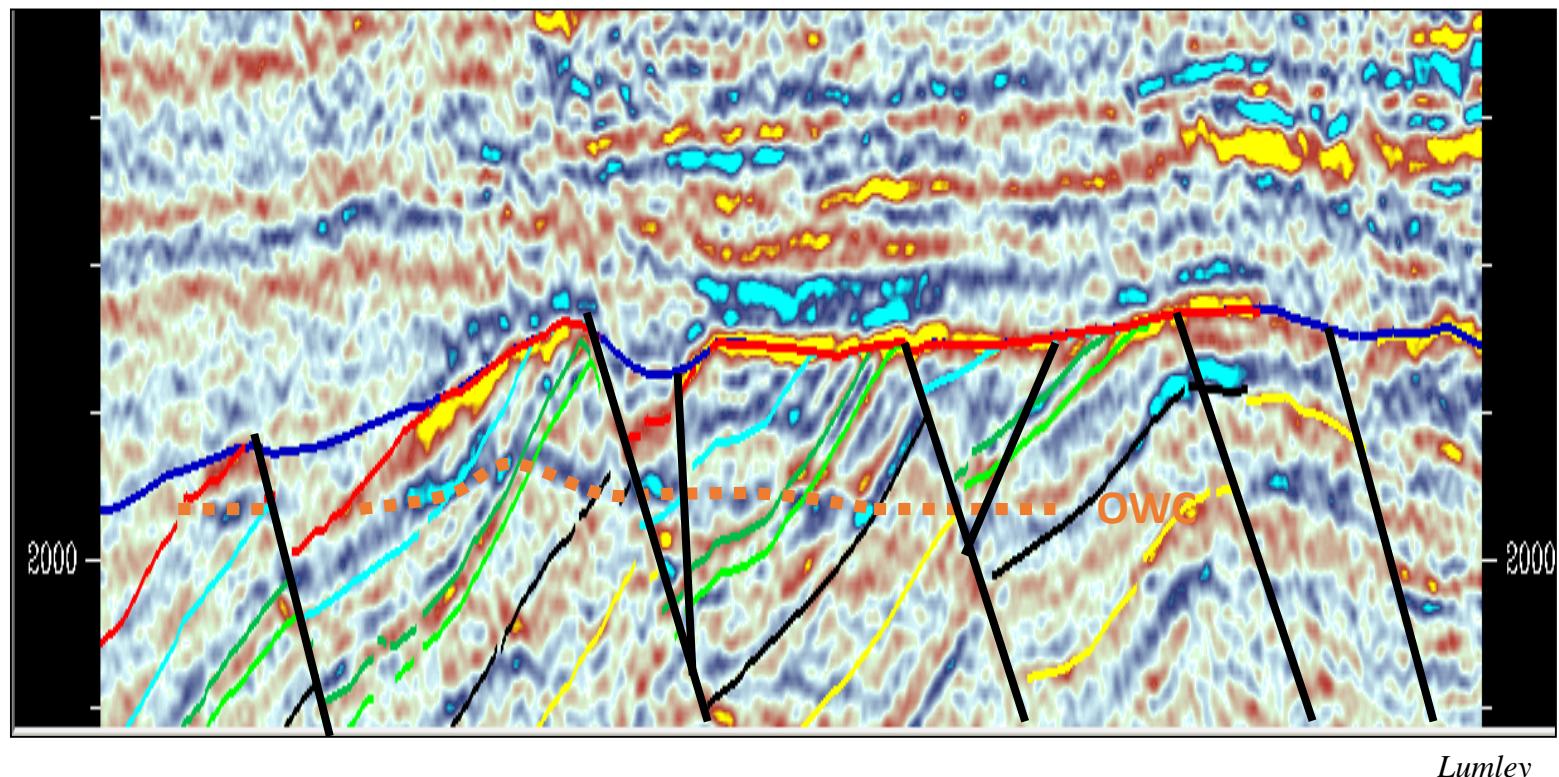


Seismic Image – *zoom on reservoirs*

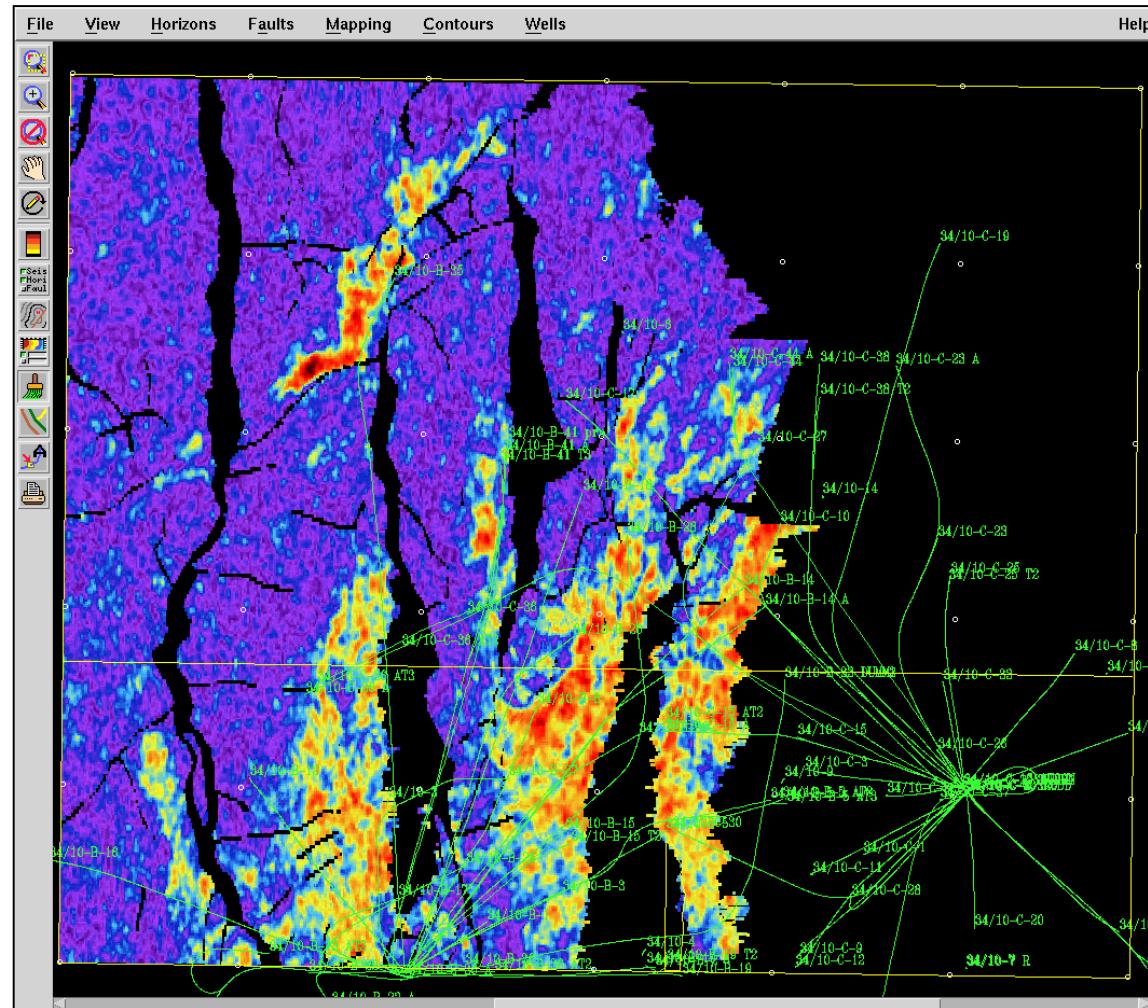


Lumley

Seismic Image – *zoom on reservoirs*

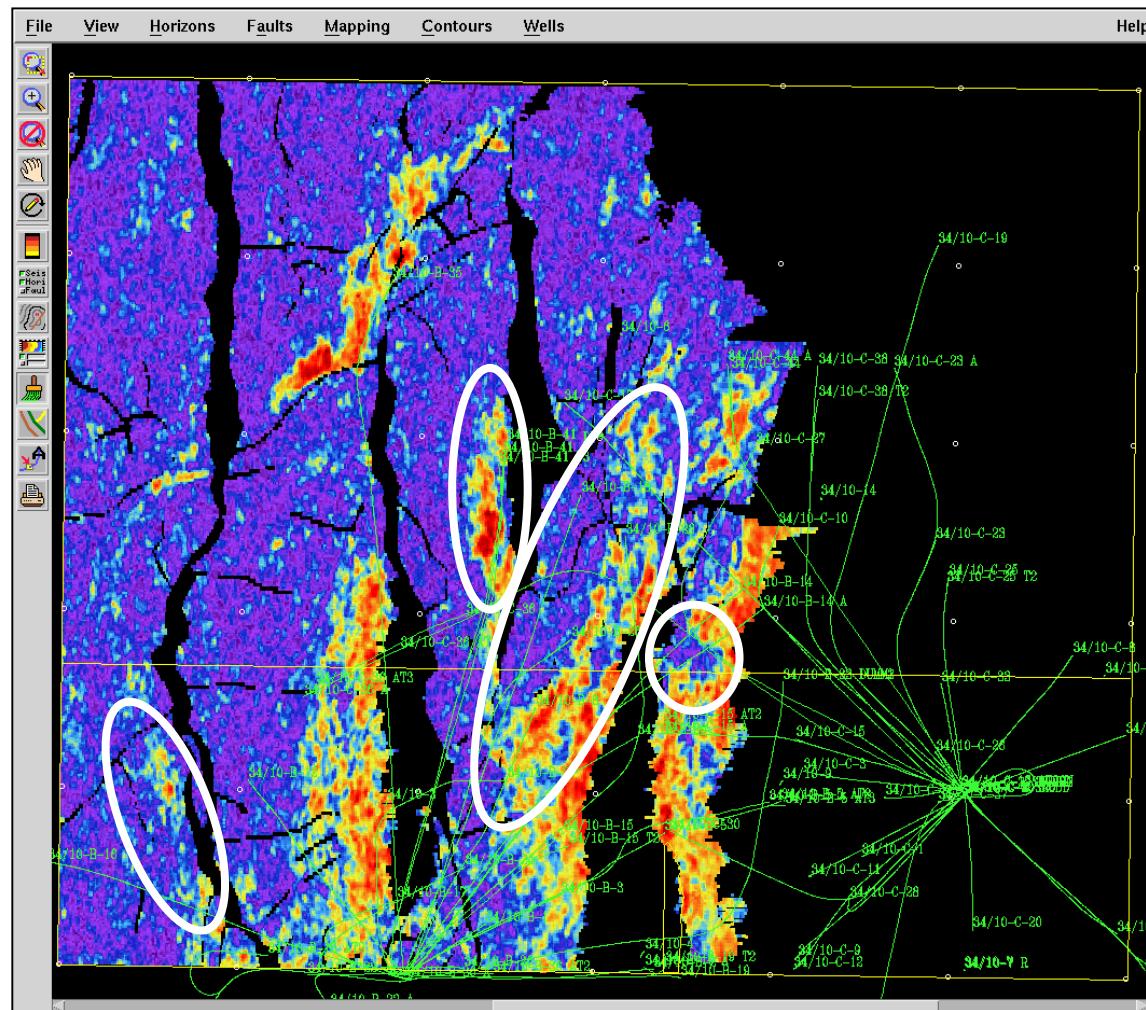


Seismic Image – 3D amplitude map extracted along top of reservoir structure



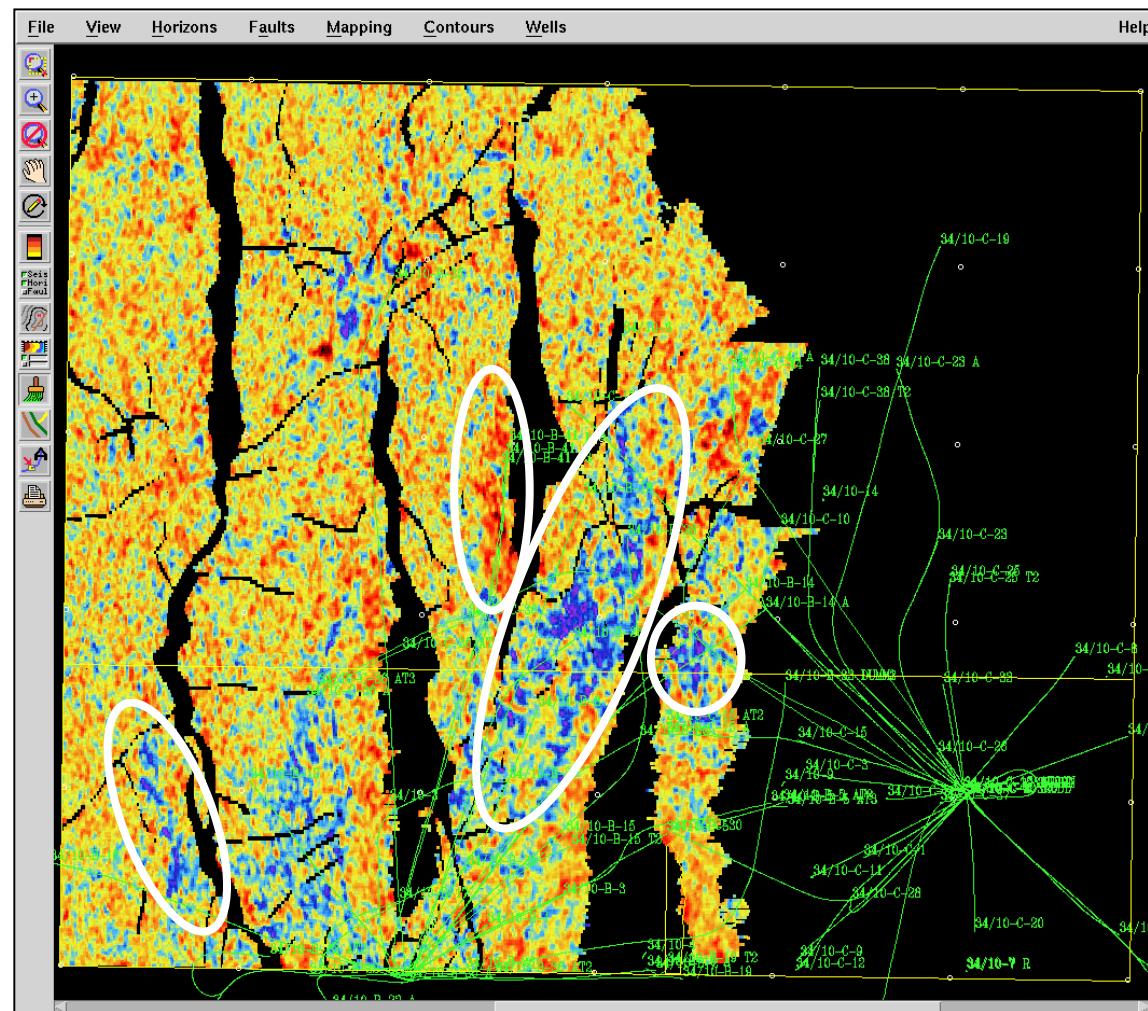
Lumley

Seismic Image – TIME 2 amplitude map extracted along top of reservoir structure



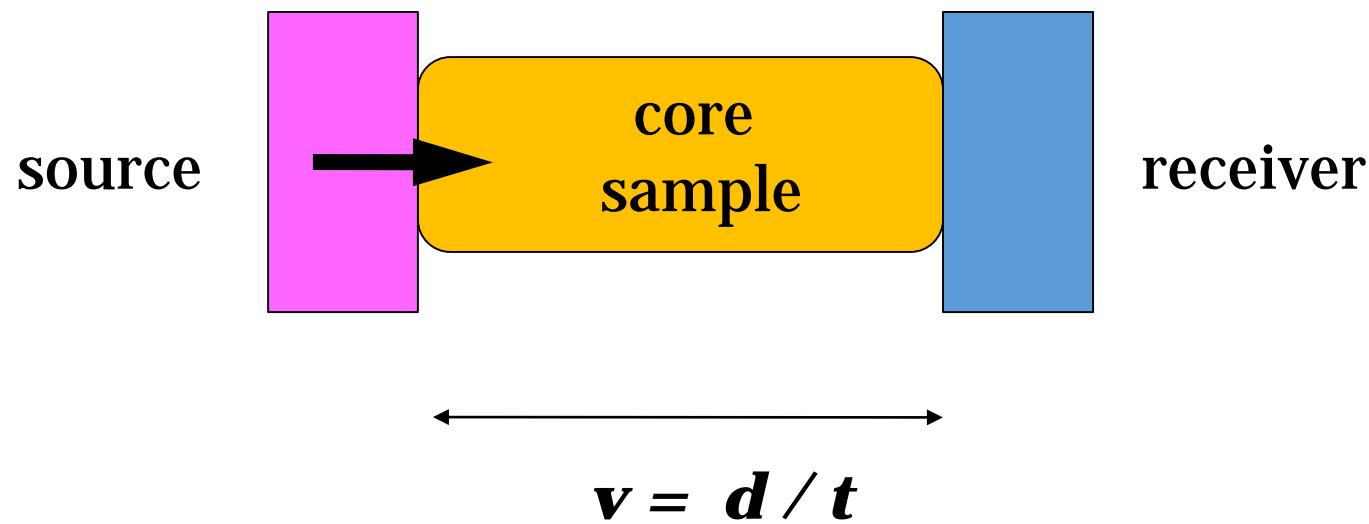
Lumley

Seismic Image – 4D difference map extracted along top of reservoir structure



Lumley

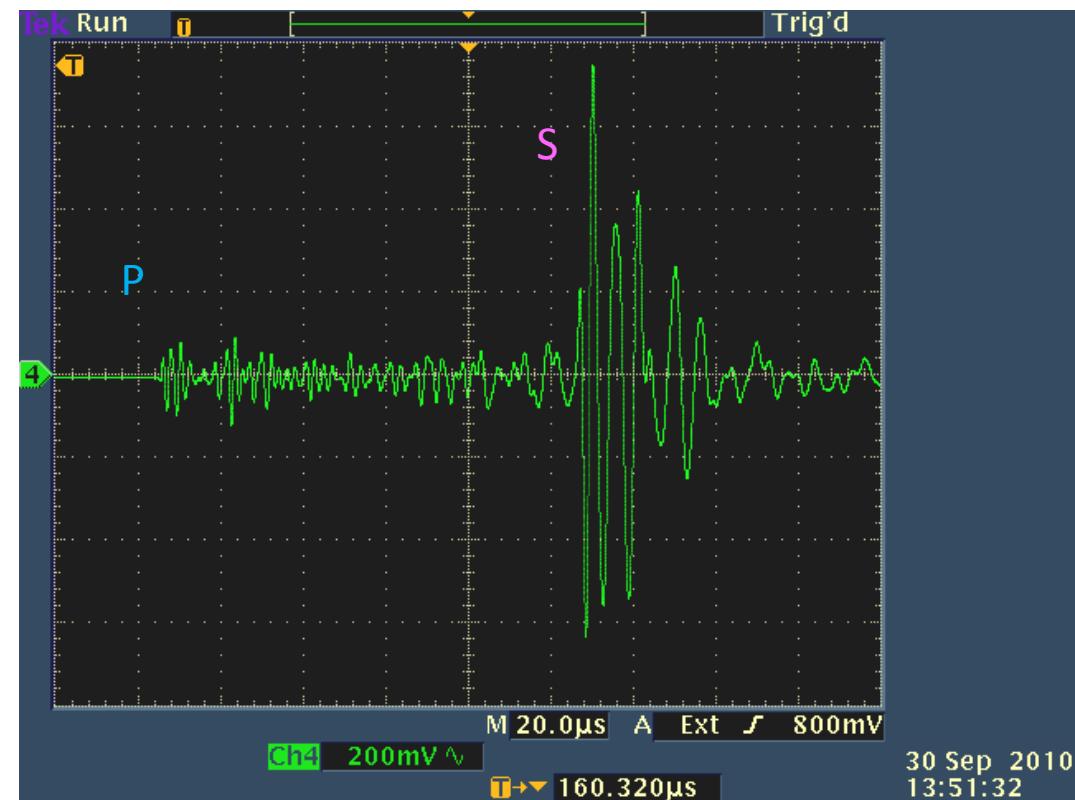
Rock Physics core measurements



rock physics lab



Curtin University



M. Lebedev, Curtin

Velocity Equations

$$V_p = \sqrt{\frac{K + \frac{4}{3}G}{\rho}}$$

P-wave velocity

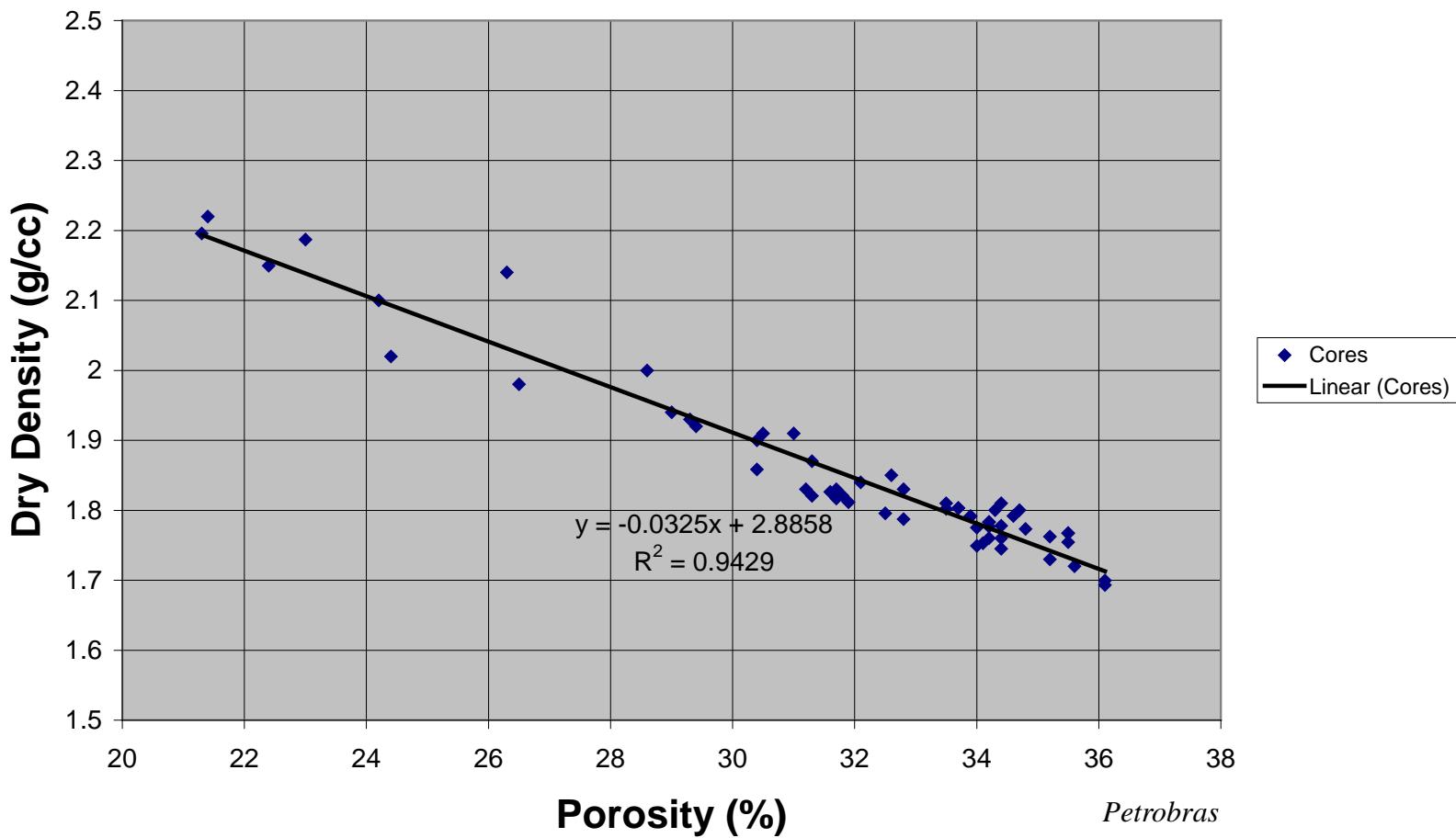
$$V_s = \sqrt{\frac{G}{\rho}}$$

S-wave velocity

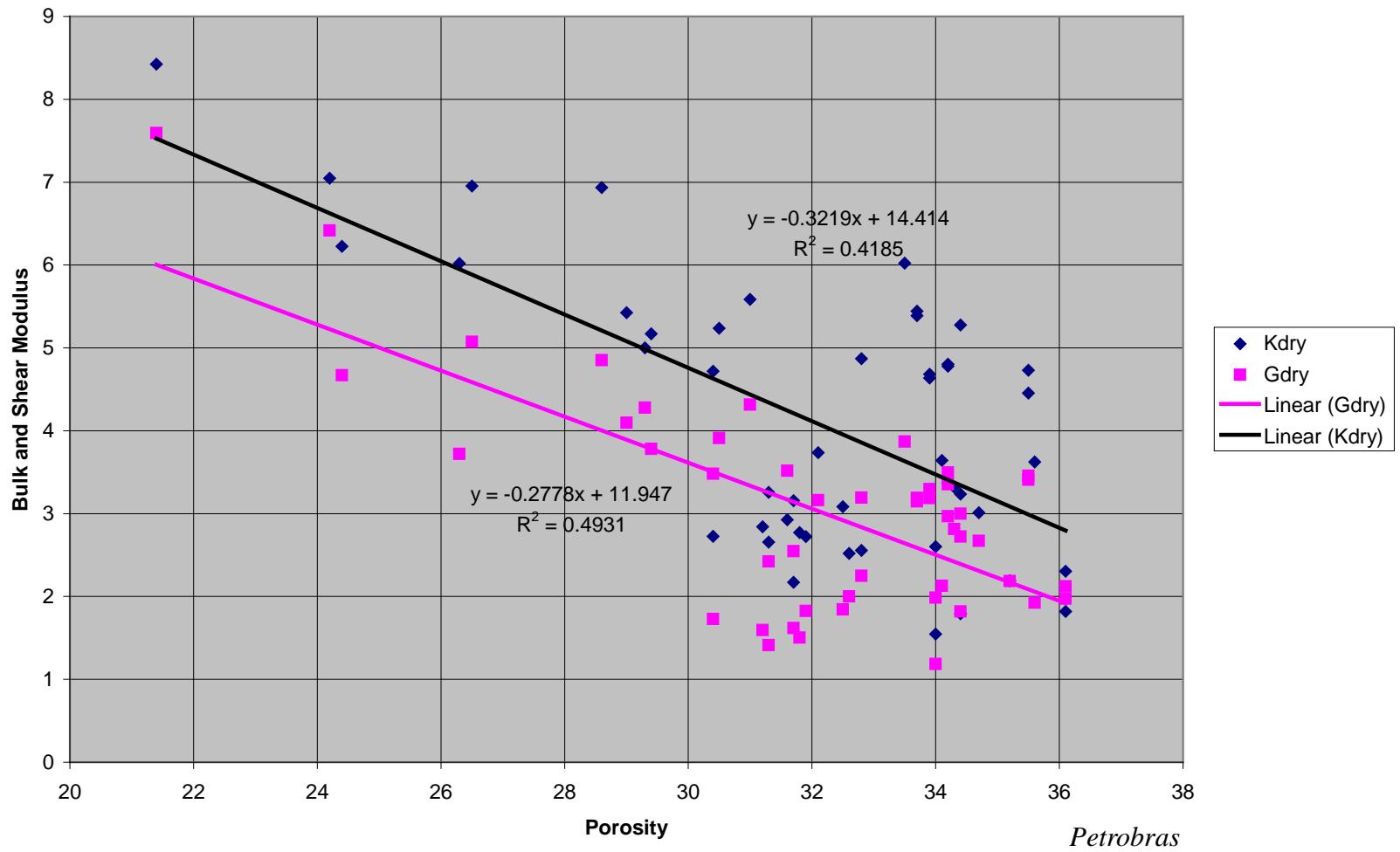
$$I_p = \rho * V_p$$

P-wave impedance

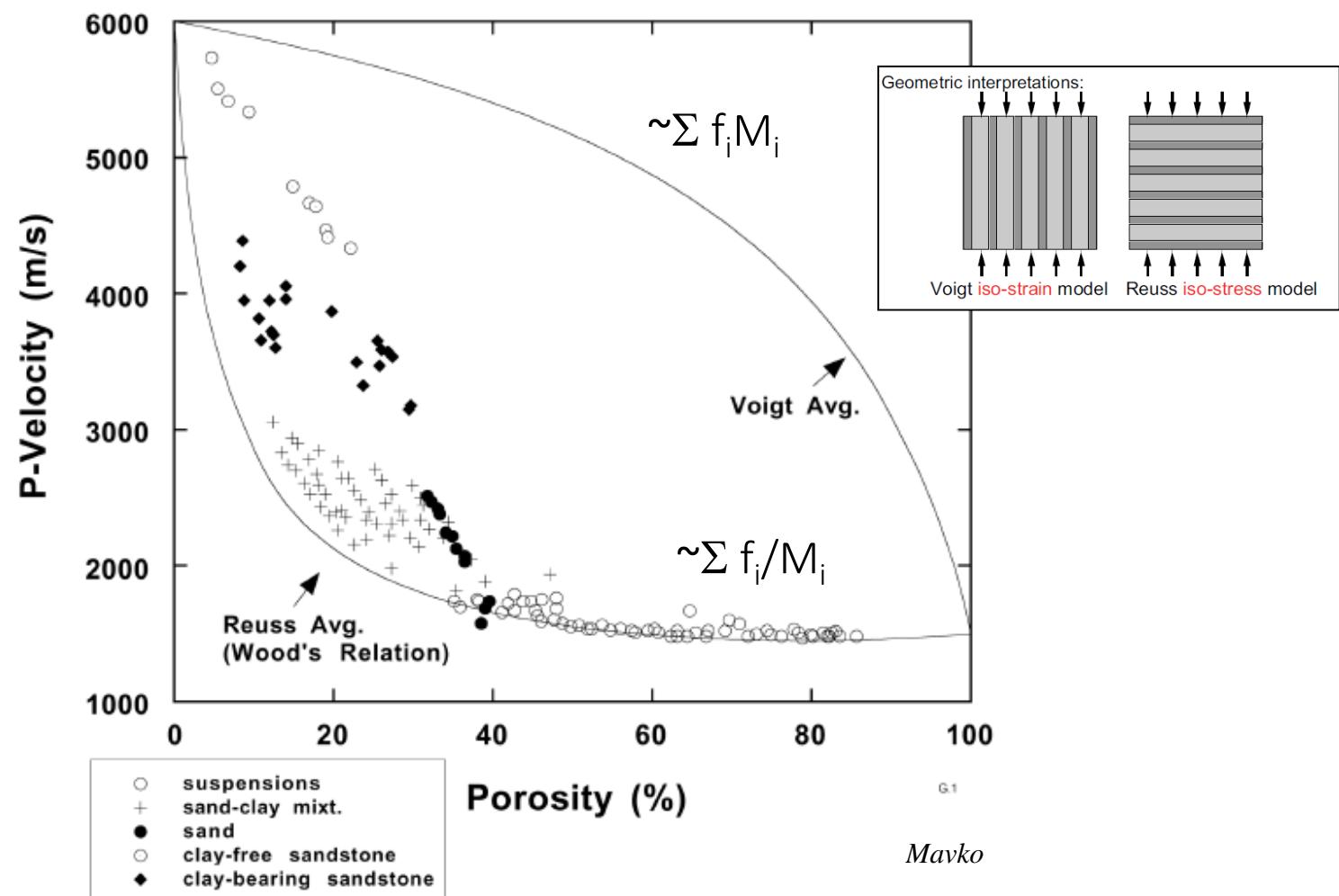
Density versus ϕ



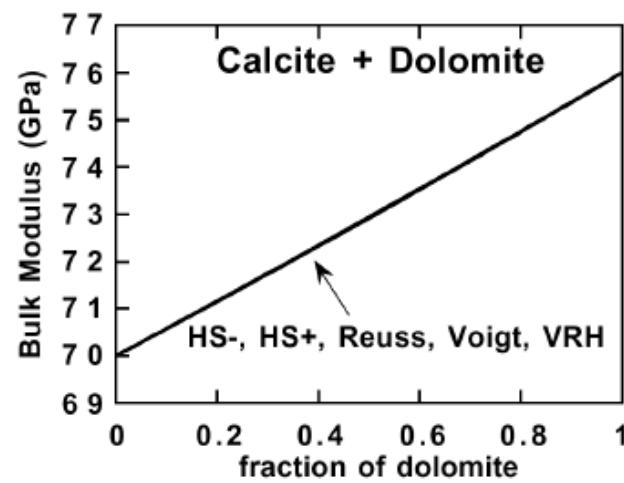
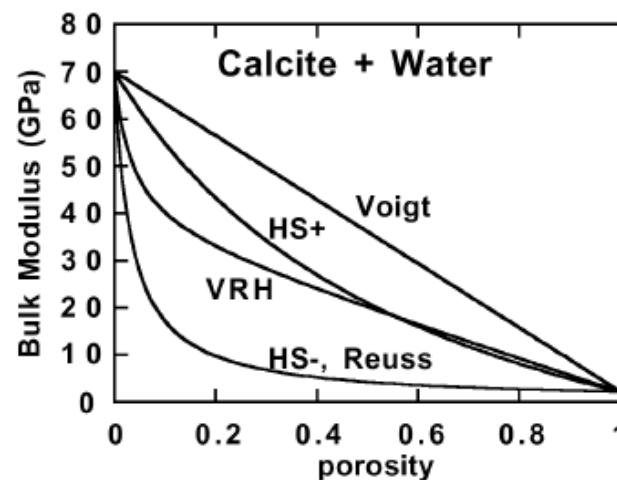
K, G versus ϕ



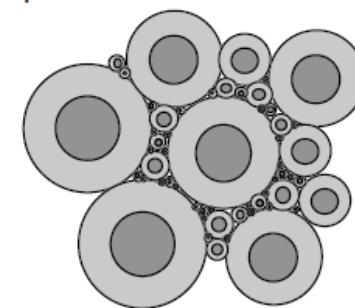
Voigt and Reuss bounds



Hashin-Shtrikman bounds



Interpretation of bulk modulus:



Mavko

Hashin-Shtrikman bounds

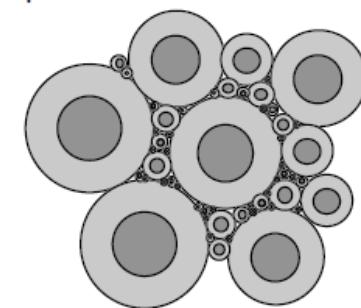
of 2 materials:

$$K^{HS\pm} = K_1 + \frac{f_2}{(K_2 - K_1)^{-1} + f_1 \left(K_1 + \frac{4}{3}\mu_1 \right)^{-1}}$$

$$\mu^{HS\pm} = \mu_1 + \frac{f_2}{(\mu_2 - \mu_1)^{-1} + \frac{2f_1(K_1 + 2\mu_1)}{5\mu_1 \left(K_1 + \frac{4}{3}\mu_1 \right)}}$$

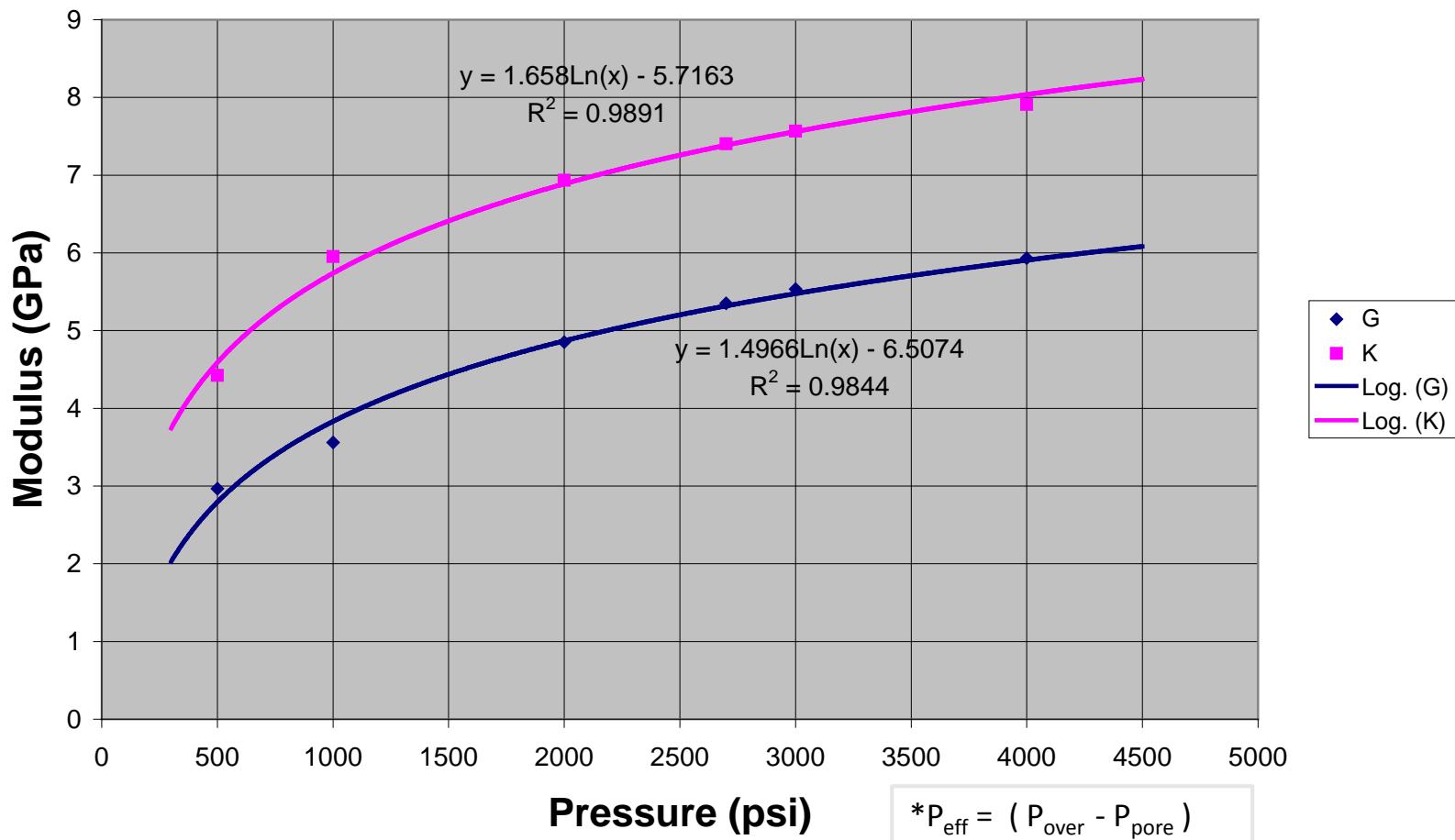
where subscript 1 = shell, 2 = sphere. f_1 and f_2 are volume fractions.

Interpretation of bulk modulus:



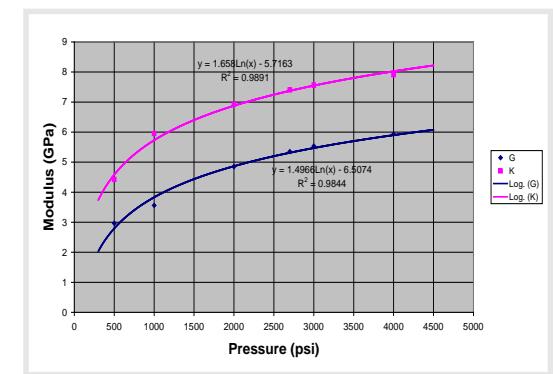
Mavko

K, G versus P_{eff} *



velocity-pressure curves

- Hertz-Mindlin...
 - $K_{dry} = f(\textcolor{blue}{c}, \varphi_c, K_g, G_g, P_{eff})^{1/3}$
 - *theoretical basis, but doesn't fit data in practice*
- Polynomial, Exponential...
 - $K_{dry} = c_o + c_1x + c_2x^2 + \dots + c_nx^n$; c_i coeffs ; $x = P_{eff}$
 - $V_{dry} = c_o + c_1x + c_2 e^{-ax}$; a, c_i coeffs ; $x = P_{eff}$
 - *Exponential fits data better than poly and has some theory basis*
- Logarithmic...
 - $K_{dry} = c_o + c_1 \ln(x)$; c_i coeffs ; $x = P_{eff}$
 - *Logarithmic fits data better than above, no theory basis (yet)...*



A new velocity-pressure model

$$\mathbf{K} = \mathbf{A} - \mathbf{B}e^{-CP_{eff}} - \mathbf{D}e^{-EP_{eff}}$$

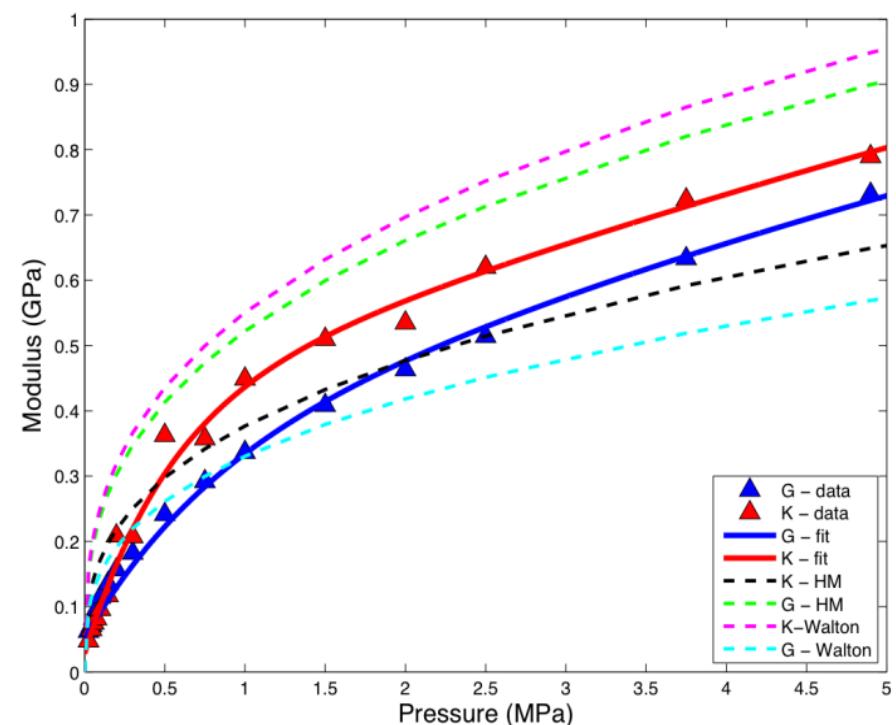
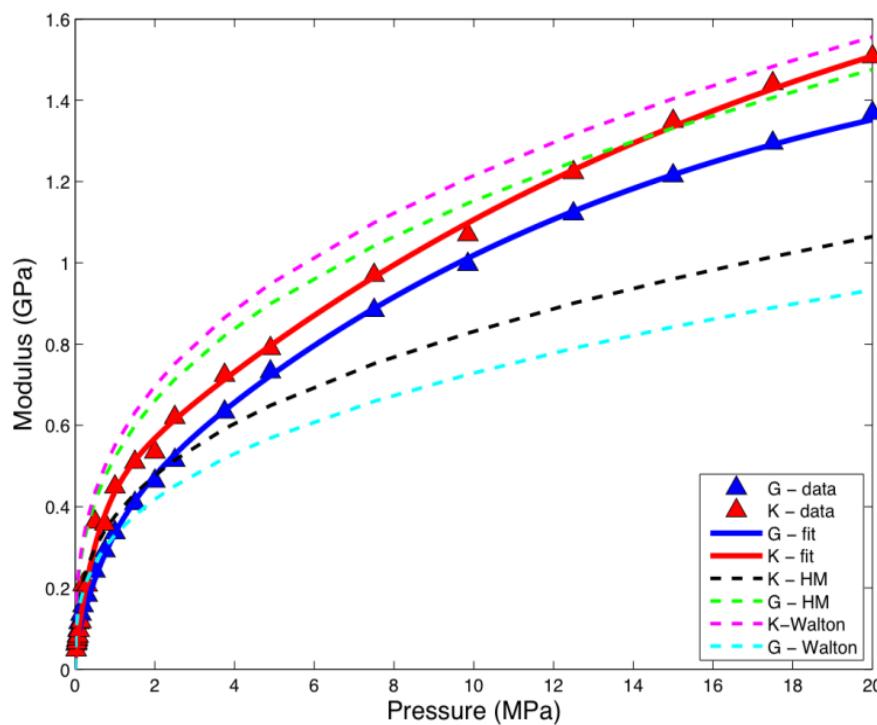
Saul & Lumley, GJI 2013

Where A, B, C, D and E are all positive constants,
with the constraint:

$$(\mathbf{A} - \mathbf{B} - \mathbf{D}) = \mathbf{K}(\mathbf{P}_{eff} = \mathbf{0}) \text{ calculated from: } K_{eff} = \left[\frac{\phi_c}{K_f} + \frac{1 - \phi_c}{K_m} \right]^{-1}$$

Fit to core data...

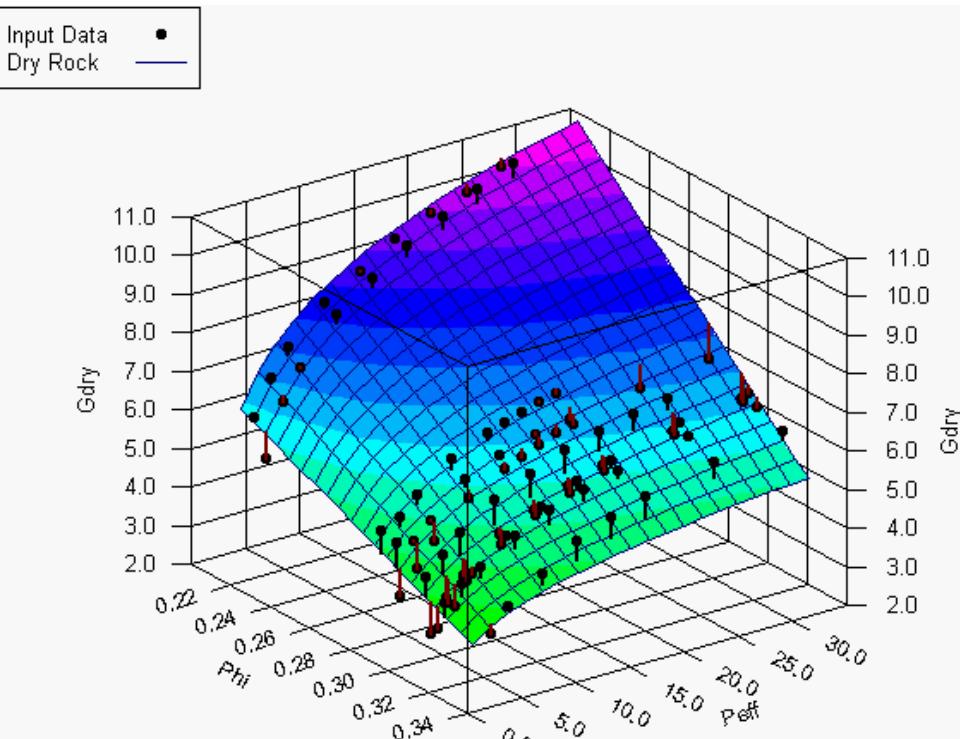
Bulk and Shear moduli – SL, HM, Walton smooth



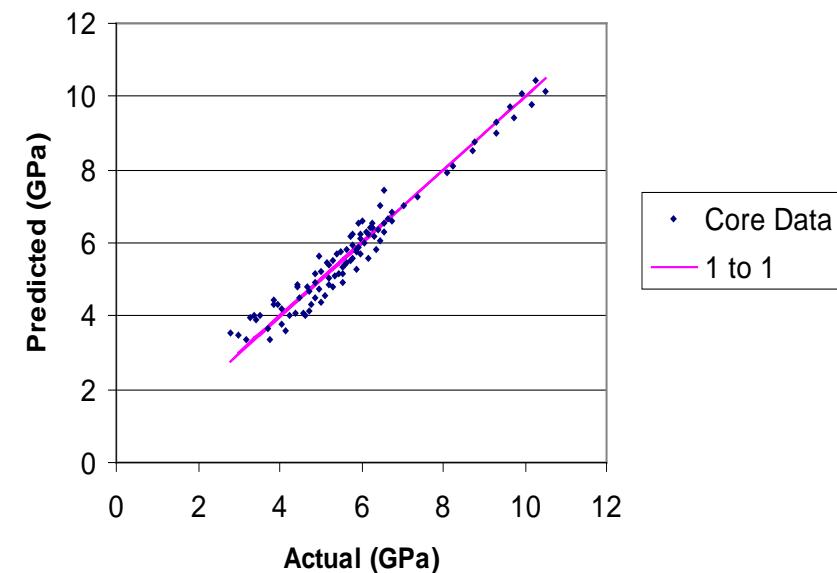
Saul & Lumley, 2011

For Contact models - ϕ_c variable, $C = 20 - 34 \phi + 14 \phi^2$ (Murphey, 1982), $\alpha = 0,1$

2D surface fit for $G_{dry}(f, P_{eff})$



Shear Modulus (log)
Schiehallion ($r^2 = 0.952$)



Meadows *et al.*, 2005

Fluid properties vary with P,T

* PVT data; * Empirical, eg. Batzle & Wang (1992); * Equations of State...

eg. Span-Wagner, GERG-2004 etc.

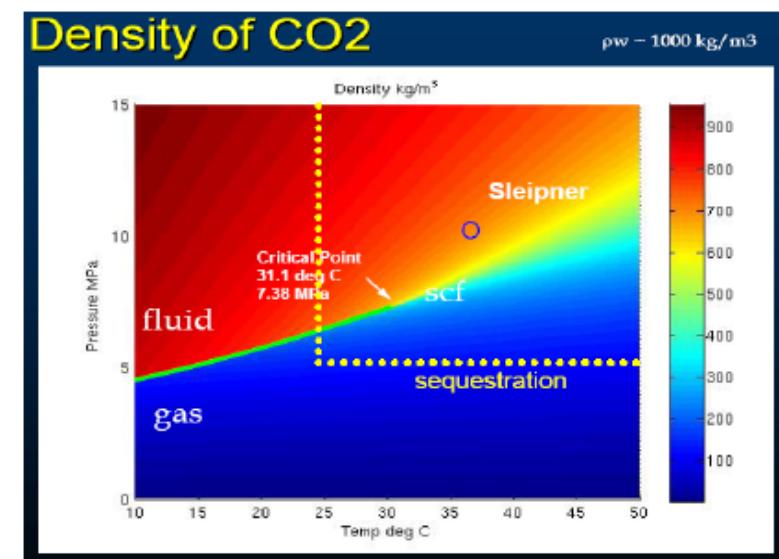
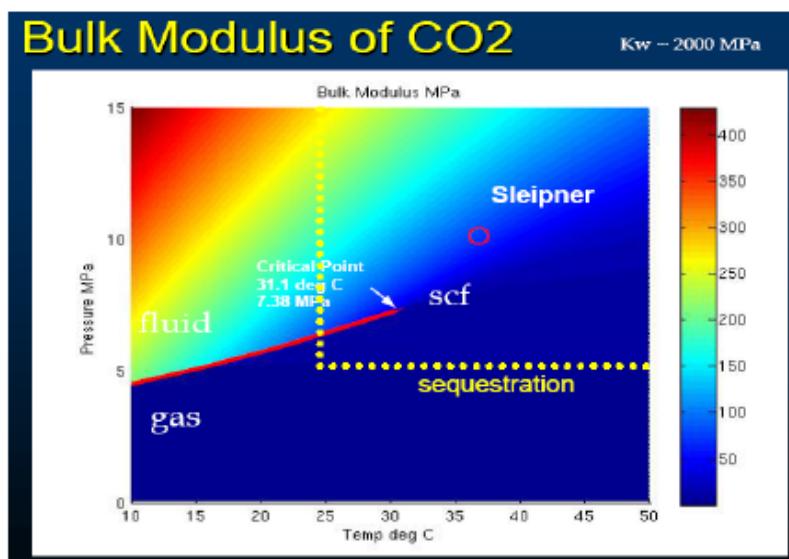


Figure 1: (a) Bulk modulus (left) and (b) density (right) of CO₂ under various pressure and temperature conditions (Lumley et al., 2008).

Lumley

Fluid mixing equations

Wood's equation:

$$1/K_{fluid} = \sum S_i / K_i$$

Effective fluid modulus

S_i is the i^{th} fluid saturation
such that $\sum S_i = 1$
 K_i is the i^{th} fluid modulus
 ρ_i is the i^{th} fluid density

Note: (S_i/K_i) averaging leads to the Reuss lower bound
 $(S_{i*}K_i)$ averaging leads to the Voigt upper bound

$$\rho_{sat} = \rho_{dry} + \phi \sum S_i \rho_i$$

Bulk density

Lumley

Gassmann Equation

Gassmann Equation:

$$K_{sat} = K_{dry} + A/B$$

Saturated bulk modulus

$$A = (1 - K_{dry}/K_m)^2$$

K_m is the matrix (grain) modulus
 ϕ is the porosity

$$B = \frac{\phi}{K_{fluid}} + \frac{1-\phi}{K_m} - \frac{K_{dry}}{(K_m)^2}$$

K_{fluid} is the effective fluid modulus

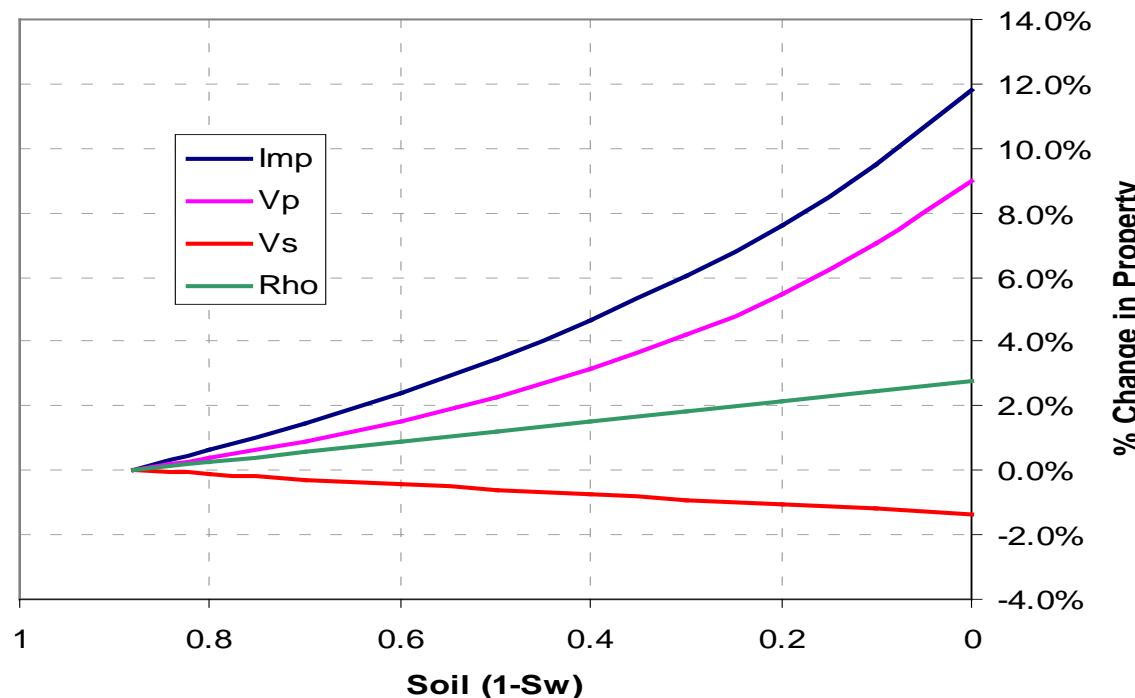
$$G_{sat} = G_{dry}$$

Shear modulus

Lumley

Velocity-saturation curves

Change in Seismic Properties with Water Flooding
Constant Pore Pressure



Lumley *et al.*

Patchy Saturation

Hill's equation:

$$1/M_{patchy} = \sum S_i/M_i$$

Patchy rock modulus

S_i is the i^{th} fluid saturation
such that $\sum S_i = 1$

$$M_i = K_{i(sat)} + 4G/3$$

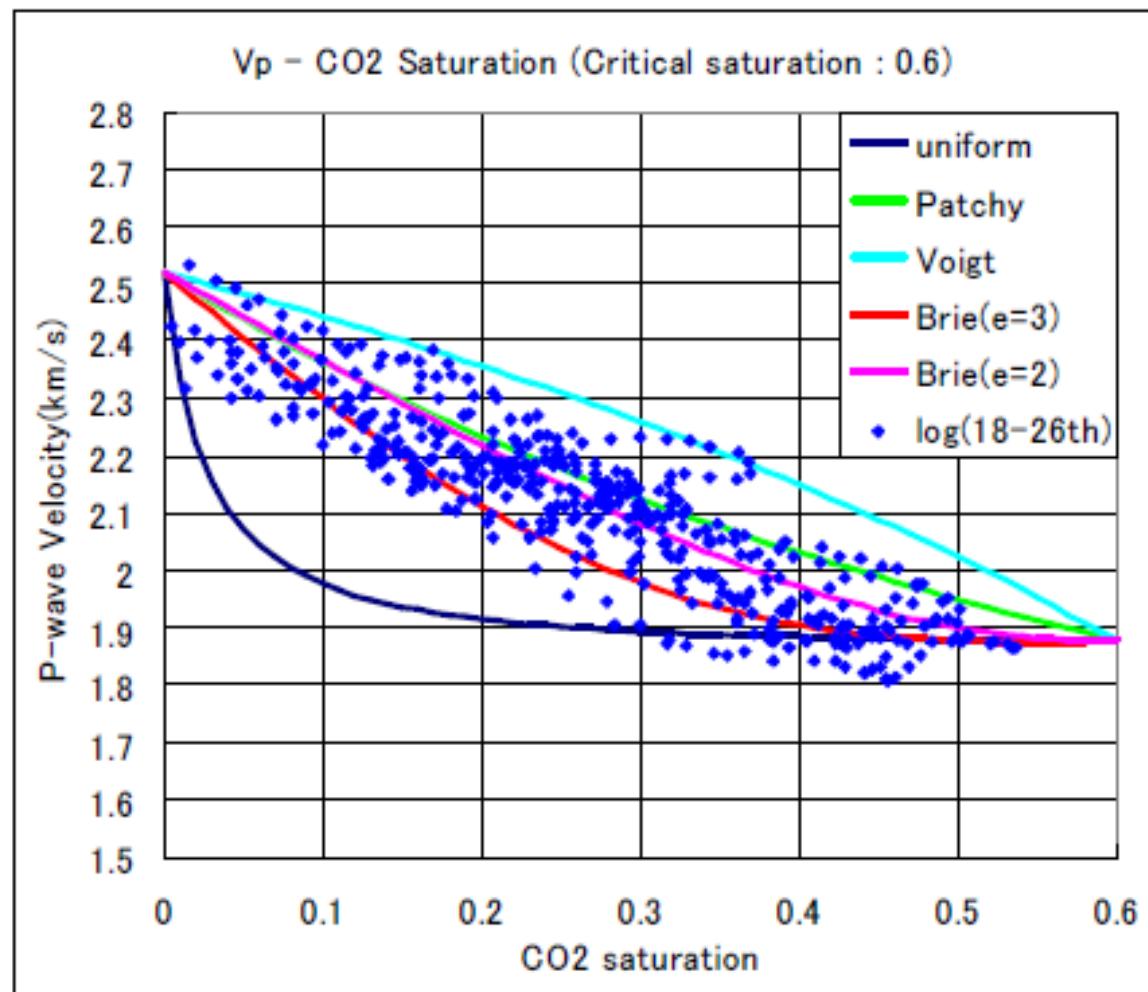
Effective rock modulus

M_i is the i^{th} rock modulus
saturated with 100% fluid “ i ”.

Substitute M_{patchy} directly into V_p equation.
(i.e., no Gassmann involved).

Lumley

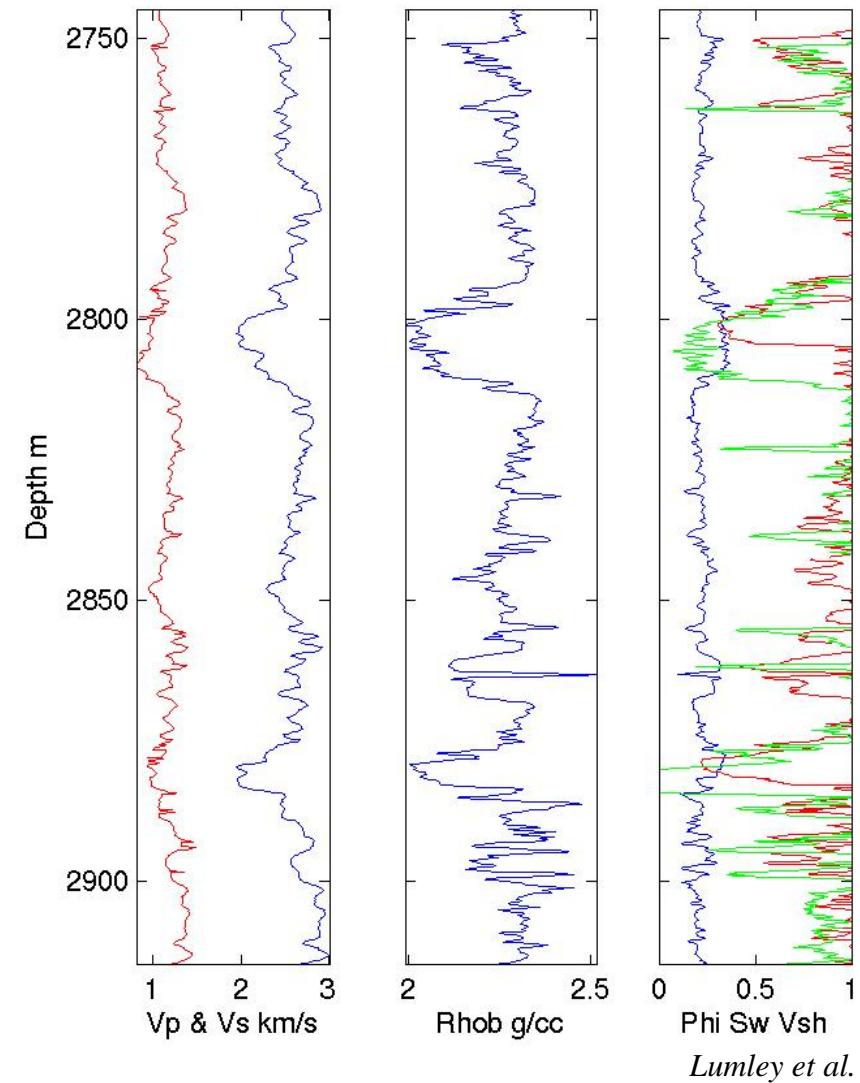
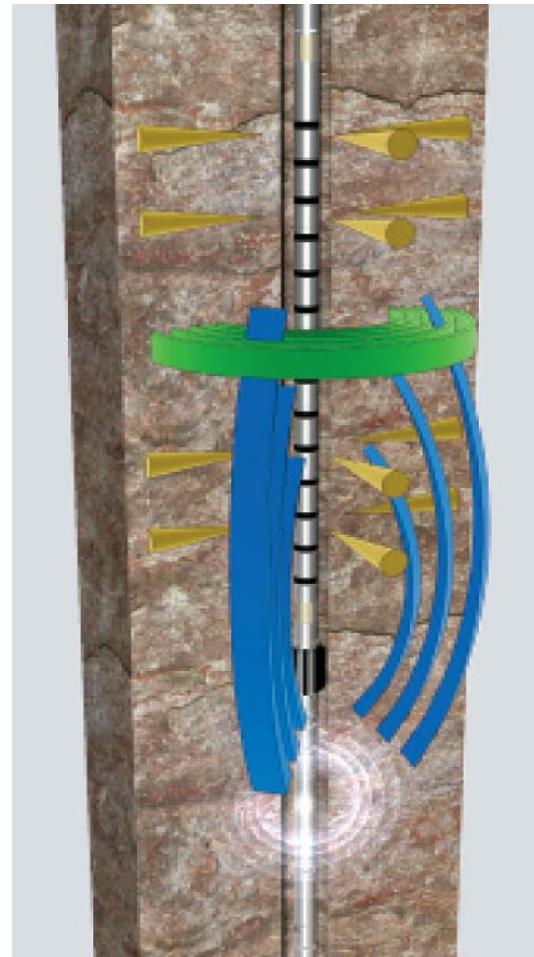
velocity-saturation curves



Konishi, OYO

Rock Physics properties from well logs

Seismic logging tools



Lumley et al.

Velocity Equations

well logs

$$V_p = \sqrt{\frac{K + \frac{4}{3}G}{\rho}}$$

P-wave velocity

$$V_s = \sqrt{\frac{G}{\rho}}$$

S-wave velocity

Velocity Equations

calculate

$$V_p = \sqrt{\frac{K + \frac{4}{3}G}{\rho}}$$

P-wave velocity

$$V_s = \sqrt{\frac{G}{\rho}}$$

S-wave velocity

Velocity Equations

inverse
Gassmann

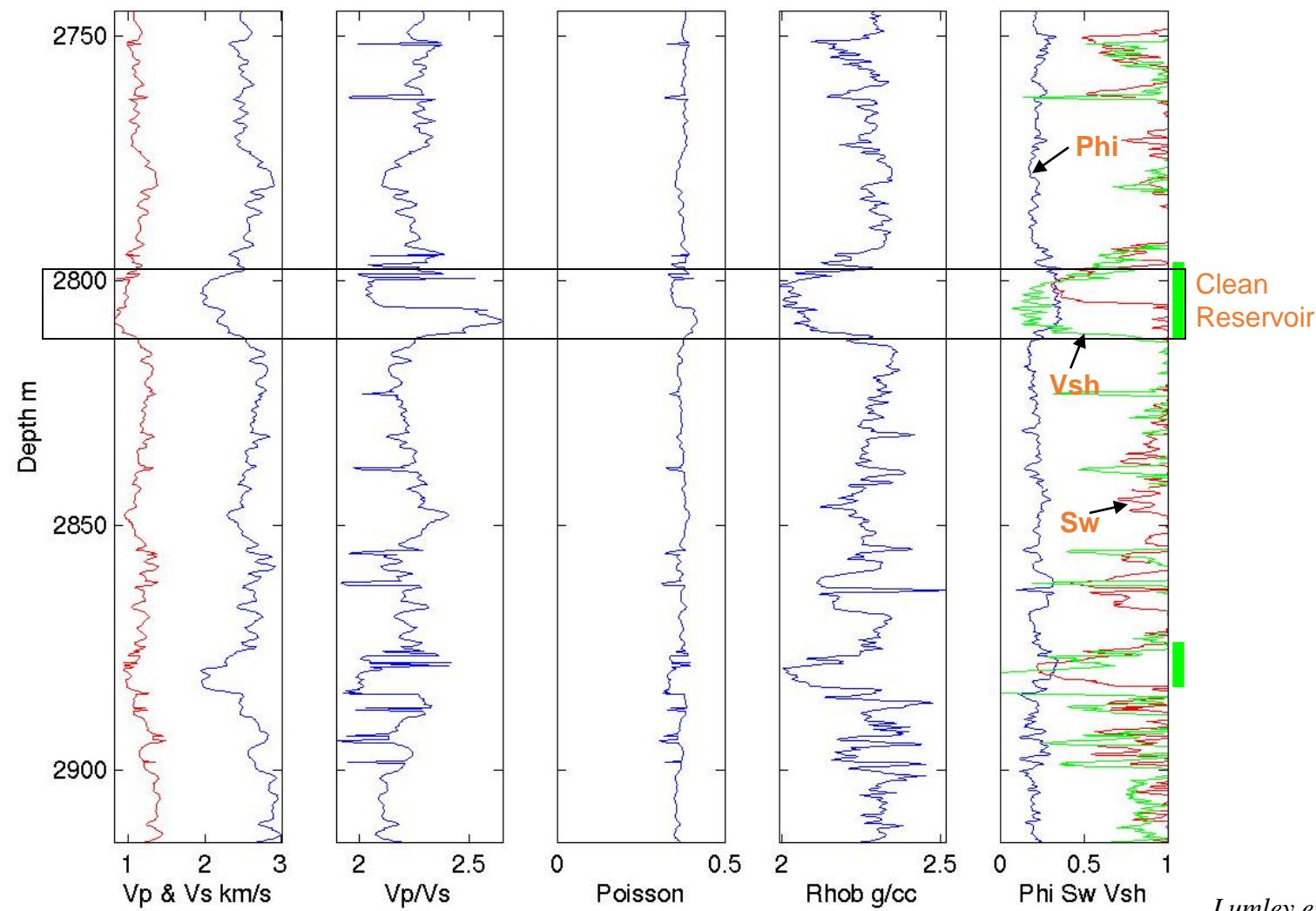
$$V_{P_{dry}} = \sqrt{\frac{K_d + \frac{4}{3}G}{\rho_d}}$$

P-wave velocity

$$V_{S_{dry}} = \sqrt{\frac{G}{\rho_d}}$$

S-wave velocity

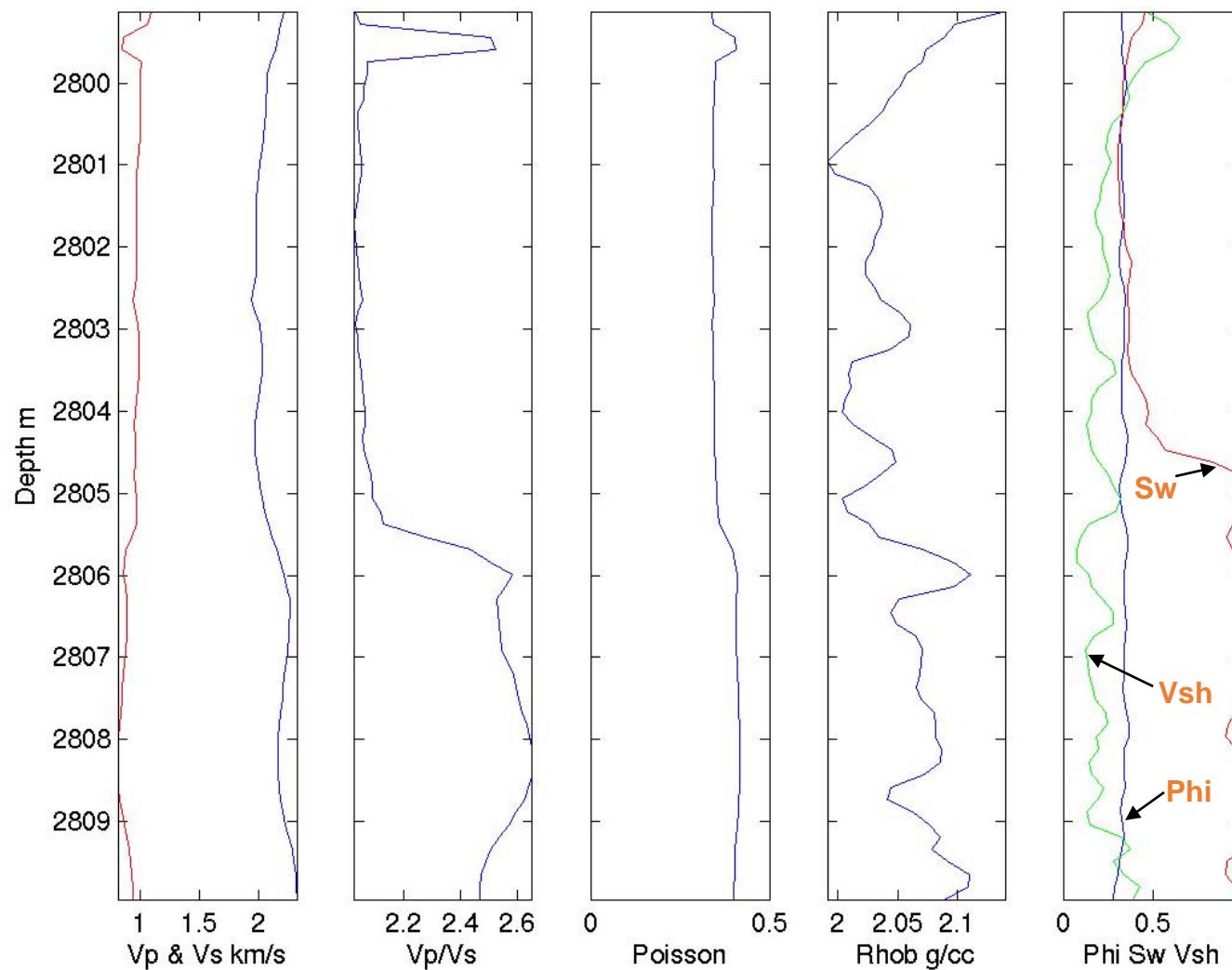
Well #1 logs... Full Reservoir Interval



Lumley et al.

Well #1 Zoom on Upper Reservoir Interval

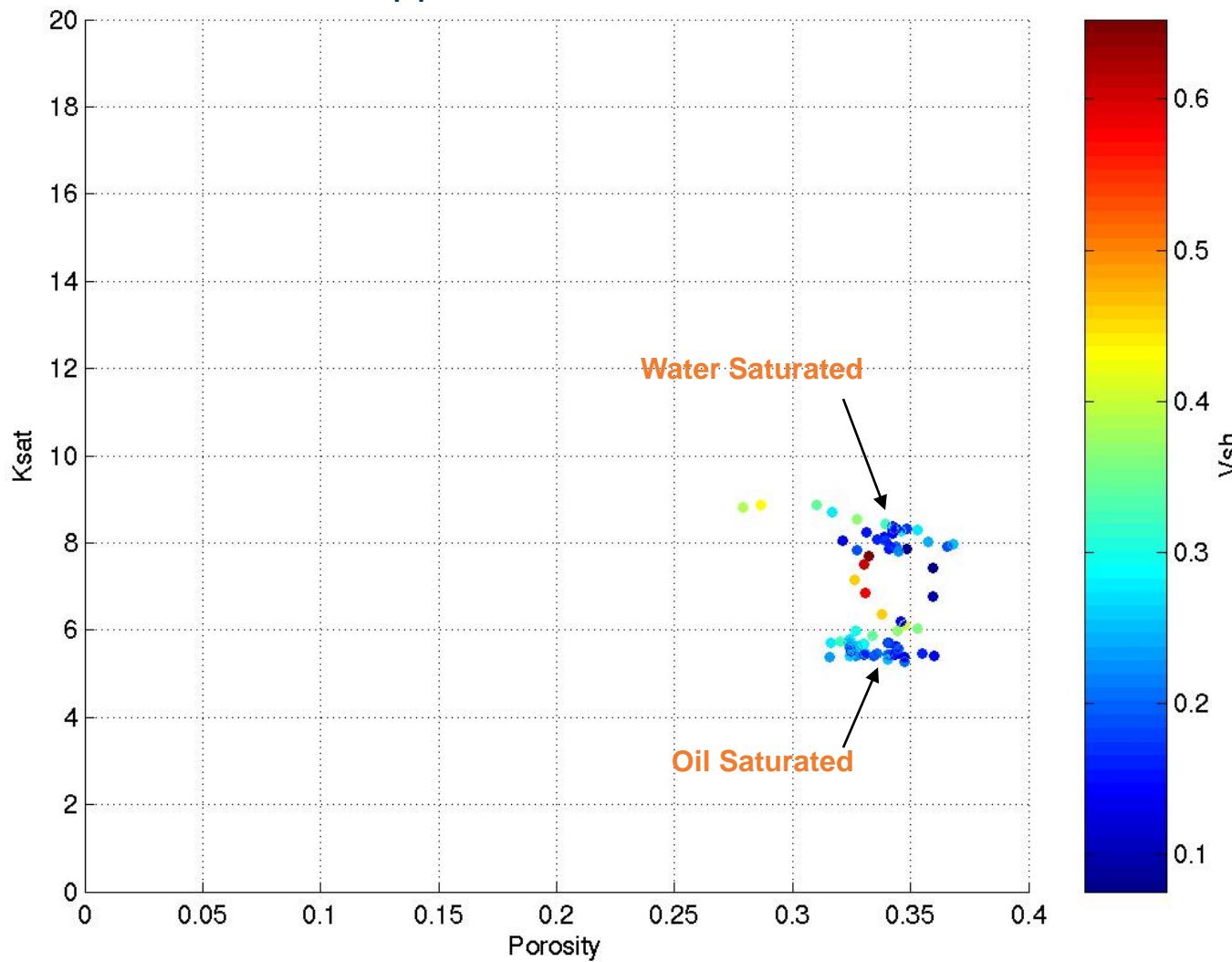
Upper Zone 2799 – 2810 m



Lumley et al.

Well #1 Ksat... Upper Reservoir Interval

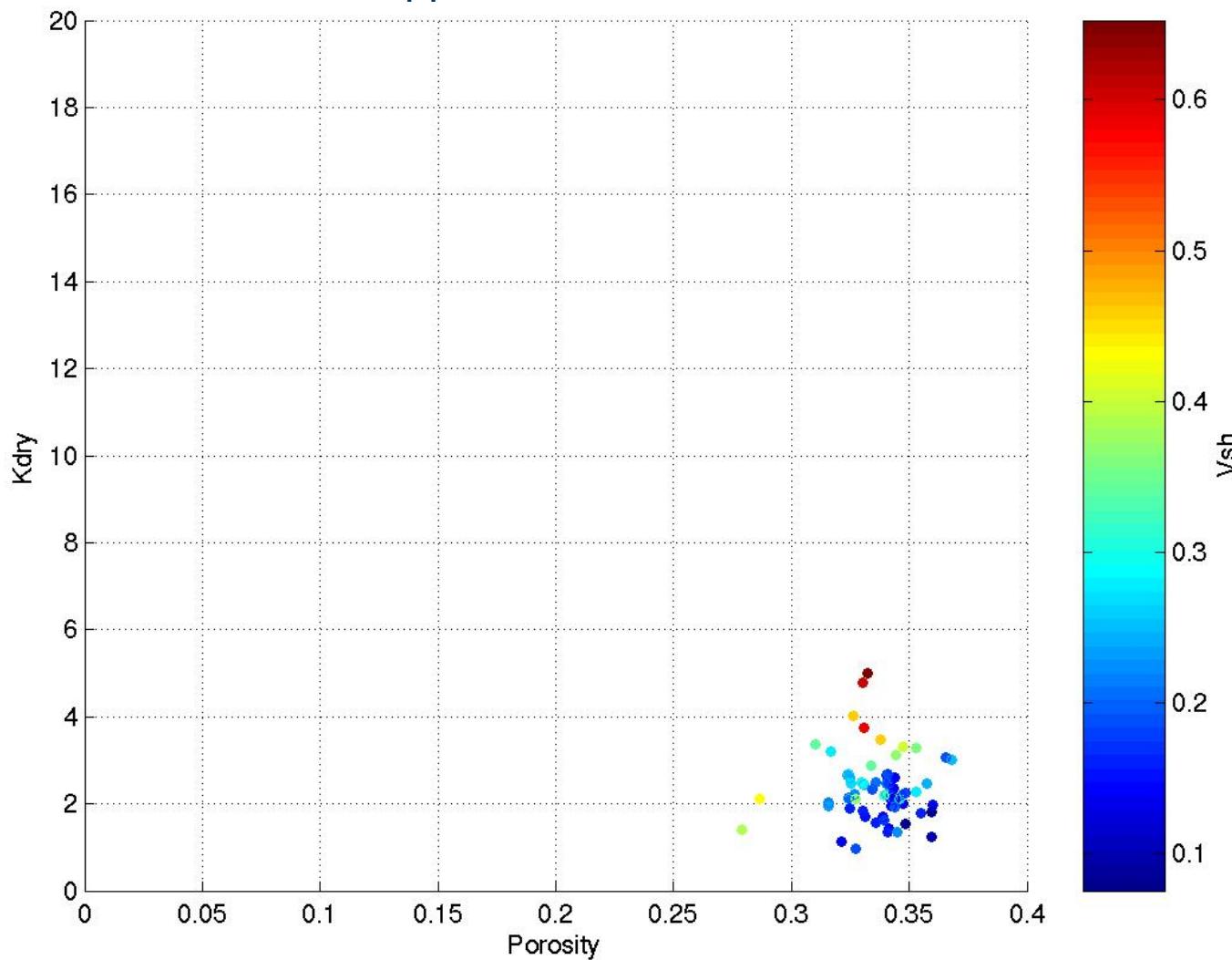
Upper Zone 2799 – 2810 m



Lumley *et al.*

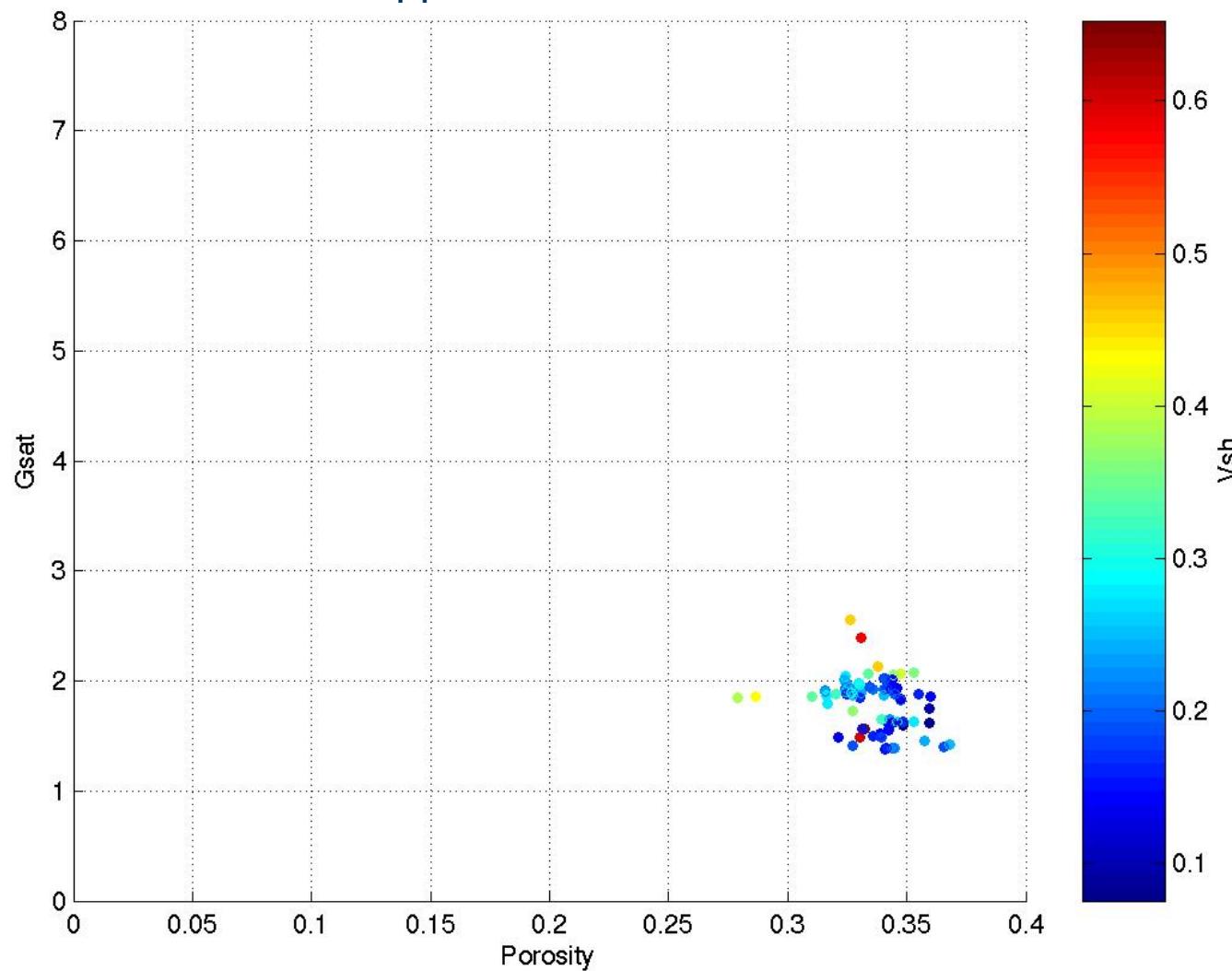
Well #1 Kdry... Upper Reservoir Interval

Upper Zone 2799 – 2810 m



Well #1 Gsat... Upper Reservoir Interval

Upper Zone 2799 – 2810 m

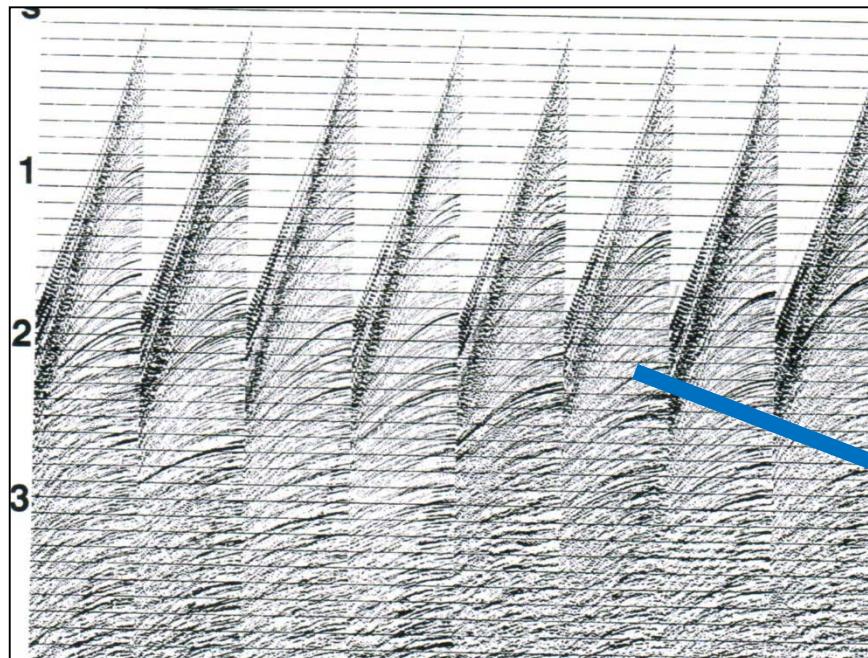




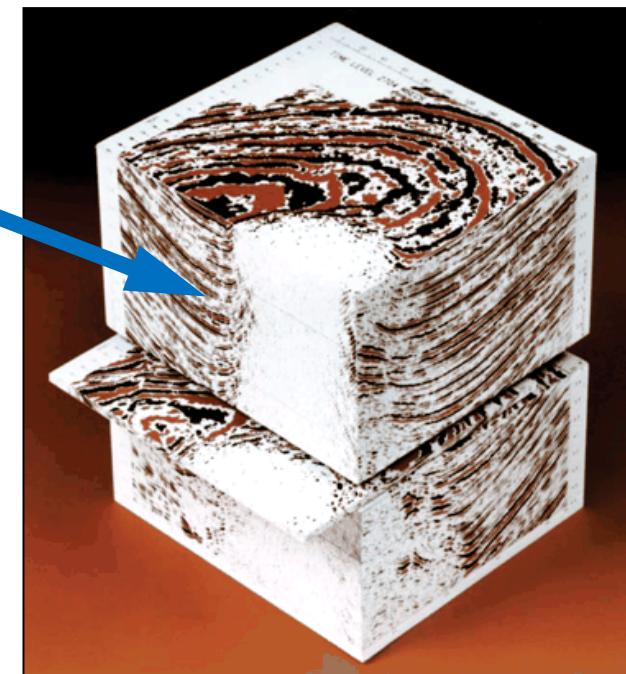
3D + 4D Seismic Imaging

3D seismic imaging

so how do we go from this...



to this... ?



Scalar wave equation modeling

$$\mathbf{d} = \mathcal{F}\mathbf{m}$$

$$(v^2 \nabla^2 - \partial_{tt}) P(\underline{x}, t) = 0$$

$$\mathbf{m} = v(\underline{\mathbf{x}})$$

$$\mathcal{F} = \nabla^2 - \partial_{tt}$$

$$\mathbf{d} = P(\underline{\mathbf{x}}, t)$$

Full waveform inversion

$$\mathbf{m} = \mathcal{F}^{-1} \mathbf{d}$$

$$\min \mathcal{E}^2 = w_d^2 (\mathbf{d} - \mathcal{F}\mathbf{m})^2 + w_m^2 (\mathbf{m} - \mathbf{m}_o)^2 + \dots$$

subject to constraints: $\nabla \mathbf{m} \approx \mathbf{0}$ etc...

- | | |
|---------------|------------------------------|
| \mathcal{F} | <i>WEQ modeling operator</i> |
| \mathbf{m} | <i>2D/3D velocity model</i> |

WEQ imaging + velocity analysis

$$\mathcal{R} \sim \nabla m \sim (\mathcal{F}^* \mathcal{F})^{-1} \mathcal{F}^* d \sim \mathcal{F}_S \times \mathcal{F}_{\textcolor{blue}{m}}^* d \mid_{ic}$$

min $\epsilon^2 = \text{Image Quality} \dots$

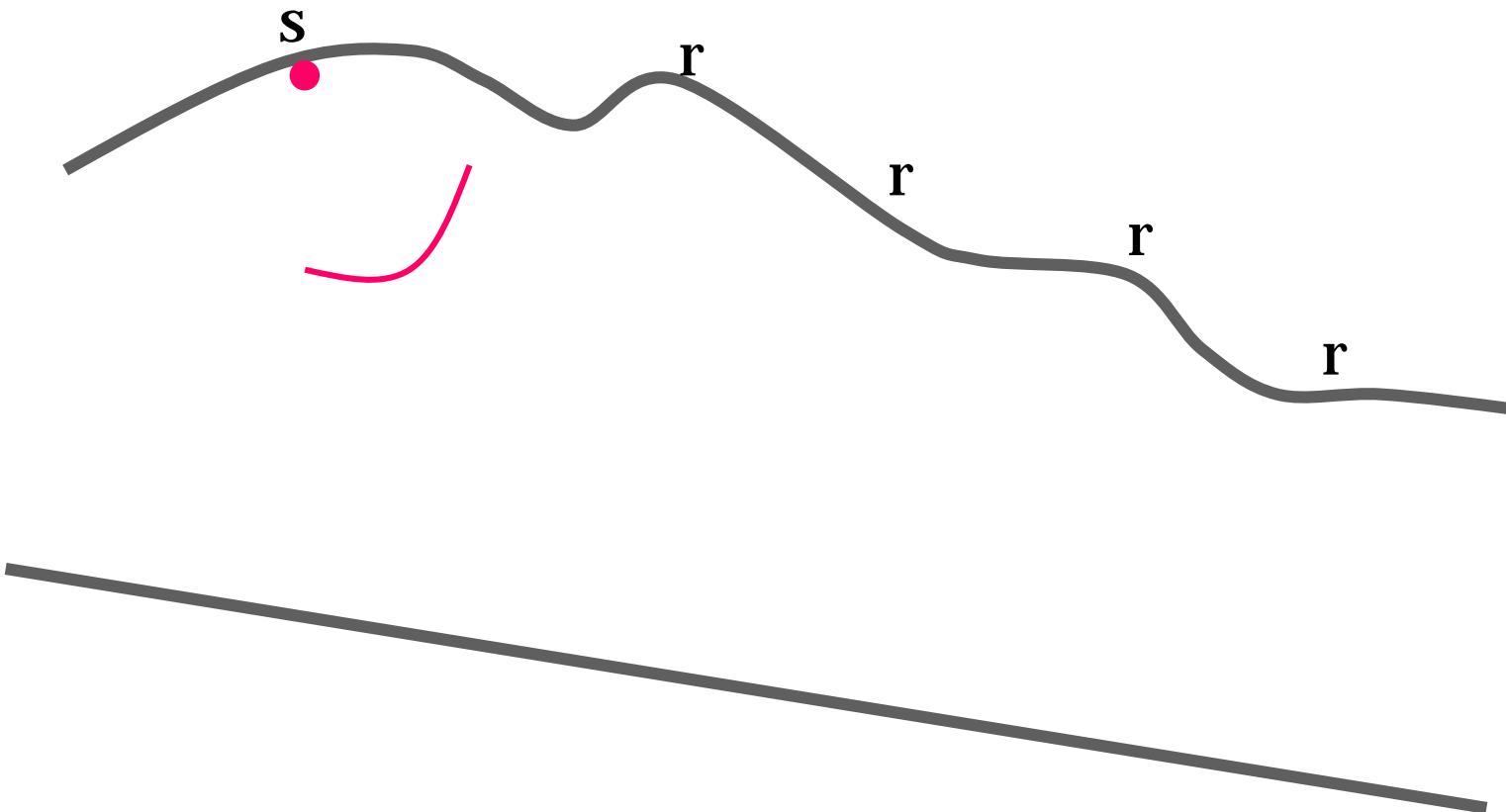
subject to constraints: $\nabla_x \mathcal{R} \approx 0$ etc...

\mathcal{F}^* WEQ imaging (adjoint) operator

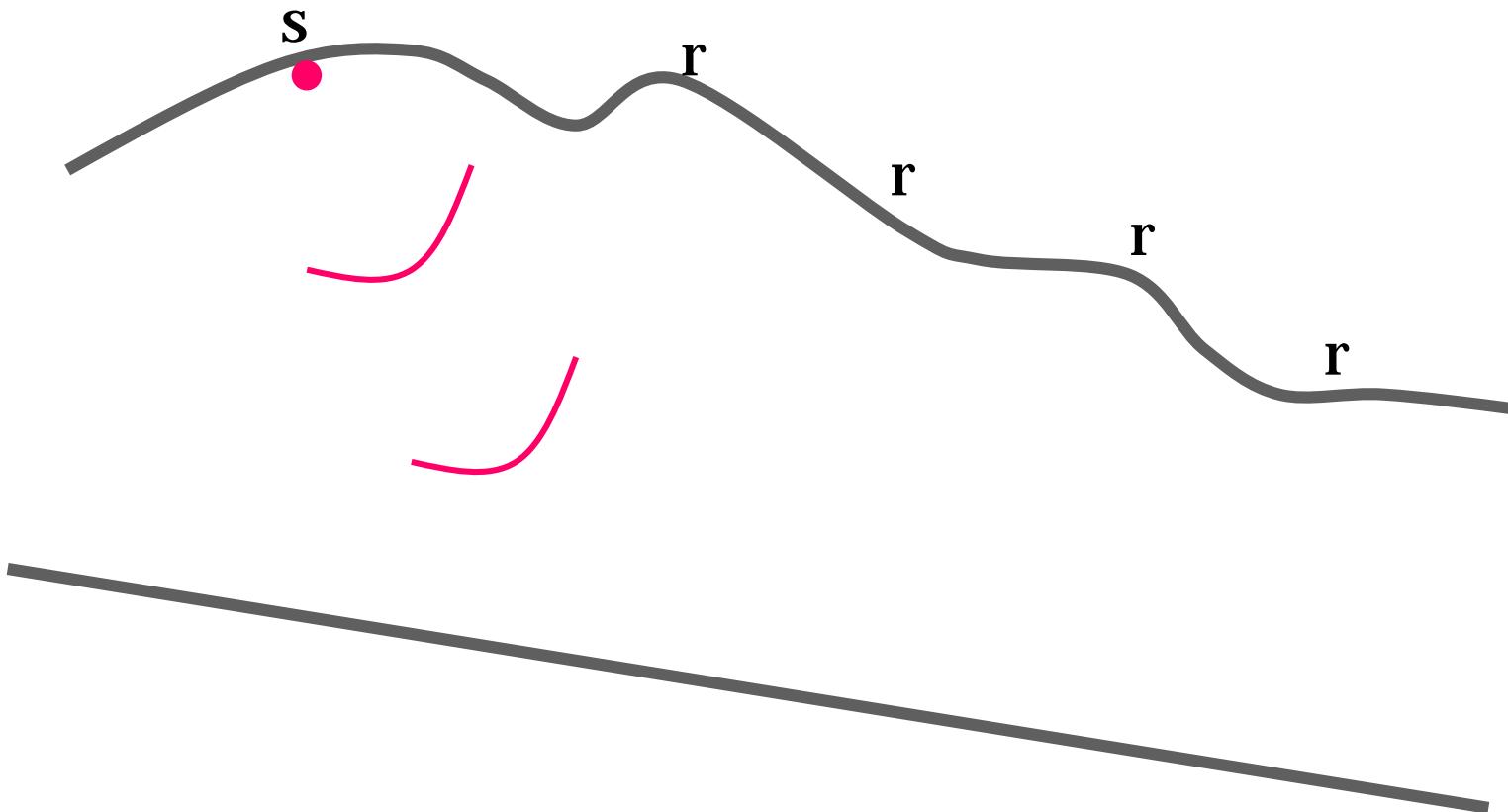
$\textcolor{blue}{m}$ 2D/3D velocity model

\mathcal{R} migrated reflectivity image

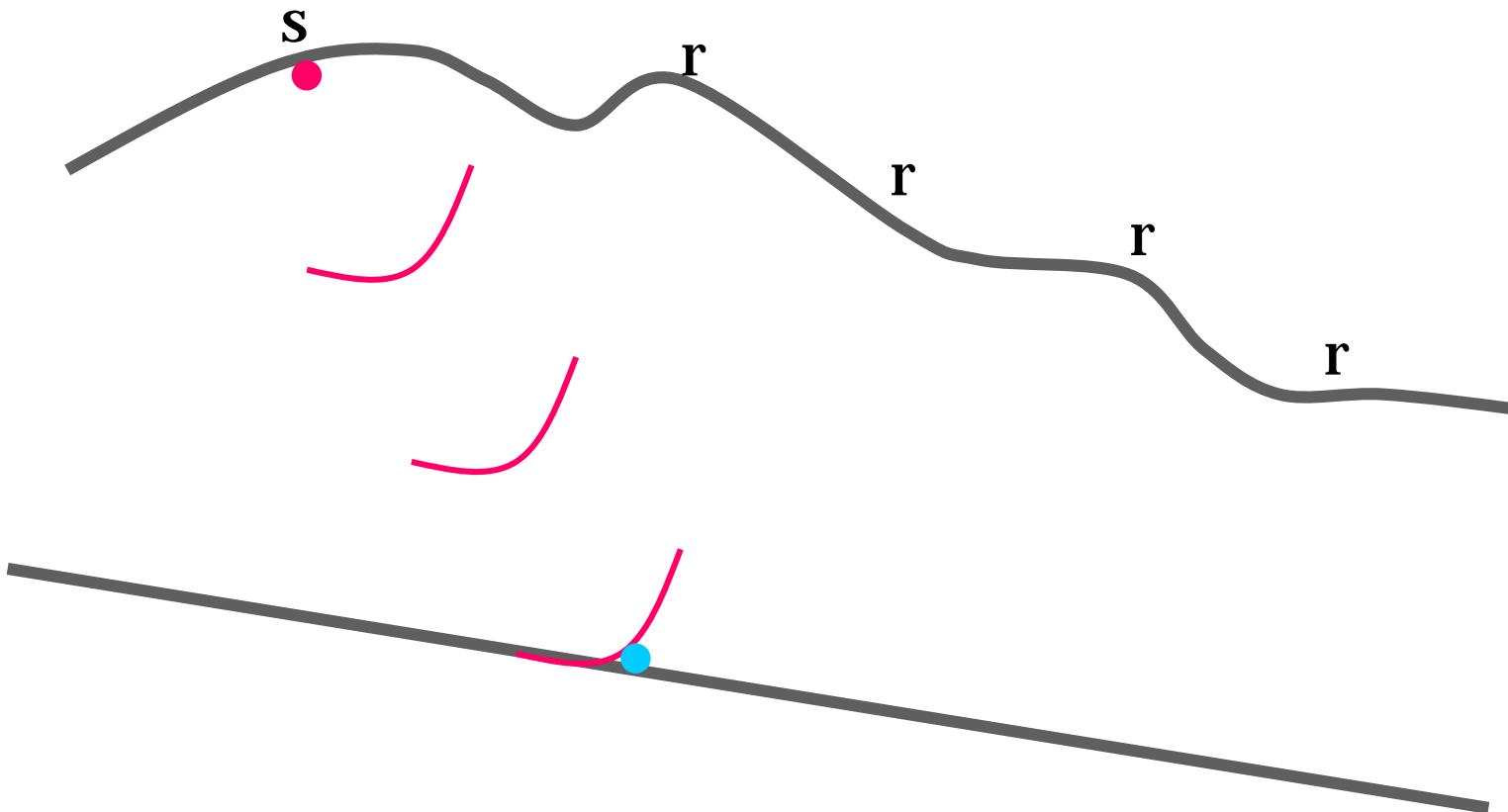
prestack modeling



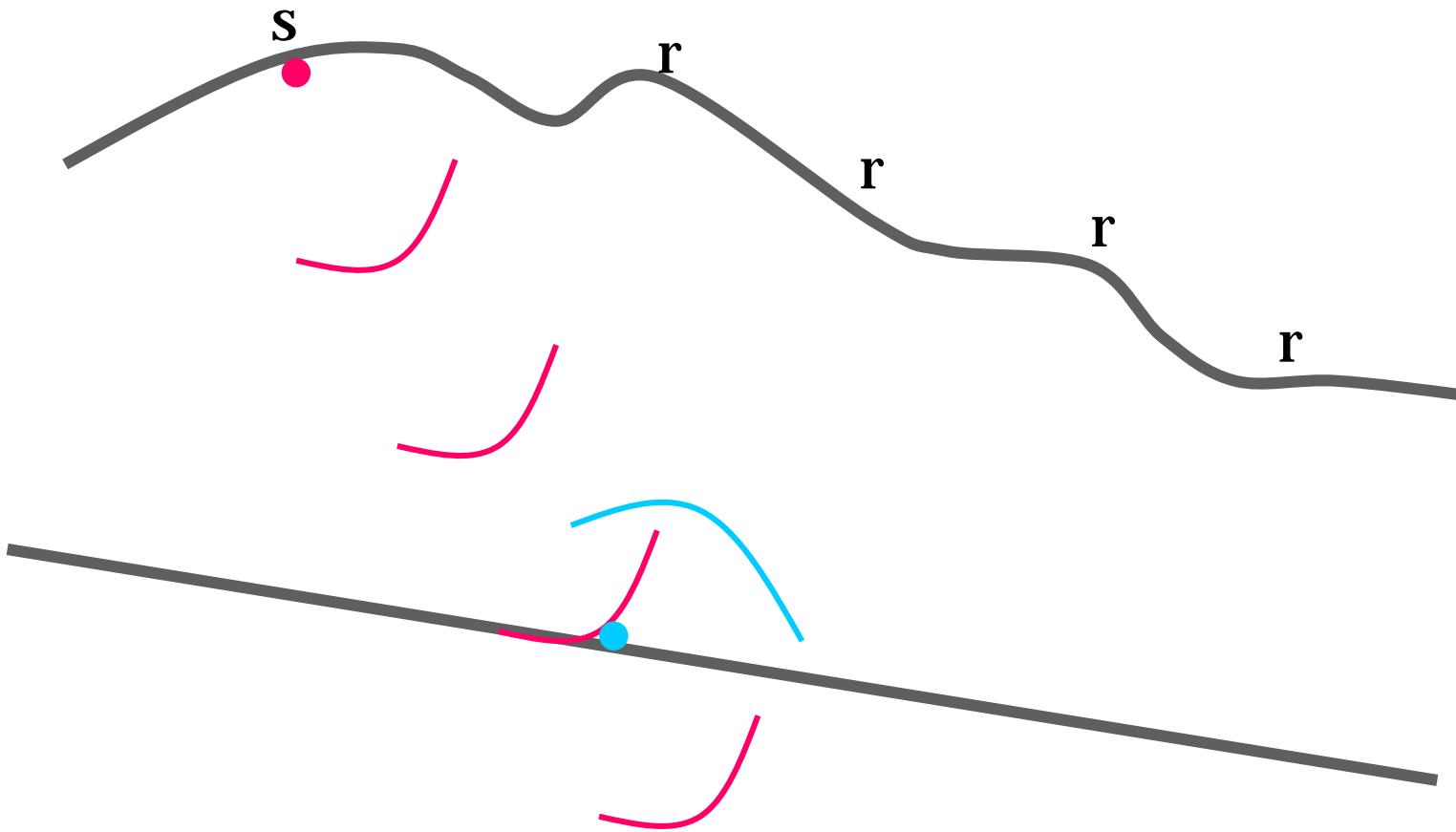
prestack modeling



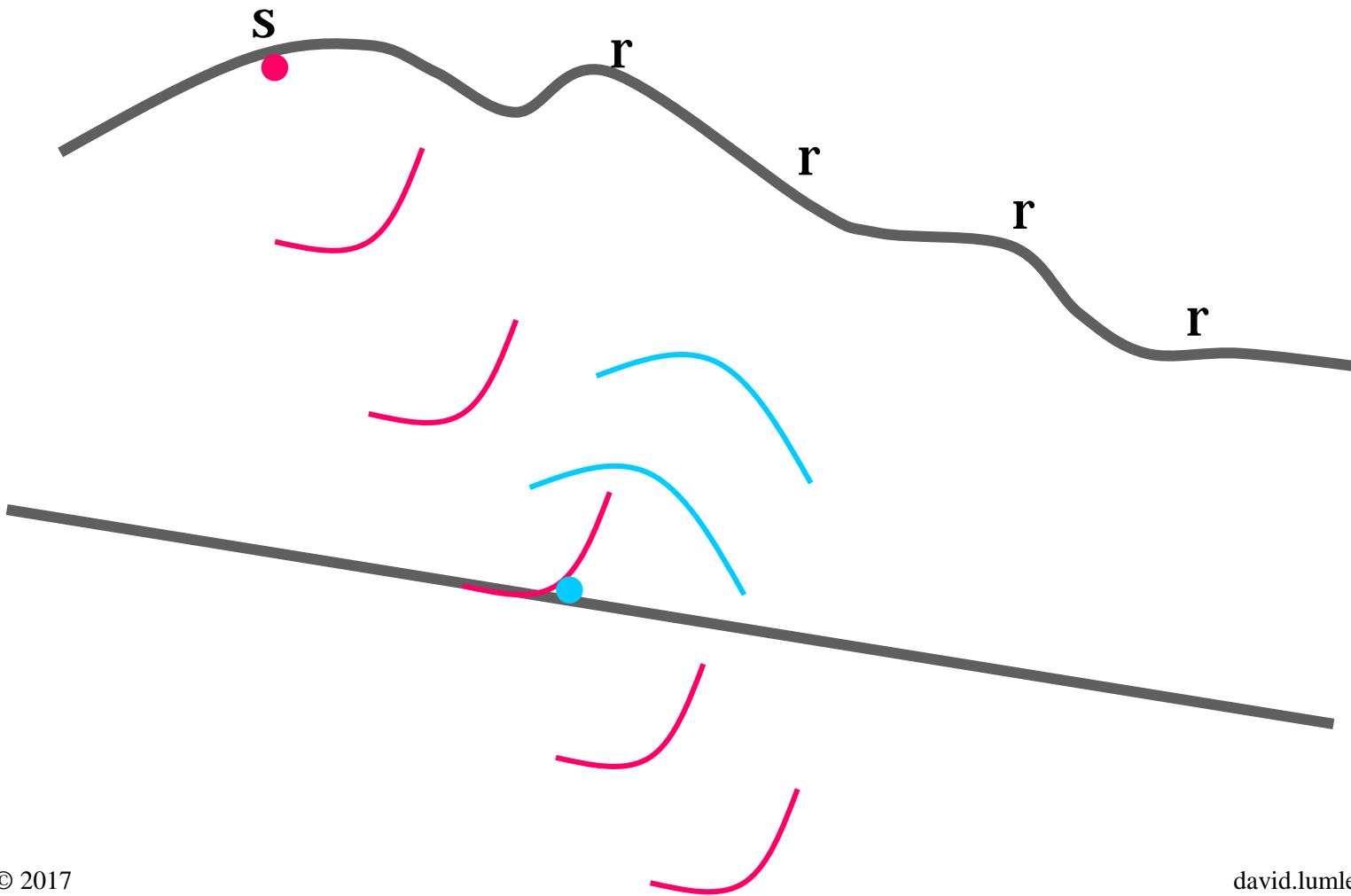
prestack modeling



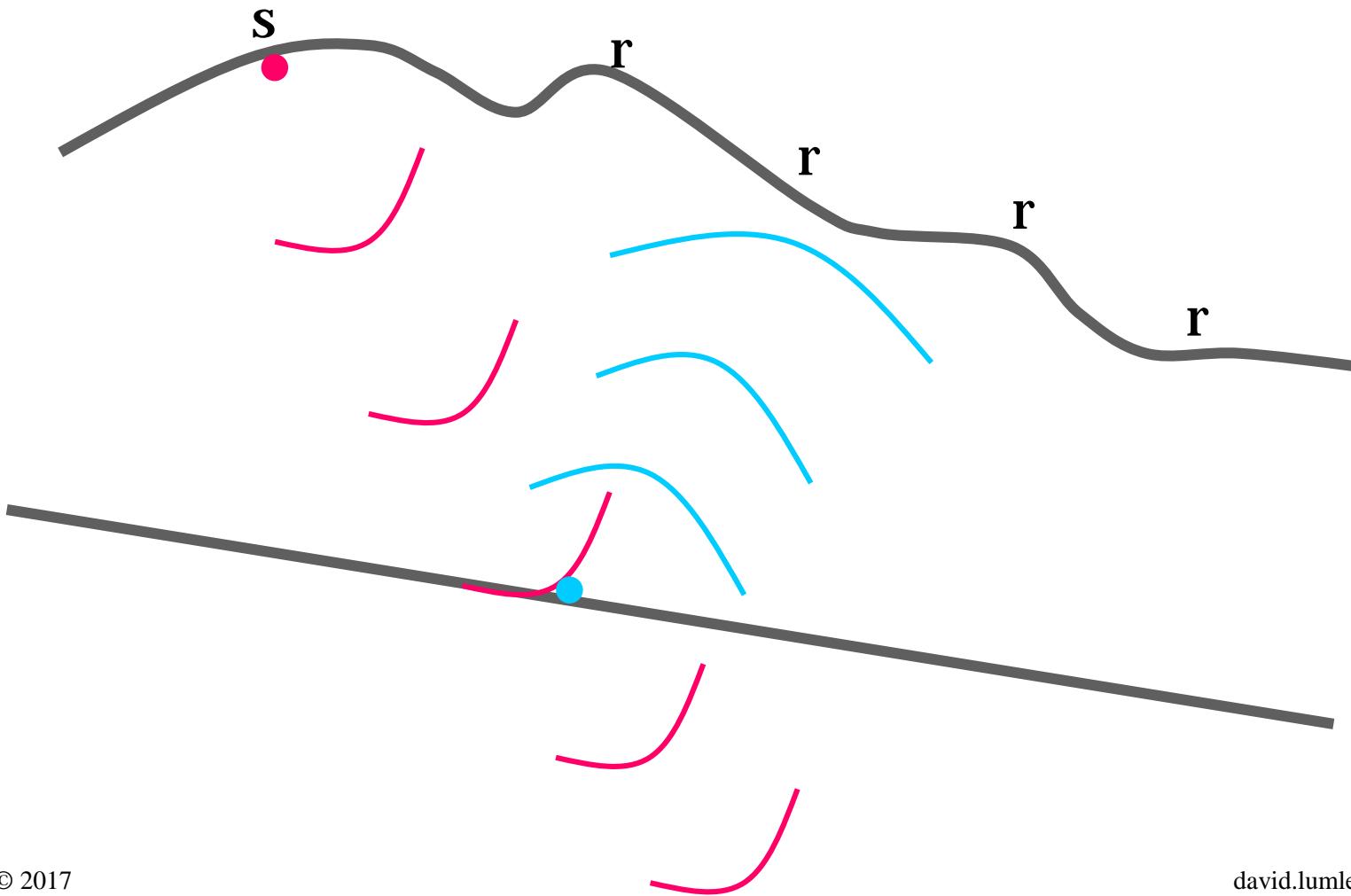
prestack modeling



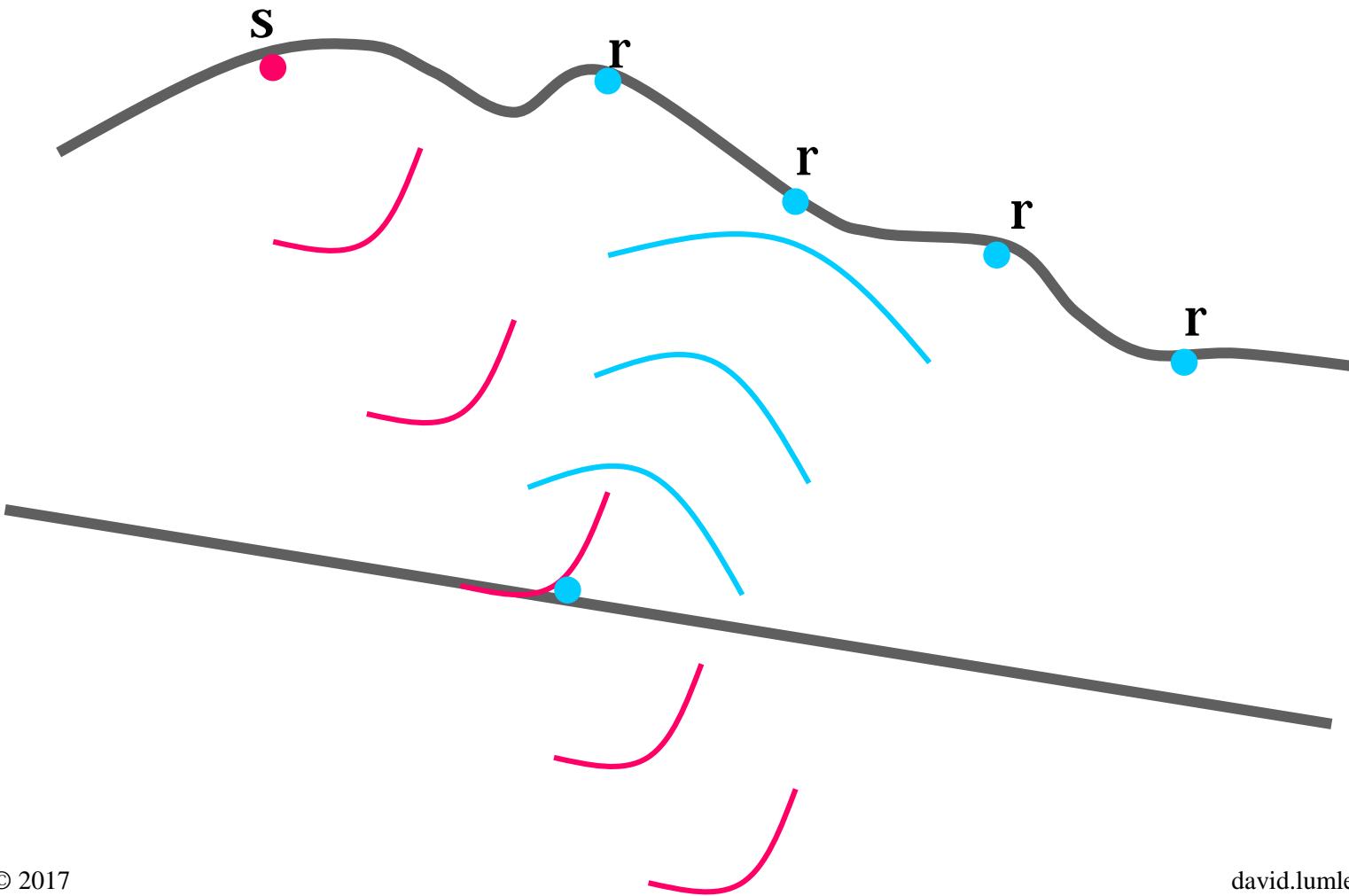
prestack modeling



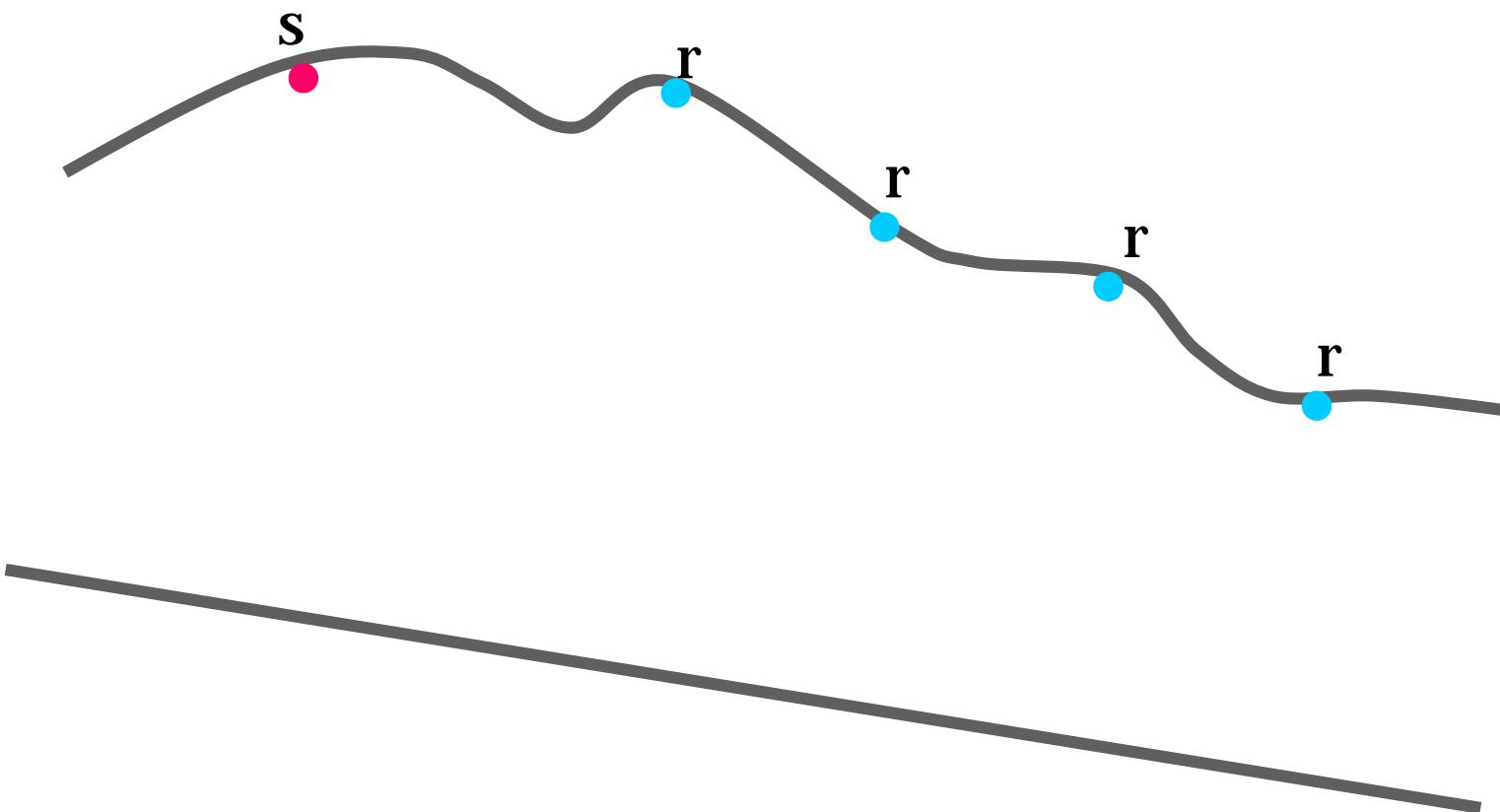
prestack modeling



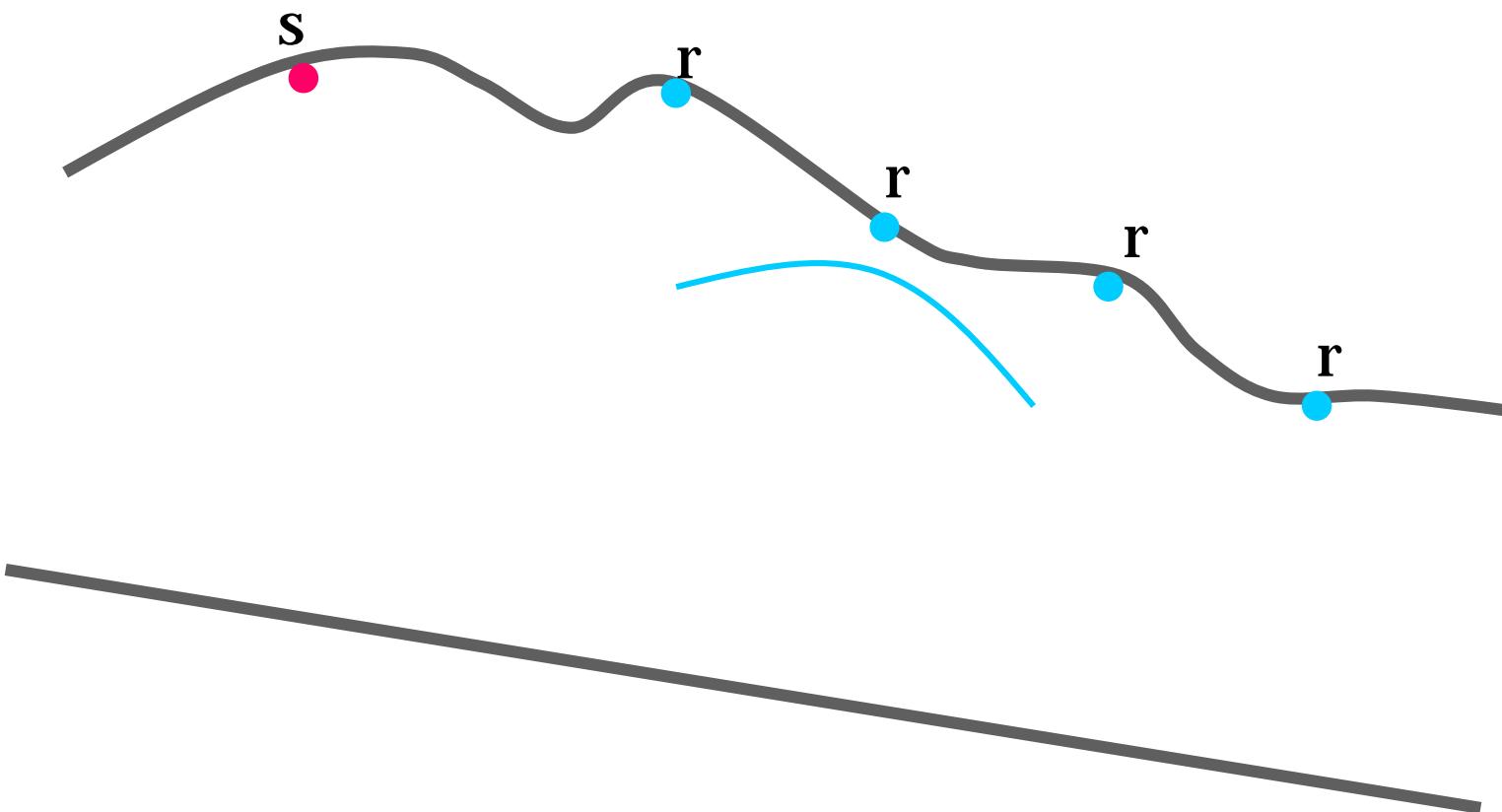
prestack modeling



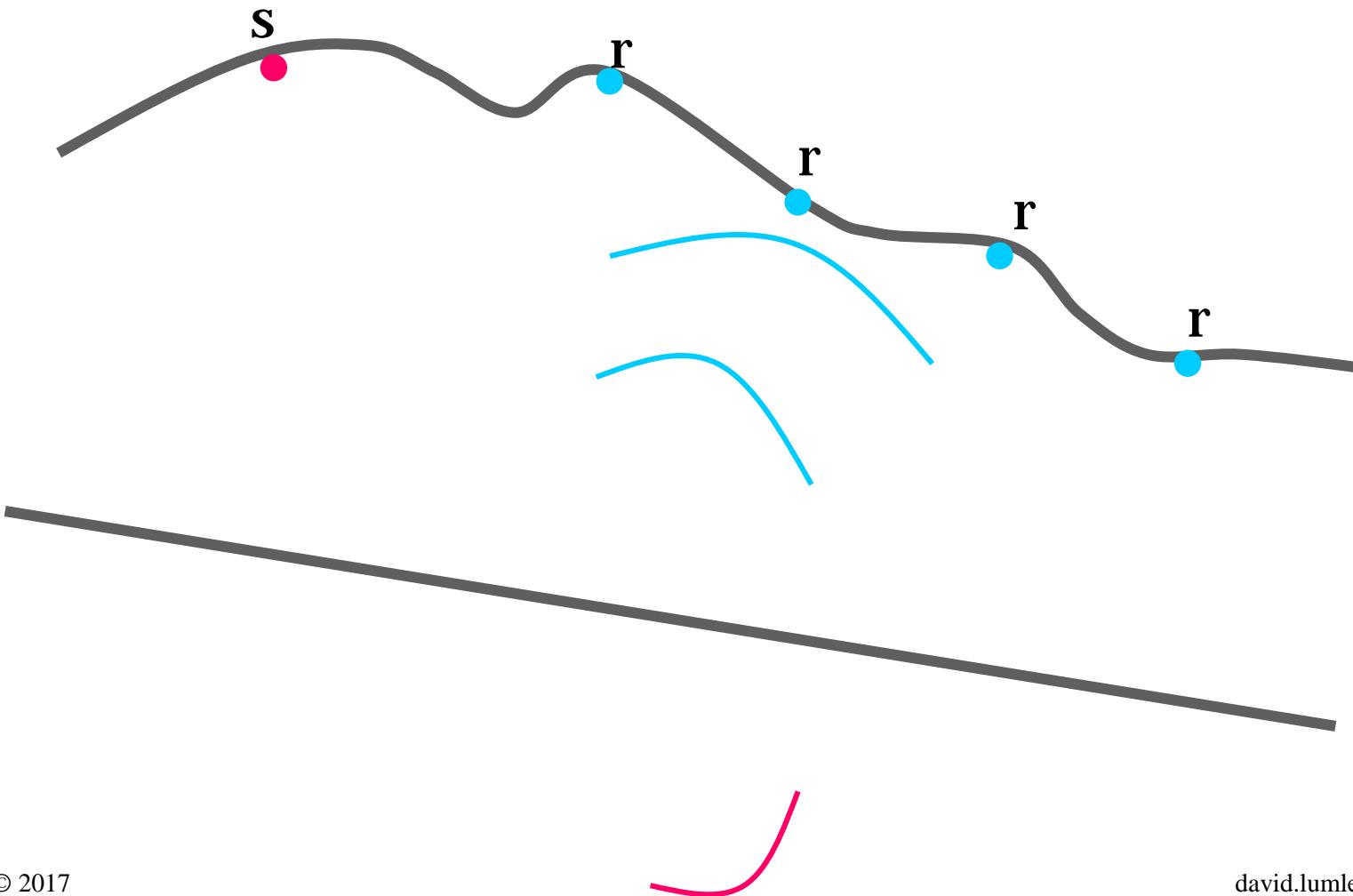
prestack imaging*



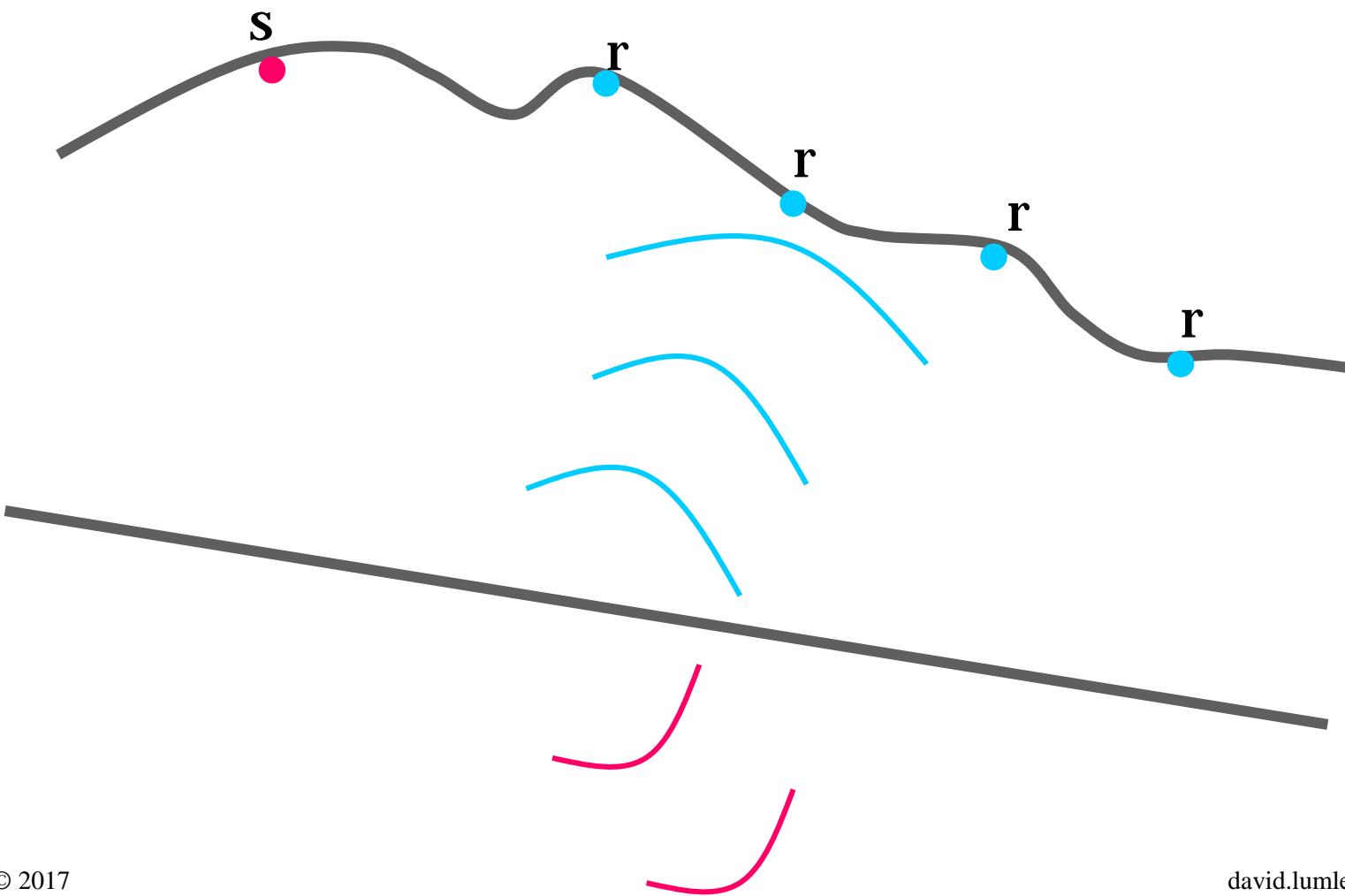
prestack imaging



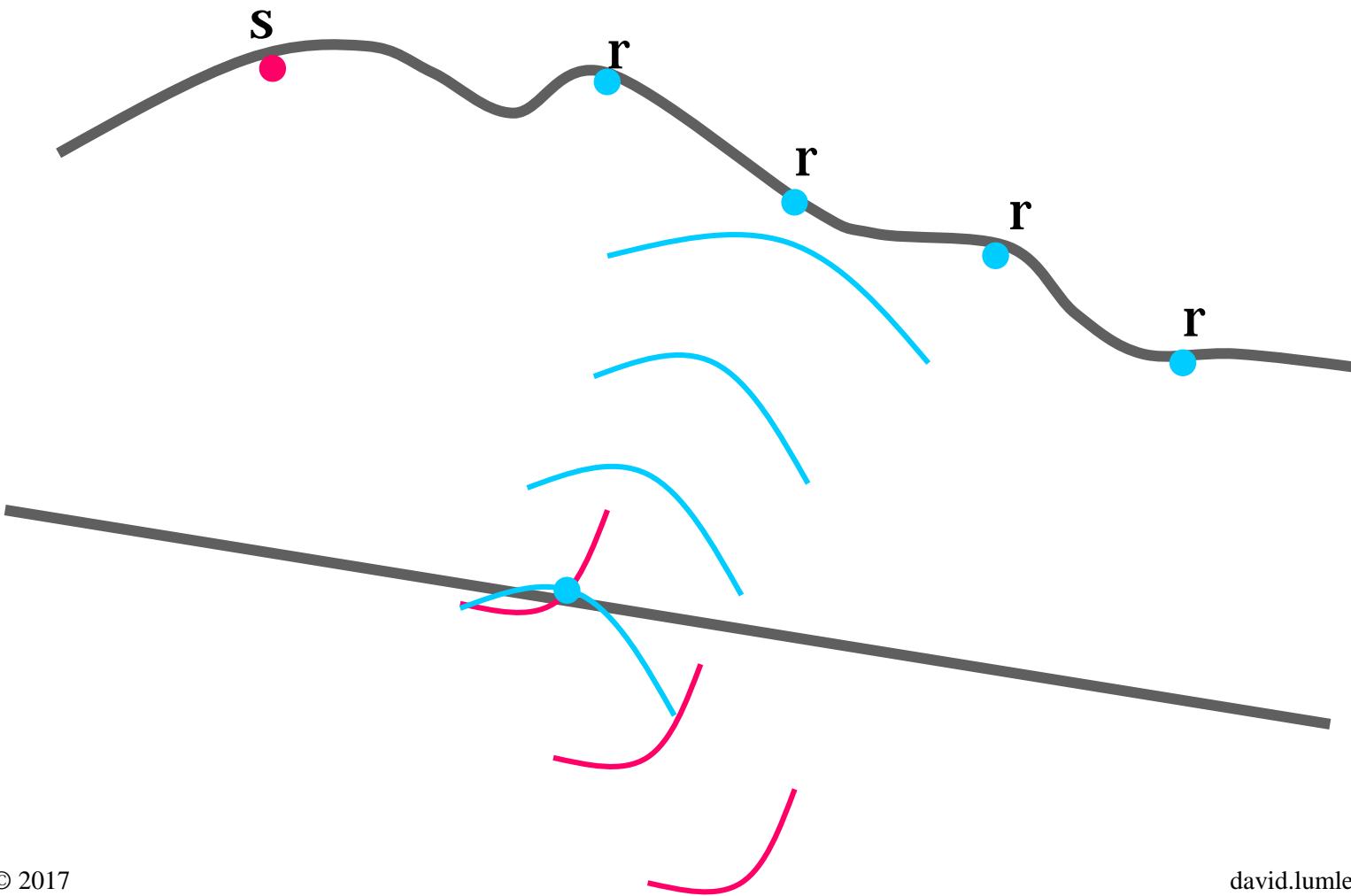
prestack imaging



prestack imaging



prestack imaging



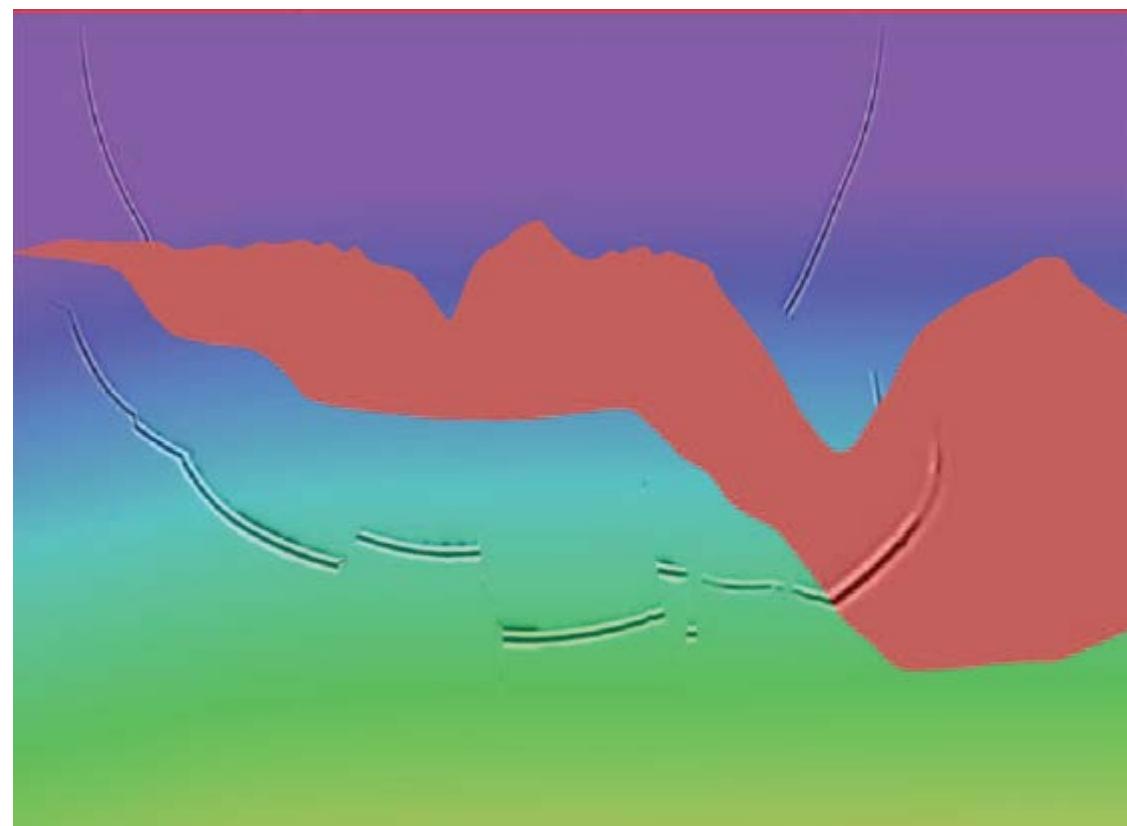
Imaging methods

- Different ways to solve the wave equation:

$$\{ \nabla^2 - \partial_{tt}/v^2 \} P(x,t) = 0$$

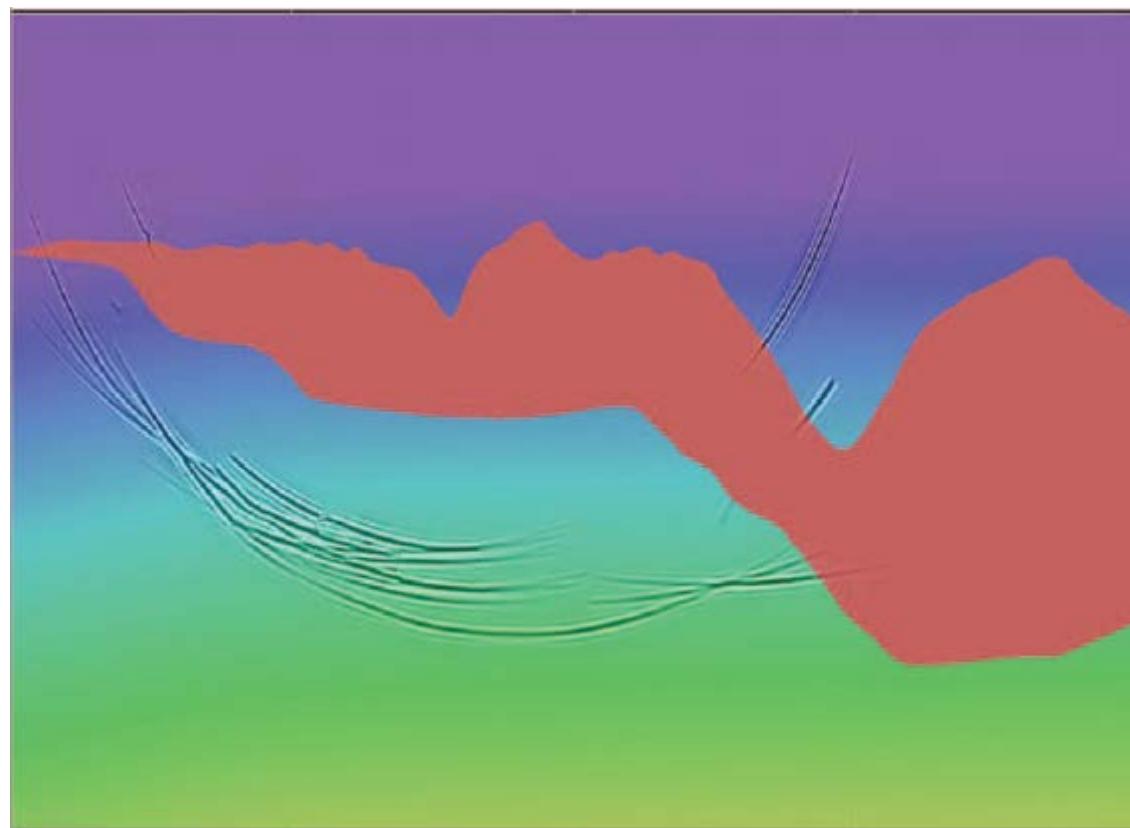
- Kirchhoff/rays/beams: *by Integral (summation) methods*
- Frequency-domain: *by Fourier/Laplace transforms*
- Finite Difference: *by FD/FEM operators*
- Hybrid methods: *any combinations of the above*

Kirchhoff



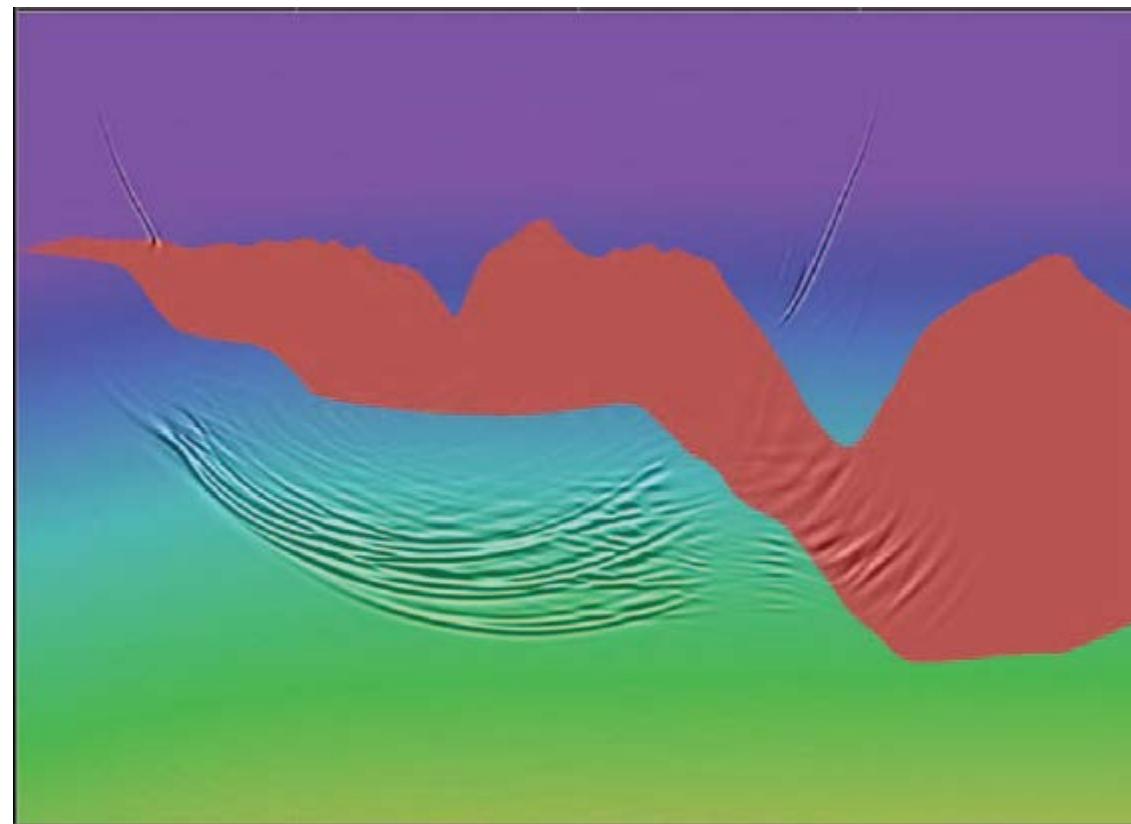
Etgen et al. (2009)

Gaussian Beam



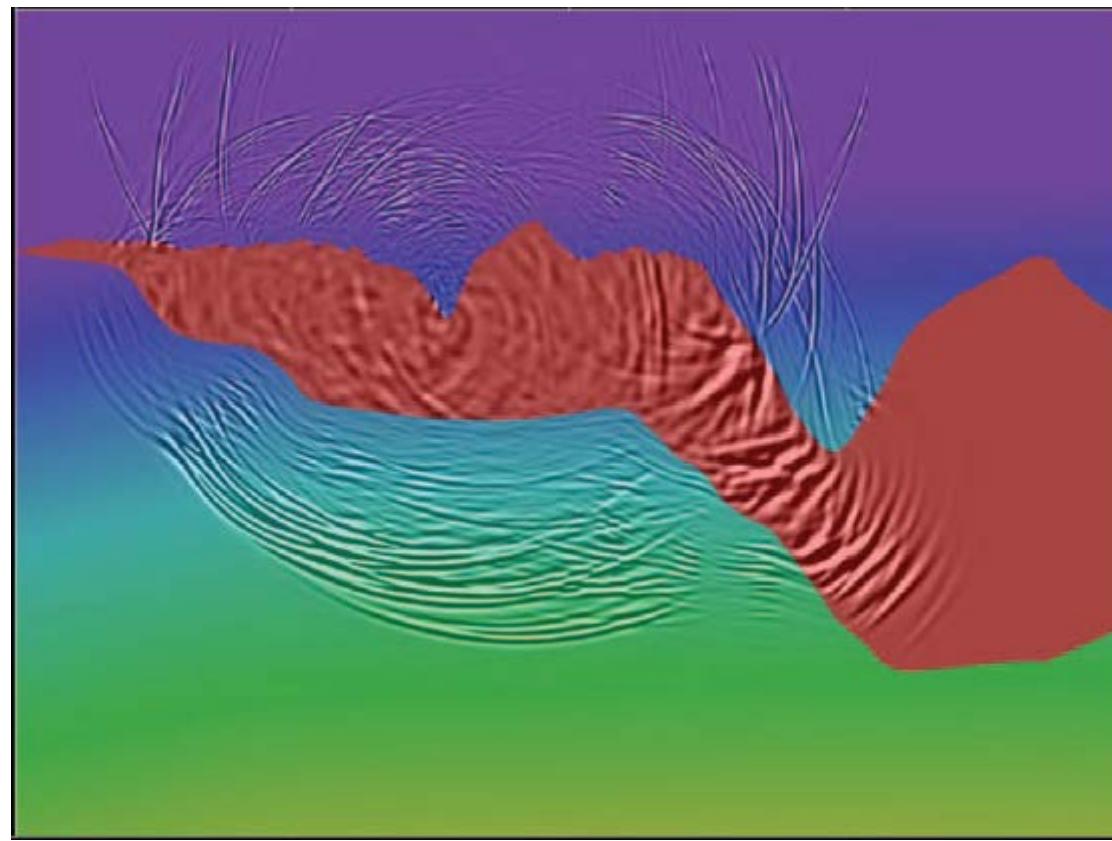
Etgen et al. (2009)

WEM (1-way)



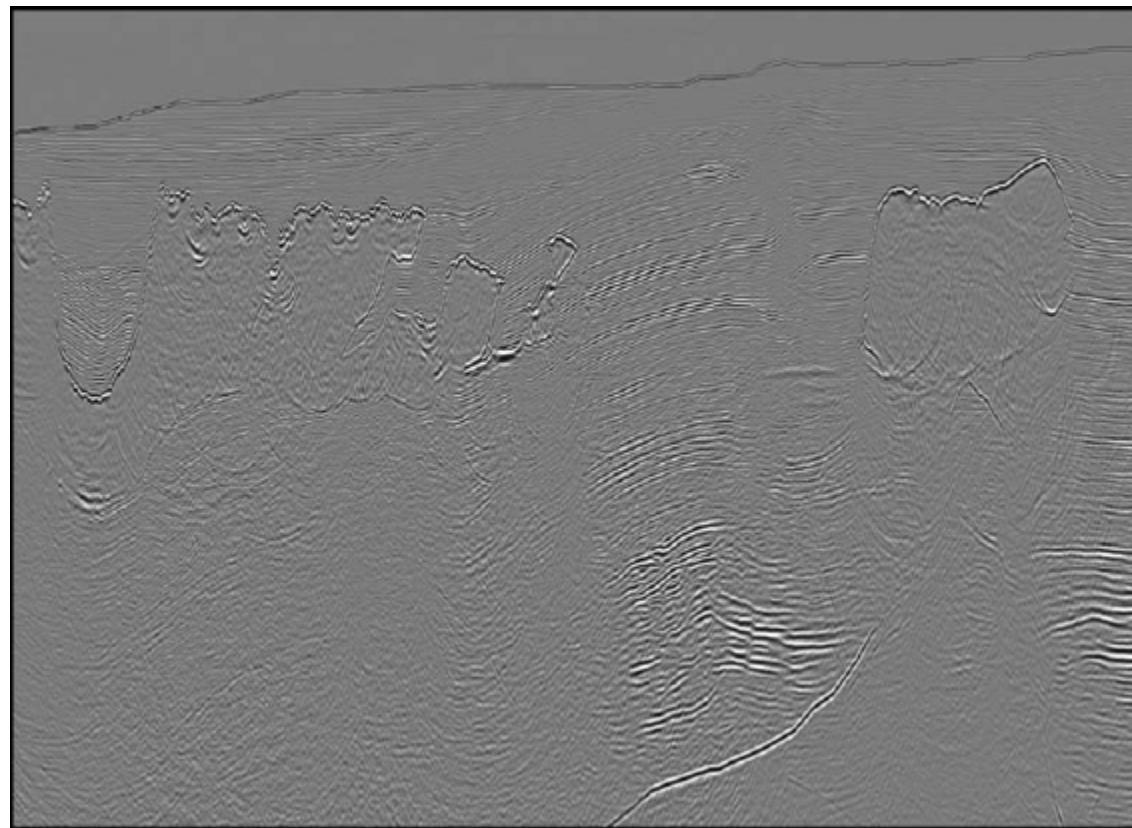
Etgen et al. (2009)

Reverse-time (RTM)



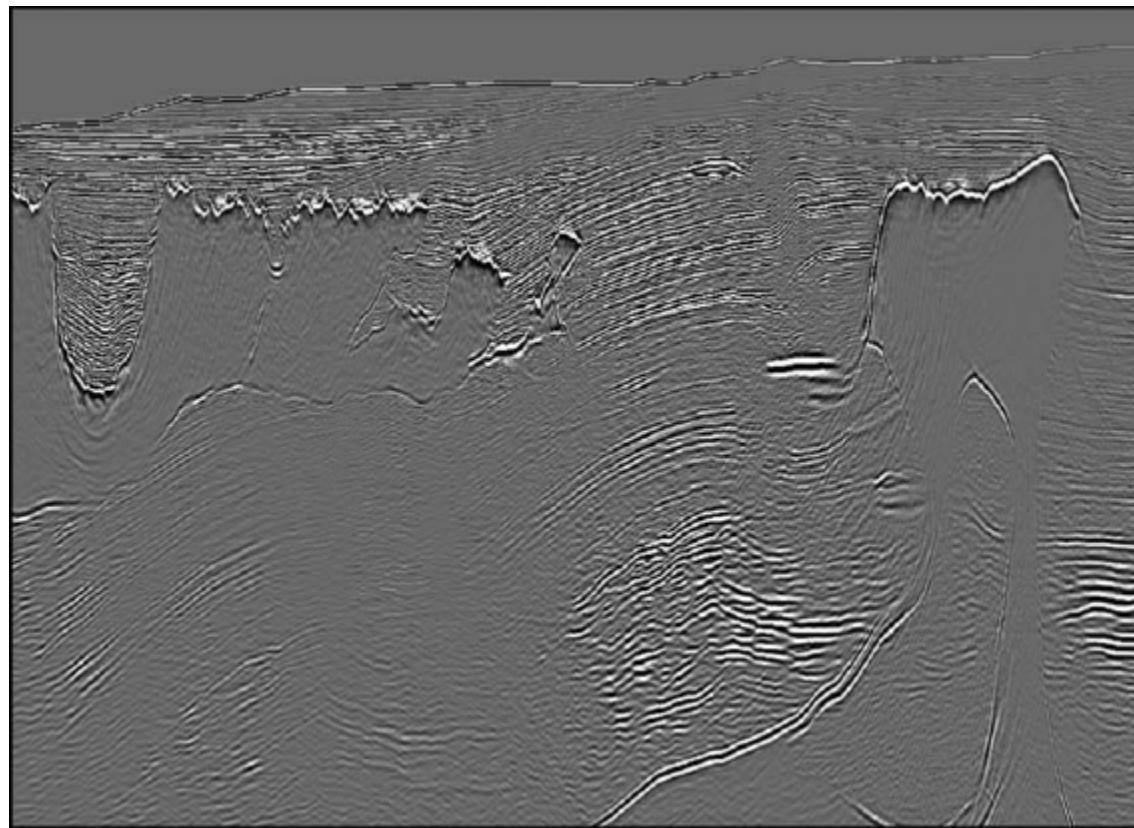
Etgen et al. (2009)

Kirchhoff



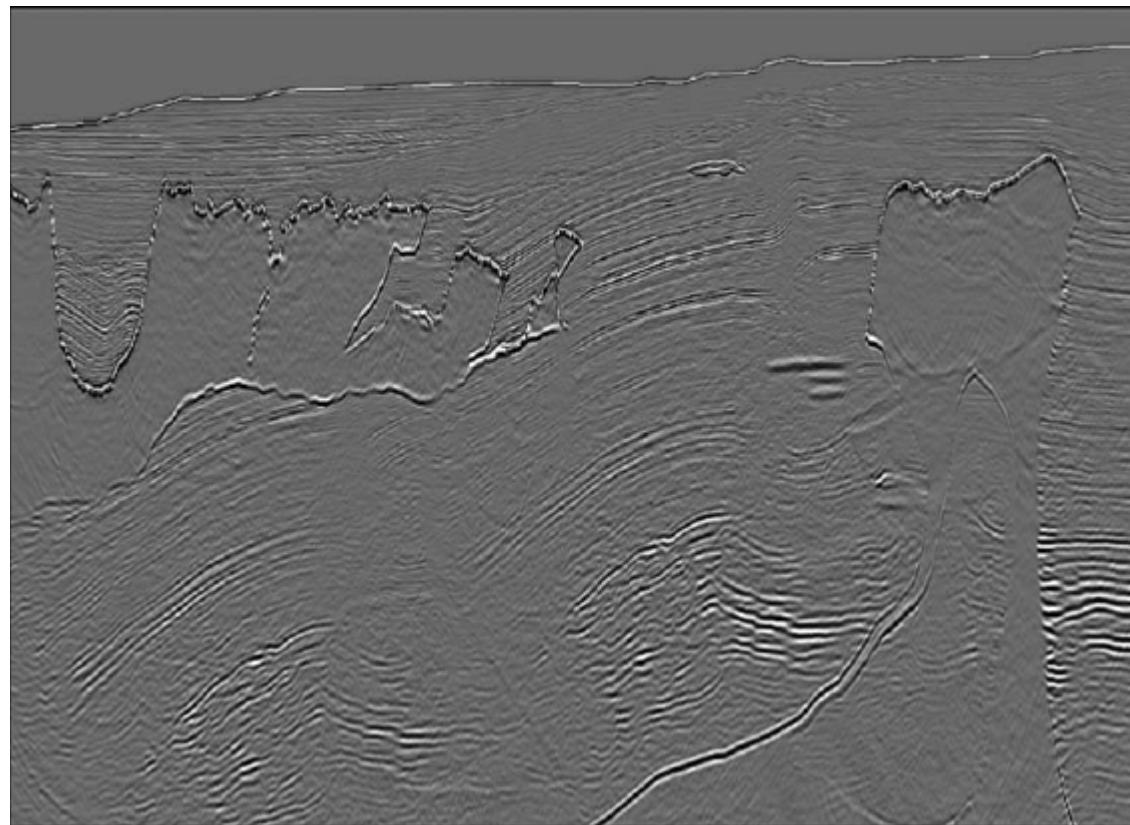
Etgen et al. (2009)

Gaussian Beam



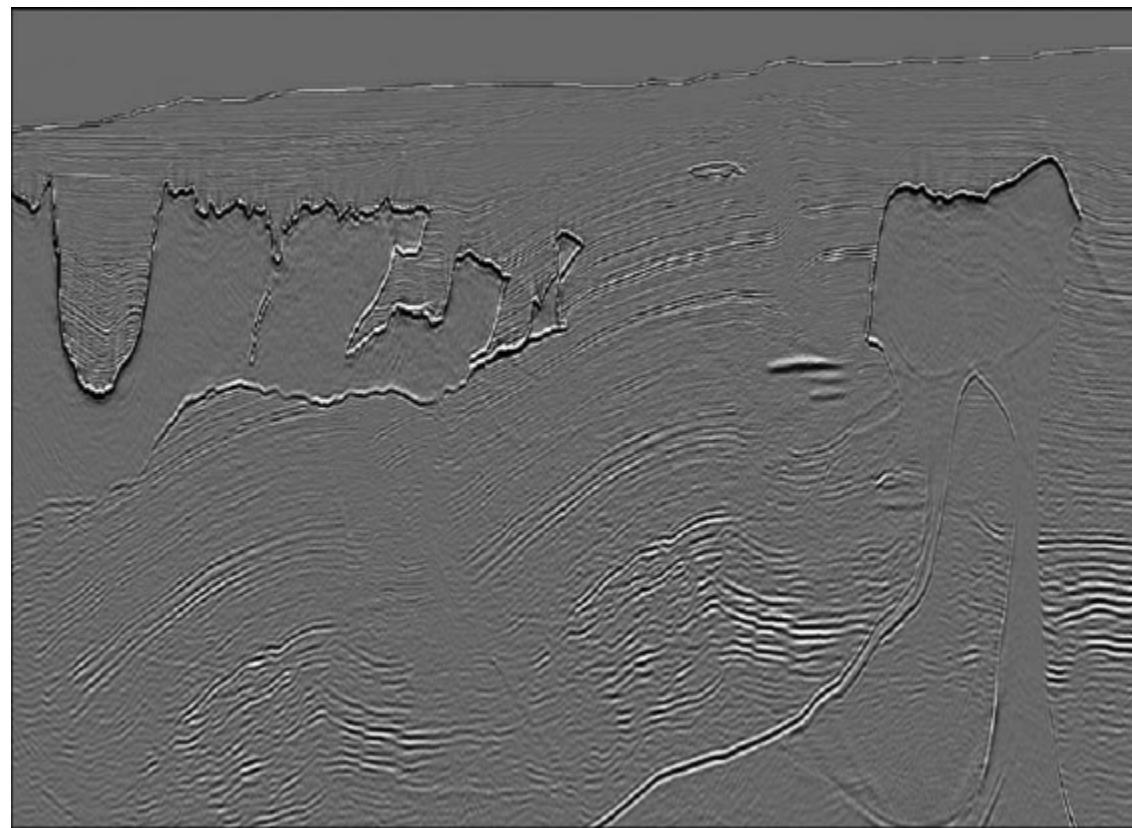
Etgen et al. (2009)

WEM (1-way)



Etgen et al. (2009)

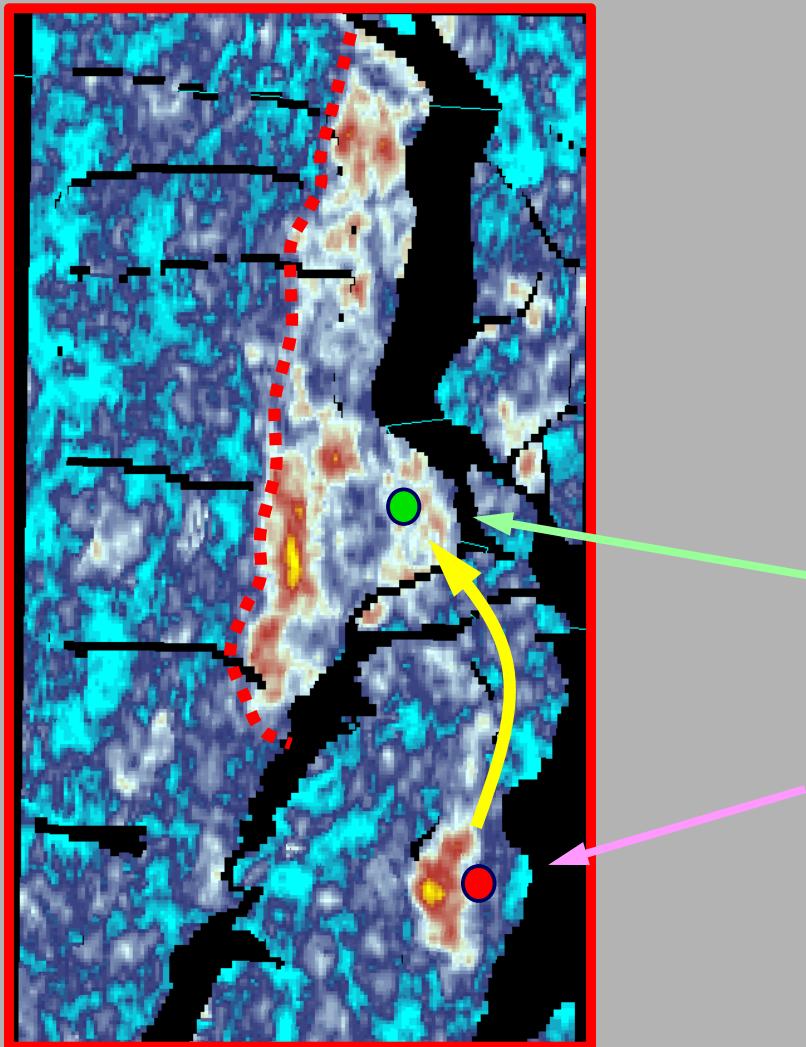
Reverse-time (RTM)(2-way)



Etgen et al. (2009)

Monitoring Production

characterize + predict

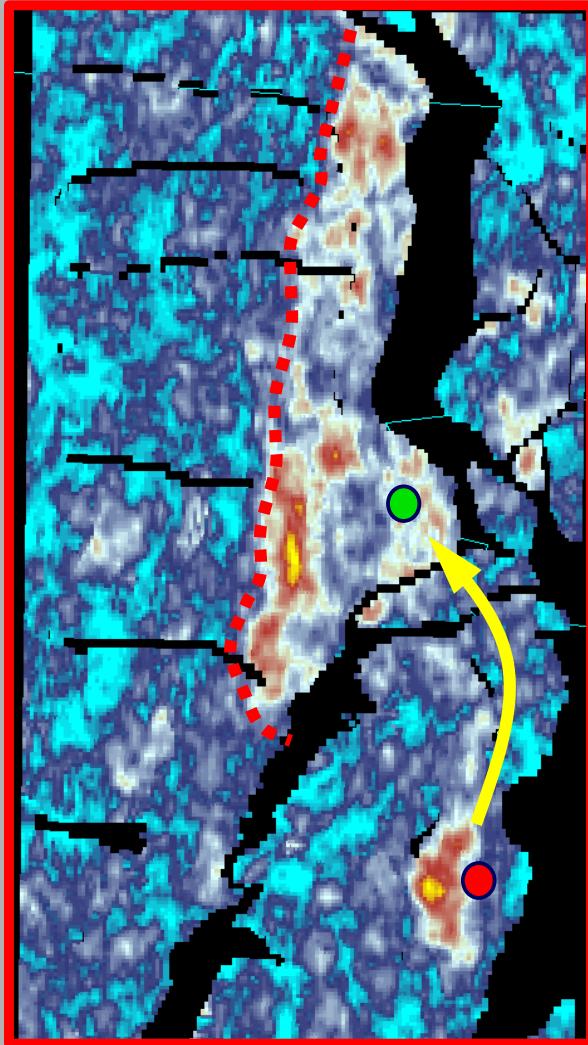


producer

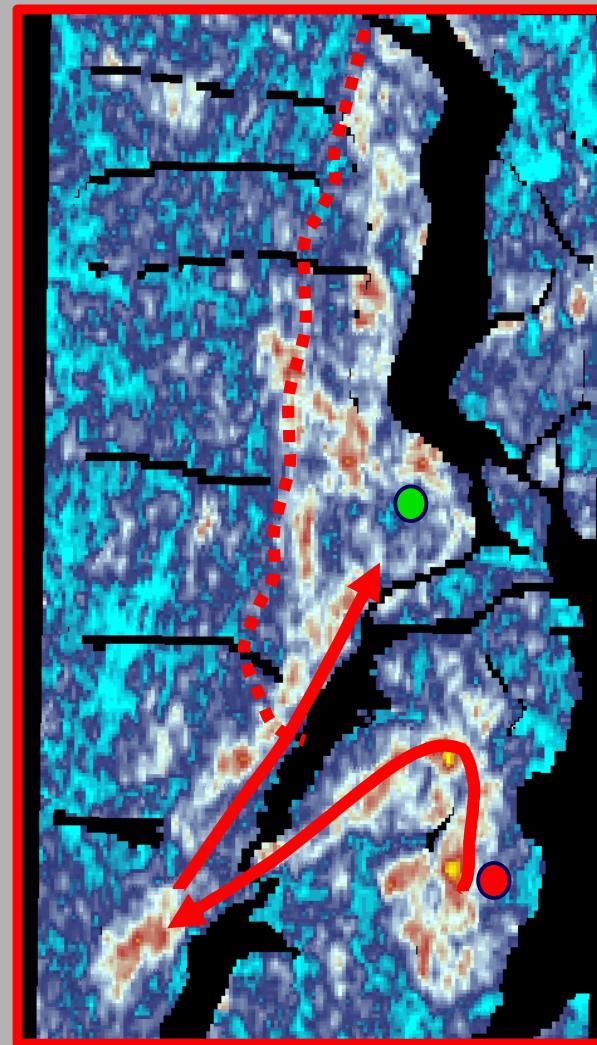
injector

Monitoring Production

characterize + predict

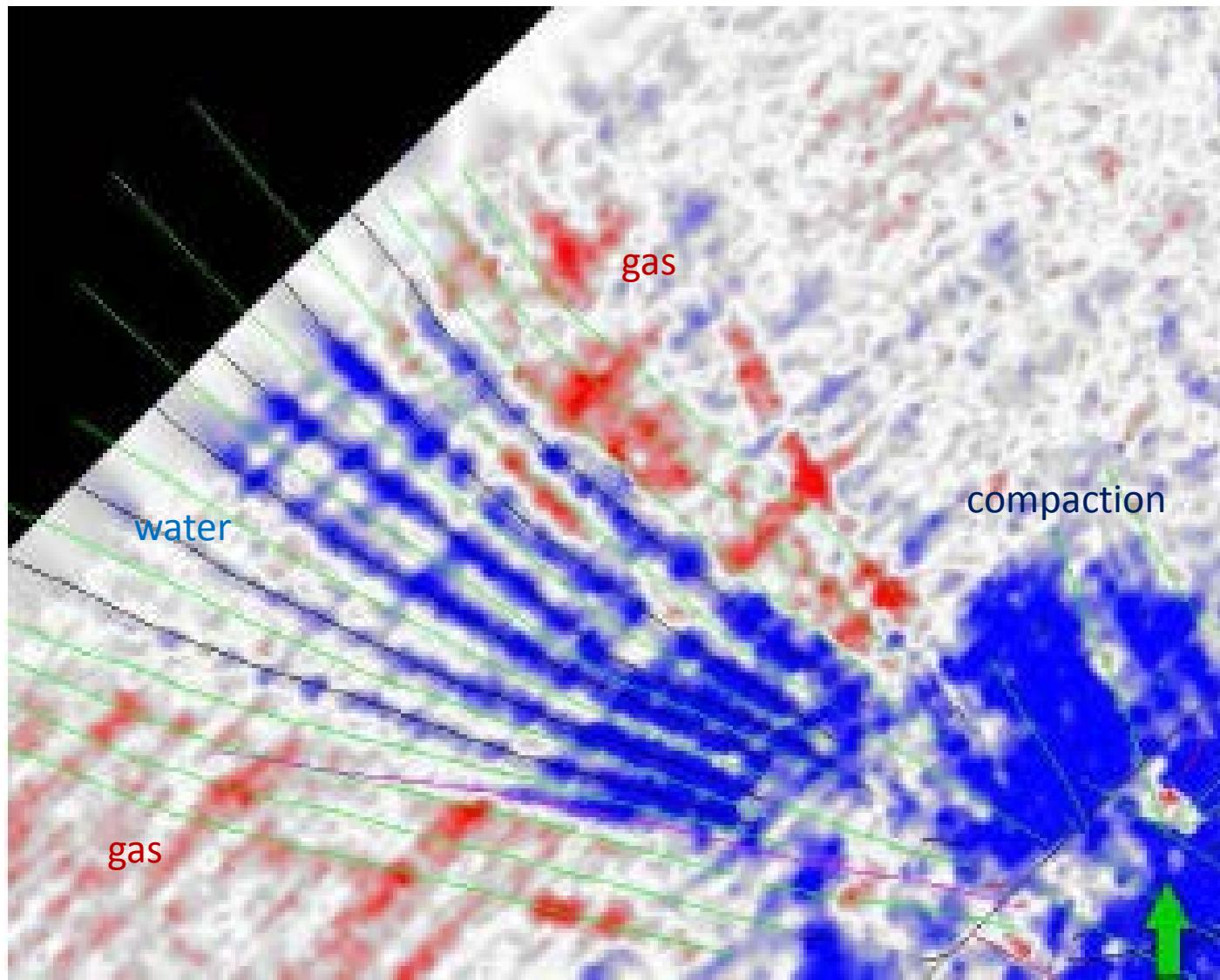


monitor directly!



Statoil

Fractured chalk reservoir

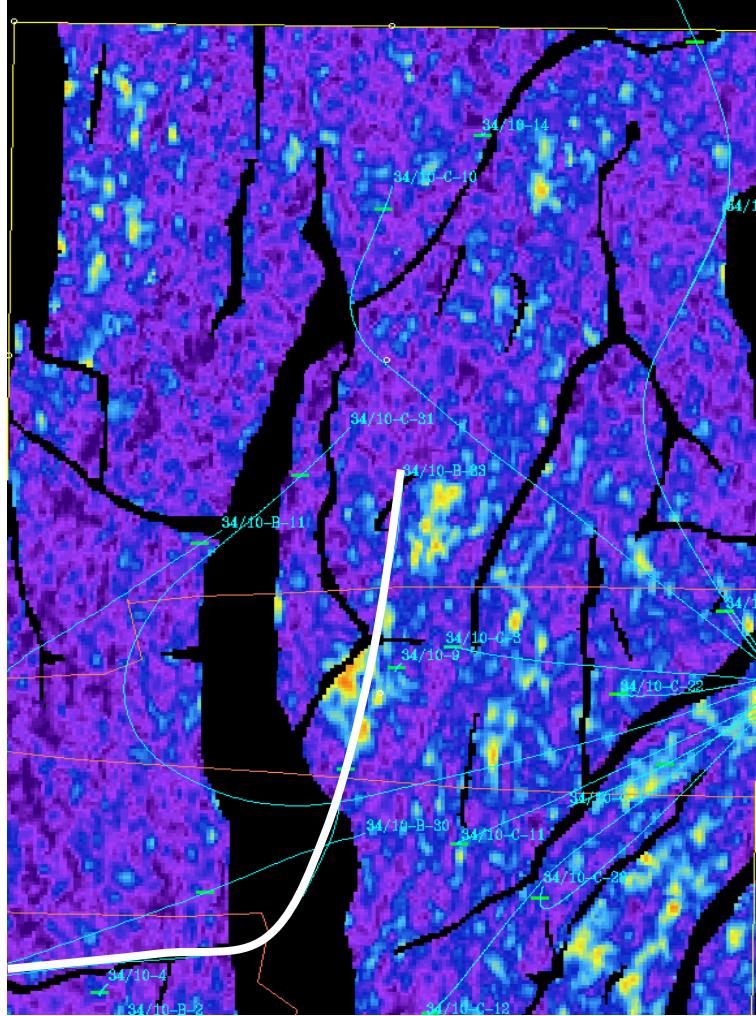


Gommesen et al., 2007

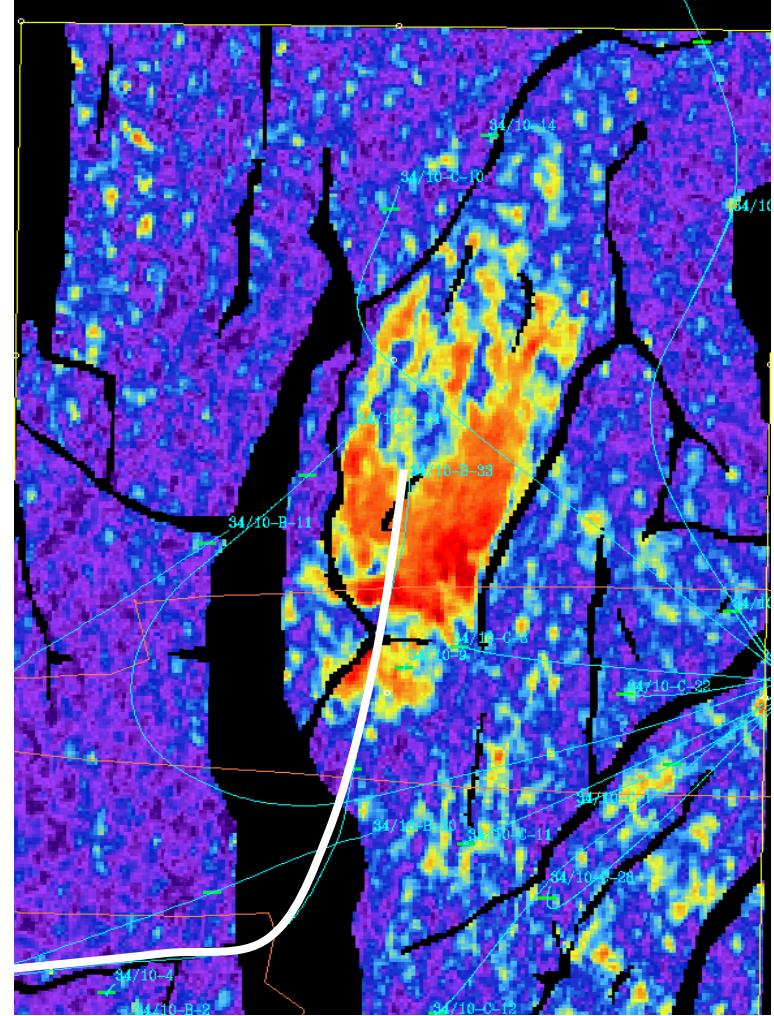
david.lumley@utdallas.edu

4D Seismic Pressure Anomaly

Before



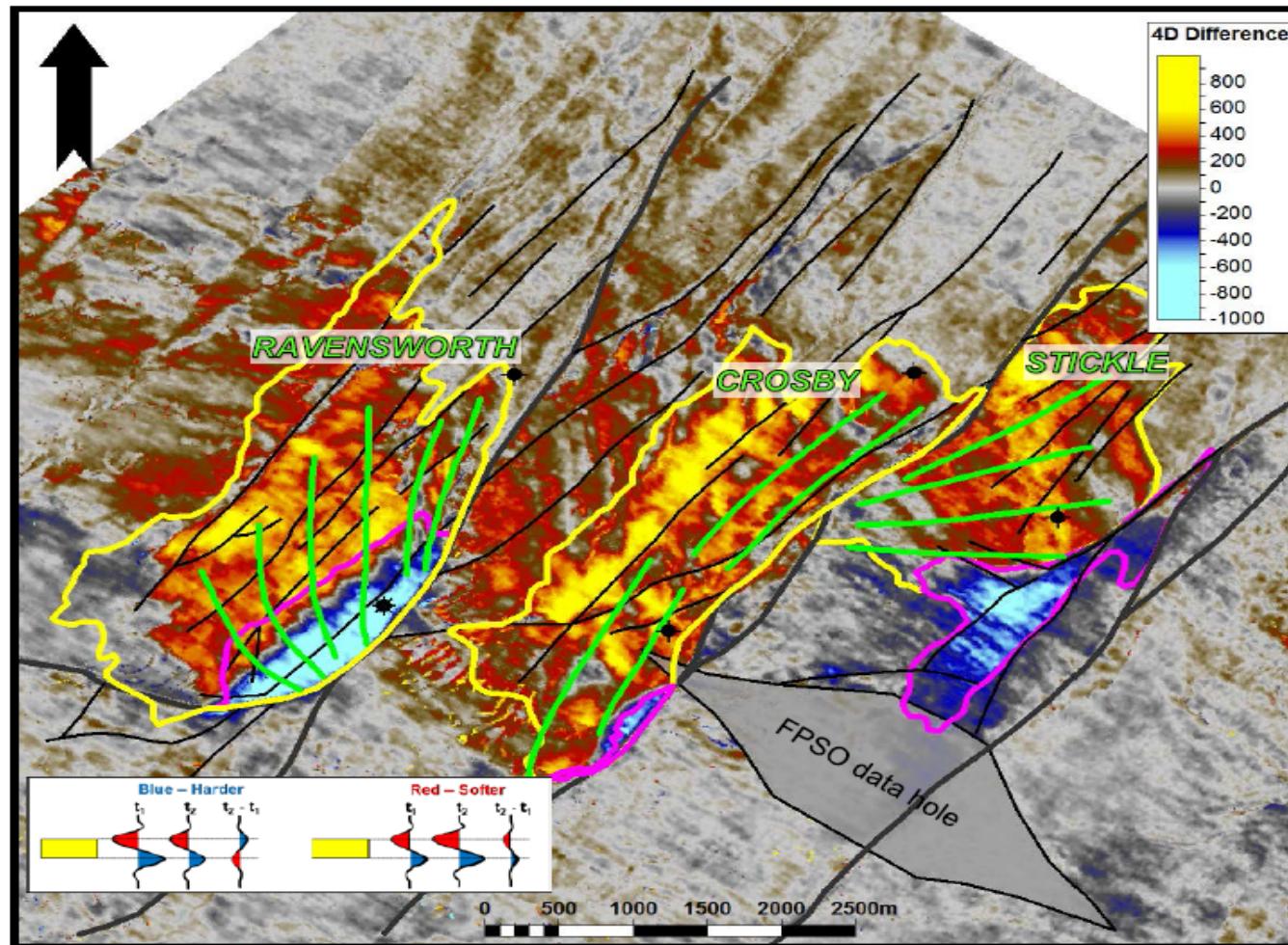
After



Lumley et al.

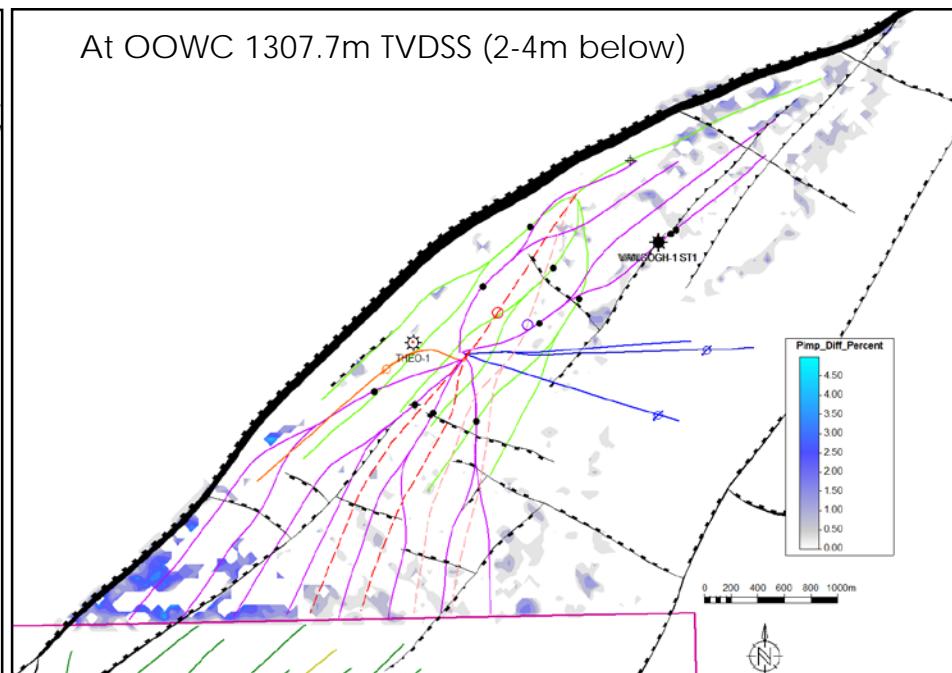
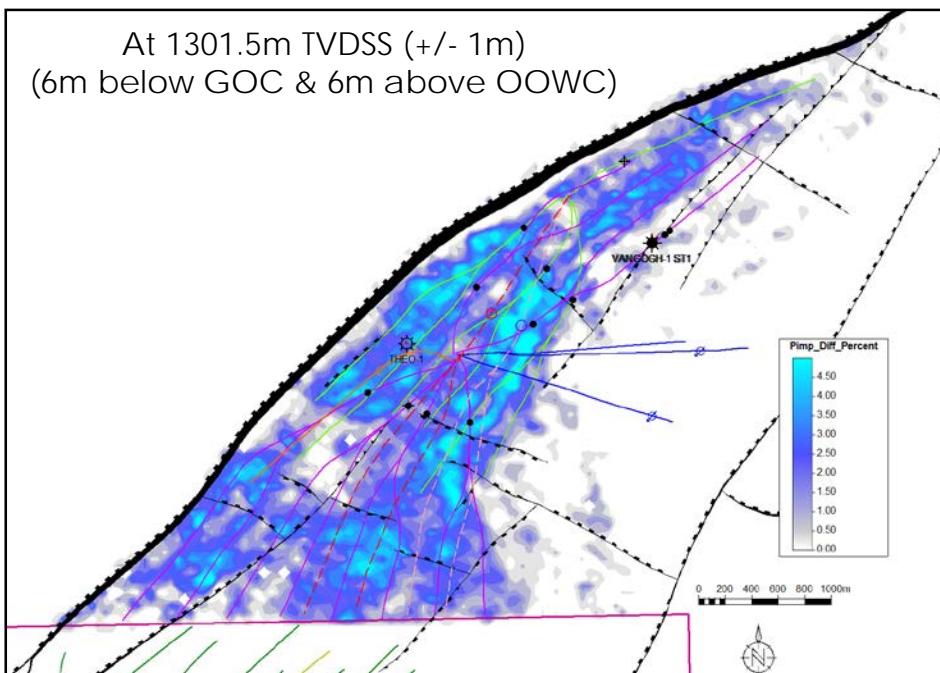
david.lumley@utdallas.edu

Full Angle Stack
Monitor minus Baseline



ASEG-PESA 2015 4D Seismic over the Pyrenees Fields: Duncan, et al.

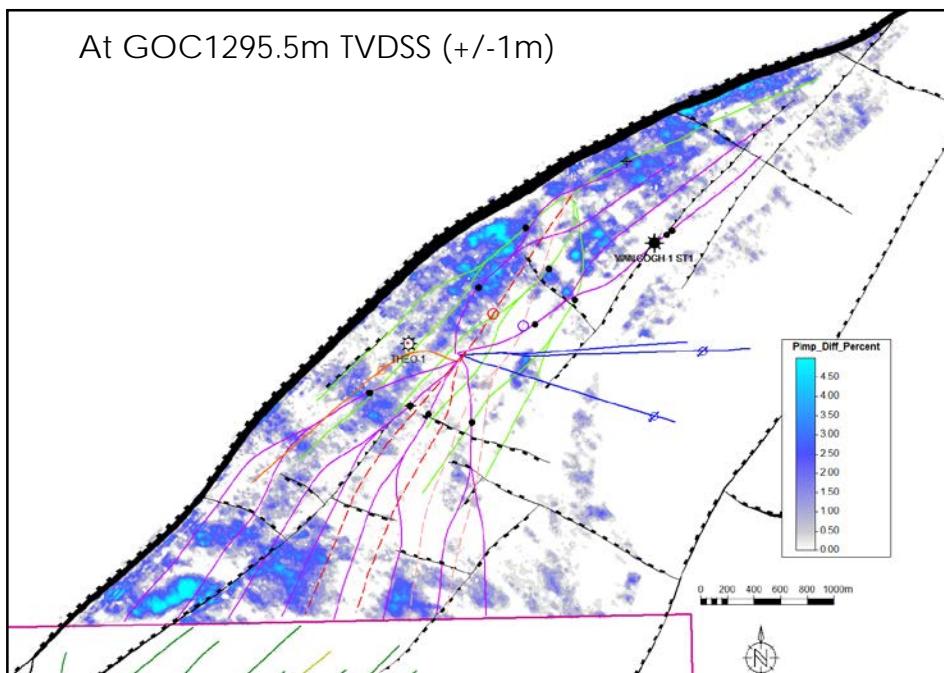
van GOGH: P-IMP 4D_{DIFF} %



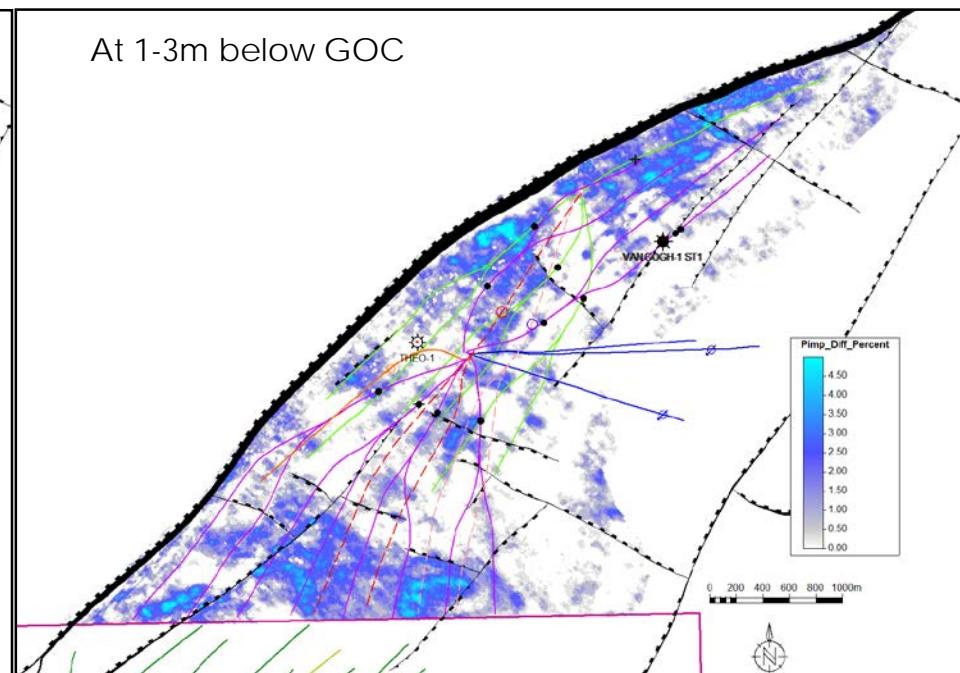
Bouloudas et al., Quadrant, 2015

van GOGH: P-IMP 4D_{DIFF} %

At GOC1295.5m TVDSS (+/-1m)

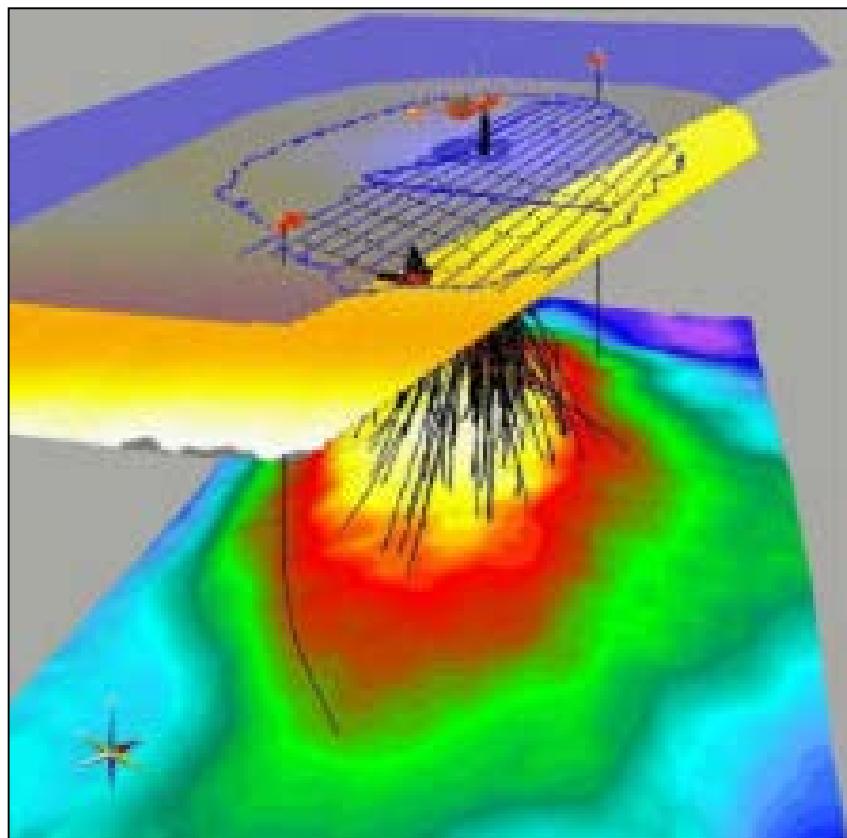


At 1-3m below GOC

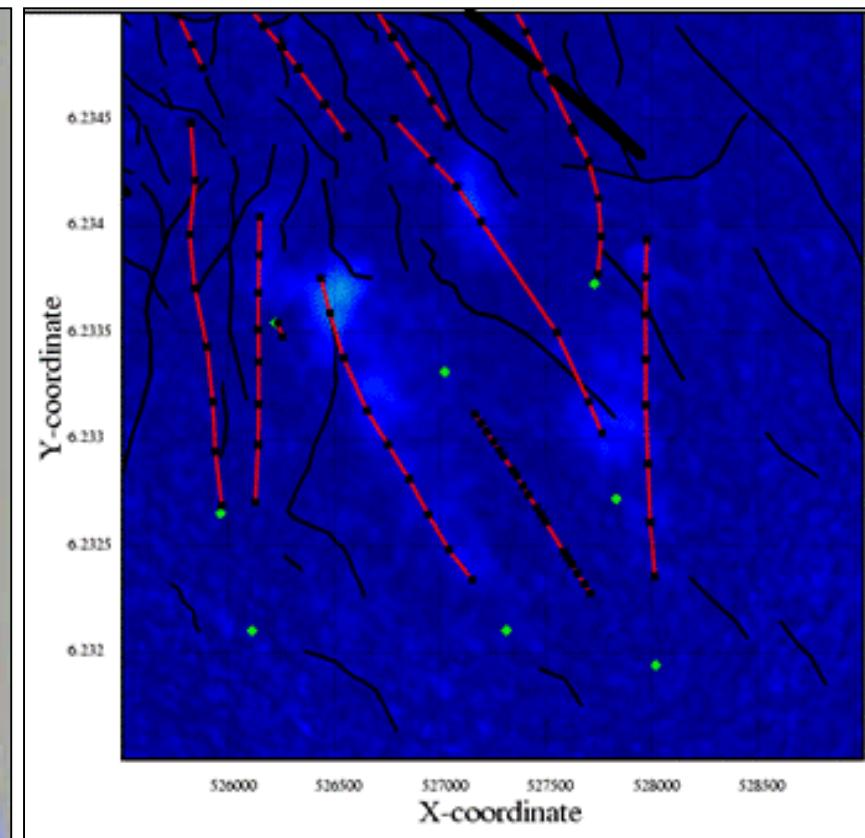


Bouloudas et al., Quadrant, 2015

Valhall permanent seafloor array



Barkved et al., 2004



courtesy BP

3D + 4D Seismic Inversion

Inverse theory (inversion)

$$d = F(m) ; m = F^{-1}(d)$$

d = data

m = model

F = physics

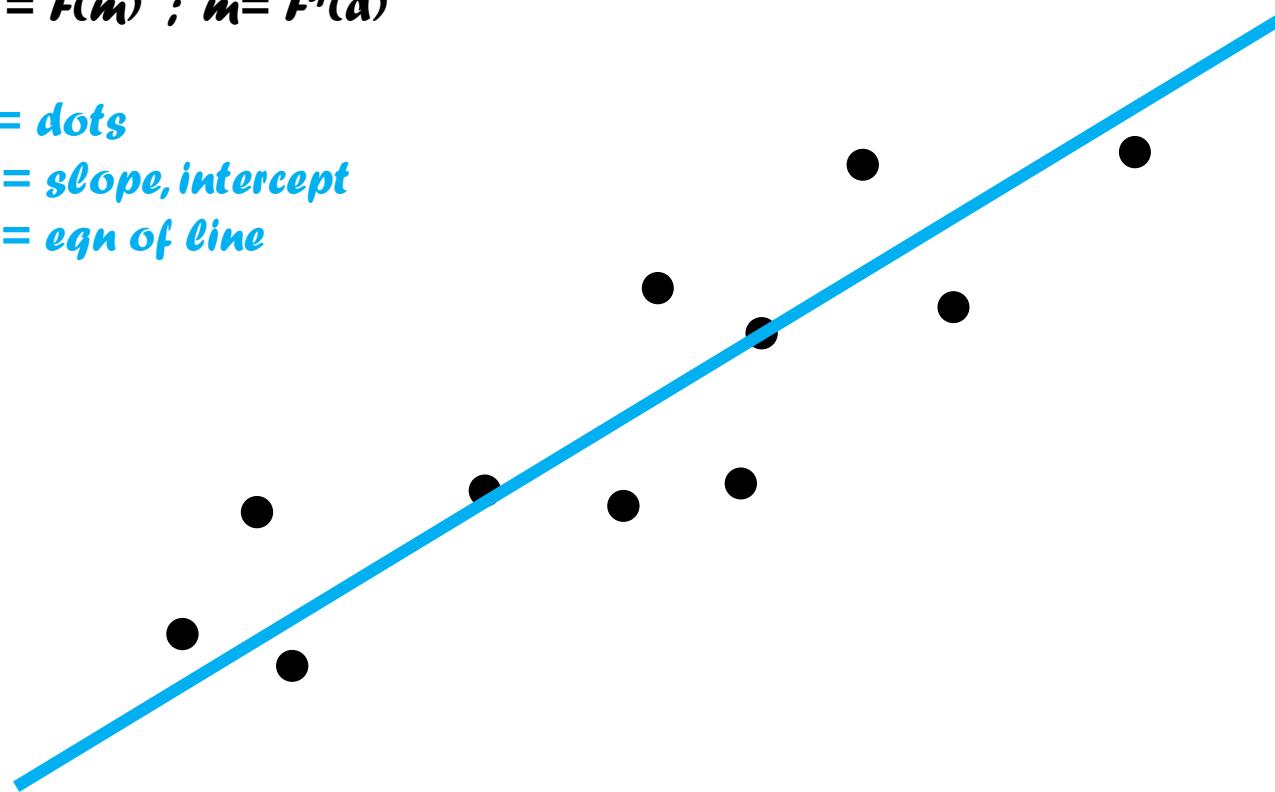
Inverse theory (inversion)

$$\mathbf{d} = \mathcal{F}(\mathbf{m}) ; \mathbf{m} = \mathcal{F}^{-1}(\mathbf{d})$$

\mathbf{d} = dots

\mathbf{m} = slope, intercept

\mathcal{F} = eqn of line



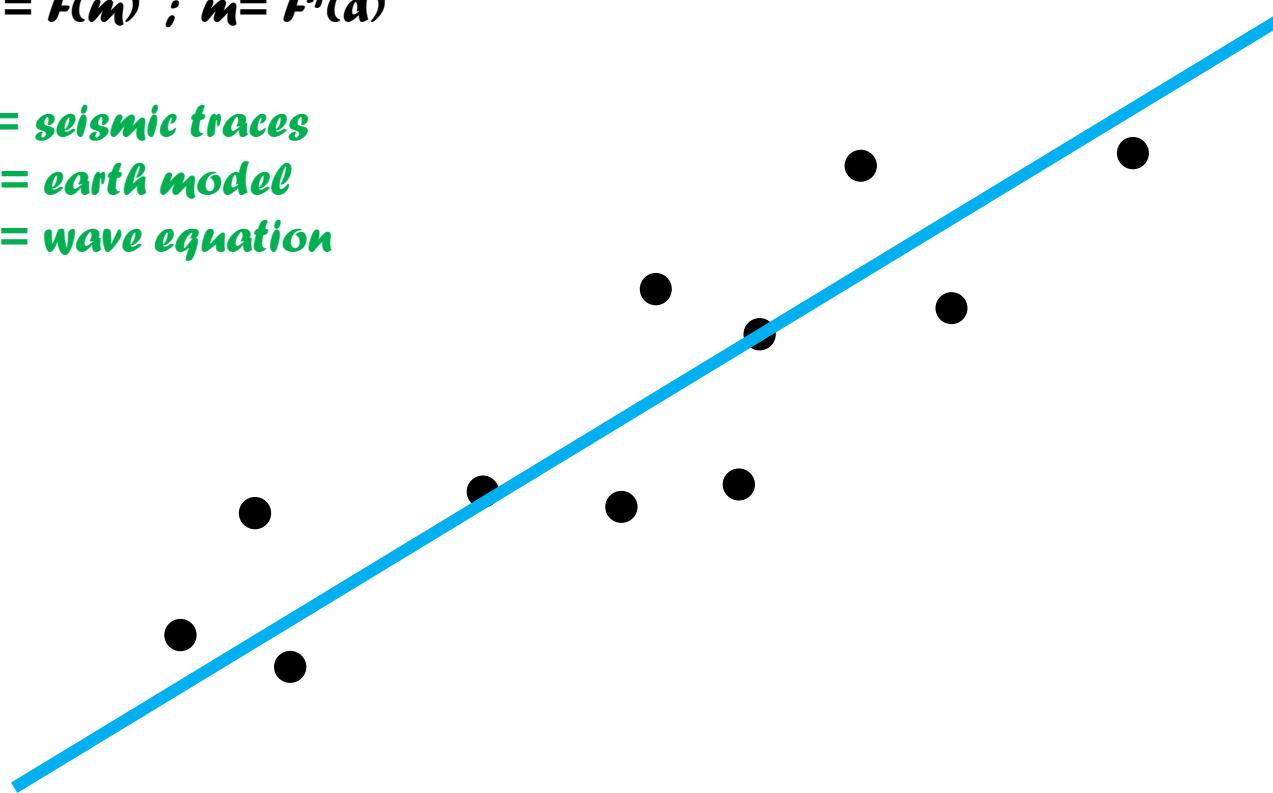
Inverse theory (inversion)

$$\mathbf{d} = \mathcal{F}(\mathbf{m}) ; \mathbf{m} = \mathcal{F}^{-1}(\mathbf{d})$$

\mathbf{d} = seismic traces

\mathbf{m} = earth model

\mathcal{F} = wave equation



Scalar wave equation modeling

$$\mathbf{d} = \mathcal{F}\mathbf{m}$$

$$(v^2 \nabla^2 - \partial_{tt}) P(\underline{x}, t) = 0$$

$$\mathbf{m} = v(\underline{\mathbf{x}})$$

$$\mathcal{F} = \nabla^2 - \partial_{tt}$$

$$\mathbf{d} = P(\underline{\mathbf{x}}, t)$$

Full waveform inversion

$$\textcolor{blue}{m} = \mathcal{F}^{-1}d$$

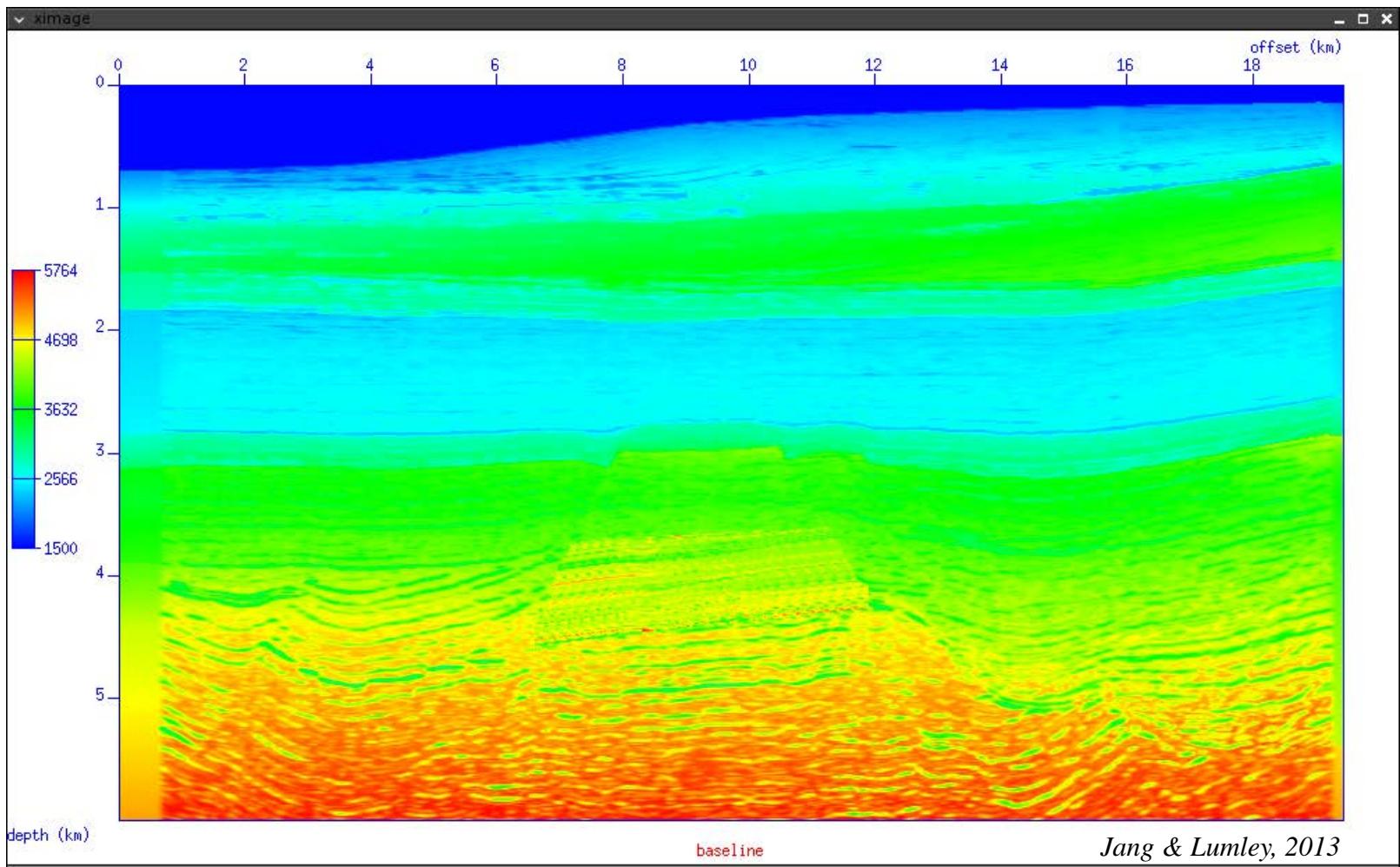
$$\min \mathcal{E}^2 = w_d^2(d - \mathcal{F}\textcolor{blue}{m})^2 + w_m^2(m - m_o)^2 + \dots$$

subject to constraints: $\nabla \textcolor{blue}{m} \approx 0$ etc...

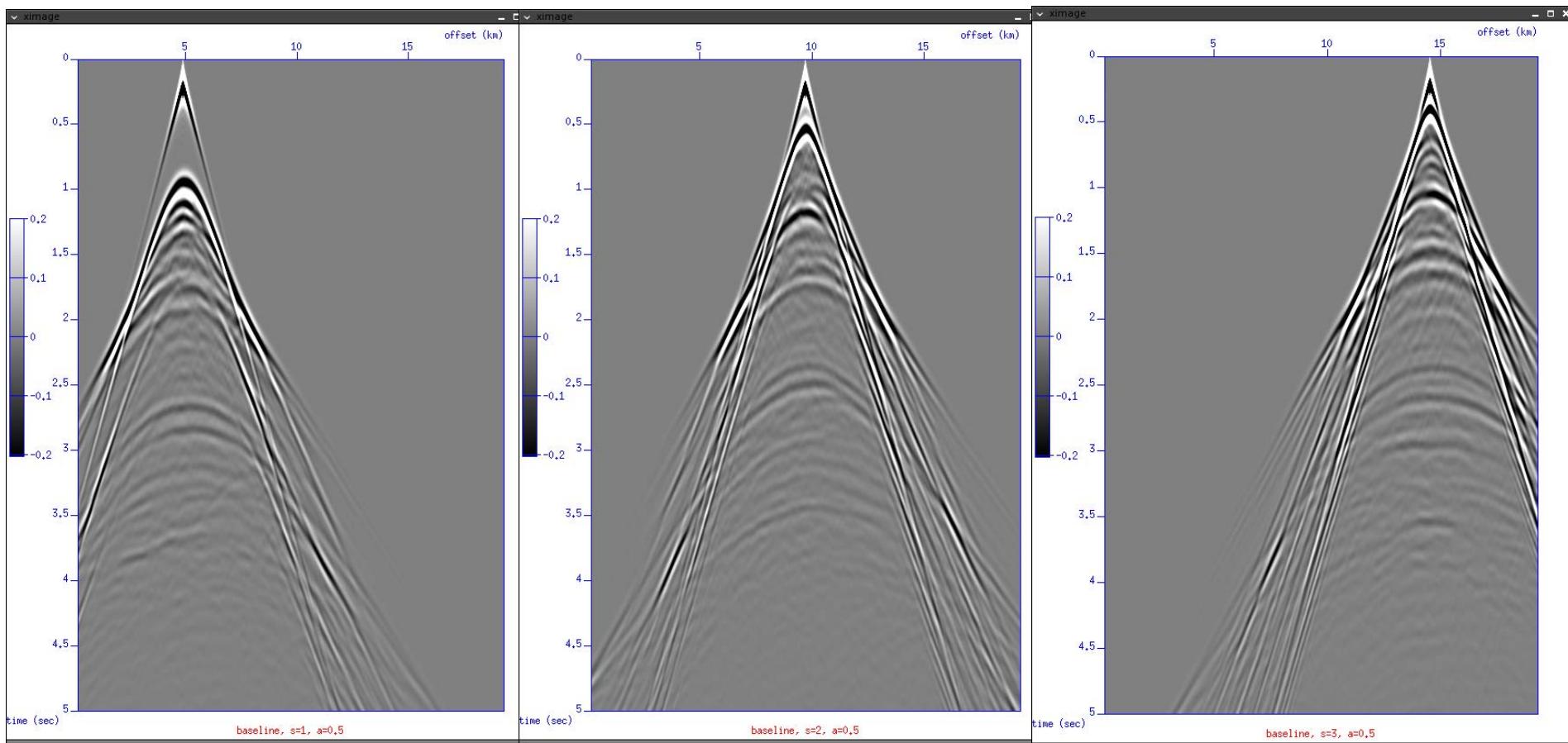
\mathcal{F} 2-way WEQ modeling operator

$\textcolor{blue}{m}$ 2D/3D elastic/velocity model

True velocity model

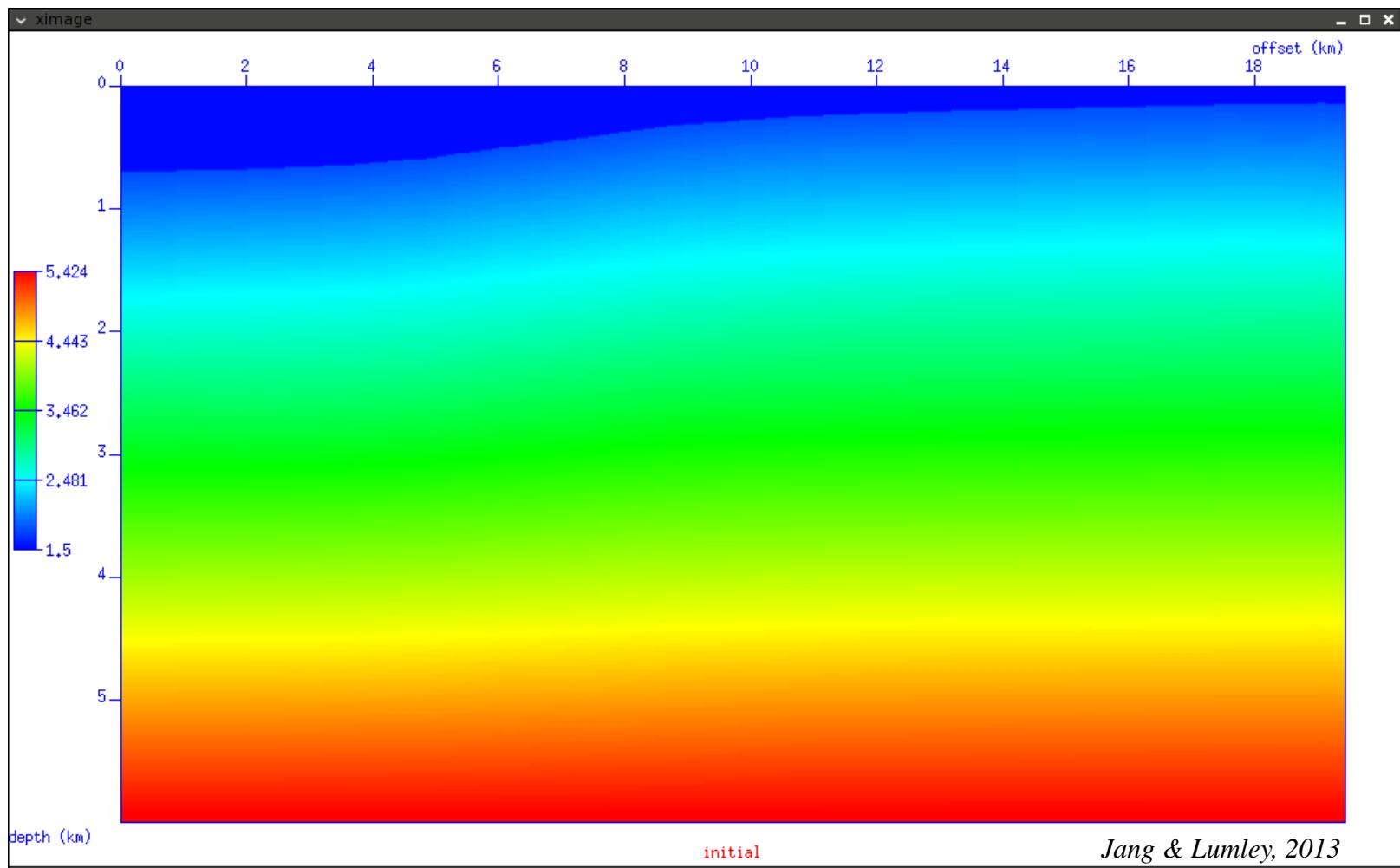


Seismic shot gathers

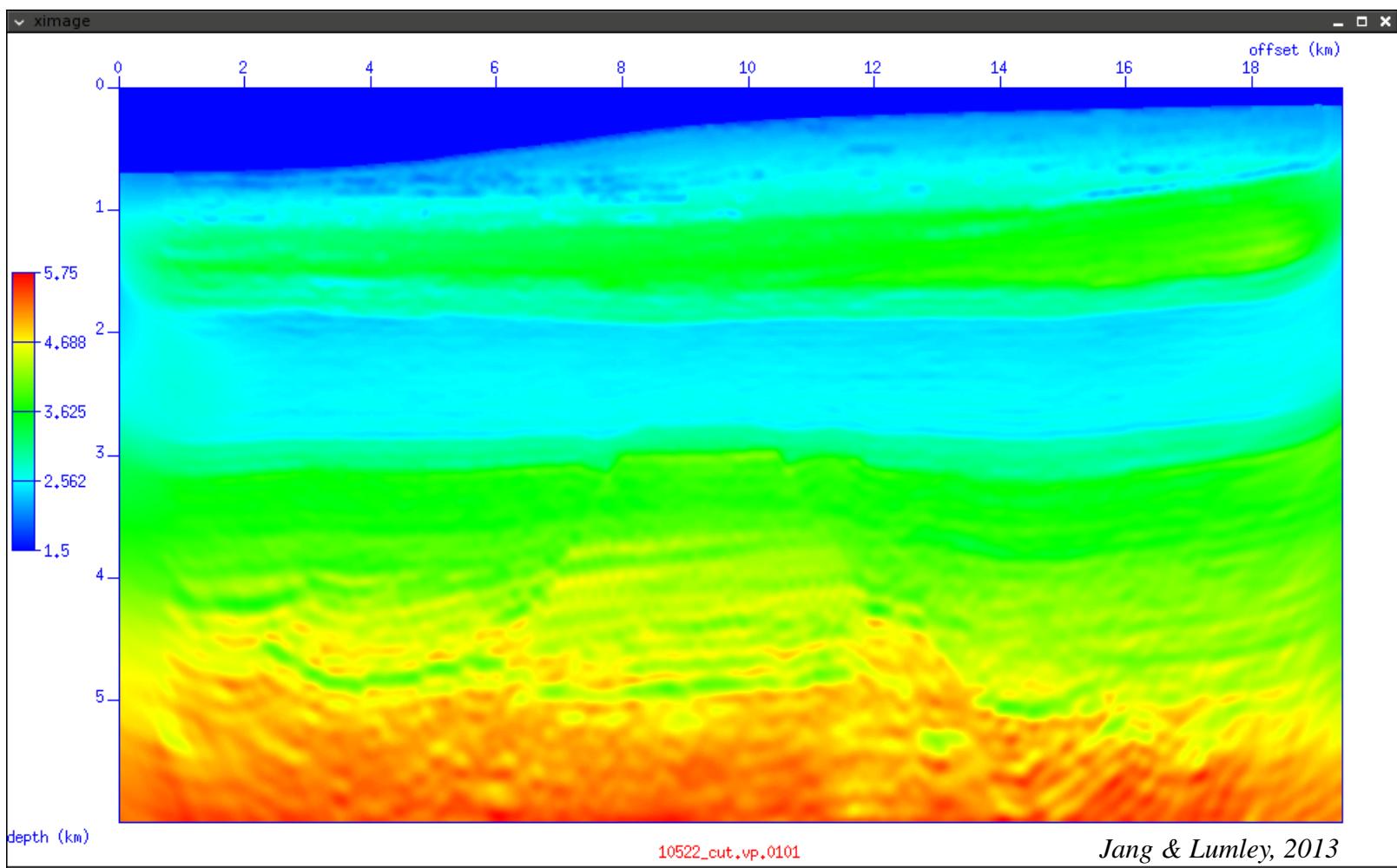


Jang & Lumley, 2013

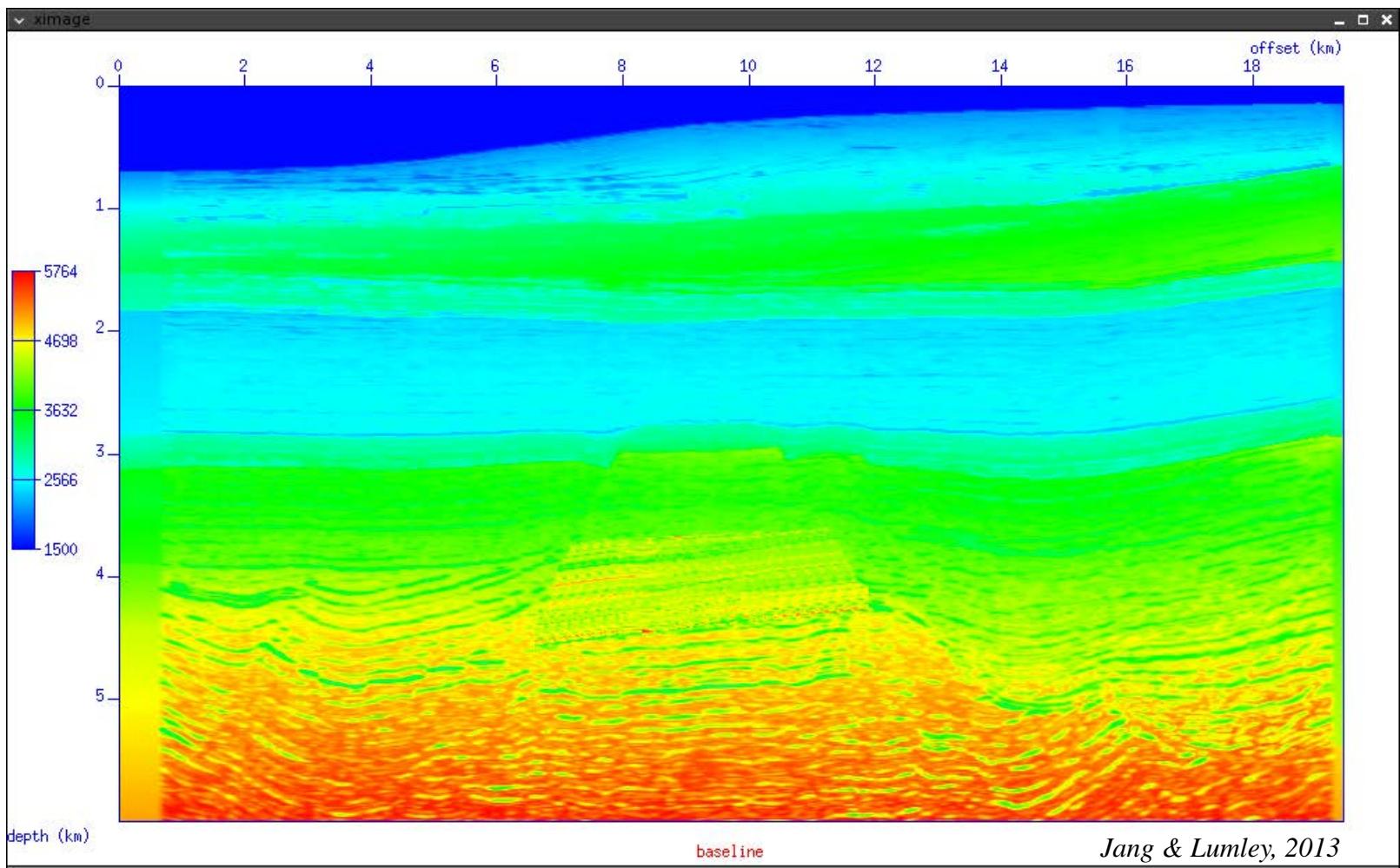
Initial velocity model



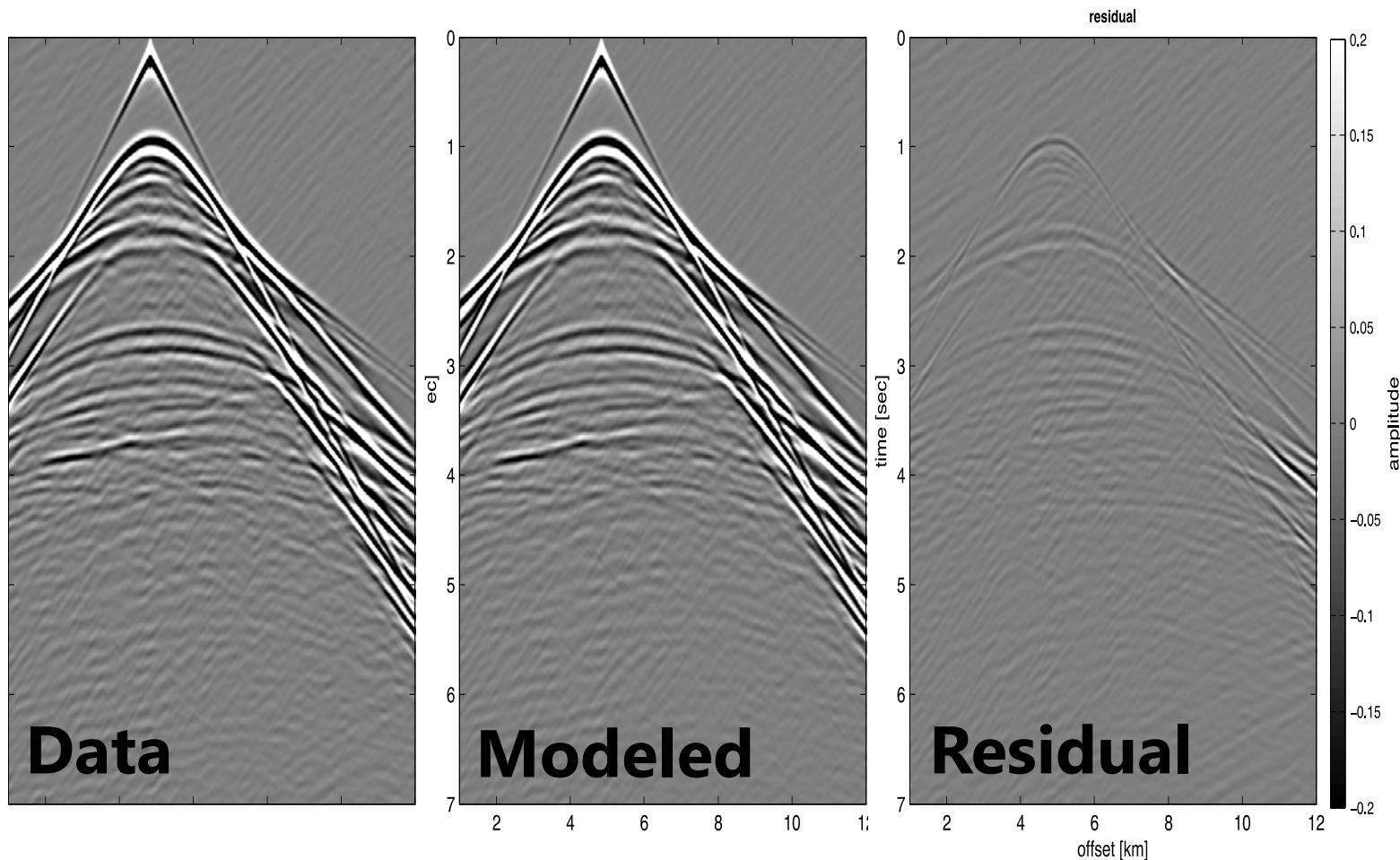
Inverted velocity model



True velocity model



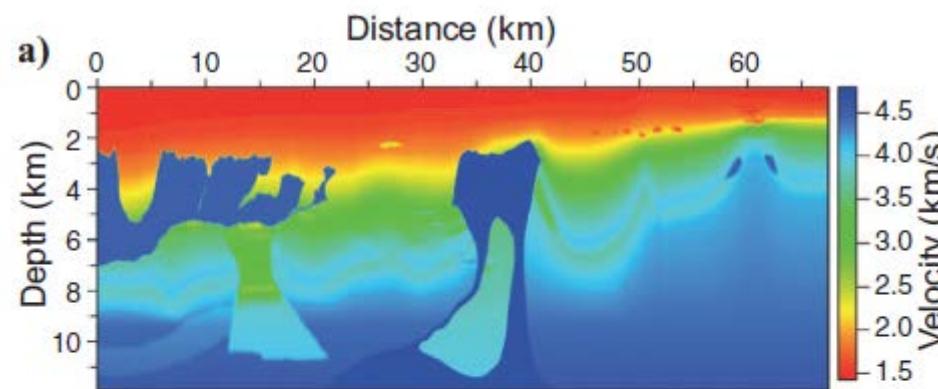
Seismic shot gathers



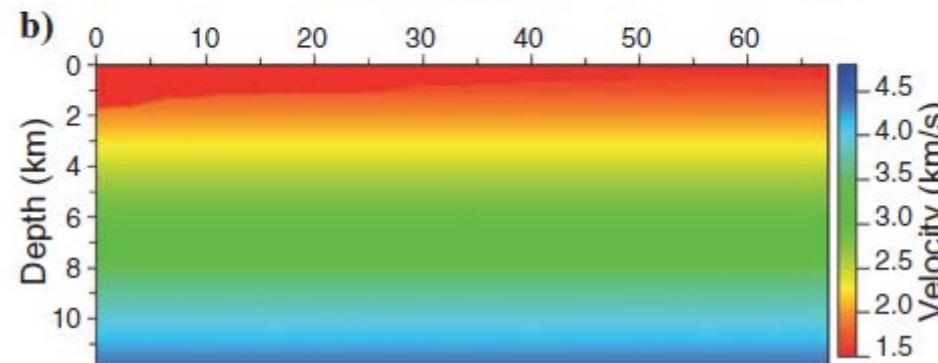
Jang & Lumley, 2013

Full waveform inversion

true model



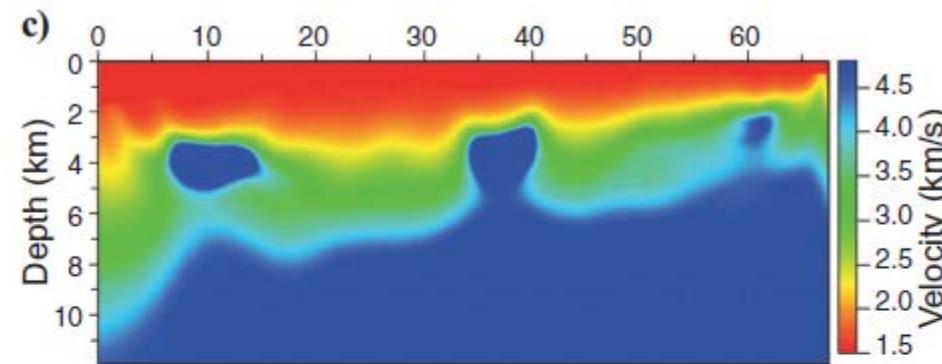
initial model



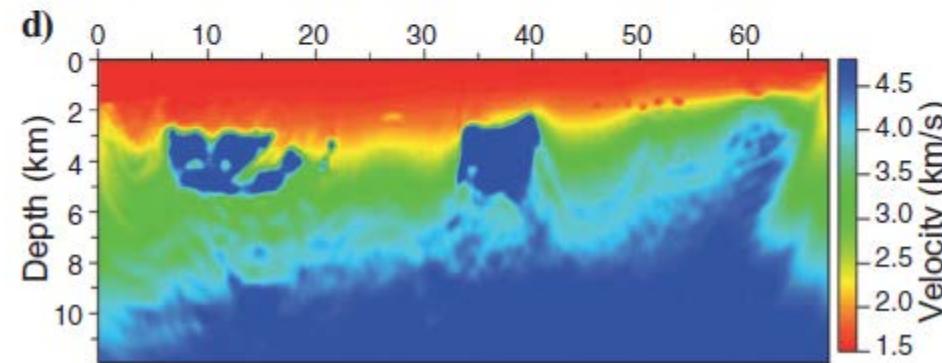
Shin & Cha 2009

Full waveform inversion

Laplace



Laplace+Fourier

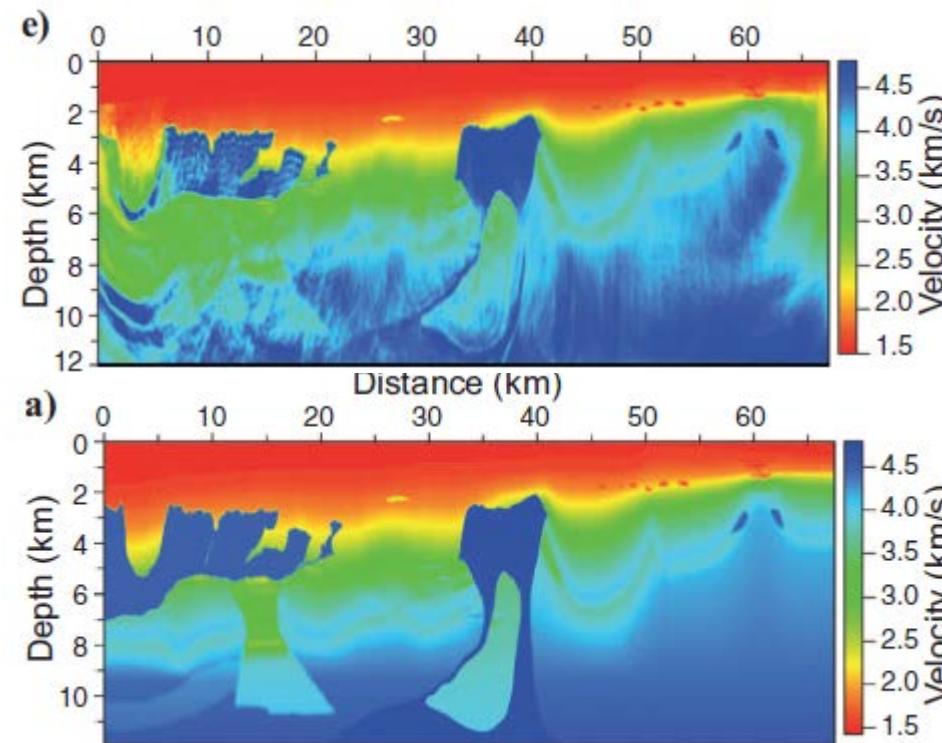


Shin & Cha 2009

Full waveform inversion

+Fourier

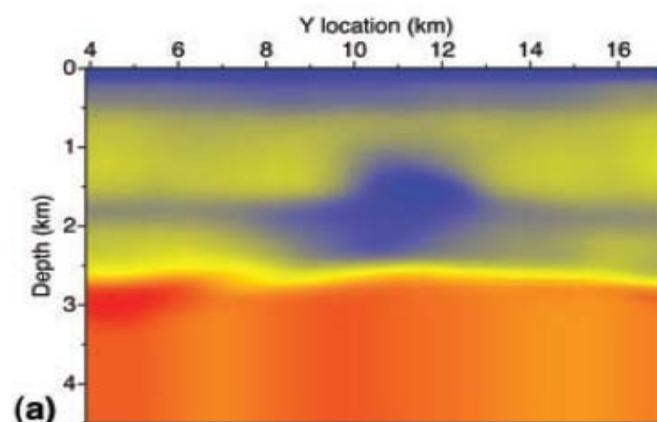
true model



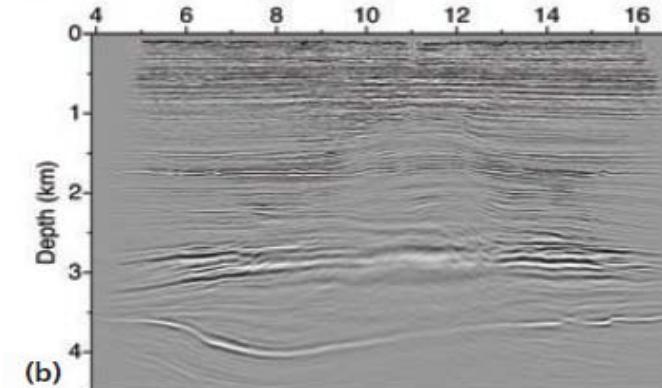
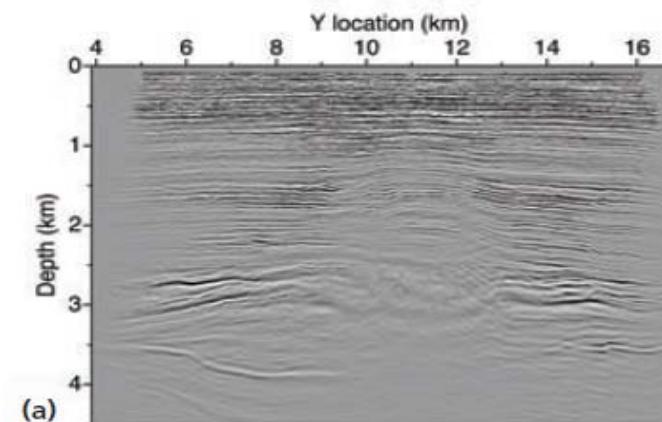
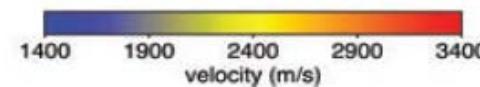
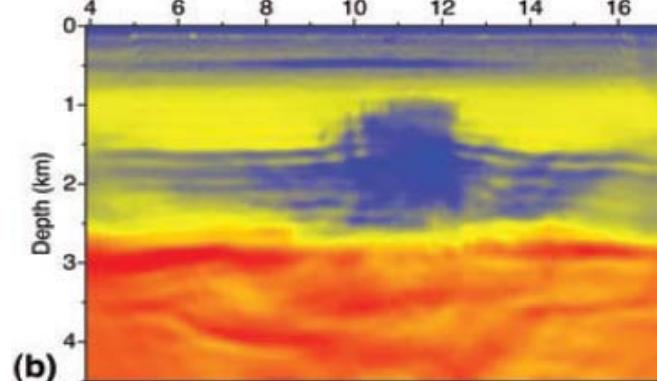
Shin & Cha 2009

Full waveform inversion

MVA



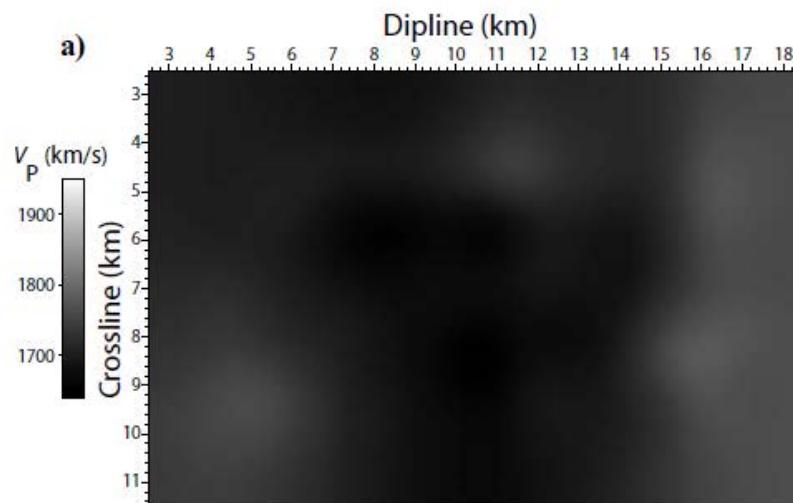
FWI



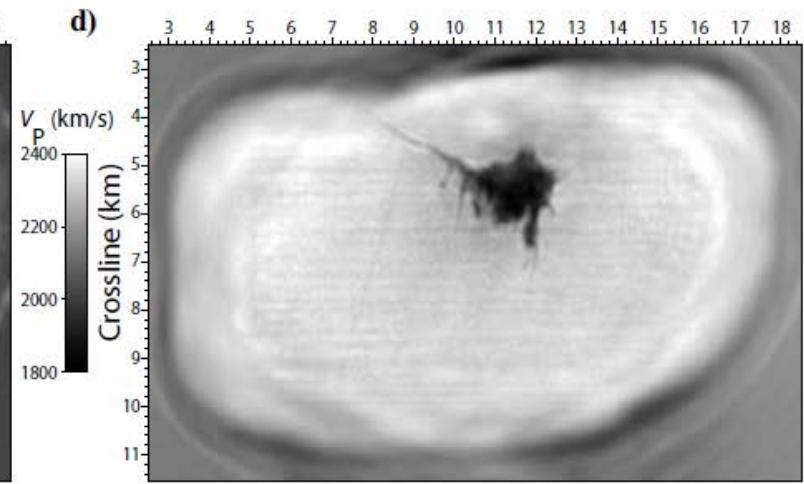
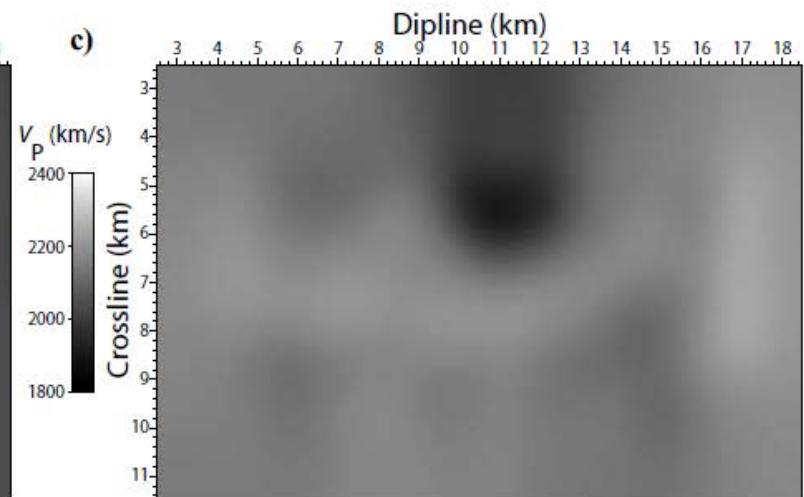
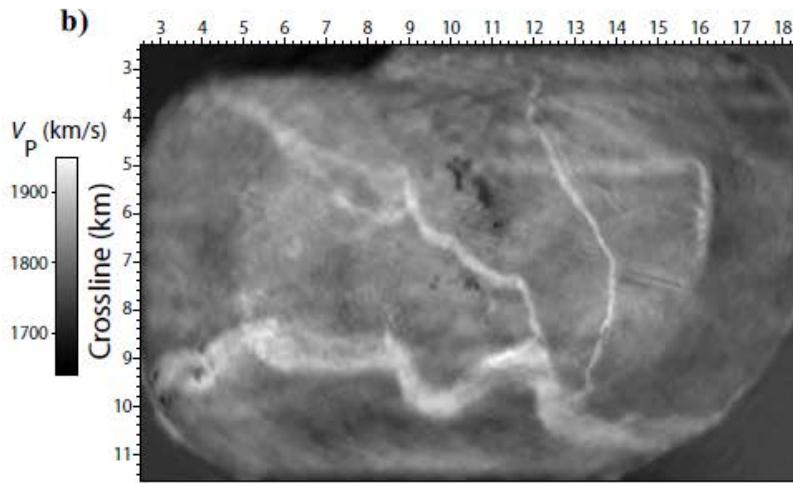
Sirgue et al. 2010

Full waveform inversion

Tomo

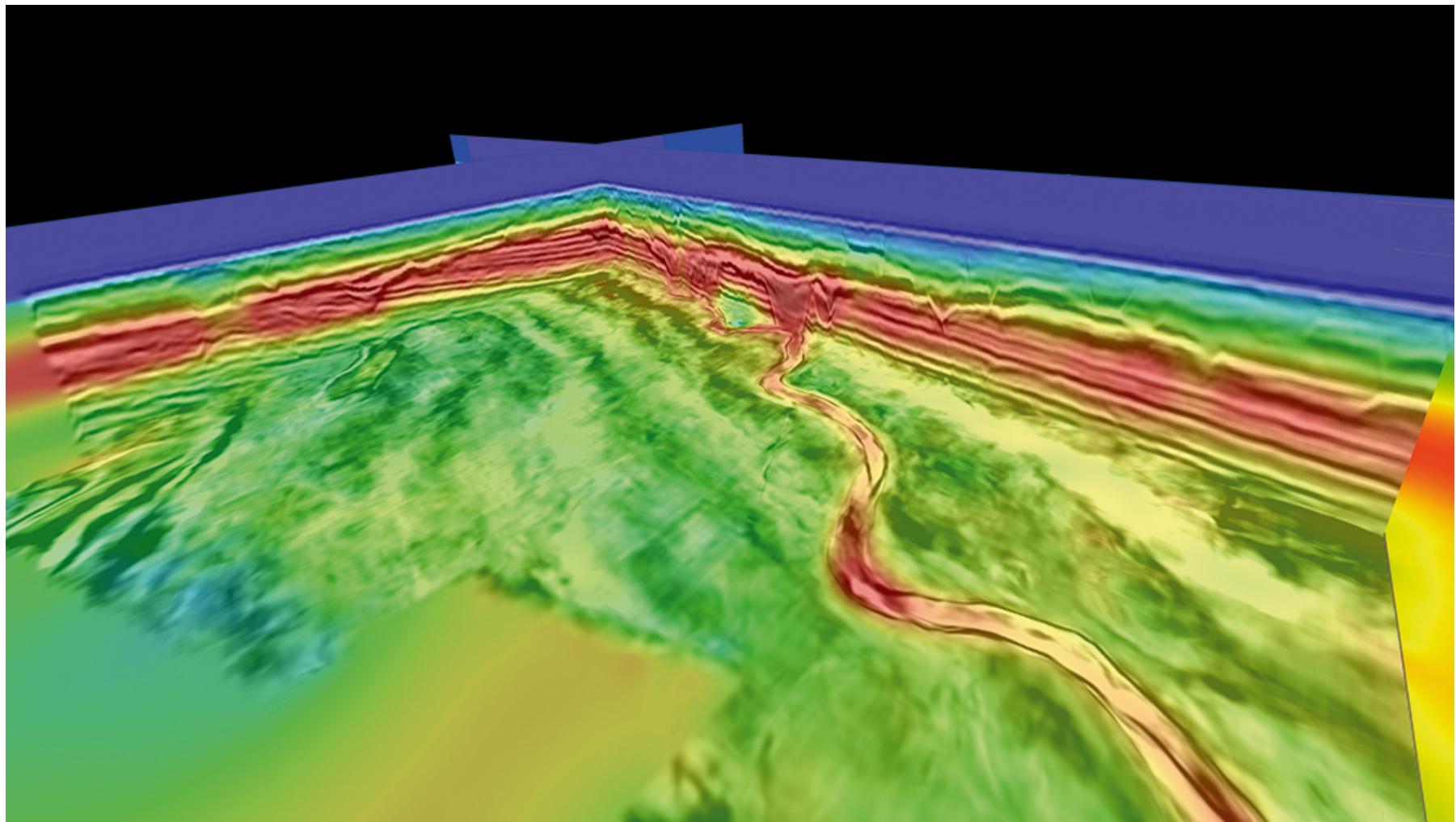


FWI



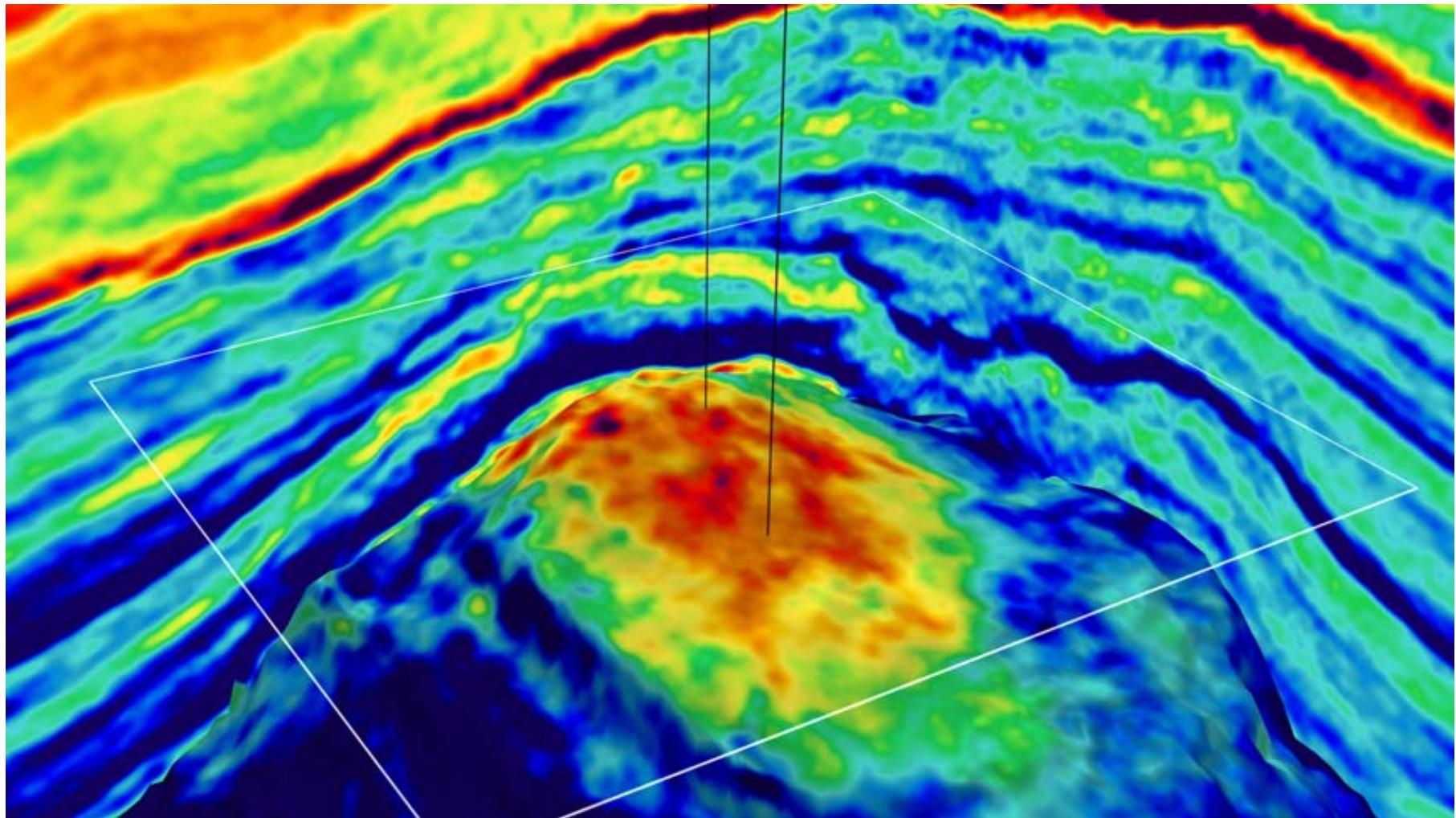
Sirgue & Barkved

Full waveform inversion



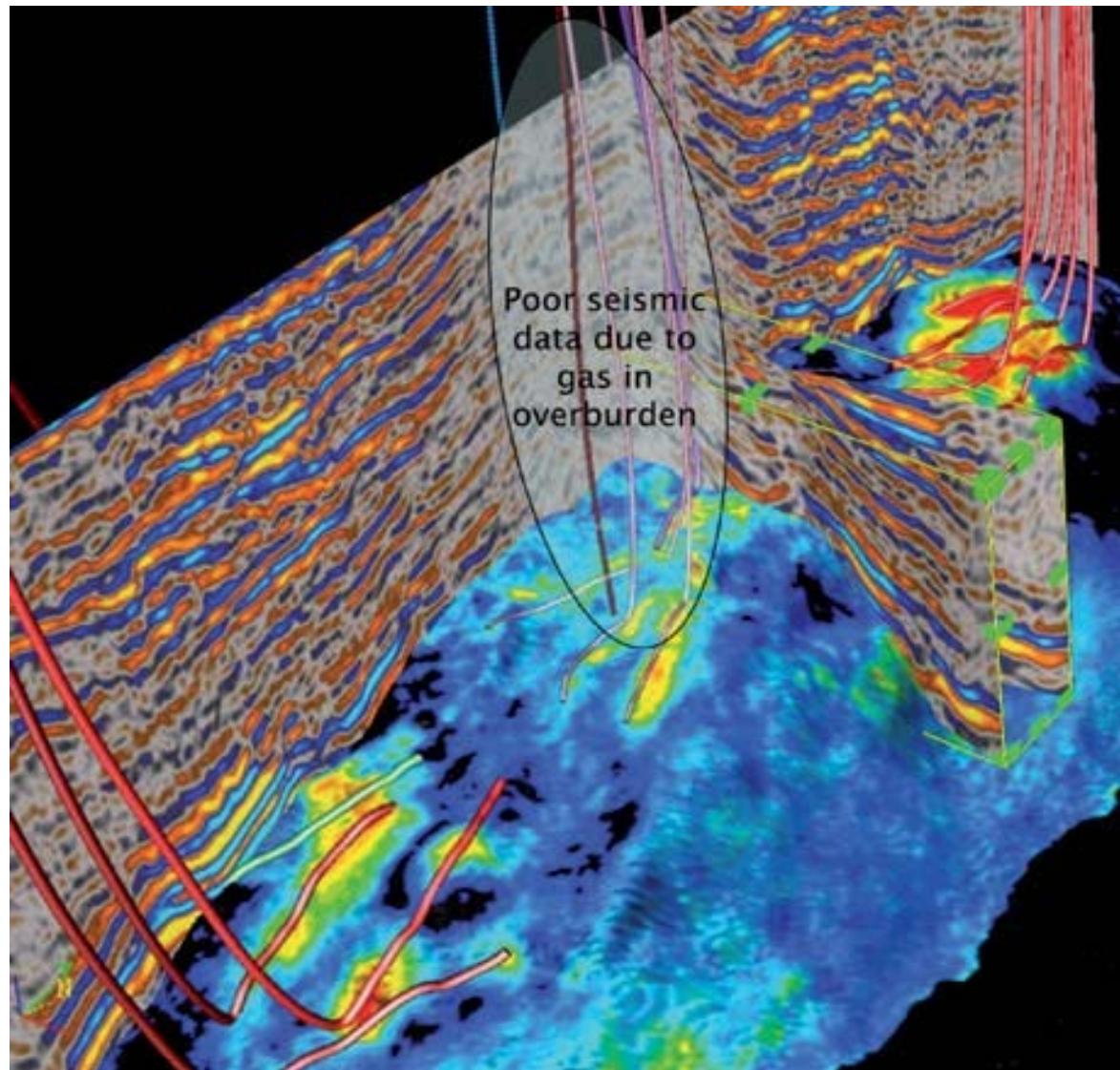
PGS

Full waveform inversion

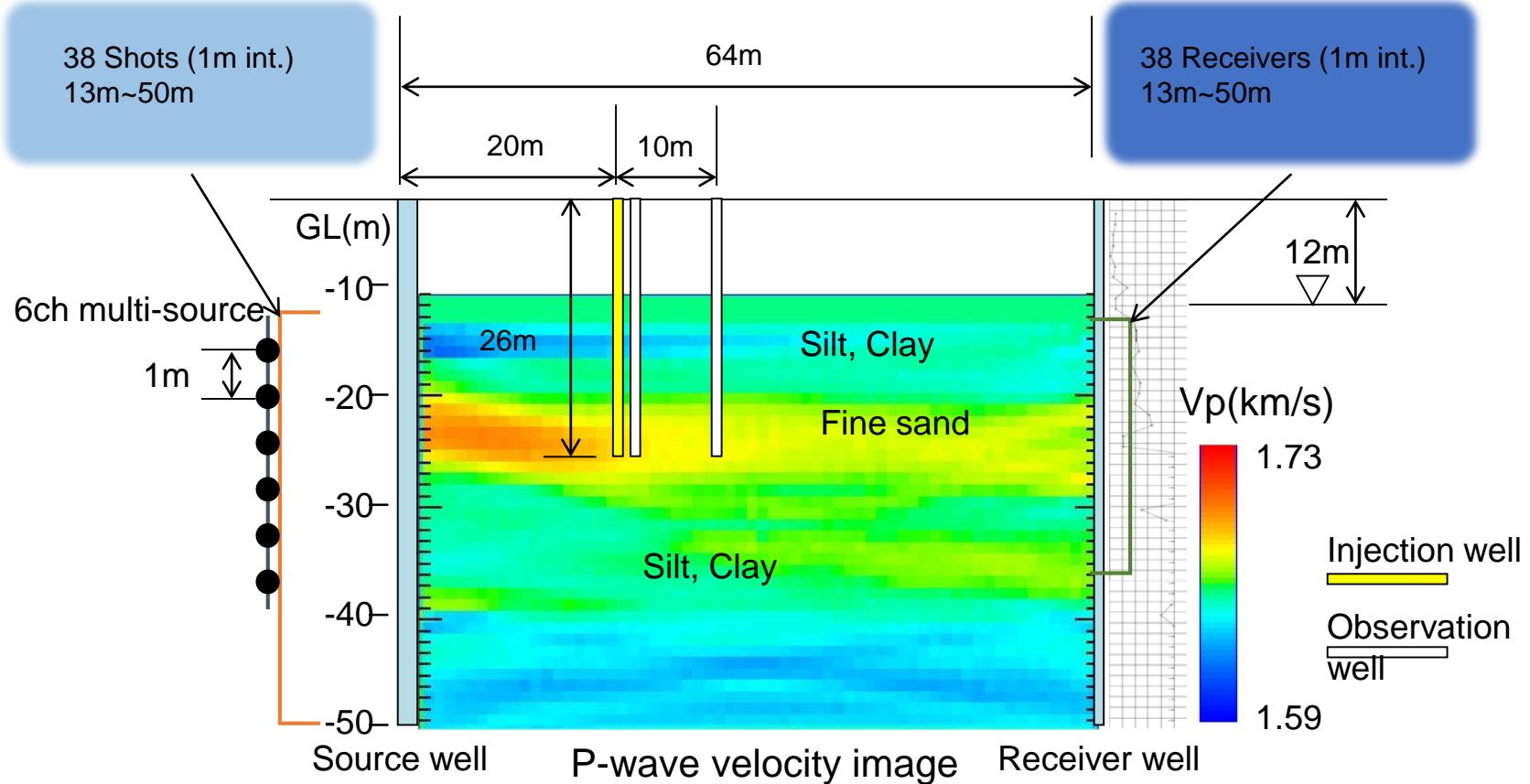


PGS

Full waveform inversion

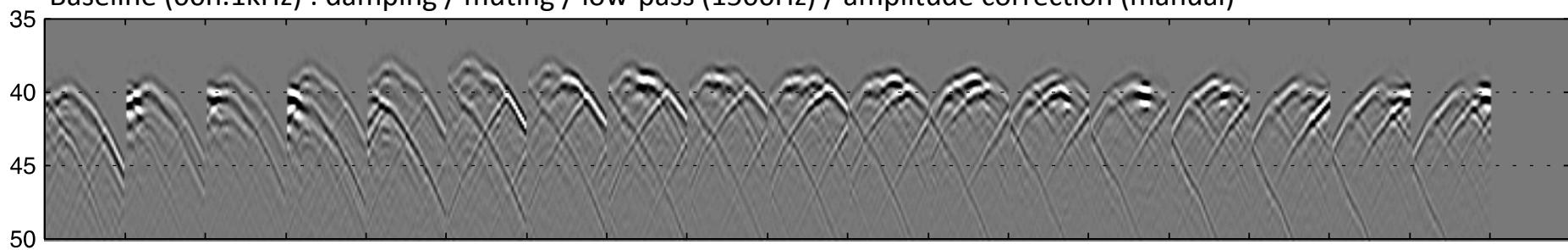


Cross-well FWI

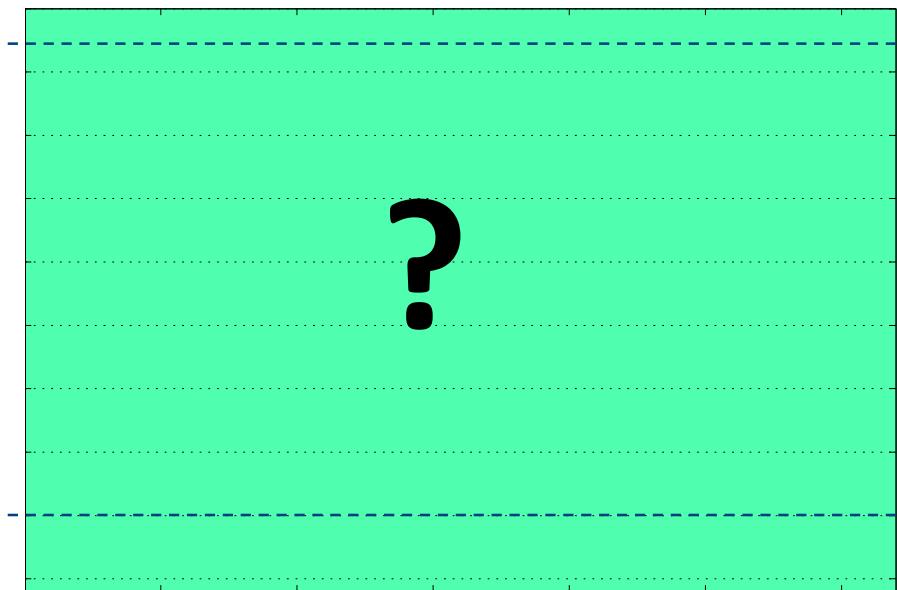
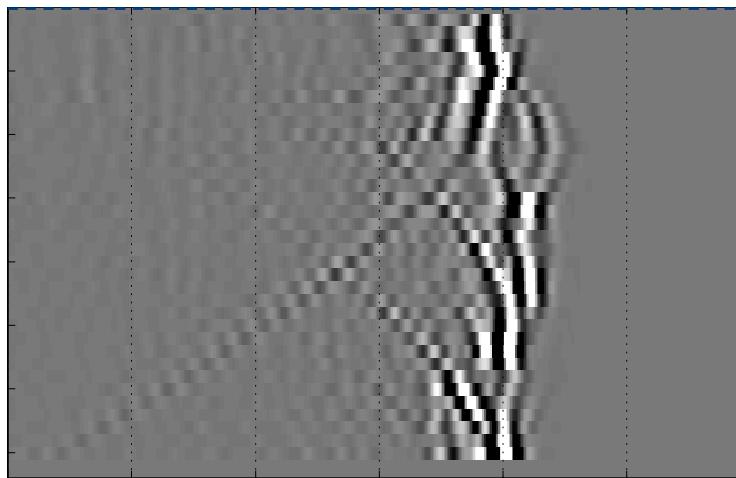


Cross-well data (real)

Baseline (00h.1kHz) : damping / muting / low-pass (1500Hz) / amplitude correction (manual)

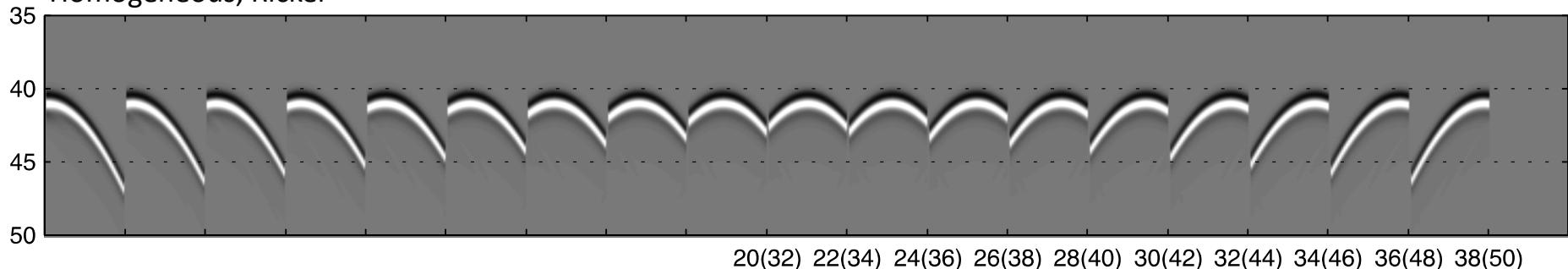


Same level section: Baseline (00h.1kHz)

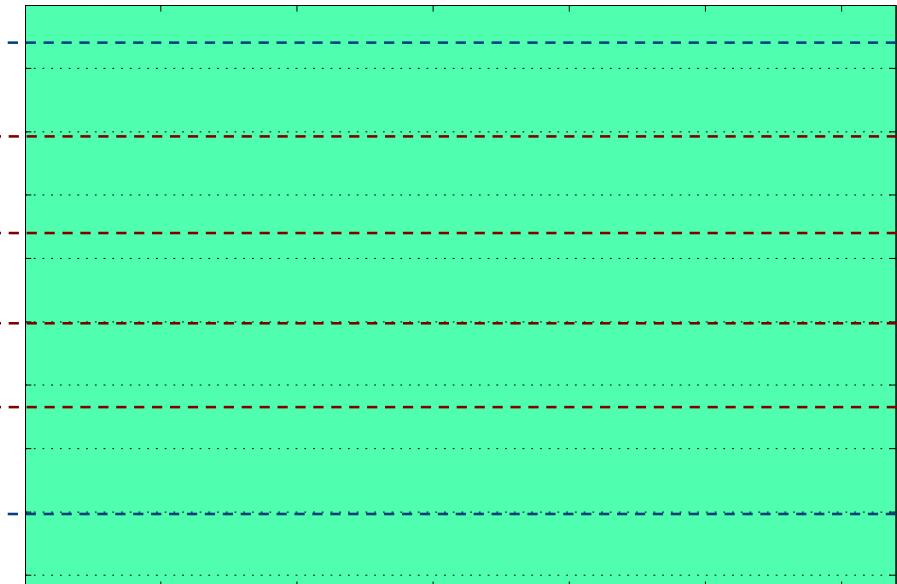
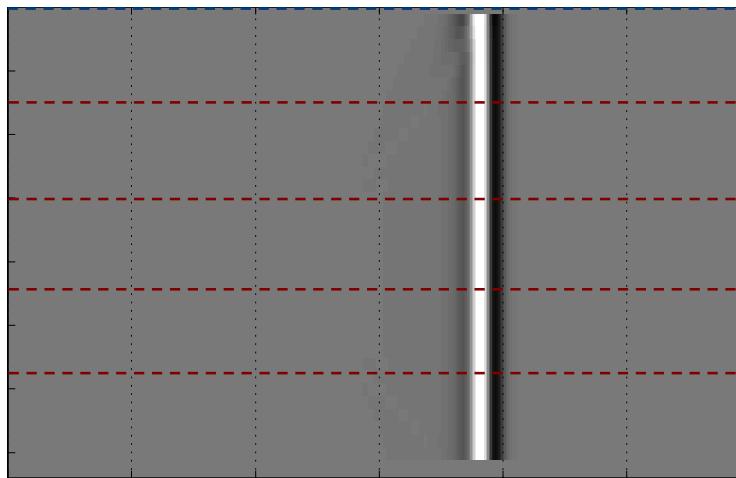


Cross-well data (modelled)

Homogeneous, Ricker



Same level section: Homogeneous, Ricker

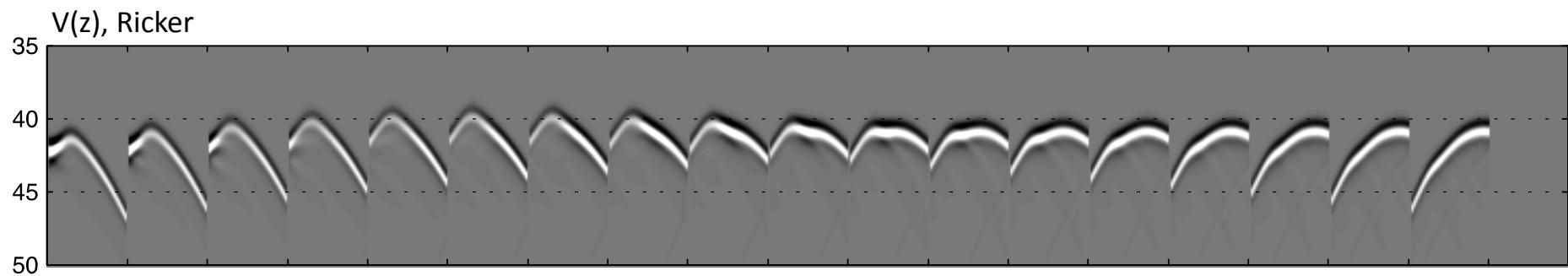


Kamei et al., 2016

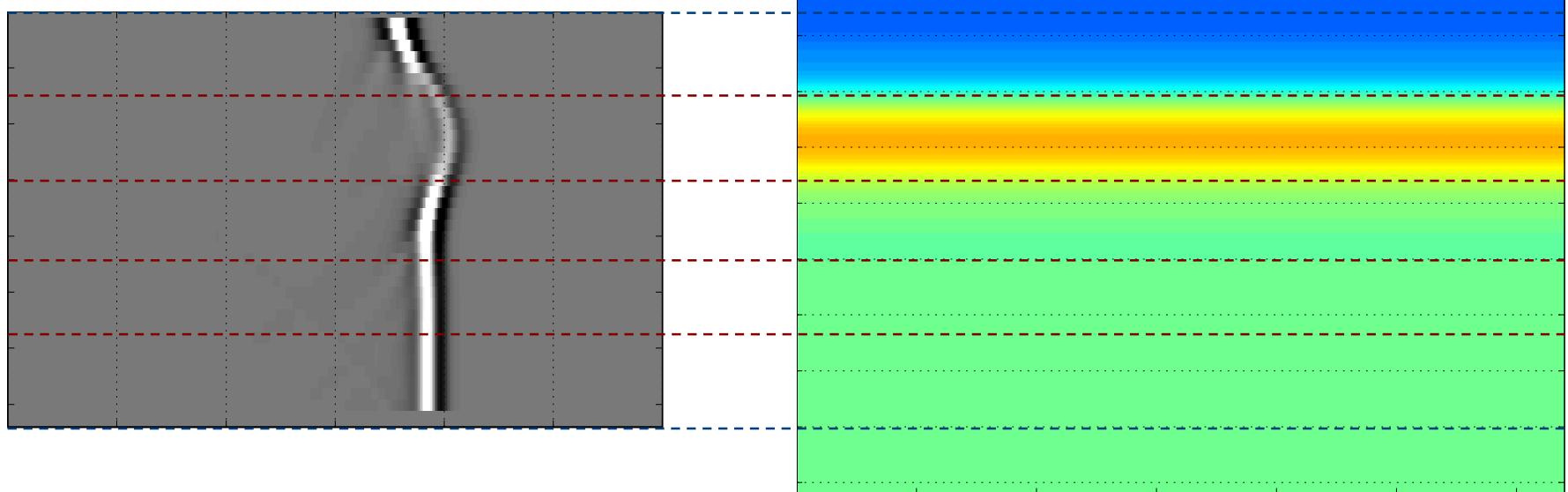
65 1.70 1.75

david.lumley@utdallas.edu

Cross-well data (modelled)

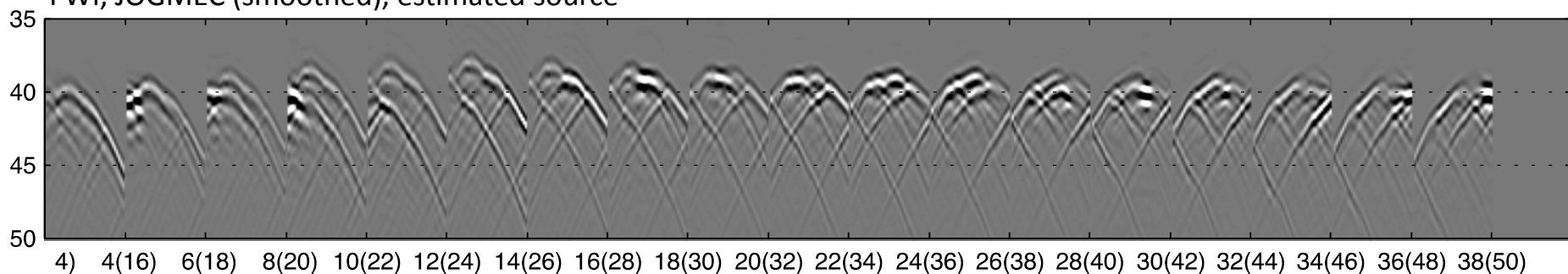


Same level section: V(z), Ricker

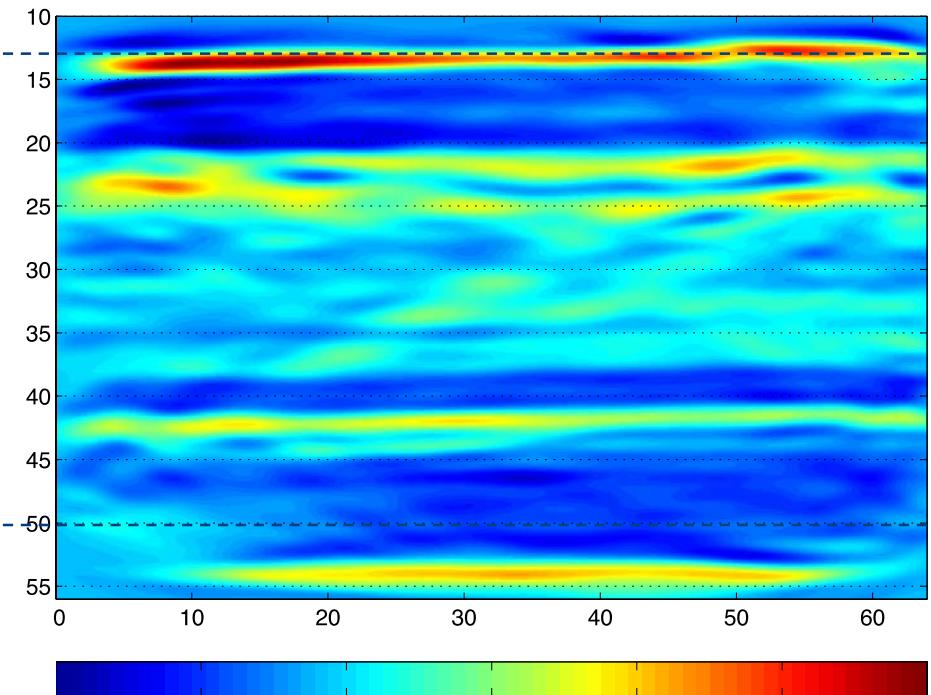
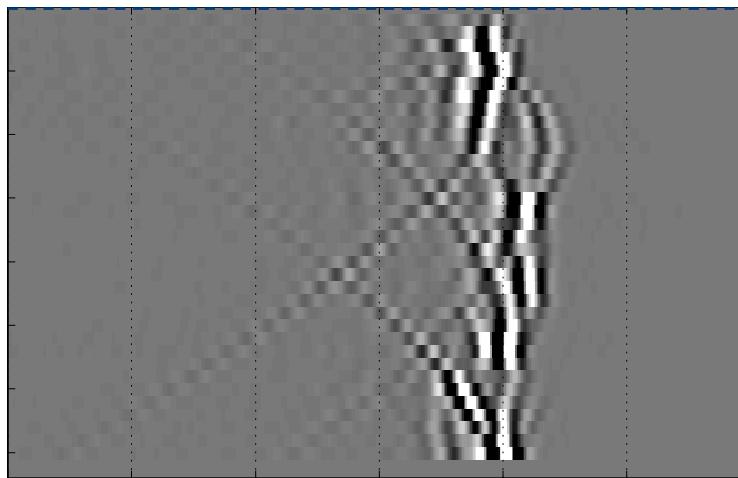


Cross-well data (modelled)

FWI, JOGMEC (smoothed), estimated source

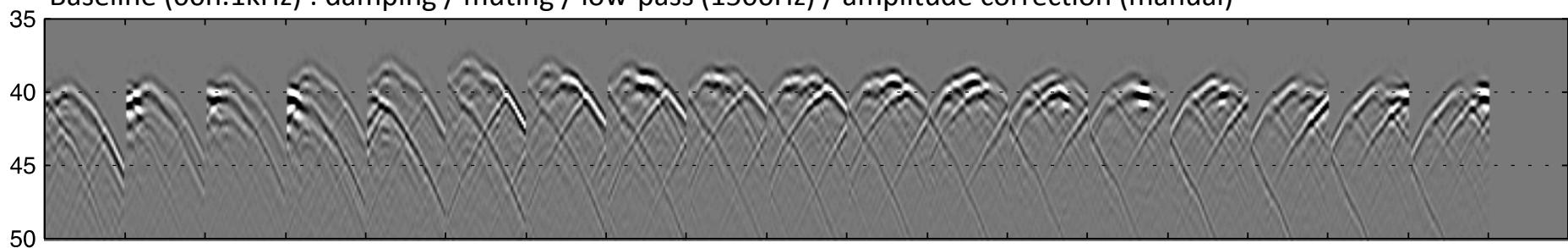


Same level section: FWI, JOGMEC, estimated source

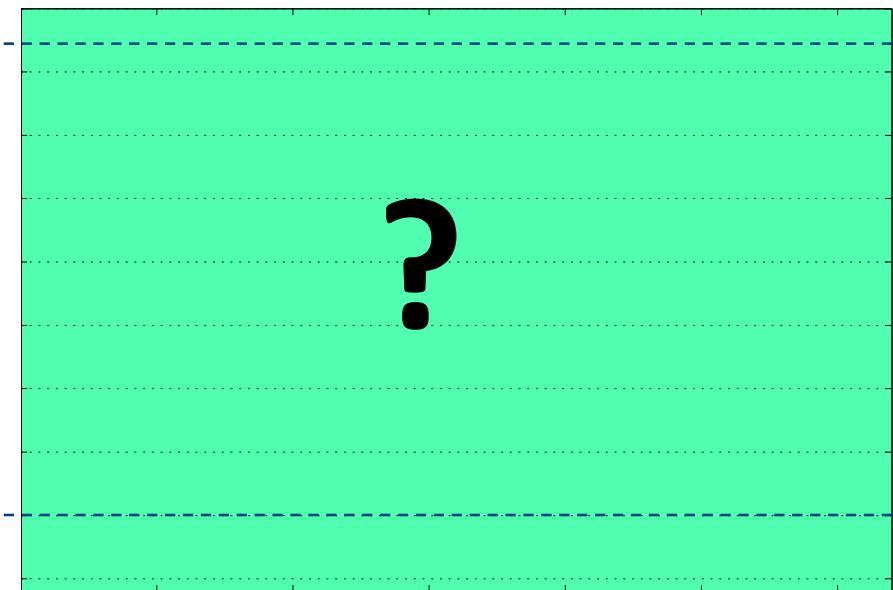
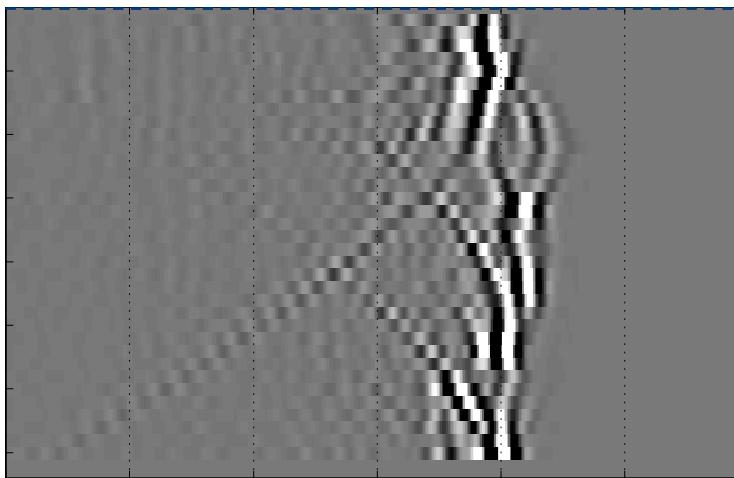


Cross-well data (real)

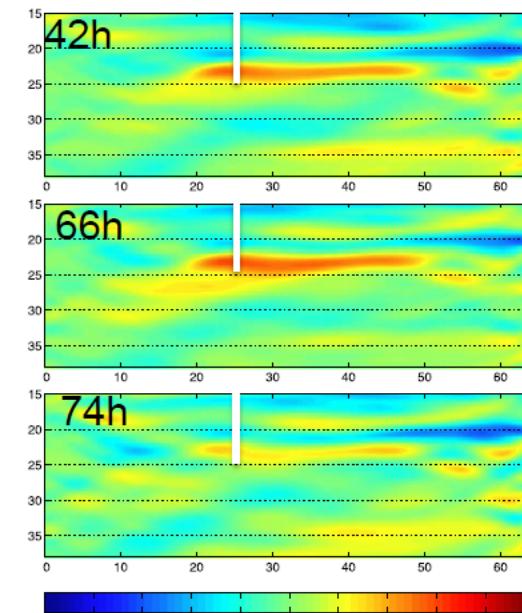
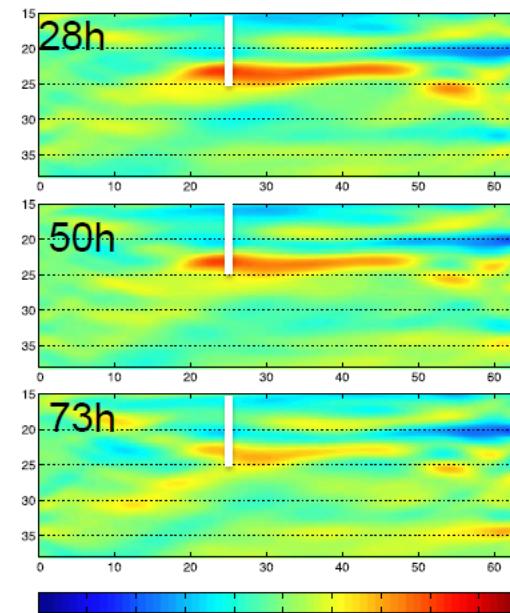
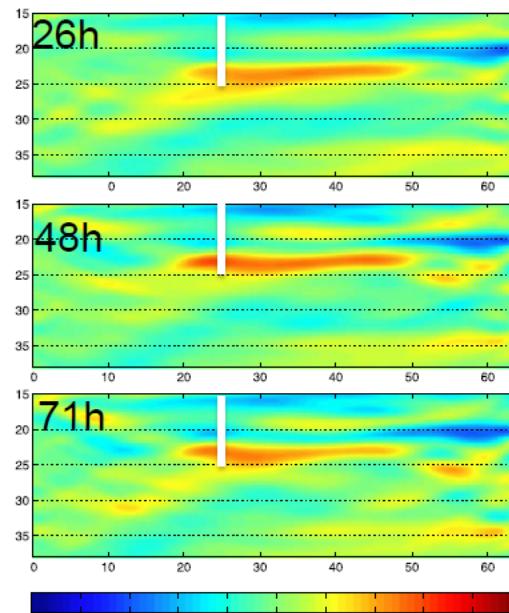
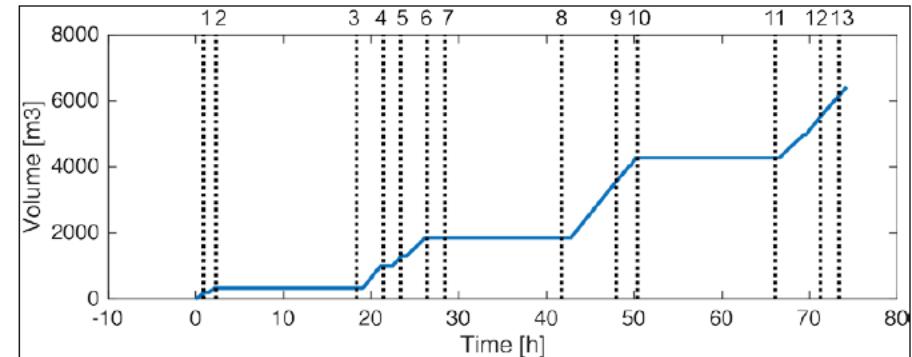
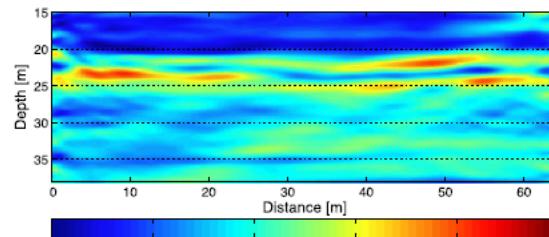
Baseline (00h.1kHz) : damping / muting / low-pass (1500Hz) / amplitude correction (manual)



Same level section: Baseline (00h.1kHz)



4D FWI (real data)



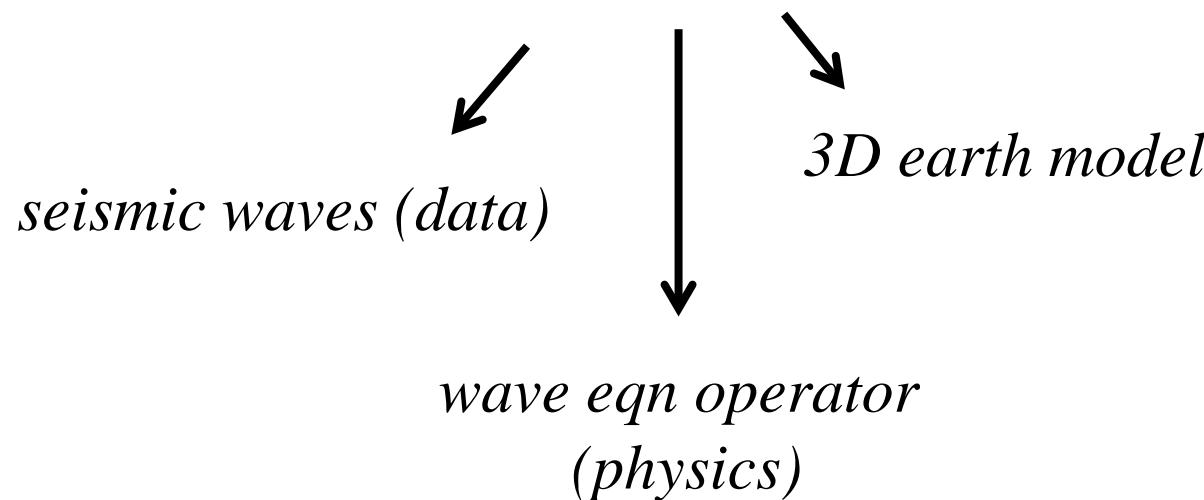
Full waveform inversion

- **Practical issues:**

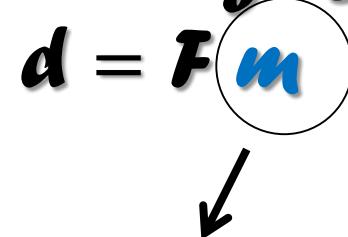
- *Very promising, but still a lot of R&D work to do... (us!)*
- *Works well on 2D synthetics; 3D and real data much harder*
- *Very computationally intensive (HPC)*
- *Many approximations being made (acoustic, time-damping...)*
- *Convergence and uniqueness issues*
- *FWI result not guaranteed to give best image...*

Why do we need HPC?

Forward modeling/simulating waves

$$\mathbf{d} = \mathcal{F} \mathbf{m}$$


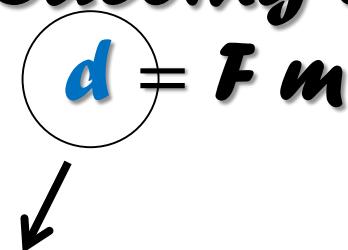
Forward modeling (simulation)

$$\mathbf{d} = \mathcal{F}(\mathbf{m})$$


A diagram illustrating forward modeling. A blue circle contains the letter 'm'. To its right is a black circle containing the letter 'd'. An arrow points from the blue circle to the black circle, indicating that the function F maps the model parameters m to the data d.

*3D earth model($x:y:z:p$) =
 $model(10^{3-4}:10^{3-4}:10^{3-4}:10^{0-1}) = 10^{10-14}$ bytes
Memory= 10 GB - 100 TB*

Forward modeling (simulation)

$$\textcolor{blue}{d} = \mathbf{F} \mathbf{m}$$


*3D seismic data(s:r:t:c) =
data(10⁴⁻⁶:10⁴:10⁴:10⁰⁻¹) = 10¹³⁻¹⁶ bytes
Storage= 10 TB - 10 PB*

Forward modeling (simulation)

$$d = \mathcal{F} m$$



Wave operator($fc:x:y:z:t:c$) =
 $weq(10^{1-2}:10^{3-4}:10^{3-4}:10^{3-4}:10^{4-5}:10^{0-1}) = 10^{14-20} flops$
computation = 100 Tflops - 100 Exaflops

3D Imaging (RTM)

$$R = \mathcal{F}^* d$$



*forall sources=1:10⁴⁻⁶ {
 fwd model the source wavefield;
 reverse-time propagate the receiver wavefield*;
 cross-correlate both wavefields;
 add contribution to update the image }*

Cost $\sim 10^{4-6} \times$ modeling = 10^{18-26} flops = 10⁰⁻⁸ Exaflops!

So we have to be clever about:

- * approximating/accelerating wave operators (Clusters, GPUs...)
- * pre-compute/store/load wavefields etc. (memory, storage, i/o)

Full waveform inversion

$$\mathbf{m} = \mathcal{F}^{-1} \mathbf{d}$$

$$\min \mathbf{E^2} = w_d^2 (\mathbf{d} - \mathbf{Fm})^2 + w_m^2 (\mathbf{m} - \mathbf{m}_o)^2 + \dots$$

forall iterations=1:10¹⁻³ {

- apply the adjoint imaging operation $\mathbf{F}^* \mathbf{d}$;
- estimate/update the earth model \mathbf{m} ;
- forward model the simulated wavefield \mathbf{Fm} ;
- compare to the recorded data \mathbf{d} ;
- check convergence criteria $\mathbf{E^2}$ }

Cost $\sim 10^{1-3} \times$ imaging $= 10^{19-29}$ flops $= 10^{1-11}$ Exaflops!

So we have to be extremely clever (ie. we don't know how to do this yet!):

- * approximating/accelerating wave operators (Clusters, GPUs...)
- * pre-compute/store/load wavefields etc. (memory, storage, i/o)

Seismic HPC Conclusions

- **Seismic modelling, imaging, and inversion maxes out on ALL key computational aspects:**
- Memory: *10 GB - 100 TB*
- Storage: *10 TB - 10 PB*
- FLOPs: *100 Tflops - 10¹¹ Exaflops*
- I/O: *network bandwidth limits (eg. 120 Gb/s Infiniband)*

>> We need HPC!



Thank you



Thank you