



Adaptive Computing and multi-fidelity learning

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Scale-up of complex systems and associated risks

Scale-up: Extending systems and processes that were developed in the laboratory to function in the real world

Device and process scale-up comes with significant technical challenges and risk

Typical challenges:

- Data-driven models perform best when interpolating, **extrapolation is inherently uncertain**, and therefore **risky**
- Increasing ranges of scale (spatial, temporal) often lead to new/enriched physics
- High-fidelity physics-based models may capture new physics, but are typically too expensive for design/optimization work
- Operational regimes of existing experiments are limited, and new experiments are expensive

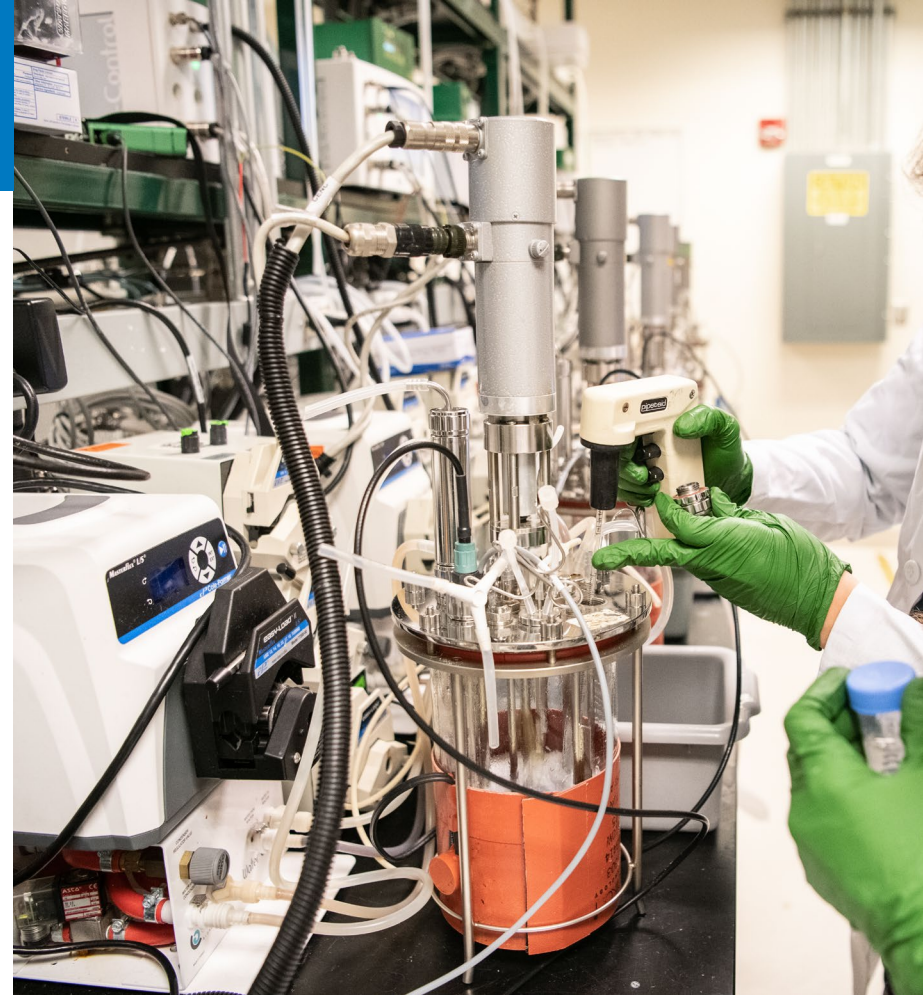
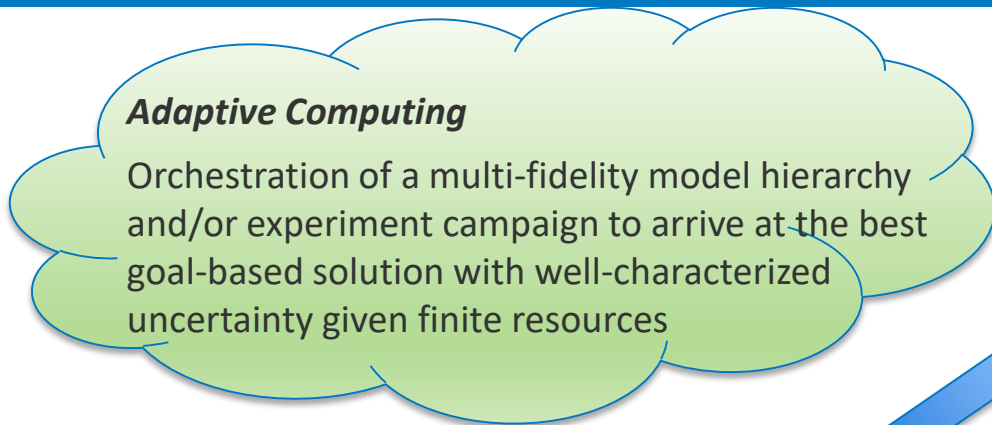


Image Credit: Dennis Schroeder, NREL63958

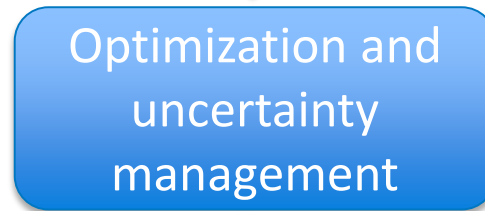
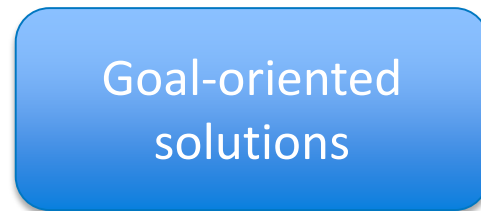
Goal: reduce scale-up challenges by integrating multi-fidelity modeling and optimal compute resource use



Connect models with experiments to drive experiment design and data acquisition needs



Optimize the use of finite resources to achieve a specific science goal



Control of extrapolation uncertainty through targeted active learning

Key capability: multi-fidelity modeling

Most applications feature an assortment of models of widely varying fidelities, developed for different purposes:

- Experiment: “Truth”, but limited operational regime
- High-fidelity simulations: Physics-based (PDE/ODE), costly
- Lower fidelity levels: reduced physics, coarser meshes, less costly
- Data-driven surrogates: AI/ML, PINNs, Gaussian Processes (GPs), really cheap

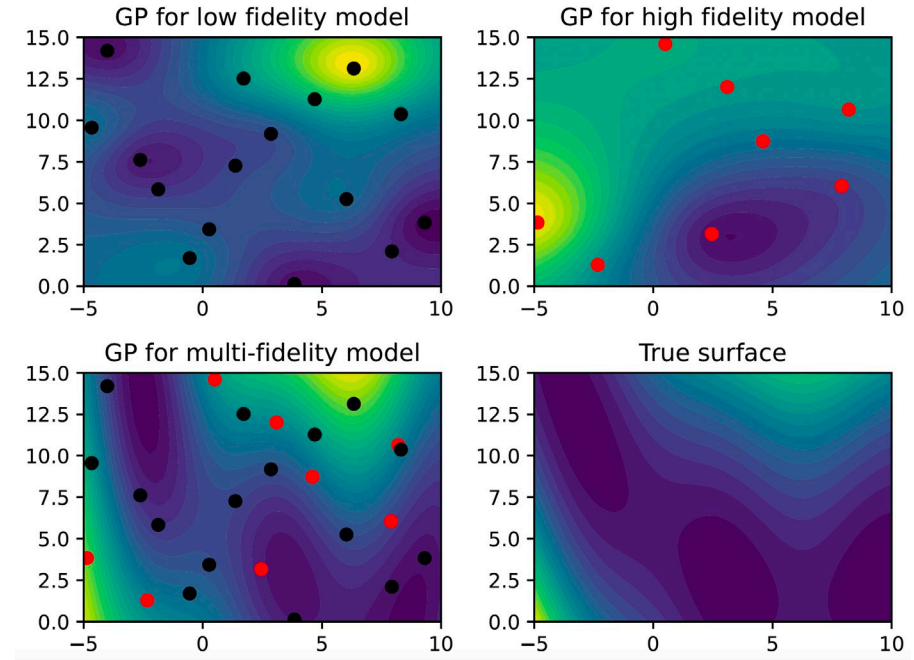


Fig: Exploiting information from multiple fidelity levels can increase surrogate accuracy

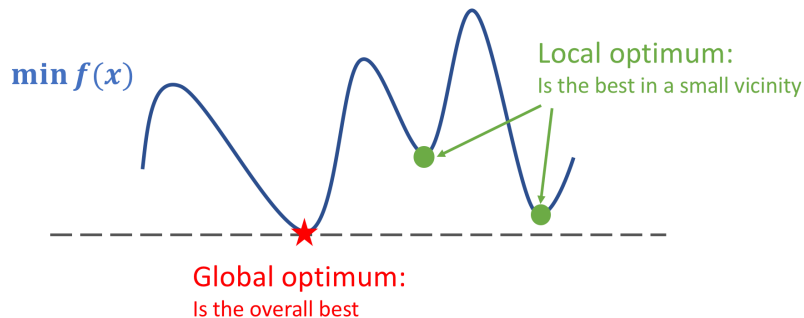
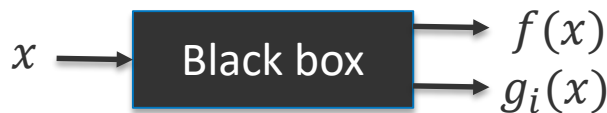
Black-box expensive optimization: high fidelity

$$\begin{aligned} & \min f(x) \\ \text{s. t. } & g_i(x) \leq 0, i = 1, \dots, I \\ & x \in \Omega \end{aligned}$$

Objective function to minimize

Constraint functions

Parameter domain



$$\frac{df}{dx}$$



Surrogate models approximate the expensive function

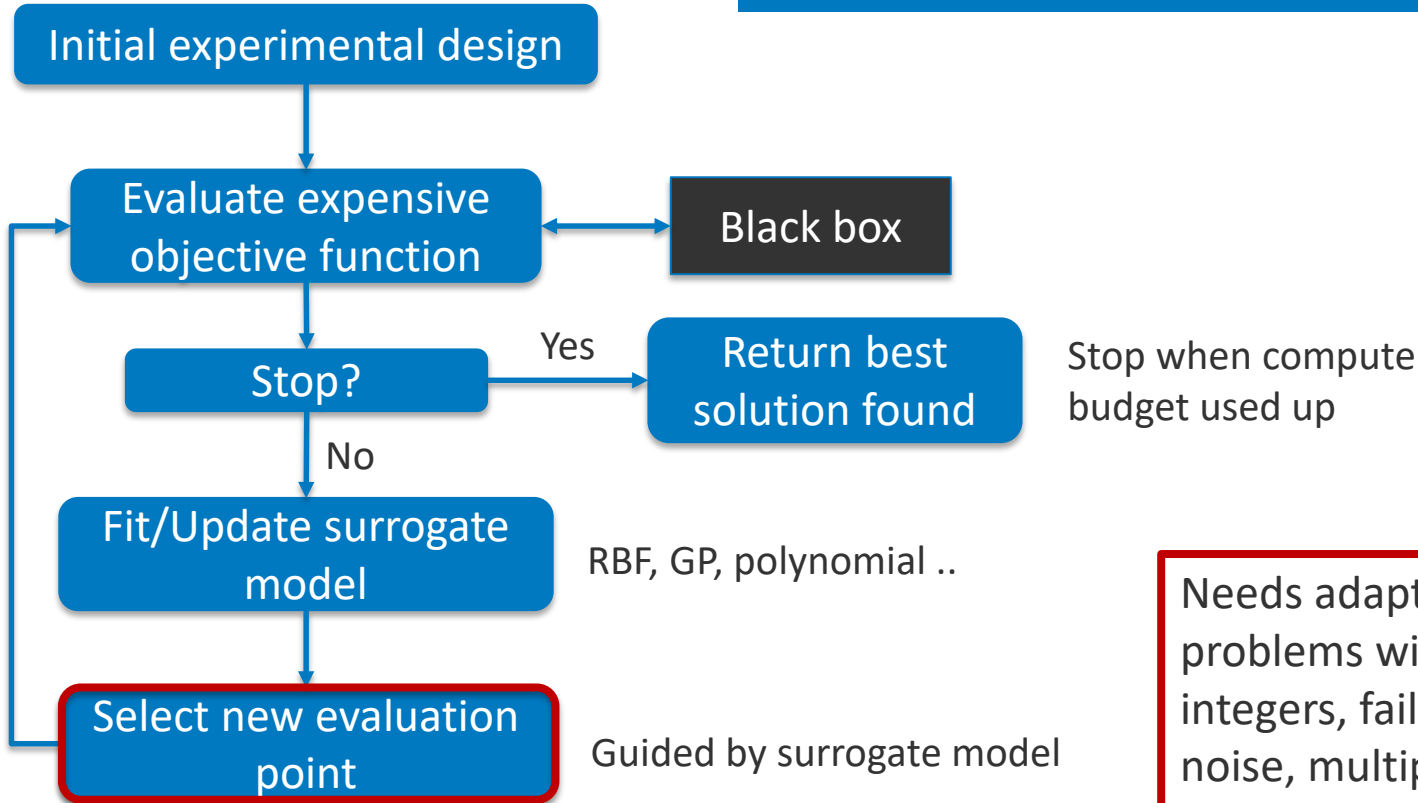
$$f(x) = m_f(x) + e_f(x) \quad \text{Surrogate of the objective function}$$
$$g_i(x) = m_{g_i}(x) + e_{g_i}(x) \quad \text{Surrogate of the constraint function}$$

Different types of surrogate models exist:

- Radial basis functions
- Gaussian Process models
- Multivariate adaptive regression splines
 - Polynomials
 -

Throughout the optimization, we let the surrogate model guide the search for improved solutions

Surrogate model based optimization loop



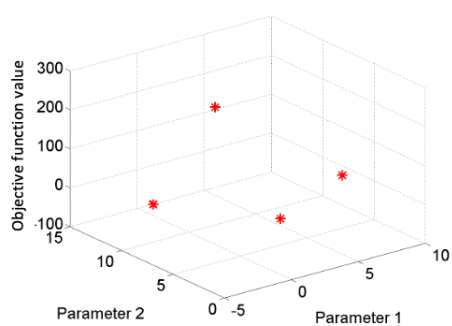
Stop when compute budget used up

RBF, GP, polynomial ..

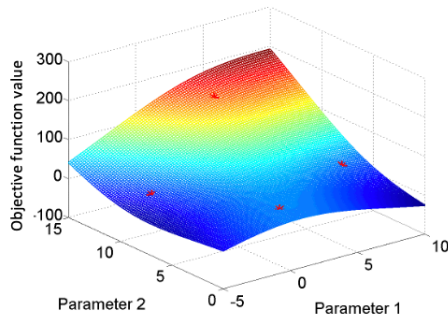
Guided by surrogate model

Needs adaptation for problems with constraints, integers, failed evaluations, noise, multiple conflicting objective functions

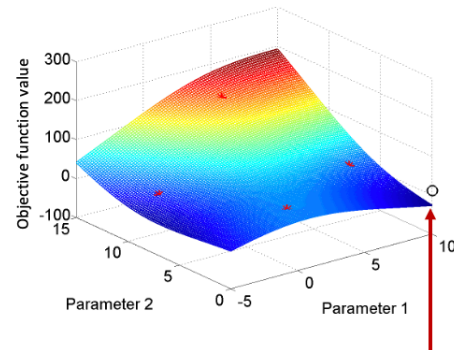
Surrogate model guided sampling



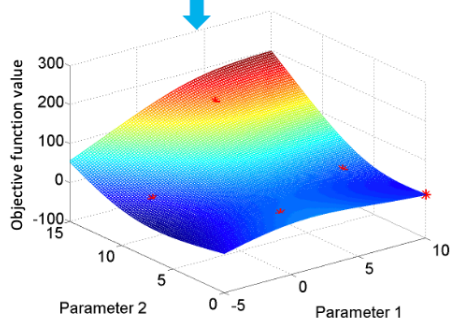
Initial experimental design



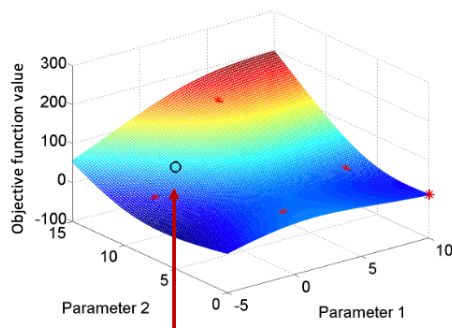
Compute surrogate surface



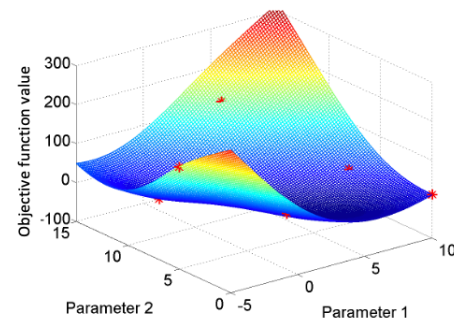
Select and evaluate new point



Update surrogate surface



Select and evaluate new point



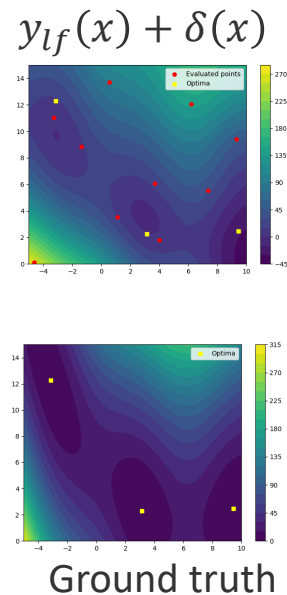
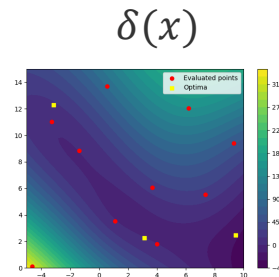
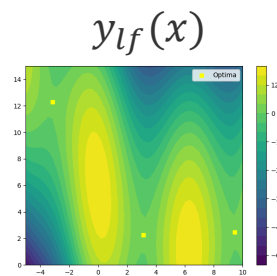
Update surrogate surface

...

Exploiting multiple fidelity levels

Correcting the low-fidelity model:

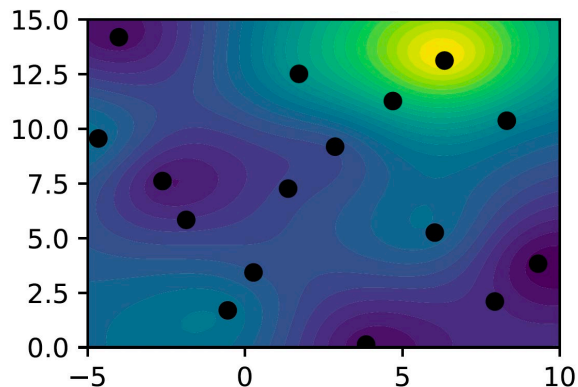
- Multiplicative: $\hat{y}_{hf}(x) = \rho(x) * y_{lf}(x)$
- Additive: $\hat{y}_{hf}(x) = y_{lf}(x) + \delta(x)$
- Hybrid:
 - $\hat{y}_{hf}(x) = \rho(x) * y_{lf}(x) + \delta(x)$ (ρ const.)
 - $\hat{y}_{hf}(x) = w(x) * \rho(x) * y_{lf}(x) + (1 - w(x)) * (y_{lf}(x) + \delta(x))$, $w \in [0,1]$



How do we make use of multiple fidelity levels during active learning?

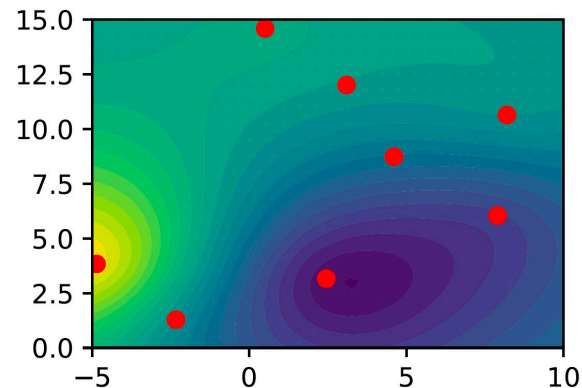
Exploiting multi-fidelity information

Build a surrogate model for the low(er) fidelity function



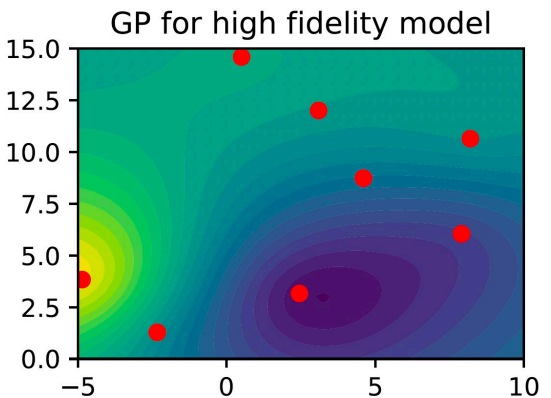
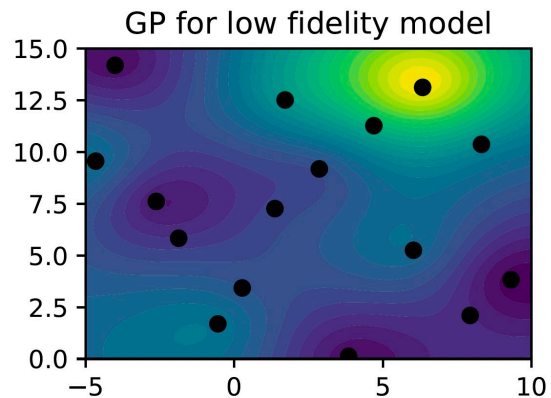
- Allow more samples than for high-fidelity function
- Use this surrogate to decide where to focus the search in the high-fidelity function
- *Low fidelity model does not have to be accurate*

Build a surrogate model for the high-fidelity function

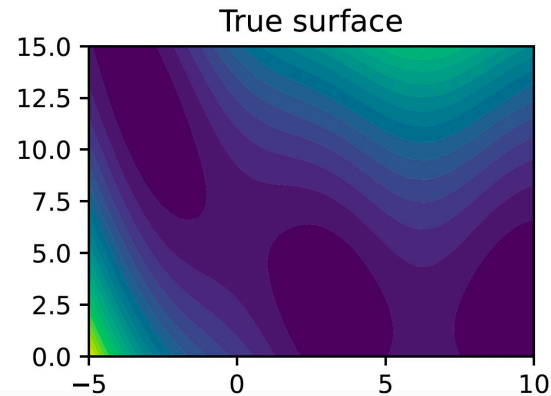
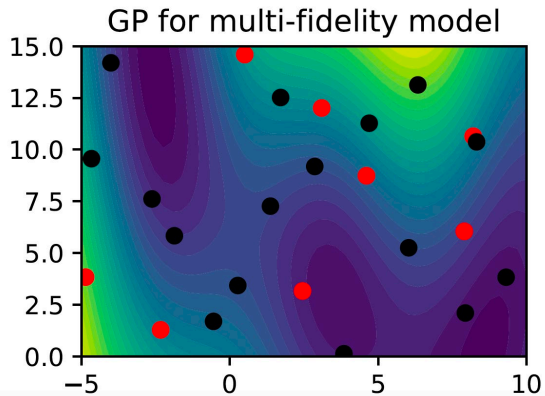


- Fewer samples are affordable
- Surrogate is less accurate (built on less data)
- Surrogate can be used to make (final) sample decisions

Gaussian Process: Using multiple fidelity information in one model



Red = high-fidelity evaluations
Black = Lower fidelity evaluations



Python package surrogate modeling toolbox (SMT)

Combining high and lower fidelity information can lead to better approximation surface (compare to true contours)

GP-based sampling methods

Expected improvement balances local and global search

$$\mathbb{E}(I)(\mathbf{x}) = s(\mathbf{x}) (\nu\Phi(\nu) + \phi(\nu)), \quad \nu = \frac{f^{\text{best}} - m_{\text{GP}}(\mathbf{x})}{s(\mathbf{x})}$$

Probability of improvement – mostly local search

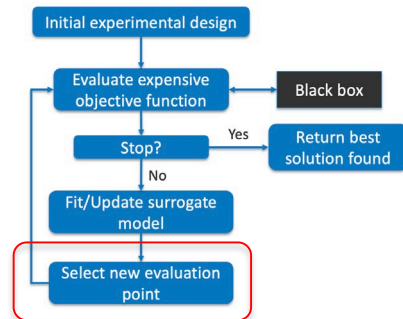
$$\mathbb{P}(I)(\mathbf{x}) = \Phi\left(\frac{f^{\text{best}} - m_{\text{GP}}(\mathbf{x})}{s(\mathbf{x})}\right)$$

m_{GP} is the GP prediction

s is the standard deviation of the GP predictions

f^{best} is the best function value found so far

ϕ, Φ are the normal density and cumulative distribution



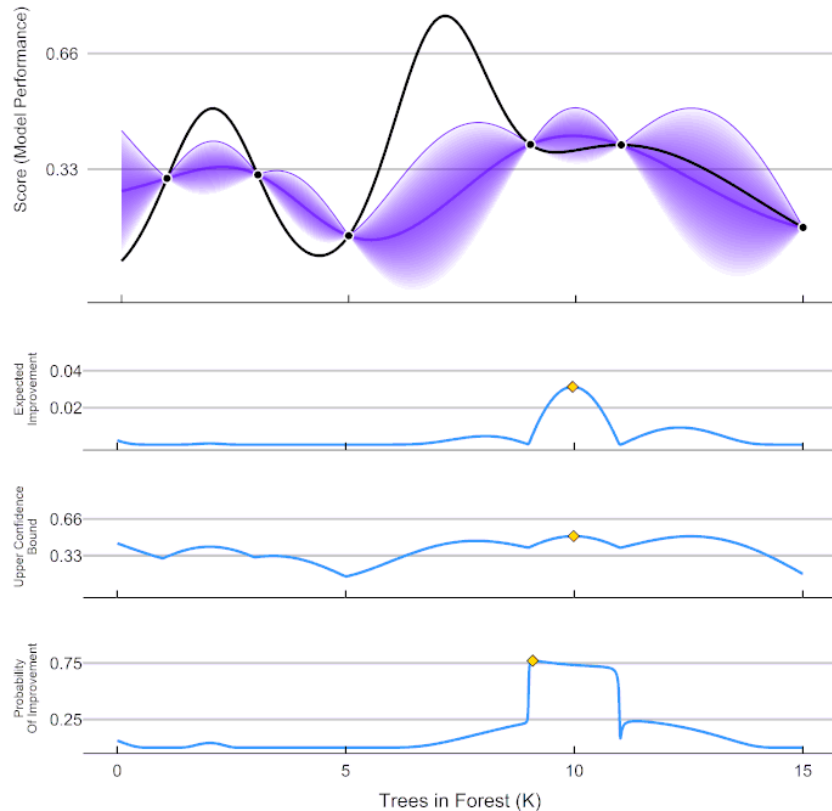
Lower confidence bound

$$LCB(\mathbf{x}) = m_{\text{GP}}(\mathbf{x}) - \kappa s(\mathbf{x})$$

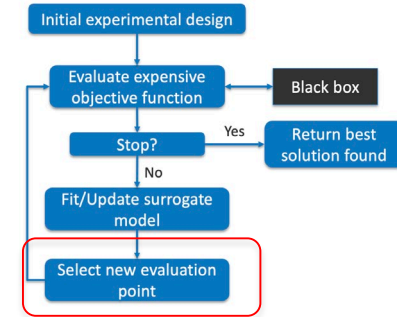
κ – adjustable parameter

GP based sampling in 1d

ParBayesianOptimization in Action (Round 1)



Maximization
problem



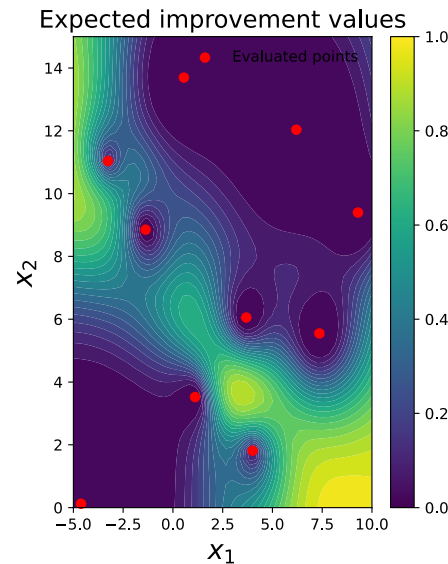
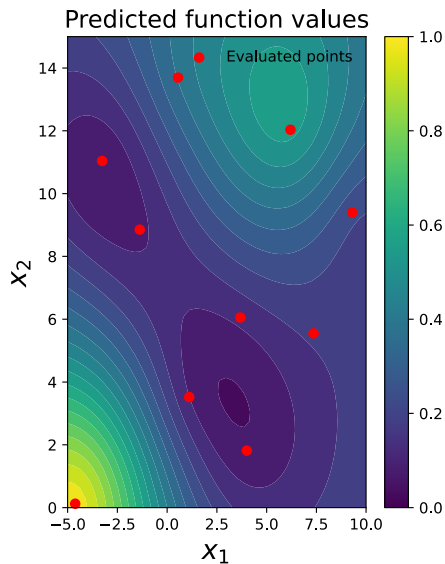
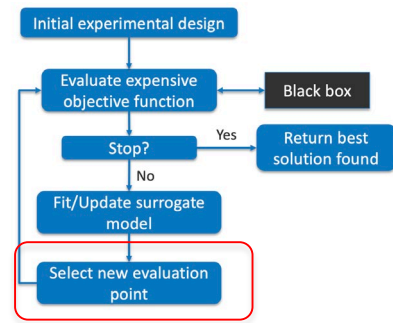
Expected improvement

Upper confidence bound

Probability of improvement

Maximize the expected improvement to select a new point

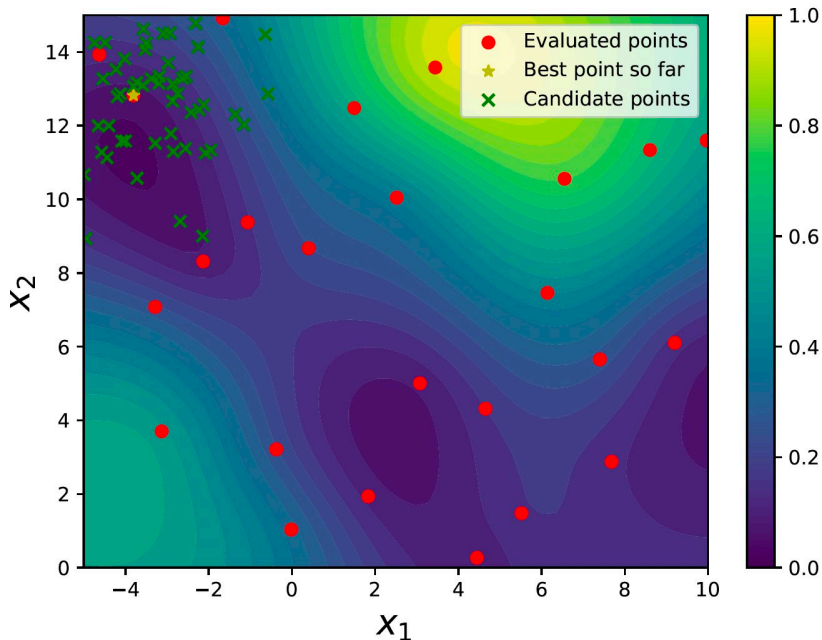
Expected improvement surface is multimodal and can become flat – making it difficult to find the global maximum...



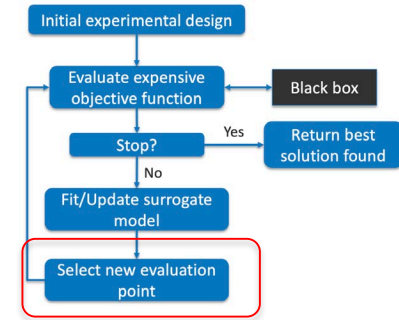
...requires development of other sampling strategies, guided by low-fidelity model

Sampling with candidate points

Add random perturbations to (select) variables of the best point(s) found so far



- Maximize a merit function that trades off predicted function value and distance to already evaluated points
 - Low function value \rightarrow local search
 - Large distance \rightarrow global search
- Select N new points for potential evaluation

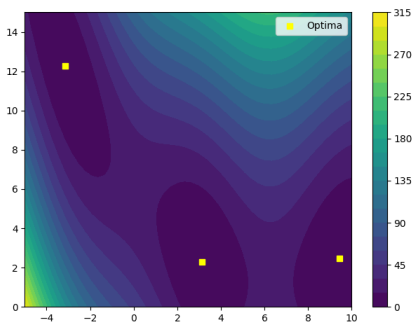


Multi-fidelity sampling: when to ignore the low-fidelity model

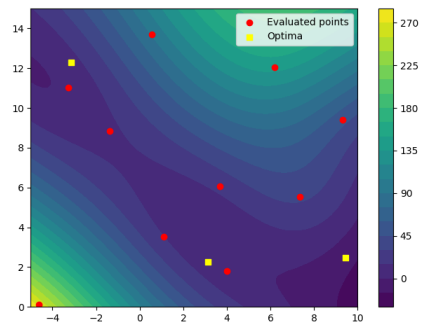
- Make use of as much information as is available
 - Surrogate of high-fidelity model
 - Low-fidelity (cheap) information – what if this one is very inaccurate/uncorrelated?
 - Surrogate of the difference as a selection constraint

1. Define auxiliary function $a(x)$ using the surrogate model predictions
2. Optimize $a(x)$ to find x_{new}
3. If $-\delta \leq d(x_{new}) \leq \delta$ probe with low fidelity model first, otherwise ignore and evaluate high-fidelity model

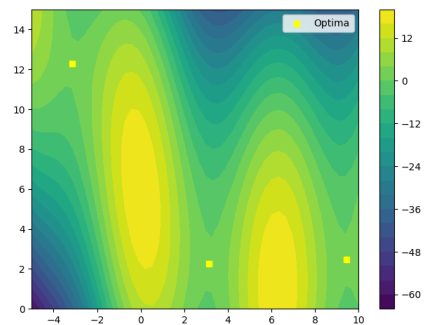
High-fidelity ground truth



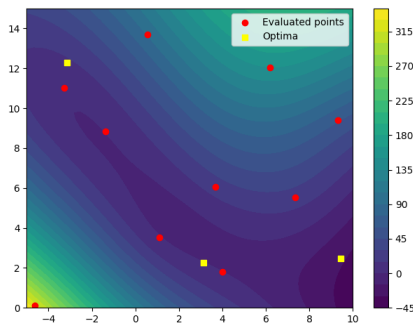
SM of high-fidelity model



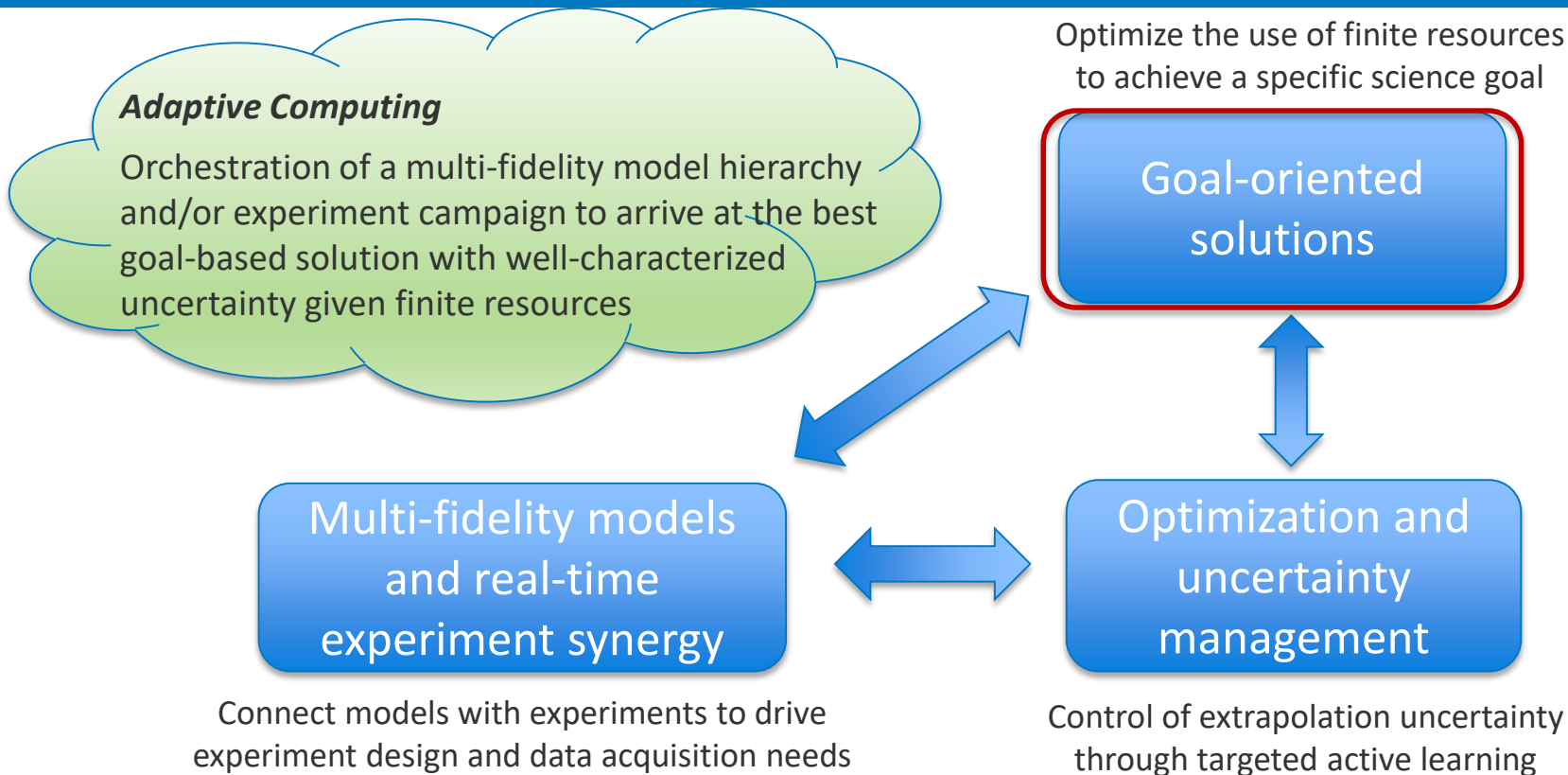
Low-fidelity model



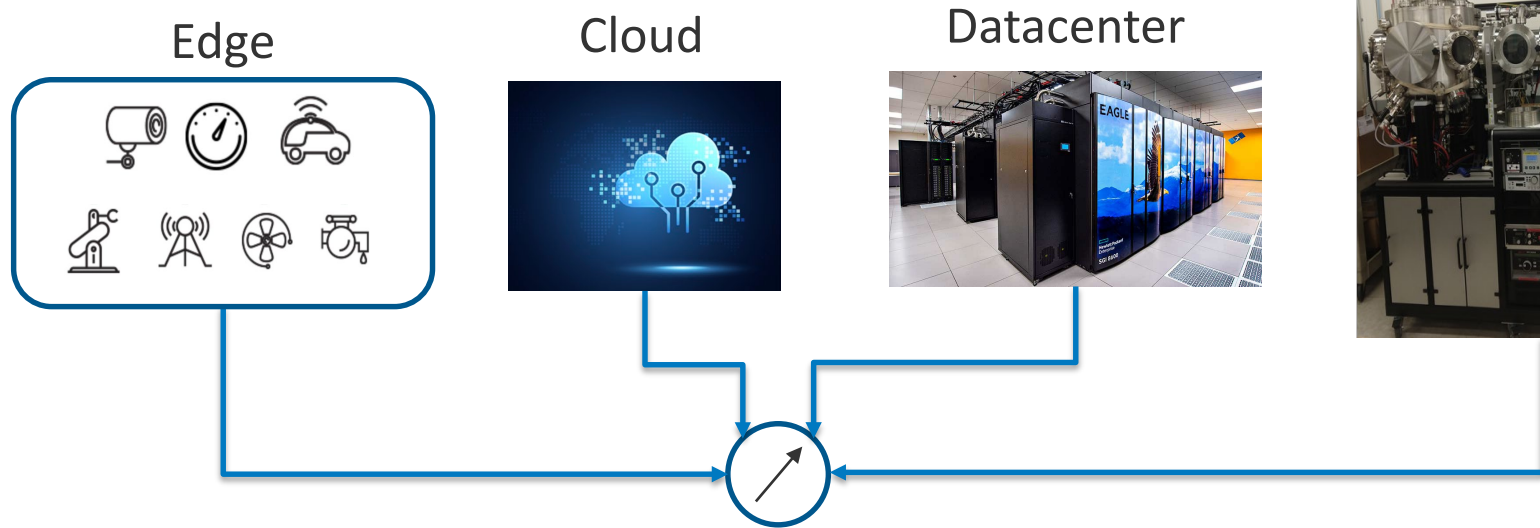
Difference between high-
and low-fidelity



Goal: reduce scale-up challenges by integrating multi-fidelity modeling and optimal compute resource use



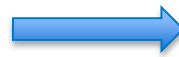
Key capability: diverse compute resources



Experiment



Resource manager:
how much and what kind of
resources do I have available?

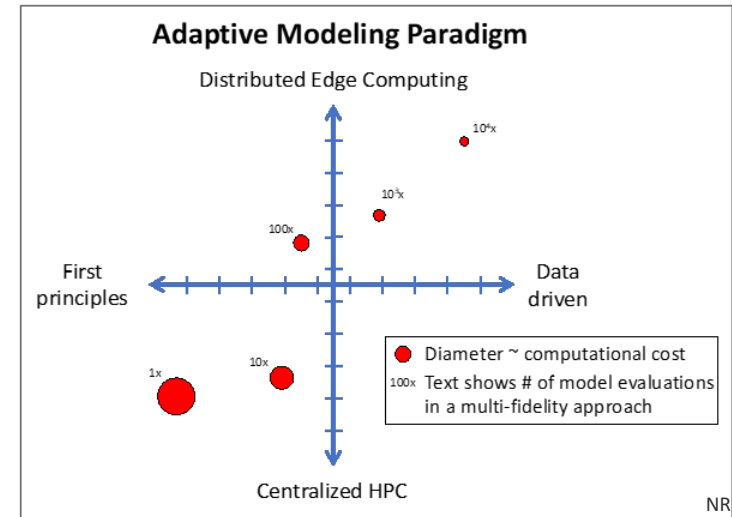
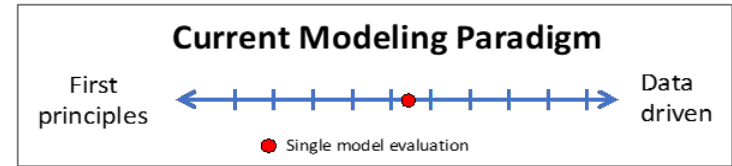


Solve stochastic discrete
optimization problem

Optimal computing strategy driven by specific output quantity of interest

Compute resource optimization problem

- What resources are available when?
- Formulate as optimization problems with stochasticity
- Implement solutions as constraints for multi-fidelity sampling
- Eventually must exploit asynchronous parallel computations
- Enumerate the user-defined simulation types (fidelity levels)
- Possible hardware configurations (# of CPUs, GPUs)
- Corresponding calculation duration
- Measurement noise estimate (aleatoric uncertainty)



Compute resource allocation with stochasticity

1. Select sample points (e.g., maximize EI with multi-start; candidate point approach)

$$\{x_1, x_2, \dots, x_N\} \in \underset{x \in \mathcal{X}}{\operatorname{argmax}} a(x)$$

2. Get total resource limit T and per level resource limit T_j and allocate compute resources

$$\max_{b_{ji} \in \{0,1\}^k} \sum_{j=1}^J r_j(x_i) * b_{ji}$$

r_j the benefit of evaluating x_i at fidelity level j , e.g.,
 r_j captures accuracy or other QoI

$$b_{ji} = \begin{cases} 1 & \text{if } x_i \text{ evaluated with fidelity level } j \\ 0 & \text{else} \end{cases}$$

$J * N$ binaries
to optimize

$$\sum_{j=1}^J \sum_{i=1}^N b_{ji} * t_j(x_i, \zeta_{ji}) \leq T$$

Total resource restriction

t_j resource consumption at level j

$\zeta_{ij} \sim ?$

$$\sum_{i=1}^N b_{ji} * t_j(x_i, \zeta_{ji}) \leq T_j \quad \forall j$$

Resource restriction on fidelity level j

AC framework

Check resource availability

- Data center
- Edge
- Cloud
- Experiment

Resource mana



Application specific code

- Optimization
- Sensitivity analysis

- Fidelity lvl 2
- ...
- Fidelity lvl M

Statistics, analysis, visualization

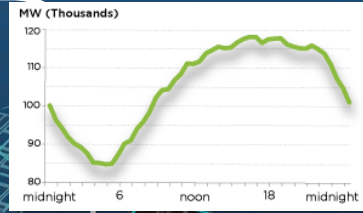
Surrogate models

Sampling methods

ARIES – Advanced Research on Integrated Energy Systems

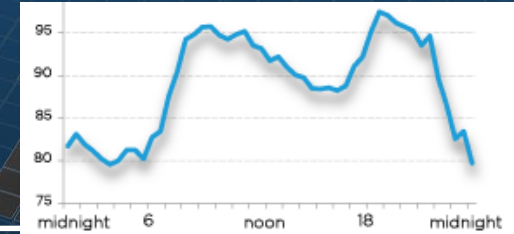


Various RE generation leading to grid needs



AC Challenge: How do we build a transferable framework to assess the available flexibility?

Generation



Data store and Control Center

Demand

Community scale real and emulated buildings, equipment, electric vehicles, etc.

Neighborhood

Real House

Community

Virtual House

How much demand flexibility is available to support the grid

Goal: Understand, evaluate, and predict the demand flexibility a device, building, or a community can provide:

- Optimizing or shaping the energy demand to support grid conditions
- Providing a way to tap into extra demand flexibility in extreme situations



Challenge: Computing the anticipated energy demand and the opportunities to exploit optimal control is computationally expensive

- Data from real-world observations and complex building simulation models to evaluate the available flexibility in the community thru:
 - Control of HVAC, lighting, water heating, etc. individually or in combination
 - Aggregating the demand profile to the distribution network and grid
- Use surrogate models and understand where they are too inaccurate and additional real-world data and/or complex full-scale simulation data must be collected
- Computational cost in deployment settings is substantially more acute than in the lab setting

Sources and characteristics of uncertainty

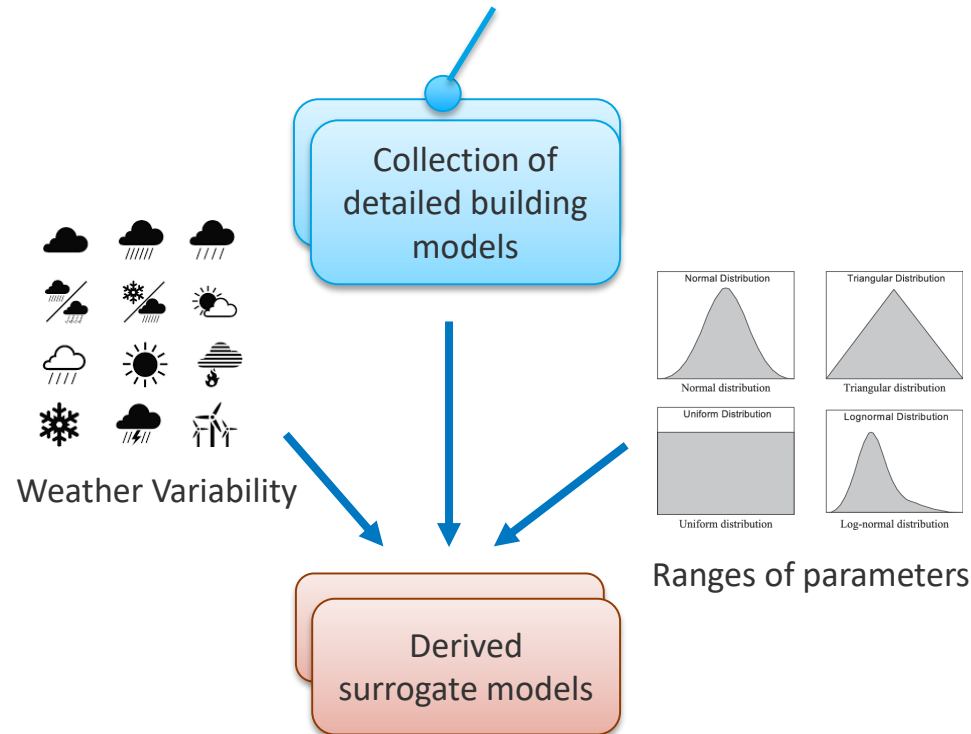


Community/urban/city scale

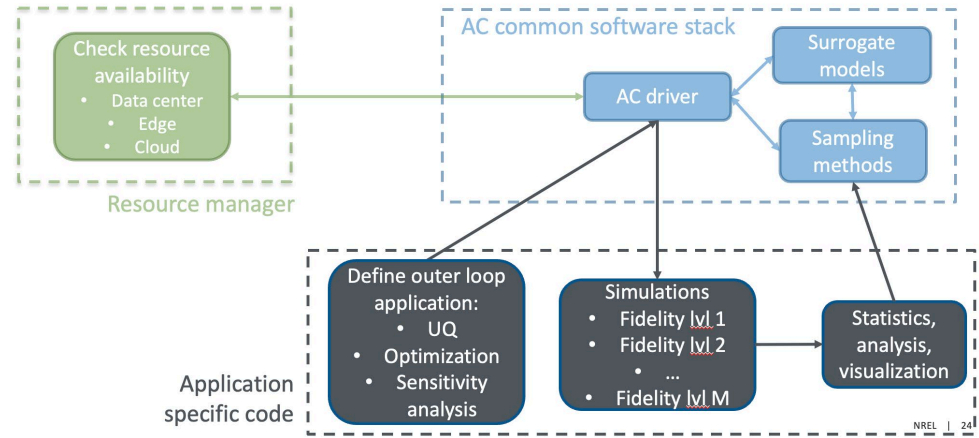
Limitations of surrogate models: surrogate models can only be created for a subset of model parameter distributions, number of dimensions, etc.

- Building energy models have 1000s of parameters with 100s that are important
- Will not represent all possible building types/configurations/equipment classes
- Sampling of only a subset of weather conditions is possible
- Limited transferability across geographic locations

Trust in the surrogate requires uncertainty quantification



ARIES AC framework definitions



Objectives: controls-oriented questions around energy and heating/cooling

- Peak shaving, load shifting, preheating/precooling
- Assess impact of higher efficiency equipment (e.g., LED lighting)
 - Some component changes come in from community questions, renewable energy mandates, prioritize based on carbon footprint
 - ResStock /ComStock libraries for components
- Widespread EV charging

ARIES AC framework definitions

Modeling ecosystem

- *EnergyPlus* is high fidelity model (1-30 minutes per building for a year simulation w/ 1min timestep, heavy on I/O)
- *OCHRE*, struggles in some locations, residential only (E+ does residential and commercial)
- *3R2C* lumped capacitance ROM (4-5 hrs to train) for model predictive control w/ 15min to 1 hour timestep (works for residential and commercial)
- Models are *deterministic and highly nonlinear* (issues with using ROM outside of intended regime)

Parameterizations

- Need to preserve explicit component representation
- Building thermodynamics should be independent of component selection

ARIES AC framework definitions

Challenges

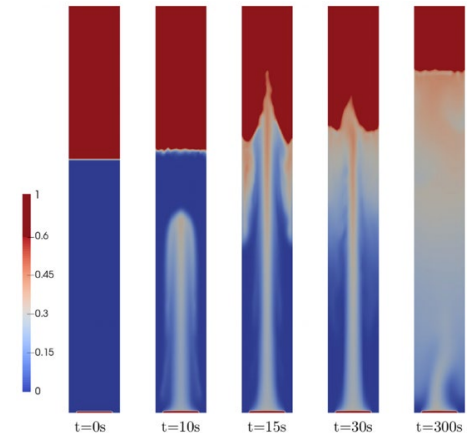
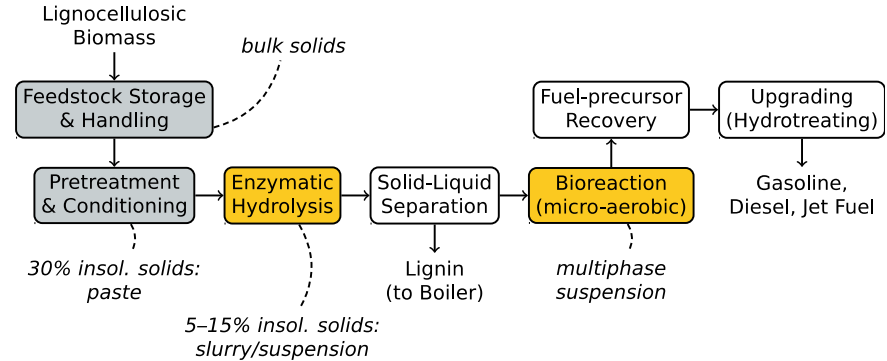
- Scaling simulation and control to larger communities
- Discrete optimization
- ROM accuracy is a function of component choice

Test case going forward

- Pena station with ~150 buildings
 - 50 defined so far
 - Multifamily buildings are challenging, EnergyPlus extra expensive
- EnergyPlus and 3R2C ROM already built
- UrbanOpt usually used to generate model inputs, but have a little more info for Pena station

Example application: virtual engineering of biofuels

- Process lignocellulose-rich biomass into biofuel
- 3 step chemical processes
 - Pretreatment: fast simulation
 - Enzymatic hydrolysis: surrogate or CFD calculation
 - Bioreaction: surrogate or CFD calculation



AC specifics for virtual engineering

- **Objective:** maximum reactor-averaged oxygen uptake rate
- **Inputs:** order 10 chemical and processing design parameters
- **Fidelity Lvl 1:** HF simulation (pretreatment, enzymatic hydrolysis, bioreactor)
 - 32 CPU-cores @ 57 hours
- **Fidelity Lvl 2:** HF pretreatment, LF Lignocellulose model, and HF bioreactor
 - {72 CPU-cores @ 4 hours, or 32 CPU-cores @ 9 hours}
- Could add simulation type that varies the time to steady state/grid resolution

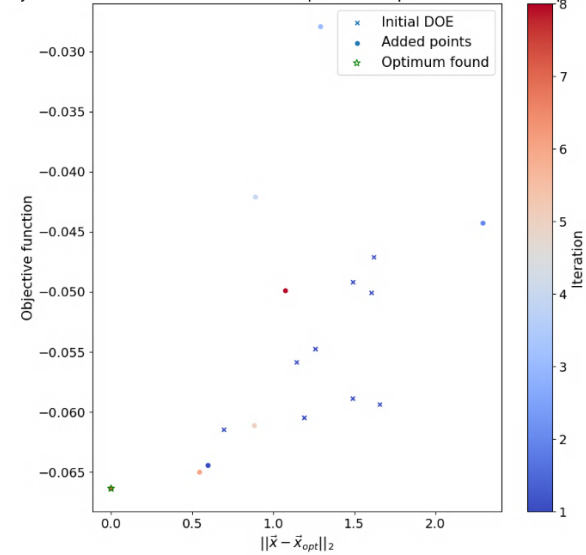
Parameter name	Double or Int*	Default	Min	Max
Fraction of solids that is xylan	Double	0.263	0	1
Fraction of solids that is glucan	Double	0.4	0	1
Porous fraction of the biomass particles	Double	0.8	0	1
Initial concentration of acid	Double	0.0001	0	1
Steam temperature (C)	Double	150	3.8	250.3
Fraction of insoluble solids	Double	0.745	0	1
Enzymatic load	Double	30	0	1000
FIS_0 target	Double	0.05	0	1
Gas velocity (m/s)	Double	0.08	0.01	0.1
Column height (m)	Double	40	10	50
Column diameter (m)	Double	5	1	6
Bubble diameter (m)	Double	0.006	0.003	0.008
OUR_max (mol/m ³ /hr)	Double	88.71	5	100

*Integers require adjustment of the MF methods

Preliminary tests on virtual engineering app

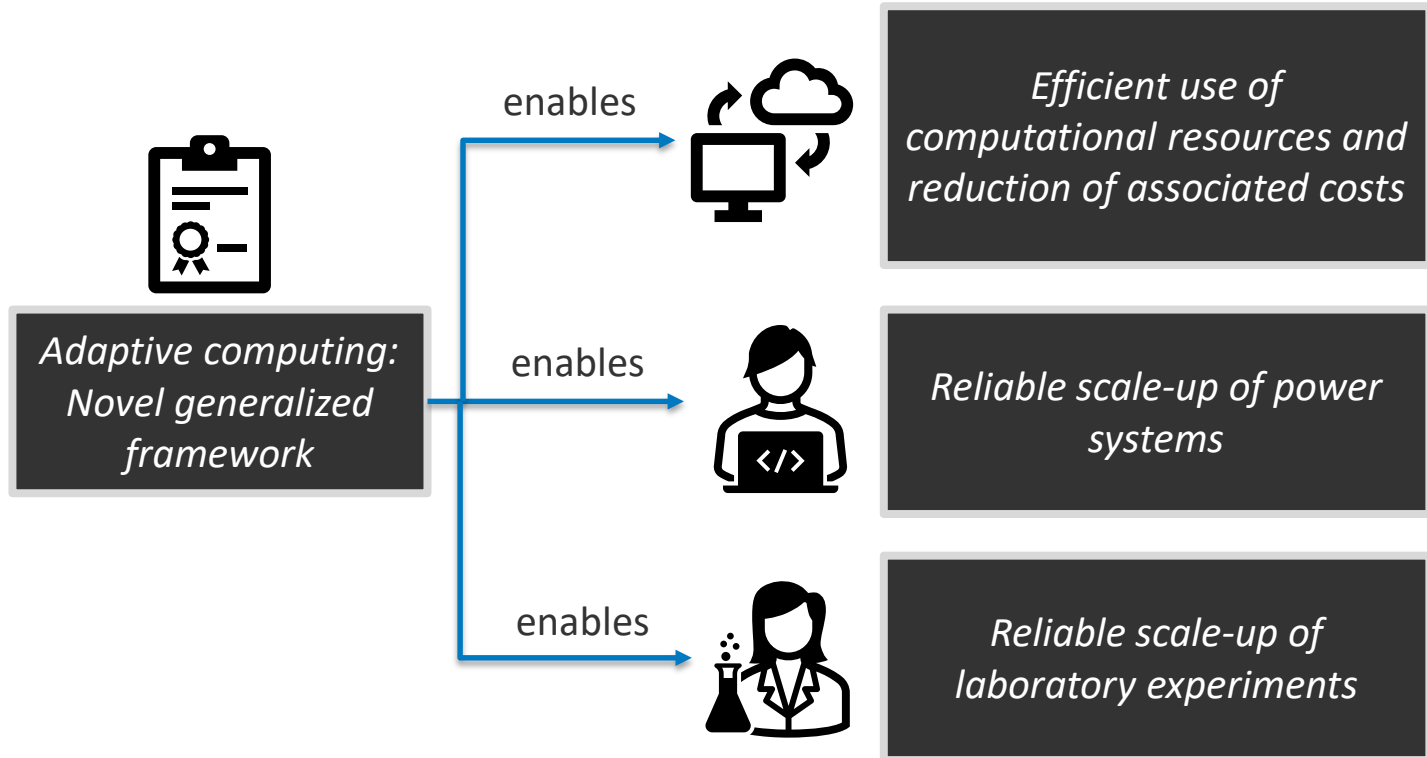
- 8 parameters, 9 random samples from LHS, 10 iterations
- Run for 5 minutes on 1 core, low fidelity models only
- Max Oxygen Uptake Rate = 0.06723323
- For some parameter settings, we obtained NaNs
 - The low fidelity models used may not be valid across the entire parameter space (hidden constraints – we know how to deal with these)

(No multi-fidelity business yet)



Parameter name	VE default	Min	Max	Final
Fraction of solids that is xylan	0.263	0	1	0.32
Fraction of solids that is glucan	0.4	0	1	0.29
Porous fraction of the biomass particles	0.8	0	1	0.64
Initial concentration of acid	1e-4	0	1e-3 (1)	1e-3
Steam temperature (C)	150	3.8	250.3	170
Fraction of insoluble solids	0.745	0	0.99 (1)	0.99
Enzymatic load	30	0	1000	57
FIS_0 target	0.05	0.005 (0)	1	0.005

Adaptive computing: optimizing the use of computational resources to target deficiencies and challenges related to scale-up





Thank You

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