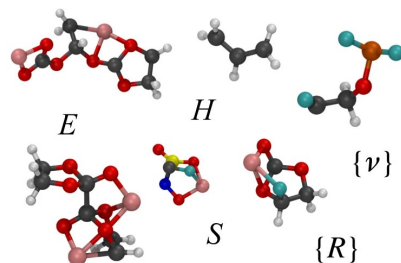
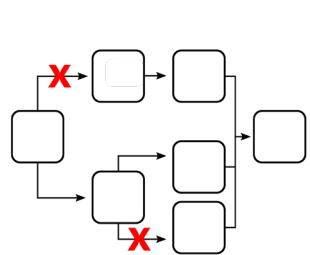
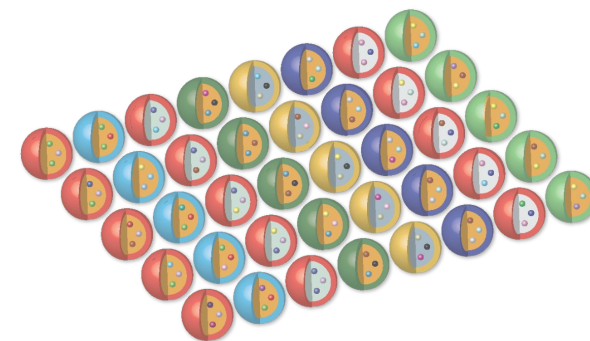


# High-Throughput DFT and Monte Carlo for Reaction Networks and Machine Learning



Samuel M. Blau  
Research Scientist  
Lawrence Berkeley Lab



# High-Throughput Molecular DFT Data Generation

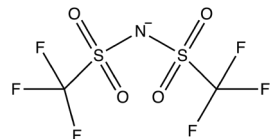
**pymatgen**

**Custodian**

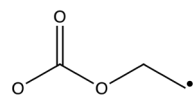
**FireWorks**

**atomate**

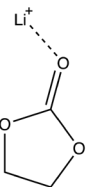
**Q-CHEM**  
A QUANTUM LEAP INTO THE FUTURE OF CHEMISTRY



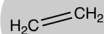
Charged molecules



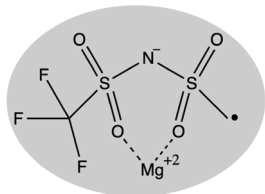
Radical molecules



Metal-coordinated molecules



Solvated molecules



Additional complexity

# High-Throughput Molecular DFT Data Generation

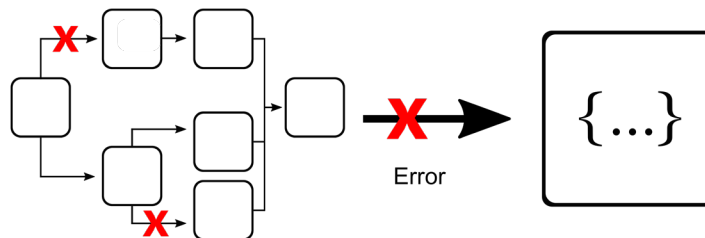
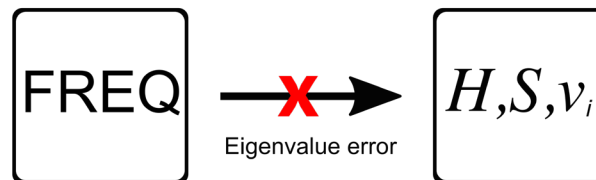
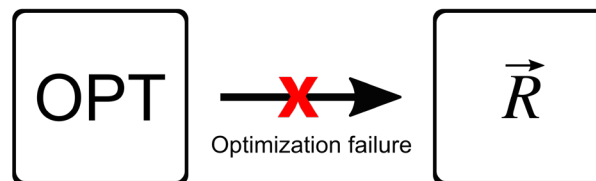
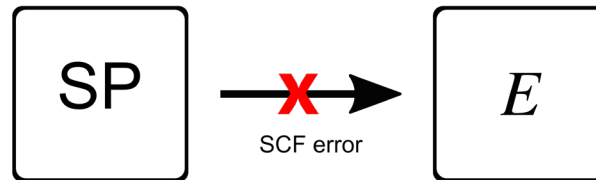
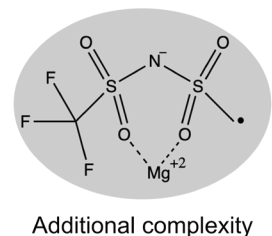
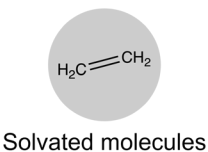
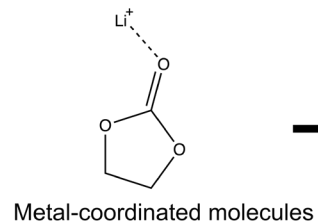
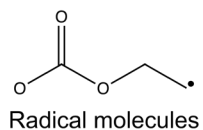
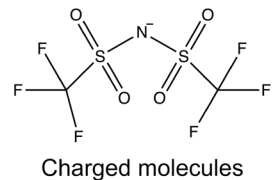
**pymatgen**

**Custodian**

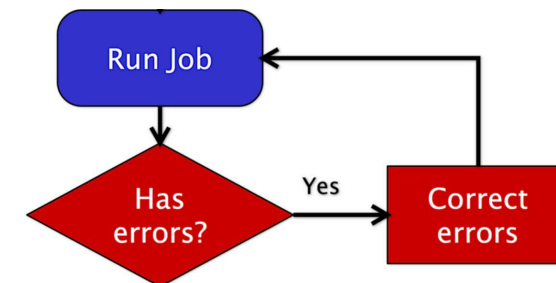
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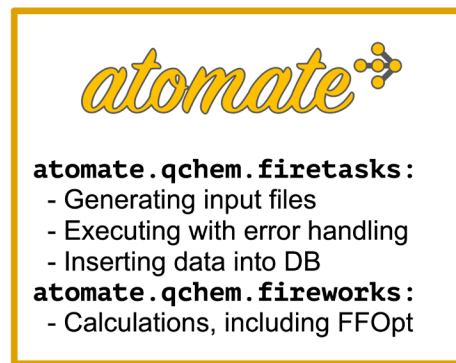
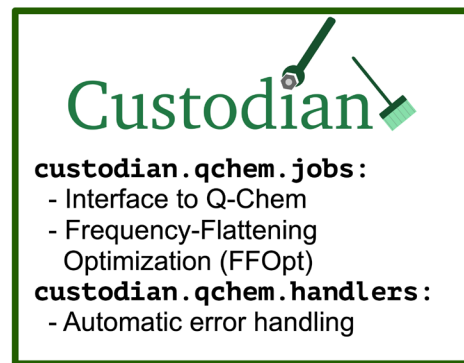
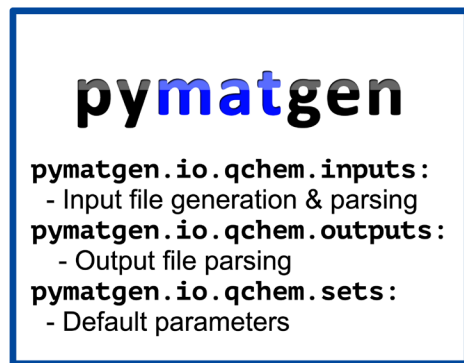
Typically, **<75% success**



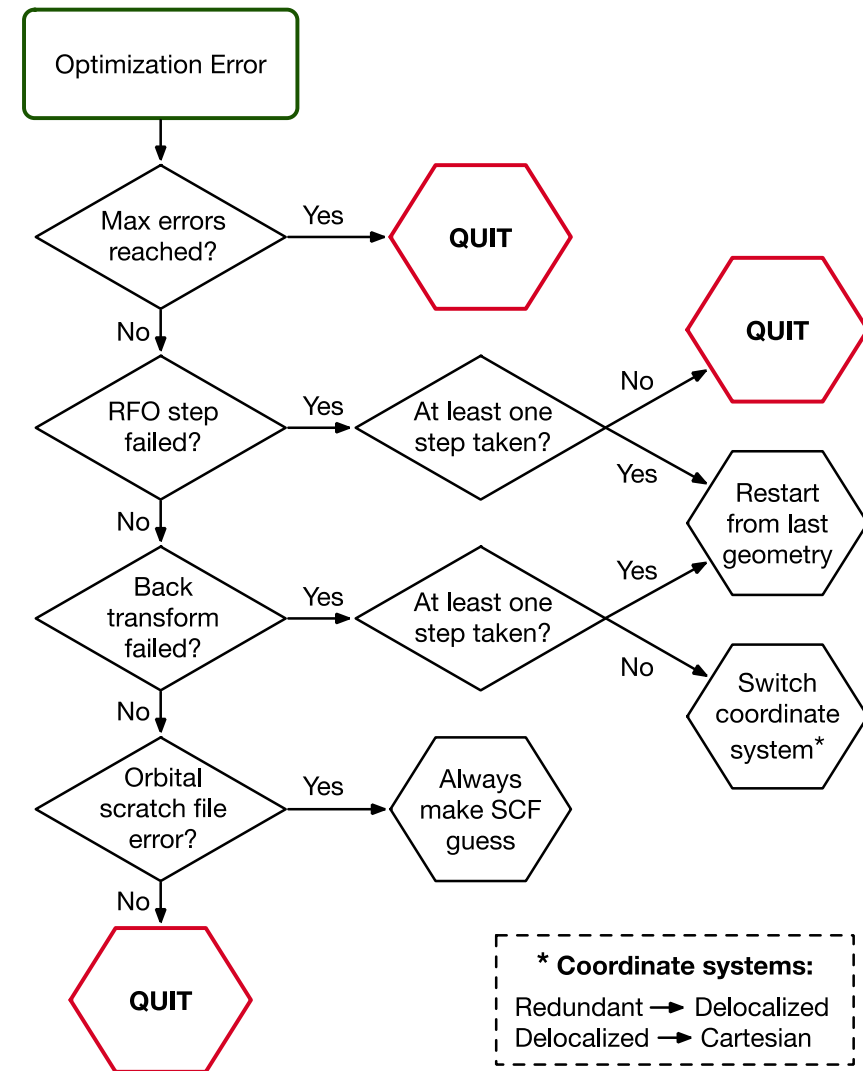
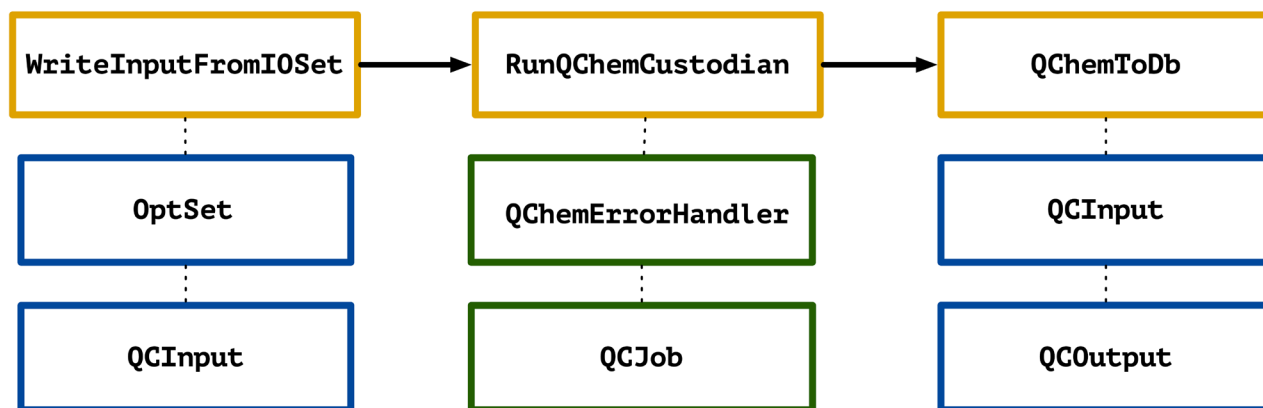
With on-the-fly error correction:

**>98% success**

# High-Throughput Molecular DFT Workflow Infrastructure

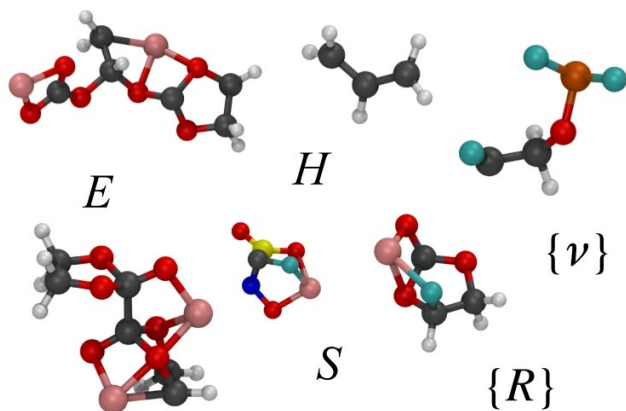


## OptimizeFW:





# We Use Workflows to Generate Unique Simulated Datasets

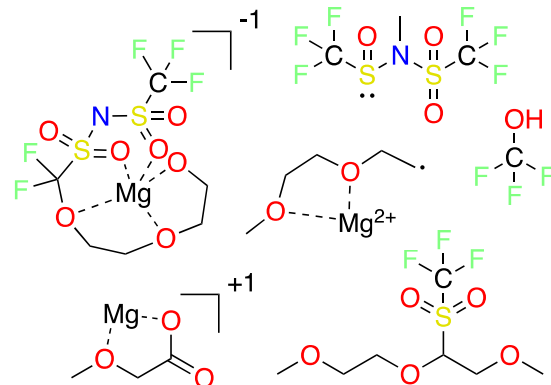


## LIBE

Lithium-Ion Battery Electrolyte  
17,190 molecules

E. W. C. Spotte-Smith\*, S. M. Blau\*, et al., *Sci. Data* 2021

$\omega$ B97X-V/def2-TZVPPD/SMD

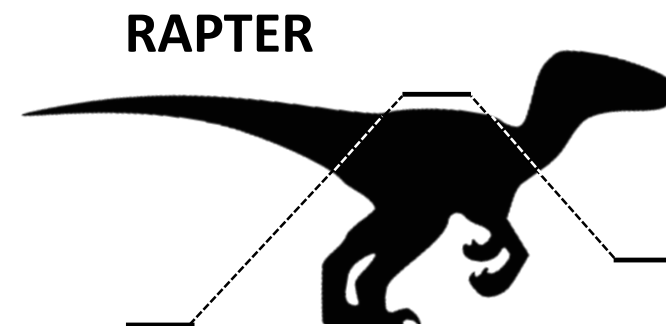


## MADEIRA

MAGnesium Dataset of Electrolyte  
and Interphase ReAgents:  
11,502 molecules

E. W. C. Spotte-Smith, S. M. Blau, et al., *JACS* (accepted)

$\omega$ B97X-V/def2-TZVPPD/SMD

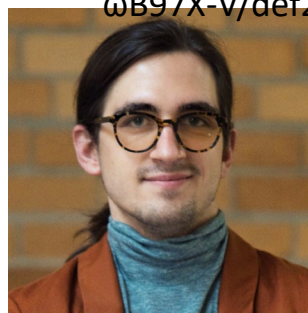


ReActants, Products, and Transition-  
states of Elementary Reactions:  
>15,000 complex reactions

E. W. C. Spotte-Smith, S. M. Blau, et al., *In preparation*

$\omega$ B97X-D/def2-SVPD/PCM

Collaborators:

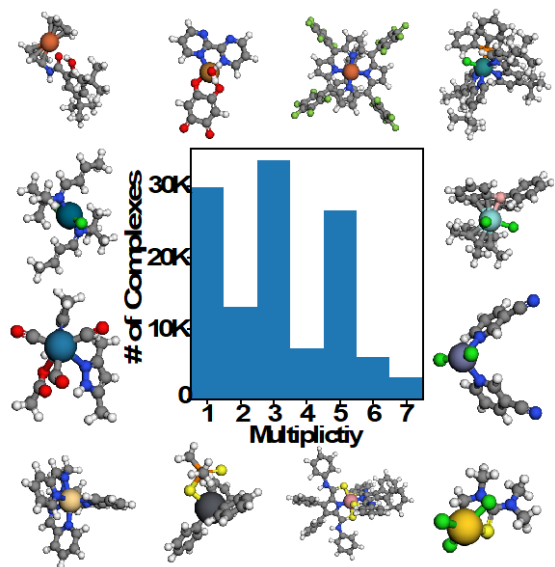


Evan Spotte-Smith



Kristin Persson

# We Use Workflows to Generate Unique Simulated Datasets

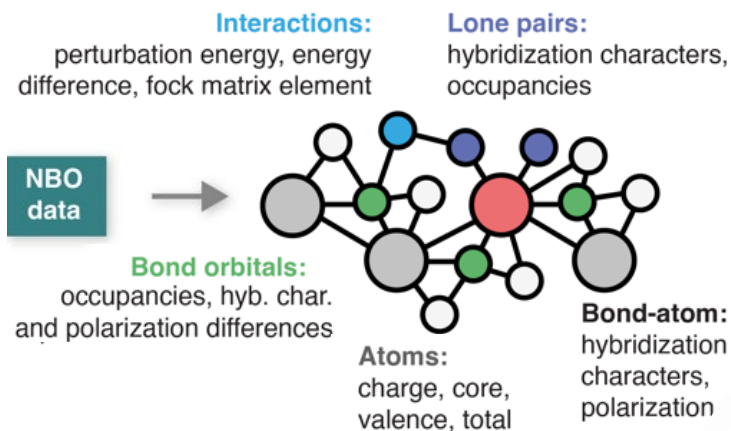


## ESCoMMS

Electronic Structure of **C**omplexes  
with **M**etals of **M**any **S**pins:

>**140,000** complexes

$\omega$ B97M-V/def2-SVPD

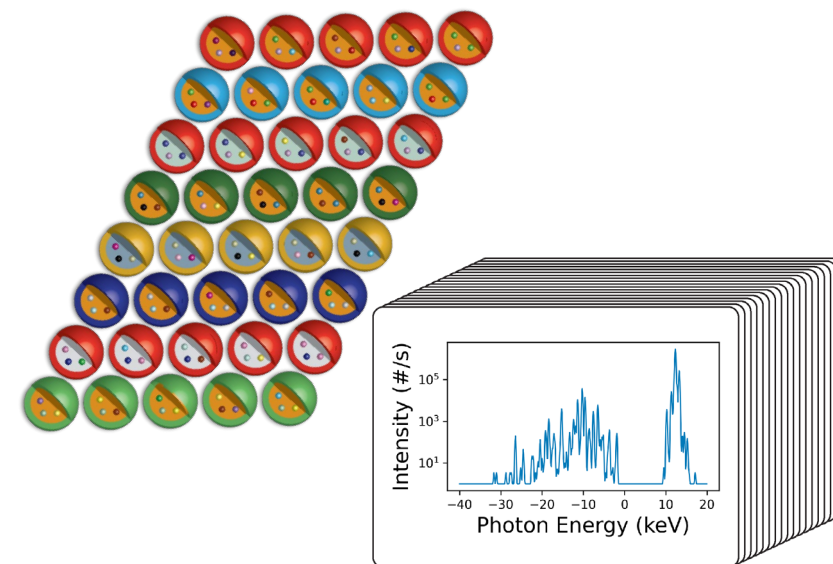


## ORIONS

**OR**bita**L** Interactions of **O**rga**N**ic Species:

>**230,000** molecules

D. Boiko et al., *ChemRxiv* 2022



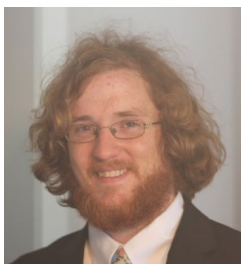
## SUNSET

Simulated **U**pconverting **N**anoparticle

Spectra for **E**missions **T**uning:

>**6,000** spectra (kMC, not DFT)

Michael Taylor



Ping Yang



Gabe Gomes



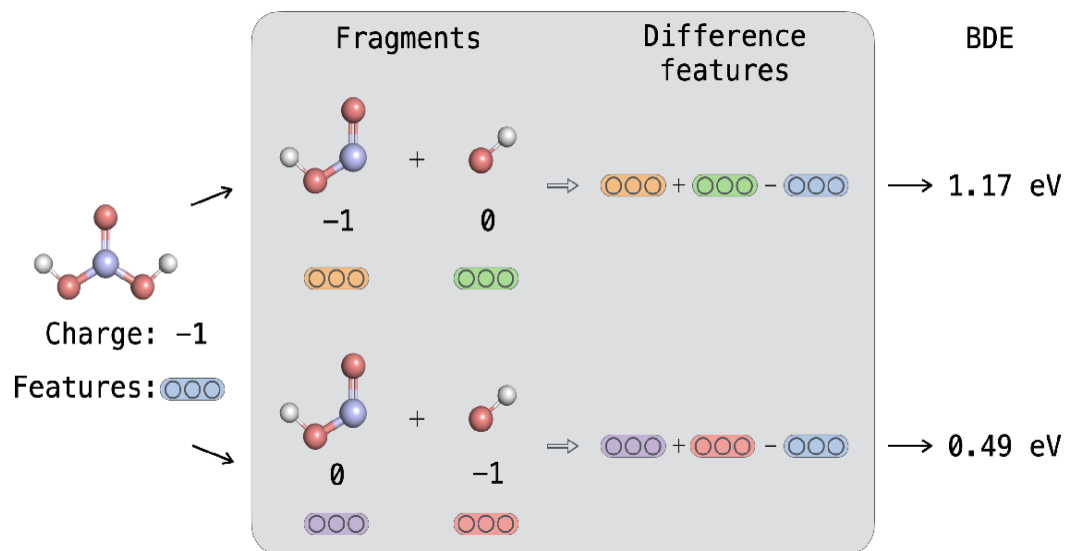
Eric Sivonxay



Emory Chan

# Machine Learning Atop Our DFT Datasets

BonDNet GNN



## An orbital-based representation for accurate quantum machine learning

Cite as: *J. Chem. Phys.* **156**, 114101 (2022); doi: [10.1063/5.0083301](https://doi.org/10.1063/5.0083301)

Submitted: 23 December 2021 • Accepted: 24 February 2022 •

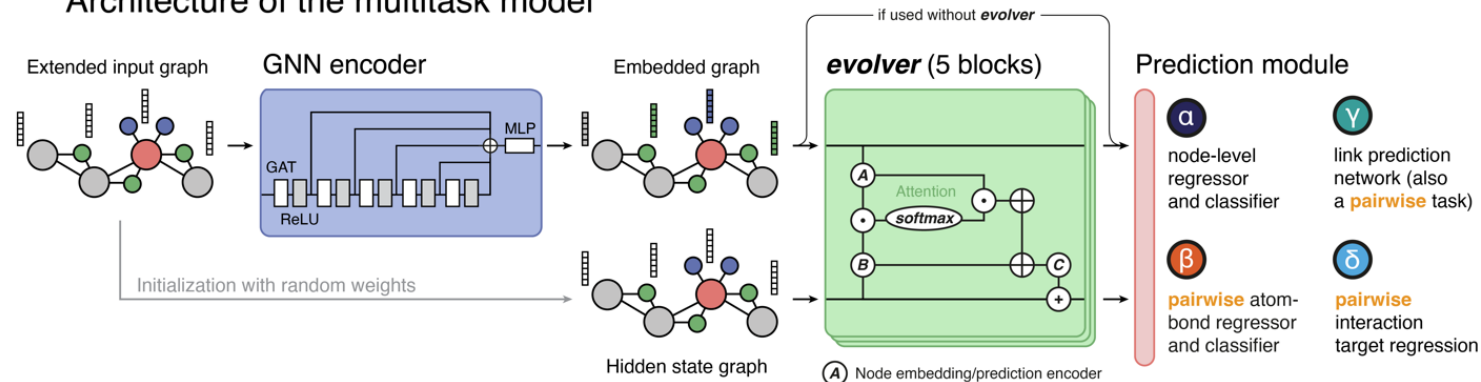
Published Online: 15 March 2022

Konstantin Karandashev<sup>1,a)</sup> and O. Anatole von Lilienfeld<sup>1,2,b)</sup>

“The LIBE dataset is of particular interest... [because] it contains species of different charge and spin states, enabling us to test [our model]’s ability to process them...”

M. Wen, S. M. Blau, E. Spotte-Smith, S. Dwaraknath, K. A. Persson, *Chem. Sci.* 2021

Architecture of the multitask model

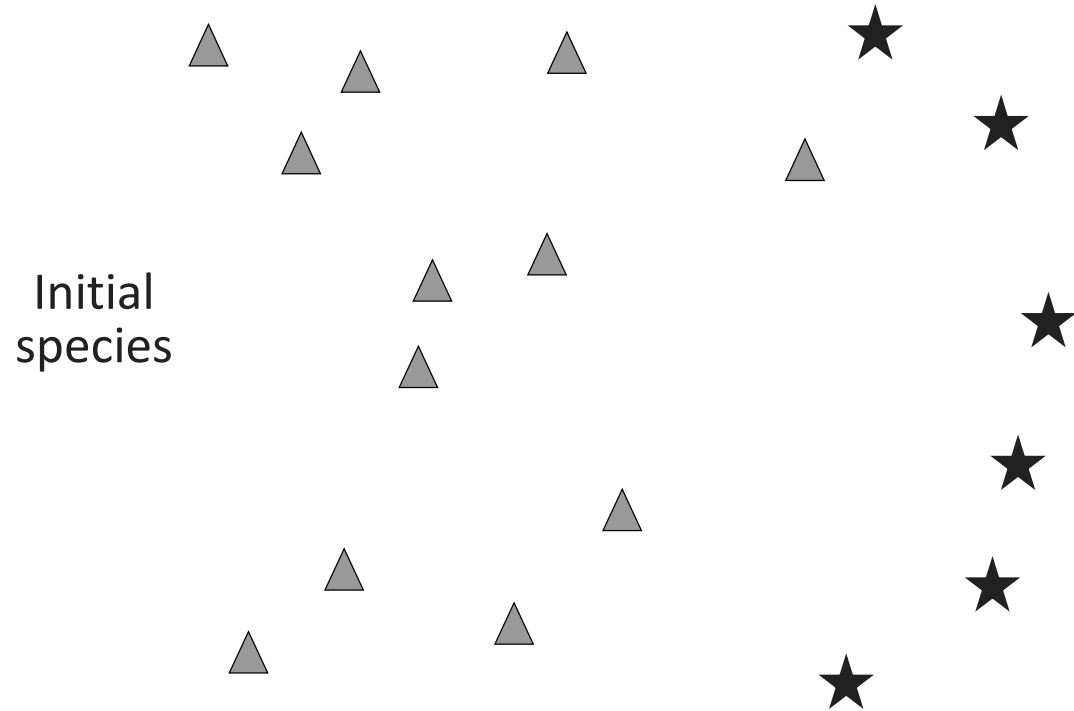


D. Boiko\*, T. Reschütze\*, B. Sanchez-Lengeling, S. M. Blau, G. d. P. Gomes, *In preparation*

# Introduction to Chemical Reaction Networks (CRNs)

▲ = Unstable intermediate

★ = Stable product

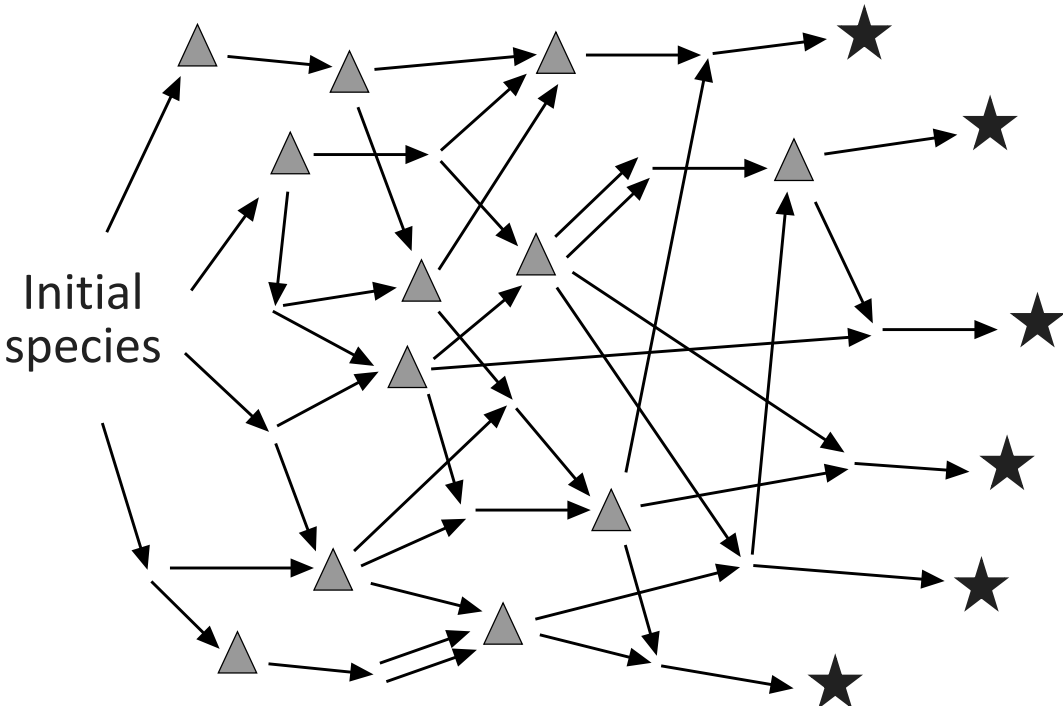


Chemical reaction network (CRN)

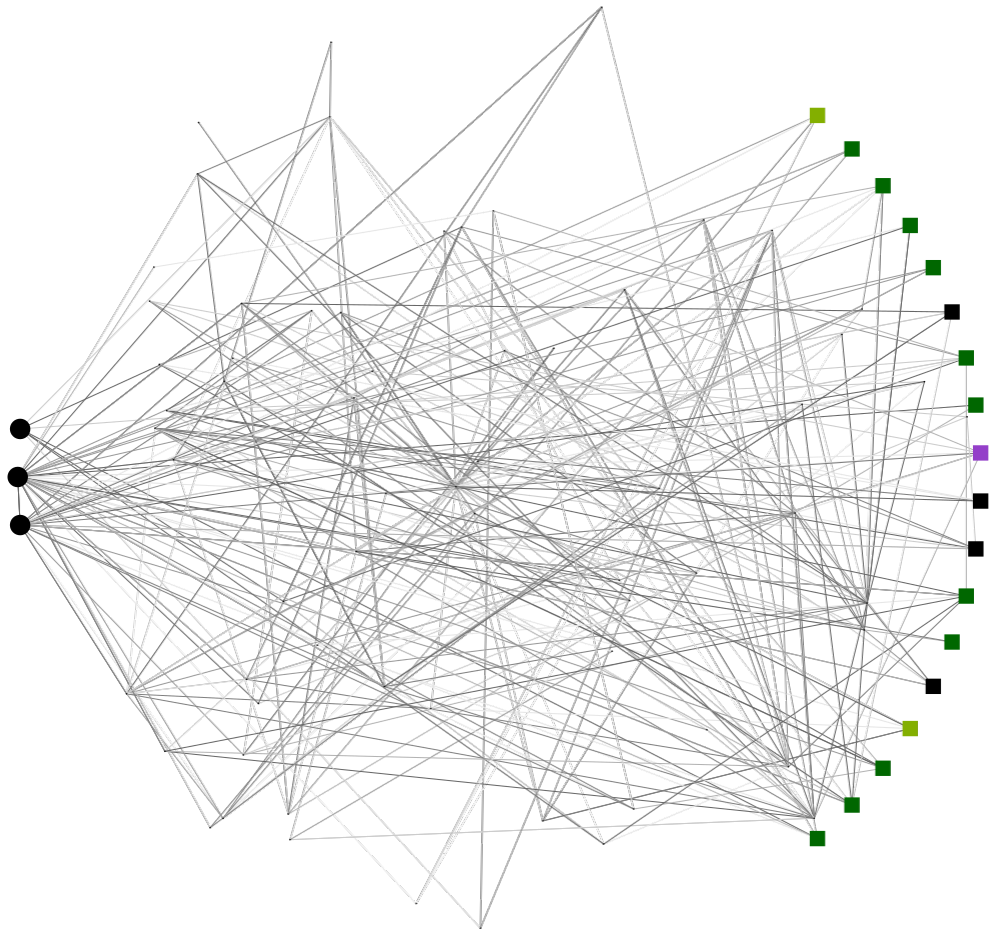


# Introduction to Chemical Reaction Networks (CRNs)

▲ = Unstable intermediate      ★ = Stable product



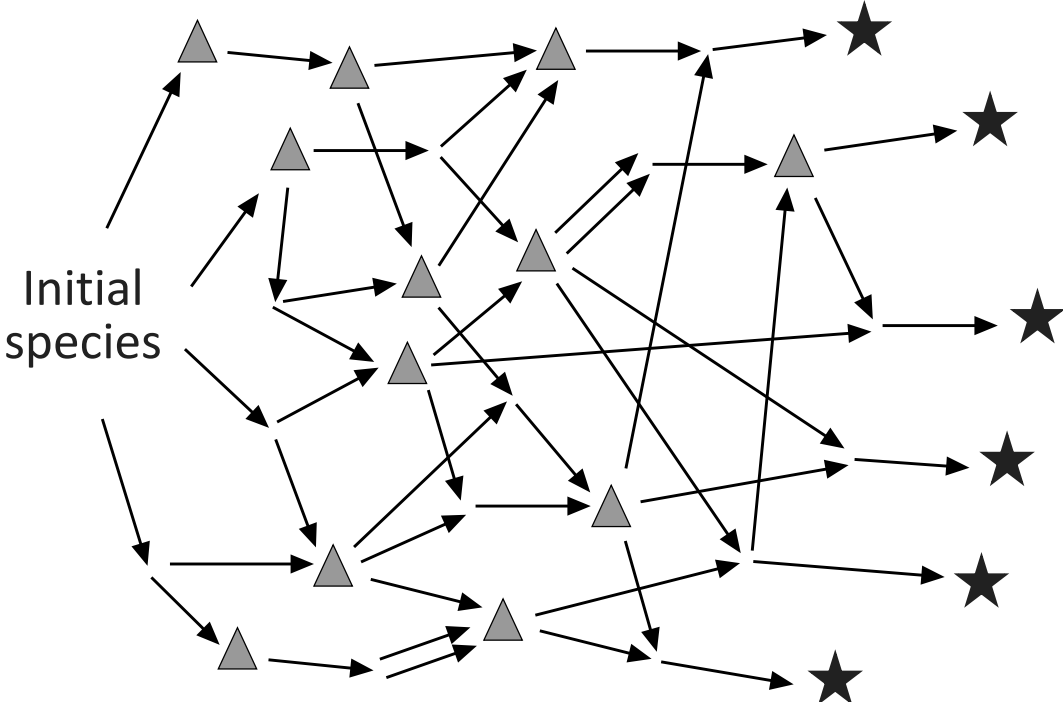
Chemical reaction network (CRN)



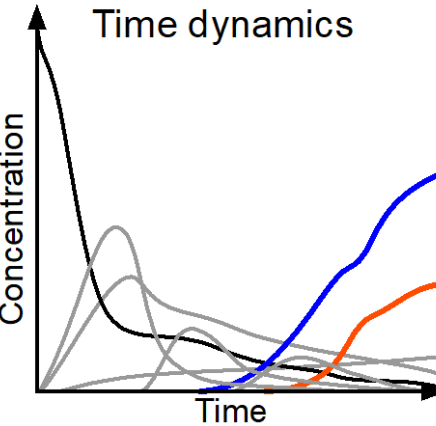
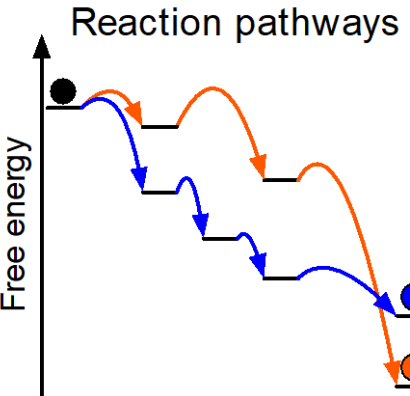
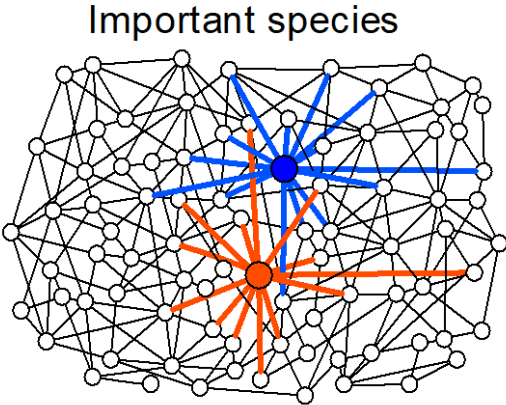
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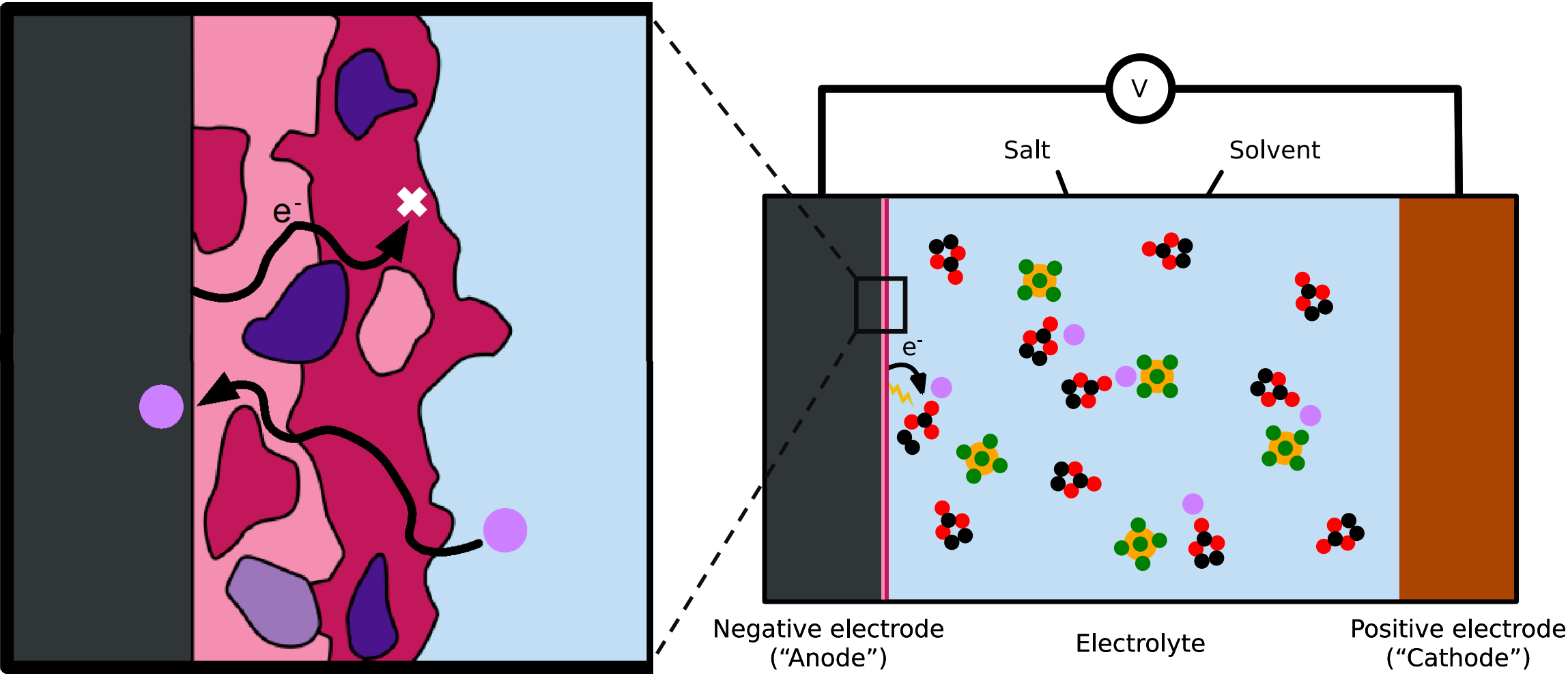


Chemical reaction network (CRN)

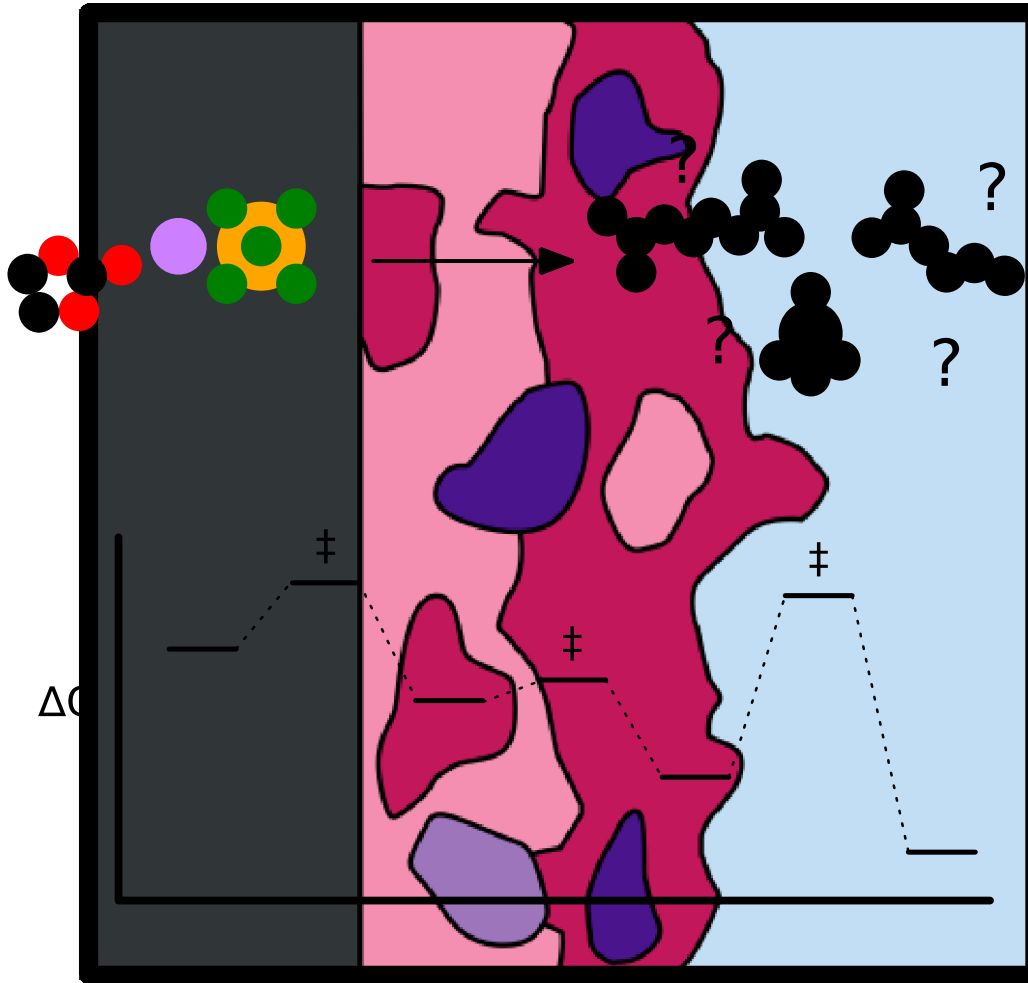


M. Wen, E. W. C. Spotte-Smith, **S. M. Blau**, M. J. McDermott, A. S. Krishnapriyan, K. A. Persson, *Nat. Comp. Sci.* 2023

# Background: Solid-Electrolyte-Interphase Formation



# Background: Solid-Electrolyte-Interphase Formation



**Goal:** enable next-generation batteries by controlling SEI formation

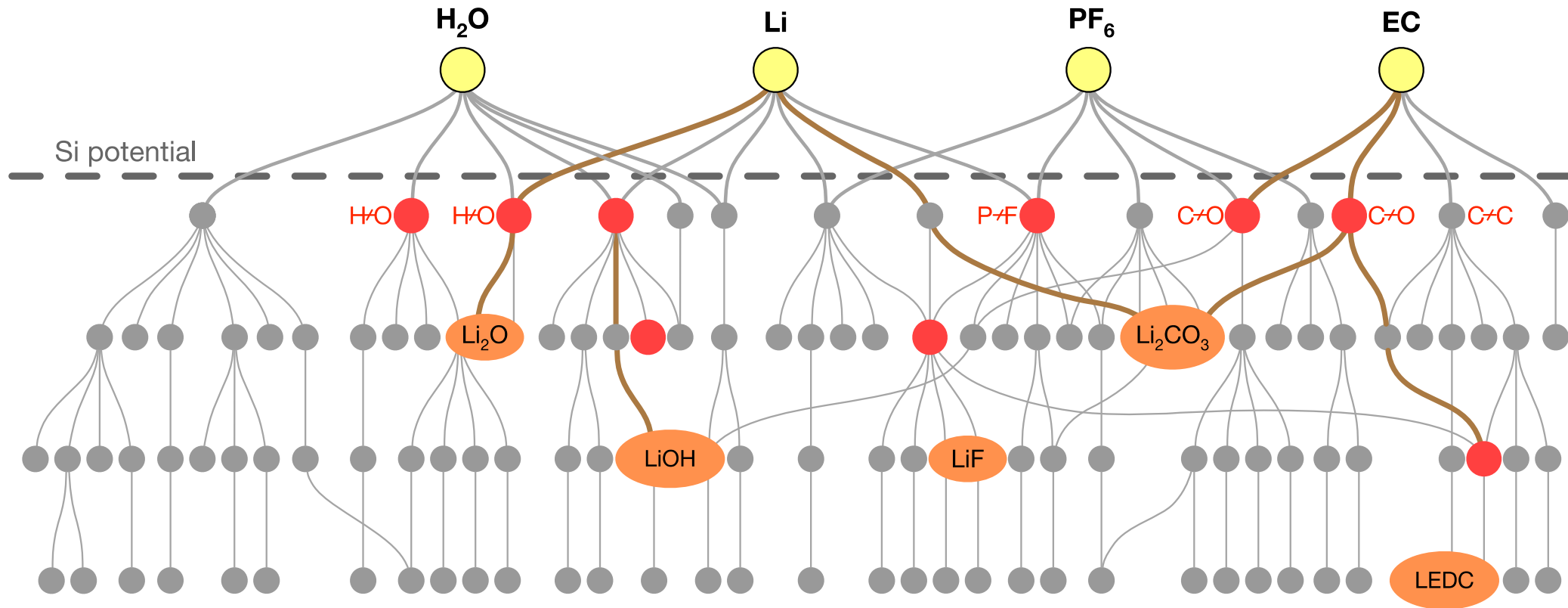
Big questions:

1. What species form?
  - Identify products
2. How do those species form?
  - Reaction mechanisms
3. How do individual species, pathways compete and interact?

AIMD, by-hand DFT investigations: limited insight



# A Data-Driven Approach to Understanding Reactivity



- Rational enumeration of possible species, reactions
- $\Delta G$  of each reaction in isolation via HT molecular DFT
- Network analysis: novel mechanistic insight
- Workflows necessary for data generation

# High-Throughput Molecular DFT Data Generation

**pymatgen**

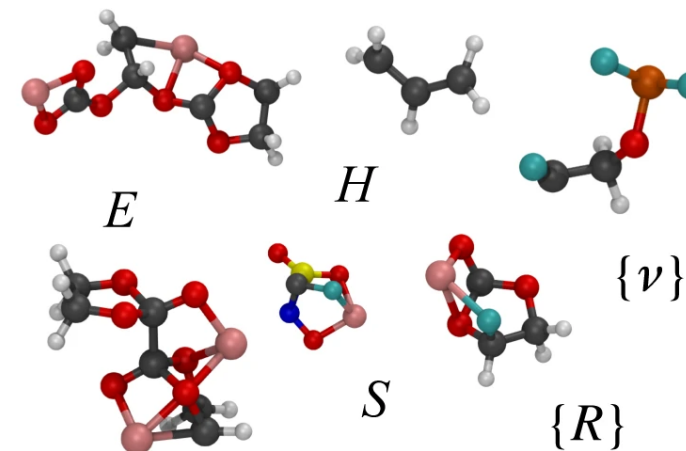
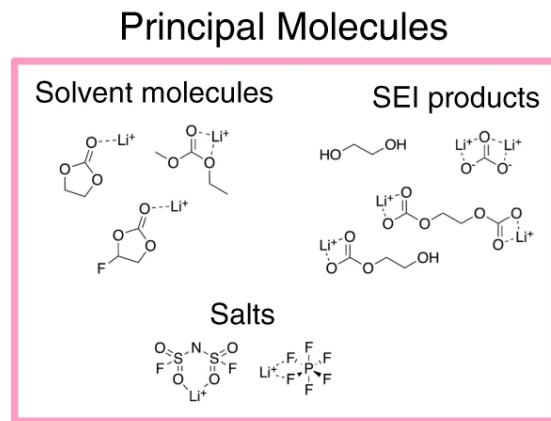
**Custodian**

**FireWorks**

**atomate**

**Q-CHEM**  
A QUANTUM LEAP INTO THE FUTURE OF CHEMISTRY

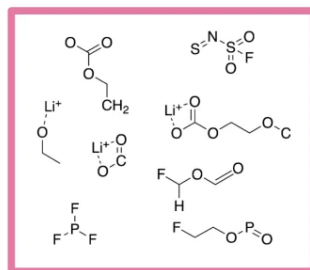
E. W. C. Spotte-Smith\*, S. M. Blau\*, X. Xie, H. D. Patel, M. Wen,  
B. Wood, S. Dwaraknath, K. A. Persson, *Sci. Data* 2021



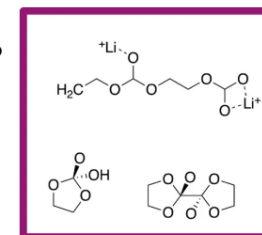
**HIGH-THROUGHPUT DFT**

**LIBE**

**Lithium-Ion Battery Electrolyte  
17,190 molecules**



Molecular Fragments

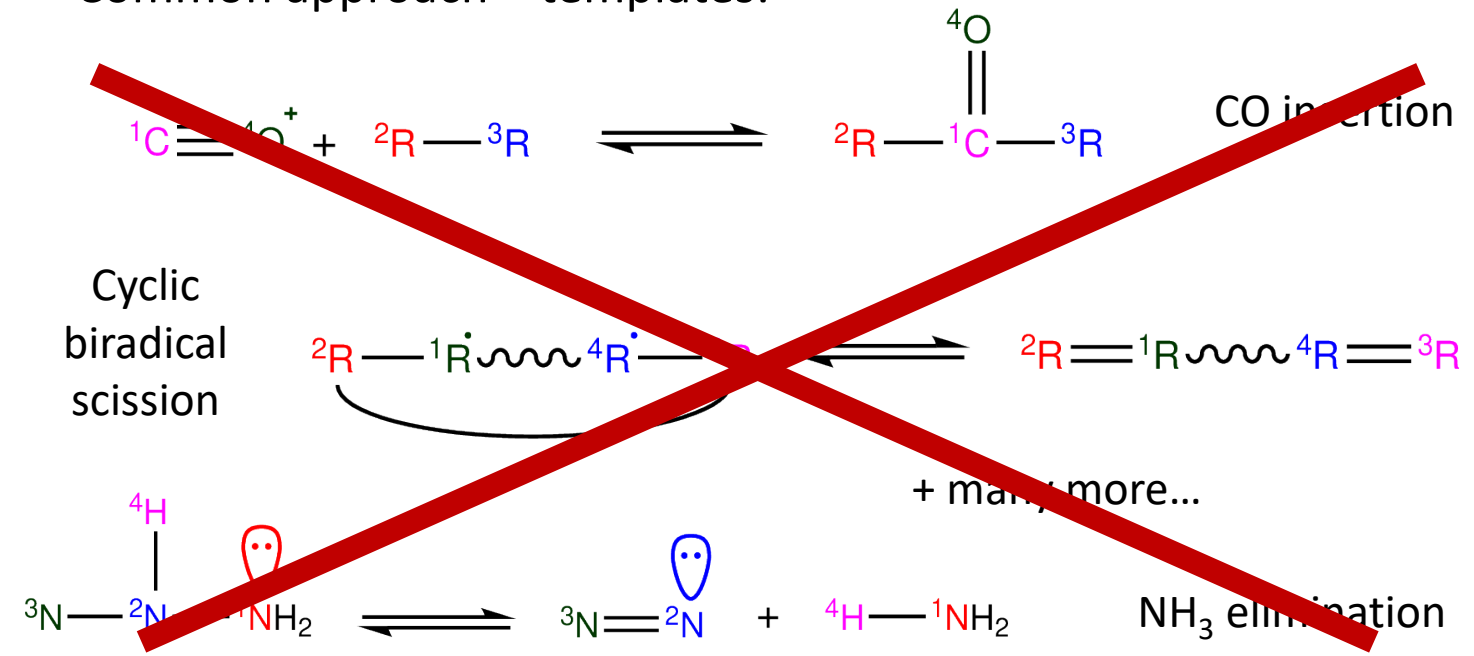


Selective Recombinant  
Molecules



# The Challenge of Reaction Generation

- Given e.g. 10k species, how to enumerate connecting reactions?
- Common approach – templates:



## Our solution: filters

### Goals:

- Minimize prescriptive constraints in order to *facilitate discovery*
- Want all reactions that:
  - Are likely to be single-step
  - May be kinetically viable
- Enable automated kinetic refinement
- Resolve complex competition

- Prescriptive templates are not well-suited to electron-driven chemistry

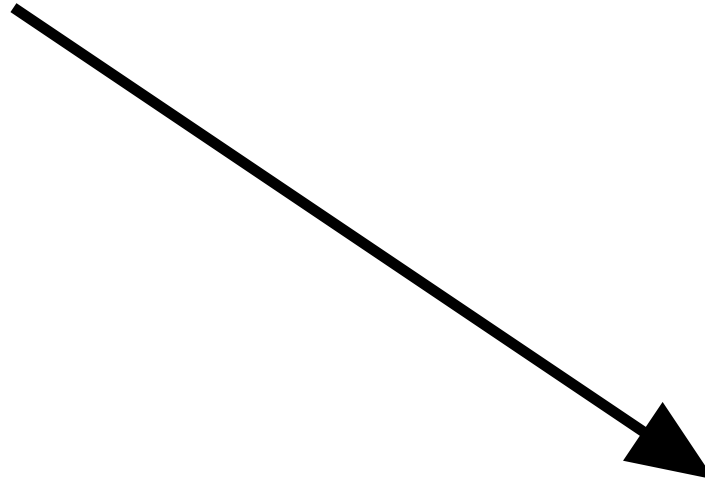
# High-Performance Reaction Generation:

HiPRGen 

$S_{init}$

**Input:** initial species

LIBE-CHOLi = 8904 species



$S_{filtered}$   $R_{filtered}$

**Output:** species, reactions that compose network



# High-Performance Reaction Generation:

# HiPRGen

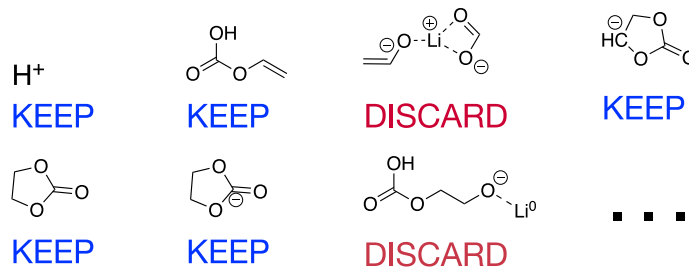
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Input: initial species

LIBE-CHOLi = 8904 species



## 1. Filter species



- Metal-centric complexes
- $Li^0$ -containing species

After filtering = 5193 species

# High-Performance Reaction Generation:

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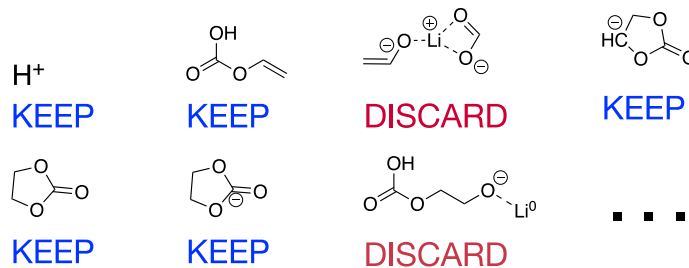
$S_{init}$

Input: initial species



LIBE-CHOLi = 8904 species

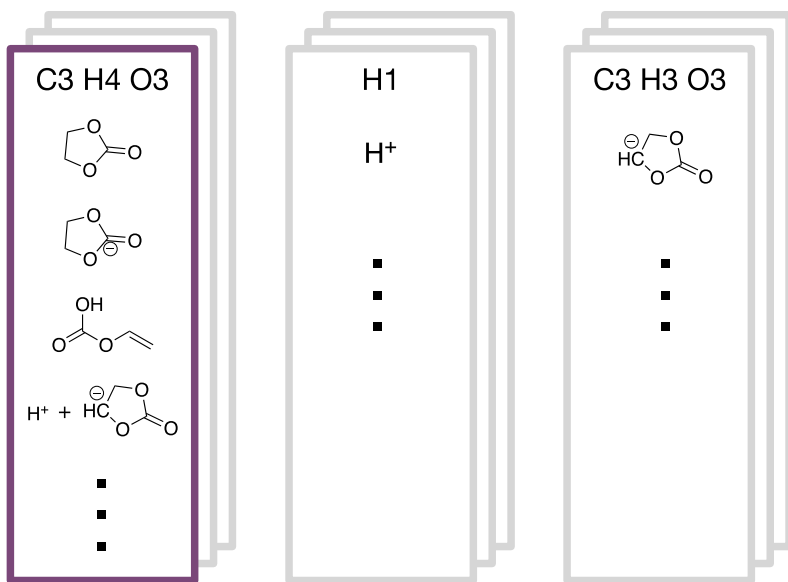
## 1. Filter species



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After filtering = 5193 species

## 2. Bucket Species by Composition



# High-Performance Reaction Generation:

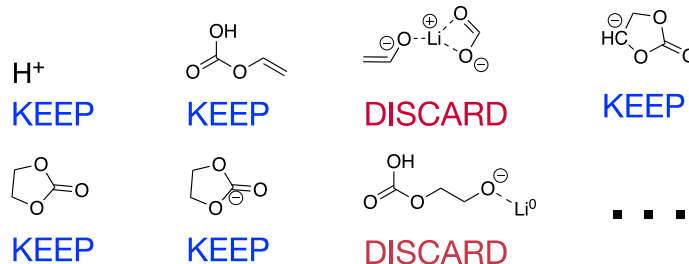
HiPRGen 

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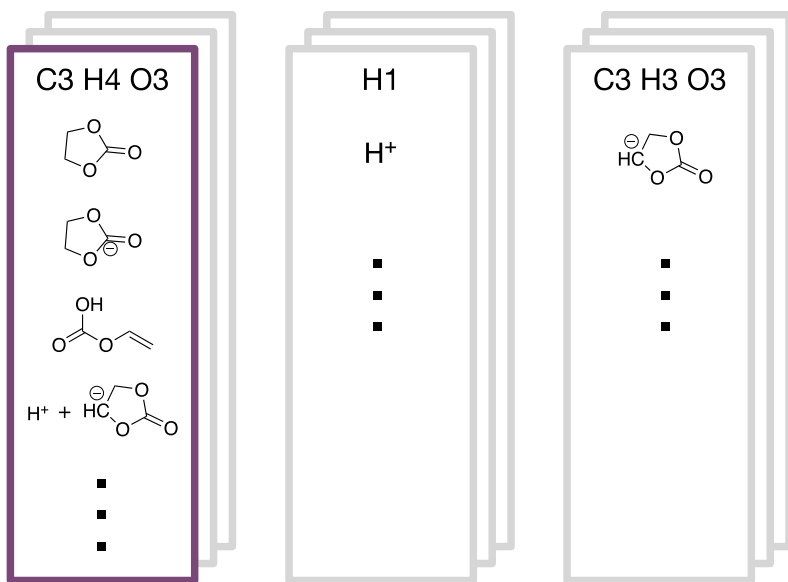
LIBE-CHOLi = 8904 species

## 1. Filter species

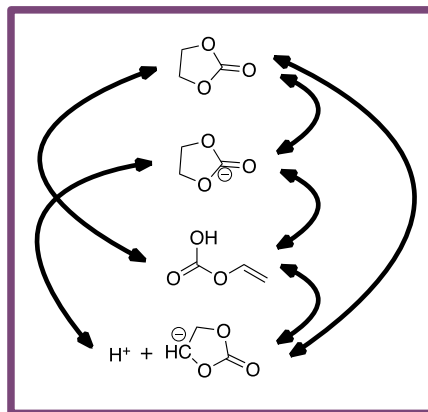


After filtering = 5193 species

## 2. Bucket Species by Composition



## 3. Generate reactions by stoichiometry



> 176 billion rxns

# High-Performance Reaction Generation:

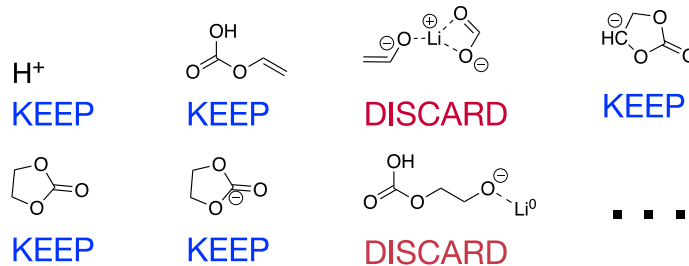
# HiPRGen

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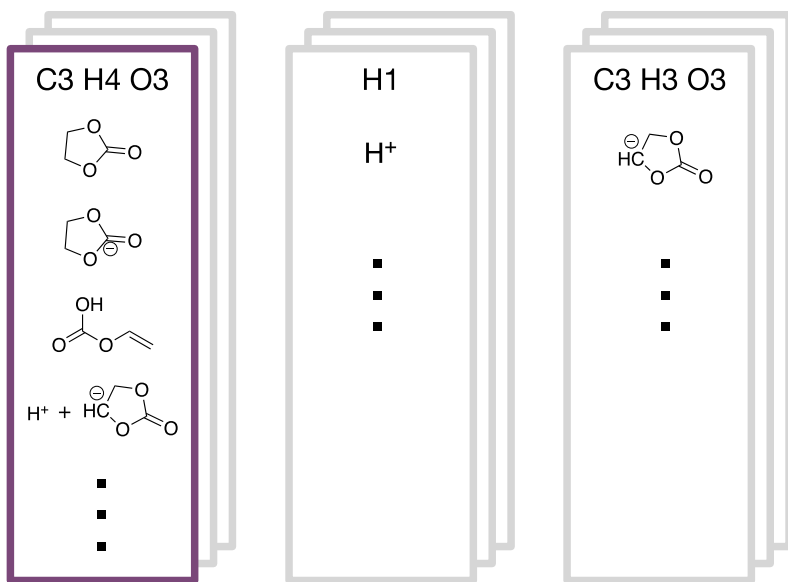
LIBE-CHOLi = 8904 species

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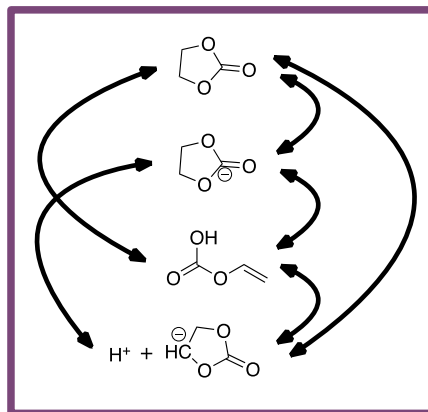


After filtering = 5193 species

## 2. Bucket Species by Composition

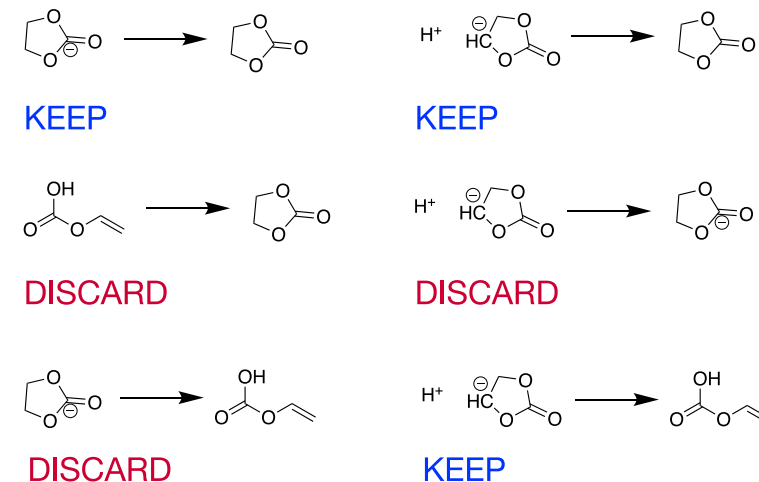


## 3. Generate reactions by stoichiometry



> 176 billion rxns

## 4. Filter reactions



- Too many bonds changing
- Bond change + redox
- Coordination + covalent bond change



# High-Performance Reaction Generation:

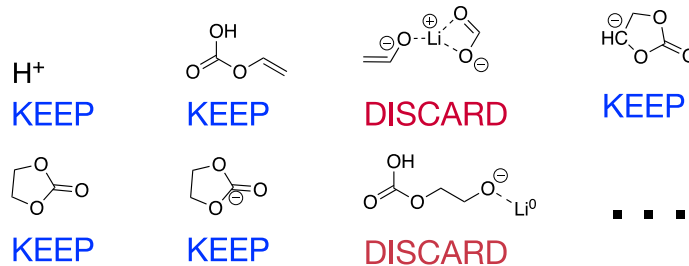
# HiPRGen

$S_{init}$

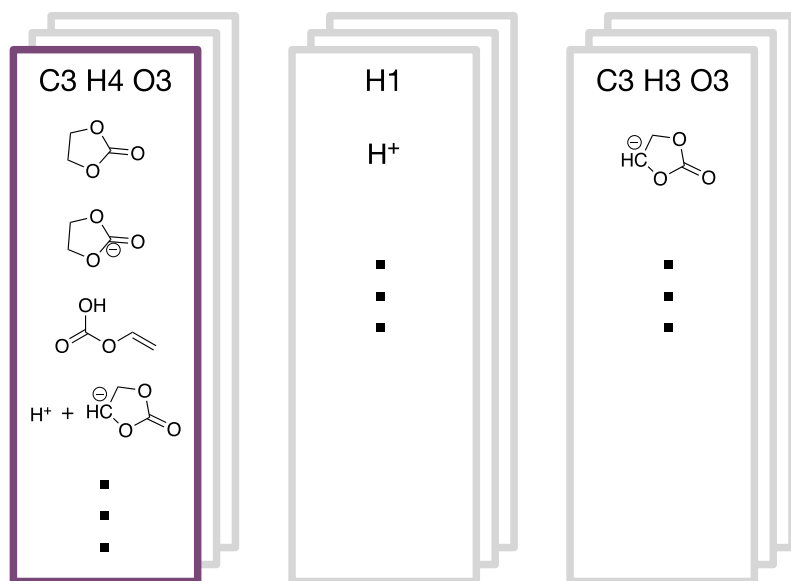
Input: initial species

LIBE-CHOLi = 8904 species

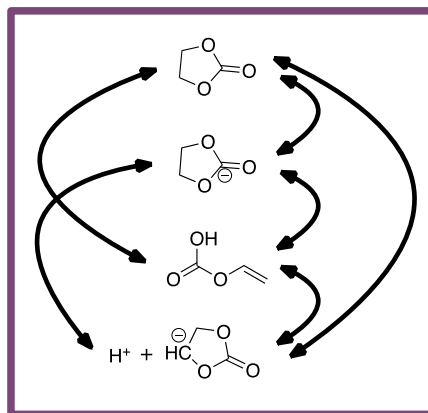
## 1. Filter species



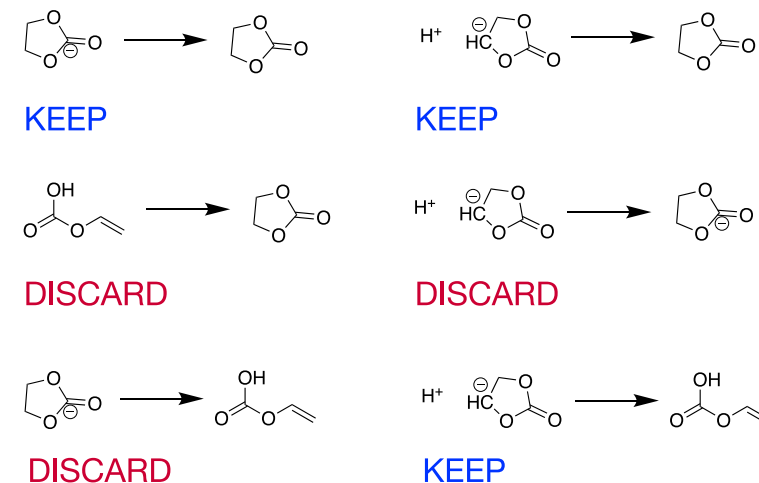
## 2. Bucket Species by Composition



## 3. Generate reactions by stoichiometry



## 4. Filter reactions



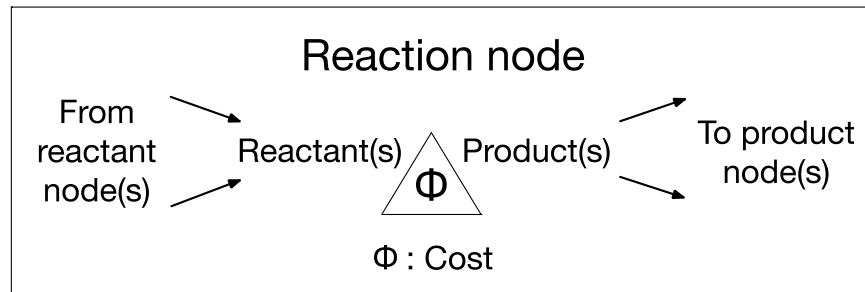
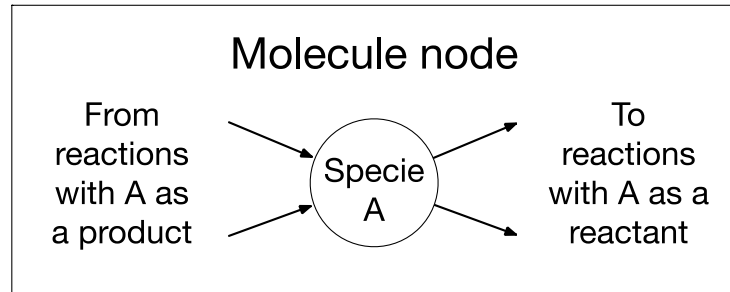
5193 species

86 million rxns

$S_{filtered}$   $R_{filtered}$

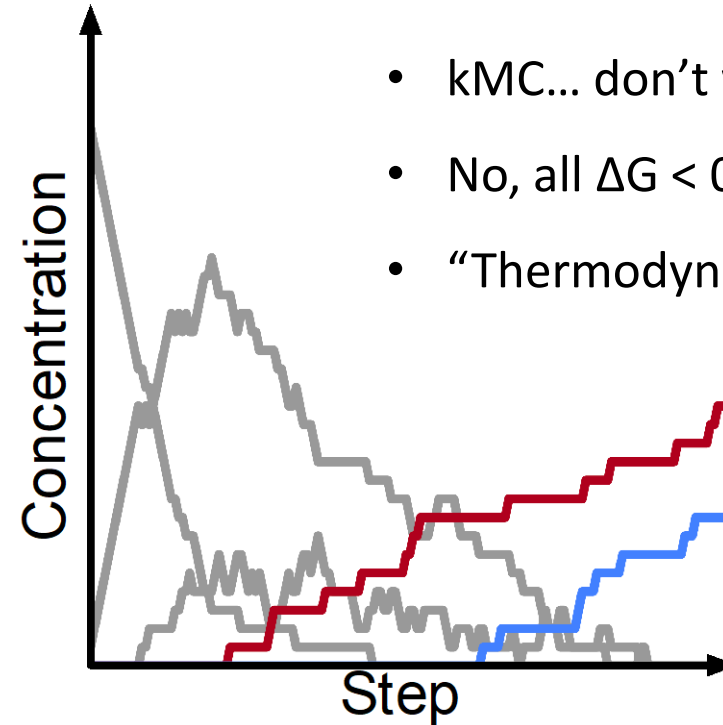
Output: species, reactions that compose network

# Reaction Network Analysis: Graphs vs Kinetic Monte Carlo



S. M. Blau, H. D. Patel, E. Spotte-Smith, X. Xie, S. Dwaraknath, K. A. Persson, *Chem. Sci.* 2021

- No concept of system state / concentrations
- Pathfinding to a given species scales as  $O(N^2)$
- **Must know target of interest a priori**



- kMC... don't we need kinetics?
- No, all  $\Delta G < 0$  rxns, all same rate
- "Thermodynamically bounded"

- Need initial state, evolve full system stepwise
- Stochastic sampling scales as  $O(\log N)$  + parallelizable
- **Target prediction from full system exploration...?**

# Reaction Network Monte Carlo:

RNMC 

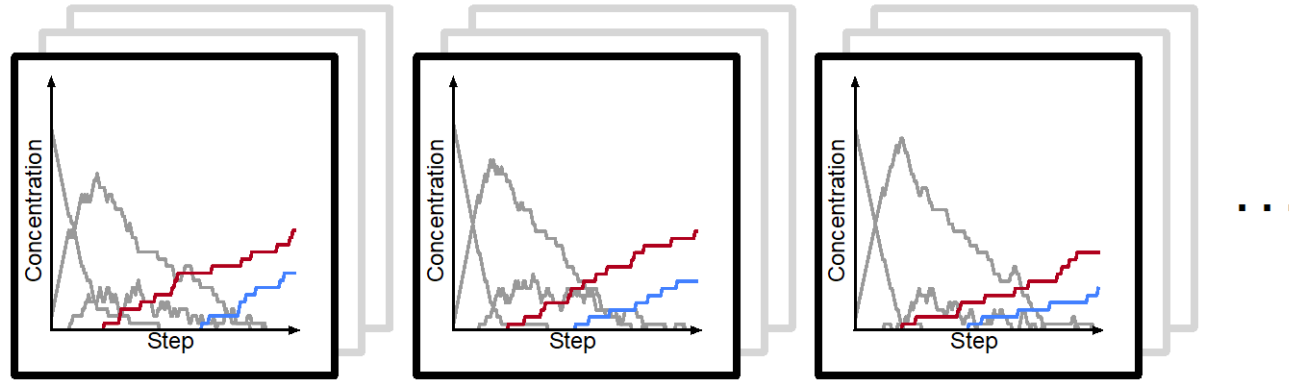
Inputs:

$\mathbf{S}_{filtered}$

$\mathbf{R}_{filtered}$

$[x_i, x_j, \dots]_0$

Perform many thermodynamically bounded Monte Carlo trajectories



- 30 of each  $x_i$
- All  $\Delta G < 0$ : can run to completion
- 100k trajectories

# Reaction Network Monte Carlo:



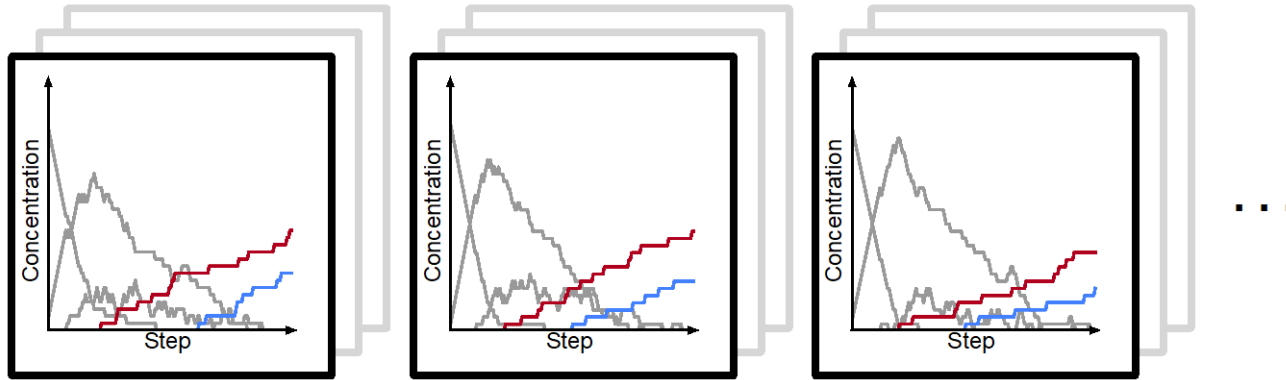
Inputs:

$S_{filtered}$

$R_{filtered}$

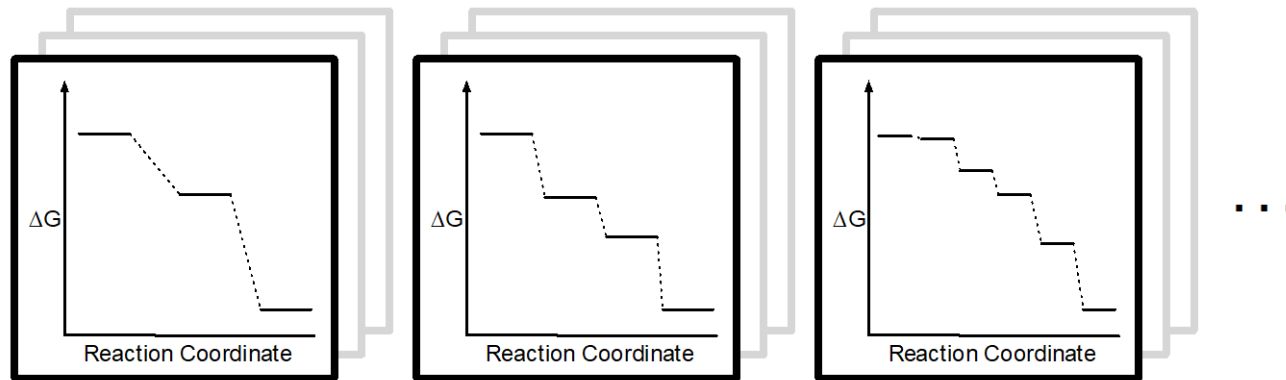
$[x_i, x_j, \dots]_0$

Perform many thermodynamically bounded Monte Carlo trajectories



- 30 of each  $x_i$
- All  $\Delta G < 0$ : can run to completion
- 100k trajectories

Extract shortest reaction pathways from each trajectory to each specie of interest

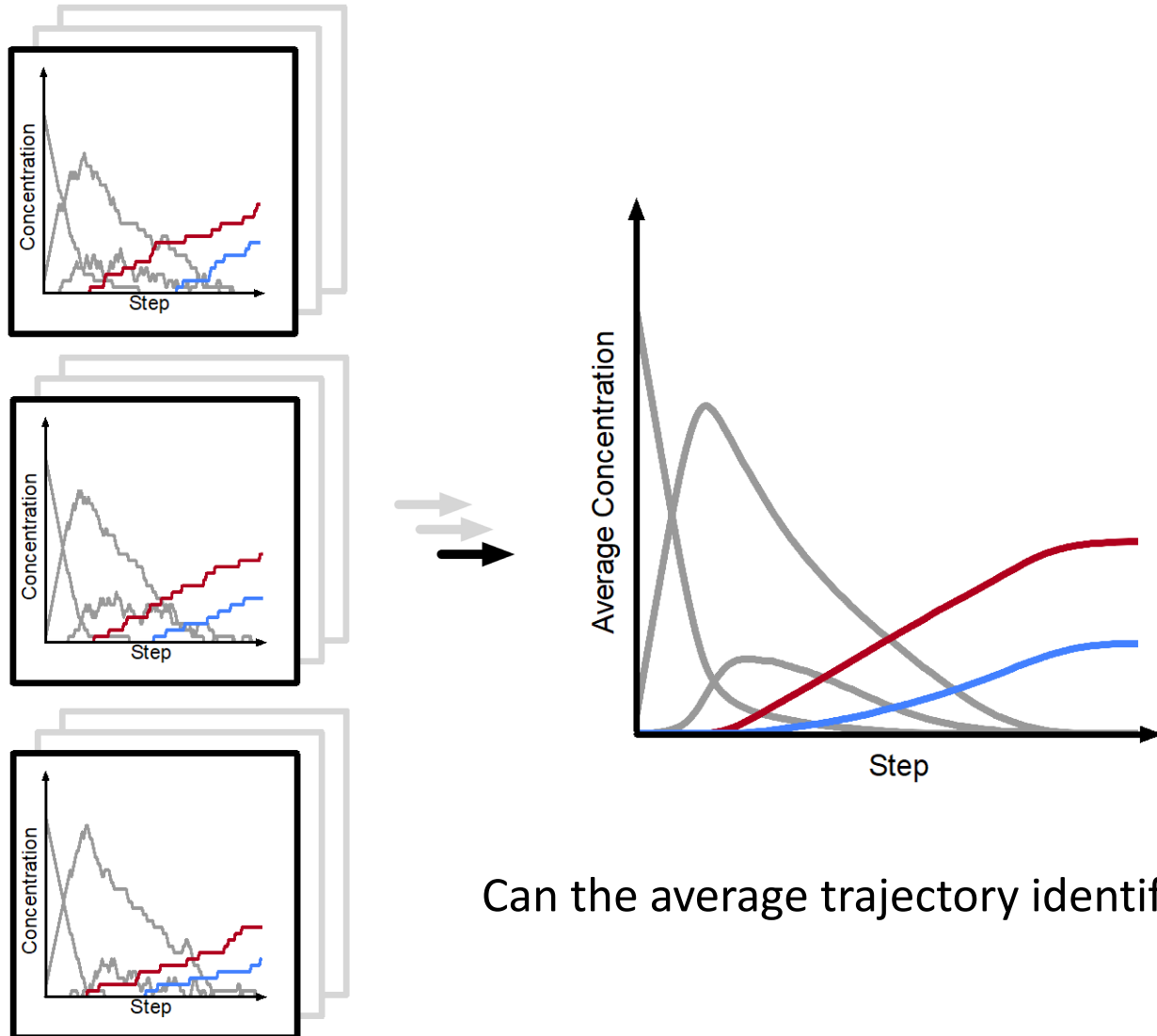


Group and order by cost  
 $\Phi \approx \#$  of reactions

Can do pathfinding  
on up to approx. 300  
million reactions

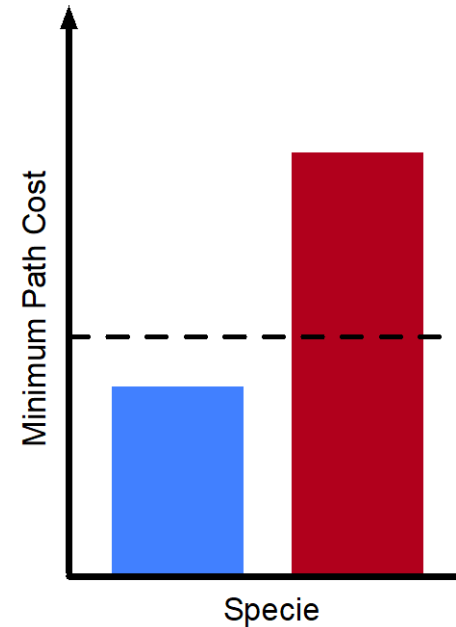
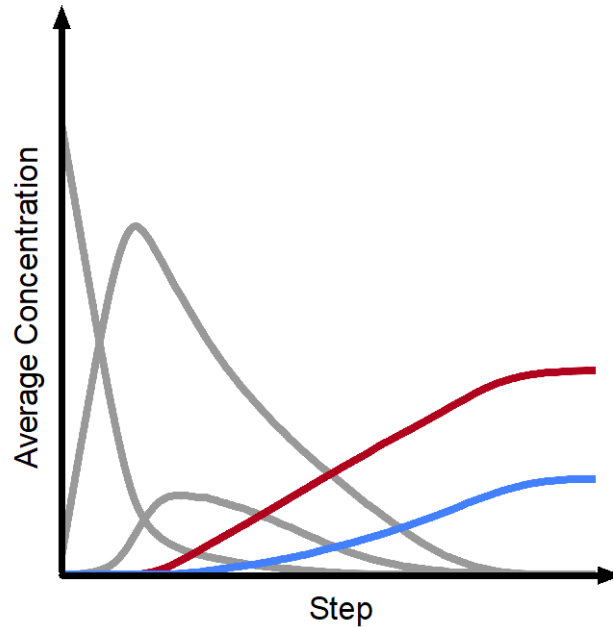
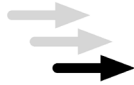
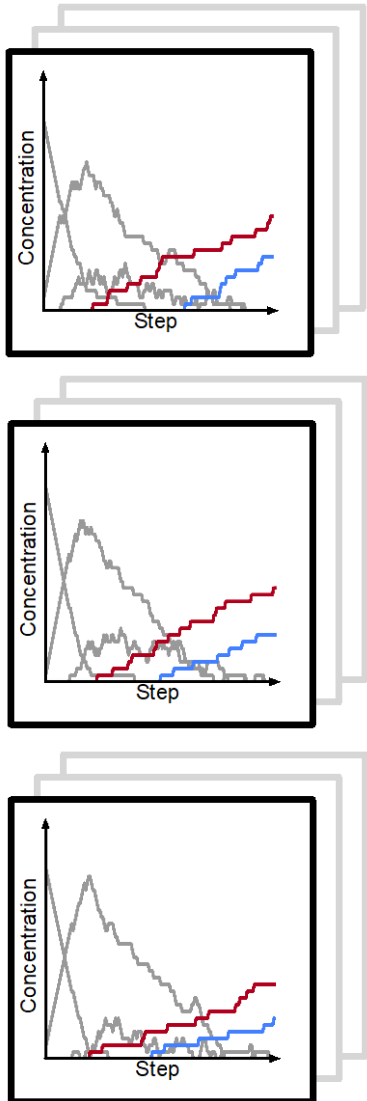
[github.com/BlauGroup/HiPRGen](https://github.com/BlauGroup/HiPRGen)  
[github.com/BlauGroup/RNMC](https://github.com/BlauGroup/RNMC)

# Converging RNMC and Identifying Network Products



Can the average trajectory identify network products?

# Converging RNMC and Identifying Network Products



- Totally heuristic
- **Network** products, not real products

High formation / consumption

Significant accumulation

Low-cost pathways available

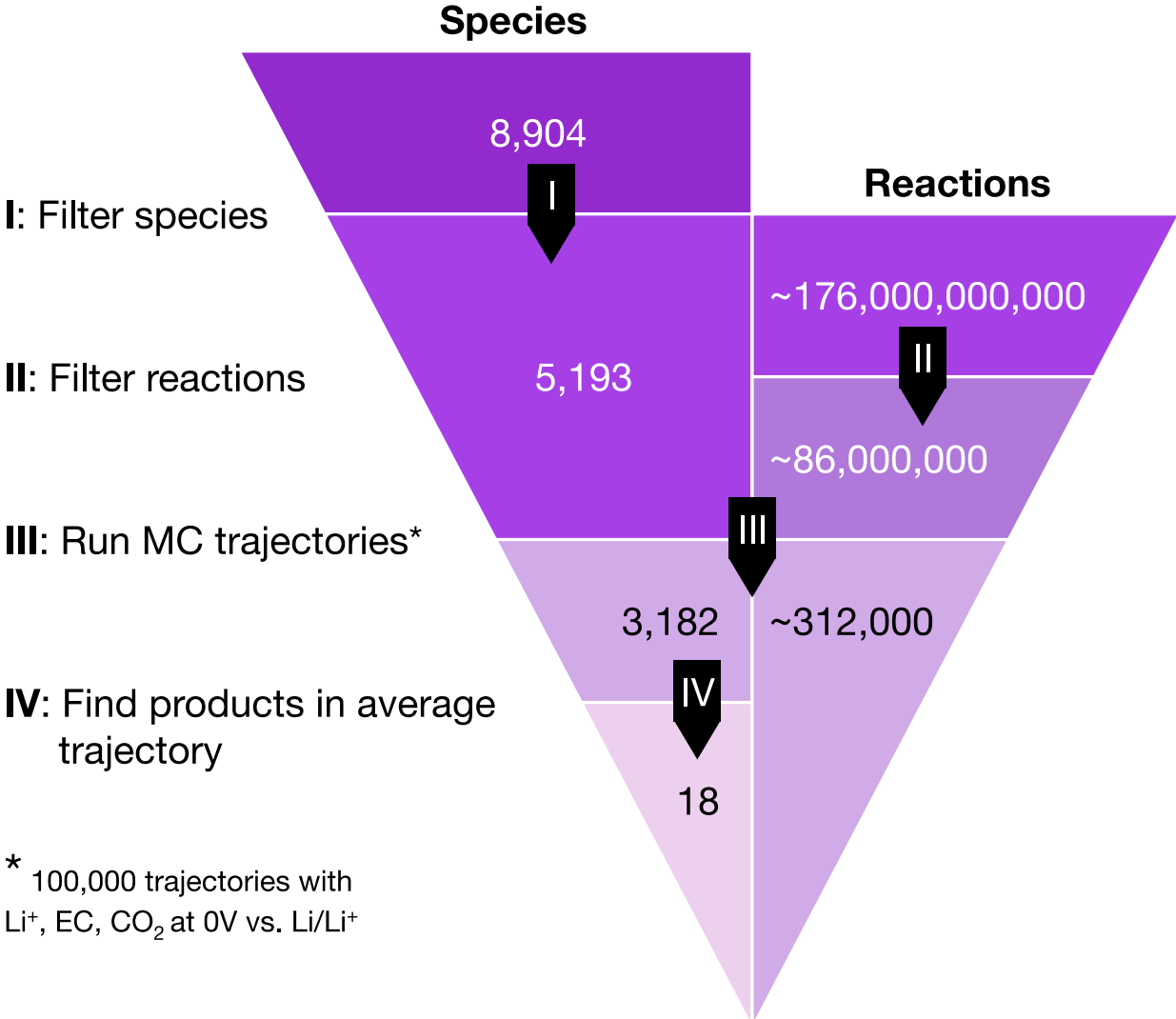
**Network product?**



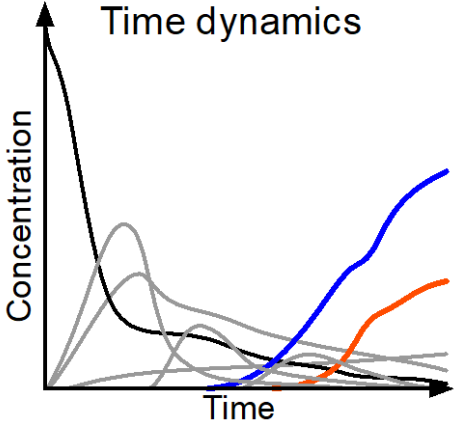
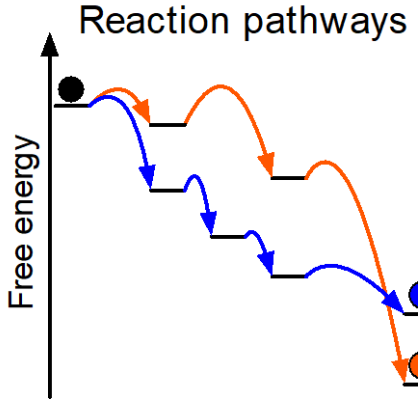
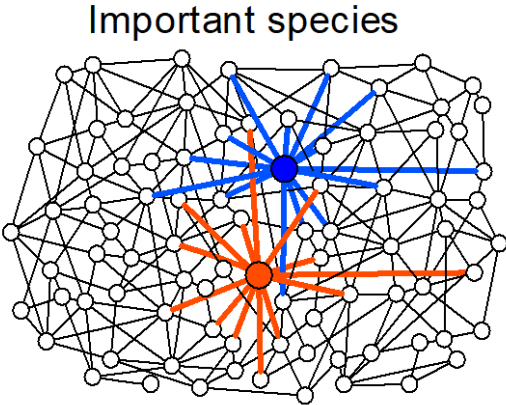
Can the average trajectory identify network products?



# Building Up and Picking Apart Complexity



\* 100,000 trajectories with Li<sup>+</sup>, EC, CO<sub>2</sub> at 0V vs. Li/Li<sup>+</sup>

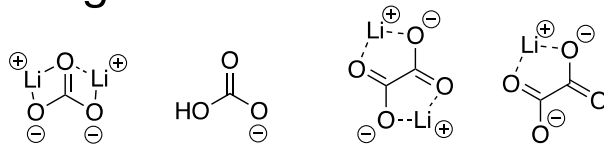


# Predicted Battery Network Products: 36 out of 5139

## Small molecules/gases



## Inorganics

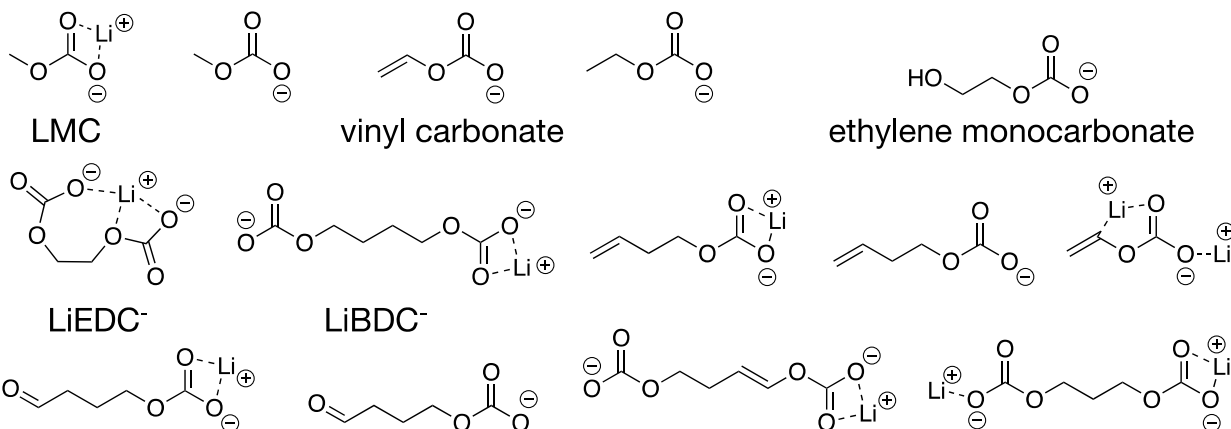


lithium carbonate

lithium oxalate

[EC, Li<sup>+</sup>] and [EC, Li<sup>+</sup>, CO<sub>2</sub>] at 0V and +0.5V vs. Li/Li<sup>+</sup>

## Alkyl carbonates



LMC

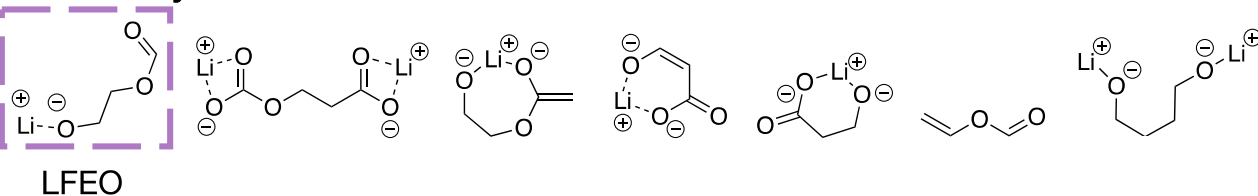
vinyl carbonate

ethylene monocarbonate

LiEDC<sup>-</sup>

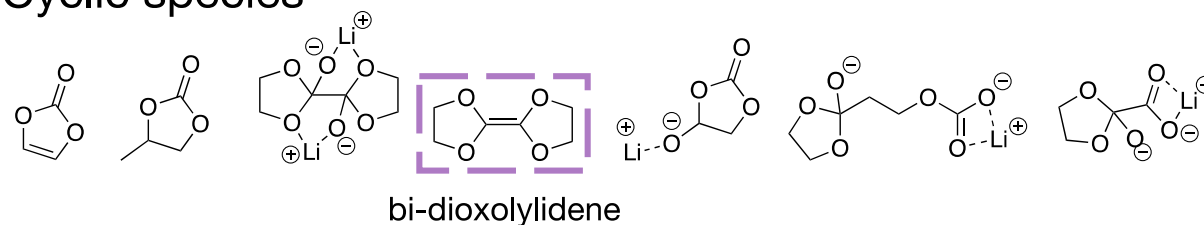
LiBDC<sup>-</sup>

## Carboxylates, esters, and oxides



LFEO

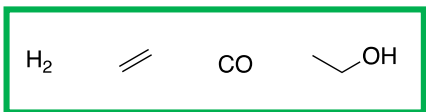
## Cyclic species



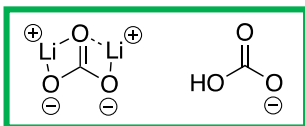
bi-dioxolylidene

# Predicted Battery Network Products: 36 out of 5139

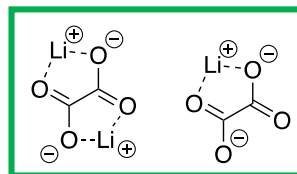
## Small molecules/gases



## Inorganics



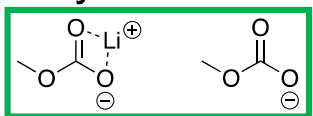
lithium carbonate



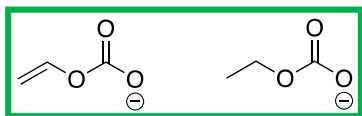
lithium oxalate

[EC, Li<sup>+</sup>] and [EC, Li<sup>+</sup>, CO<sub>2</sub>] at 0V and +0.5V vs. Li/Li<sup>+</sup>

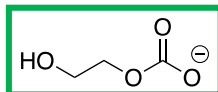
## Alkyl carbonates



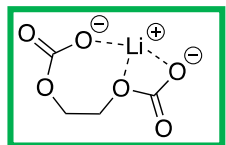
LMC



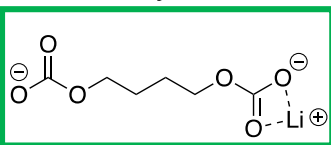
vinyl carbonate



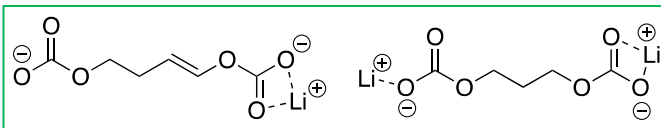
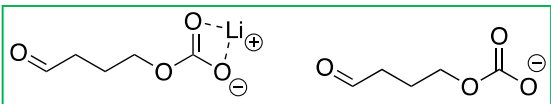
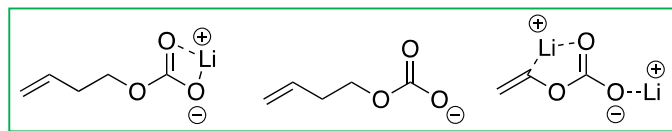
ethylene monocarbonate



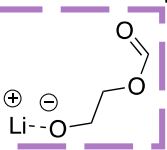
LiEDC<sup>-</sup>



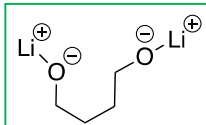
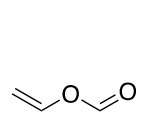
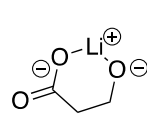
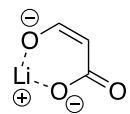
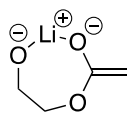
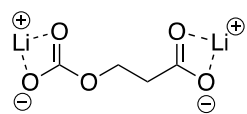
LiBDC<sup>-</sup>



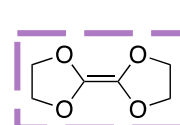
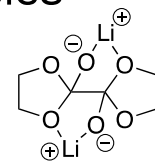
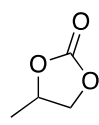
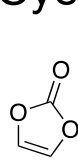
## Carboxylates, esters, and oxides



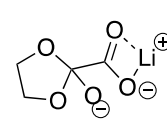
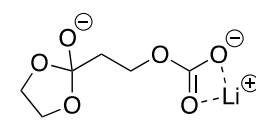
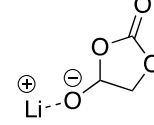
LFEO



## Cyclic species



bi-dioxolylidene

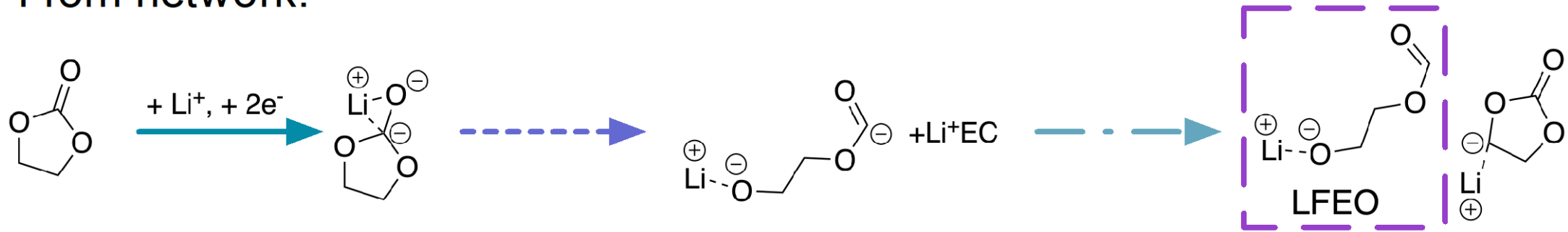


- Recovered nearly all observed or proposed molecular SEI components
- Only thermodynamics – unexpectedly effective!
- So about those particularly weird molecules...

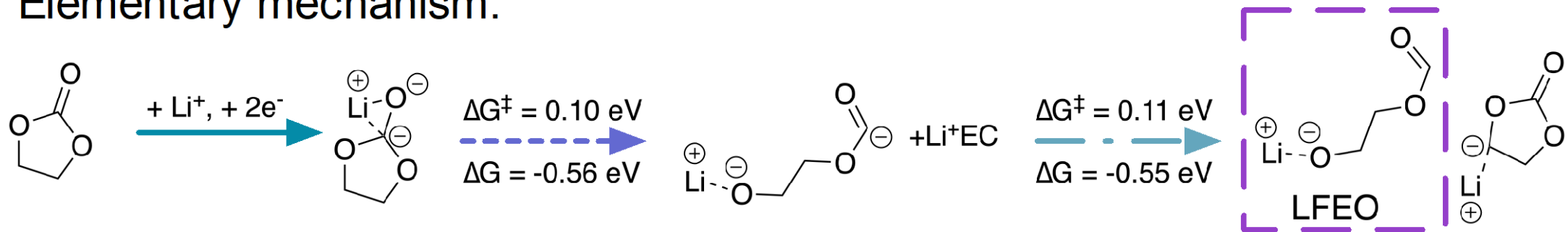
# Network Path to Refined Mechanism: LFEO

Applied semi-automated TS procedure to 15 shortest thermo. paths – 12<sup>th</sup> shortest with [Li<sup>+</sup>, EC] at 0V vs Li/Li<sup>+</sup>:

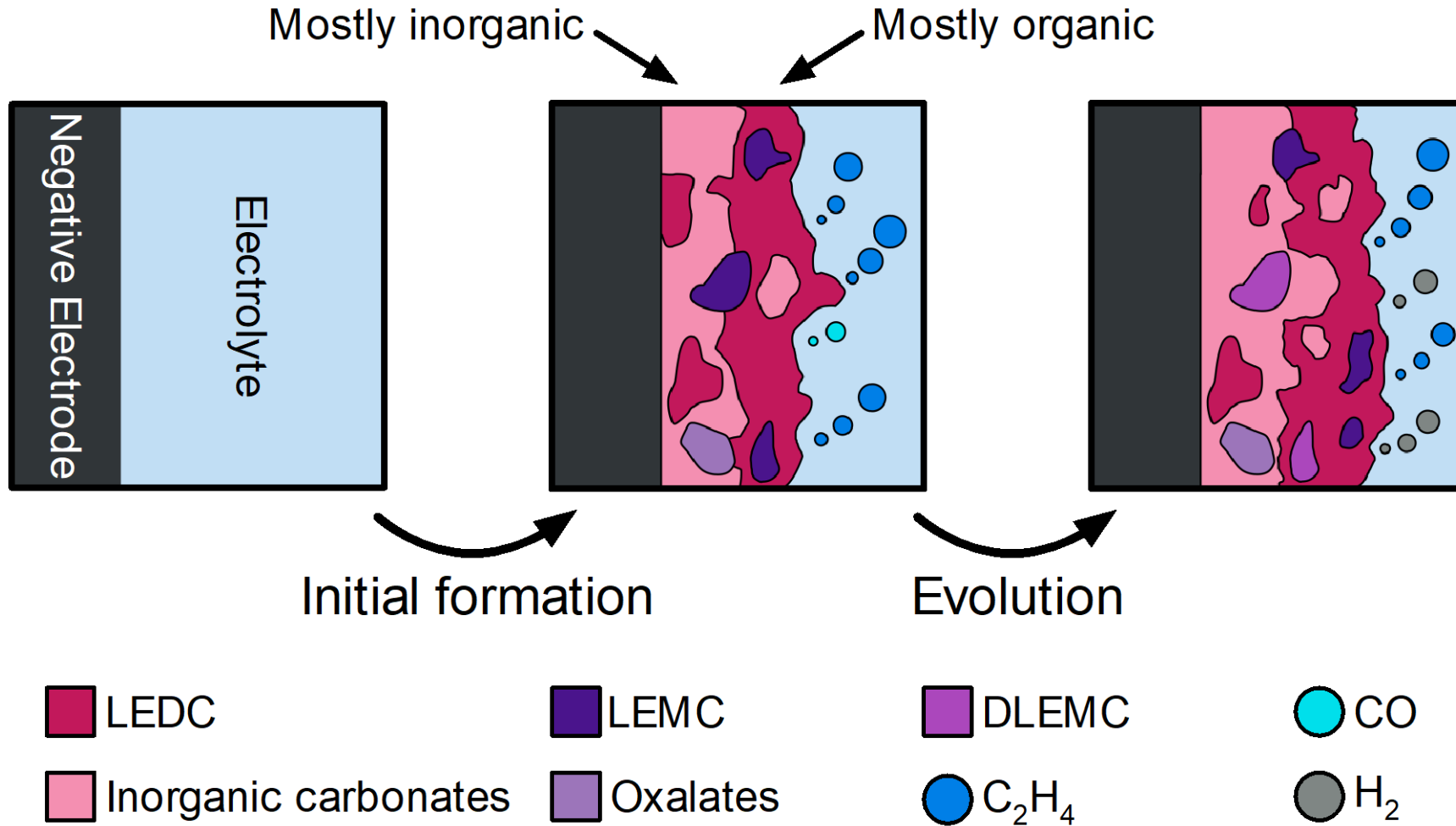
From network:



Elementary mechanism:

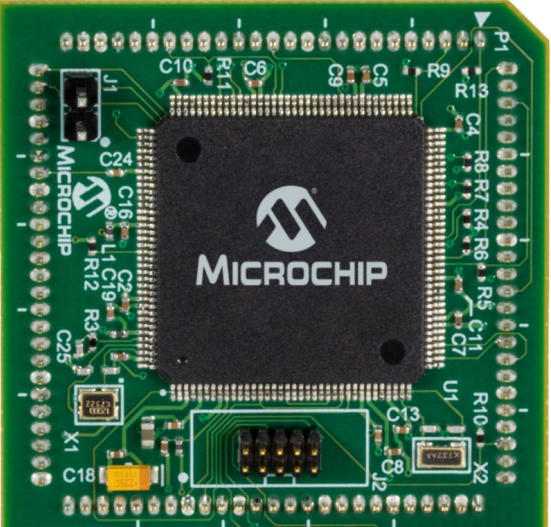
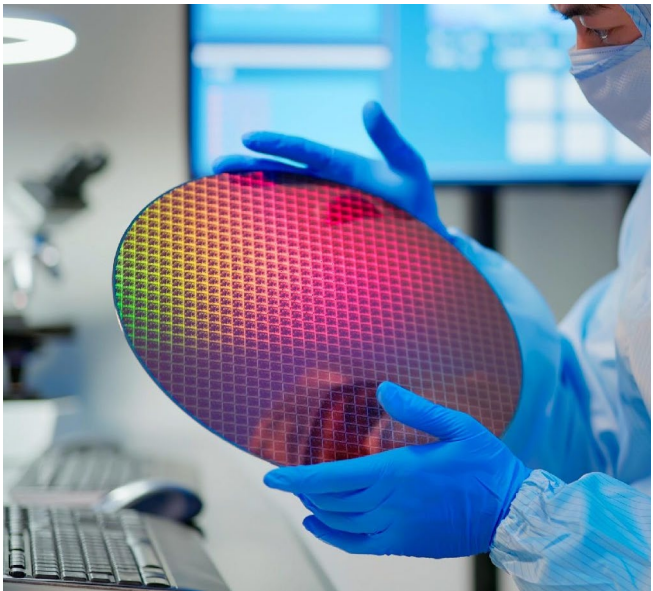


# Mechanistic Model of SEI Formation Derived from CRN



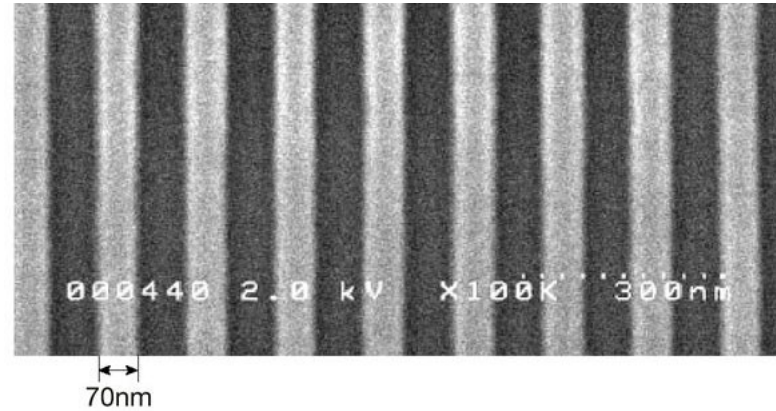
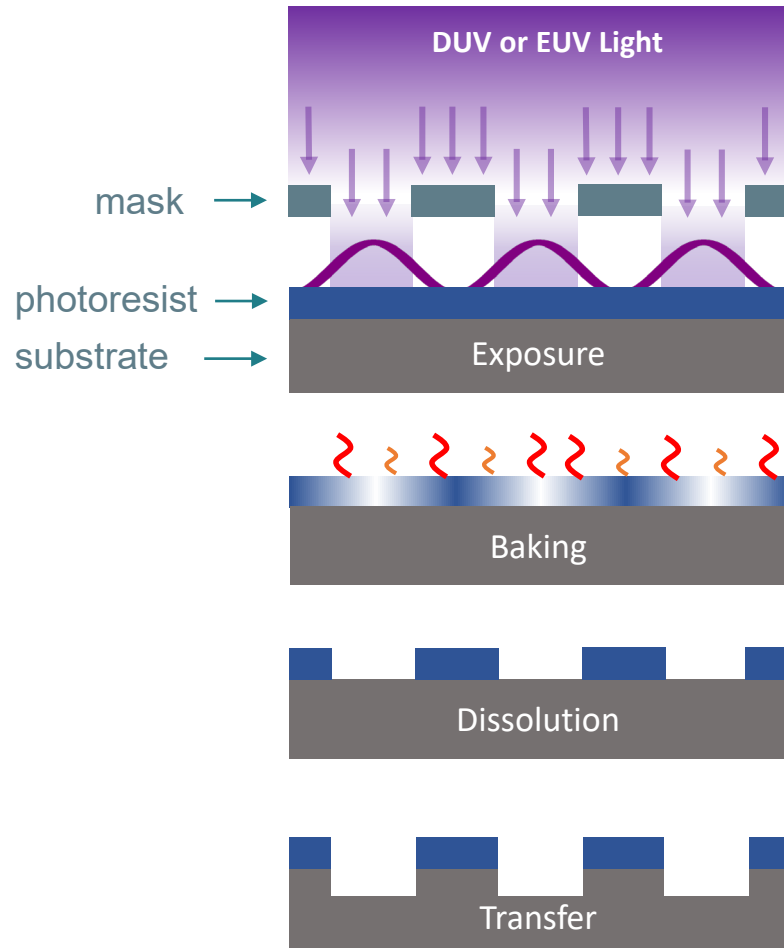
- Pathways derived from CRN, semi-automated  $\Delta G^\ddagger$  calcs
- Recovered bi-layer SEI from first principles for first time
- **Is this approach limited to just SEI formation? No!**

# Background: Nanoscale Patterning with Photolithography





# Background: Nanoscale Patterning with Photolithography



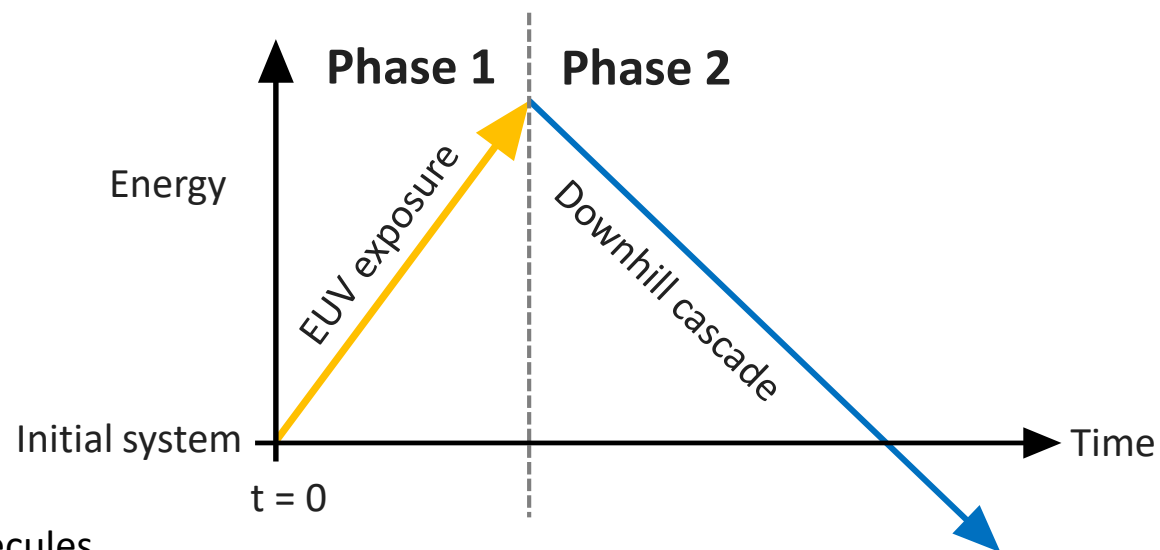
Chemical reactions  
cause solubility switch



- 1994 to 2017: “deep” UV, 248 nm – 134 nm light
  - 5 eV – 9 eV photons
  - **Selective** resonant photochemistry
- Want smaller patterns? Need shorter wavelength!
- 2018 to now: “extreme” UV, 13.5 nm light
  - 92 eV photons
  - Stochastic photoionization yields **poorly understood** radical ion reaction cascade



# EUV Lithography Reaction Network Construction



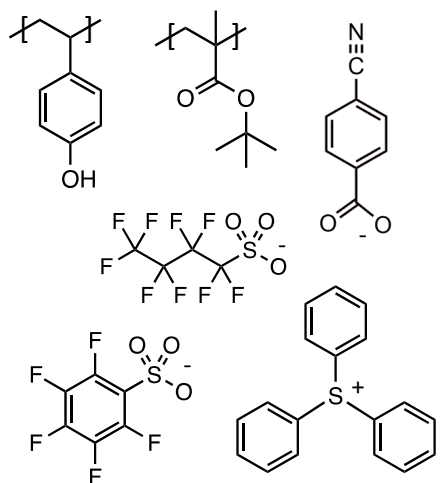
## Phase 1: EUV exposure

Keep reactions that are:

- Electron detachment (all  $\Delta G > 0$ )
- Electron attachment (all  $\Delta G < 0$ )
- $\Delta G > 0$  one-bond fragmentation
- $\Delta G > 0$   $H^+$  or  $H^0$  transfer

185,929 reactions

## Principal molecules



Fragment  
DFT opt.

108  
species

Recombine  
DFT opt.

3367  
species

HiPRGen

pymatgen

FireWorks

Custodian

atomate

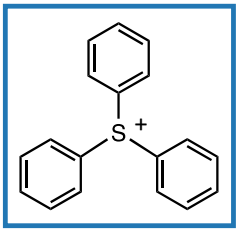
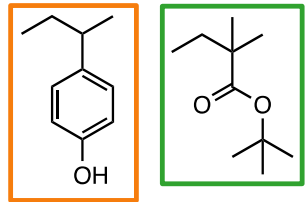
## Phase 2: Post-exposure cascade

Remove reactions with:

- $\Delta G > 0$
- Unbalanced redox
- $>2$  covalent bonds changing
- Sterically hindered reaction center

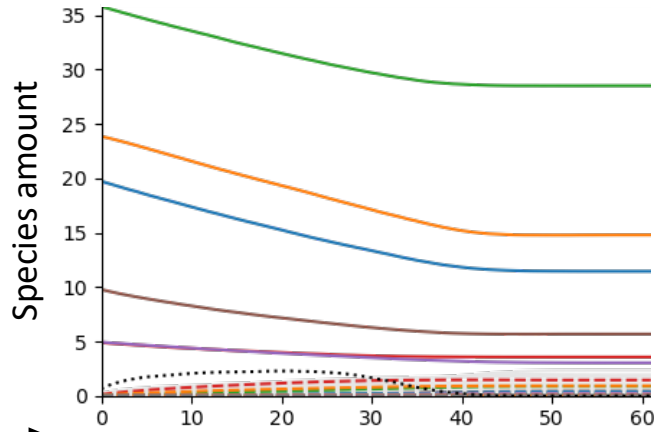
2,776,867 reactions

# EUV Lithography Reaction Network Analysis

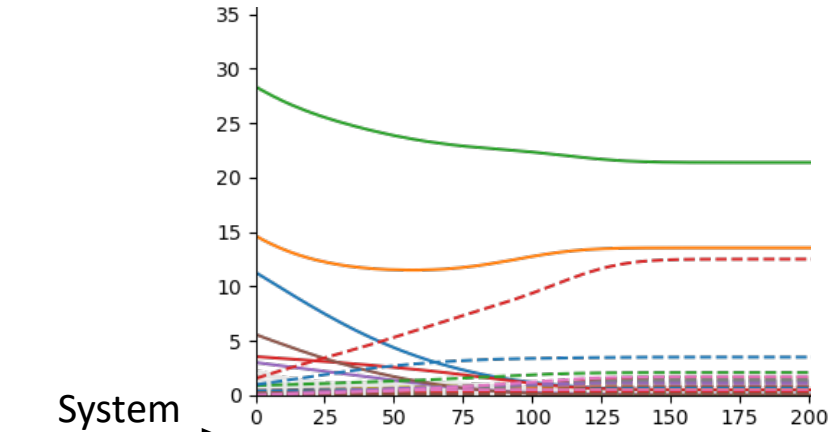


Initial state

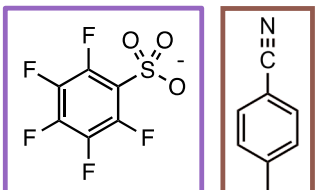
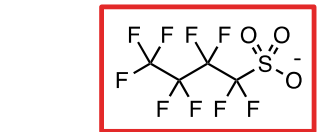
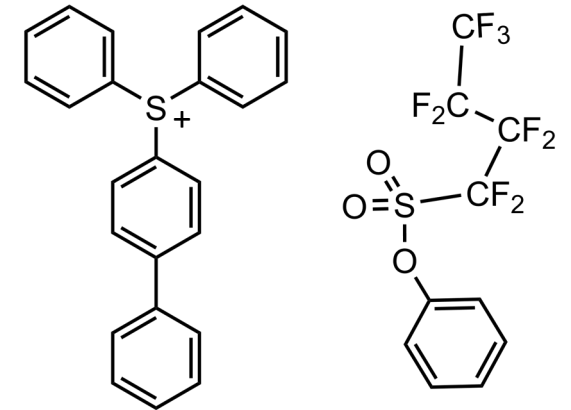
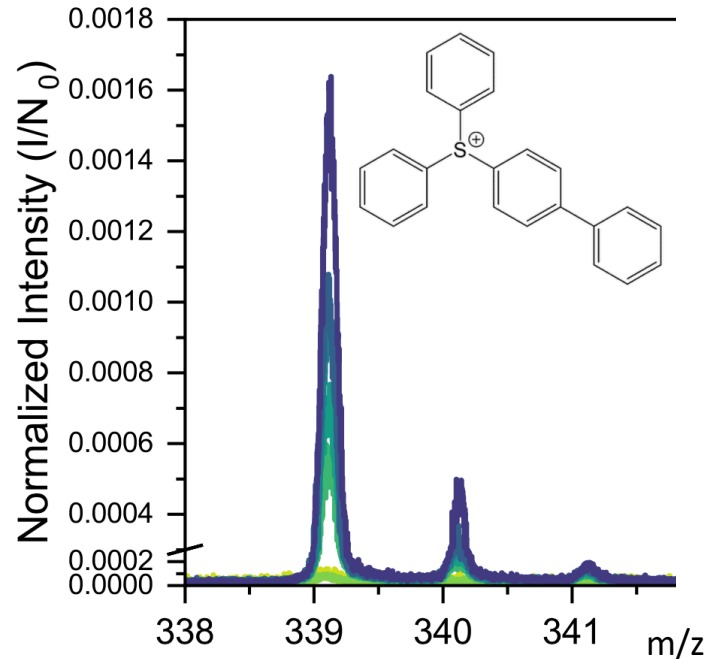
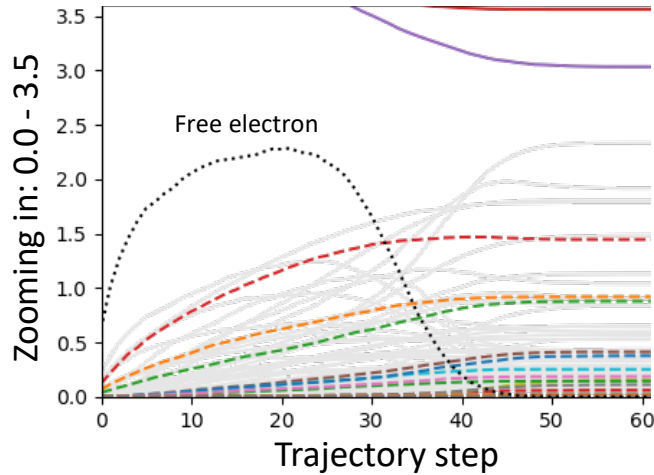
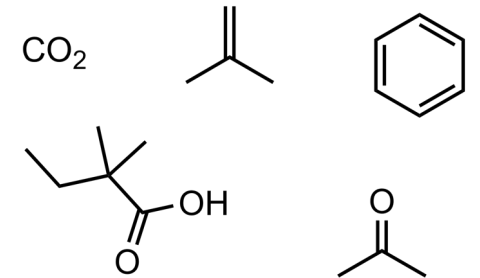
Phase 1: EUV exposure



Phase 2: Post-exposure cascade



Network products include:

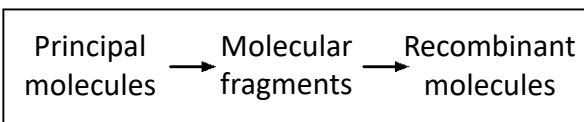


RNMC

- +92 eV “energy budget”
- Explicit free electron species

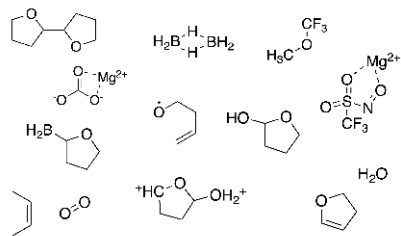
# Recap: The Steps of Building and Analyzing a CRN

## 1. Species generation



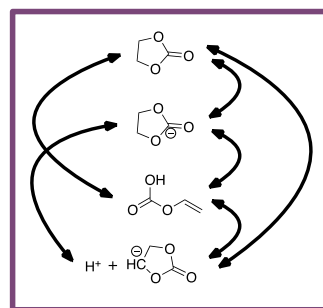
Species Enumeration

High-throughput DFT

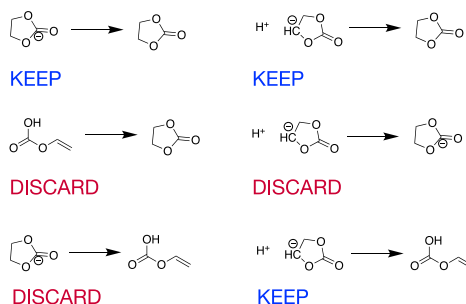


## 2. Reaction generation

Generate reactions by stoichiometry

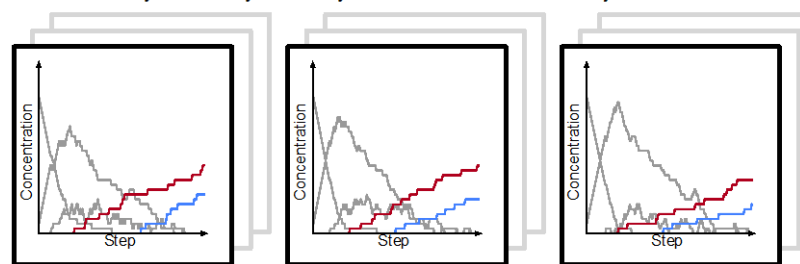


Filter reactions

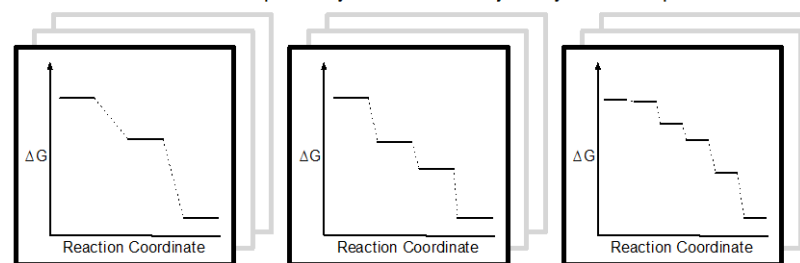


## 3. Pathway sampling

Perform many thermodynamically bounded Monte Carlo trajectories

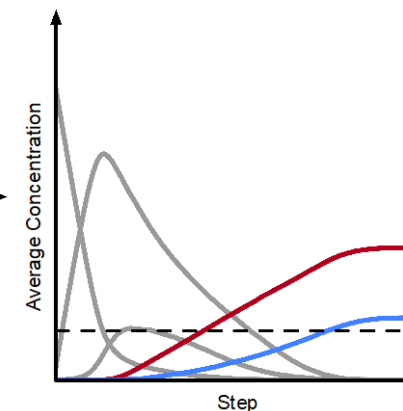


Extract shortest reaction pathways from each trajectory to each specie of interest



Transition state calcs  
Build kinetic models

## 4. Identify Products



High formation / consumption

Significant accumulation

Low-cost pathways available

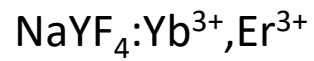
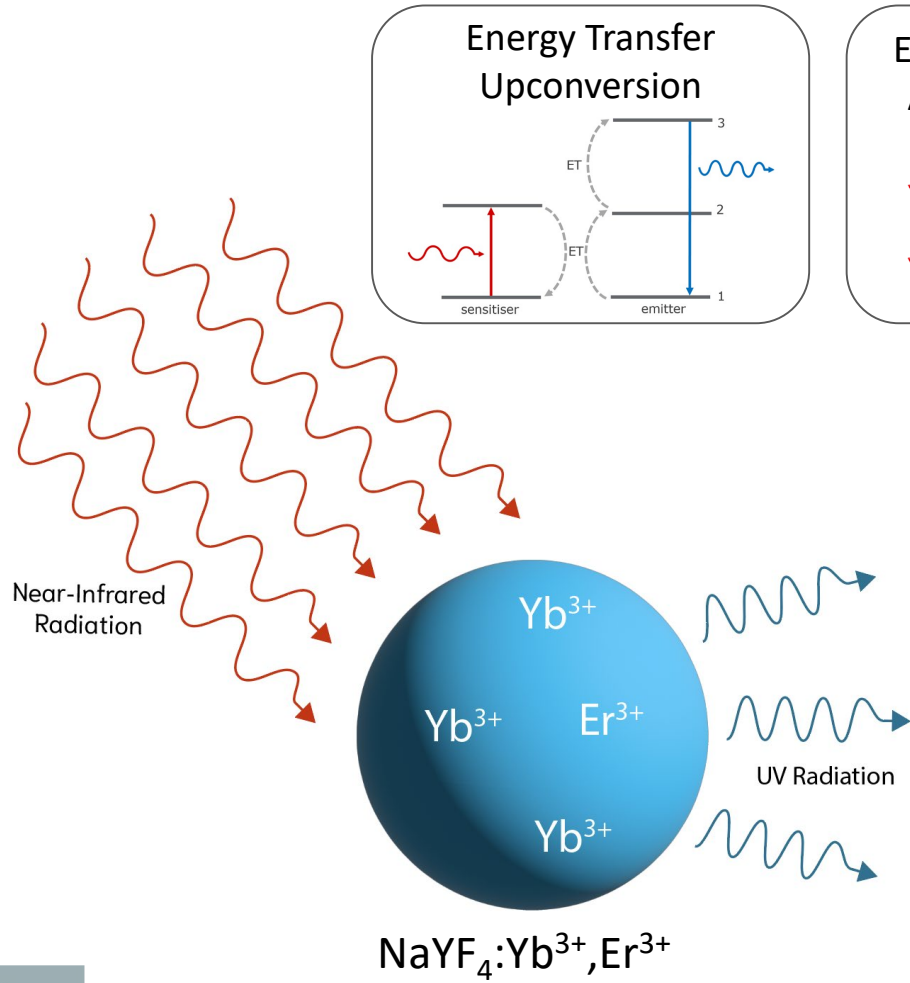
Network product?



Discover novel important species and pathways

Under development: ML-assisted network expansion

# Background: Upconverting Nanoparticles (UCNPs)

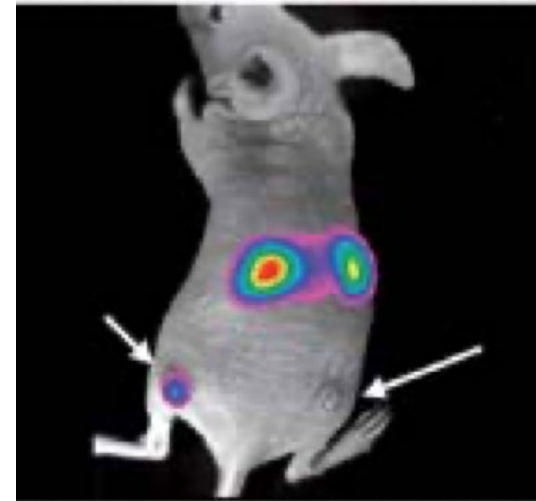


## Security Printing



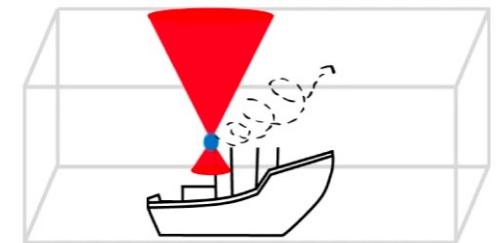
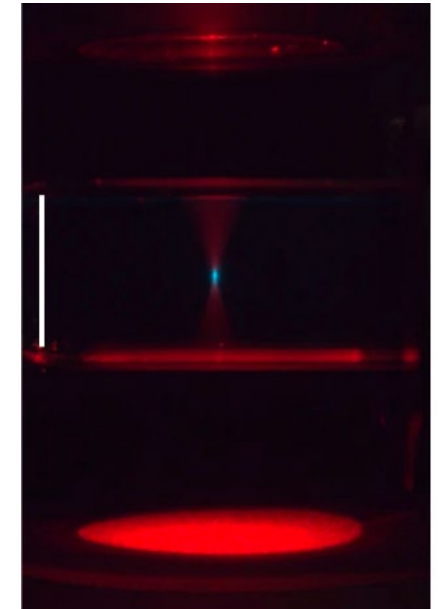
Lu et al. *Nat. Photon.* 2014

## Bio-imaging



Xiong et al. *Anal. Chem.* 2009

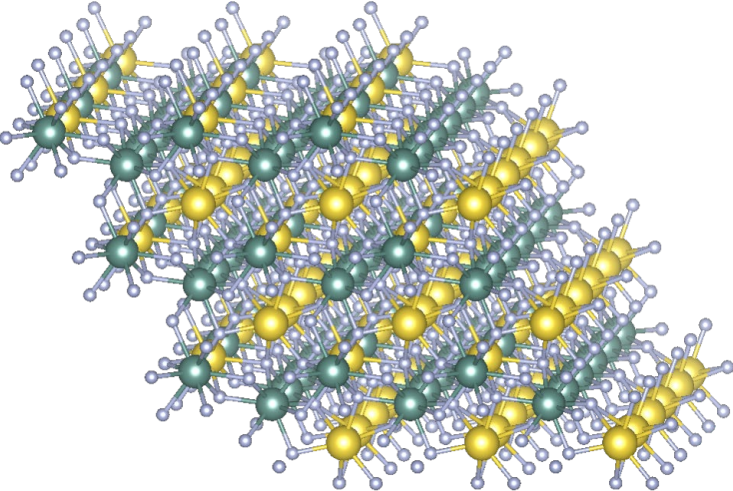
## 3D Printing



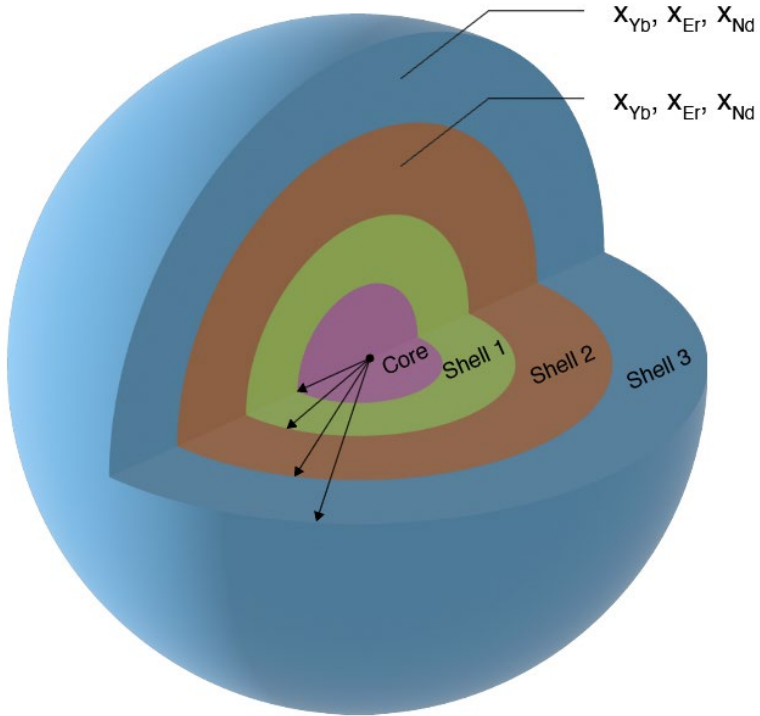
Sanders et al. *Nature* 2022

# UCNP Doping and Heterostructure

Host Material: NaYF<sub>4</sub>



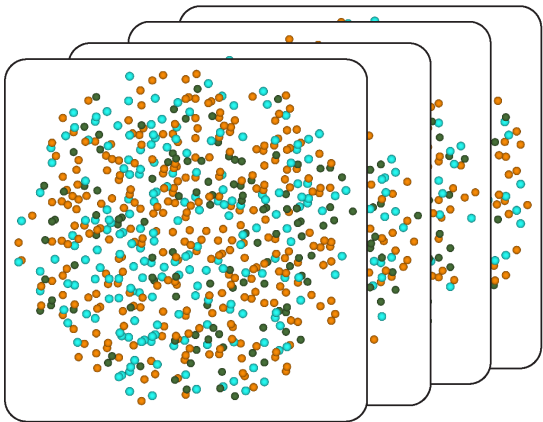
↑ Dope Y<sup>3+</sup> sites with Ln<sup>3+</sup>



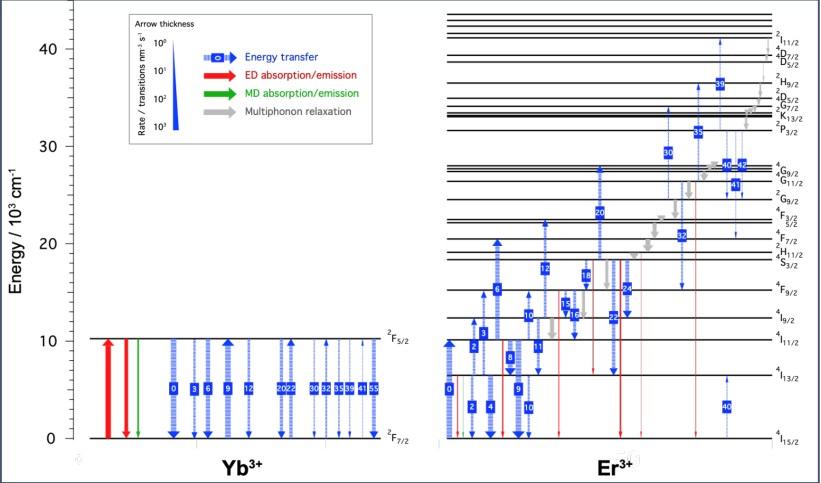
58	59	60	61	62	63	64	65	66	67	68	69	70
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb

# UCNP Photophysics Can Be Simulated With kMC

Generate ensemble of randomly doped structures



Transition rate constants



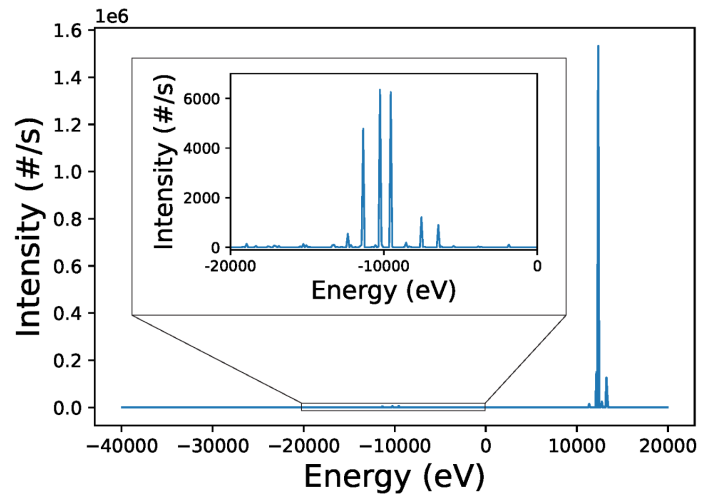
Teitelboim et al. *J. Phys. Chem. C* 2019

Energy Transfer  
Kinetic Monte Carlo (kMC)

[github.com/BlauGroup/NanoParticleTools](https://github.com/BlauGroup/NanoParticleTools)  
[github.com/BlauGroup/NPMC](https://github.com/BlauGroup/NPMC)

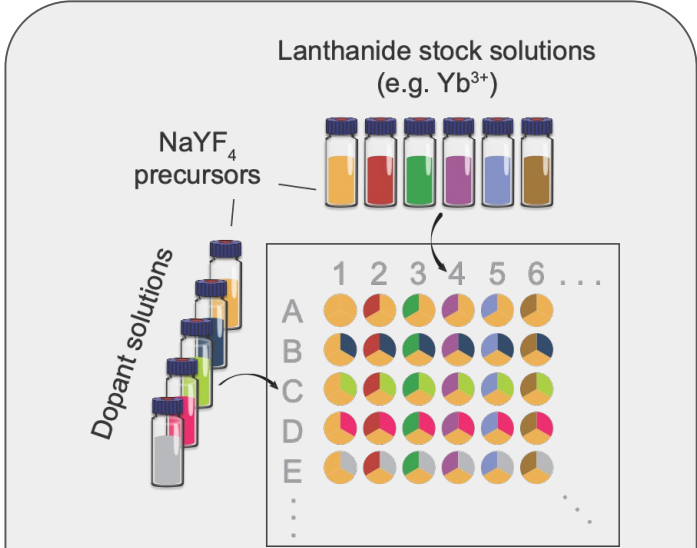
- Simulations require 10-150+ hours on one CPU core
  - Cannot be parallelized

Spectra





# Large Search Space Necessitates Intelligent Searching



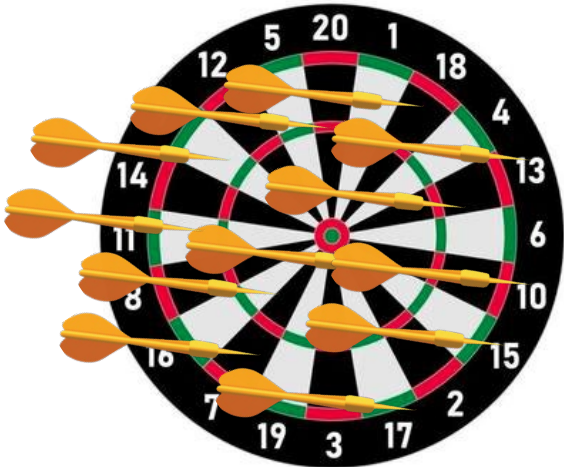
Combinatorial/Robotic Synthesis



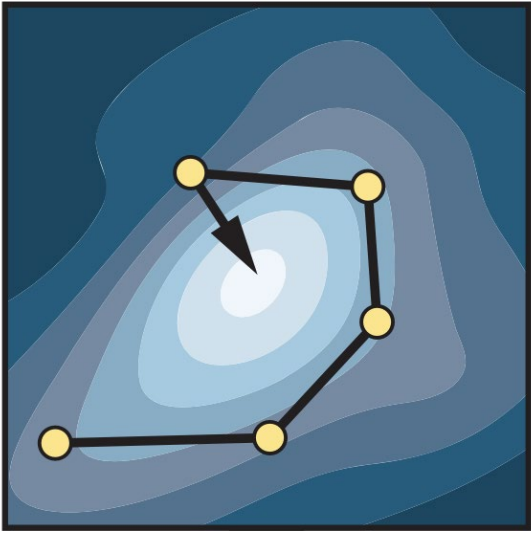
Consider a simple spherical nanoparticle:

- Chose up to 4 dopants (of 13 lanthanides)  
1,093 combinations
- 3 Dopant concentrations - Low, Medium, High  
66,379 dopant configurations
- 5 particle sizes - 4, 6, 8, 10, & 12nm

265,516 nanoparticle configurations

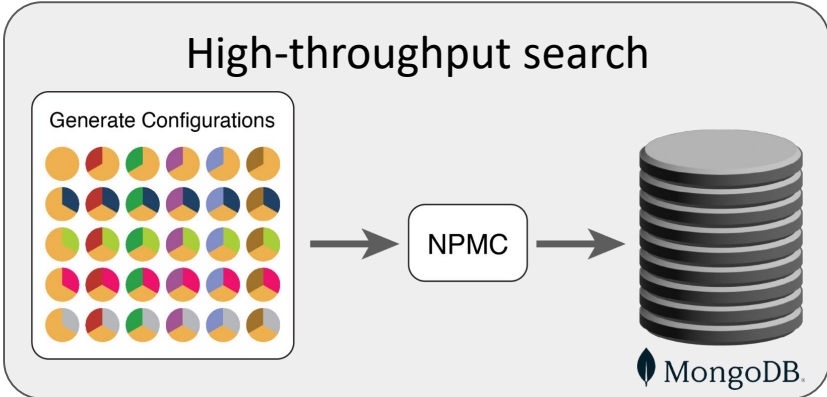


Inverse Design



Sanchez-Lengling et al. *Science* 2018

High-throughput search





# Generating a Dataset for Machine Learning

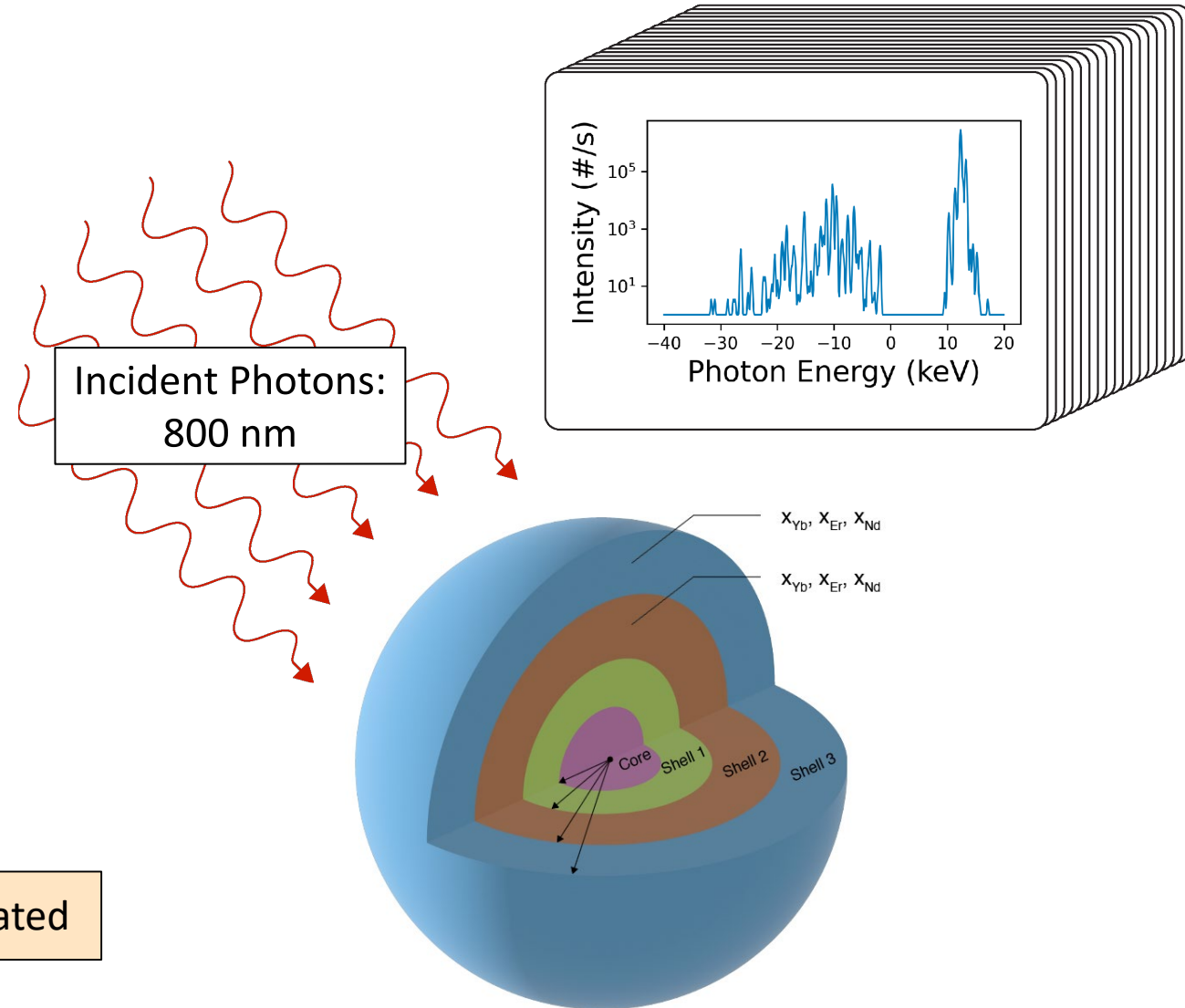
## IID Dataset:

- Up to 8 nm diameter core
- Up to 3 shells
  - Each shell is 1-2.5 nm thick
- Consider only Yb, Er, and Nd dopants

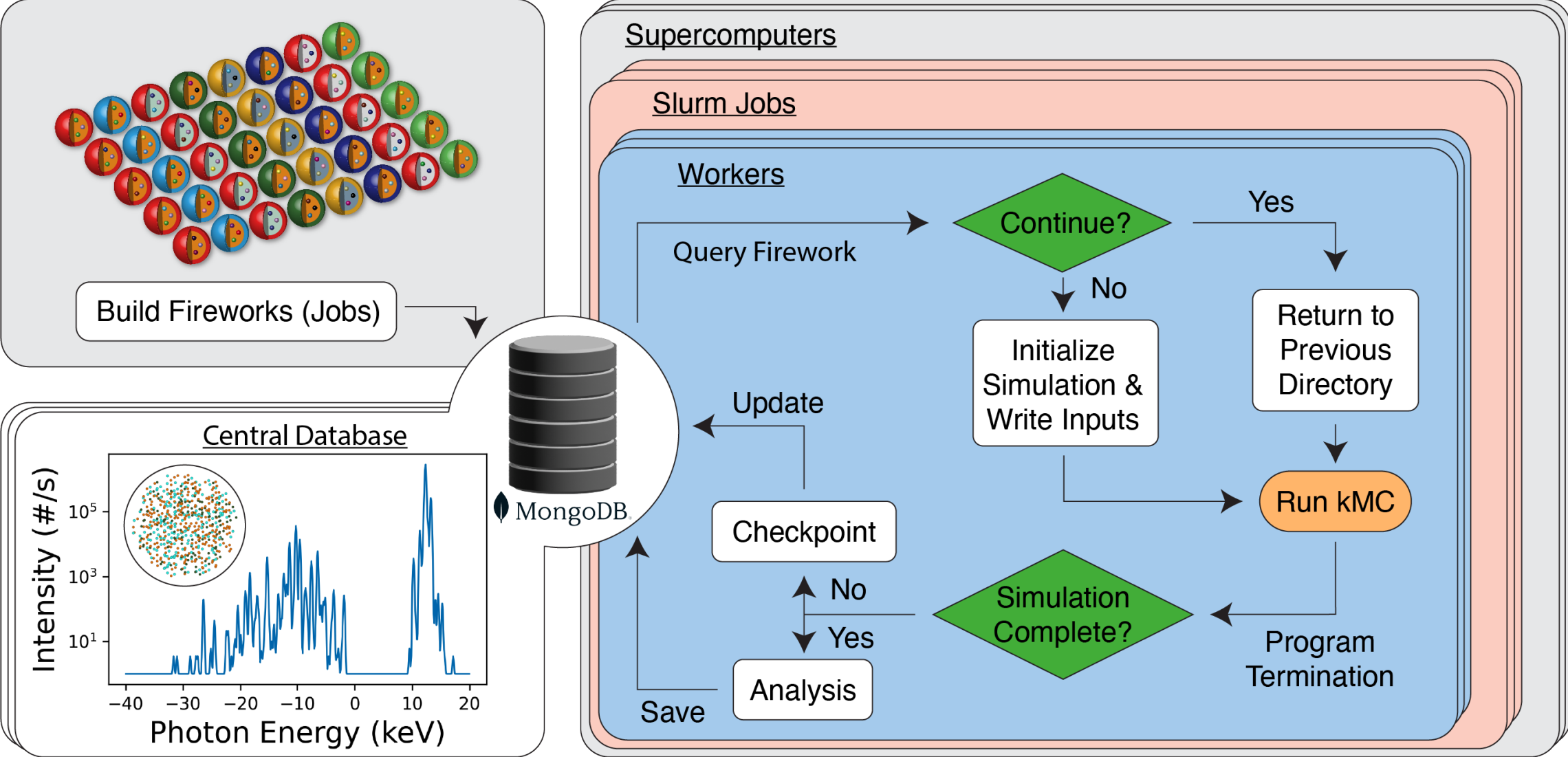
## OOD Testing Dataset:

- Up to 8 nm diameter core
- 4 shells
  - Each shell is 1-2.5 nm thick
- Consider only Yb, Er, and Nd dopants

>6,000 nanoparticle configurations/spectra simulated

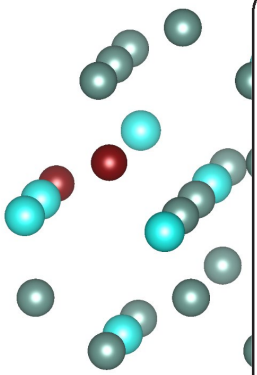
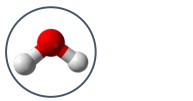


# UCNP kinetic Monte Carlo Simulation Workflow

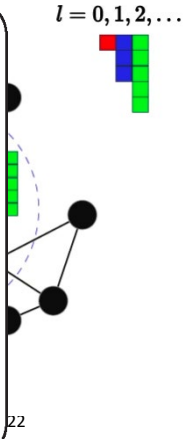


# Representations of Nanoparticles for Machine Learning

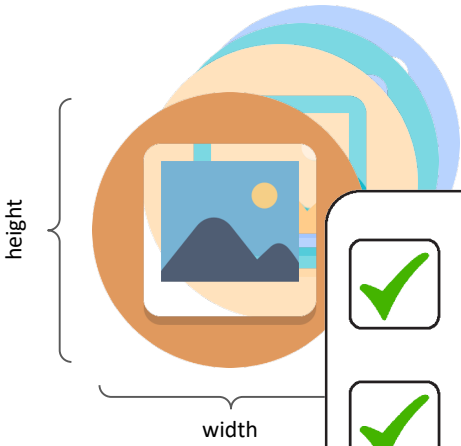
## Atomistic Representation



- Prediction Accuracy and Generalizability
- Gradients w.r.t dopant conc.
- Gradients w.r.t layer radii



## Image Representation



- Prediction Accuracy and Generalizability
- Gradients w.r.t dopant conc.
- Gradients w.r.t layer radii

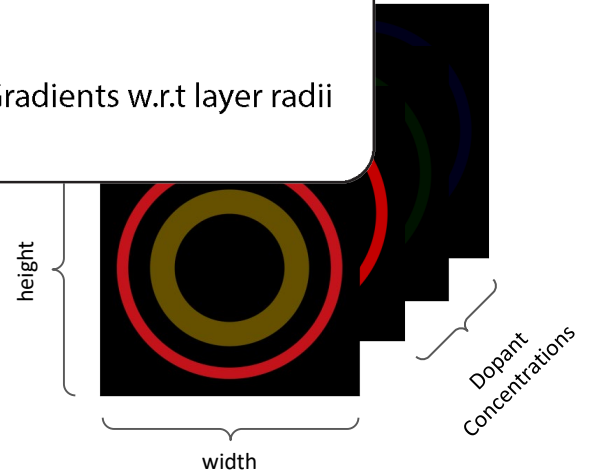
## Tabular Representation



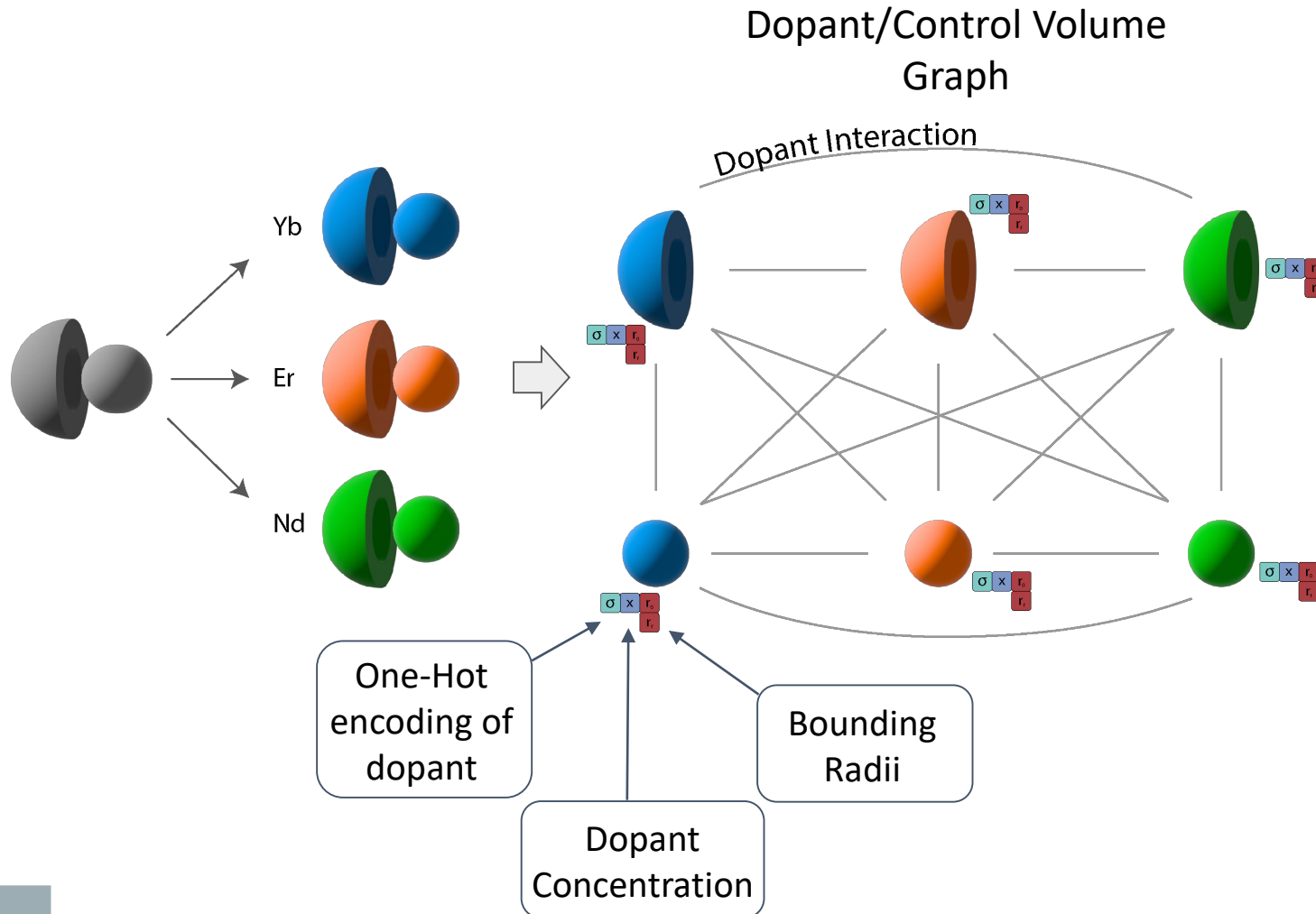
$r_0$	$V_0$	$x_{0,Yb}$	
Core features			

- Prediction Accuracy and Generalizability
- Gradients w.r.t dopant conc.
- Gradients w.r.t layer radii

$x_{n,Yb}$	$x_{n,Er}$	$x_{n,Nd}$
Layer features		

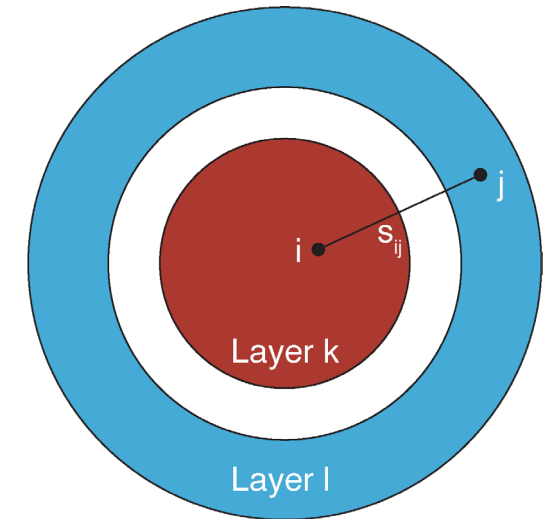


# Developing a Physics-Infused Graph Representation



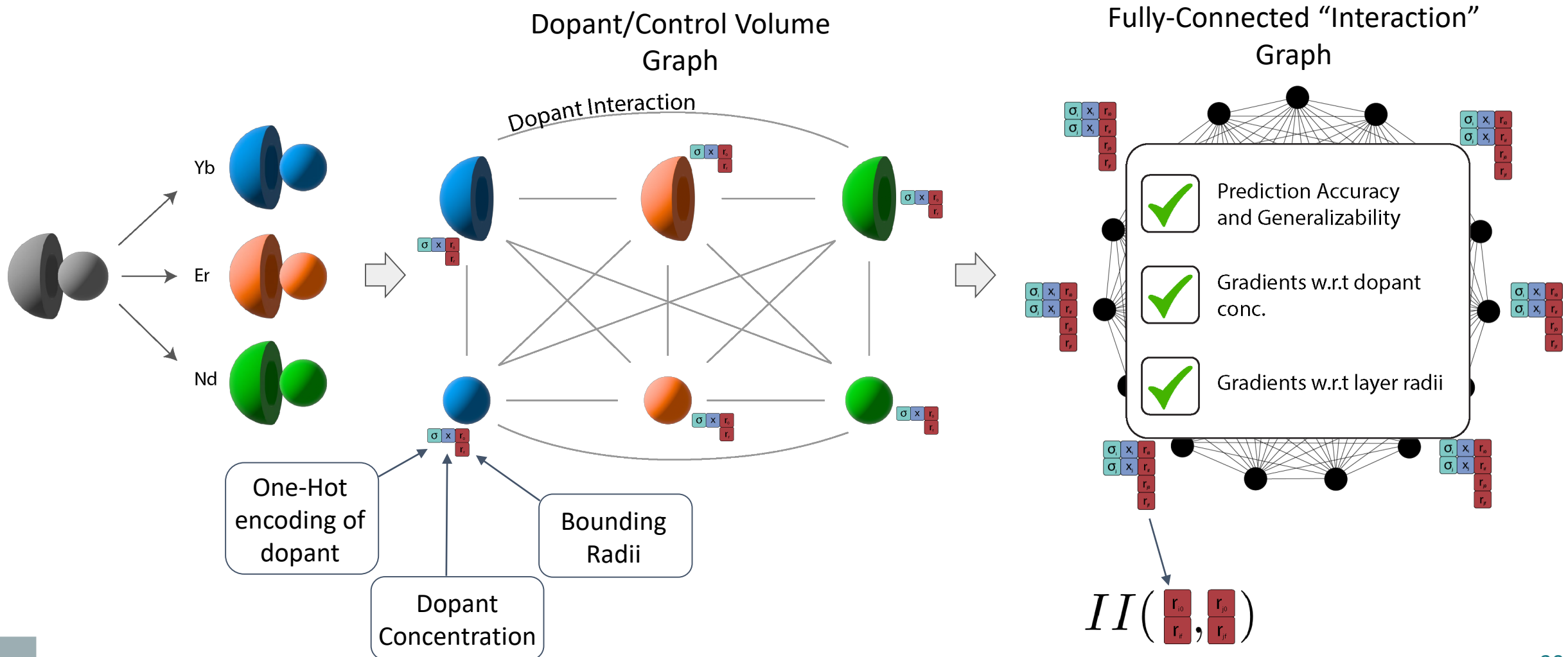
Edge feature - Integrated Interaction

$$I_{ij} = \frac{1}{\sigma\sqrt{2\pi}} e^{-1/2\frac{s_{ij}^2}{\sigma^2}}$$

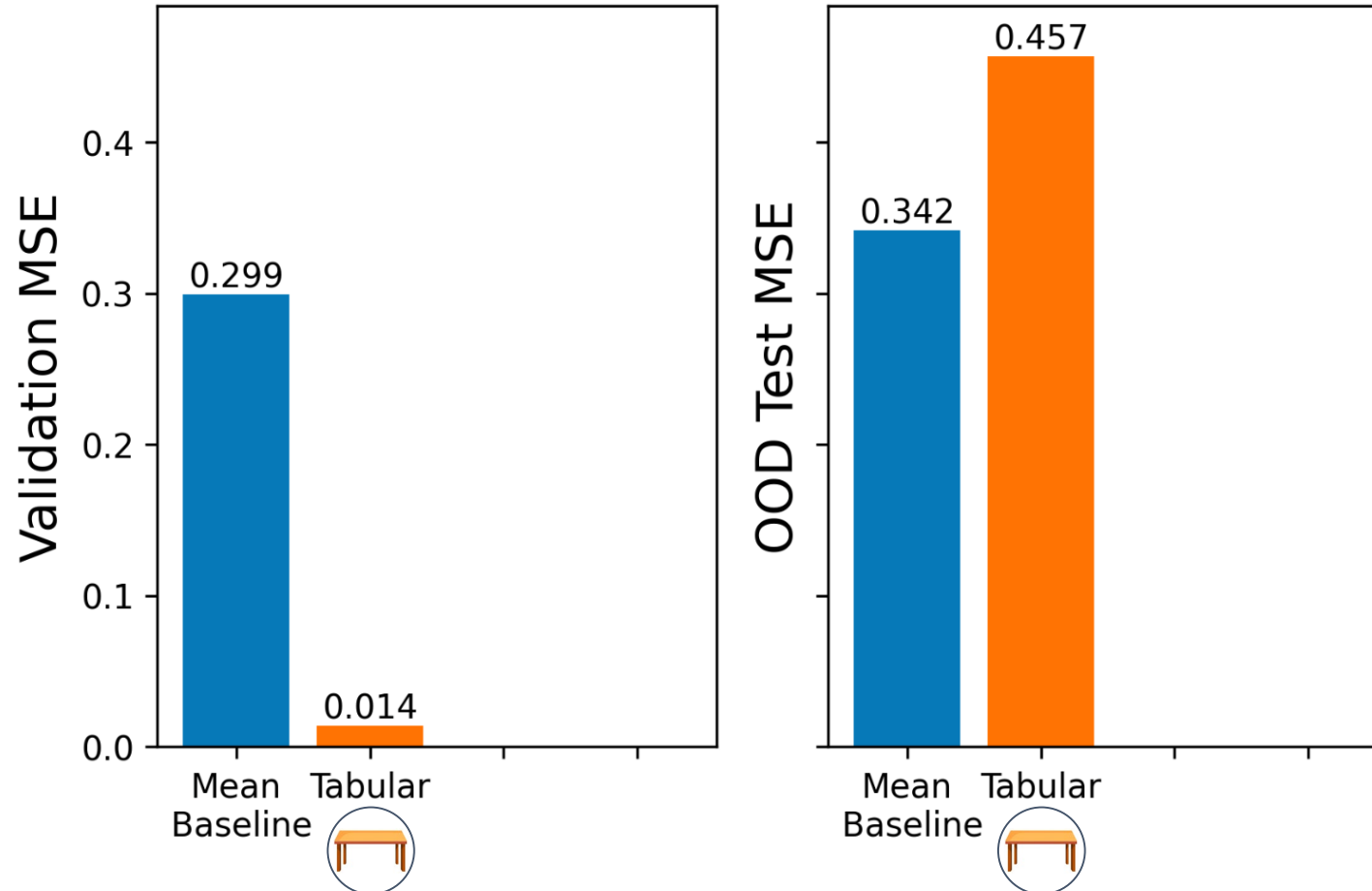


$$II\left(\begin{matrix} r_{i0} & r_{i1} \\ r_{i2} & r_{i3} \end{matrix}, \begin{matrix} r_{j0} & r_{j1} \\ r_{j2} & r_{j3} \end{matrix}\right) = \int \int I_{ij} dV_k dV_l$$

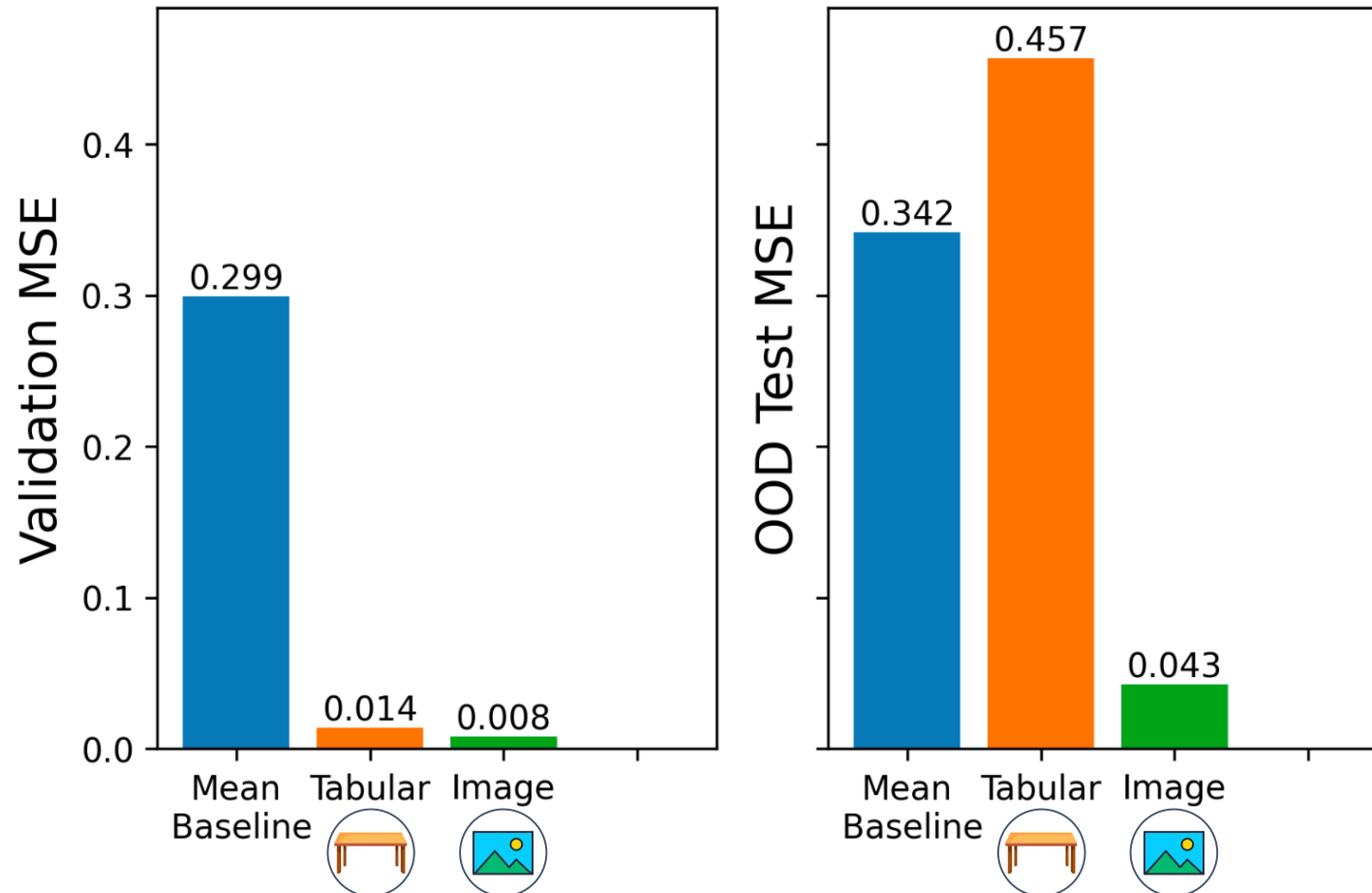
# Developing a Physics-Infused Graph Representation



# Comparing Tabular vs. Image vs. Graph Rep. Performance

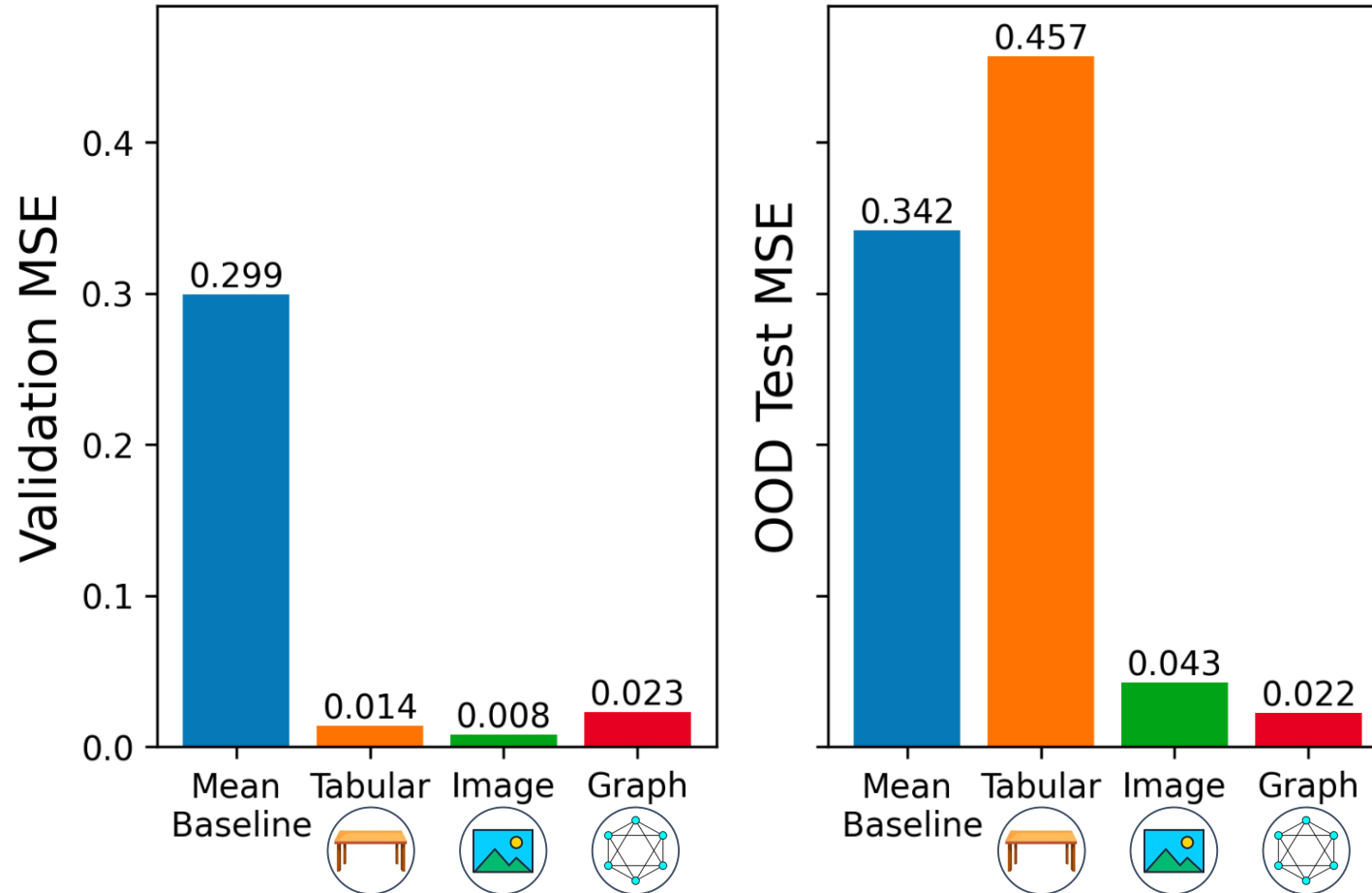


# Comparing Tabular vs. Image vs. Graph Rep. Performance

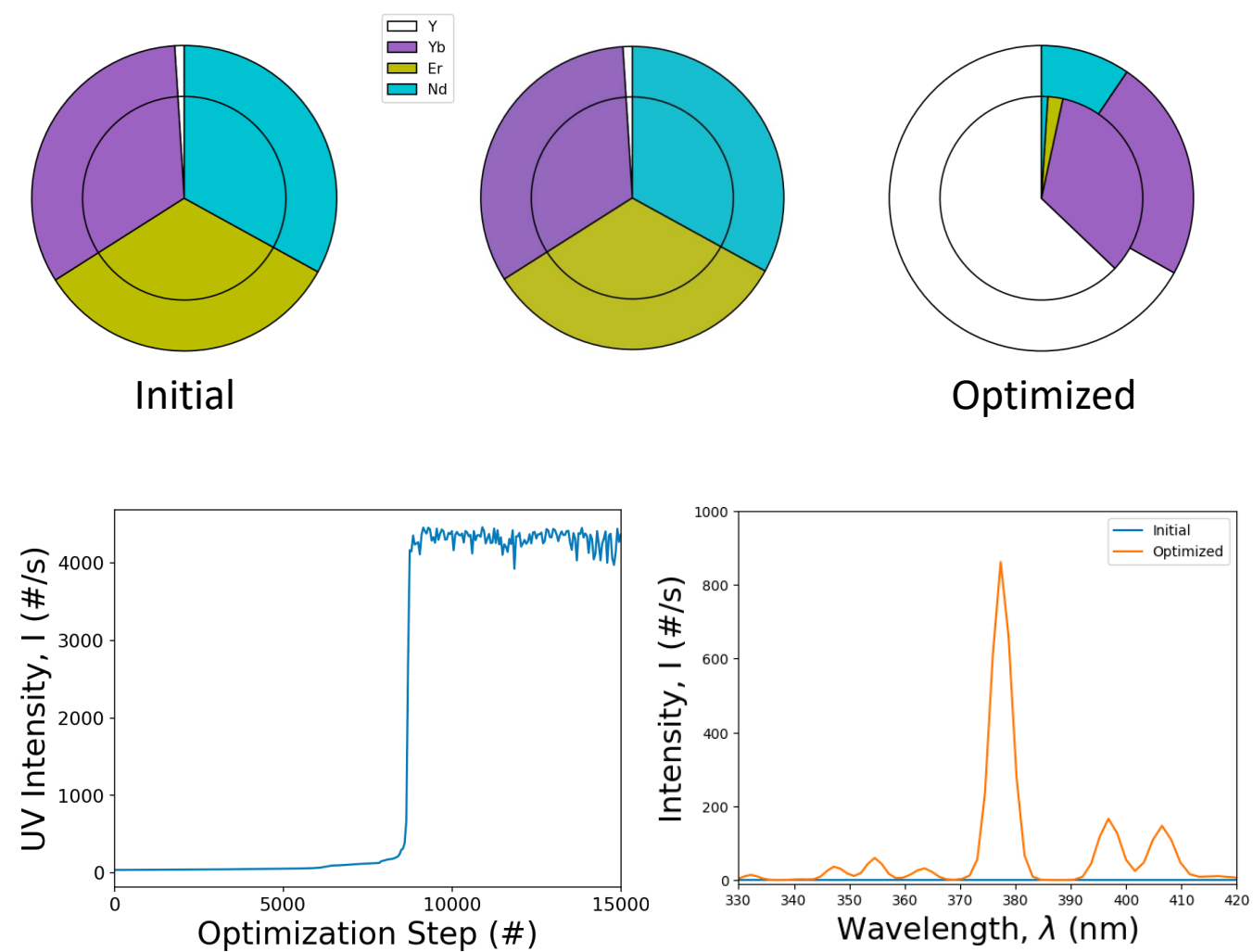
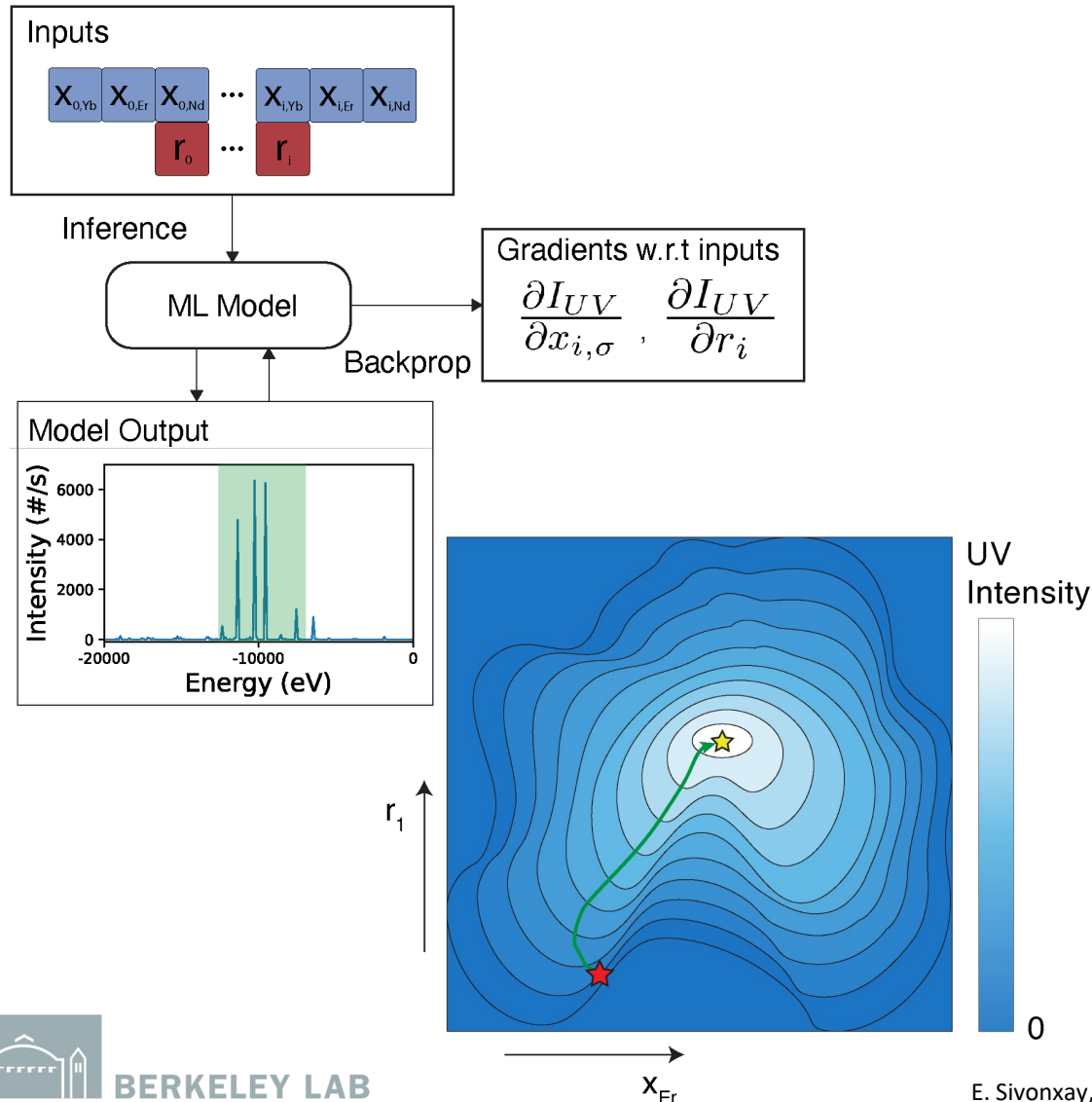




# Comparing Tabular vs. Image vs. Graph Rep. Performance



# Inverse Design of Nanoparticles Via Gradient Ascent

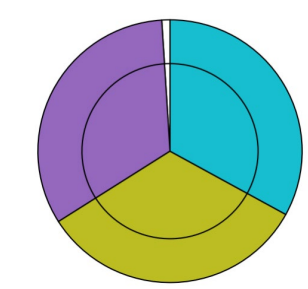
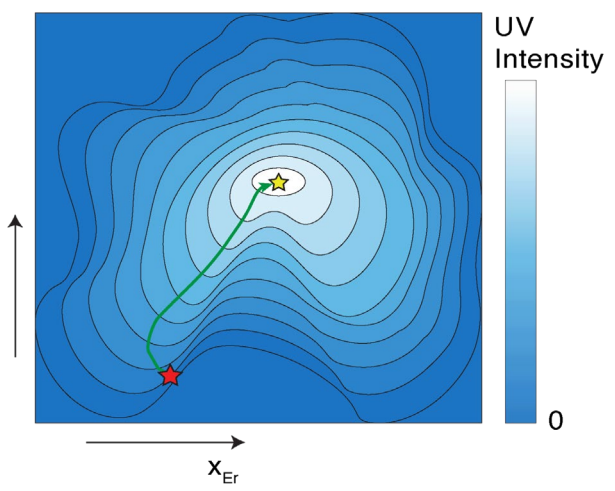
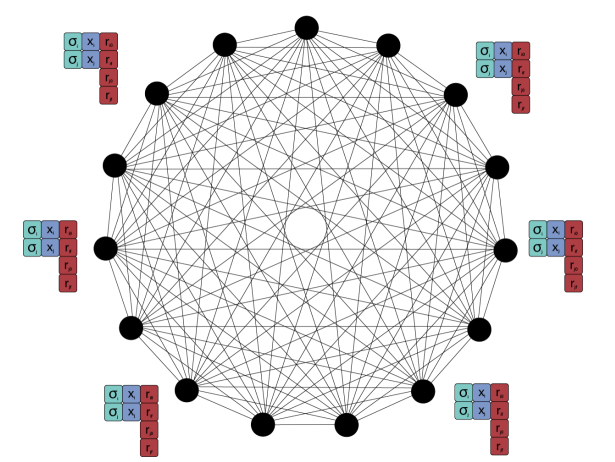
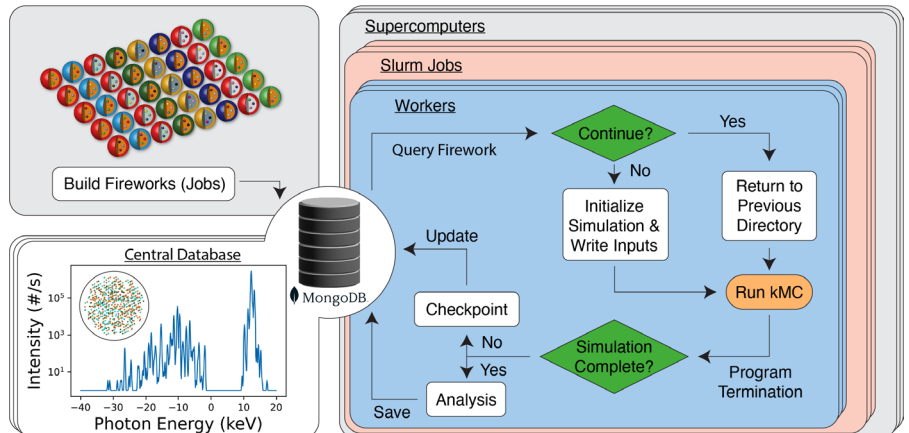
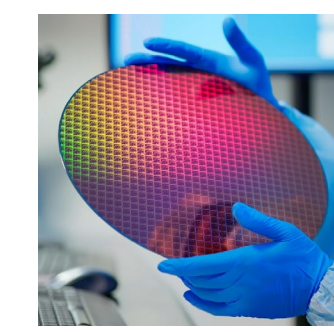
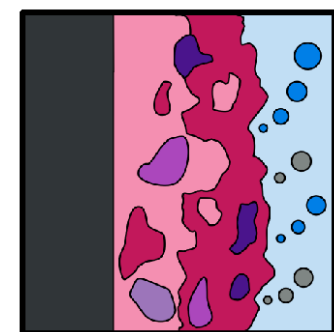
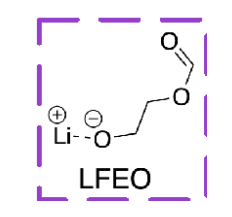
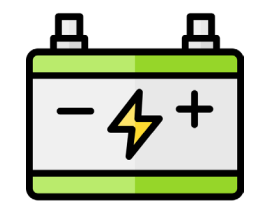
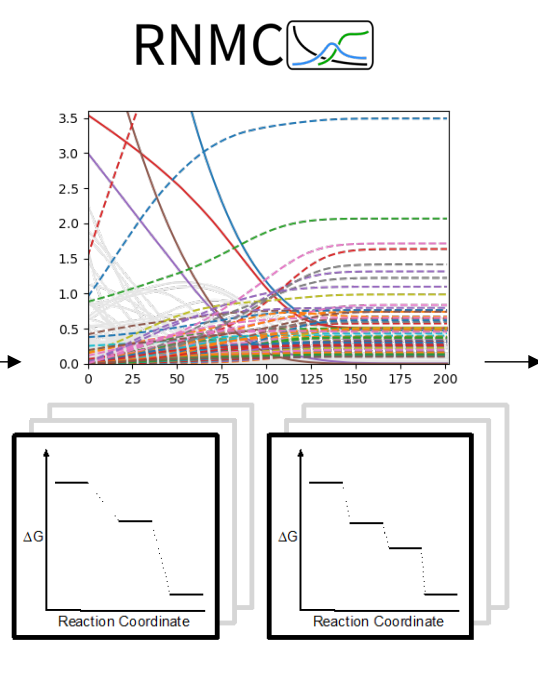
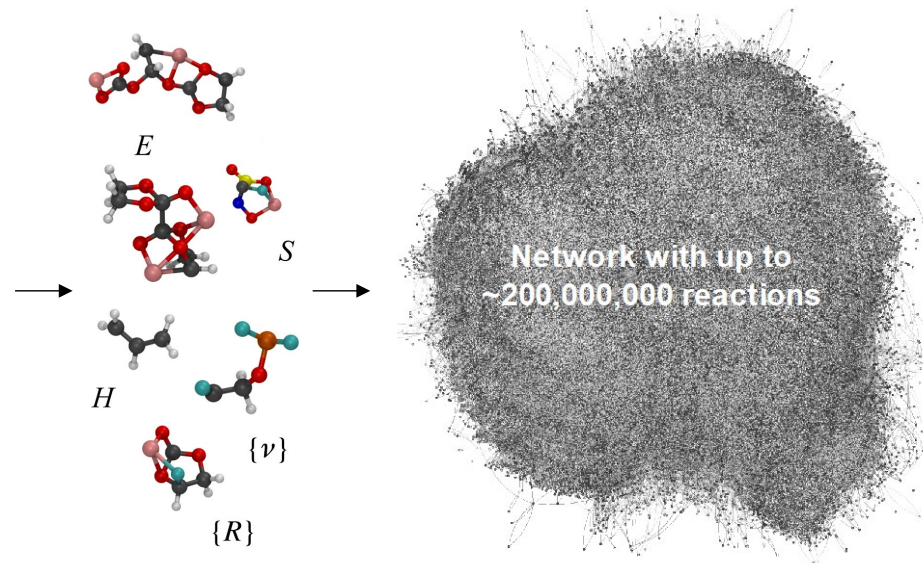


# Summary



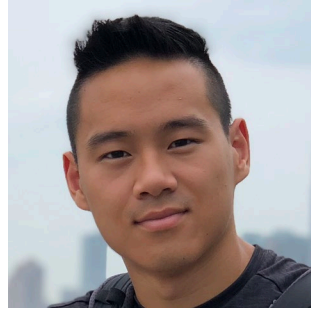
# Acknowledgements



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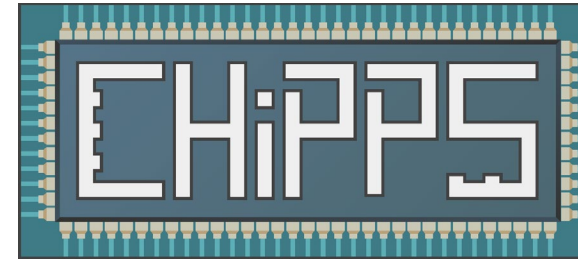
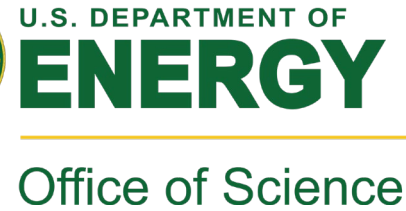
Frances Houle



Kristin Persson



Emory Chan



Center for High Precision Patterning Science

