



Material Surfaces, Grain Boundaries and Interfaces: Structure-Property Relationship Predictions

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**Understanding Many-Particle Systems with Machine Learning Tutorials
IPAM, UCLA**

Ti-C Parameterization

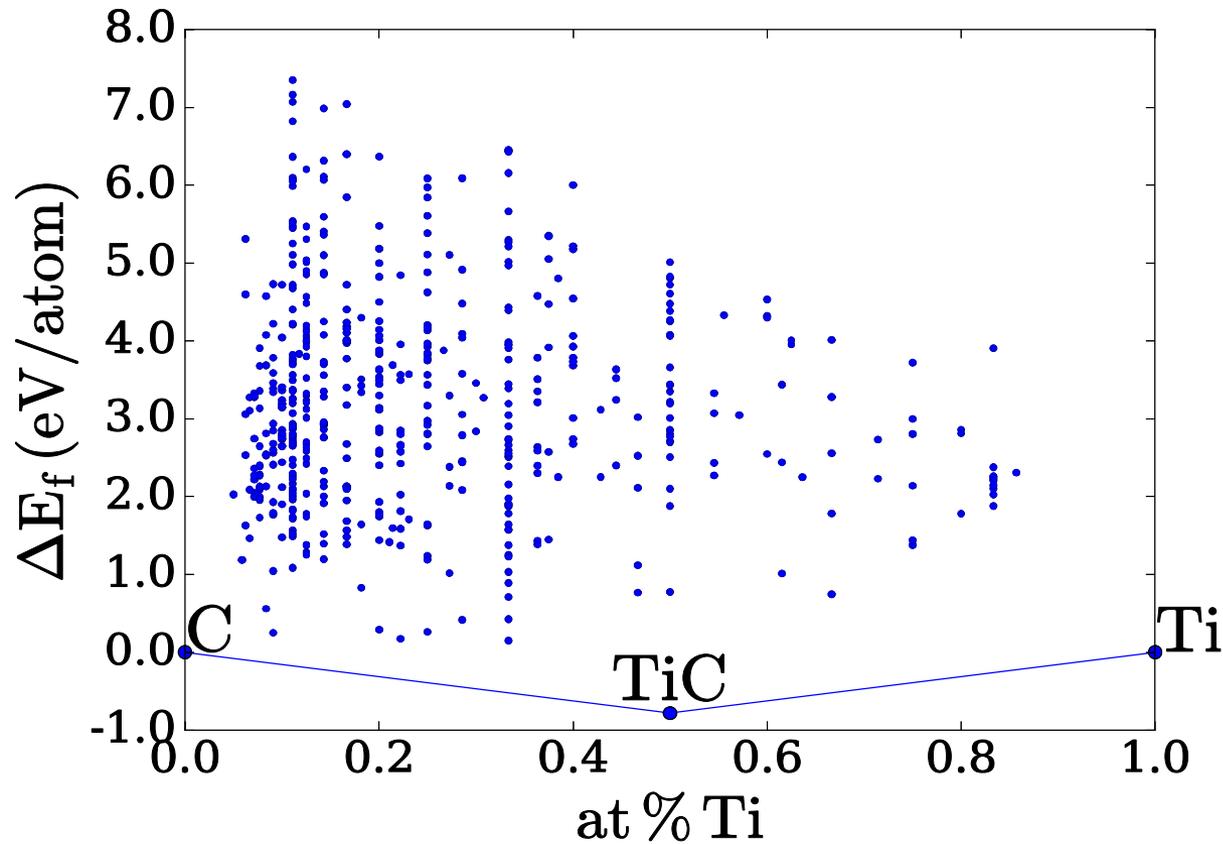
- Parameterize a COMB3 potential for TiC
- Exhibits satisfactory bulk, surface and point defect properties for the ground state structure of bulk TiC
- Also optimize for molecular Ti-C-O-H interactions such as occur in molecular systems such as Ti-(OC₃H₇)₄ or TTIP

- a. J.L. Murray, *OH: ASM International* (1987)
 b. L.F.S. Dumitrescu LFS, *Z. Metallkd* (1999)
 c. G. Simmons, *Cambridge: MIT Press* (1971)
 d. T. Liang et al. (under revision)
 e. A. Arya, *J. Chem. Phys.* (2003)

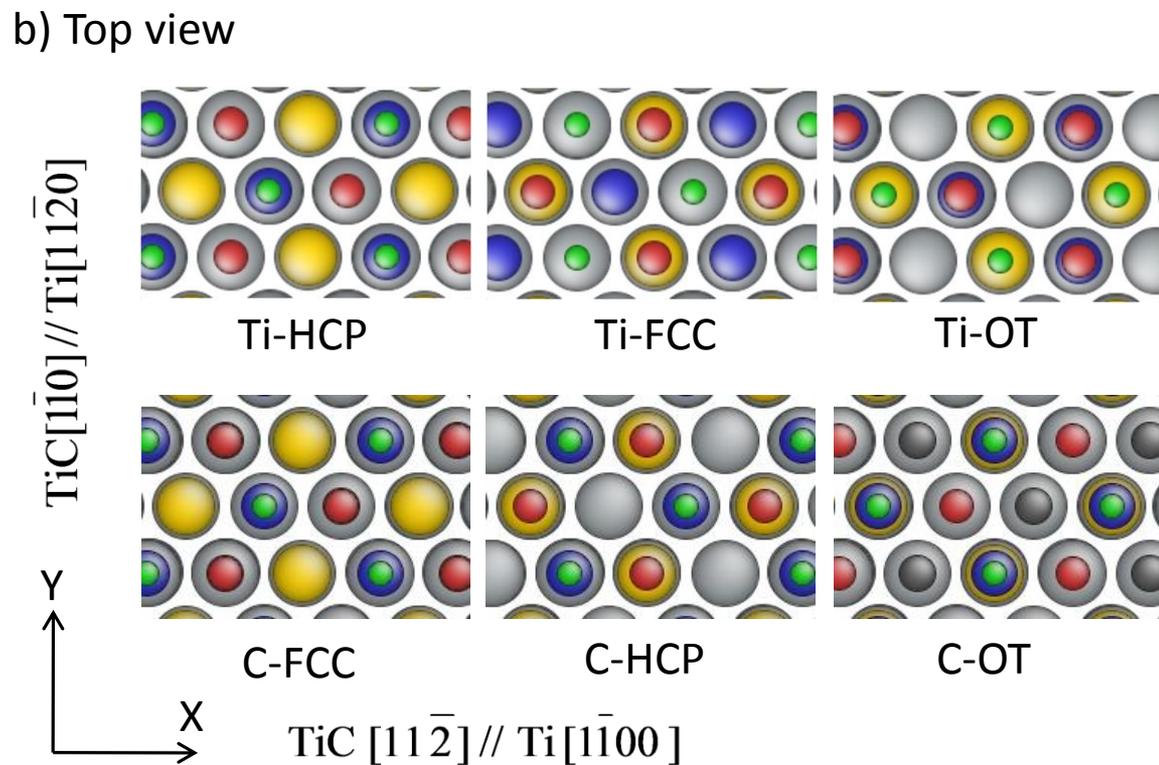
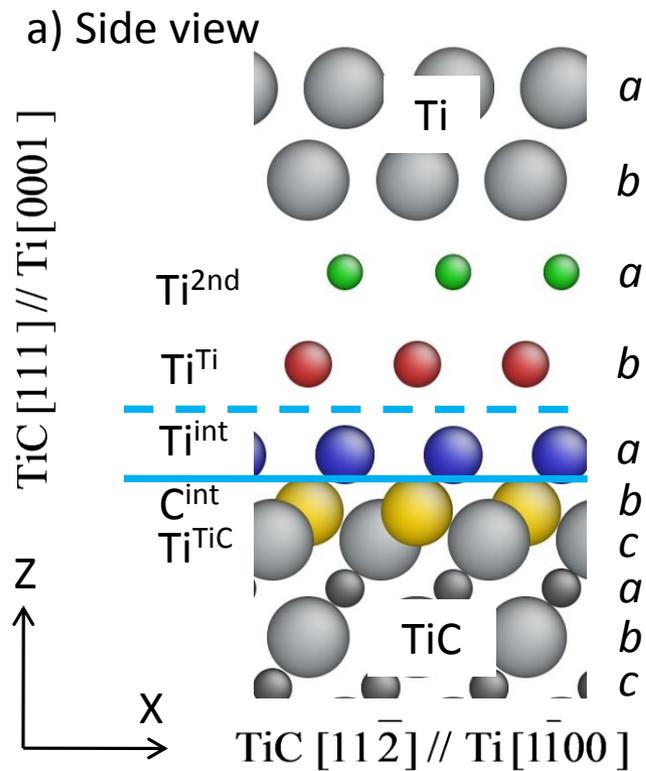
	TARGET	COMB3
a (Å)	4.33 ^a	4.34
ΔH_f (eV)	-1.56 ^b	-1.52
B (GPa)	241 ^c	262
C ₁₁ (GPa)	500 ^c	504
C ₁₂ (GPa)	113 ^c	144
C ₄₄ (GPa)	175 ^c	204

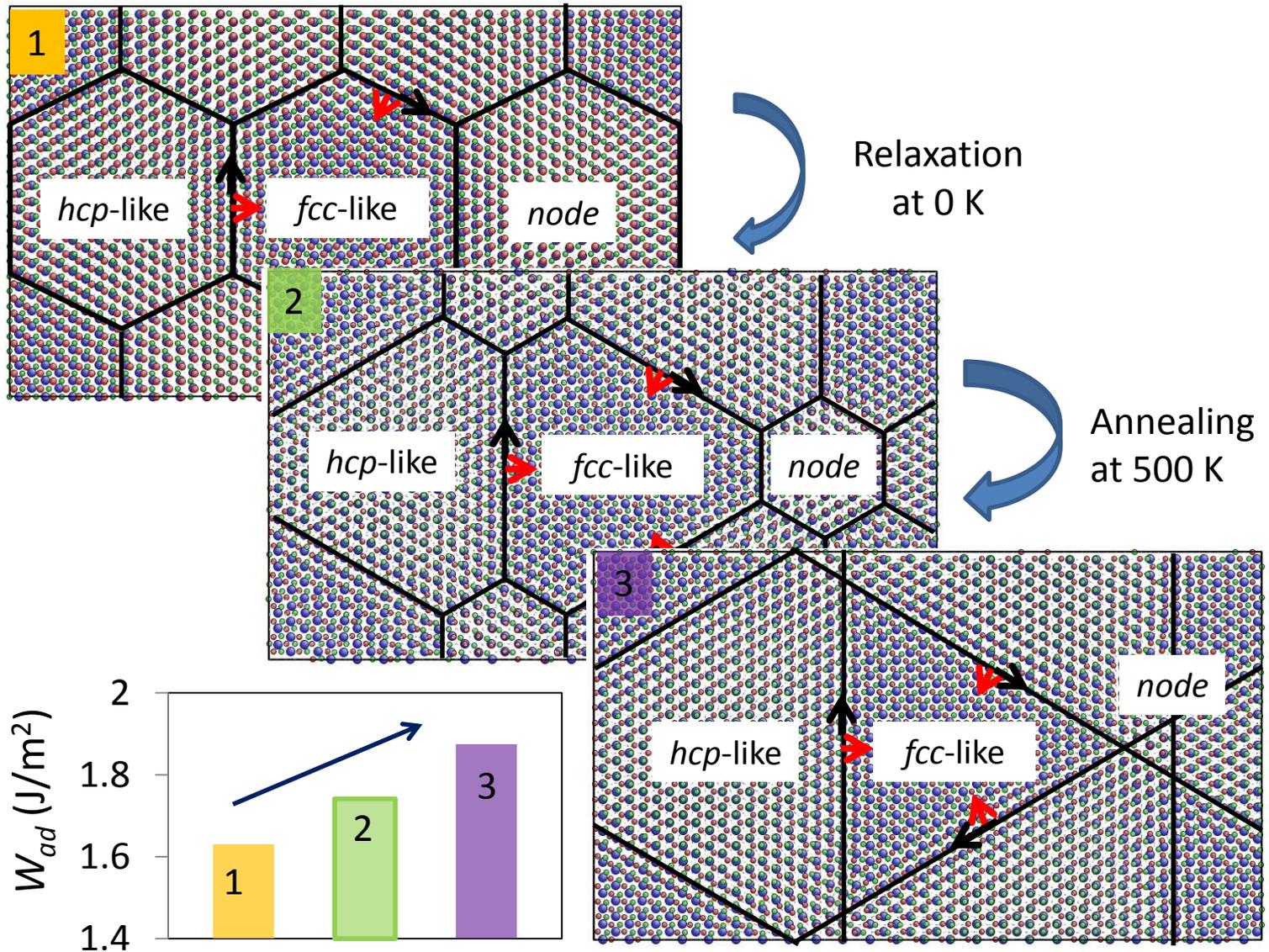
	TARGET	COMB3
V _{Ti} (eV)	14.38 ^d	5.39
V _C (eV)	5.91 ^d	18.45
Ti _i (eV)	12.47 ^d	22.35
C _i (eV)	8.89 ^d	16.16
Y ₍₀₀₁₎ (J/m ²)	2.3 ^e	3.6

Genetic algorithm to investigate predicted phases

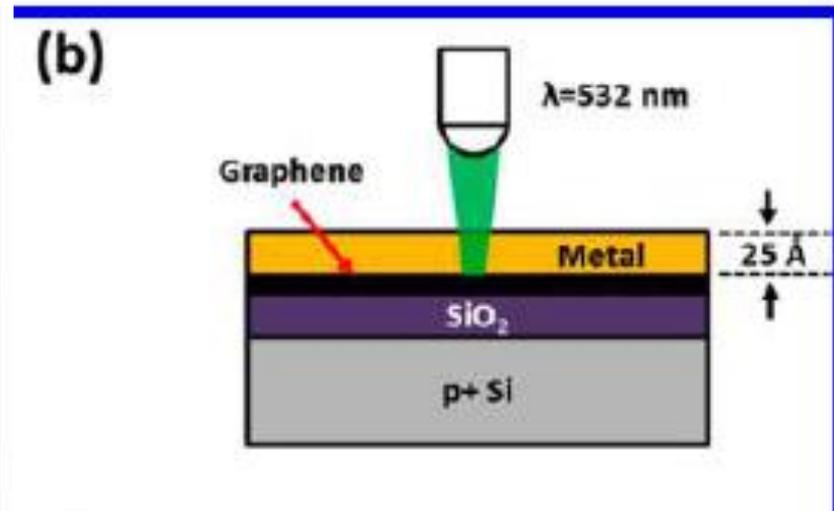
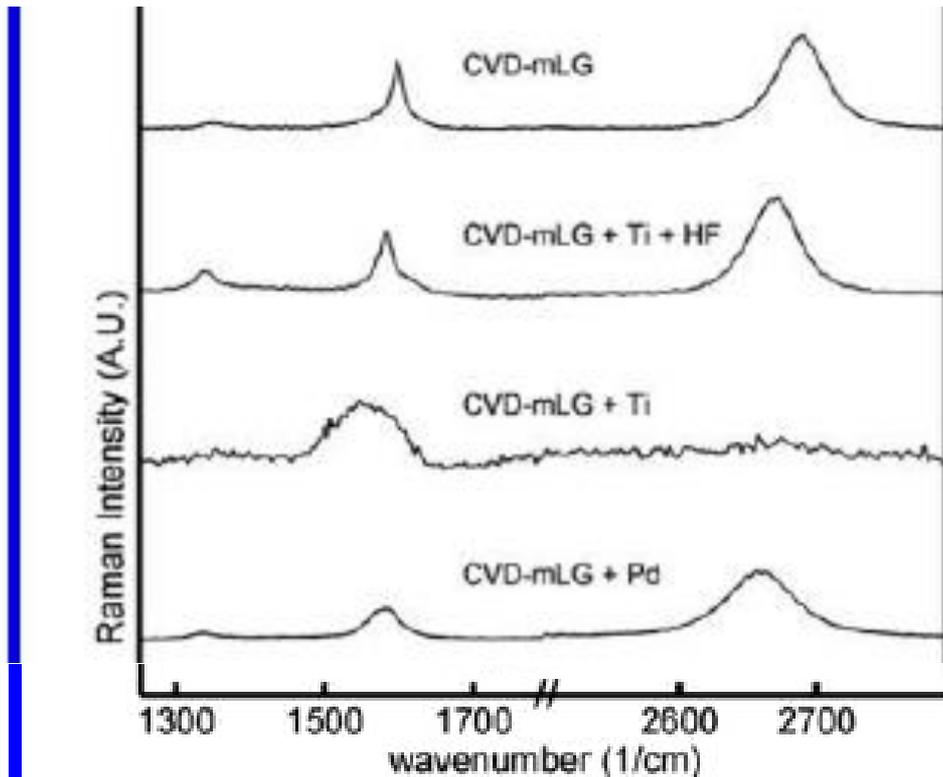


Ti/TiC Interfaces





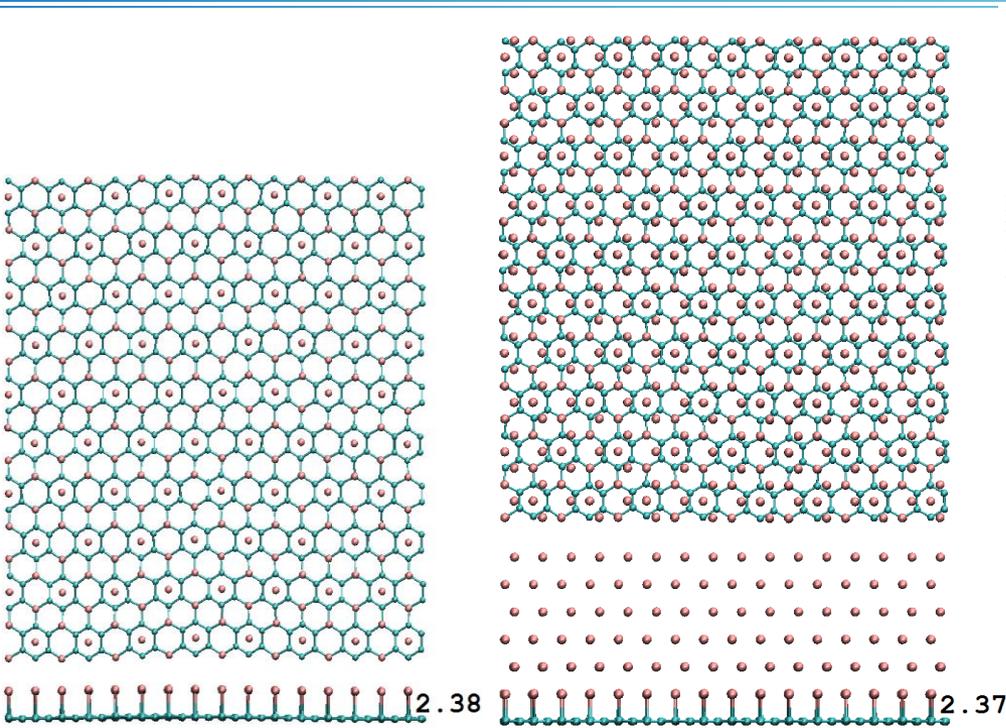
Experimental Results of Ti on Graphene



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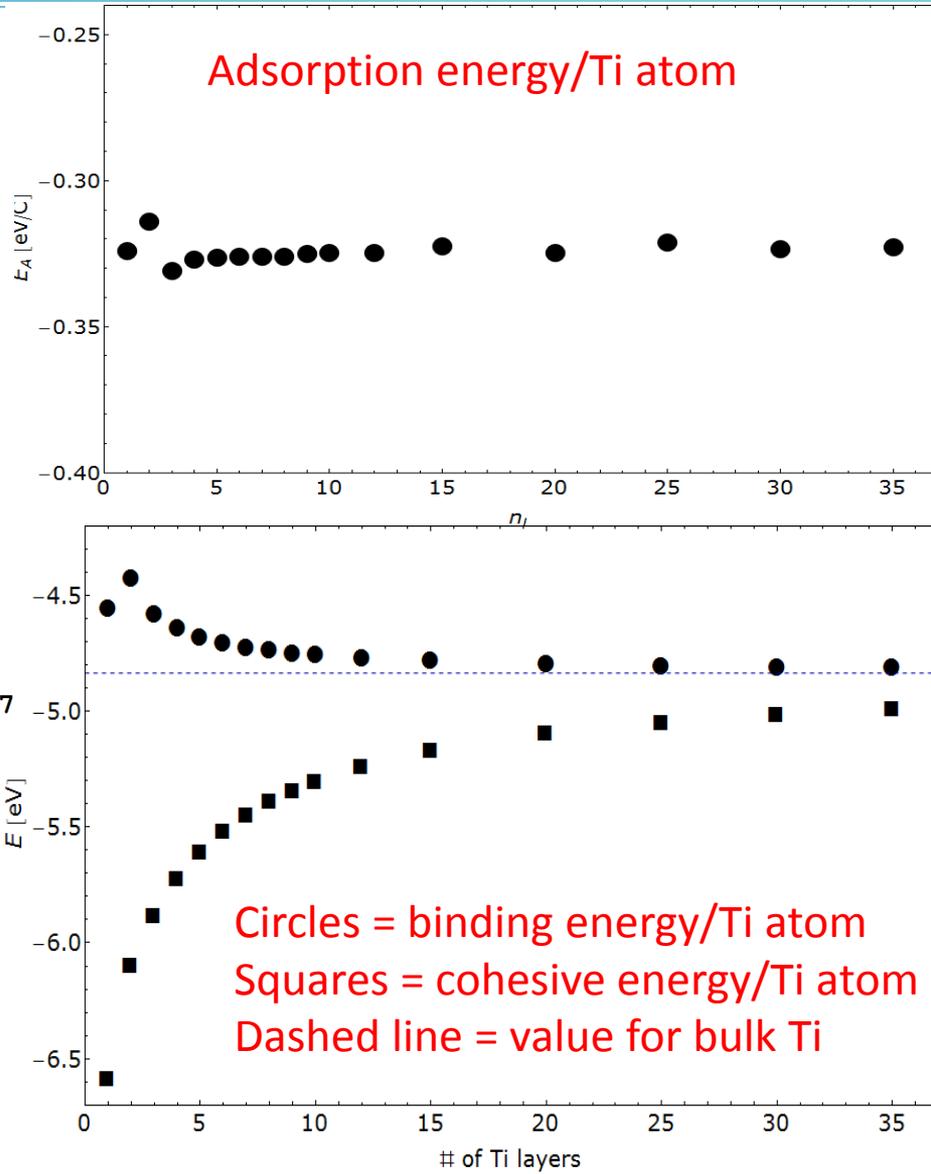
Raman spectra of pure graphene, **graphene after removing Ti film**, Ti film on graphene and Pd film on graphene for comparison. Raman shows that graphene structure remains after removing Ti thin film.

Predicted Interactions of Ti with Graphene



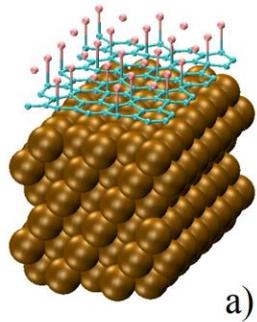
Energies of different Ti thin films on graphene

A. F. Fonseca et al. (in preparation)

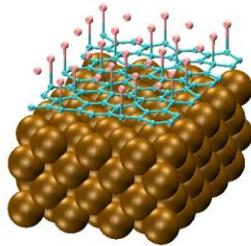


Influence of Substrate on Ti/Graphene Adsorption

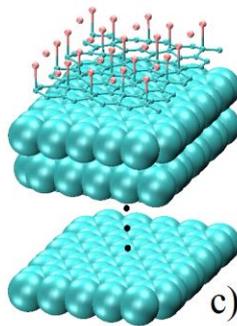
substrate	none	Graphene	Cu (111)	Cu (100)	Cu ₂ O:Cu (110)	Cu ₂ O:CuO (110)	Anatase Ti ₂ O (101)
E_A [eV/C]	-0.318	-0.3269	-0.4579	-0.4573	-0.5194	-0.4543	-0.0433
ΔE_A [eV/C]	0	-0.0089	-0.1399	-0.1393	-0.2014	-0.1363	+0.2747



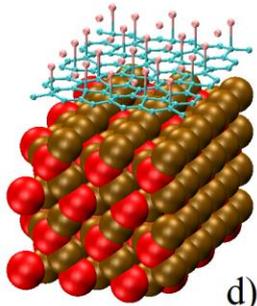
a)



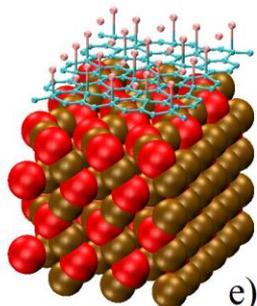
b)



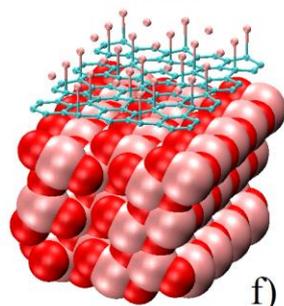
c)



d)



e)



f)

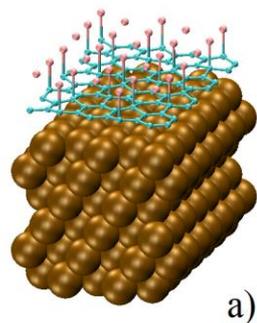
- (a) Cu(111)
- (b) Cu(100)
- (c) Graphene
- (d) Cu₂O:Cu(110)
- (e) Cu₂O: CuO(110)
- (f) Anatase TiO₂ (101)

A. F. Fonseca et al. (in preparation)

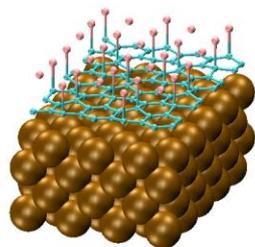
Influence of Substrate on Ti/Graphene Adsorption

Induced charges on the surface (first row) of atoms of the substrate

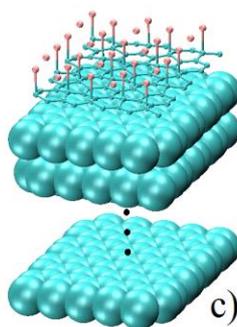
1 layer of graphene	Cu (111)	Cu (100)	Cu ₂ O:Cu (110)	Cu ₂ O:CuO (110)	Anatase TiO ₂ (101)
+ (C)	+ (Cu)	+ (Cu)	+ (Cu)	+ (Cu)	- (O)



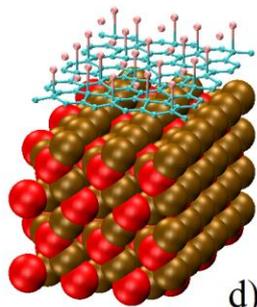
a)



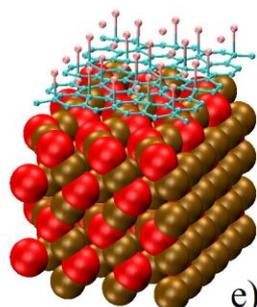
b)



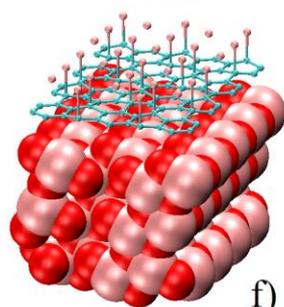
c)



d)



e)



f)

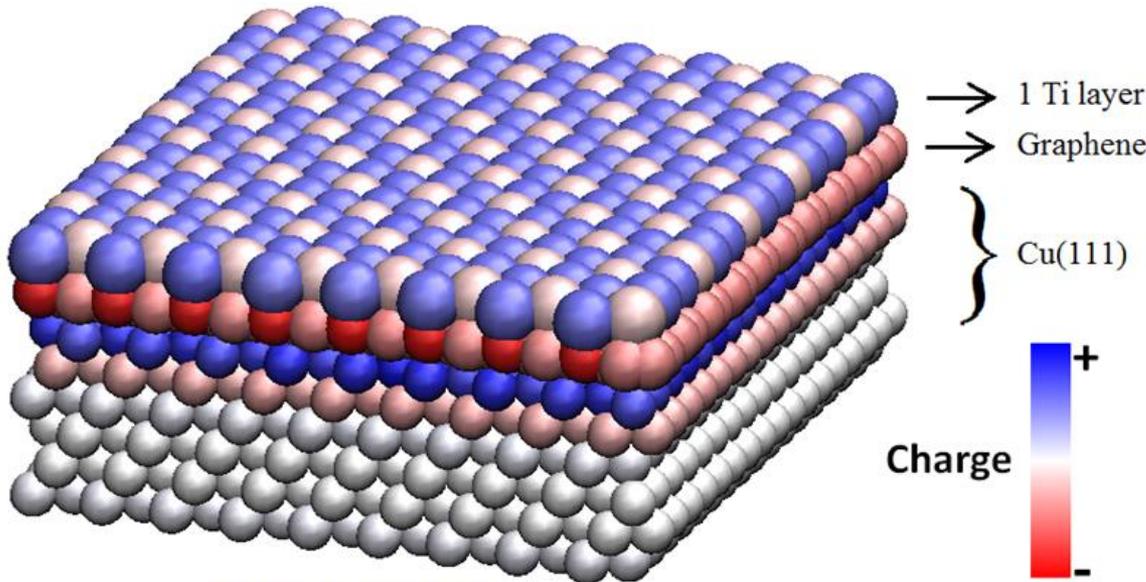
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A. F. Fonseca et al. (in preparation)

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+ (C)	+ (Cu)	+ (Cu)	+ (Cu)	+ (Cu)	- (O)

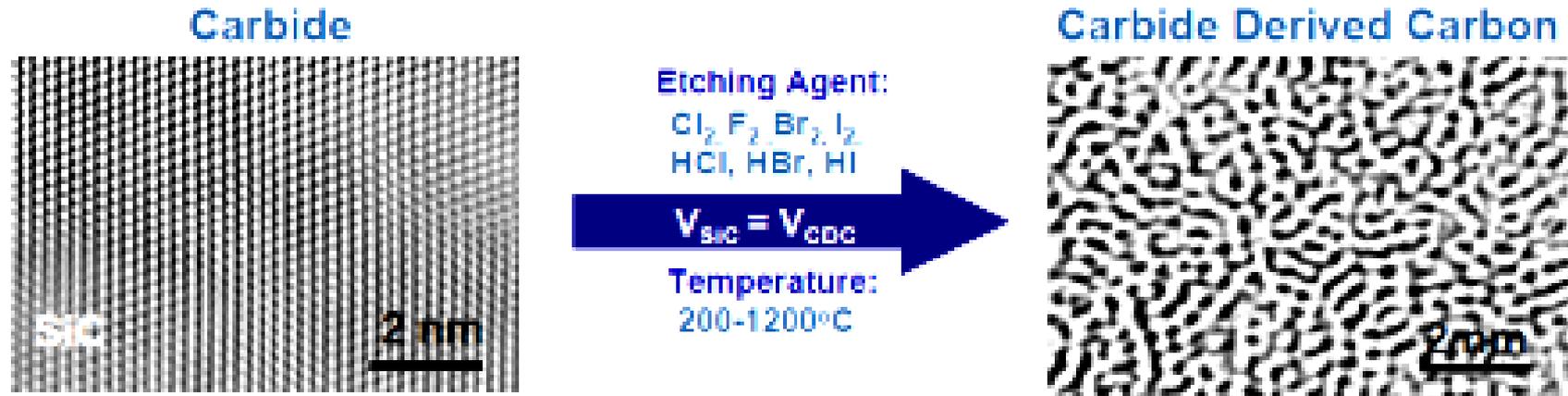


- (a) Cu(111)
- (b) Cu(100)
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- (d) Cu₂O:Cu(110)
- (e) Cu₂O: CuO(110)
- (f) Anatase TiO₂ (101)

Large the **POSITIVE CHARGE** of substrate,
large the **ADHESION** of Ti-graphene on the substrate

A. F. Fonseca et al. (in preparation)

Carbide-Derived Carbon (CDC)

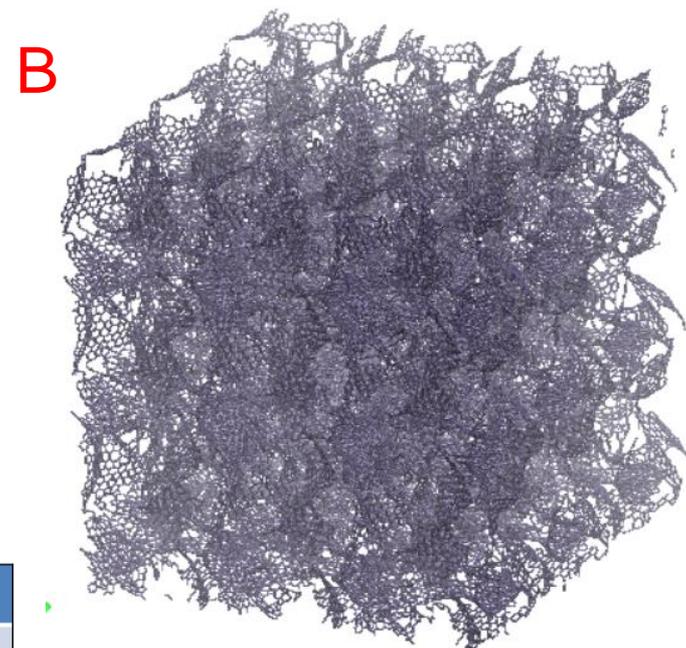
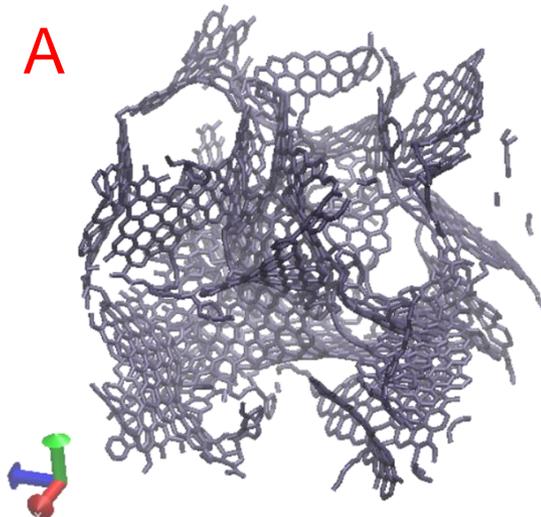


- Carbide precursors:
 SiC , TiC , Al_4C_3 , ZrC
- Etching Agent:
 Cl_2 , F_2 , Br_2 , I_2 , HCl , HBr , HI
- Characteristics:
 Mixture of sp -, sp^2 -, sp^3 -bonded carbons
 Porous
 High surface area

CDC Structure Optimization

- Generated using Hybrid Reverse Monte Carlo simulations (Prof. Suresh Bhatia, University of Queensland)
- Stable after relaxation in MD simulations with the COMB3 potential

CDC model of different sizes
(A) 4 nm
(B) 12 nm



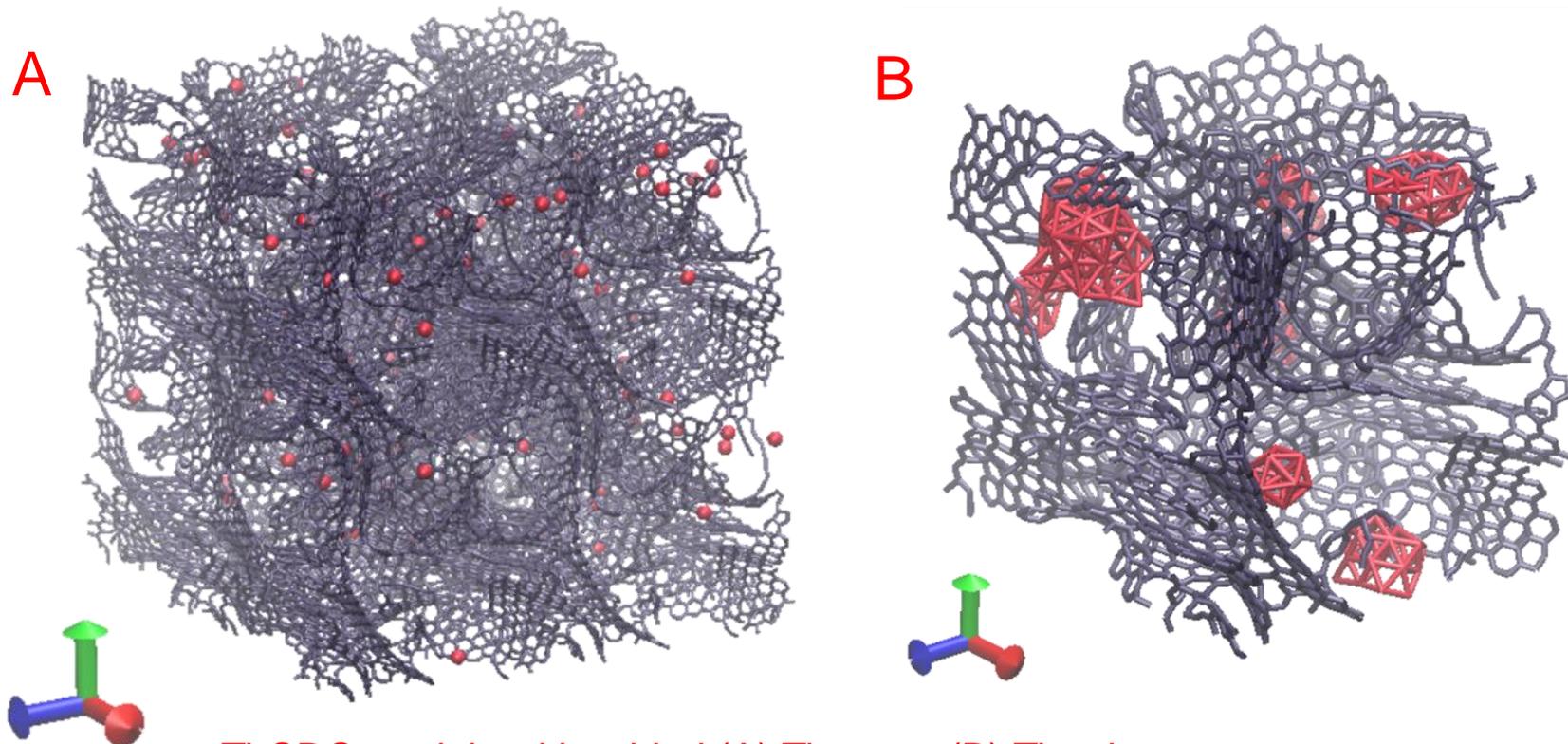
Change of carbon's coordination number (CN) distribution (%)

CN	0	1	2	3	4	5
Initial	0.33	1.32	23.53	74.25	0.59	0
Final	0	0.03	19.99	78.74	1.24	0

A.H. Farmahini, *J. Phys. Chem. C* (2013)

CDC+Ti Structures

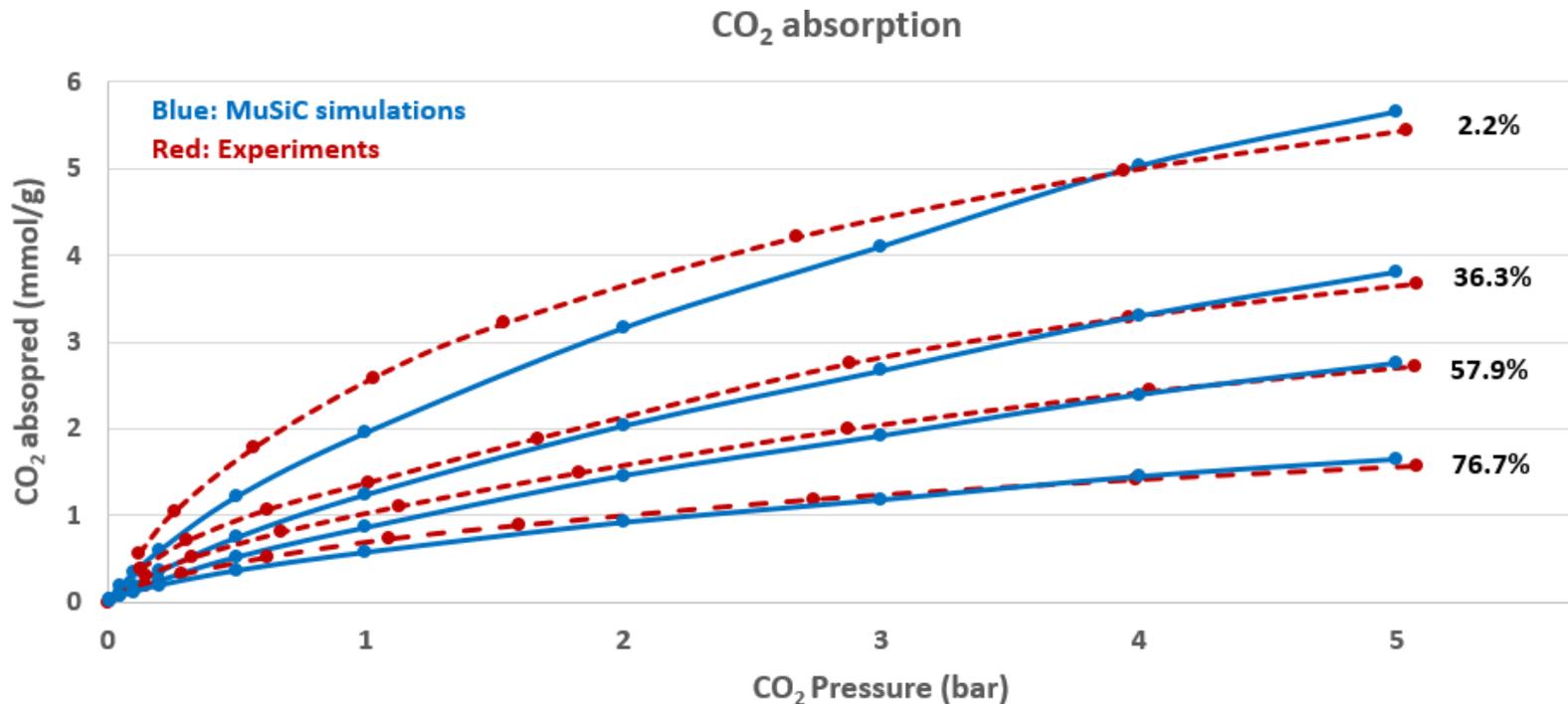
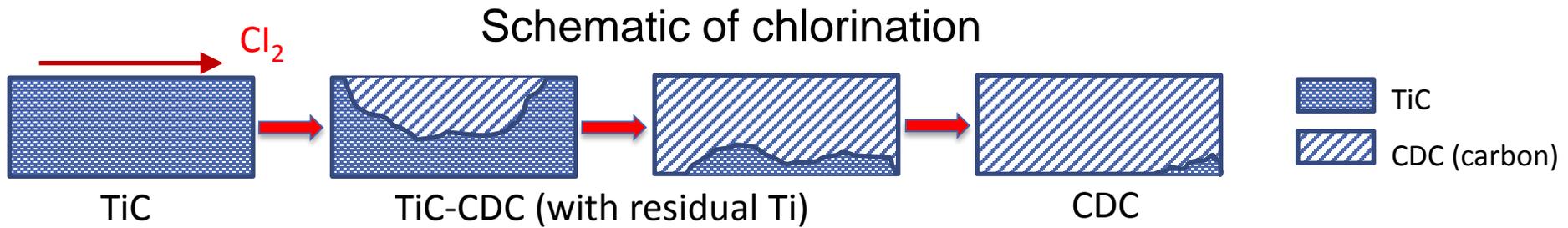
- Ti atoms or clusters added throughout the structure
- Systems are evolved at 300-900K using MD simulations



Ti-CDC models with added (A) Ti atoms (B) Ti_{13} clusters

D. Zhang et al. (in preparation)

Weighted Combination of Models



Absorption of weighted combination

D. Zhang et al. (in review)

Summary

- Thin films of Ti do not disrupt graphene structure
- Graphene vacancies have mixed effect on Ti-graphene interaction
- Substrates have significant effects on Ti-graphene interactions (mainly due to electrostatic interactions between charges that were induced in both graphene and the surface of substrate)
- Predictions of COMB3 potentials are consistent with DFT results
- These potentials may be used to investigate Ti-CDC systems

Functional Form of the COMB3 Potential

$$E_T = \sum_i \left\{ \begin{aligned} &E_i^{Self}(q_i) + \frac{1}{2} \sum_{j \neq i} [V_{ij}^{short}(r_{ij}, q_i, q_j) + V_{ij}^{Coul}(r_{ij}, q_i, q_j)] \\ &+ B_i(q_i) + C_i(r_{ij}, \theta_{ijk}) + E^{polar}(q_i, r_{ij}) + E^{vdW}(r_{ij}) \end{aligned} \right\}$$

- **Self energy:** ionization energies and electron affinities; includes penalty function to capture change in self-energy due to the field from the ionic lattice
- **Short-range interactions:** reactive bond-order potential
- **Coulomb interactions:** Coulomb integral over the charge densities
- **Charge and angular correction terms**
- **Polarization:** Atomic polarizability for organic systems
- **van der Waals energy**

S.R. Phillpot and S.B. Sinnott, *Science* (2009)
T. Liang et al., *Materials Science and Engineering R* (2013)

COMB and ReaxFF

COMB3:

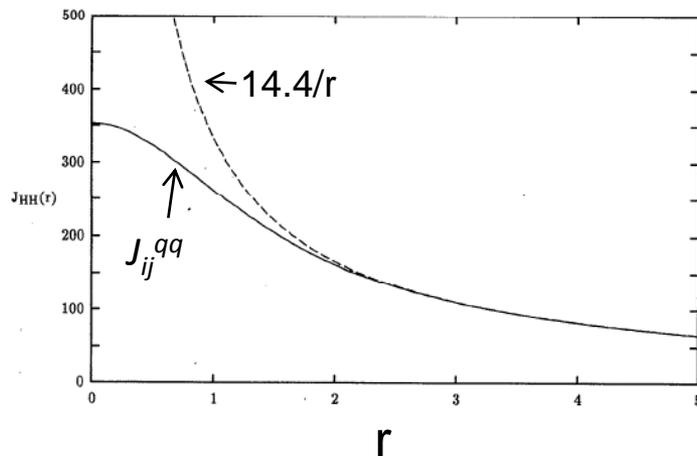
- Charge density function, ρ
- Core charge, Z
- Coulomb integrator, J^{qq} , J^{qz}
- DirectSum

$$f(|\mathbf{r} - \mathbf{r}_i|) = \xi_i^3 \pi^{-1} \exp(-2\xi_i|\mathbf{r} - \mathbf{r}_i|)$$

$$\rho_i(\mathbf{r}; q_i) = Z_i \delta(|\mathbf{r} - \mathbf{r}_i|) + (q_i - Z_i) f_i(|\mathbf{r} - \mathbf{r}_i|)$$

$$J_{ij}^{qq} = [\rho_i | \rho_j] = \int d^3 r_1 \int d^3 r_2 \frac{\rho_i(\mathbf{r}_1) \rho_j(\mathbf{r}_2)}{r_{12}}$$

$$E^{qz}[\{q\}, \{r\}] = \sum_i \sum_{j>i} (q_i J_{ij}^{qz} q_j + q_j J_{ji}^{qz} q_i)$$



ReaxFF:

- Point charge
- No core charge
- Shielded Coulomb
- Tap function

$$- \text{Tap} \cdot C \sum_{j \neq i}^N \frac{q_j}{[r_{ij}^3 + (1/\gamma_{ij})^3]^{1/3}}$$

$\sim 1/r \rightarrow$ Coulomb catastrophe
when r is infinitely small

- Both $1/r$ at long distance
- To avoid Coulomb catastrophe at short distance
 - Coulomb integrator over charge density in COMB3
 - Shielding parameter γ in ReaxFF

COMB and ReaxFF

$\sim 1/r \rightarrow$ does not converge at infinitely long distances; the Ewald Summation method is costly

COMB3 uses Direct Sum

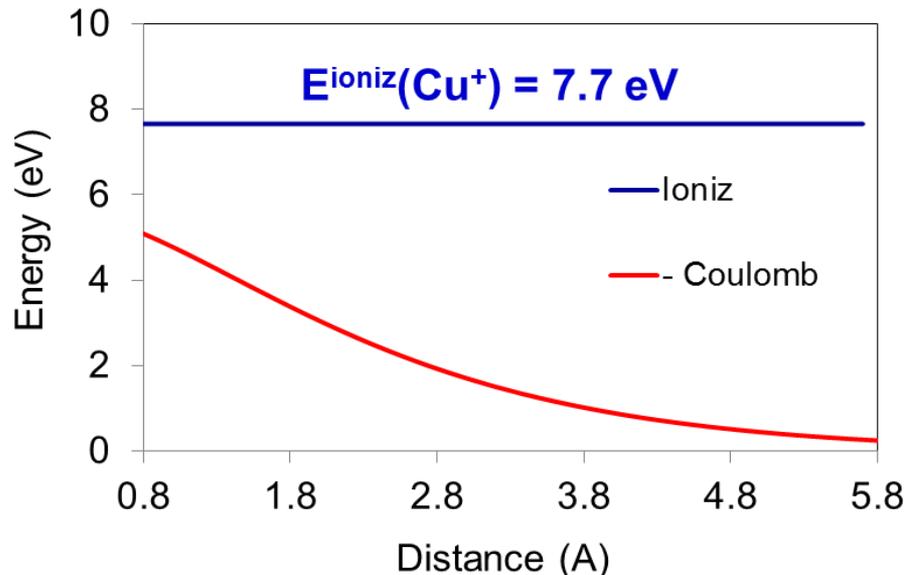
- Coulomb cutoff
- Design for crystals
- Underestimate the Coulomb in molecules

ReaxFF uses the Taper Function

$$- \text{Tap} \cdot C \sum_{j \neq i}^N \frac{q_j}{[r_{ij}^3 + (1/\gamma_{ij})^3]^{1/3}}$$

- Coulomb cutoff
- The Taper function can adjust the strength of Coulomb interactions

Coulomb + Ionization



- Energy minima at infinitely short distances
- No charge transfer

COMB and ReaxFF

Coulomb + Ionization -> underestimates charge transfer

COMB3 adds field effects

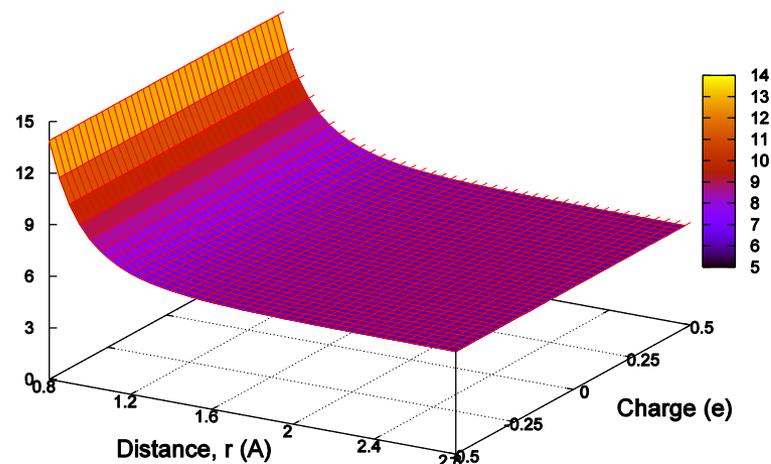
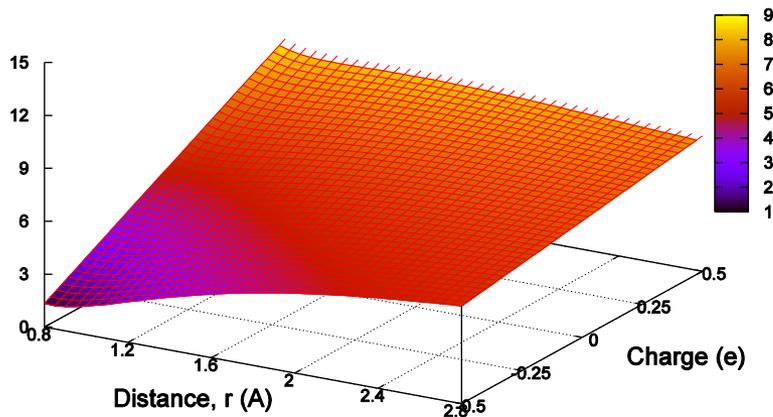
ReaxFF modifies the ionization energy curve

$$F_i^{Field}(r_{ij}, q_j) = \frac{1}{4\pi\epsilon_o} \sum_{j \neq i}^{NN} \left(\frac{P^X q_j}{r_{ij}^3} + \frac{P^J q_j^2}{r_{ij}^5} \right)$$

$$\chi_i^0 q_i + \frac{1}{2} J_i^0 q_i^2$$

Electronegativity

Self-Coulomb

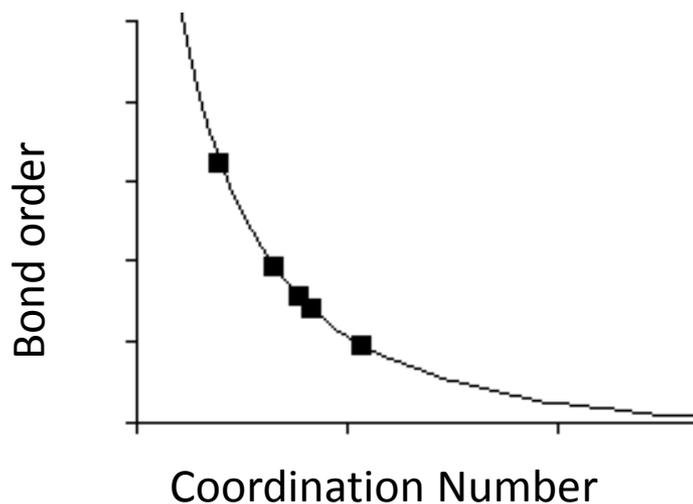


- COMB3 still underestimates charge transfer
- Original version of ReaxFF may have large residual charge in the case of bond dissociation; being resolved via integration with ACKS2 method

Short Range Bond Order Differences

COMB3:

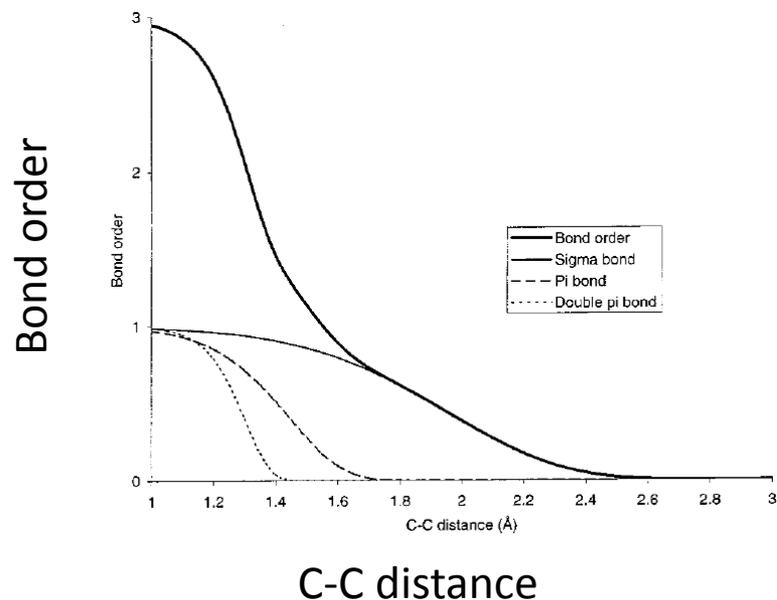
- Abell-Tersoff-Brenner
- Bond order evaluated based on CN, bond angle, torsion ...
- Bond order scales the pairwise attraction
- Uses Tersoff cutoff function



- Bond order in COMB3 is not directly related to distance
- CN increase -> increased electron-electron repulsion -> increased bond length

ReaxFF:

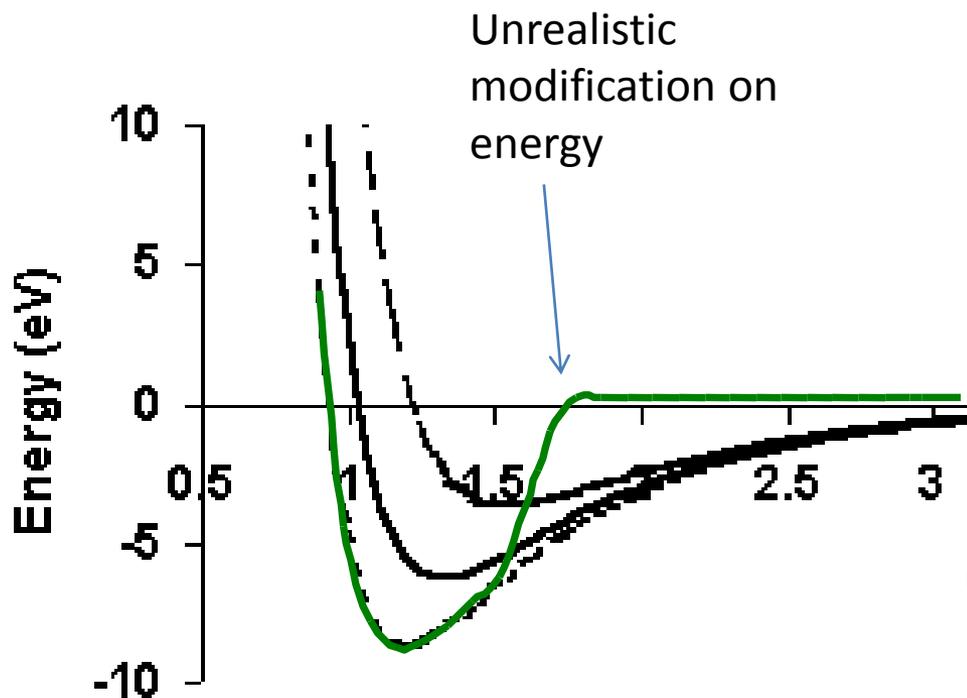
- The bond order is first evaluated from bond length
- All other energy terms can be scaled by a bond order
- No cutoff function is used



COMB3 and ReaxFF

Cutoff Function

Unrealistic energy and forces inside cutoff region for COMB3



Parameterization

- COMB3 is more focused on crystals than molecules since DirectSum works better.
- ReaxFF can do a better job for transition states since there is no cutoff on short-range interaction.