



Negative feedback as a noise suppression mechanism in collective foraging

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Mathematics of Intelligences Programme - Workshop IV: Modeling Multi-Scale Collective Intelligence



A talk in two parts

Part one: how can we think about collective animal behaviour?



Wikipedia





Proximate View	
Ultimate View	

	Dynamic View	
Proximate View		
Ultimate View		

	Dynamic View	Static View
Proximate View		
Ultimate View		

	Dynamic View	Static View
Proximate View	Behavioural development	
Ultimate View		

	Dynamic View	Static View
Proximate View	Behavioural development	Behavioural mechanism
Ultimate View		

	Dynamic View	Static View
Proximate View	Behavioural development	Behavioural mechanism
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Marshall & Reina, 2024

Question A: What quantity should be optimised?

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A Dog a Day



A Dog a Day



A Dog a Day

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Optimisation tools

Behavioural function What quantity should be

optimised?





Optimal statistical tests

Drift-Diffusion Model (DDM): based on likelihood ratio test











PERSPECTIVES

During the search for a new nest site, use of an inhibitory signal enables honevbees

to reach a decision.

BEHAVIOR

How Honeybees Break a Decision-Making Deadlock

Jeremy E. Niven

or a honeybee swarm of potentially thousands of individuals, choosing a home is a momentous decision Failhome is a momentous decision. Failing to choose a single location may cause the swarm to split and the queen to be lost (1); choosing poorly may limit the swarm's growth or expose it to freezing temperatures during the winter (2). Studies over the past 60 years have shown that honeybee swarms use quorum sensing, a form of decentralized decision-making, to choose a suitable nest site, but many gaps remain in our understanding of this process. On page 108 in this issue, Seeley *et al.* (3) show that an inhibitory signal between bees advocating different locations allows them to make a decision even when potential nest sites are equally favorable.

Honeybee colonies reproduce through budding, whereby the queen and some workers leave the nest and bivouac on a branch. Some of the most experienced workers leave to locate suitable nest sites (4). Upon their return, these scouts advertise potential locations and their qualities by performing a waggle dance. During the dance, the scout walks straight across the bivouacking bees, making side-to-side waggles of her body. She then stops, turns left or right, and walks a semicircular return path to her starting point. The waggle run's duration and orientation encode the length and the angle of the outward flight, respectively, whereas the number of dance circuits

encodes the quality of the potential nest site (5). Waggle dances recruit additional scouts to a site until a quorum number is reached and the swarm prepares to move to its new home (2).

Scouts advocating less attractive sites produce fewer dance circuits and make fewer trips to the site (6). Along with the recruitment of uncommitted scouts to more attractive sites, this was assumed to be sufficient to enable the bees to reach a quorum, thereby deciding which site to choose (2). However, foraging workers use an additional type of signal to communicate with other bees. Upon returning from a feeder that is crowded or where a predator is present, forager bees produce a brief vibrational signal that discourages other bees from producing waggle dances that advertise the location of that feeder (7). Hypothesizing that a similar signal may be used by house-hunting bees, Seeley et al. set out to observe scout behavior. They found that scouts received "stop" signals—head butts mainly to their head and thorax-from other bees during the return run of the waggle dance (see the figure). These stop signals occurred more frequently just before a scout stopped dancing.

The authors next established swarms on Appledore Island (Maine), which lacks natural nest sites, and gave them a choice of two identical nest boxes. Scouts visiting one box were marked with yellow paint; those visiting the other were marked with pink paint. Most of the bees giving "stop" signals

selection process, dancing scouts with yellow paint received many more stop signals from scouts with pink paint and vice versa, showing that scouts from one site preferentially inhibit the dances of those advertising a competing site (see the figure, panel A). Once the scouts started implementing the decision, dancing scouts received stop signals from scouts that had visited either site. When swarms were given only one nest box, scouts received few stop signals during the decision phase but many during the implementation phase. This general inhibition of dancing during the implementation phase presumably ensures that all the bees are present when the swarm takes flight.

To demonstrate a role for the observed cross inhibition between scouts advertising competing sites, Seeley *et al.* constructed a series of computational models of the collective decision-making process, based on the interaction rules they had observed among the scouts. Models that incorporated no or indiscriminate stop signaling predicted that the scouts would reach a stable deadlock, failing to choose between two

Cease and desist. (A) Seeley *et al.* have found that during house hunting, scouts advertising one nest site preferentially inhibit scouts advertising another site during the decision-making process. Inhibition is conveyed by a "stop" signal, given mainly to the head and thorax of a scout during the return phase of the waggle dance. (B) Stop signals from scout bees inhibit other scouts, discouraging them from advertising a potential site. These





PERSPECTIVES

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Pais et al. (2013)



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 $\overline{v} = 4$ $\sigma = 4$

 Δv

Pais et al. (2013)











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But how do we *know* this strategy is optimal?

Stochastic dynamic programming

A classic optimisation tool applied in behavioural ecology



• Solved the Bellman equation for decisions:

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 $V(t, \hat{r}_1, \hat{r}_2) = \max \{ V_d(\hat{r}_1, \hat{r}_2), \\ \langle V(t + \delta t, \hat{r}_1(t + \delta t), \hat{r}_2(t + \delta t)) \mid \hat{r}_{1,2}(t) = \hat{r}_{1,2} \rangle - c \ \delta t \}.$

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Solved the Bellman equation for decisions:





- Found DDMs with decision boundaries that collapse over time
 - Optimise speed-accuracy tradeoffs
 - <u>No magnitude-sensitive deadlock-breaking</u>



 $V(t, \hat{r_1}, \hat{r_2}) = \max\{V_d(\hat{r_1}, \hat{r_2}), \\ \gamma \langle V(t + \delta t, \hat{r_1}(t + \delta), \hat{r_2}(t + \delta) | \hat{r_{1,2}}(t) = \hat{r_{1,2}}) \rangle\}$

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• Solved the geometric Bellman equation for decisions:



- Found time and magnitude-varying decision boundaries
 - Optimise <u>speed-value</u> trade-off
 - Magnitude-sensitive deadlock-breaking









Audrey Dussutour

Part two: noise suppression in collective foraging



An evolutionary framework for collective behaviour Tinbergen, Behavioural Ecology, and Collective Behaviour

	Dynamic View	Static View
Proximate View	Behavioural development	Behavioural mechanism
Ultimate View	Behavioural evolution	Behavioural function

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Positive feedback



Positive feedback





hristoph Grüter

Positive feedback

Negative feedback



Stephen Pratt







Grüter hristoph

Positive feedback

Negative feedback



Duncan Jackson



Schlegel

In previous work, negative feedback signals have been identified as a mechanism to indicate that forage **sources are not ideal**. For example:

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We propose an alternative function for negative feedback signals, variance reduction

Behavioural evolution What quantity should be

optimised?

Collective emigration foraging model

Honeybee foraging



[Bidari et al. R.Soc.O.S. 2019, Seeley at al. Science 2012]

Collective emigration foraging model

Honeybee foraging



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Honeybee foraging



Honeybee foraging



Honeybee foraging



Honeybee foraging



Chemical reaction model

Chemical reaction model



Chemical reaction model





Chemical reaction model









Chemical reaction model

Insect committed to food source





Discovery

Abandonment



Chemical reaction model

Insect committed to food source





Discovery

Abandonment

Recruitment



Chemical reaction model







Chemical reaction model

Insect committed to food source





Abandonment

Recruitment

Inhibition



Chemical reaction model





Collective foraging model Chemical reaction model Uncommitted Insect committed to food source with quality: $q_1 q_2$ Yi Υi Discovery α_i α_i Abandonment Recruitment β_{ij} β_{ij} Inhibition

Chemical reaction model



Collective foraging model Chemical reaction model Group distribution Uncommitted Insect committed to food source with quality: q1 **q**₂ Υi Υi Discovery α_i α_i Abandonment ρ_i ρ_i Recruitment β_{ii} $\beta_{i\,i}$ Inhibition

Chemical reaction model



Chemical reaction model















Our analysis

Mean-field model of collective foraging

Model without negative feedback



Model with negative feedback

Our analysis

Mean-field model of collective foraging

Model without negative feedback



Model with negative feedback





Model without negative feedback

Model with negative feedback

Sum of Squared Error



Sensitivity analysis

Varying the recruitment strength and system size



Sensitivity analysis

Varying the recruitment strength and food patch quality





The model without negative feedback looks quicker



The model without negative feedback looks quicker



The model without negative feedback looks quicker



asymmetric initial conditions

The model without negative feedback looks quicker



The model without negative feedback looks quicker but it is actually slower


Speed-robustness trade-off

Negative feedback strength regulates the trade-off



as a variance reduction mechanism

Negative feedback as a variance reduction mechanism

We know negative feedback is an efficient mechanism to allow social insects:

- break symmetry in collective decisions [Seeley et al. Science 2012, Reina et al. PhyRev. E 2015]
- adapt to time-varying environments [Nieh Curr. Biol. 2010, Robinson et al. Nature 2005,...]

Negative feedback as a variance reduction mechanism

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We find an additional important role of negative feedback: variance reduction

- similar strategy found in **gene networks** or **electronics**
- it could explain why, even in static conditions, honeybees always deliver a small quantity of stop signals to foragers visiting the same forage patch [Lau & Nieh Apidologie 2010]

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Progression in the evolution of collective foraging

Progression in the evolution of collective foraging



low efficiency

Progression in the evolution of collective foraging



Progression in the evolution of collective foraging



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