

Learning Libraries of Programmatic Policies

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Assistant Professor

Canada CIFAR AI Chair, Amii

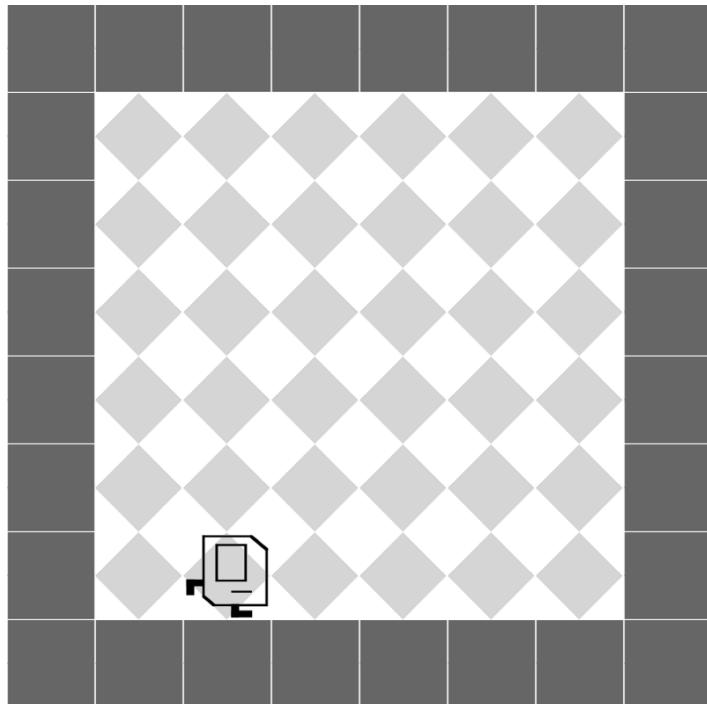
University of Alberta, Canada

Universidade Federal de Viçosa, Brazil

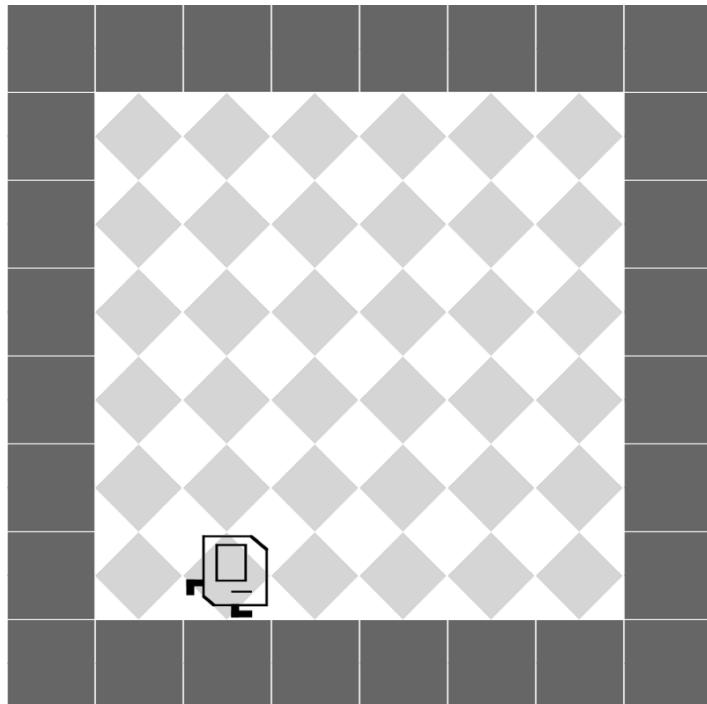
Mahdi Alikhasi, Ken Thjia, Tales Carvalho, Rubens Moraes

Programs are Everywhere

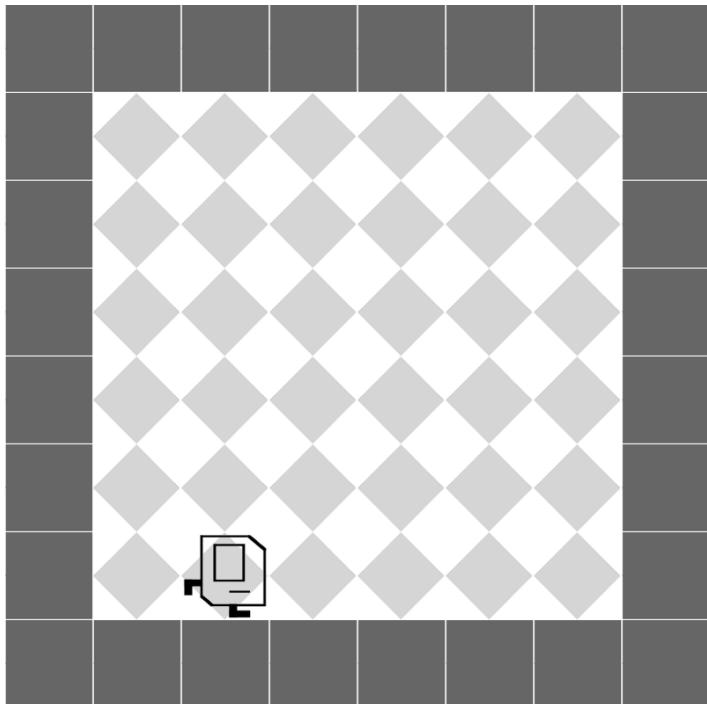
Sequential Decision Making



Sequential Decision Making

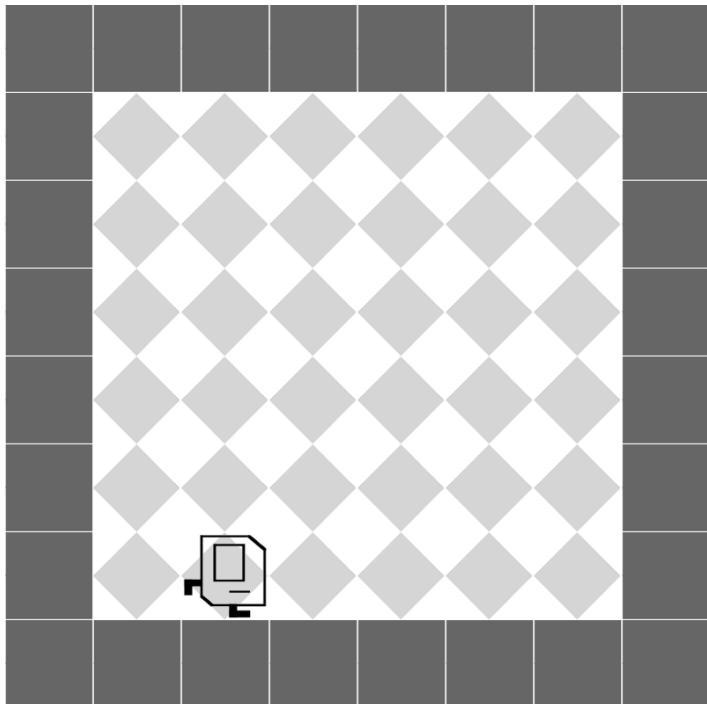


Sequential Decision Making



```
WHILE markerPresent  
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    IF frontIsClear  
        move  
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```

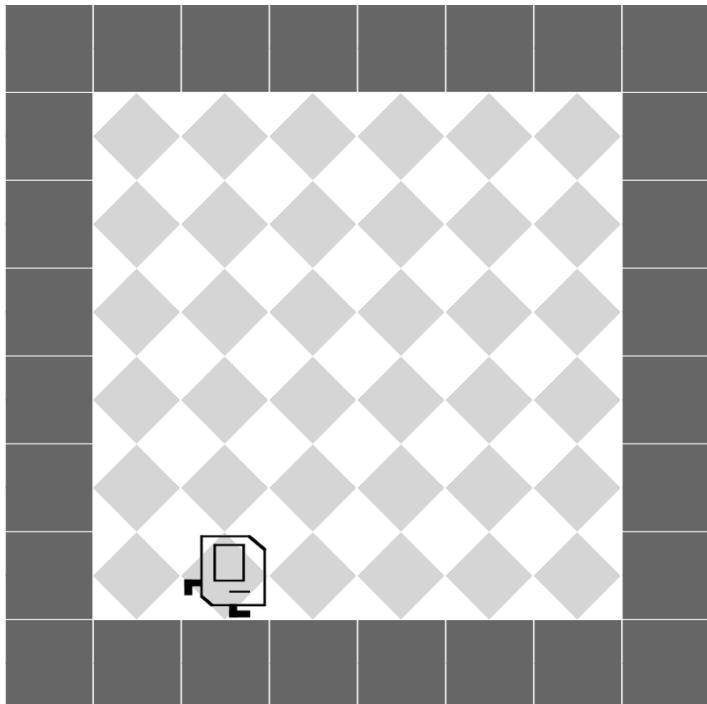
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Programmatic policy

Sequential Decision Making



Reinforcement learning problem

```
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```

Programmatic policy

Search for Programmatic Policies

Search for Programmatic Policies

- ❖ Search space.

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- ❖ Search space.
- ❖ Search procedure.

Programming Language

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$$S \rightarrow x \mid y \mid 0 \mid 1 \mid (S + S) \mid \text{if } B \text{ then } S \text{ else } S$$
$$B \rightarrow (S \leq S) \mid (S == S) \mid (S \geq S)$$

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Quiz: Can the program `if x <= y then 0 else 1` be written in this language?

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Answer: Yes.

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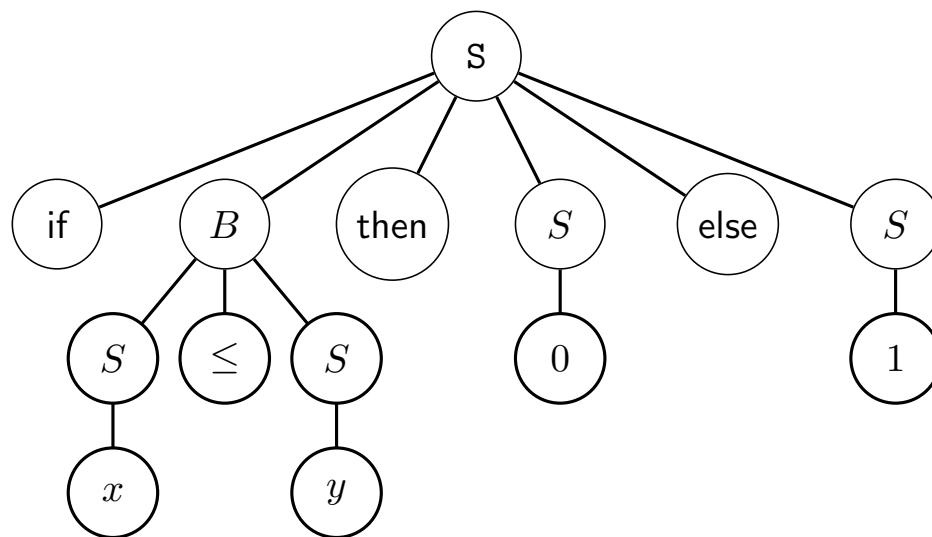
Quiz: Can the program `if x <= y then 0 else 1` be written in this language?

Answer: Yes.

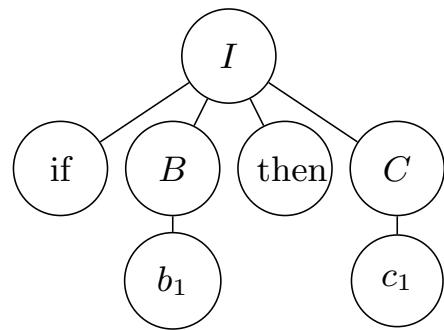
$$\begin{aligned} S &\rightarrow \text{if } B \text{ then } S \text{ else } S \\ &\rightarrow \text{if } S \leq S \text{ then } S \text{ else } S \\ &\rightarrow \text{if } x \leq S \text{ then } S \text{ else } S \\ &\rightarrow \text{if } x \leq y \text{ then } S \text{ else } S \\ &\rightarrow \text{if } x \leq y \text{ then } 0 \text{ else } S \\ &\rightarrow \text{if } x \leq y \text{ then } 0 \text{ else } 1 \end{aligned}$$

Representing Programs in Memory

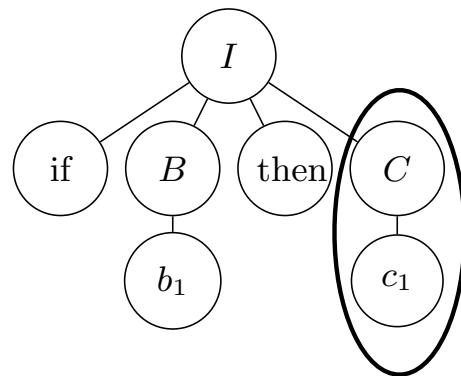
```
if x <= y then 0 else 1
```



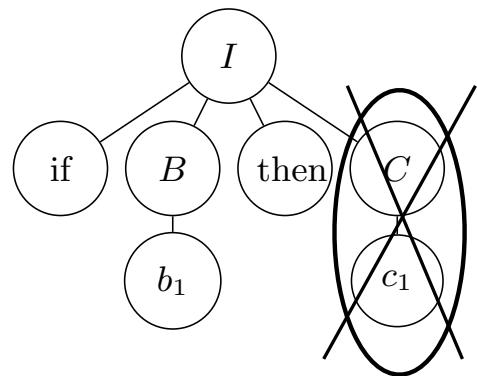
Stochastic Neighborhood Function



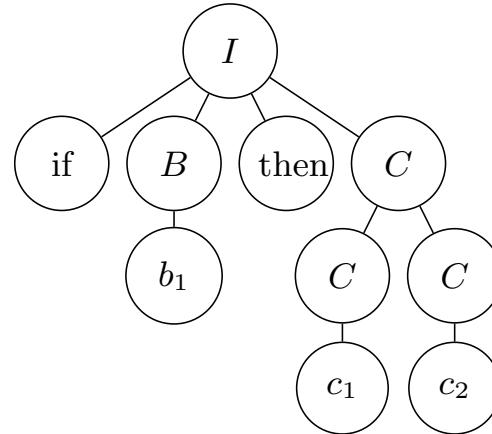
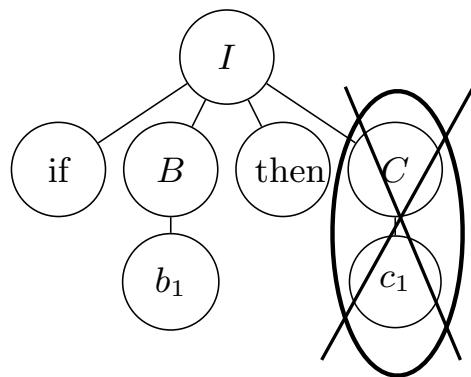
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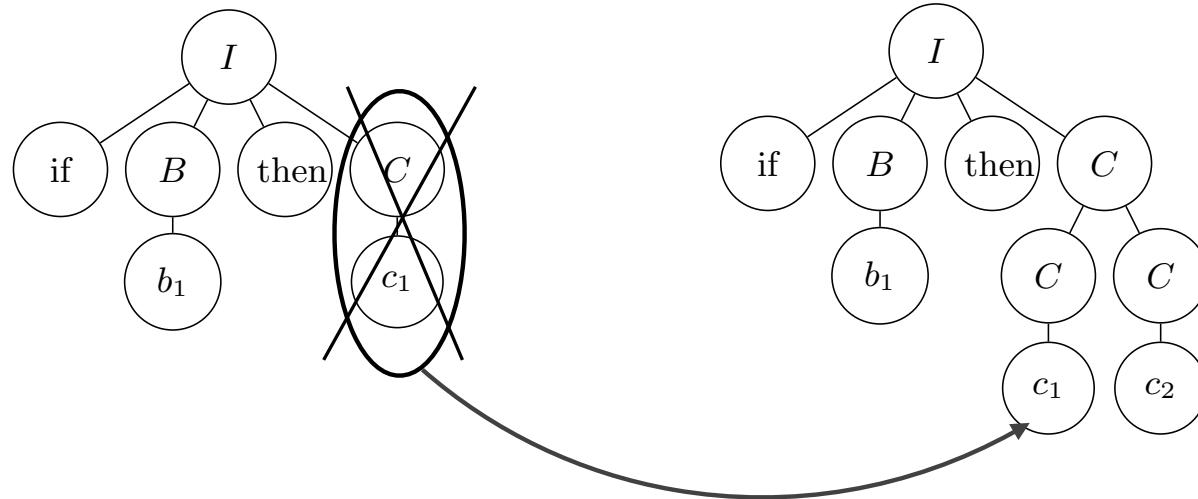
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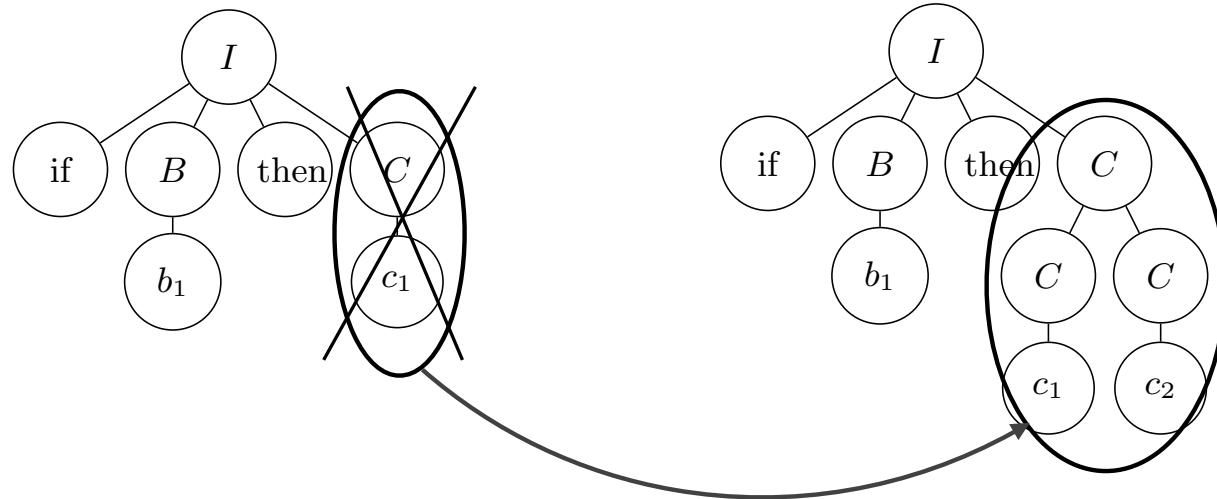
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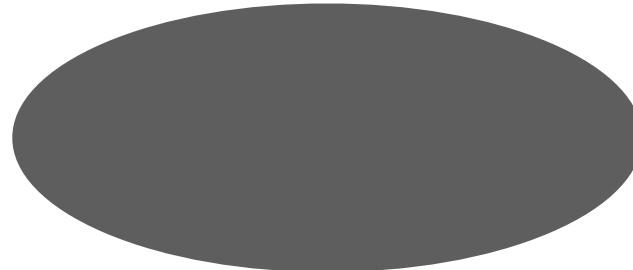
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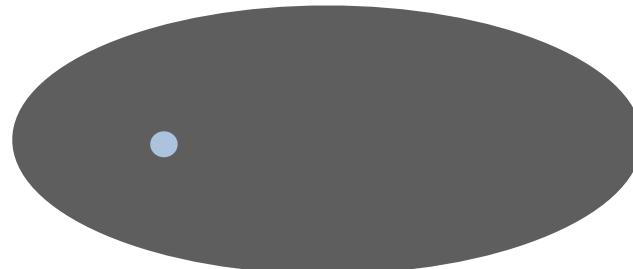
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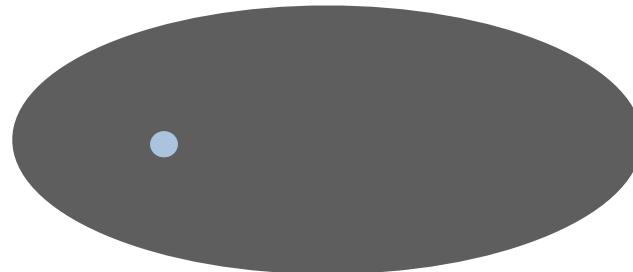
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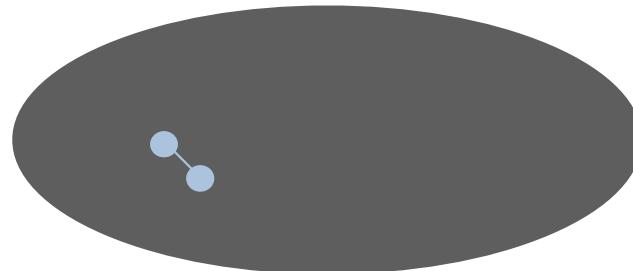
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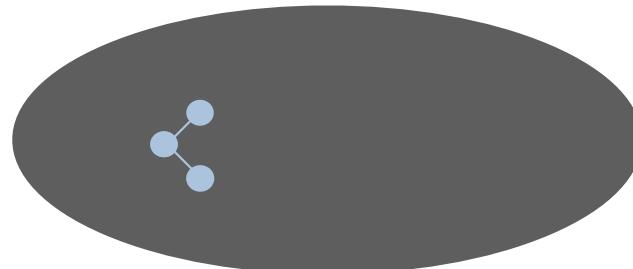
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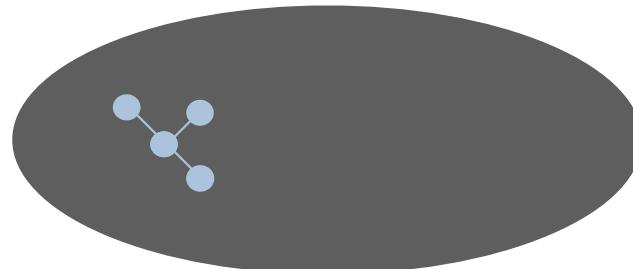
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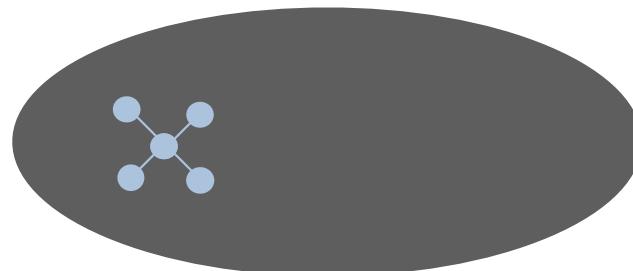
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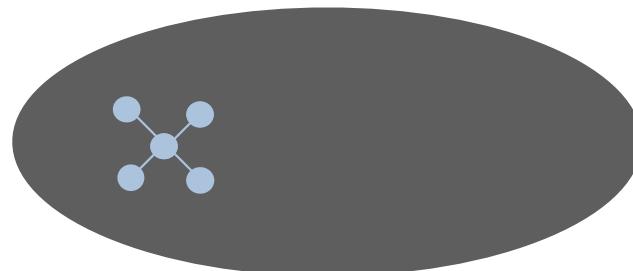
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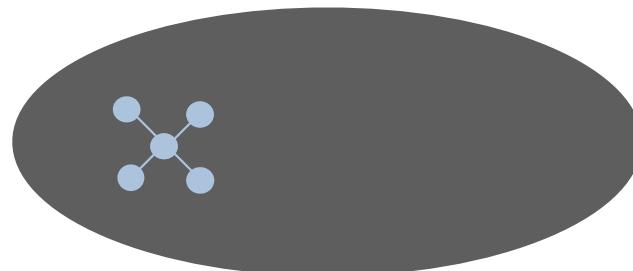
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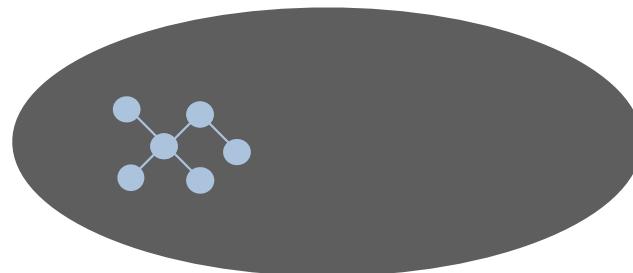
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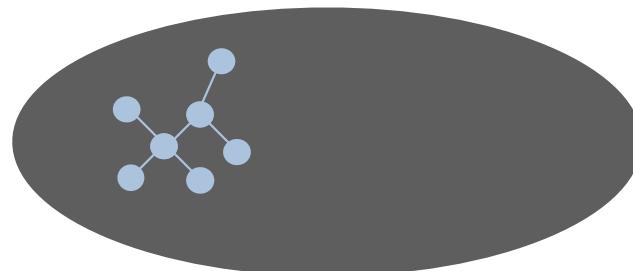
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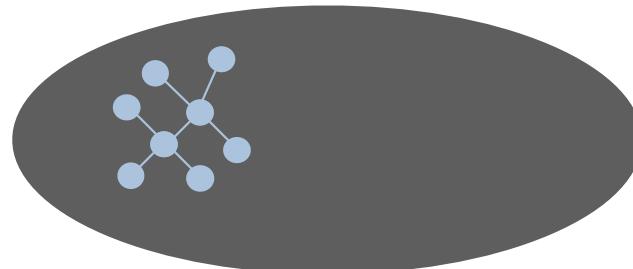
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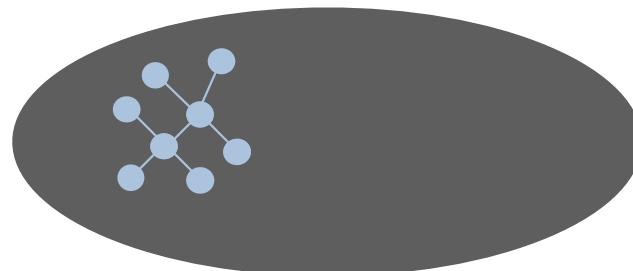
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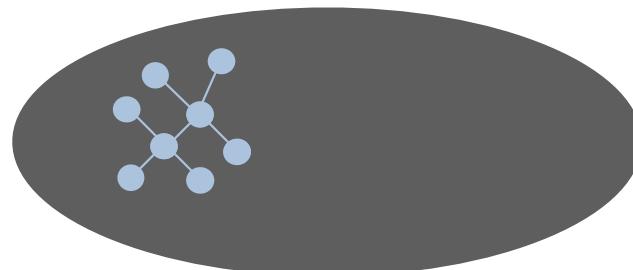
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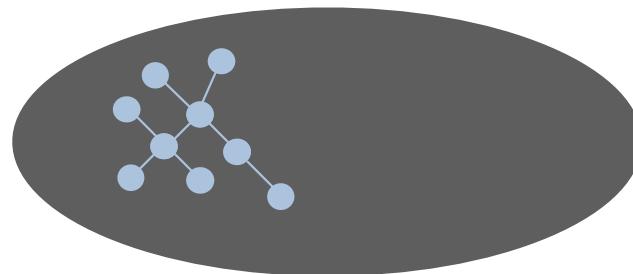
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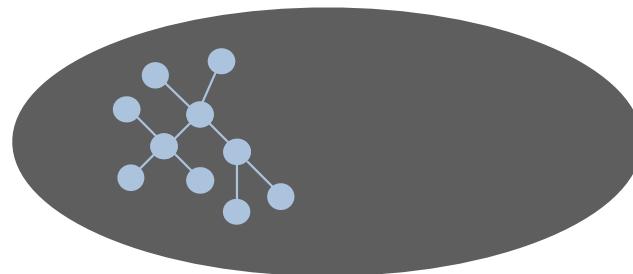
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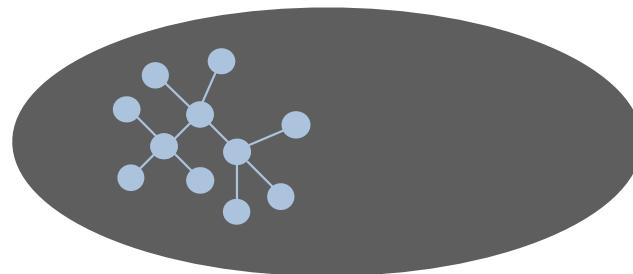
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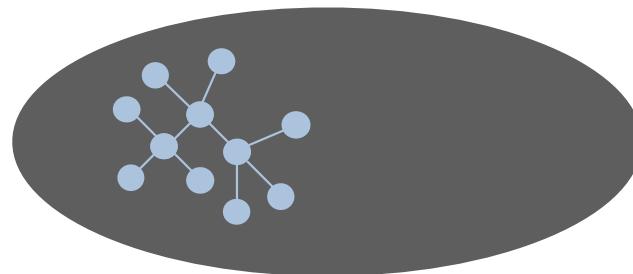
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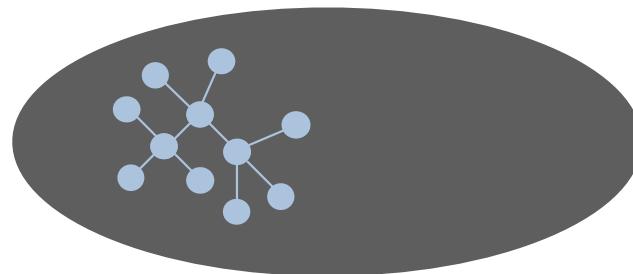
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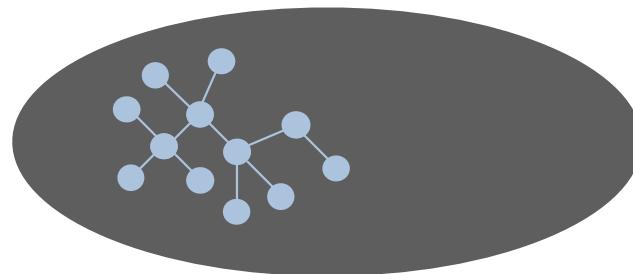
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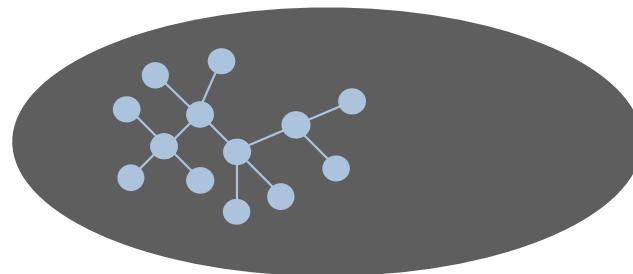
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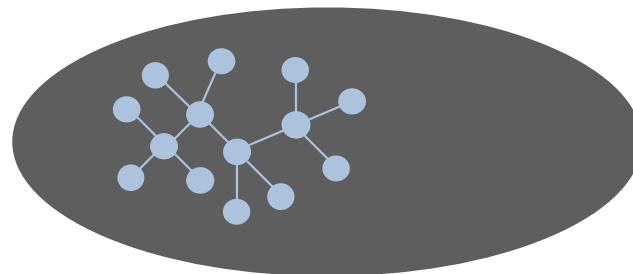
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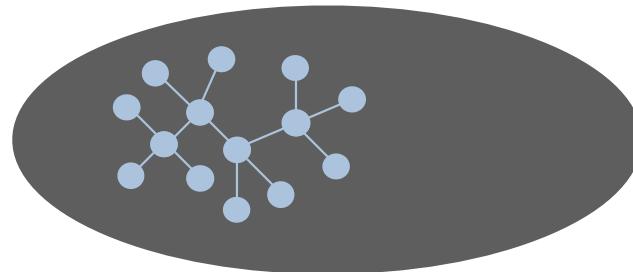
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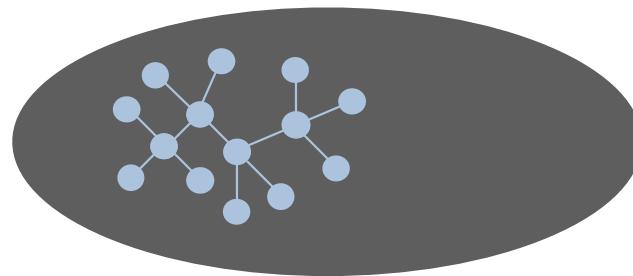
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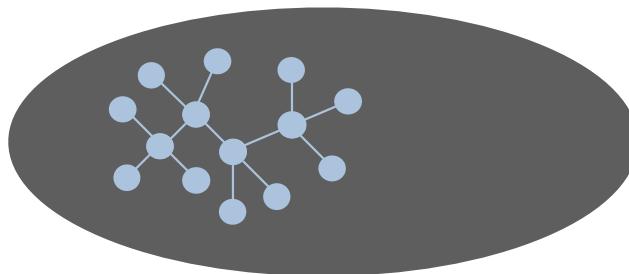
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Restarts, restarts, restarts...

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- ❖ Search procedure.

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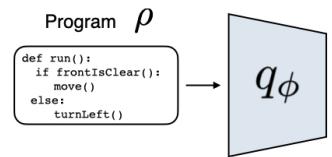
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Spaces Conducive to Search - LEAPS

Program ρ

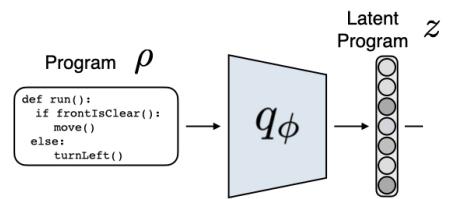
```
def run():
    if frontIsClear():
        move()
    else:
        turnLeft()
```

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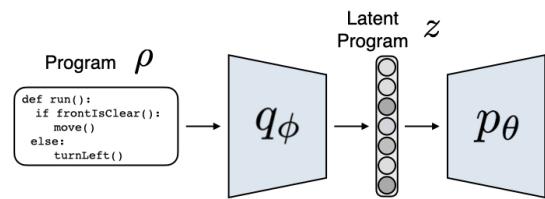
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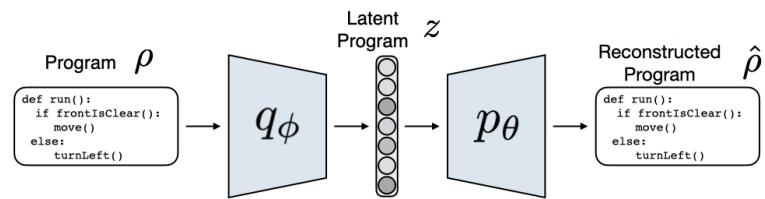
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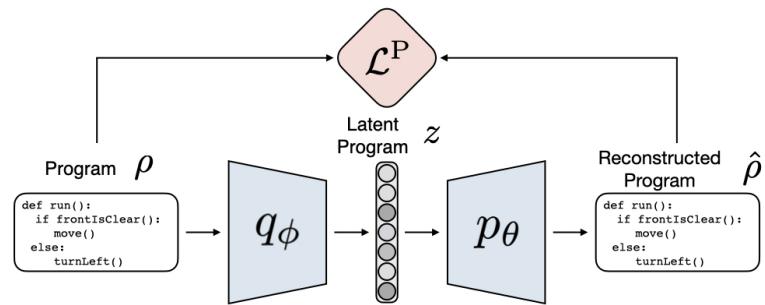
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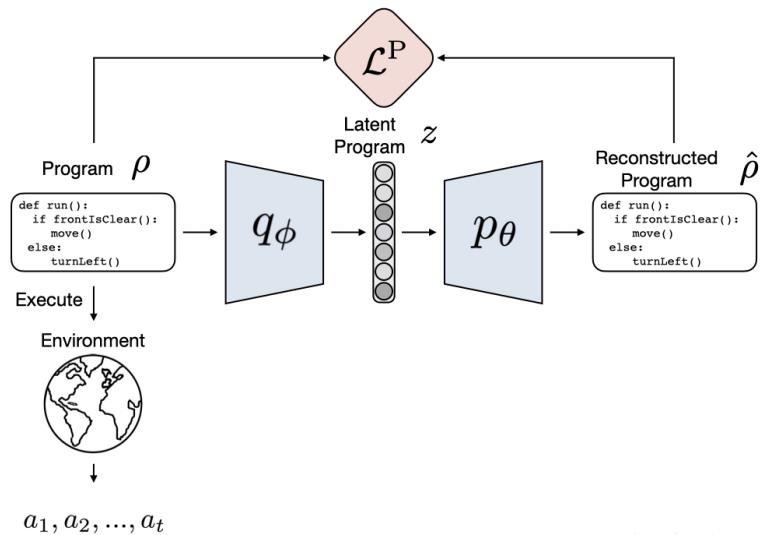
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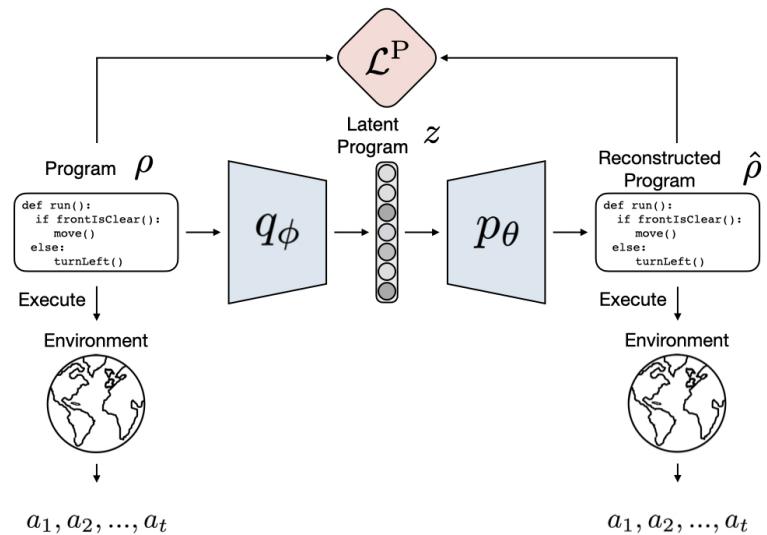
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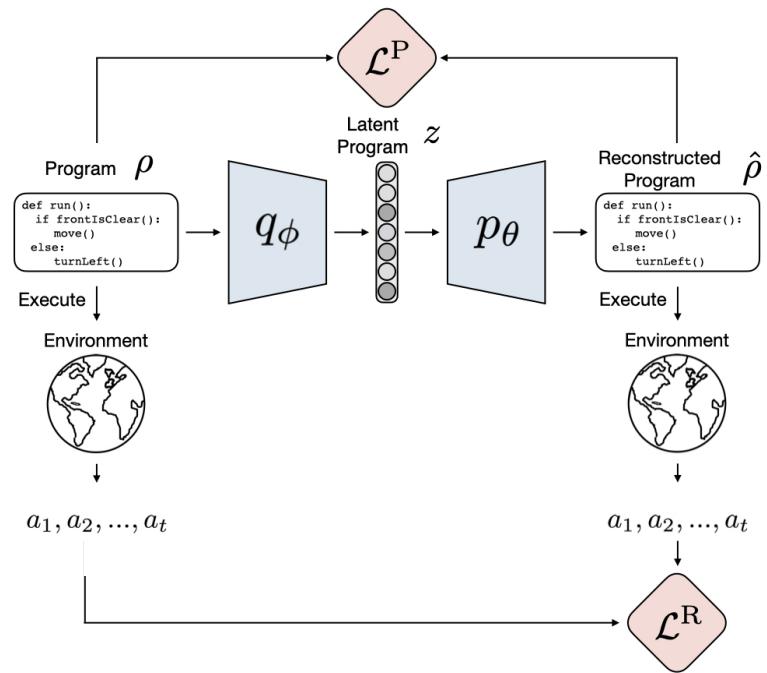
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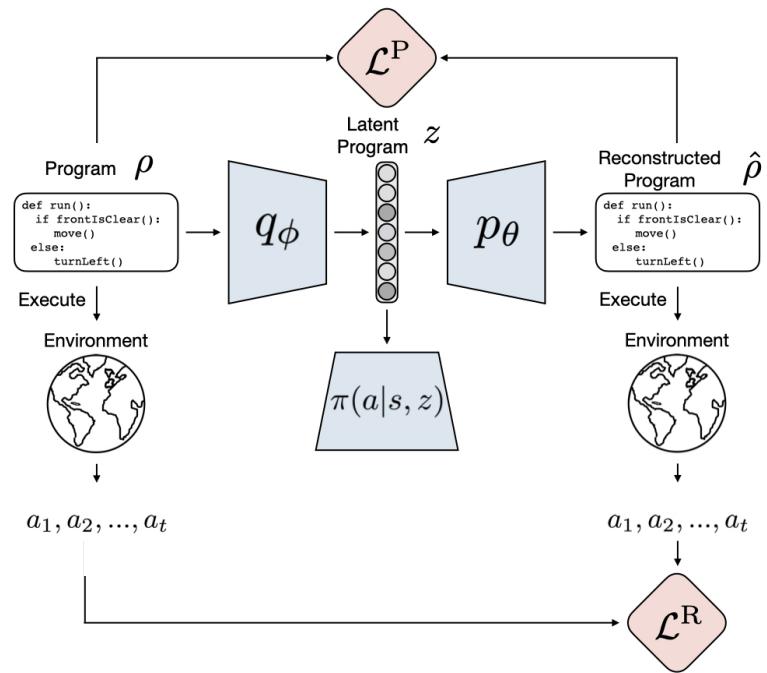
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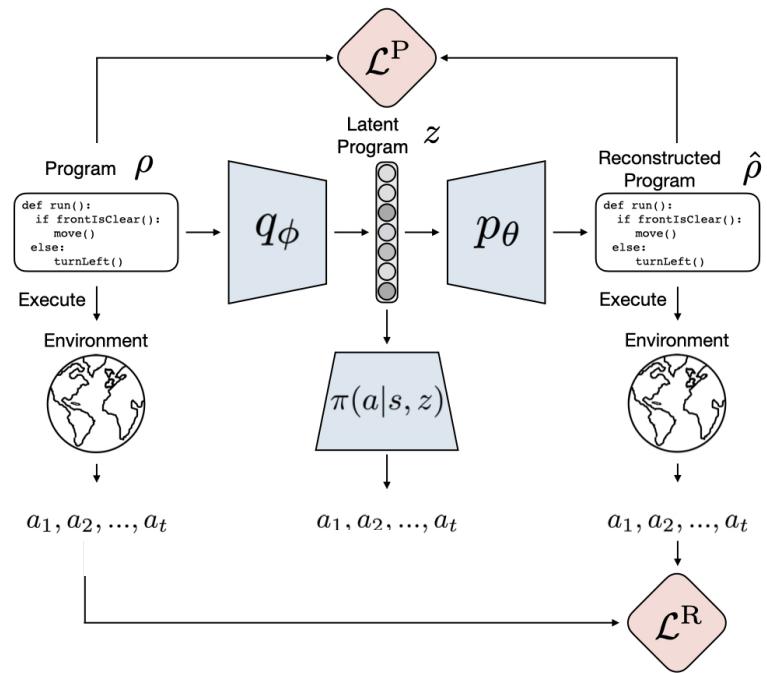
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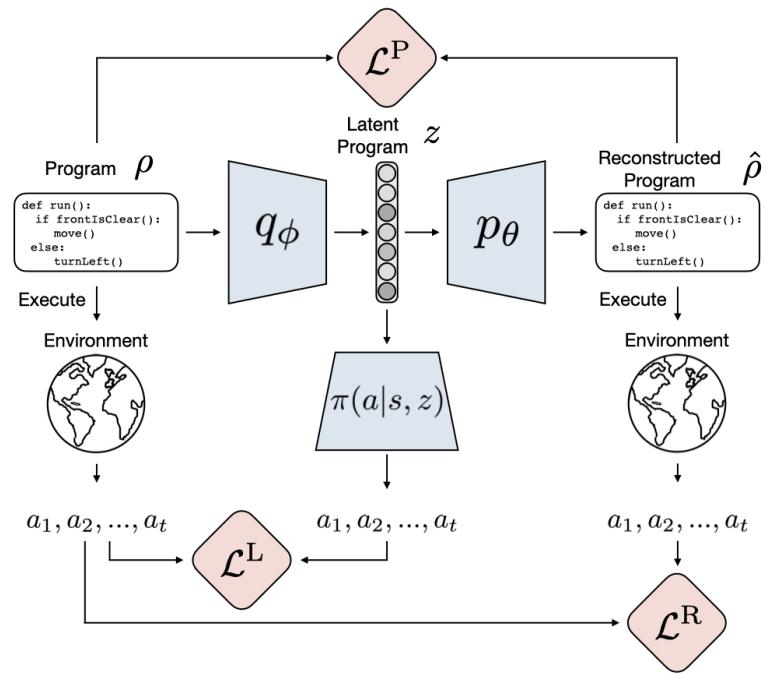
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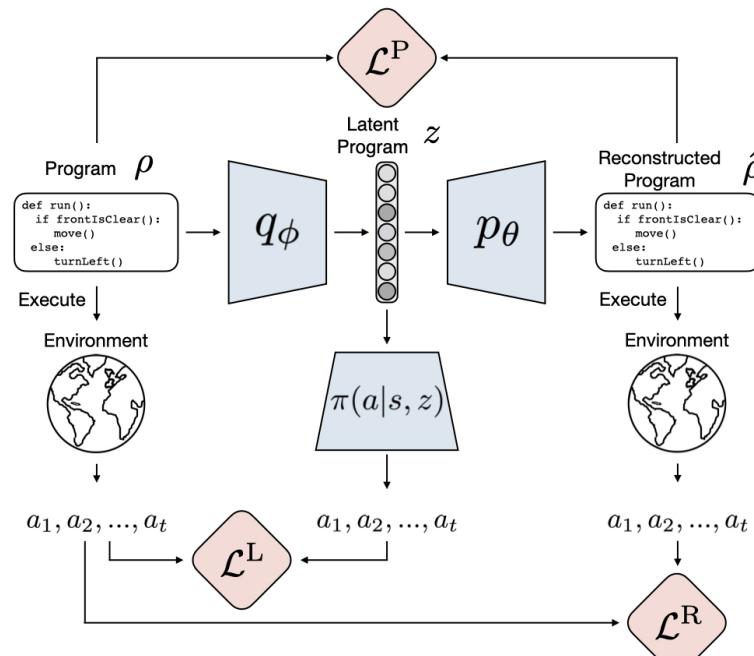
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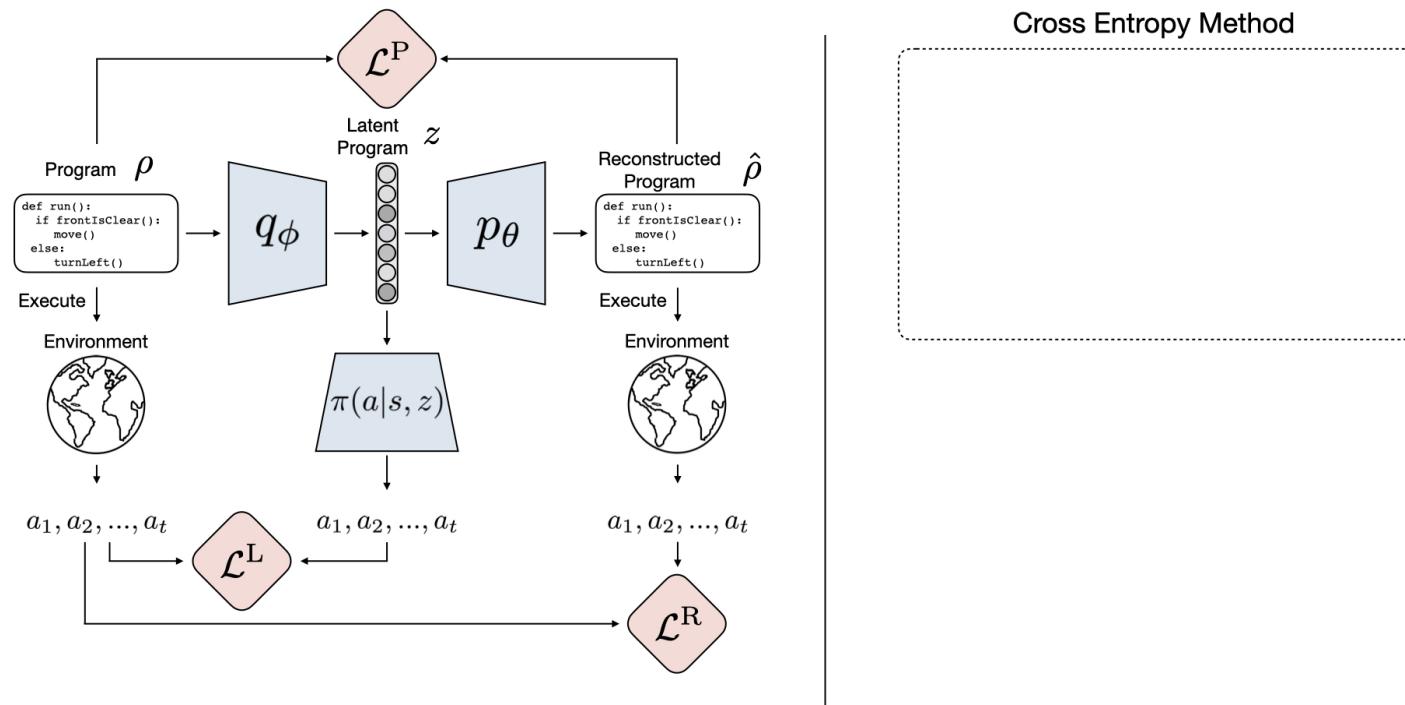
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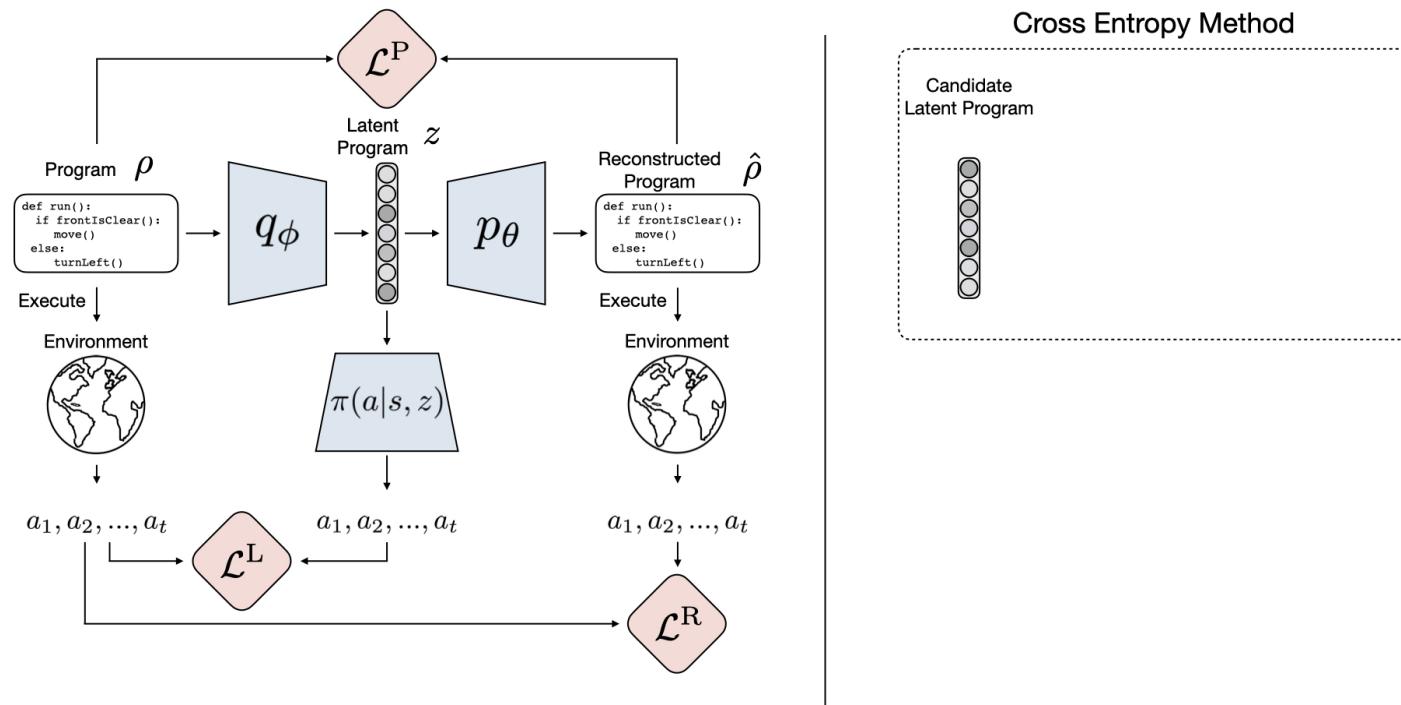
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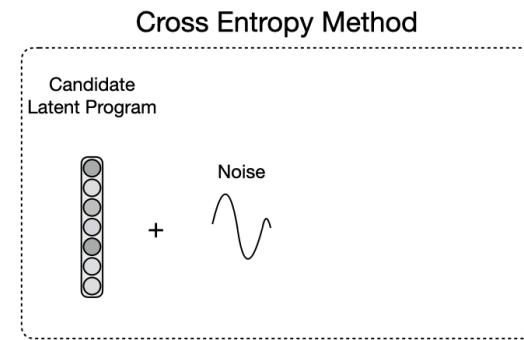
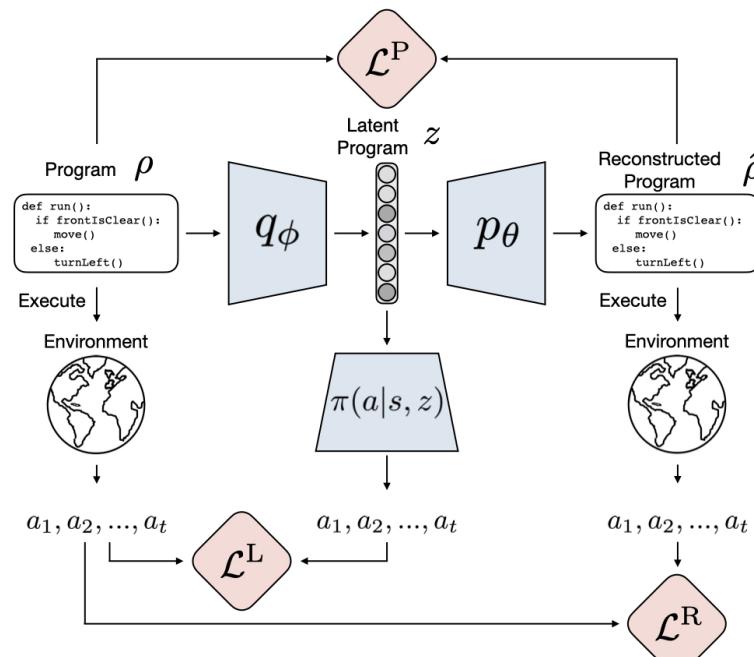
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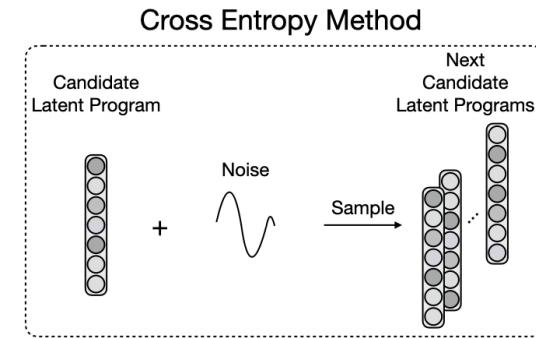
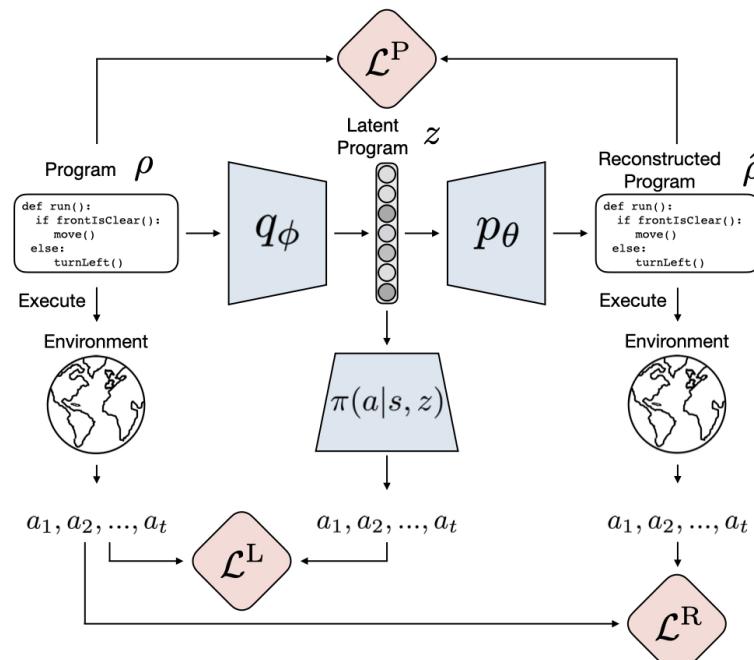
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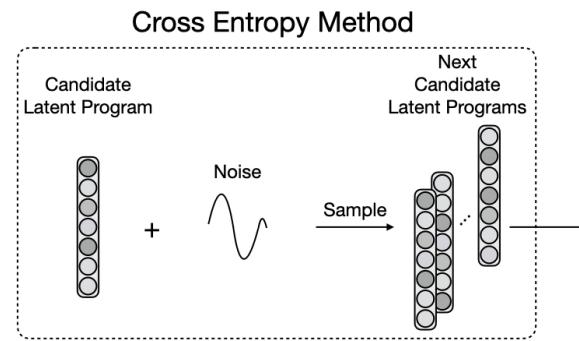
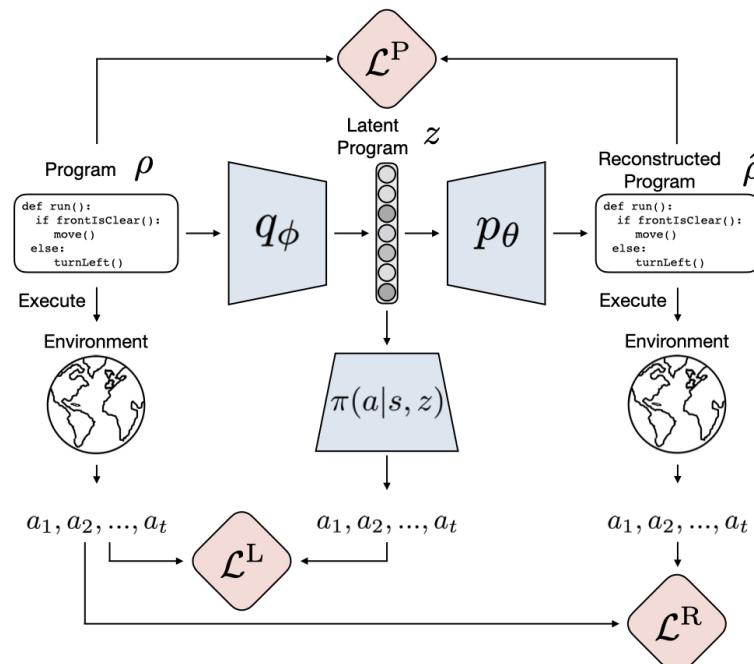
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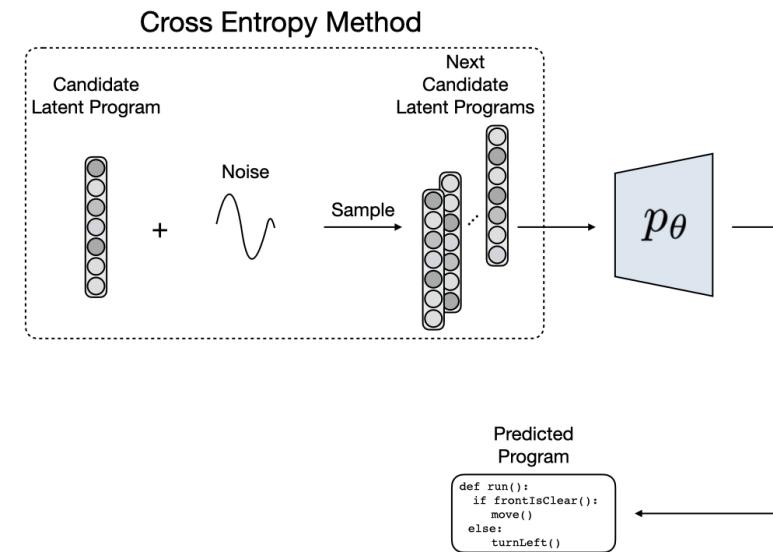
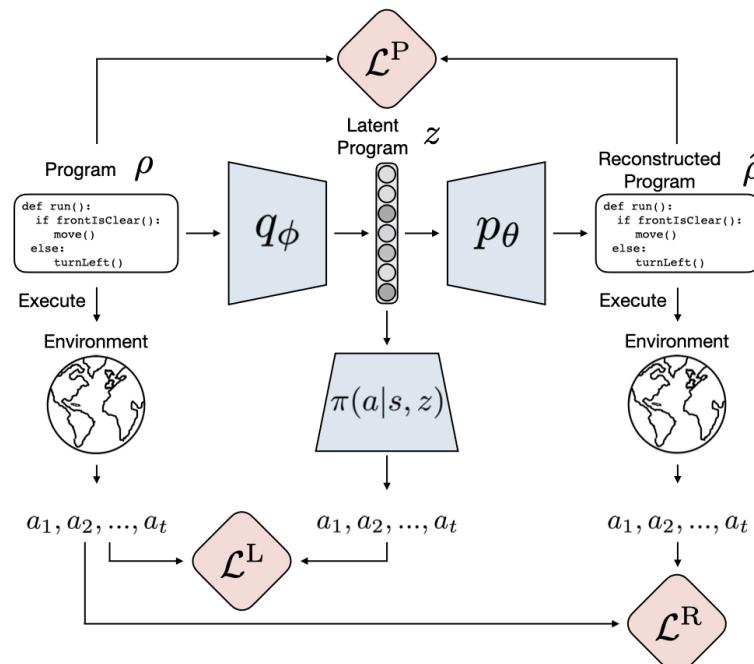
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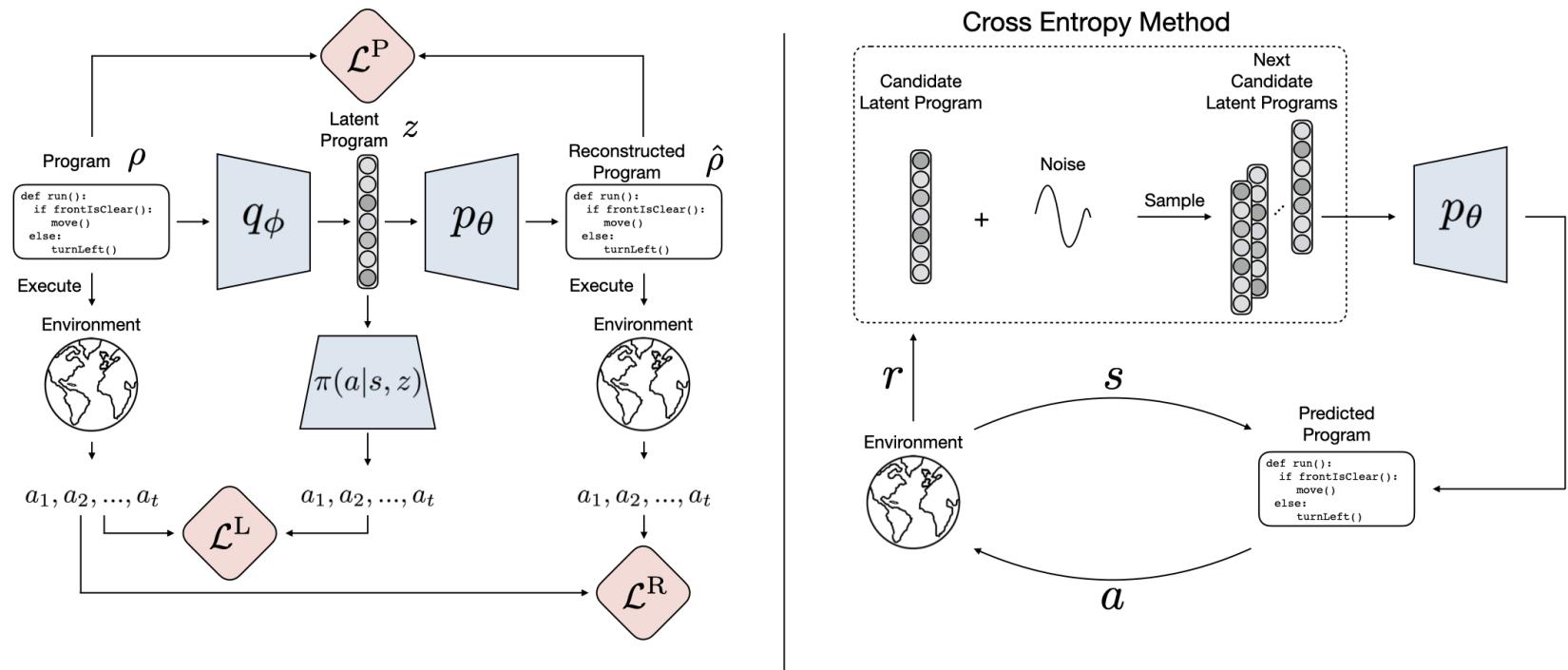
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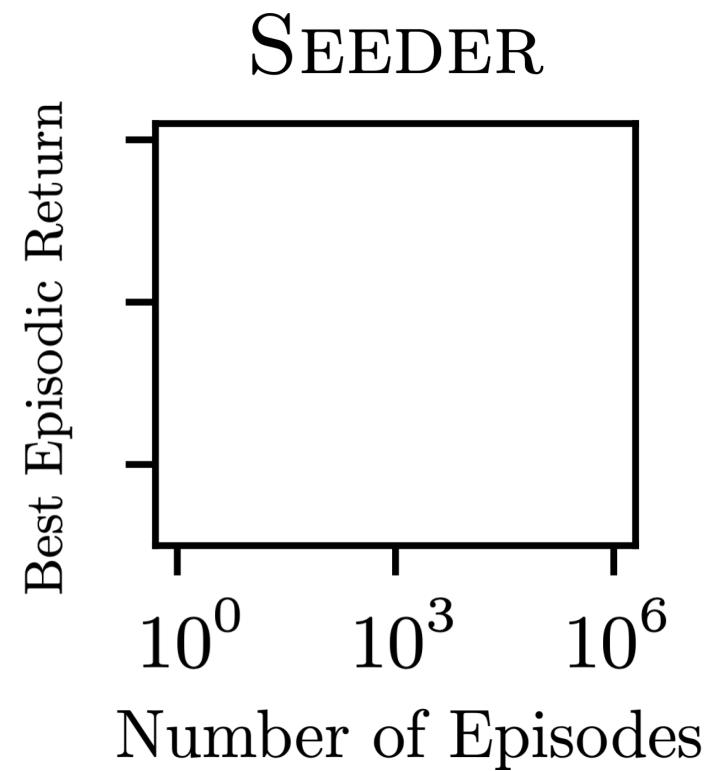
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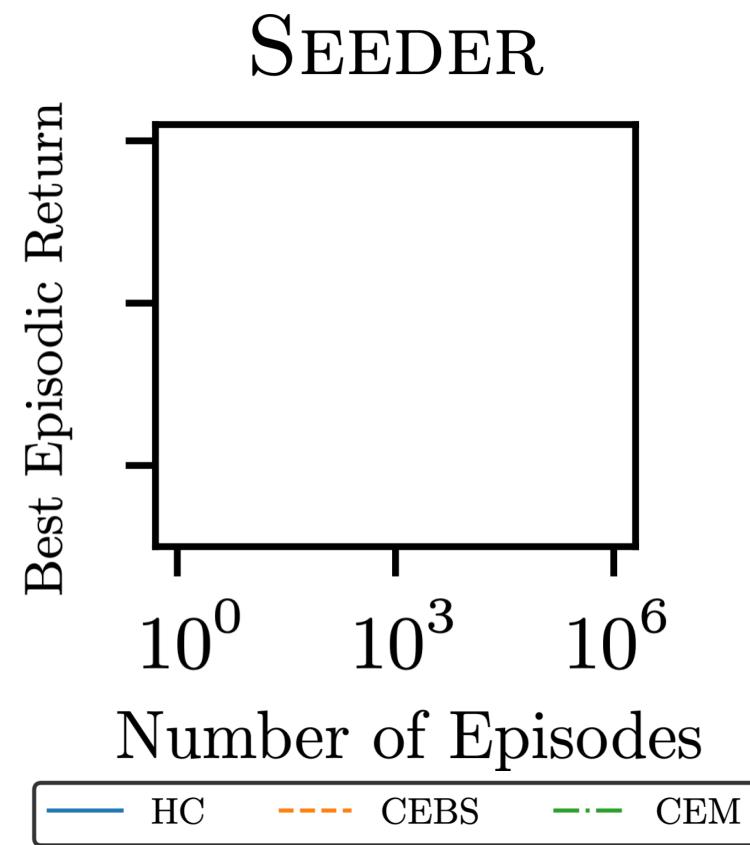


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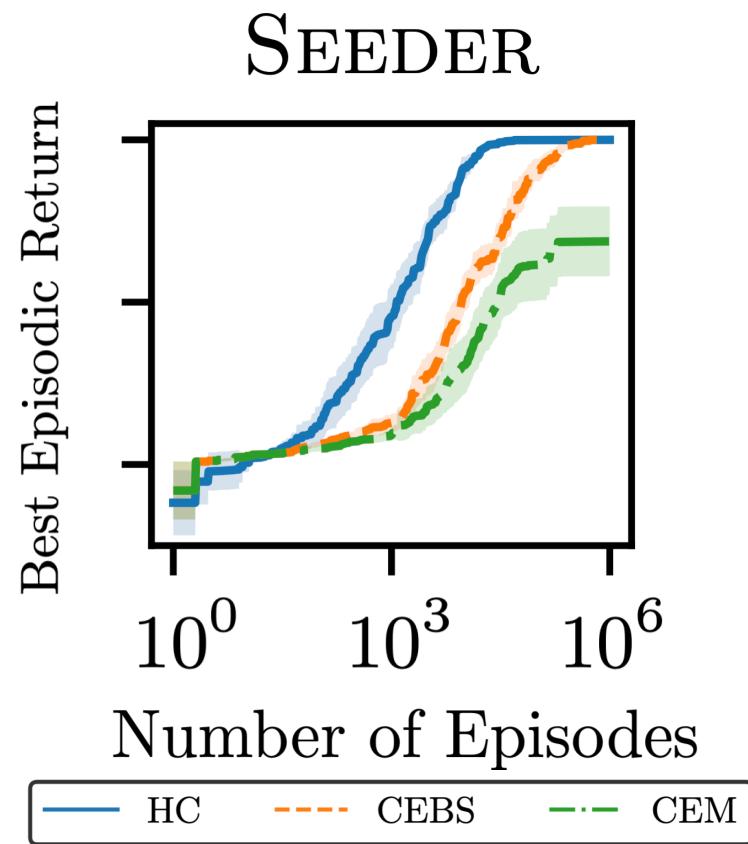
Empirical Results



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Semantic Spaces

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Key idea: Neighbor programs should be semantically different.

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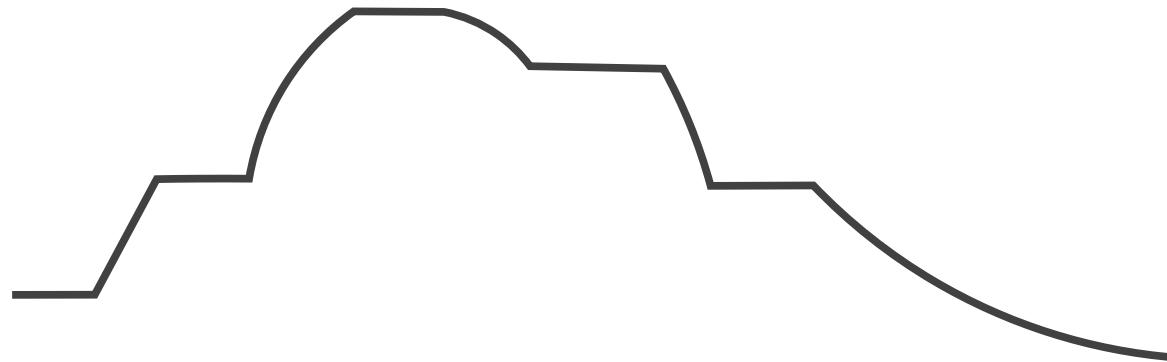
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Syntax Space

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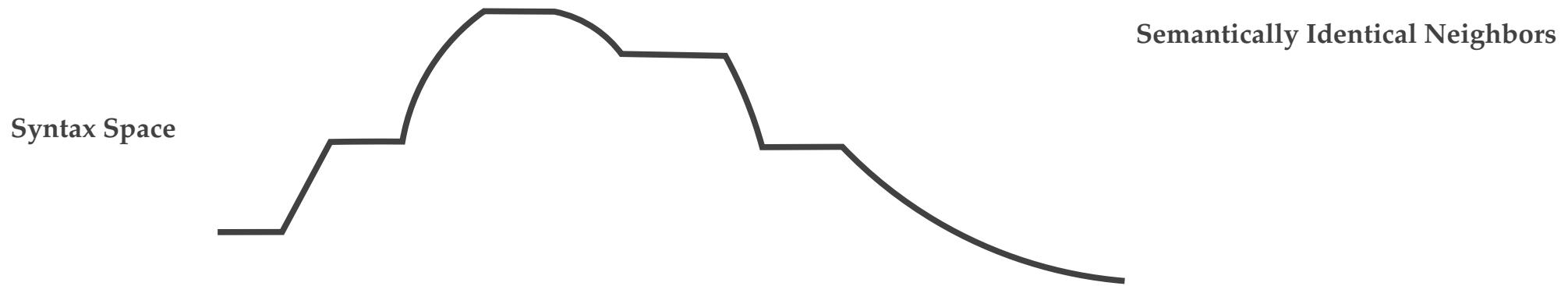
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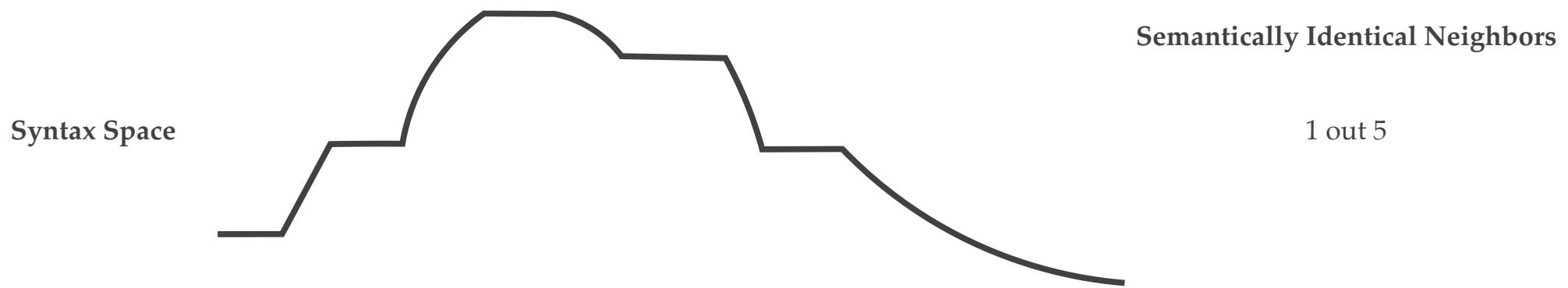
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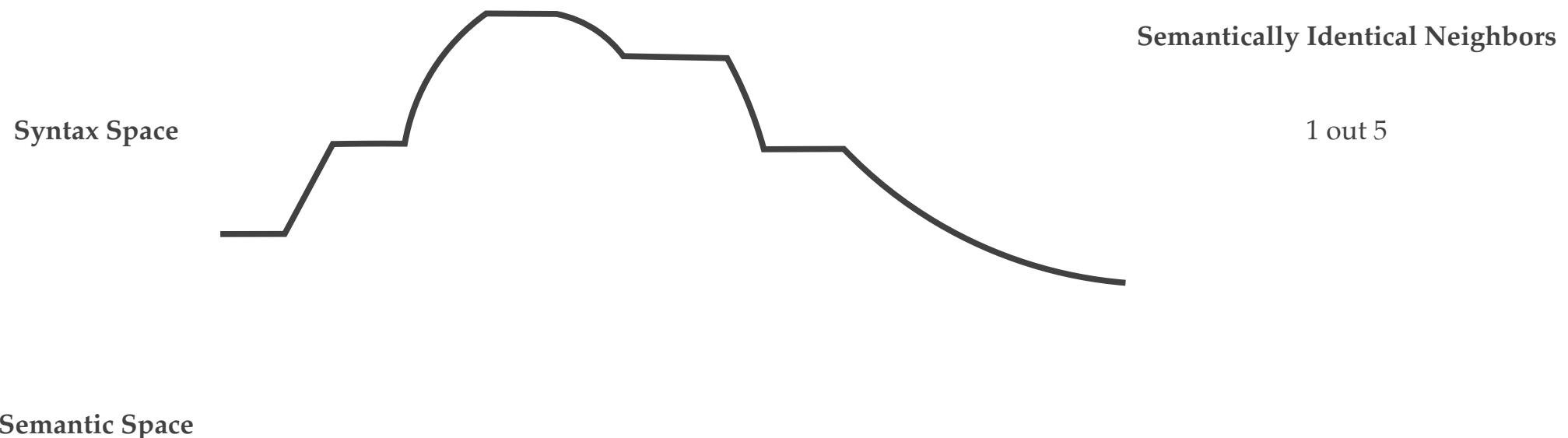
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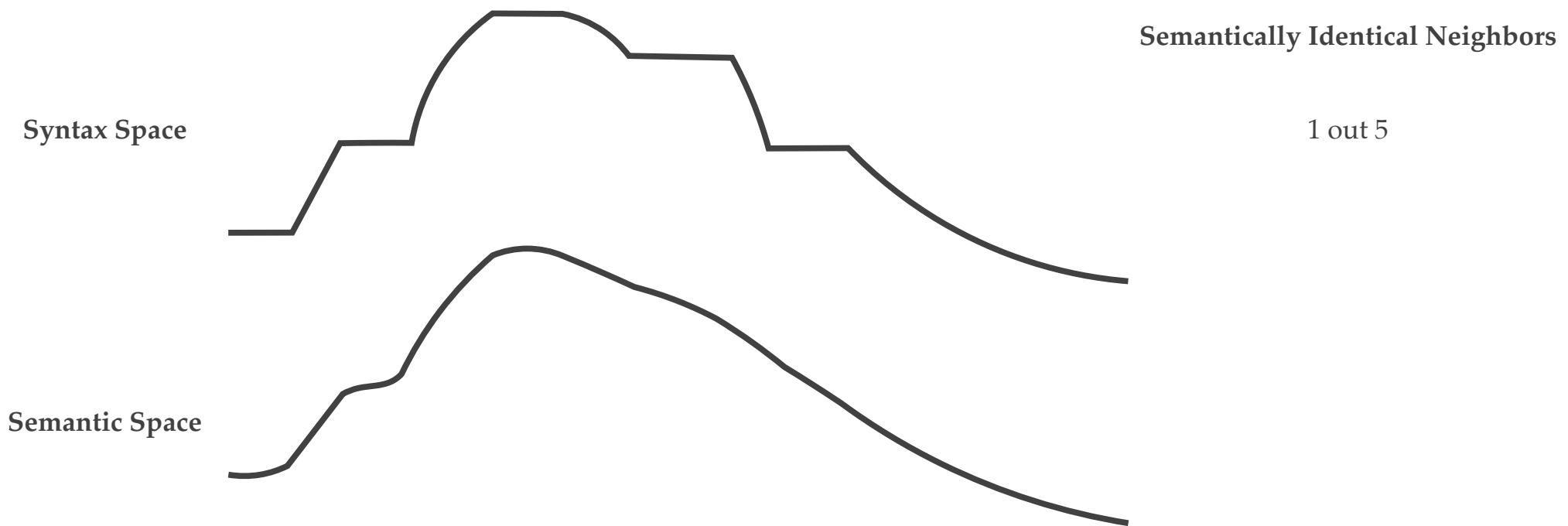
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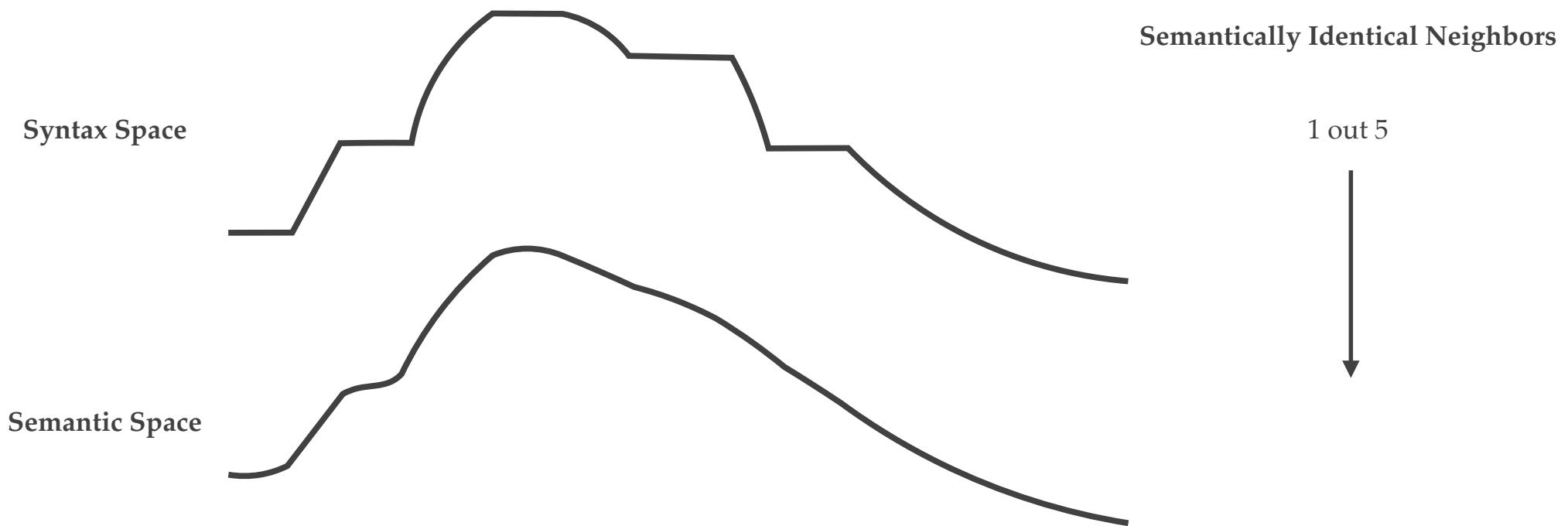
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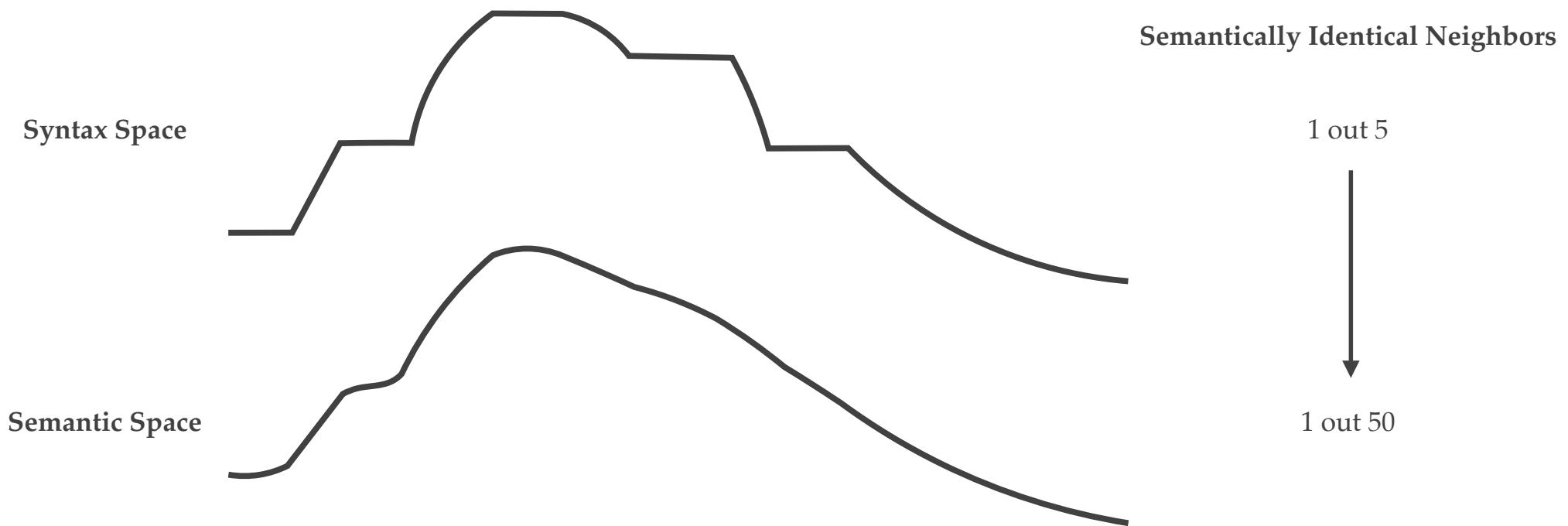
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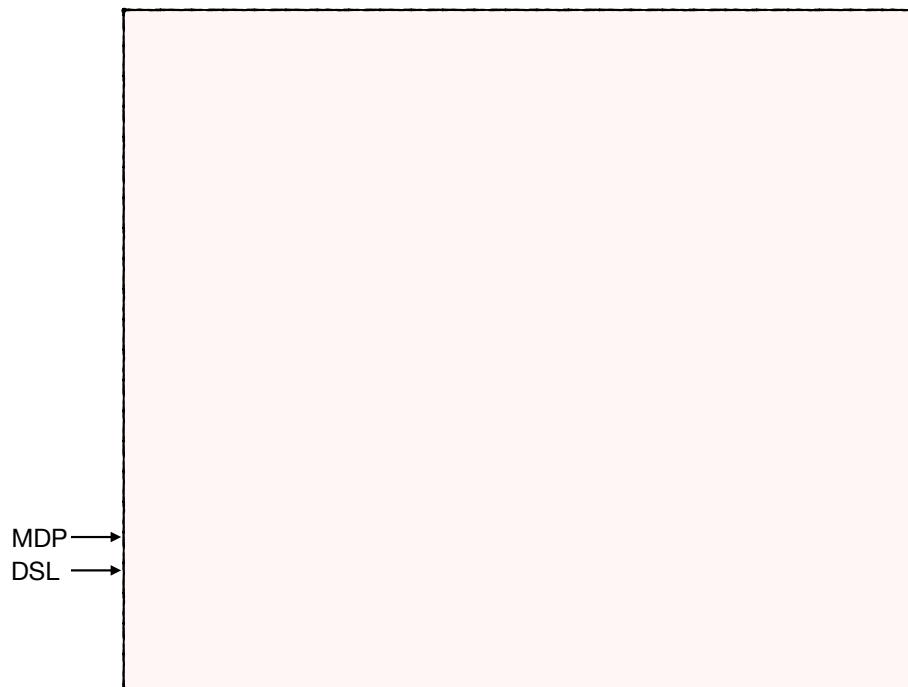
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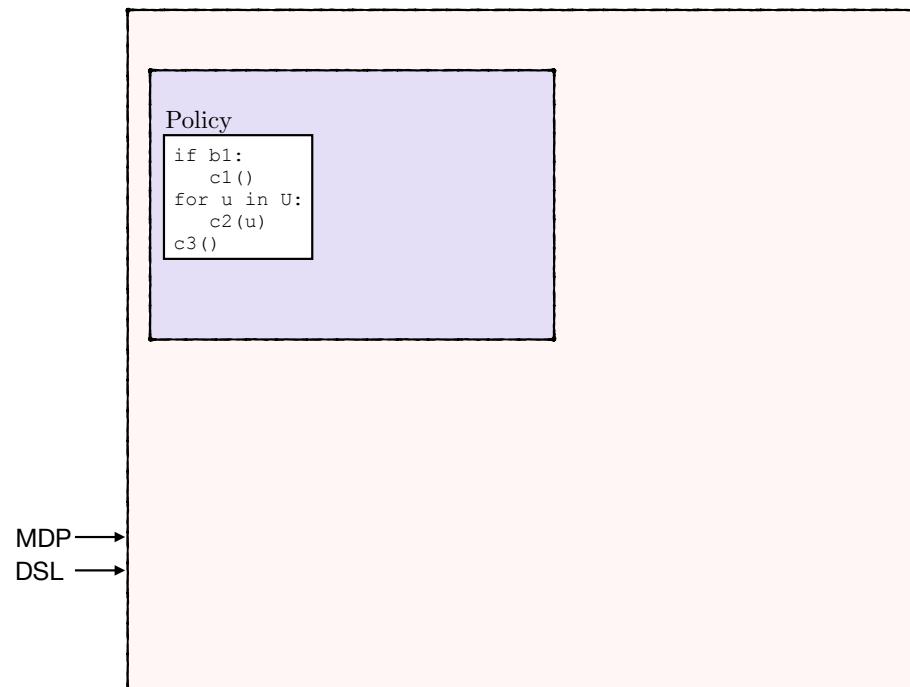
Library-Induced Semantic Spaces



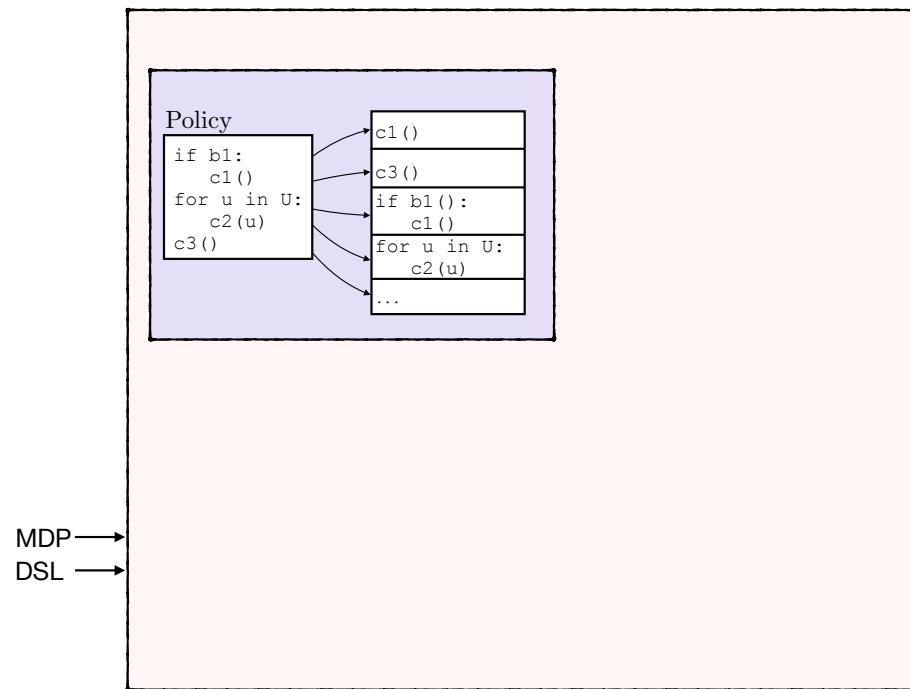
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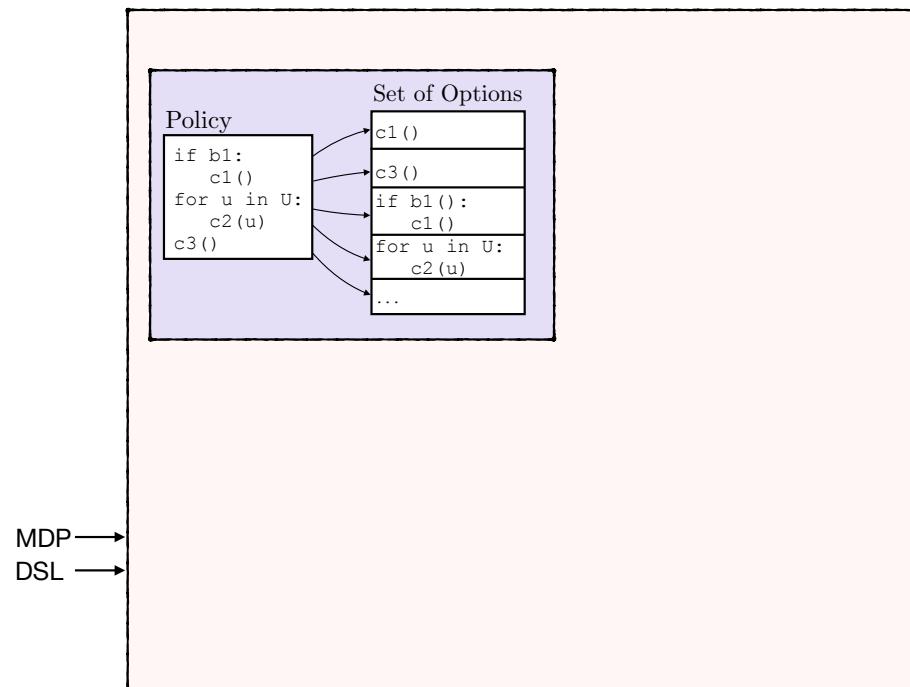
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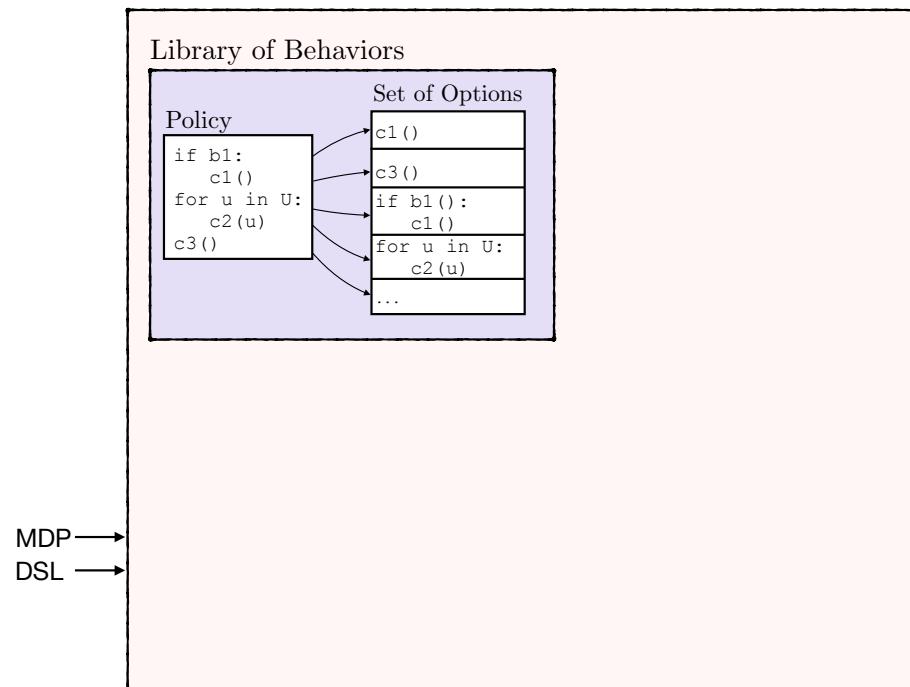
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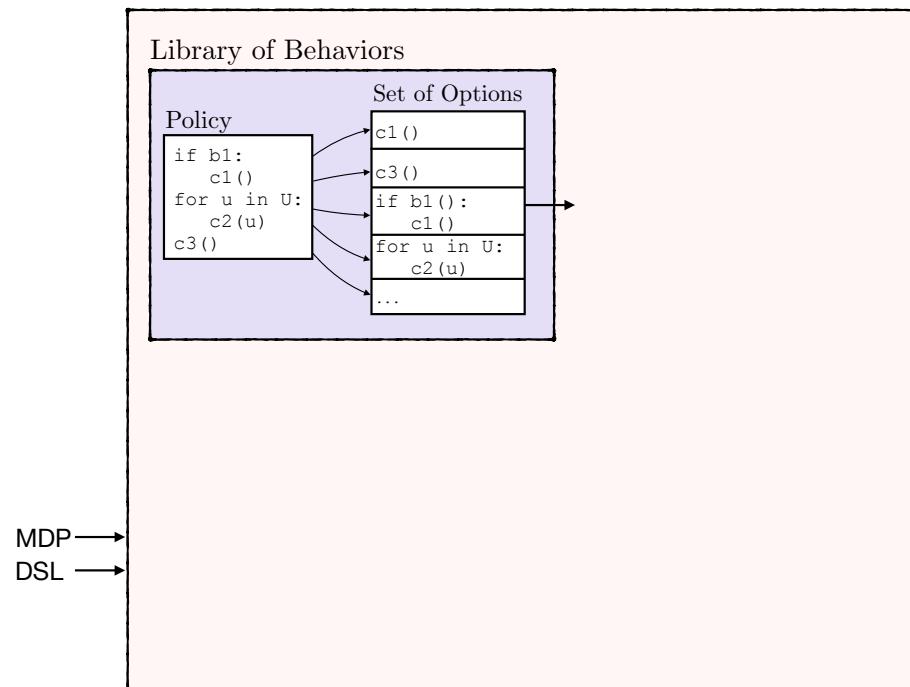
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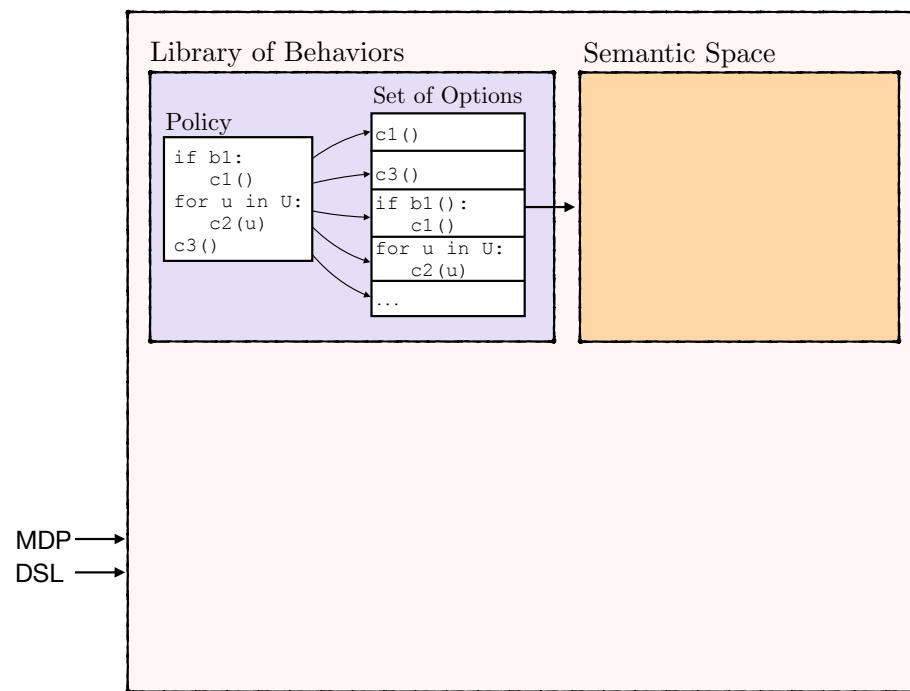
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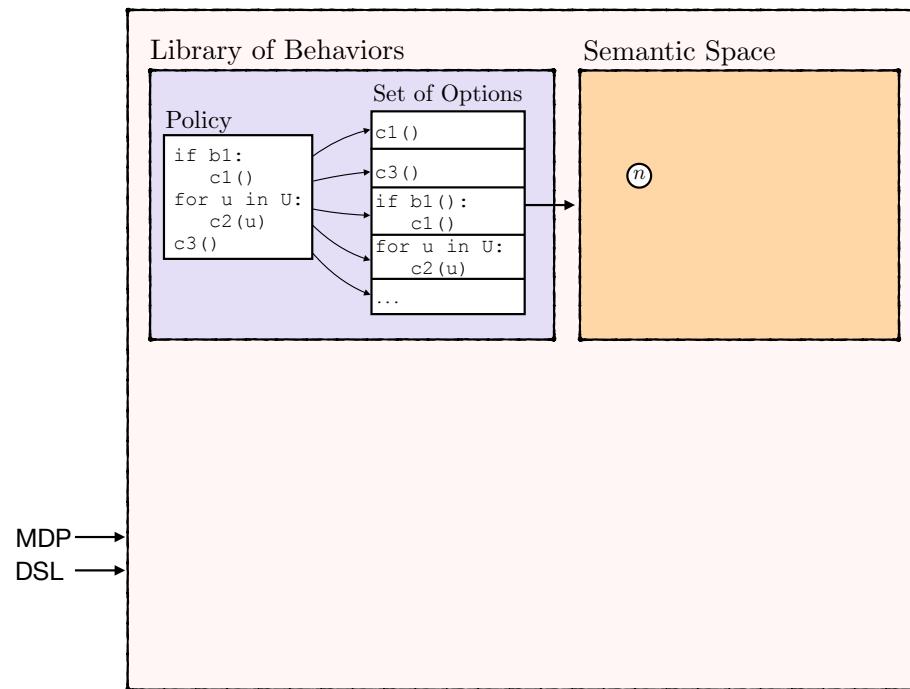
Library-Induced Semantic Spaces



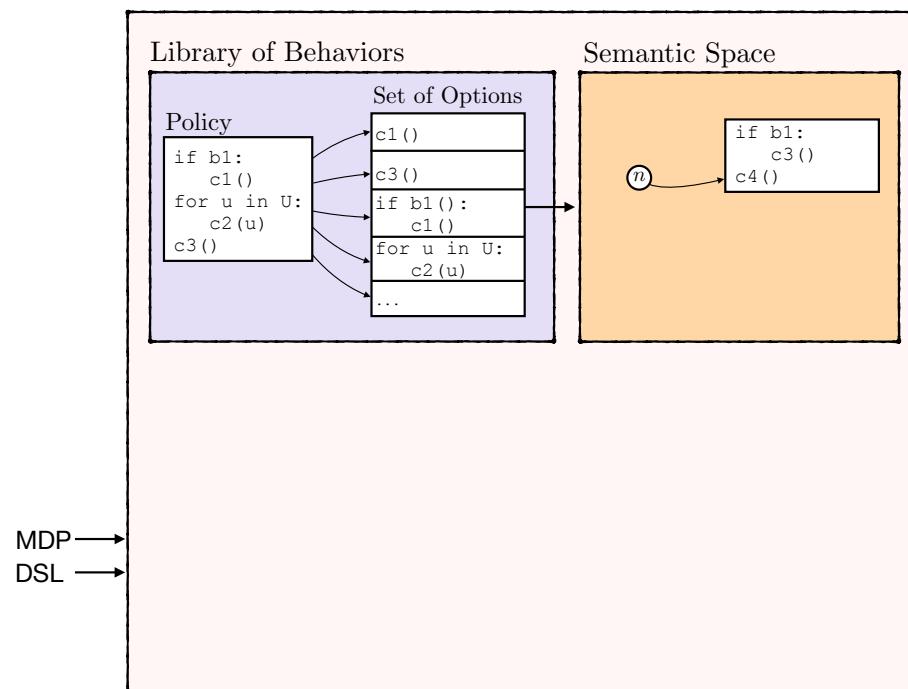
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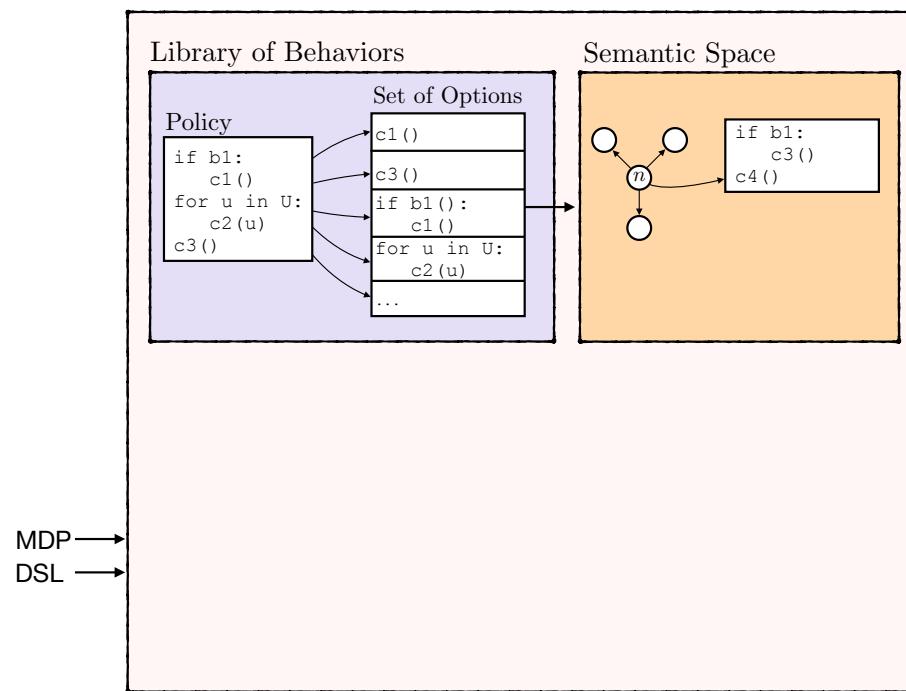
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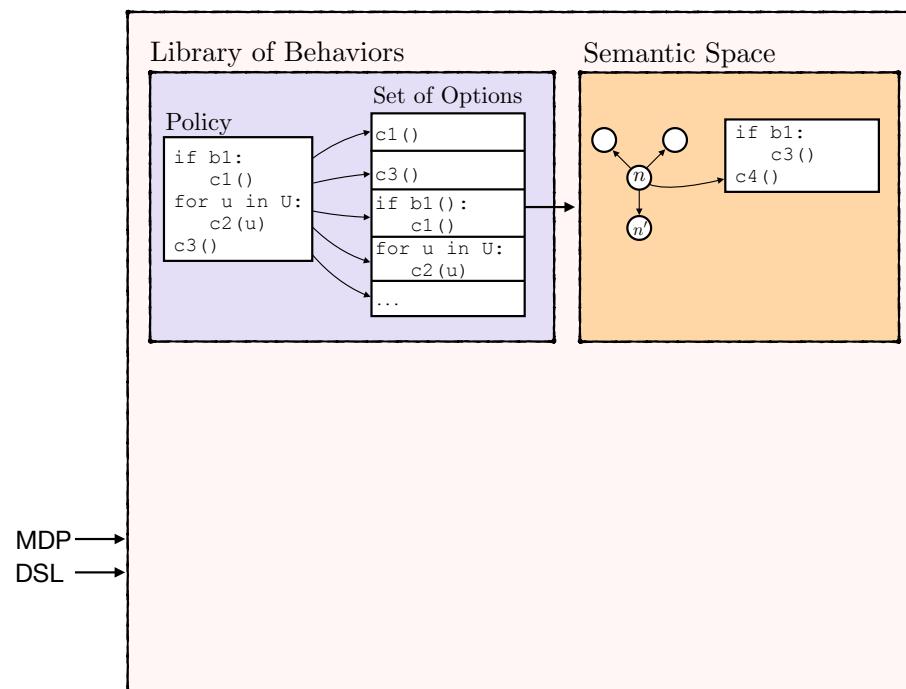
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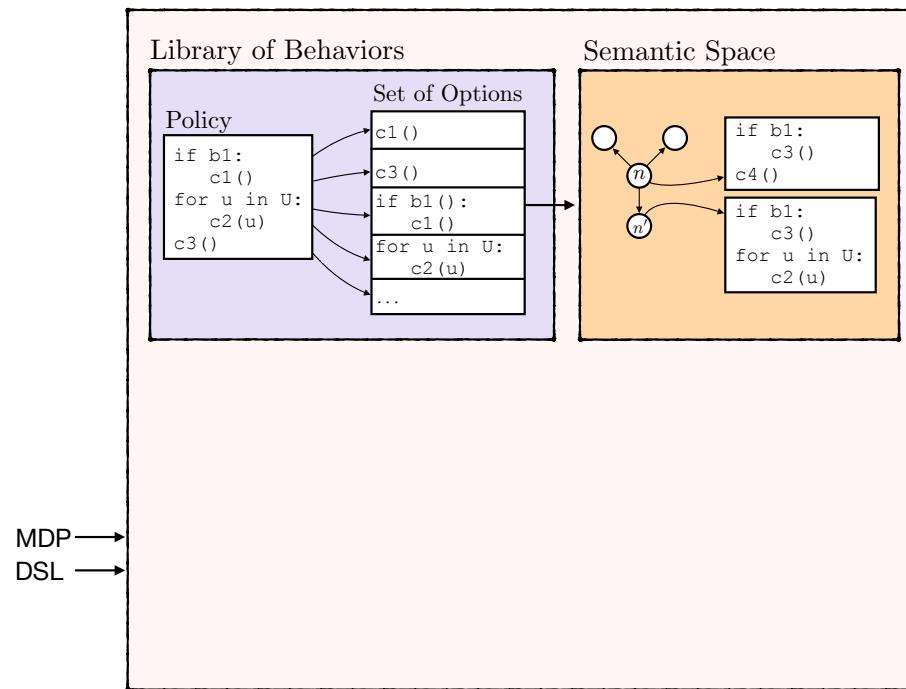
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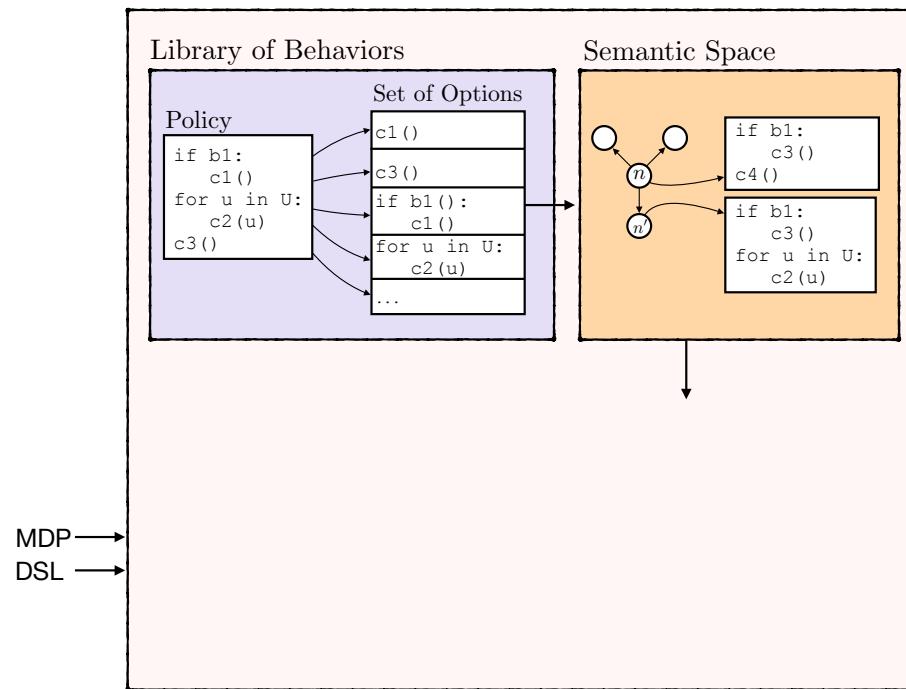
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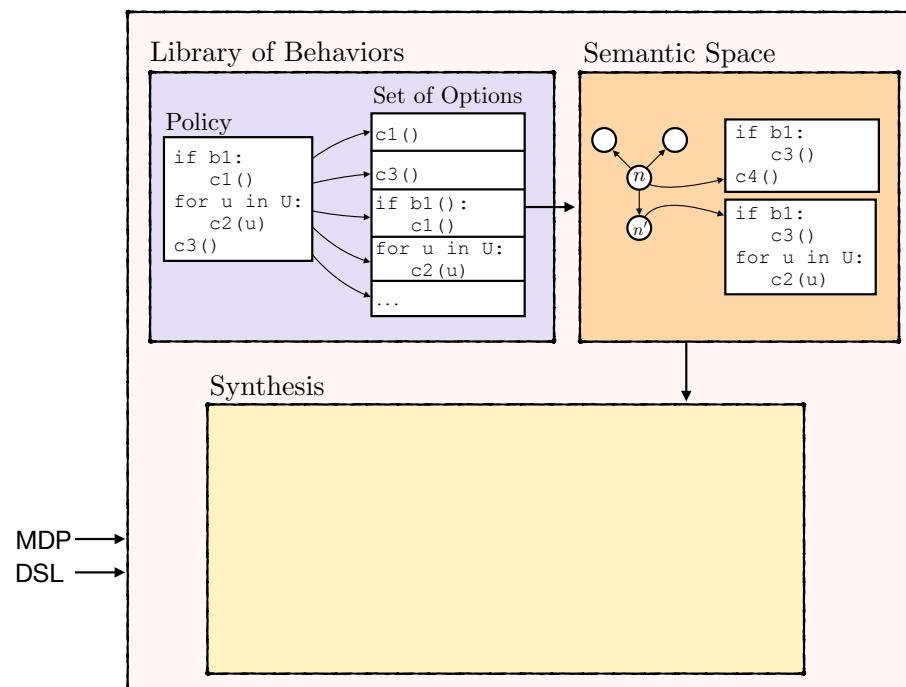
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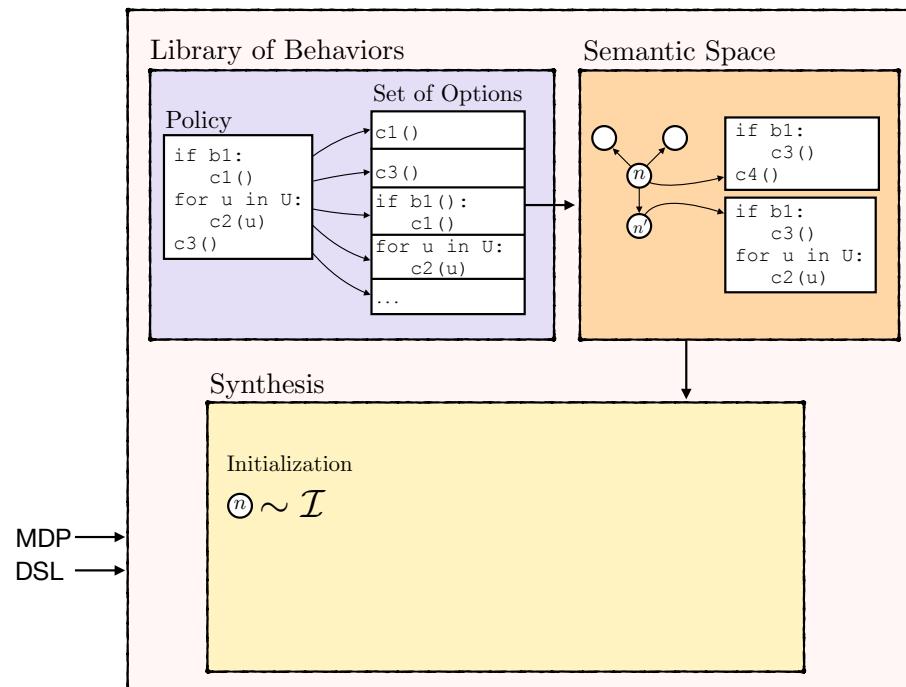
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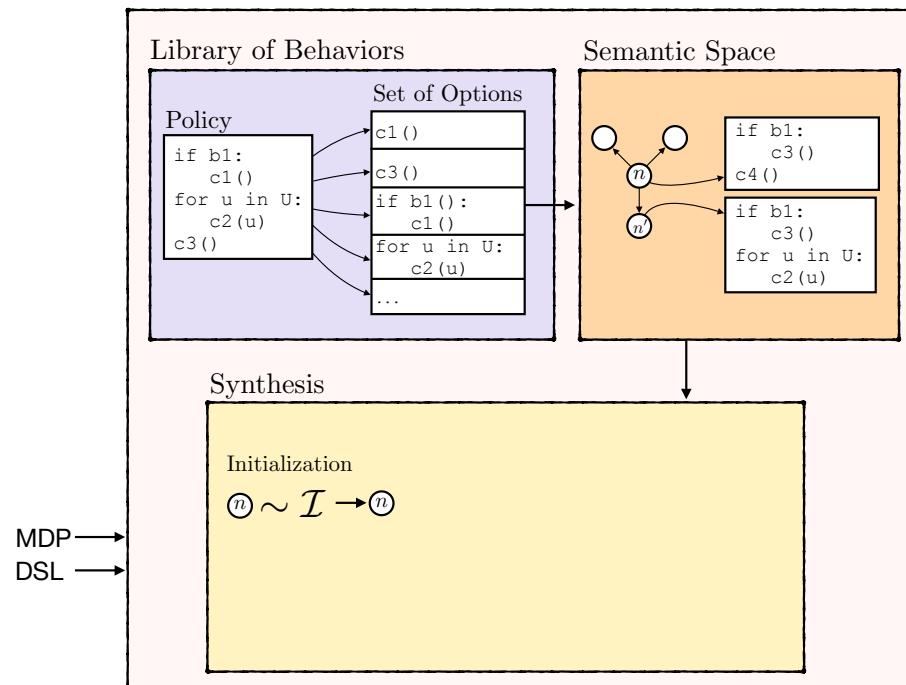
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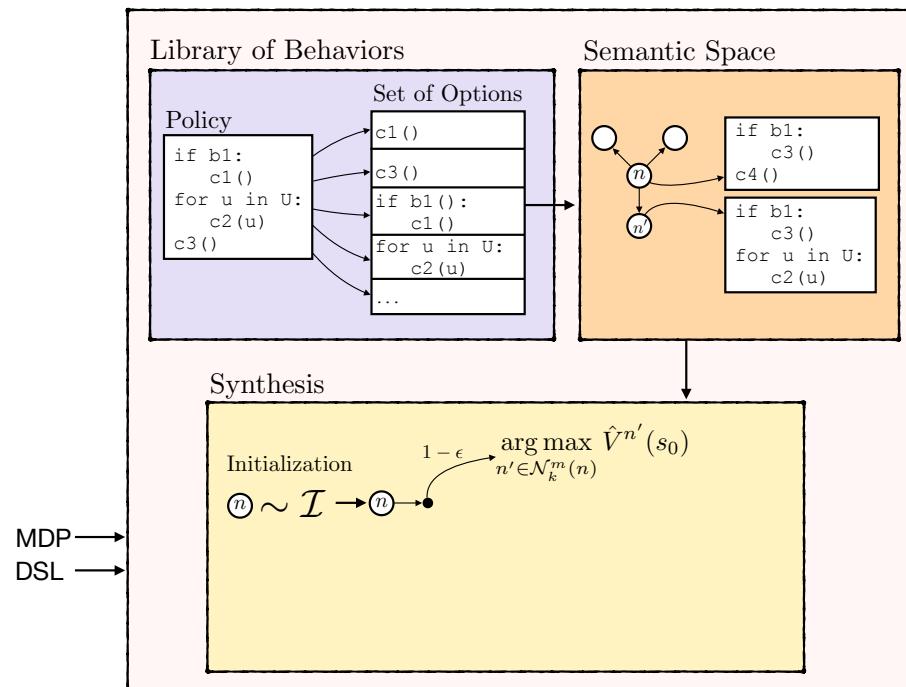
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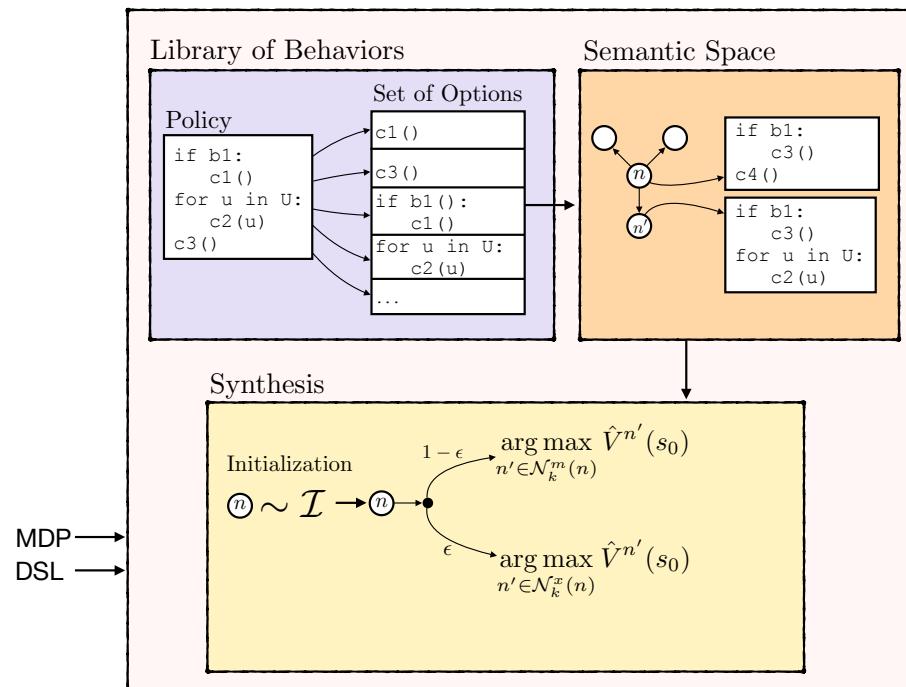
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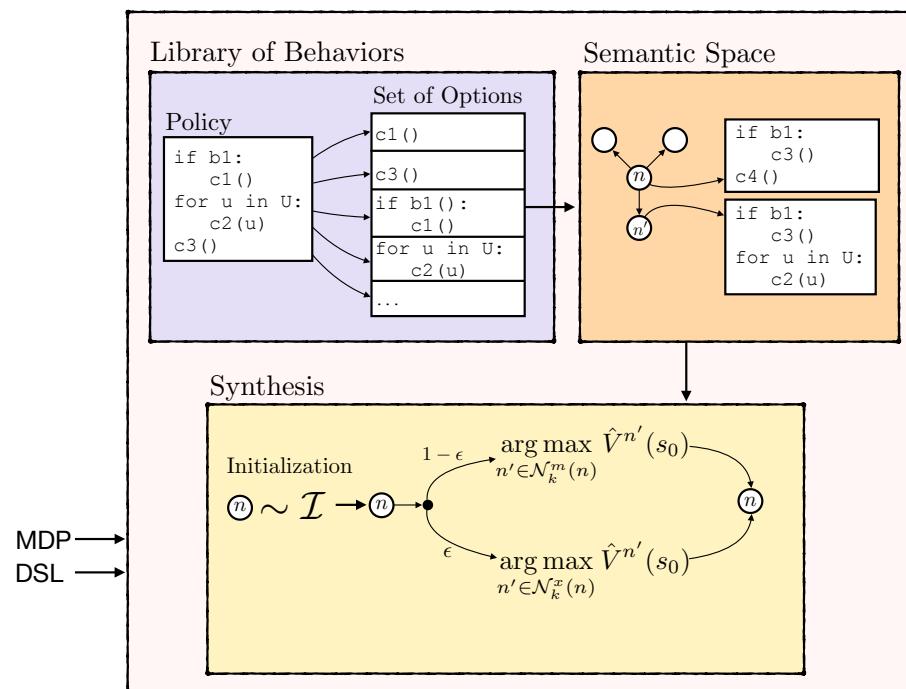
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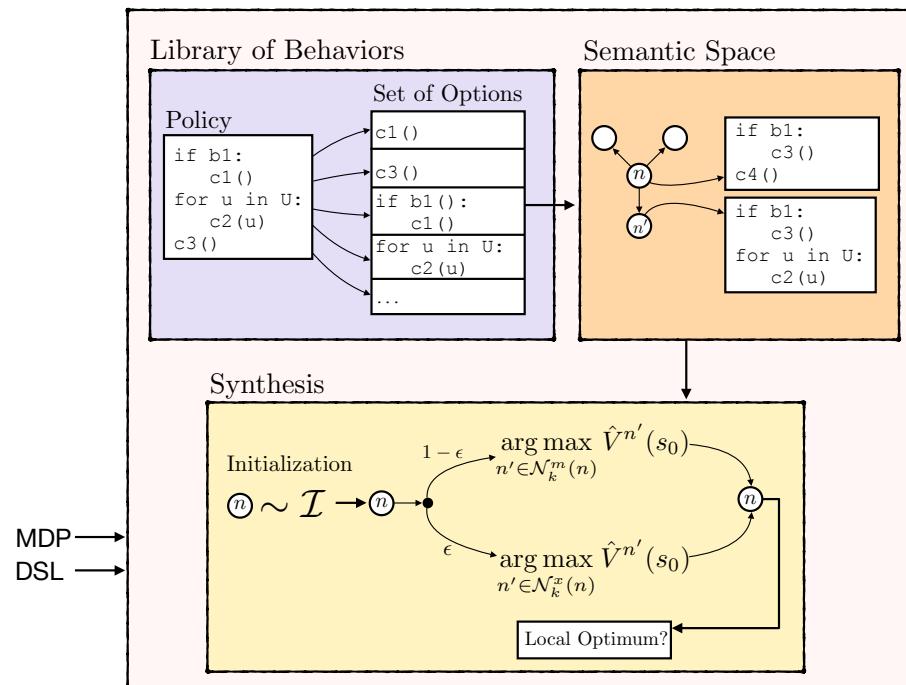
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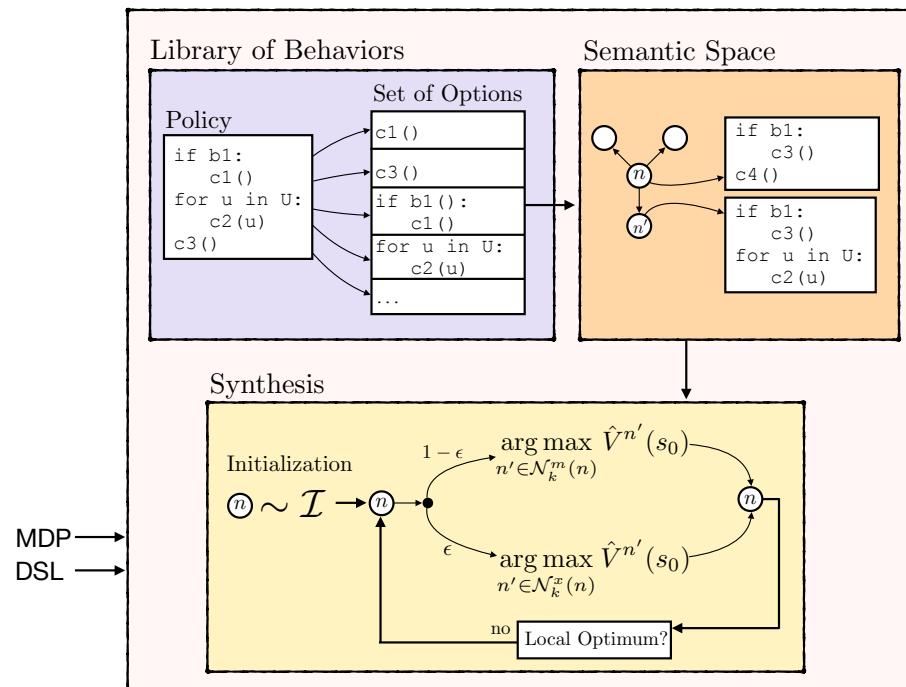
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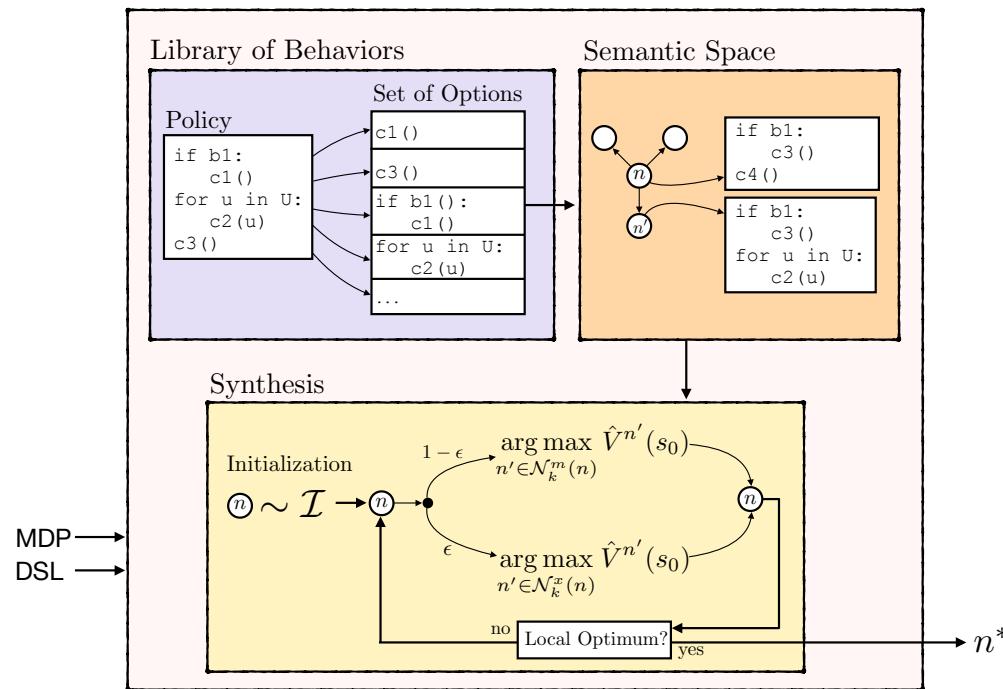
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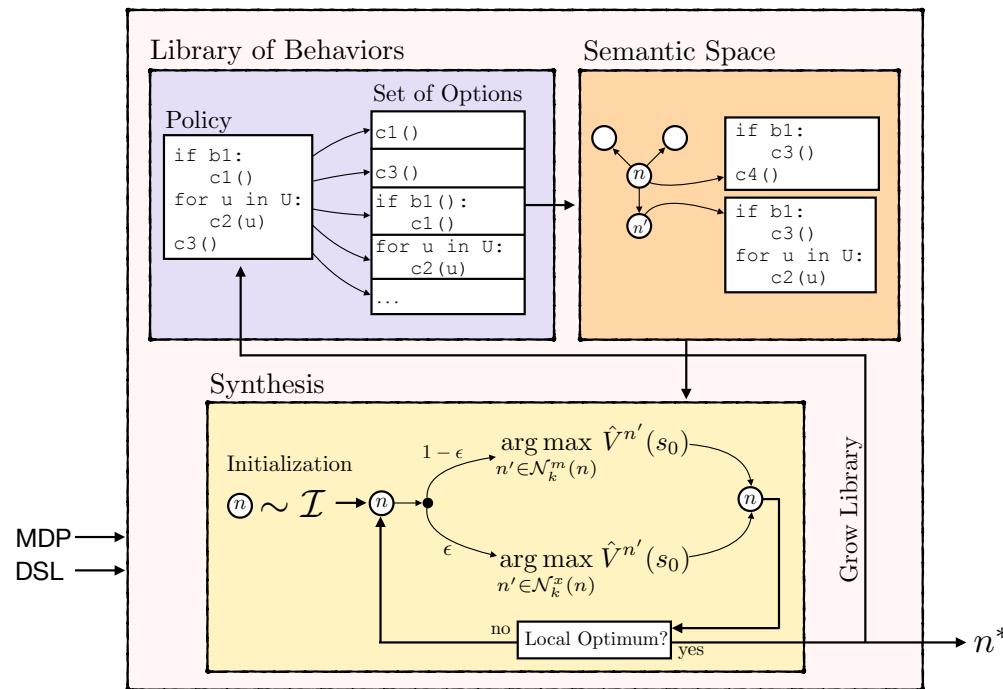
Library-Induced Semantic Spaces



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- ❖ Semantic spaces are more conducive to search.
 - ❖ “*give me the next behavior*”
- ❖ LLMs can give “innate” abilities to agents.
- ❖ **Future:** learning how to learn (recognizer in DreamCoder).

Learning Programs with Gradient Descent

```
# Sales data for two stores
store_1_sales = [120.0, 250.5, 310.0, 95.0]
store_2_sales = [200.0, 150.0, 275.0, 100.0]

# Process data for Store 1
store_1_total = sum(store_1_sales)
if store_1_total > 500:
    store_1_total *= 0.9 # Apply a 10% discount
store_1_report = f"Store 1 Total Sales: ${store_1_total:.2f}"

# Process data for Store 2
store_2_total = sum(store_2_sales)
if store_2_total > 500:
    store_2_total *= 0.9 # Apply a 10% discount
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print(store_1_report)
print(store_2_report)
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Learning Programs with Gradient Descent

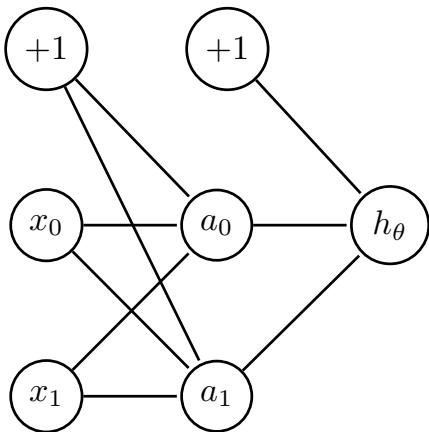
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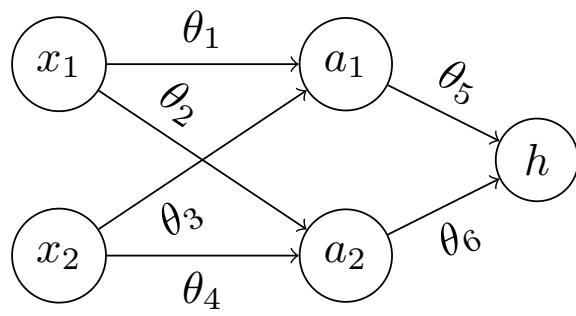
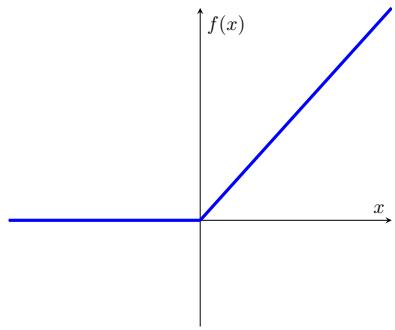


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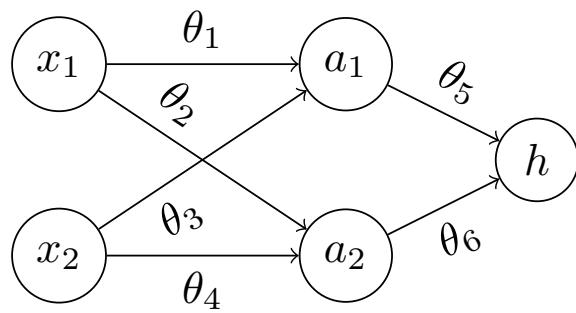
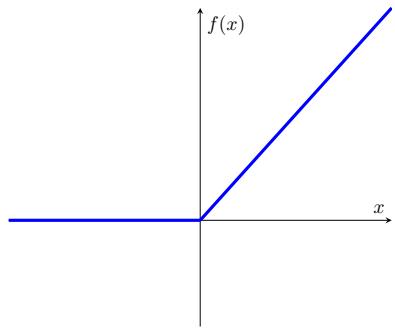
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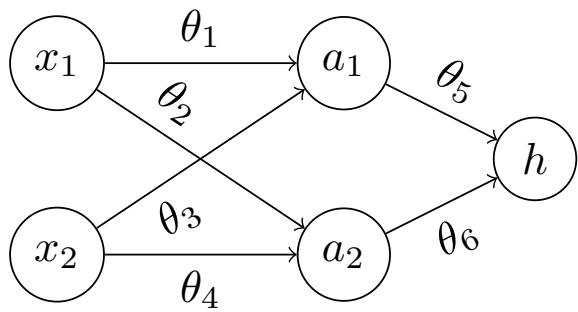
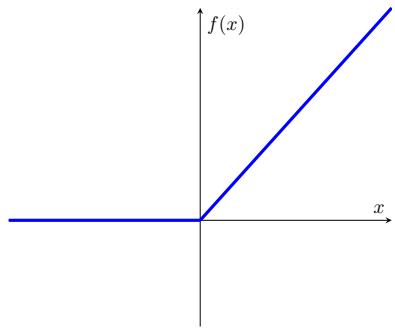
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Orfanos & Lelis (2023)

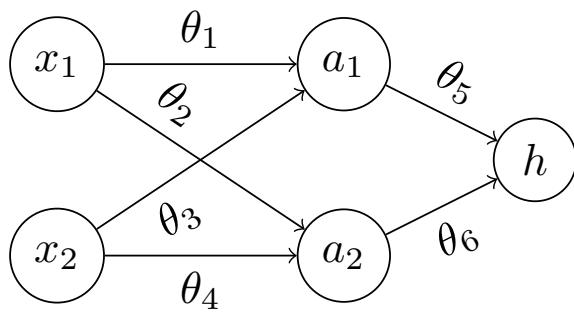
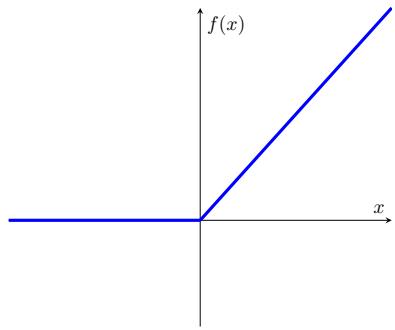


a_1 can be either $x_1\theta_1 + x_2\theta_3$ or 0



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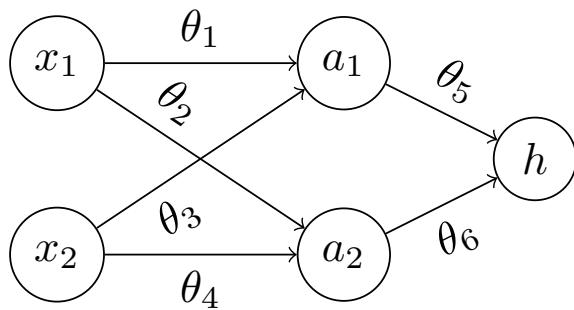
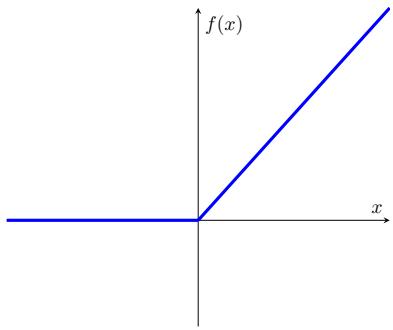
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if $a_1 = x_1\theta_1 + x_2\theta_3$ and $a_2 = x_1\theta_2 + x_2\theta_4$ then



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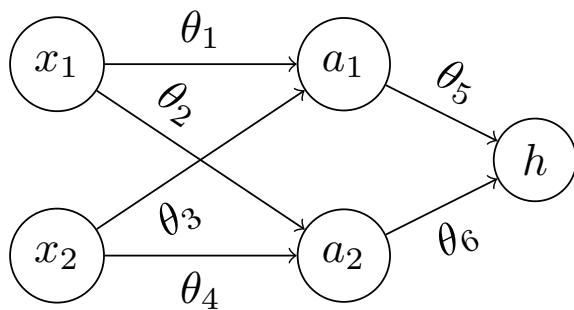
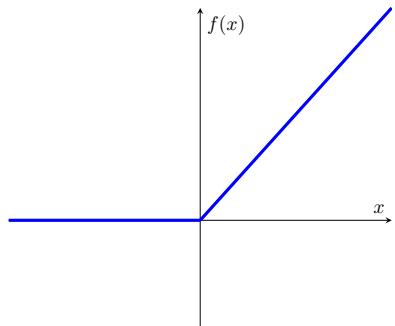
if $a_1 = x_1\theta_1 + x_2\theta_3$ and $a_2 = x_1\theta_2 + x_2\theta_4$ then

$$h = \theta_5 a_1 + \theta_6 a_2$$

$$= \theta_5(x_1\theta_1 + x_2\theta_3) + \theta_6(x_1\theta_2 + x_2\theta_4)$$

$$= x_1(\theta_5\theta_1 + \theta_6\theta_2) + x_2(\theta_5\theta_2 + \theta_6\theta_4)$$

$$= x_1\theta' + x_2\theta''$$



The network above is equivalent to:

if $a_1 = x_1\theta_1 + x_2\theta_3$ and $a_2 = x_1\theta_2 + x_2\theta_4$ then

$$h = \theta_5 a_1 + \theta_6 a_2$$

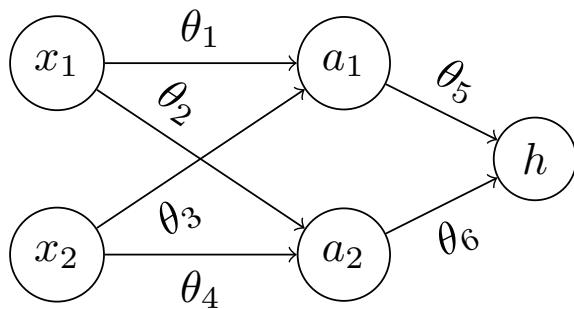
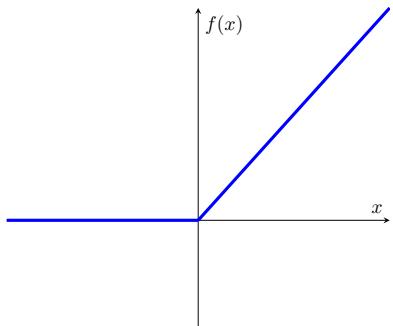
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$$= x_1(\theta_5\theta_1 + \theta_6\theta_2) + x_2(\theta_5\theta_2 + \theta_6\theta_4)$$

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a_1 can be either $x_1\theta_1 + x_2\theta_3$ or 0

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a_1 can be either $x_1\theta_1 + x_2\theta_3$ or 0

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The network above is equivalent to:

if $x_1\theta_1 + x_2\theta_3 > 0$

if $x_1\theta_2 + x_2\theta_4 > 0$

then $x_1\theta' + x_2\theta''$

else ...

...

if $a_1 = x_1\theta_1 + x_2\theta_3$ and $a_2 = x_1\theta_2 + x_2\theta_4$ then

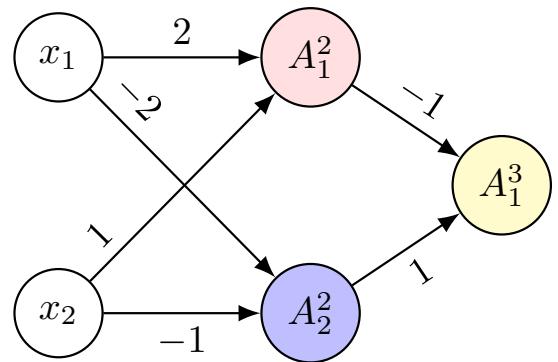
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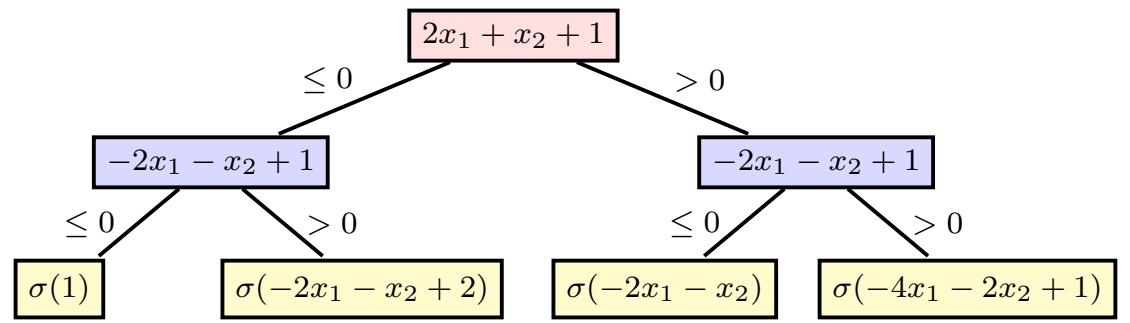
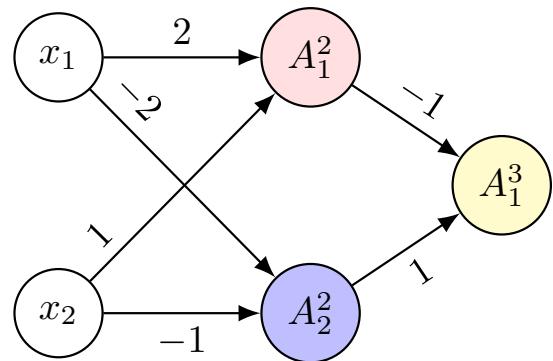
$$= x_1(\theta_5\theta_1 + \theta_6\theta_2) + x_2(\theta_5\theta_2 + \theta_6\theta_4)$$

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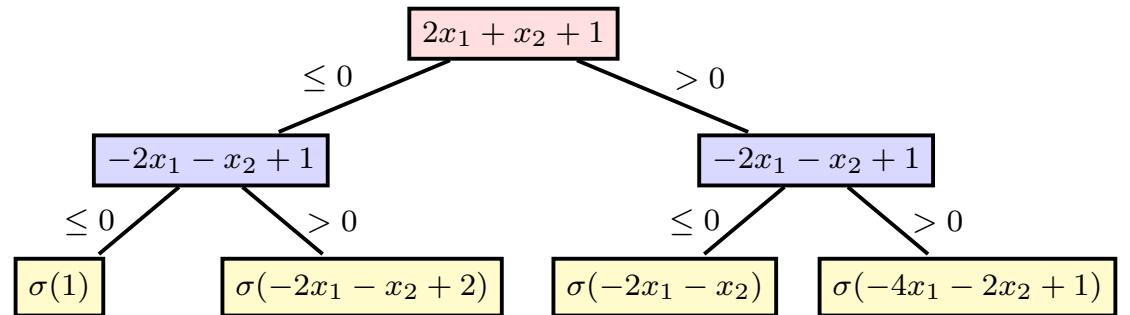
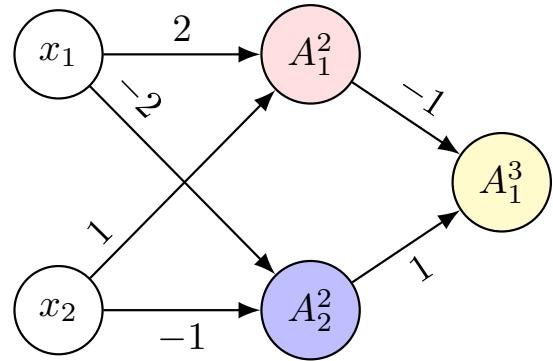
Neural Trees



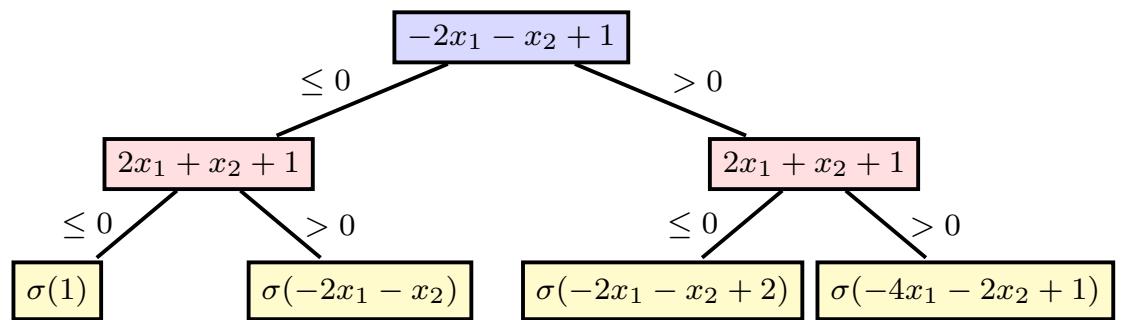
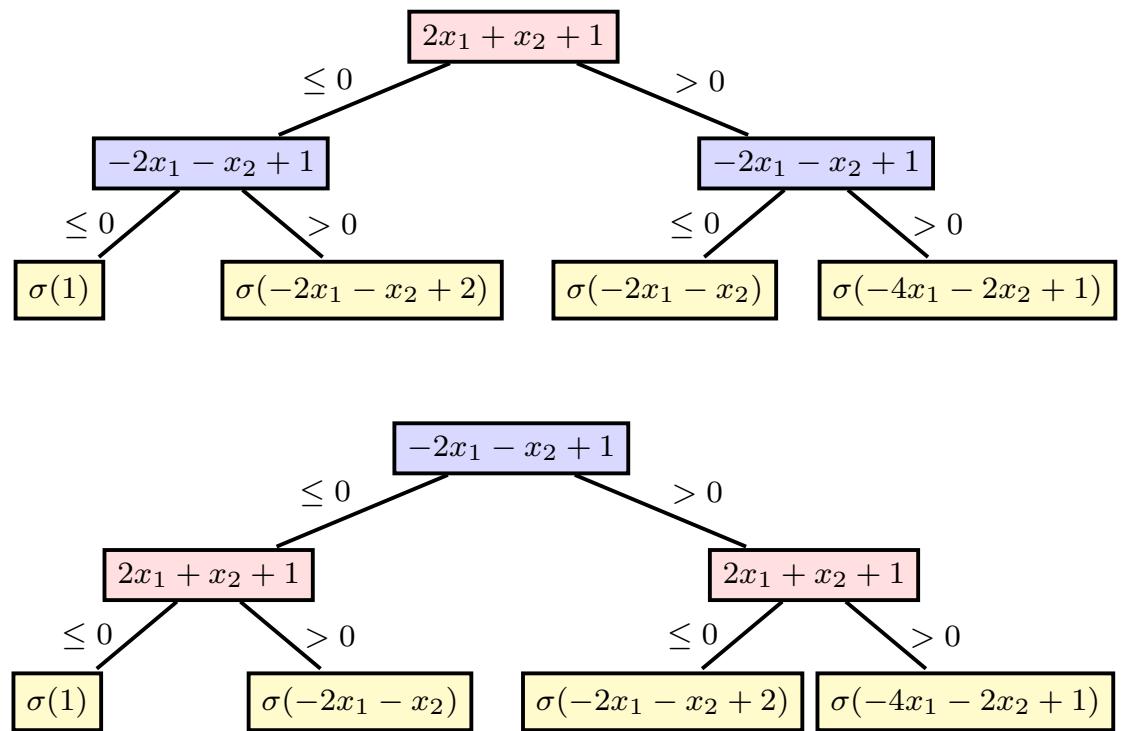
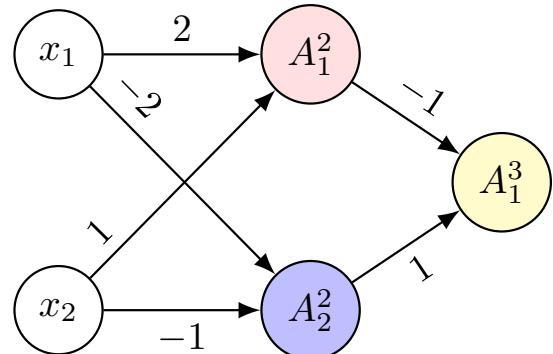
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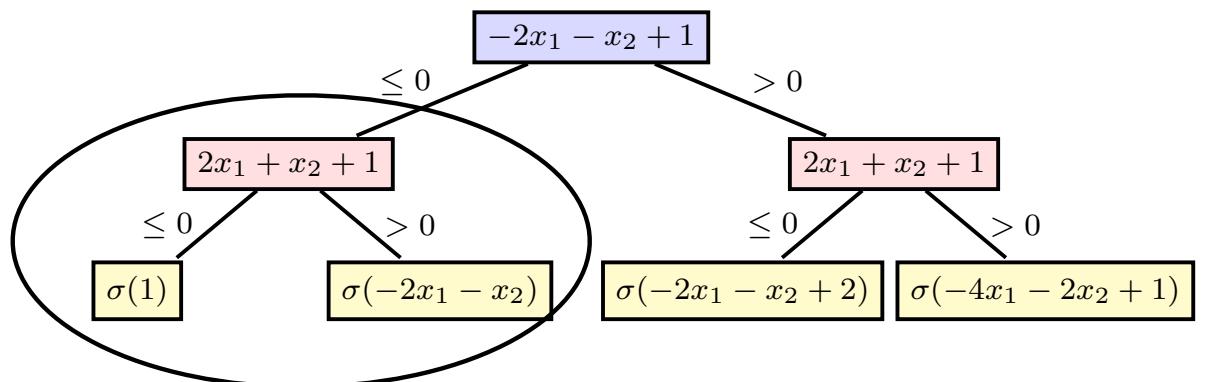
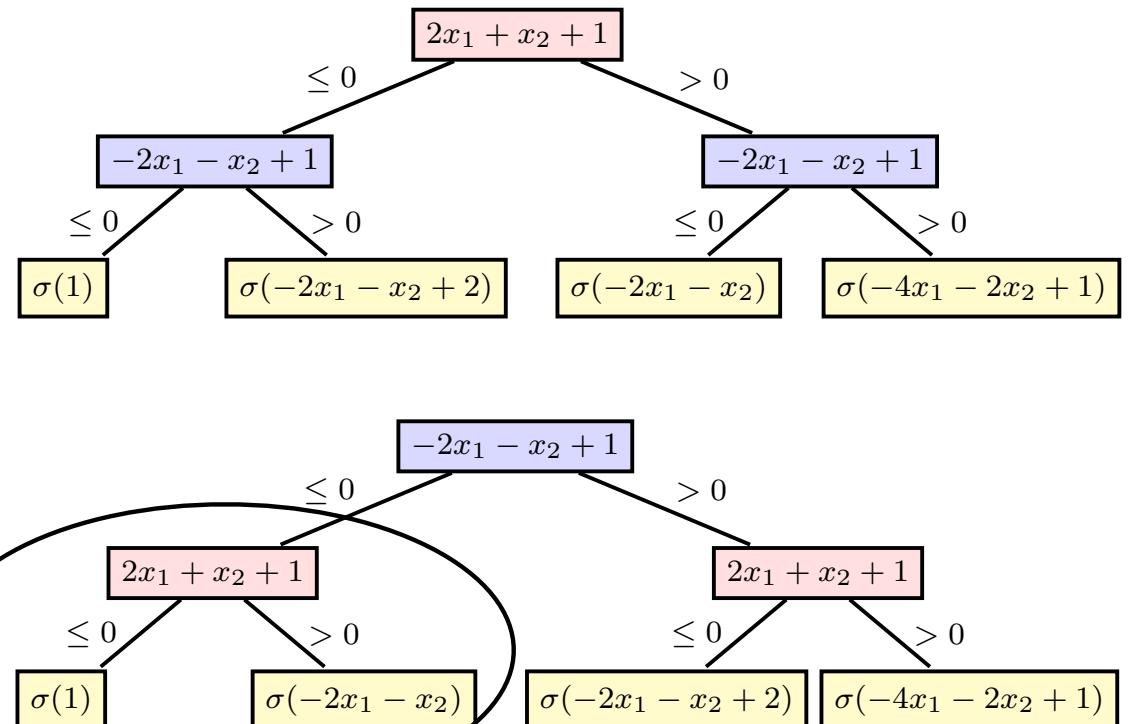
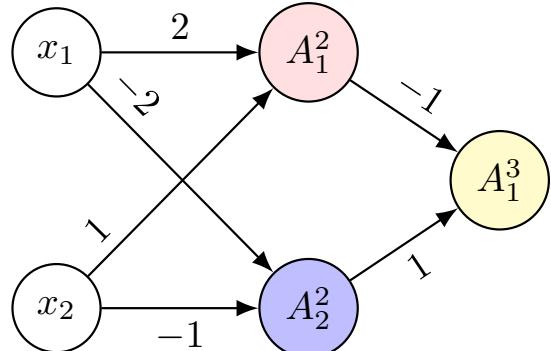
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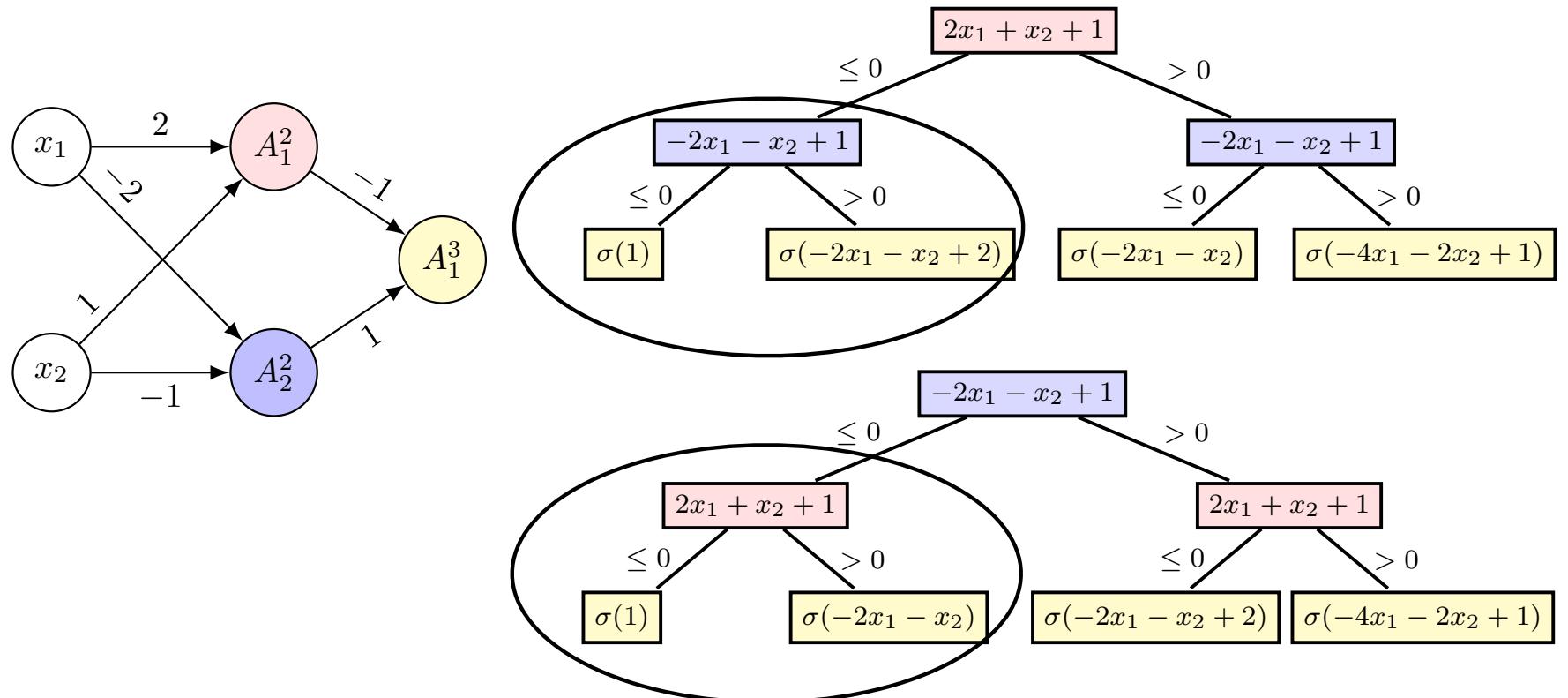
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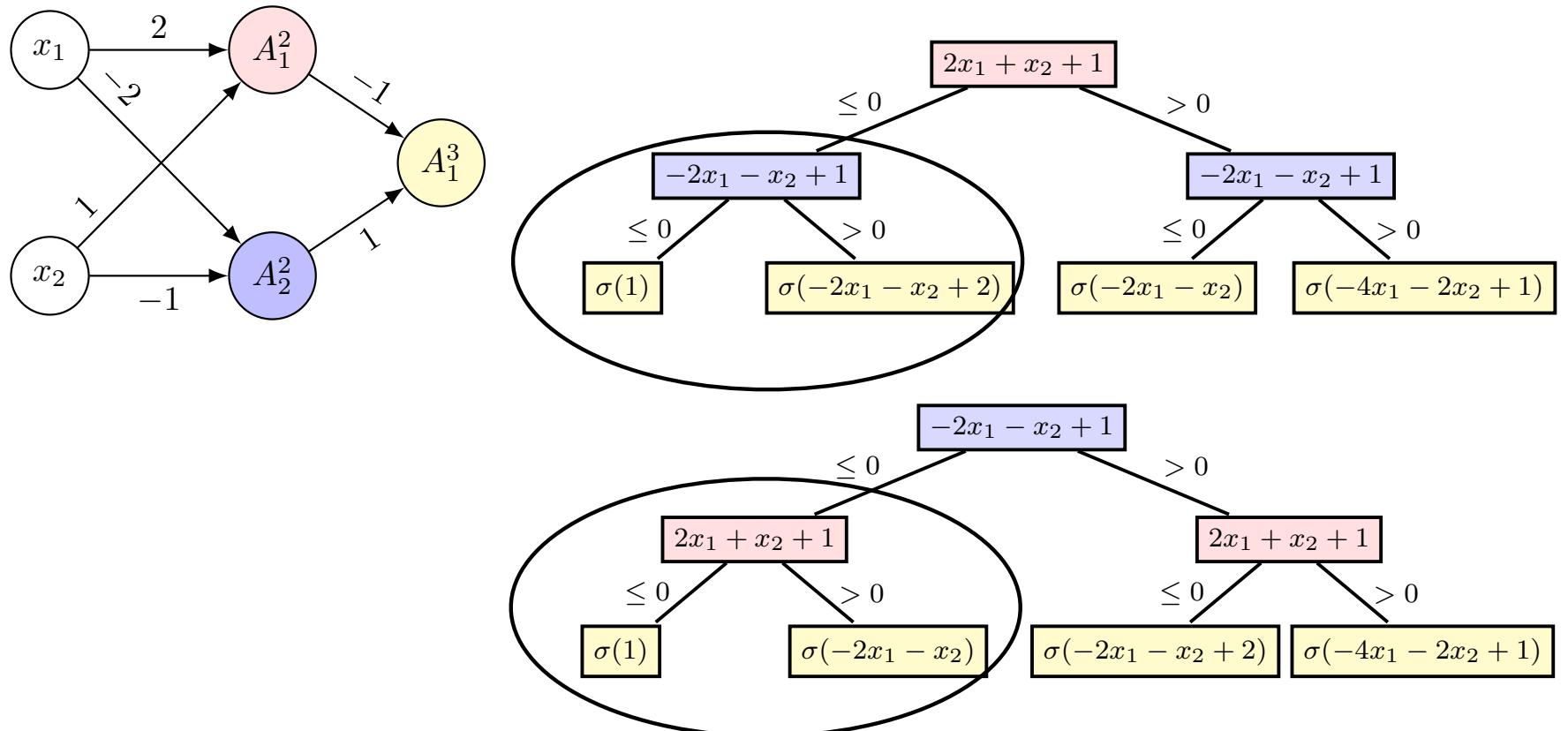
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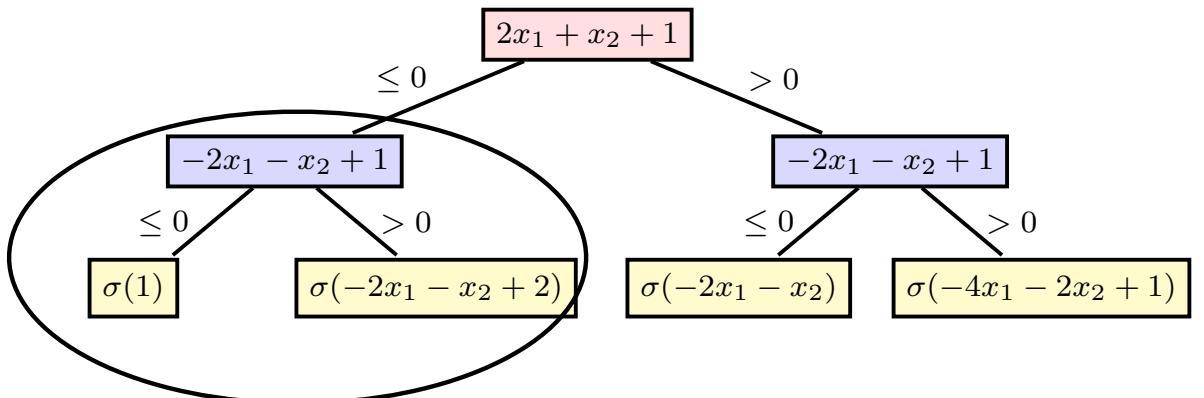
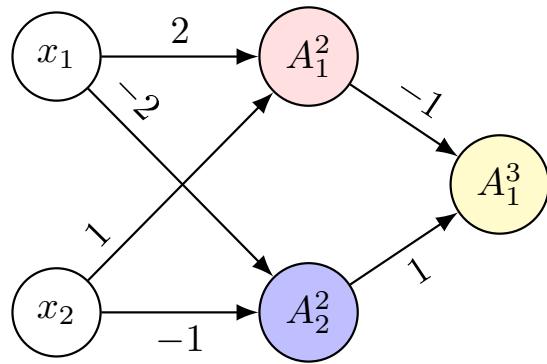
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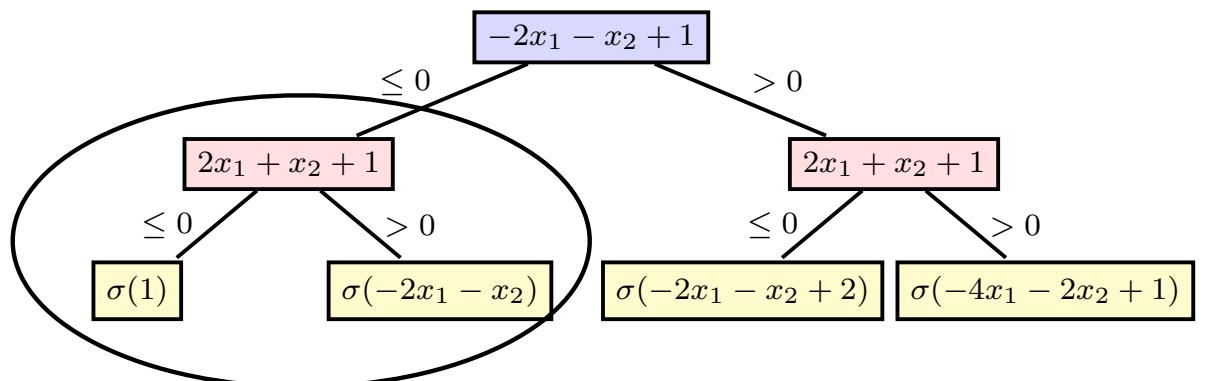
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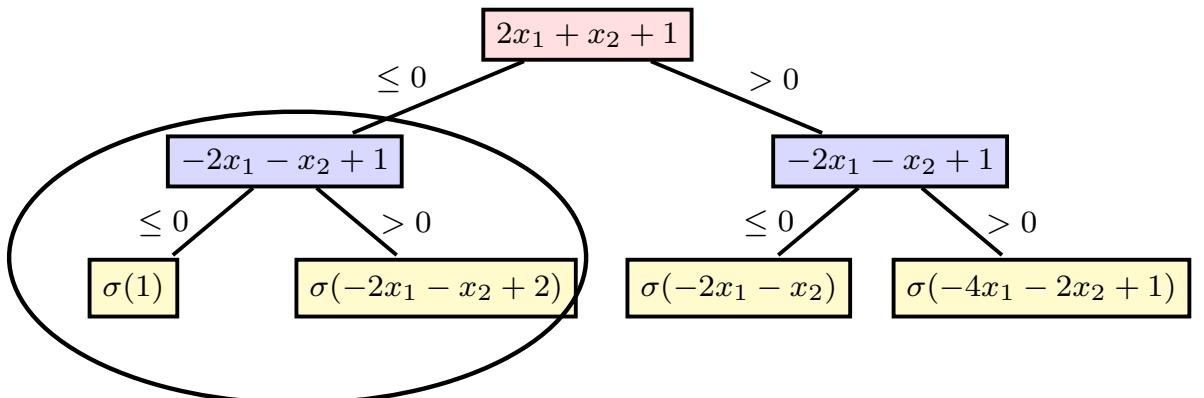
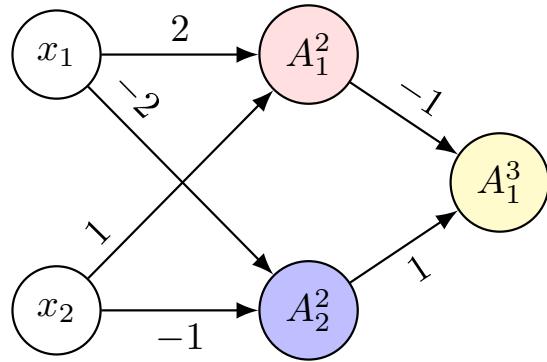
Neural Trees



Three possibilities for each neuron:

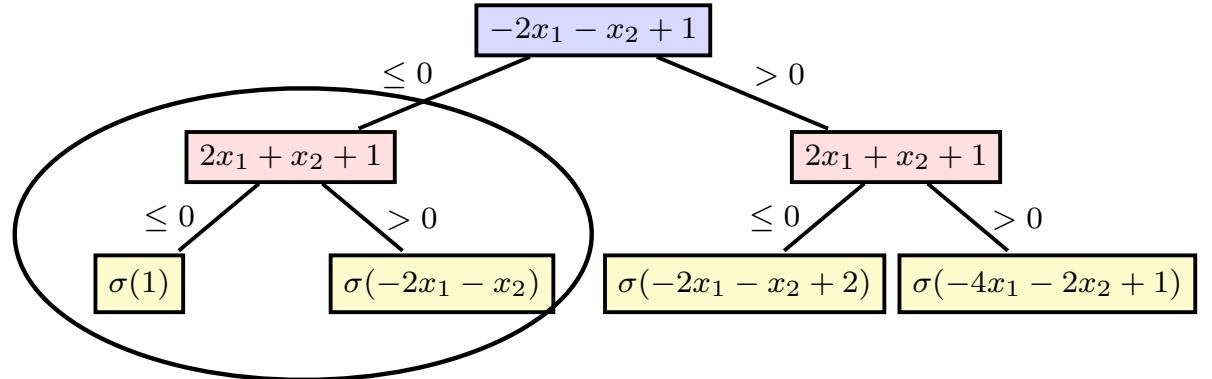


Neural Trees

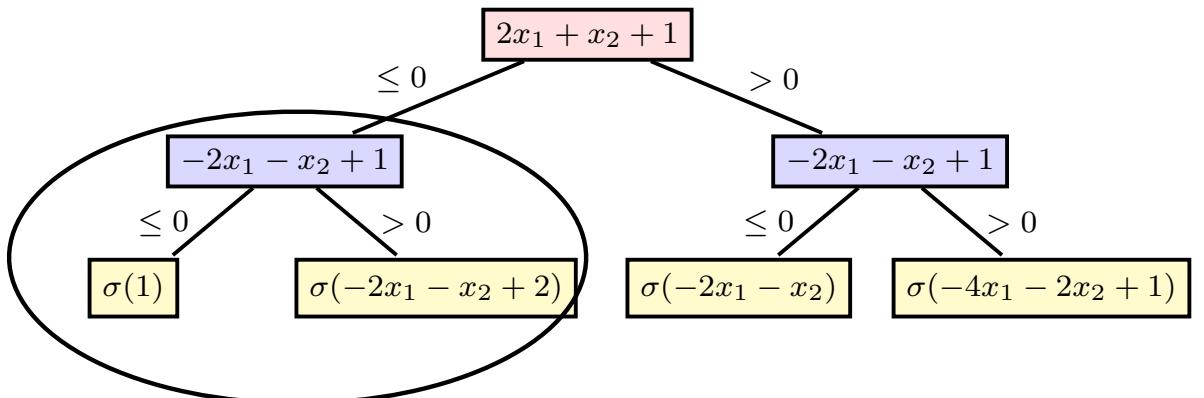
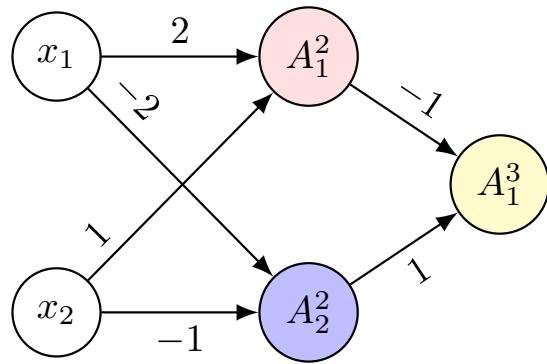


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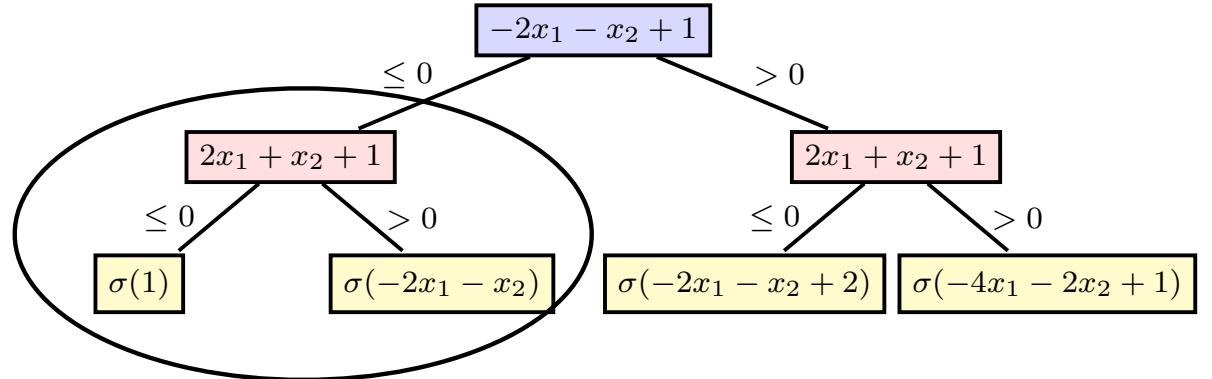


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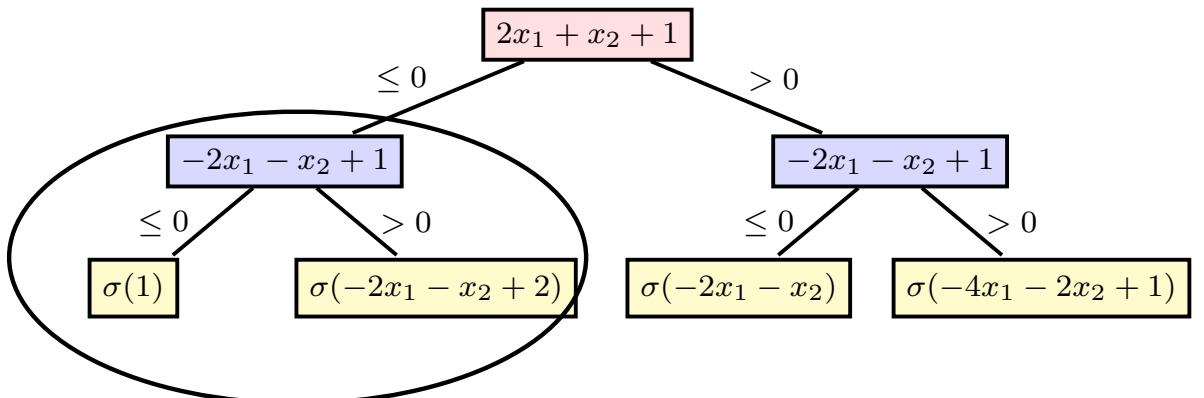
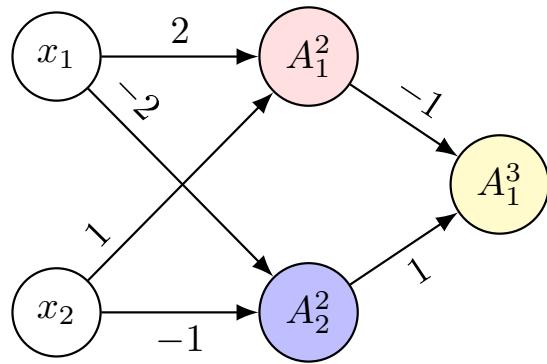


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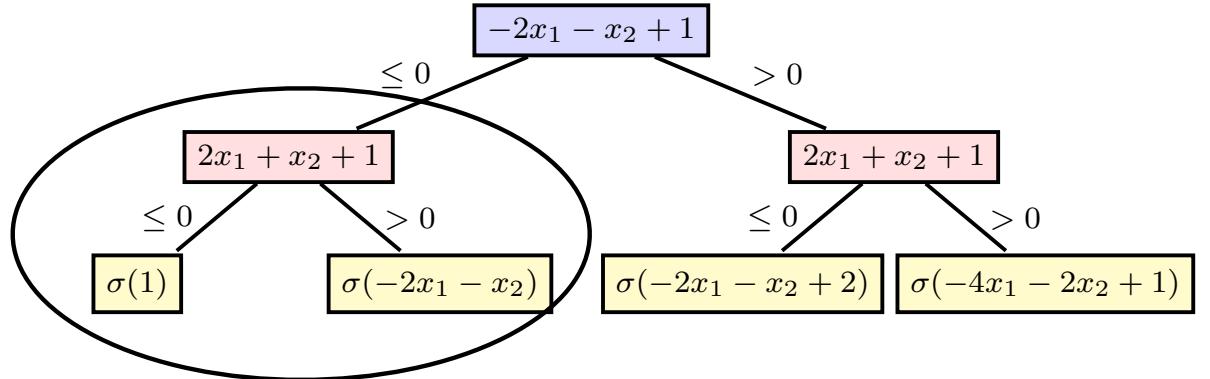


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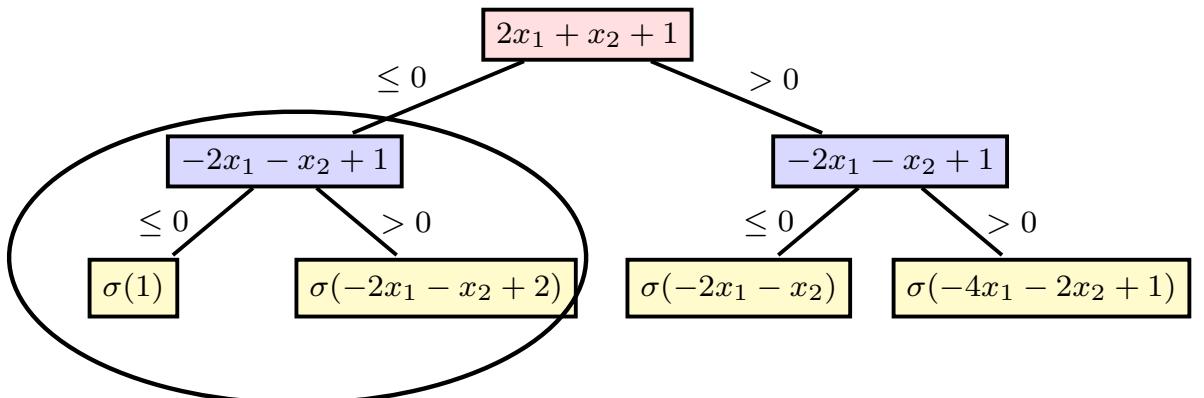
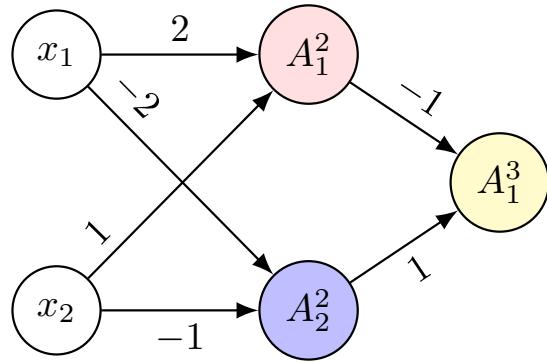


Three possibilities for each neuron:

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3. Part of the program



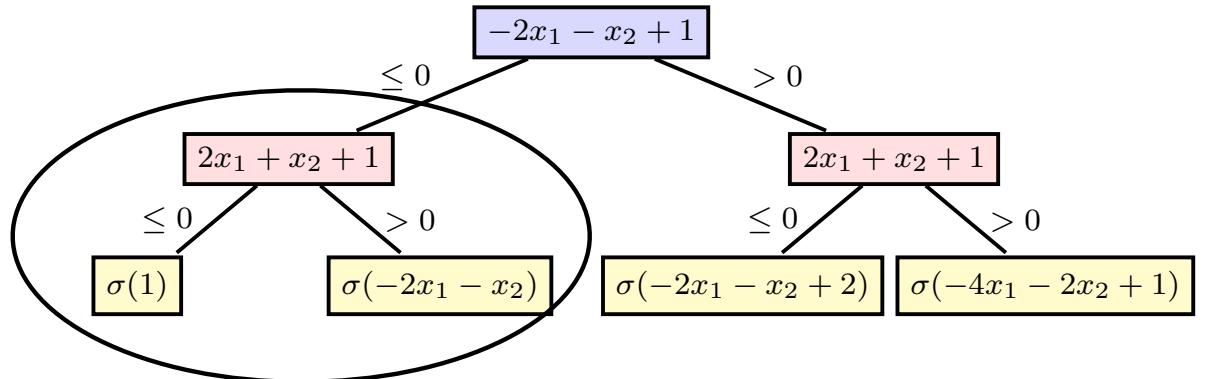
Neural Trees



Three possibilities for each neuron:

1. Inactive
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3. Part of the program

For N hidden neurons, 3^N subprograms.



Two Effects of a Growing Library

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- ❖ Evaluates all programs. :-(

Levin Loss

$$\frac{d(n)}{\pi(n)}$$

Orseau et al. (2018)

Levin Loss

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$\frac{1}{\pi(n)}$ is the expected of number of samples to observe n .

Orseau et al. (2018)

$$\frac{d(n)}{\pi(n)}$$

$\frac{1}{\pi(n)}$ is the expected number of samples to observe n .

$d(n)$ is the cost of each sample.

Orseau et al. (2018)

Selecting a Subset of Options

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- ❖ Iteratively select the option that minimizes the Levin loss.

Selecting a Subset of Options

- ❖ Iteratively select the option that minimizes the Levin loss.
- ❖ Stop when Levin loss goes up for the selected subset.

Dec-Options

Alikhasi & Lelis (2024)

Dec-Options

- ❖ Learn policy to solve some problems.

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- ❖ Select a sub-set of them to use as options.
- ❖ Use options in downstream tasks.

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2

	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M		M
	A M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M		M
	A M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M		M
	A M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M _A	
M		M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	A
M		M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M		A M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
M	A	M
	M	

Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2



	M	
A M		M
	M	

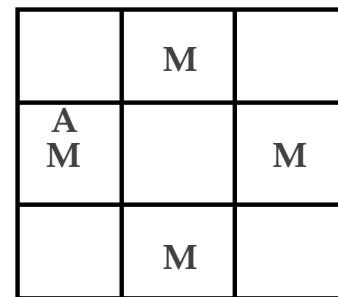
Extracting Modules from Networks

0, 2, 2, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 2, 1, 0, 0, 2, 2, 1, 1, 0, 2, 2, 1, 0, 2, 2

	M	
A M		M
	M	

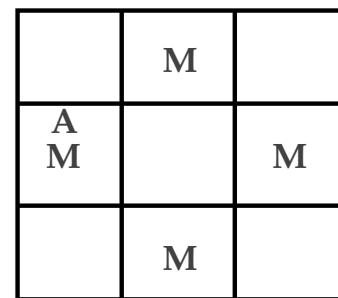
Extracting Modules from Networks

down	up	up	right	down	left	left
0, 2, 2, 1,	0, 0, 1, 1,	0, 0, 1, 1,	1, 2, 1, 0,	0, 2, 2, 1,	1, 0, 2, 2,	1, 0, 2, 2



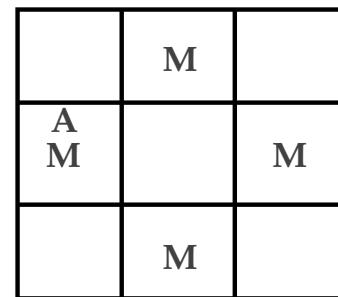
Extracting Modules from Networks

down	up	up	right	down	left	left
0, 2, 2, 1,	0, 0, 1, 1,	0, 0, 1, 1,	1, 2, 1, 0,	0, 2, 2, 1,	1, 0, 2, 2,	1, 0, 2, 2
option 3	option 2	option 2	option 2	option 4	option 2	option 4



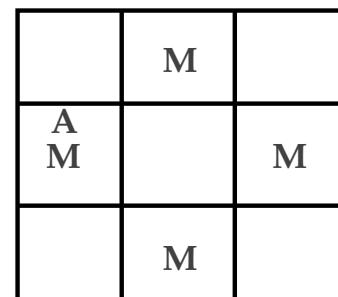
Extracting Modules from Networks

down	up	up	right	down	left	left
<u>0, 2, 2, 1,</u>	0, 0, 1, 1,	0, 0, 1, 1,	1, 2, 1, 0,	0, 2, 2, 1,	1, 0, 2, 2,	1, 0, 2, 2
option 3	option 2	option 2	option 2	option 4	option 2	option 4



Extracting Modules from Networks

down	up	up	right	down	left	left
<u>0, 2, 2, 1,</u>	<u>0, 0, 1, 1,</u>	<u>0, 0, 1, 1,</u>	<u>1, 2, 1, 0,</u>	<u>0, 2, 2, 1,</u>	<u>1, 0, 2, 2,</u>	<u>1, 0, 2, 2</u>
option 3	option 2	option 2	option 2	option 4	option 2	option 4



Learning Programs

Learning Programs

- ❖ Libraries of programs can be used to approximate the semantic space of a language.

Learning Programs

- ❖ Libraries of programs can be used to approximate the semantic space of a language.
- ❖ Libraries of programs can be learned by decomposing neural networks.

We Are Hiring! University of Alberta, Canada.

- ❖ Several (10+) AI+X faculty positions across campus.
- ❖ 3 CS Positions (Theory+ML, SE+ML, and Theory)
- ❖ Please spread the word!

