



Machine learning for molecular simulations: priors and predictive constraints

MAX PLANCK INSTITUTE FOR POLYMER RESEARCH

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High-throughput screening







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High-throughput screening











High-throughput screening















Outline









High-throughput thermodynamics



Outline

Intermolecular interactions across chemical space









Predicting the intermolecular energy landscape 🔰











Predicting the intermolecular energy landscape $\left| \begin{array}{c} \mathbf{z} \end{array} \right|$









$\{Z_i, \mathbf{r}_i\} \mapsto U(\{Z_i, \mathbf{r}_i\})$







Predicting the intermolecular energy landscape







Coordinates



$\{Z_i, \mathbf{r}_i\} \mapsto U(\{Z_i, \mathbf{r}_i\})$ Potential energy







$\{Z_i, \mathbf{r}_i\} \mapsto U(\{Z_i, \mathbf{r}_i\})$

Phase (e.g., gas vs. condensed)

Conformational (e.g., *cis* vs. *trans*)

Compositional



Transferability challenges









AMOEBA polarizable force field

 $U = U_{bond} + U_{angle} + U_{b\theta} + U_{oop} + U_{torsion} + U_{vdW} + U_{ele}^{perm} + U_{ele}^{ind}$

Water-sulfate anion clusters



Ponder et al., Phys Chem B (2010)

Max Planck Institute for Polymer Research

Small molecule solvation free energies



Phase and conformational transferability





$\{Z_i, \mathbf{r}_i\} \mapsto U(\{Z_i, \mathbf{r}_i\})$

1. Physics-based (force field)

2. Data-driven (machine learning)







$\{Z_i, \mathbf{r}_i\} \mapsto U(\{Z_i, \mathbf{r}_i\})$

1. Physics-based (force field) **More parameters**

Transferability

2. Data-driven (machine learning) **Extrapolation**



Strategies for energy landscape prediction





Extrapolation in machine learning









Extrapolation in machine learning









Extrapolation in machine learning









Machine learning: encoding physics



Chmiela, Sauceda, Müller, Tkatchenko, Nat. Comm. 9:3887 (2018)





"Transform the configuration, and the prediction transforms with it"

conservation

 $\mathbf{K}(\mathcal{S}\rho, \mathcal{S}'\rho') = \mathbf{S}\mathbf{K}(\rho, \rho')\mathbf{S}'^{\mathrm{T}}$

Glielmo, Sollich, De Vita, *Phys Rev B* **95** (2017)







Machine learning: encoding physics



Wishlist

THEORY

GROUP

- long-range interactions
- chemical-space transferability

Size of the interpolation-space?



"Transform the configuration, and the prediction transforms with it"

018)

$\mathbf{K}(\mathcal{S}\rho, \mathcal{S}'\rho') = \mathbf{S}\mathbf{K}(\rho, \rho')\mathbf{S}'^{\mathrm{T}}$

Glielmo, Sollich, De Vita, *Phys Rev B* **95** (2017)







Intermolecular interactions across chemical space











Intermolecular interactions across chemical space 📿

Nuclear charges





Coordinates











Intermolecular interactions across chemical space 📿

Nuclear charges





Coordinates



Any small molecule made of H, C, O, N neutral compounds























Coordinates



Physics-based models

- Encode laws, symmetries
- Little chemical information

Any small molecule made of H, C, O, N neutral compounds



Intermolecular interactions across chemical space









Physics-based aspect

Long-ranged

- Static electrostatics
- Many-body dispersion
- Polarization

Van Vleet, Misquitta, Stone, and Schmidt, *J. Chem. Theory Comput.* **12** (2016); Vandenbrande, et al., *J. Chem. Theory Comput.* **13** (2017); Grimme, *J. Chem. Theory Comput.* **10** (2014); Verstraelen, et al., *J. Chem. Theory Comput.* **12** (2016); Metz et al, *J. Chem. Theory Comput* **12** (2016)

Short-ranged

- Charge penetration
- Repulsion
- (Charge transfer)





Physics-based aspect

Long-ranged

Perturbation theory

- Static electrostatics
- Many-body dispersion
- Polarization



Van Vleet, Misquitta, Stone, and Schmidt, J. Chem. Theory Comput. 12 (2016); Vandenbrande, et al., J. Chem. Theory Comput. 13 (2017); Grimme, J. Chem. Theory Comput. 10 (2014); Verstraelen, et al., J. Chem. Theory THEORY *Comput.* **12** (2016); Metz et al, *J. Chem. Theory Comput* **12** (2016)

Short-ranged

Overlap models

- Charge penetration
- Repulsion
- (Charge transfer)

 $S_{ij} = \int \mathrm{d}^3 \mathbf{r} \rho_i(\mathbf{r}) \rho_j(\mathbf{r})$





Physics-based aspect

Long-ranged

- Static electrostatics
- Many-body dispersion
- Polarization

Use ML to predict atoms-in-molecules properties

- Multipole moments
- Hirshfeld ratios

Van Vleet, Misquitta, Stone, and Schmidt, J. Chem. Theory Comput. 12 (2016); Vandenbrande, et al., J. Chem. Theory Comput. 13 (2017); Grimme, J. Chem. Theory Comput. 10 (2014); Verstraelen, et al., J. Chem. Theory THEORY *Comput.* **12** (2016); Metz et al, *J. Chem. Theory Comput* **12** (2016) GROUP

Short-ranged

- Charge penetration
- Repulsion
- (Charge transfer)

Atomic density widths/populations







Van Vleet, Misquitta, Stone, and Schmidt, J. Chem. Theory Comput. 12 (2016); Vandenbrande, et al., J. Chem. Theory Comput. 13 (2017); Grimme, J. Chem. Theory Comput. 10 (2014); Verstraelen, et al., J. Chem. Theory THEORY *Comput.* **12** (2016); Metz et al, *J. Chem. Theory Comput* **12** (2016) GROUP











Stone, The Theory of Intermolecular Forces

Static multipole electrostatics





THEORY GROUP Stone, The Theory of Intermolecular Forces





THEORY Stone, The Theory of Intermolecular Forces





THEORY GROUP Stone, The Theory of Intermolecular Forces

Static multipole electrostatics

dipoles, quadrupoles rotate with the sample $1 \frac{3R_{\alpha}R_{\beta} - R^2\delta_{\alpha\beta}}{-7}$









 $e^{\lambda l}$

kernel-ridge regression $\mathbf{K}\alpha = p$

0.01

0.1

0.001

Descriptor: aSLATM

$\mathbf{M}^{I} = [Z_{I}, \{\rho_{I}^{IJ}(R)\}, \{\rho_{I}^{IJK}(\theta)\}]$

Huang and von Lilienfeld, J. Chem. Phys. 145 (2016) Huang and von Lilienfeld, arXiv:1707.04146, 2017



Multipoles: Learning curves



 $10^1 \, 10^2 \, 10^3 \, 10^4 \, 10^1 \, 10^2 \, 10^3 \, 10^4 \, 10^1 \, 10^2 \, 10^3 \, 10^4$

Atoms in training set

Easier to learn H,O than C,N₁₅





Multipoles: Correlation curves









monopole







C,**N** have more complex valencies









Many-body dispersion

Pairwise London dispersion: $E_{AB} = -\frac{C_{6AB}}{R^6}$

 $U_{\rm LJ}(r) = 4\epsilon \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6 \right]$

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Casimir-Polder: $C_{6AB} = \frac{3}{\pi} \int_0^\infty \mathrm{d}\omega \alpha_p(i\omega) \alpha_q(i\omega)$









Many-body dispersion

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Need atomic polarizabilities as input parameters









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Many-body dispersion

Coupled fluctuating dipole model:

Quantum harmonic oscillators

Donchev, Chem Phys (2006)

Max Planck Institute for Polymer Research

Casimir-Polder:

$$C_{6AB} = \frac{3}{\pi} \int_{0}^{\infty} d\omega \alpha_{p}(i\omega) \alpha_{q}(i\omega)$$

Need atomic polarizabilities as input parameters



Atomic polarizabilities

Atom-in-molecule: Hirshfeld ratios

Tkatchenko et al., Phys Rev Lett (2012)








Many-body dispersion

Pairwise London dispersion:



Many-body dispersion

Coupled fluctuating dipole model:

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Donchev, Chem Phys (2006)

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Atomic polarizabilities

Atom-in-molecule: Hirshfeld ratios

Tkatchenko et al., Phys Rev Lett (2012)









Learning Hirshfeld ratios

Reference Hirshfeld ratio



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 $\alpha_p^0 \approx \frac{V_p^{\text{eff}}}{V_p^{\text{free}}} \alpha_p^{\text{free}} = \frac{\int d\mathbf{r} r^3 w_p(\mathbf{r}) \mathbf{n}(\mathbf{r})}{\int d\mathbf{r} r^3 n_p^{\text{free}}} \alpha_p^{\text{free}}$

Training: 12.3k atoms in 1k molecules MAE: 0.006

 $\frac{Z_i Z_j}{|\mathbf{R}_i - \mathbf{R}_j|} \quad \forall \quad i \neq j$





Polarizability

Thole model

N point dipole polarizabilities placed in a homogeneous field F

Induced dipole moment at point p:

$$\mu_p = \alpha_p \left(\mathbf{F}_p \cdot \mathbf{F}_p$$

- I_{pq} : dipole field tensor
- $\mathbf{F}_{\mathcal{D}}$ given by static electrostatic interactions at site p

Thole, Chem Phys, **59**, 341 (1981)

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Thole, Chem Phys, **59**, 341 (1981)

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Need atomic polarizabilities and multipoles as input parameters









 $\alpha_{\text{model}}^{\text{iso}}$ [Bohr³]

Tkatchenko and Scheffler, Phys Rev Lett (2009)

Molecular polarizabilities

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7 parameters to cover chemical space of CHON intermolecular energies

Polarization

Many-body dispersion

Repulsion



Few global parameters

2

1.50 Mixed complexes: benzene C; H; O; N





















Validation: SSI



THEORY Burns *et al.*, *J Chem Phys*, **147** (2017).



2,200+ amino-acid pairs

Ref: CCSD(T)/CBS

Error: 0.4 kcal/mol













THEORY GROUP Jurečka et al., Phys Chem Chem Phys 8 (2006)



Toward the condensed phase











THEORY Bereau, DiStasio Jr., Tkatchenko, von Lilienfeld, *JCP* **148**, 241706 (2018)

Intermolecular interactions across chemical space

7 global parameters



Lessons learned ML force fields can be systematically improved

- physical effects (perturbation theory at short range)
- chemical groups
- provide data + ML model











Outline









High-throughput thermodynamics



Outline

Intermolecular interactions across chemical space















Drug permeability













Drug permeability











Drug permeability







Fokker-Planck; Smoluchoswki

Permeability coefficient

$$P^{-1} = \int \mathrm{d}z \frac{\exp\left(\Delta G(z)/k_{\rm B}T\right)}{D_z(z)}$$

Swift & Amaro, Chem Biol & Drug THEORY GROUP *Design* **81** (2013)

Drug permeability









Fokker-Planck; Smoluchoswki

Permeability coefficient

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Swift & Amaro, Chem Biol & Drug THEORY GROUP *Design* **81** (2013)

Drug permeability



 $\Delta G(z)$













Fokker-Planck; Smoluchoswki

Permeability coefficient

$$P^{-1} = \int \mathrm{d}z \frac{\exp\left(\Delta G(z)/k_{\rm B}T\right)}{D_z(z)}$$

Swift & Amaro, Chem Biol & Drug THEORY GROUP *Design* **81** (2013)

Drug permeability



force from computer simulations





Chipot and Comer, *Scientific Reports* (2016)





- Manual force-field parametrization
- Sampling: 100,000+ CPU-hours

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Chipot and Comer, *Scientific Reports* (2016)





THEORY

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Chemical group:

- net charge
- hydrogen bond
- water/octanol partitioning









Automated coarse-graining: Martini

Chemical group:

- net charge
- hydrogen bond
- water/octanol partitioning



18 bead types: chemical fragments Marrink, Tieleman, Chem Soc Rev 42 (2013) Periole, Marrink, Biomolecular Simulations (2013)











Chemical group:

- hydrogen bond
- water/octanol partitioning

neural network trained on experimental data

Tetko et al., J Chem Inf Comput Sci 41 (2001)

Automated parametrization for small molecules

THEORY GROUP Bereau & Kremer, *J Chem Theory Comput* **11** (2015)









THEORY Jakobtorweihen et al. J Chem Phys **141** (2014); Bereau & Kremer, J Chem Theory Comput, **11** (2015)

Solute insertion in the membrane



ACS Publications





THEORY Jakobtorweihen et al. J Chem Phys **141** (2014); Bereau & Kremer, J Chem Theory Comput, **11** (2015)



THEORY Jakobtorweihen et al. J Chem Phys **141** (2014); Bereau & Kremer, J Chem Theory Comput, **11** (2015)





Construct reduced chemical space





We don't focus on specific compounds, instead explore chemical diversity

Molecular weight:



~ 30-160 Da





Construct reduced chemical space





We don't focus on specific compounds, instead explore chemical diversity

Molecular weight:

2 ~ 30-160 Da

CG: combinatorial explosion is reduced





G

Identifying simple thermodynamic relations

Midplane

Water

Intertace

THEORY GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)







G

Identifying simple thermodynamic relations

 \boldsymbol{Z}

Midplane

$\Delta G_{I \rightarrow}$ Water Interface

 $\Delta G_{W\to O}$

• GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)







 GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)

🕼 Identifying simple thermodynamic relations 🔰







 GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)

Identifying simple thermodynamic relations









 GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)




 THEORY
GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)



PMF prediction from experimental value

High-throughput coarse-grained



THEORY GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)





PMF prediction from experimental value

High-throughput coarse-grained





THEORY GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)



PMF prediction from experimental value

High-throughput coarse-grained





Error across chemical space: linear relations: 1.8 kcal/mol coarse-grained: 1.4 kcal/mol

THEORY GROUP Menichetti, Kanekal, Kremer, Bereau, J Chem Phys 147 (2017)









Coarse-graining reduces chemical space









Reduction due to limited number of bead types



Coarse-graining reduces chemical space









High-throughput coarse-graining scheme







Menichetti, Kanekal, Bereau, ACS Cent. Sci. 5 (2019)







Menichetti, Kanekal, Bereau, ACS Cent. Sci. 5 (2019)

High-throughput coarse-graining scheme

Potential of mean force of neutral and charged species $\Delta G(z)$ $\Delta G_{W \rightarrow M}$ pK_{a} $\bigstar \Delta G(z)$ ********** $\blacktriangle \Delta G(z)$ \mathbf{r}_{z}







Menichetti, Kanekal, Bereau, ACS Cent. Sci. 5 (2019)



THEORY GROUP Menichetti, Kanekal, Bereau, ACS Cent. Sci. 5 (2019)



12 9 3 6 $\Delta G_{W \rightarrow M} \text{ [kcal/mol]}$

> What type of chemistry covers the surface?

 $\mathsf{ap}K\mathsf{a}$

THEORY GROUP Menichetti, Kanekal, Bereau, ACS Cent. Sci. 5 (2019)





12 9 3 6 $\Delta G_{W \rightarrow M} \text{ [kcal/mol]}$

> What type of chemistry covers the surface?

Analysis of **500,000+** compounds

THEORY GROUP Menichetti, Kanekal, Bereau, ACS Cent. Sci. 5 (2019)



 $\mathsf{ap}K\mathsf{a}$

Chemical-space coverage











Kernel-based machine learning

$\Delta G(\mathbf{x}) = \sum \alpha_i K(\mathbf{x}_i^*, \mathbf{x})$

THEORY GROUP Hoffmann, Menichetti, Kanekal, Bereau, *Phys Rev E* **100** (2019)

Boosting the database with machine learning

Training of machine learning model on Monte Carlo dataset Training data Predictions









THEORY GROUP Hoffmann, Menichetti, Kanekal, Bereau, *Phys Rev E* **100** (2019)





••• GROUP Hoffmann, Menichetti, Kanekal, Bereau, Phys Rev E 100 (2019)



Physics offers controlled exploration of chemical space



THEORY Hoffmann, Menichetti, Kanekal, Bereau, *Phys Rev E* **100** (2019)









THEORY GROUP Hoffmann, Menichetti, Kanekal, Bereau, Phys Rev E 100 (2019)



Physics offers controlled exploration of chemical space



THEORY GROUP Hoffmann, Menichetti, Kanekal, Bereau, Phys Rev E 100 (2019)







Conclusions



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Conclusions



High-throughput thermodynamics

- Coarse-graining reduces the size of chemical space: fewer simulations
- Structure-property relationships: CG suggests low-dimensional representation



Force fields across chemical space

- Physics encode long-range interactions Symmetries reduce the interpolation
- Learning from QM (atomistic) or physicochemical properties (CG)







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MAX PLANCK RESEARCH **NETWORK** on big-data-driven materials science



Noether-Programm



