(Big) Data of Materials Science from First Principles -- Critical Role of the Descriptor --

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From the periodic table of the elements to a chart of materials: Organize materials according to their properties and functions

- o figure of merit of thermoelectrics (as function of T)
- turn-over frequency of catalytic materials (as function of T and p)
- o efficiency of photovoltaic systems
- o etc.







(*) Work performed in collaboration with Luca Ghiringhelli, Jan Vybiral, Claudia Draxl, Sergey Levchenko, Alexandre Tkatchenko, Patrick Rinke, Xinguo Ren, and Igor Ying Zhang



Dmitri Mendeleev (1834-1907)



Materials Genome Initiative for Global Competiveness



Compute the basic properties ("genes") of many (ten or hundred thousand) materials and disseminate that information to the materials community to enable rapid searches of materials properties and help design improved materials.

To help business discover, develop, and deploy new materials twice as fast, we're launching what we call the Materials Genome Initiative. The invention of silicon circuits and lithium ion batteries made computes and iPods and iPads possible, but it took years to get those technologies from the drawing boards to the market place. We can do it faster.

President Obama Carnegie Mellon University, June 2011

"twice as fast, at a fraction of the cost"



Materials Genome Initiative for Global Competitiveness http://www.whitehouse.gov/sites/deault/files/microsites/stp/materials-genome-initiative-final.pdf

The Four V of Big Data and an A

Data – data – data (analog to Moore's law) numbers, arrays, figures, movies, ...

(so far: most data are not used and even thrown away)



Big-Data Challenge: "four V": Volume (amount of data), Variety (heterogeneity of form and meaning of data),

Veracity Juncertainty of data quality),

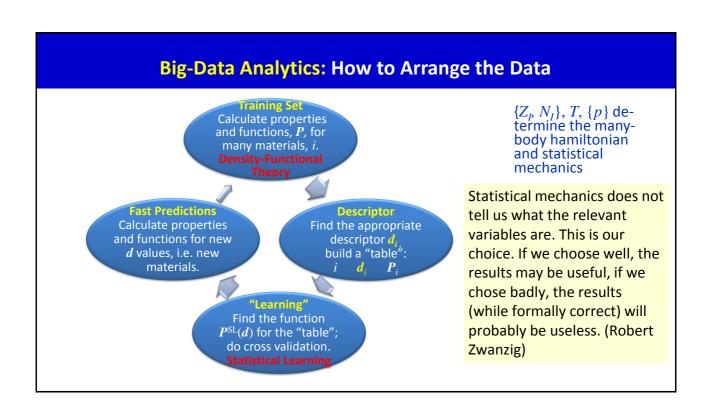
Velocity at which data may change or new data arrive.

Computed data: Query and read out what was stored. (high-throughput screening) Shouldn't we do more?!



The four V should be complemented by an "A", Big-Data Analytics:

- identify (so far) hidden trends,
- which materials should be studied next as most promising candidates,
- identify anomalies,
- identify the mechanisms that govern a certain material property or function.



Big-Data Analytics: How to Arrange the Data raining Sel $\{Z_{I}, N_{I}\}, T, \{p\}$ determine the many-Calculate properties and functions, P, for body hamiltonian many materials, *i*. and statistical mechanics Statistical mechanics does not **Fast Predictions** Descriptor tell us what the relevant Calculate properties Find the appropriate variables are. This is our and functions for new descriptor d_i build a "table" d values, i.e. new choice. If we choose well, the materials. results may be useful, if we chose badly, the results (while formally correct) will Find the function probably be useless. (Robert $P^{\rm SL}(d)$ for the "table"; do cross validation. Zwanzig)

Big-Data Analytics: How to Arrange the Data

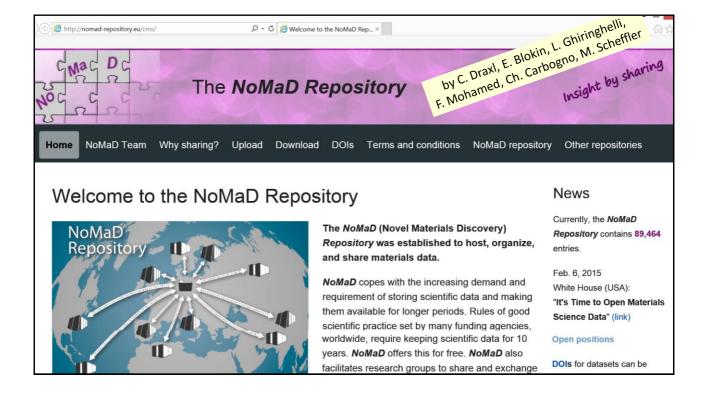
Calculate properties and functions, *P*, for many materials, *i*.

Density-Functional Theory

 $\{Z_p, N_I\}, T, \{p\}$ determine the manybody hamiltonian and statistical mechanics

d characterizes the relevant mechanisms that govern the observed property/function P. The $d \to P^{\rm SL}$ mapping is complex; identifying the descriptor d from known data P_i , is an ill-posed problem (statistical-learning theory): A little error in the data P_i may suggest a different descriptor d. Thus, knowledge of the accuracy of data P_i is crucial (veracity). The choice of d is not unique.

- **A) Veracity:** Accuracy of state-of-the-art density-functional theory (validation and verification)
- **B)** Descriptor: How to find it, how to understand the causality between d and P^{SL} ?





scientific practice set by many funding agencies, worldwide, require keeping scientific data for 10 years. **NoMaD** offers this for free. **NoMaD** also facilitates research groups to share and exchange their results, inside a single group or between two

or more, and to recall what was actually done some years ago.

The NoMaD Repository enables the confirmatory analysis of materials data, their reuse, and repurposing.

Upload of data is possible without any barrier. Results are accepted in their raw format as produced by the underlying code. The only condition is that the list of authors is provided, and code and code version can be retrieved from the uploaded files. These data can be restricted to the owner or made available to other people (selected by the owner). They can be updated and downloaded at any time.

Read more details concerning the upload. Please, register or login to participate.

At present, the repository contains *ab initio* electronic-structure data from density-functional theory and methods beyond. At a later stage, it will be extended by force-field studies and by experimental data. We also give an outlook on the *NoMaD Laboratory* that will be dedicated to a *Materials Encyclopaedia*, as the basis for complex queries and the development of various data-analytics tools.

Codes: Abinit, crystal, exciting, CASTEP, FHI-aims, Quantum Espresso, VASP – more coming; various xc functionals

Science Data (IIIIK)

Open positions

DOIs for datasets can be requested

Check for related conferences and workshops.

We are moving to the HPC Center of the Max Planck Society (RZG). We apologize for any possible instability during the next 2 days.

The **NoMaD Repository** is about joining eudat.

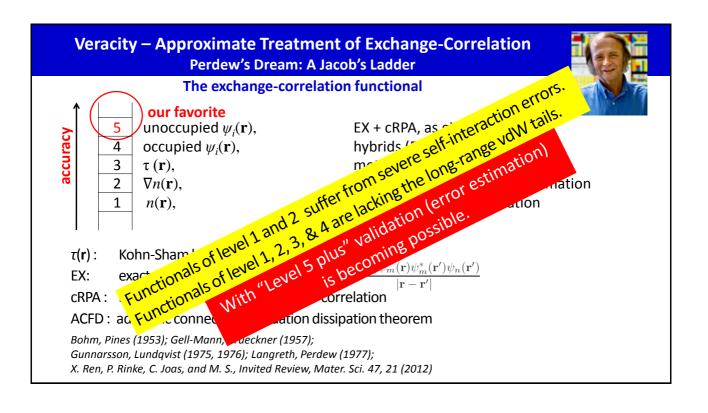
Financial Support

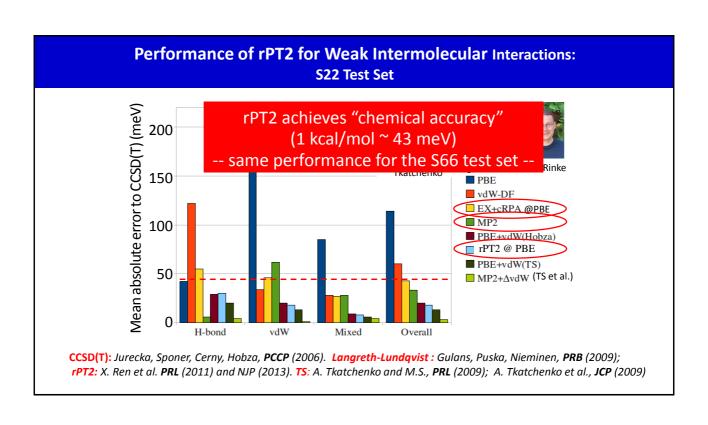


Veracity – Validation and Verification

- accuracy of materials-science codes: basis sets, relativity, pseudopotentials, other numerical approximations (verification)
- accuracy of the exchange-correlation functional (validation)

Comparing Solid State DFT Codes, Basis Sets and Potentials						
Code	Version	Basis	Electron treatment	∆-value	Authors	
WIEN2k ₪	13.1	LAPW/APW+lo	all-electron	0 meV/atom	S. Cottenier	
FHI-aims ₽	081213	tier2 numerical orbitals	all-electron (relativistic atomic_zora scalar)	0.2 meV/atom	ASE [2]	
Exciting ₽	development version	LAPW+xlo	all-electron	0.2 meV/atom	Exciting [10]	
FHI-aims ₫	081213	tier2 numerical orbitals	all-electron (relativistic zora scalar 1e-12)	0.4 meV/atom	ASE [2]	
CASTEP 🗗	8.0	plane waves	OTFG CASTEP 8.0	0.5 meV/atom	CASTEP [7]	
ABINIT₫	7.7.3	plane waves	PAW JTH v0.2 🗗	0.6	F. Jollet and N	





Test Sets for Materials Science and Engineering?

Chemists have shown the way. For small and light molecules they developed test sets: G2, NHTBH38, HTBH38, S22, S66 ...

We need a materials test set! We can now do renormalized second-order perturbation theory (similar to CCSD) and even full CI (*) — for certain systems.

Comparison with experiment is very important as well (adsorption energies of molecules, *e.g.* by microcalometry). However, theory-theory comparison is better defined.

(*) G. H. Booth, A. J. W. Thom, and A. Alavi, J. Chem. Phys. 131, 054106 (2009). G. H. Booth, A. Grüneis, G. Kresse, and A. Alavi, Nature 493, 365 (2013).

Test set for materials science and engineering



7 elements and 12 binaries with cubic structure (for the start)

н	
Li	Be
Na	Mg
K	Ca
Rb	Sr
Cs	Ba

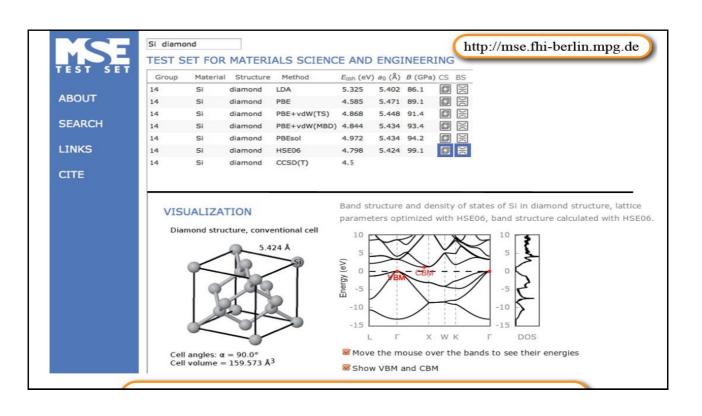
Light main group elements

В	С	N	0	F	Ne
A1	Si	P	S	C1	Ar
Ga	Ge	As	Se	Br	Kr
In	Sn	Sb	Te	I	Xe

Ne, Ar, Al (fcc); Li, Na (bcc); C, Si (diamond); LiH, LiF, LiCl, NaF, NaCl, MgO, MgS (rocksalt); BeS, BP, AlP, SiC, BN (zincblende)



- MSE properties: cohesive, electronic, elastic and vibrational
- Representative for cubic metals, semiconductors, and insulators
- Numerically accurate reference values from theory, incl. MP2, RPA, CCSD(T)



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Finding d from P

Causality: the science behind P(d)



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Kernel Regression

We have data $\{P_i\}$ at "coordinates" $\{x_i\}$ x_i = set of descriptive parameters (descriptor)

$$\boldsymbol{P}_i = \boldsymbol{P}(\boldsymbol{x}_i) = \sum_{k=1}^N c_k K(\boldsymbol{x}_i, \boldsymbol{x}_k)$$

Linear regression: $K(x_i, x_k) = x_i \cdot x_k$ $P(x_i) = x_i \cdot c^*$

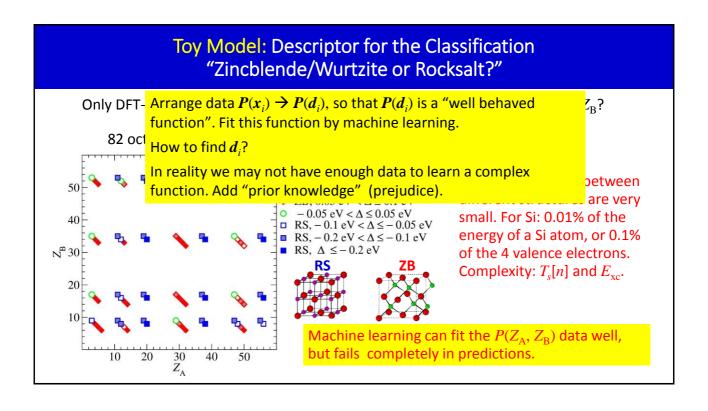
Polynomial kernel $K(\mathbf{x}_i, \mathbf{x}_k) = (\mathbf{x}_i \cdot \mathbf{x}_k + c)^d$

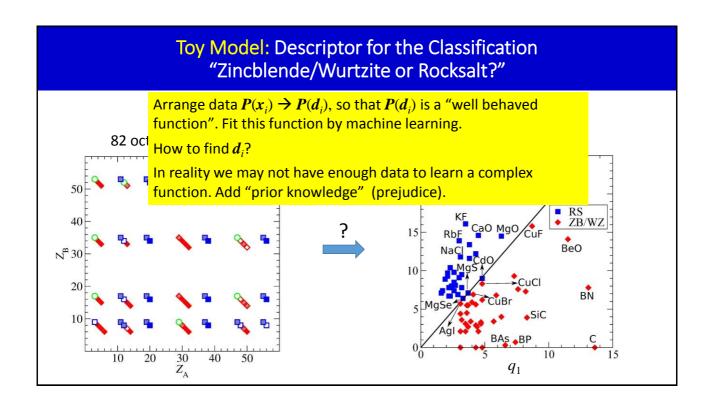
Gaussian kernel $K(x_i, x_k) = \exp(-\sum_i (x_i - x_k)^2 / 2\sigma_i^2)$

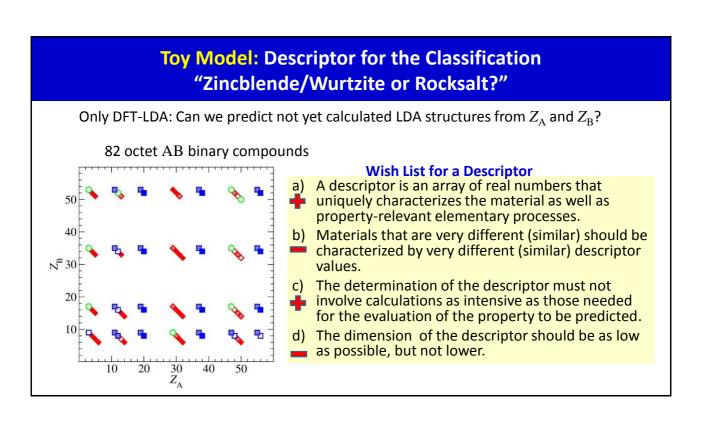
More data means better representation.

Do we "learn" anything?

For successful learning, we need a "good" descriptor: $P(x_i) \rightarrow P(d_i)$







■ RS • ZB/WZ

BeO

Toy Model: Descriptor for the Classification "Zincblende/Wurtzite or Rocksalt?"

the key scientific challenge: find a descriptor d that works.

How to find a good descriptor, also for more complicated properties and functions?

Example (the traditional way):

J. C. Phillips and J. A. Van Vechten (1969/70)^(*): A two-dimensional descriptor that distinguishes materials that crystallize in ZB/WZ vs. RS structures:

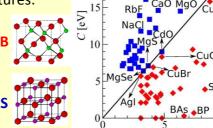
 $E_{\rm h} =$ C =

related to crystal's band gap, dielectric constant, nearest-neighbor distance

There are several other descriptors for this

J. A. Van Vechten, Phys. Rev. B 182, 891 (1969);
 J. C. Phillips, Rev. Mod. Phys. 42, 317 (1970)

classification goal, by various authors.



20

Statistical Learning (Machine Learning)

fit and/or interpolation of discrete, known data points $\{P_i\}$ and building a function P(d) the key scientific challenge: find a reliable, low dimensional descriptor d.

kernel ridge regression

$$P(\boldsymbol{d}) = \sum_{i=1}^{N} c_i \exp\left(-\|\boldsymbol{d}_i - \boldsymbol{d}\|_2^2 / 2\sigma^2\right)$$

$$\sum_{i=1}^{N} (P(\boldsymbol{d}_{i}) - P_{i})^{2} + \lambda \sum_{i,j=1}^{N,N} c_{i}c_{j} \exp\left(-\|\boldsymbol{d}_{i} - \boldsymbol{d}_{j}\|_{2}^{2}/2\sigma^{2}\right)$$

$$\|\boldsymbol{d}_{i} - \boldsymbol{d}_{j}\|_{2}^{2} = \sum_{\alpha=1}^{\Omega} (d_{i,\alpha} - d_{j,\alpha})^{2}$$

linear

R. Tibshirani, J. Royal Statist. Soc. B 58, 267 (1996) $P(oldsymbol{d}) = oldsymbol{d} oldsymbol{c}$

$$\sum_{i=1}^{N}(P(\boldsymbol{d}_{i})-P_{i})^{2}$$
 +
$$\lambda \|\boldsymbol{c}\|_{1}$$

$$\|\boldsymbol{c}\|_1 = \sum_{\alpha=1}^M |c_{\alpha}|$$

least absolute shrinkage and selection operator (LASSO) for feature selection

1) Primary Features, 2) Feature Space, 2) Descriptors

ID	Description free atoms	Symbols	#	
A1	Ionization Potential (IP) and Electron Affinity (EA)	IP(A) EA(A) IP(B) EA(B) [1]	4	
A2	Highest occupied (H) and lowest unoccupied (L) Kohn-Sham levels	H(A) L(A) H(B) L(B)	4	
A3	Radius at the max. value of $s, p,$ and d valence radial radial probability density	$\begin{vmatrix} r_s(\mathbf{A}) \ r_p(\mathbf{A}) \ r_d(\mathbf{A}) \\ r_s(\mathbf{B}) \ r_p(\mathbf{B}) \ r_d(\mathbf{B}) \end{vmatrix}$	6	

1)

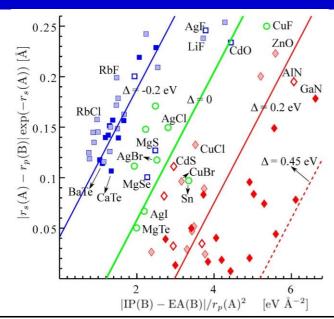
ID	Description	free dimers	Symbols	#
A4	Binding energy		$E_b(AA) E_b(BB) E_b(AB)$	3
A5	HOMO-LUMO KS gap		HL(AA) HL(BB) HL(AB)	3
A6	Equilibrium distance		$d(AA) \ d(BB) \ d(AB)$	3

2)

We start with 23 primary features and build > 10,000 non linear combinations

3) LASSO finds the most important descriptors: $\frac{\mathrm{IP}(\mathrm{B}) - \mathrm{EA}(\mathrm{B})}{r_p(\mathrm{A})^2}, \frac{|r_s(\mathrm{A}) - r_p(\mathrm{B})|}{\exp(r_s(\mathrm{A}))}, \frac{|r_p(\mathrm{B}) - r_s(\mathrm{B})|}{\exp(r_d(\mathrm{A}) + r_s(\mathrm{B}))}$





- $\Delta = E(RS) E(ZB)$
- \bullet ZB, $\Delta > 0.2$ eV
- \diamond ZB, 0.1 eV $< \Delta \le 0.2$ eV
- \diamond ZB, 0.05 eV $< \Delta \le 0.1$ eV
- $-0.05 \text{ eV} < \Delta \le 0.05 \text{ eV}$
- RS, −0.1 eV < Δ ≤ −0.05 eV RS, −0.2 eV < Δ ≤ −0.1 eV
- RS, $\Delta \le -0.2 \text{ eV}$
- K5, Z = 0.2 CV

$$P(\mathbf{d}) = \mathbf{dc}$$

The complexity and science is in the descriptor (identified from >10,000 features).

Statistical Learning (Machine Learning): Descriptor

Mean absolute error (MAE), and maximum absolute error (MaxAE), in eV, (first two lines) and for a leave-10%-out cross validation (CV), averaged over 150 random selections of the training set (last two lines). For (Z_A^*, Z_B^*) , each atom is identified by a string of three random numbers.

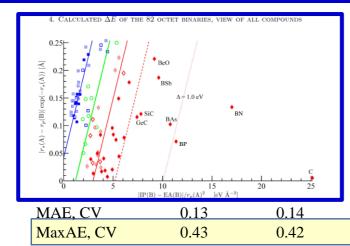
Descriptor	$Z_{\rm A}, Z_{\rm B}$	$Z_{\mathrm{A}}^{*}, Z_{\mathrm{B}}^{*}$	1D	2D	3D	5D
MAE	1*10 ⁻⁴	3*10 ⁻³	0.12	0.08	0.07	0.05
MaxAE	8*10 ⁻⁴	0.03	0.32	0.32	0.24	0.20
MAE, CV	0.13	0.14	0.12	0.09	0.07	0.05
MaxAE, CV	0.43	0.42	0.27	0.18	0.16	0.12

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Drawing Causal Inference from Big Data (Scientific Insight)

Correlation between d and P, i.e. P is a function of d, P(d), reflects causal inference

if it is based on sufficient information(*)

There are four possibilities (types of causality) behind P(d):

- 1. $d \rightarrow P$: P "listens" to d
- Judea Pearl 2. $A \rightarrow d$ and $A \rightarrow P$: There is no direct connection between d and P, but d and P
- 3. $P \rightarrow d$: d "listens" to P

both "listen" to a third "actuator"

4. There is no direct connection between *d* and *P*, but they have a common effect that listens to both and screams: "I occurred" (Berkson bias; Judea Pearl)

(*) Construct d with scientific knowledge (prejudice?), or use "big data" for $\{P_i\}$.

Drawing Causal Inference from Big Data (Scientific Insight)

Example:

The probability of childhood leukemia is higher for people living close to electricity power lines.

There is no direct connection between leukemia and the electromagnetic field.

Living close to electric power lines is not a desired residence. People living near power lines tend to be poorer than the control group, and there is a relationship between poverty and cancer.

Poverty → higher probability for living close to power lines correlation

Poverty → higher chances for cancer no direct relation causality

Drawing Causal Inference from Big Data (Scientific Insight)

Our previous example:

Prediction of the energy difference between ZB/WZ and RS of binary Compound semiconductors





There is no scientific law that connects the descriptor

$$\frac{\text{IP(B)} - \text{EA(B)}}{r_p(\text{A})^2}, \frac{|r_s(\text{A}) - r_p(\text{B})|}{\exp(r_s(\text{A}))}, \frac{|r_p(\text{B}) - r_s(\text{B})|}{\exp(r_d(\text{A}) + r_s(\text{B}))}$$

directly with the total-energy difference (we are not able to write it down). However, $Z_{\rm A}$, $Z_{\rm B}$ determine these descriptors, and $Z_{\rm A}$, $Z_{\rm B}$ determine the many-body Hamiltonians and the total-energy difference.

Poverty → higher probability for living close to power lines correlation

Poverty → higher chances for cancer no direct relation causality

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Judea Pear

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Drawing Causal Inference from Big Data (Scientific Insight)

ROMEO: "It was the lark, the bird that sings at dawn, not the nightingale. Look, my love, what are those streaks of light in the clouds parting in the east? Night is over, and day is coming. ... "



The *singing of the lark* is a good descriptor for "*the sun will rise soon*". The *singing of the lark* is not the actuator of (the mechanism behind) the sunrise.



Conclusion / Suggestion: Accept "larks" (not just scientific laws) to predict materials properties.

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Big-Data Analytics

- Finding d from $\{P_i\}$: LASSO and leave-some-out cross validation and noise
 - Analyze the science behind the *d* -- *P* correlation
- The big-data challenge in materials science: Look for anomalies, not the crowd

Summary and Outlook

- Machine learning may find structure in data that is invisible to humans.
- Causal models, i.e. finding causal descriptors, are richer. They are able to provide scientific insight and understanding.
- They can tell how to do machine learning on difficult tasks.
- Question: Why do we want to achieve insight and understanding? Isn't it good enough to have a predictive model?
- Question: Is it possible to assign error bars to predictions (of unexpected situations)?

Next steps:

- Beyond the linear fit: Non-linear kernel with l_1 -norm regularization.
- Higher accuracy: MaxAE loss function with l_1 -norm regularization.
- Improving the systematic creation of the feature space.