

Development and Application of Charge Optimized Many-Body (COMB) Potentials for Surface Chemistry and Heterogeneous Material Interfacial Interactions

Tao Liang, Tzu-Ray Shan, Bryce Devine, Yu-Ting Cheng, Jianguo Yu, Simon R. Phillpot, Susan B. Sinnott

*Department of Materials Science and Engineering
University of Florida*

Supported by: NSF-DMR, DOE EFRC, NSF-CHE, DOE

**IPAM Workshop 1: Quantum and Atomistic Modeling of Material Defects,
October 3, 2012**

Reactive many-body empirical potentials in materials science



May 2012 issue

Historically developed for materials with specific types of chemical bonds

- Tersoff potentials for Si
 - Brenner or REBO potential for C,H + O,F,S,.....
 - AIREBO
- EAM potentials for metals
 - MEAM for metals and oxides
 - EAM+ES for metals and oxides
- Buckingham potentials for ionically bound materials

$$V_{LJ} = 4\varepsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]$$

Lennard-Jones potential

$$= \varepsilon \left[\left(\frac{r_m}{r} \right)^{12} - 2 \left(\frac{r_m}{r} \right)^6 \right]$$

$$V_{ij}(r_{ij}) = V_{repulsive}(r_{ij}) + b_{ijk} V_{attractive}(r_{ij})$$

Bond-order potential
(Tersoff, Brenner,
REBO, etc.)

$$E_i = F_\alpha \left(\sum_{i \neq j} \rho_\beta(r_{ij}) \right) + \frac{1}{2} \sum_{i \neq j} \phi_{\alpha\beta}(r_{ij})$$

Embedded Atom Method
(EAM) potential

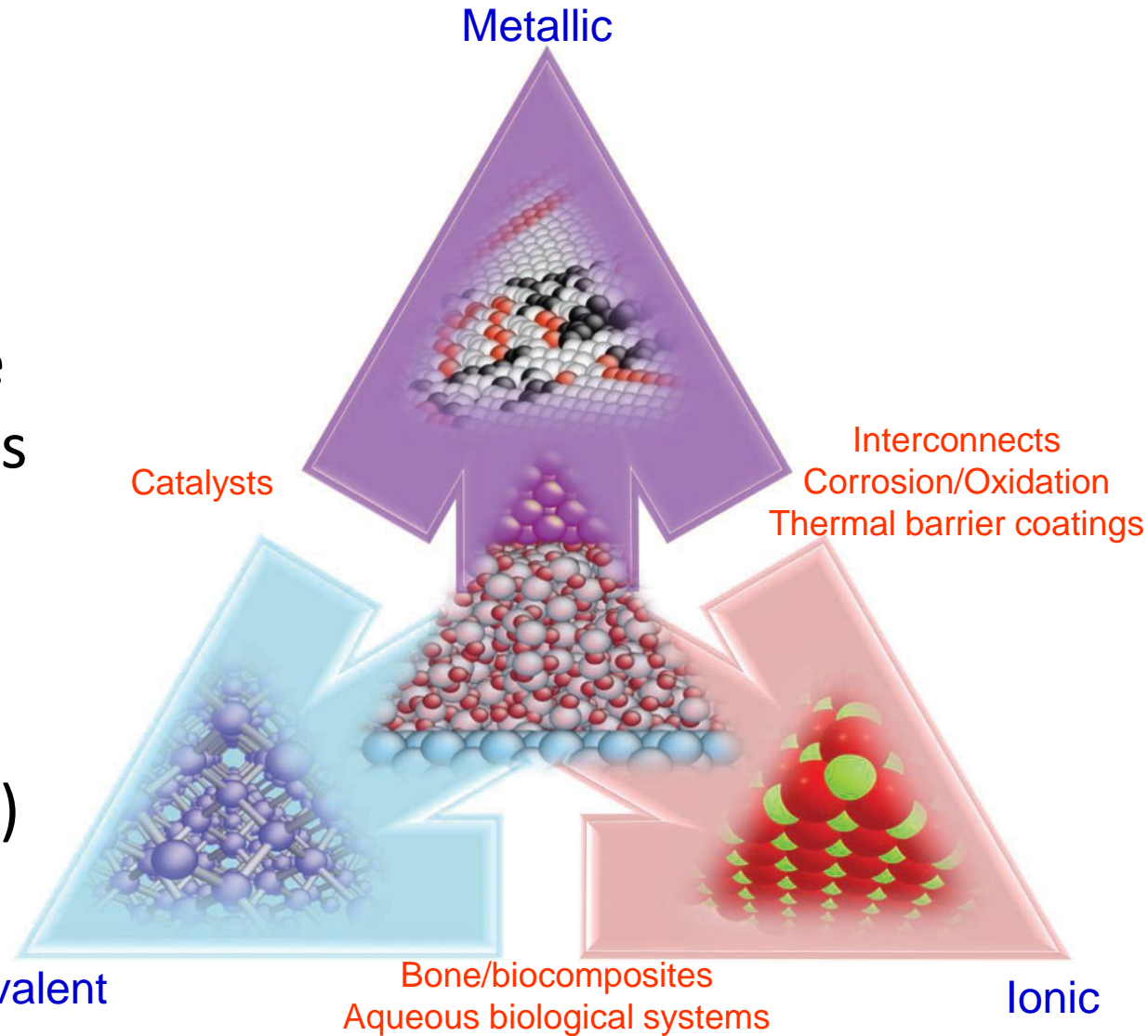
$$V_{ij}(r) = A_{ij} \exp \left(-\frac{r}{\rho_{ij}} \right) - \frac{C_{ij}}{r^6}$$

Buckingham potential

Equations from Wikipedia, October, 2012

Modeling Multicomponent Systems

- Inherent to many applications
- Challenge for traditional reactive empirical potentials (force fields)
- Developed the charge optimized many body (COMB) potential to model heterogeneous systems



S. R. Phillpot, S. B. Sinnott, *Science* 325, 1634 (2009).

Development

Overview of COMB Implementations

- 1st generation¹ (COMB1)
 - Si/SiO₂, Cu, Al
- 2nd generation²(COMB2) In LAMMPS, available
 - Si/SiO₂, Cu/Cu₂O/CuO, Hf/HfO₂, Ti/TiO₂
- 3rd generation³(COMB3) In LAMMPS, will be released shortly
 - C/H/O/N, Cu/Cu₂O/CuO, Zr/ZrO₂, Zn/ZnO, U/UO₂, Al/Al₂O₃/AlN, Ti/TiN/TiO₂, Pt, PbTiO₃

¹ J. Yu, et. al., *Phys. Rev. B* 75 085311 (2007)

² T.-R. Shan, et al., *Phys. Rev. B* 81, 125328 (2010).

³ T. Liang, et al., *Journal of Physical Chemistry A* 116, 7976 (2012).

Functional Form of COMB Potential

General formalism:

$$E_T = \sum_i \left[E_i^S(q_i) + \frac{1}{2} \sum_{j \neq i} V_{ij}(r_{ij}, q_i, q_j) + B_i(q_i) + C_i(r_{ij}, \theta_{jik}) \right]$$

- Self energy: fit to atomic ionization energies and electron affinities
 - $E_i^S(q_i) = \chi_i q_i + J_i q_i^2 + K_i q_i^3 + L_i q_i^4$
 - Penalty function to capture change in self energy due to field of ionic lattice
 - $E_i^{field}(r, q_j) = \sum_{j \neq i}^{NN} \left(\frac{\rho_1 q_j}{r_{ij}^5} + \frac{\rho_2 q_j^2}{r_{ij}^5} \right)$

J. Yu, S. B. Sinnott, S. R. Phillpot, *Phys. Rev. B* 75 085311 (2007)

T.-R. Shan, B. D. Devine, T. W. Kemper, S. B. Sinnott, S. R. Phillpot, *Phys. Rev. B* 81 125328 (2010)

- $V_{ij}(r_{ij}, q_i, q_j) = f_c(r_{ij}) \cdot A_{ij}(q_i, q_j) \cdot e^{-\lambda_{ij} \cdot r_{ij}} - f_c(r_{ij}) \cdot b_{ij} \cdot B_{ij}(q_i, q_j) \cdot e^{-\alpha_{ij} \cdot r_{ij}} + q_i \cdot J_{ij}(r_{ij}) \cdot q_j$
- Short range interactions: Tersoff type made charge dependent
 - A change in the partial charge on an atom affects the effective ionic radius, which influences the short-range repulsion and attraction
 - $A_{ij}(q_i, q_j) = A_{ij} \cdot \exp[\lambda_i D_i(q_i) + \lambda_j D_j(q_j)]$ → repulsive
 - $B_{ij}(q_i, q_j) = B_{ij} \cdot B_{ij}^*(q_i, q_j) \cdot \exp[\alpha_i D_i(q_i) + \alpha_j D_j(q_j)]$ → attractive
- Bond order term, b_{ij} , includes many-body effect
 - $b_{ij} = \left[1 + \left(\beta_i \sum_{k \neq i, j} \xi_{ijk} g(\theta_{jik}) \right)^{n_i} \right]^{-1/(2n_i)}$
 - $\xi_{ijk} = f_{S_{ik}} e^{\left[\alpha_{ij}^{m_i} (r_{ij} - r_{ik})^{m_i} \right]}$ → symmetry function
 - $g(\theta_{jik}) = 1 + c_i^2 / d_i^2 - c_i^2 / [d_i^2 + (h_i - \cos \theta_{jik})^2]$ → angular function

J. Yu, S. B. Sinnott, S. R. Phillpot, *Phys. Rev. B* 75 085311 (2007)

T.-R. Shan, B. D. Devine, T. W. Kemper, S. B. Sinnott, S. R. Phillpot, *Phys. Rev. B* 81 125328 (2010)

- $V_{ij}(r_{ij}, q_i, q_j) = f_c(r_{ij}) \cdot A_{ij}(q_i, q_j) \cdot e^{-\lambda_{ij} \cdot r_{ij}} - f_c(r_{ij}) \cdot b_{ij} \cdot B_{ij}(q_i, q_j) \cdot e^{-\alpha_{ij} \cdot r_{ij}} + q_i \cdot J_{ij}(r_{ij}) \cdot q_j$
- Long range interactions: Coulomb electrostatics
 - Spherical charge distribution: 1s-type Slater orbital
 - $J_{ij}(r_{ij}) = n_{ij} \int d^3 r_i \int d^3 r_j \rho_i(r_i, q_i) \rho_j(r_j, q_j) / r_{ij}$
 - $\rho_i(r_i, q_i) = q_i \frac{\xi_i^3}{\pi} \exp(-2\xi_i |r - r_i|)$
 - Treats long range interactions with Wolf summation

D. Wolf, P. Keblinski, S. R. Phillpot, and J. Eggebrecht, *J. Chem. Phys.* 110, 8254 (1999)

J. Yu, S. B. Sinnott, S. R. Phillpot, *Phys. Rev. B* 75 085311 (2007)

T.-R. Shan, B. D. Devine, T. W. Kemper, S. B. Sinnott, S. R. Phillpot, *Phys. Rev. B* 81 125328 (2010)

- Extended to include:

- Organic molecules: C/H/O/N, NO_x
- Oxides and nitrides: ZrO₂, ZnO, UO₂, TiN, AlN, Al₂O₃

- $$E_T = \sum_i \left[E_i^S(q_i) + \frac{1}{2} \sum_{j \neq i} V_{ij}(r_{ij}, q_i, q_j) + B_i(q_i) + C_i(r_{ij}, \theta_{jik}) + E^{polar}(q_i, r_{ij}) + E^{vdW}(r_{ij}) \right]$$

- $$E^{Polar}[q_i, r_{ij}] = \sum_i \frac{\vec{\mu}_i^2}{2\alpha_i} + \sum_i \vec{\mu}_i \cdot \vec{E}_i^q + \frac{1}{2} \sum_i \sum_{j \neq i} \vec{\mu}_i T_{ij} \vec{\mu}_j \quad \rightarrow \text{polarization}$$

- $$b_{ij} = \left[1 + \left(\sum_{j \neq i} \sum_{k \neq i, j} \zeta_{ijk} g(\cos(\theta_{ijk})) + P_{ij}(N_i^1, N_i^2, N_i^3 \dots) \right)^{\eta_i} \right]^{-\frac{1}{2\eta_i}} + b_{ij}^{\pi} + b_{ij}^{DH}$$

← modified angular
← tri-cubic spline coordination
← radicals and dihedrals

Bond Order for COMB C/H/O

- Radicals and Aromatics

$$b_{ij}^{\pi} = \pi_{ij}(\Omega_i, \Omega_j, N_{ij}^{conjug})$$

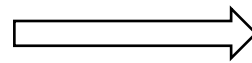
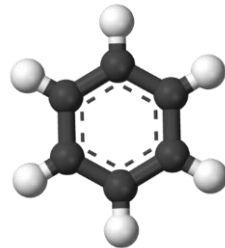
π_{ij} is a tri-cubic spline function

T_{ij} is the induced dipole field tensor

$$N_{ij}^{conjug} = 1 + \left[\sum_{k \neq ij}^{carbon} F_C(r_{ik}) T_{ik} P(X_{ik}) \right]^2 + \left[\sum_{l \neq ij}^{carbon} F_C(r_{jl}) T_{jl} P(X_{jl}) \right]^2$$

$$P(X_{ik}) = \begin{cases} 1 & X_{ik} < 2 \\ \frac{1}{2} [1 + \cos(\pi(X_{ik} - 2))] & 2 < X_{ik} < 3 \\ 0 & X_{ik} > 3 \end{cases} \quad \text{and} \quad X_{ik} = \Omega_k$$

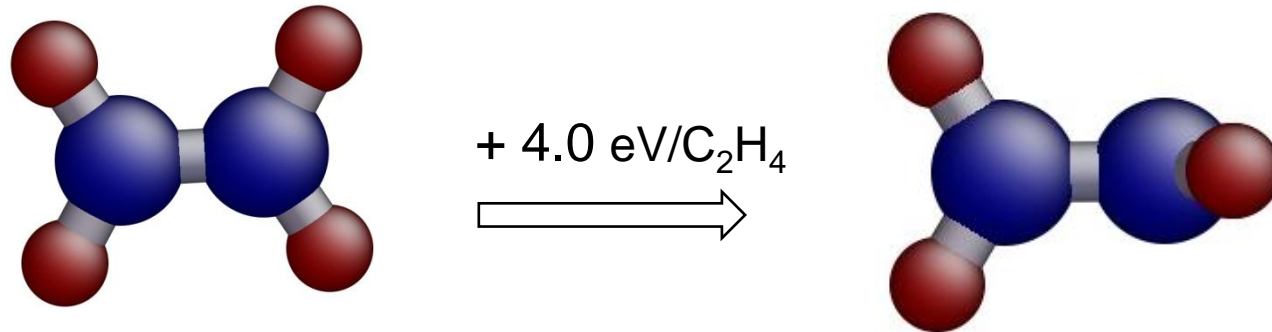
Ω_i is the coordination number of i^{th} atom



$$\pi_{ij}(2, 2, 3)$$

Bond Order for COMB C/H/O

- Torsion Term



Θ_{ijkl} : dihedral angle

$$b_{ij}^{DH} = \phi_{ij}(\Omega_i, \Omega_j, N_{ij}^{conjug}) \left[\sum_{k \neq i} \sum_{j_l \neq i, j} (1 - \cos^2(\Theta_{ijkl})) F_C(r_{ik}) F_C(r_{jl}) \right]$$

$$\phi_{ij}(\Omega_i, \Omega_j, N_{ij}^{conjug})$$

ϕ_{ij} is a tri-cubic spline function

Cost of Potentials in LAMMPS

Potential	System	# Atoms	Memory	LJ Ratio
Lennard-Jones	LJ liquid	32000	12 Mb	1.0x
EAM	bulk Cu	32000	13 Mb	2.4x
Tersoff	bulk Si	32000	9.2 Mb	4.1x
Stillinger-Weber	bulk Si	32000	11 Mb	4.1x
EIM	crystalline NaCl	32000	14 Mb	6.5x
CHARMM + PPPM	solvated protein	32000	124 Mb	13.6x
MEAM	bulk Ni	32000	54 Mb	15.6x
AIREBO	polyethylene	32640	101 Mb	54.7x
ReaxFF/C	PETN crystal	32480	976 Mb	185x
COMB2 (fixed q) QEq	Ti crystalline SiO ₂	32400 32400	31 Mb 85 Mb	55x 284x
eFF	H plasma	32000	365 Mb	306x
ReaxFF	PETN crystal	16240	425 Mb	337x
VASP/small*	water	192 (512e ⁻)	320 procs	17.7×10 ⁶

Intel Xeon 2.66 GHz, single processor

*Not from LAMMPS

Courtesy of Steve Plimpton, Sandia
<http://lammps.sandia.gov/bench.html>

Example: Mechanical Properties of Metals COMB1

COMB1 potential for Cu/Al

- Single component system ($q_i=0$)

$$E_T = E_{Tersoff} + E_{bb}$$

Does $E_{bb}=0$ work for Cu/Al ?

Cohesive energy (eV/atom)	Fcc Cu	Hcp Cu
Expt.	-3.54	(+0.012)
DFT	-3.495	(+0.006)
COMB	-3.54	(+0.0)

With first nearest neighbor shell, fcc and hcp structures can't be distinguished without E_{bb} !

TABLE 1 Properties of the first five coordination shells

		Neighbour				
		1st	2nd	3rd	4th	5th
f.c.c.	Number of neighbours	12	6	24	12	24
	Separation/ d_0	1	$2^{1/2}$	$3^{1/2}$	$4^{1/2}$	$5^{1/2}$
h.c.p.	Number of neighbours	12	6	2	18	12
	Separation/ d_0	1	$2^{1/2}$	$(8/3)^{1/2}$	$3^{1/2}$	$(11/3)^{1/2}$

Applying the potential to 3rd nearest neighbor shell solves the problem, but efficiency is significantly compromised !

E_{bb} : Legendre Polynomial

$$P_0(x) = 1$$

$$P_1(x) = x$$

$$P_2(x) = \frac{1}{2}(3x^2 - 1)$$

$$P_3(x) = \frac{1}{2}(5x^3 - 3x)$$

$$P_4(x) = \frac{1}{8}(35x^4 - 30x^2 + 3)$$

$$P_5(x) = \frac{1}{8}(63x^5 - 70x^3 + 15x)$$

$$w_i = \sum_{j \neq i} \sum_{k \neq i} f_{C_j} f_{C_k} [K_{LP}^1 P^1(\cos \theta_{jik}) + K_{LP}^3 P^3(\cos \theta_{jik})].$$

Bond bending correction

$$E_{bb} = \sum_i \sum_{j \neq i} \sum_{k \neq i} E_{jik} = k \sum_i w_i^{(3)}$$

$$k = (E_{hcp} - E_{fcc}) / 0.833$$

$$\text{Al: } k = 0.035 / 0.833 = 0.042$$

$$\text{Cu: } k = 0.008 / 0.833 = 0.0095$$

Properties of Al (unpublished)

- Fitted properties

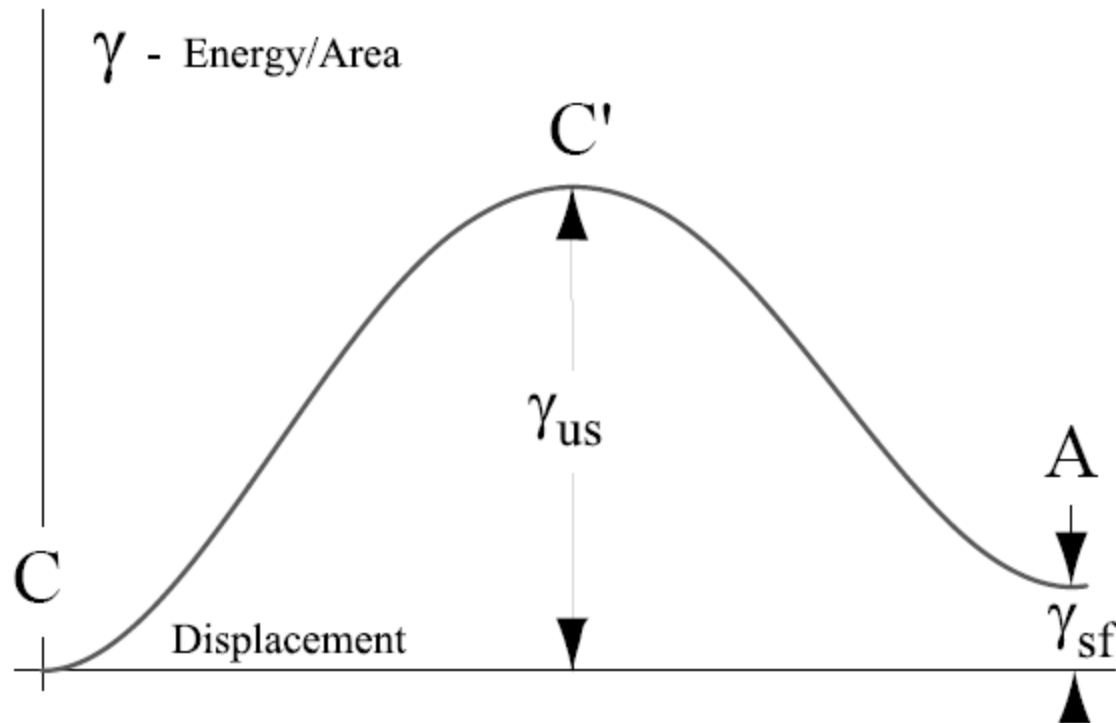
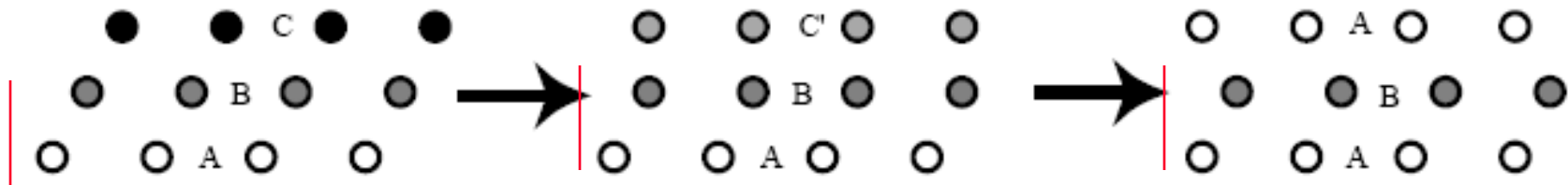
	Exp	DFT	COMB
a_0 (Å)	4.05	4.04	4.047
E_c (eV/atom)	-3.39	-3.40	-3.39
B (GPa)	79	73	72
C_{11} (GPa)	114	113	95
C_{12} (GPa)	62	53	60
C_{44} (GPa)	32	30	35
E (hcp-fcc) (eV/atom)	--	0.035	0.750

- Predicted properties

	Exp	DFT	COMB
γ (100) (mJ/m ²)	980*	928	1026
γ (110) (mJ/m ²)	980*	992	1193
γ (111) (mJ/m ²)	980*	817	806
E (dia-fcc) (eV/atom)	--	0.750	1.680
Intrinsic SF (mJ/m ²)	--	22	48

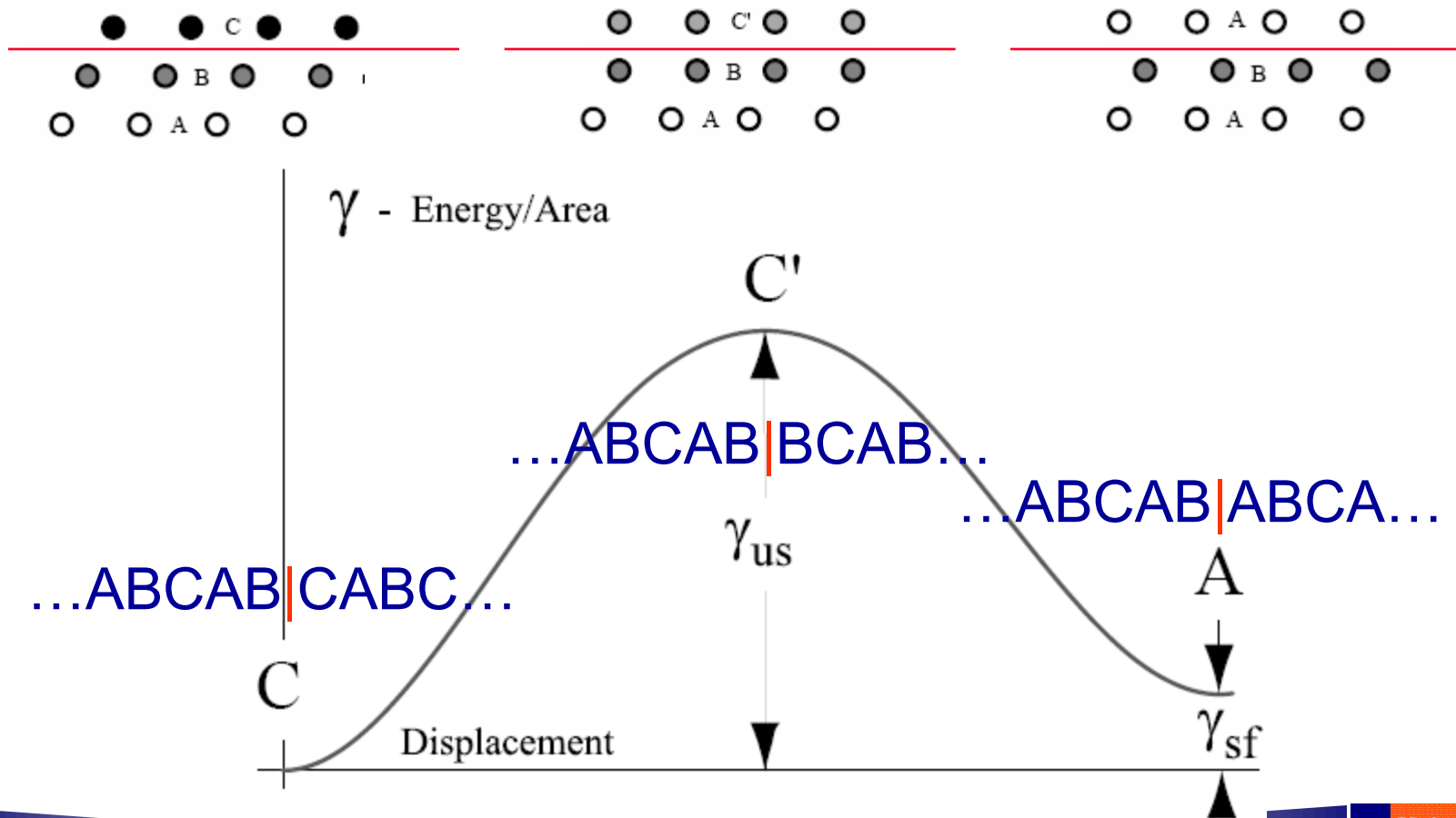
Stacking fault energies of fcc metals

- Stacking fault occurs along $\langle 211 \rangle$

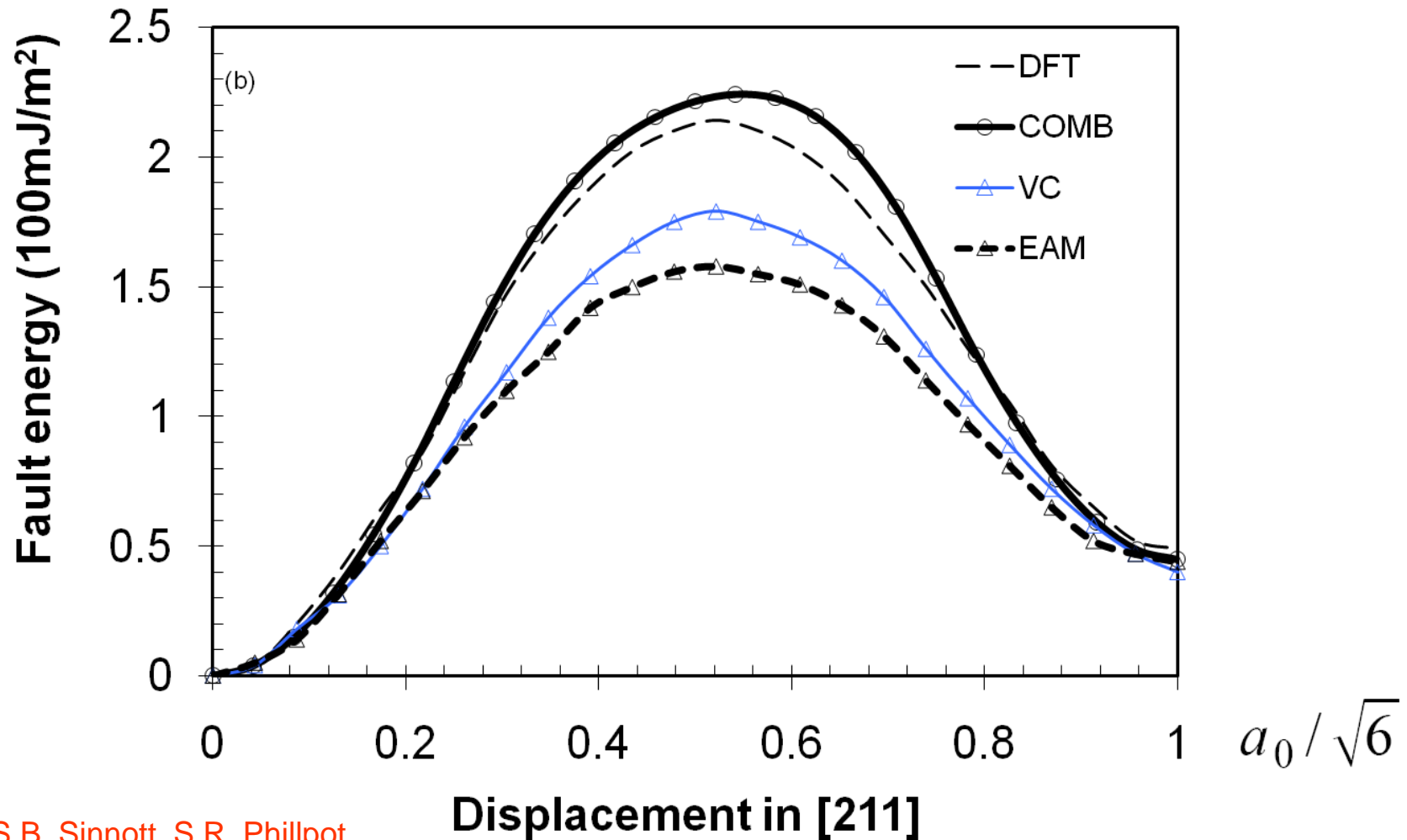


Stacking fault energies of fcc metals

- Displacement along $\langle 211 \rangle$



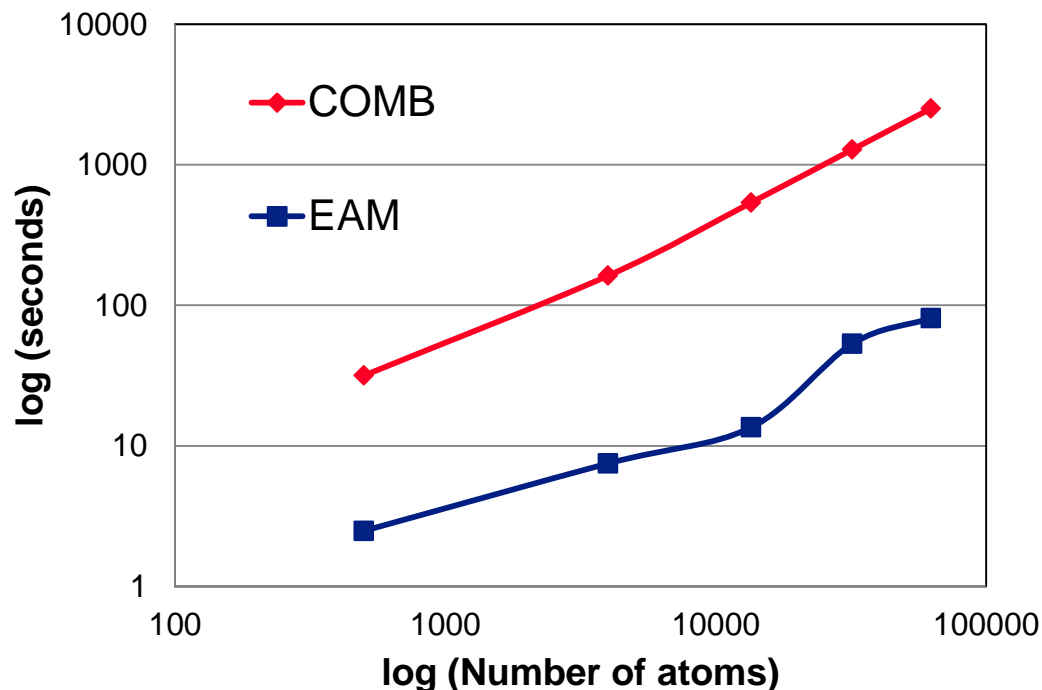
Stacking fault energies – Cu



J. Yu, S.B. Sinnott, S.R. Phillpot,
Phil. Mag. Lett. **89**, 136 (2009)

Simulation of a Cu Crystal

- Scaling of COMB1 and EAM in LAMMPS
 - System sizes vary from 500 to 64,000 atoms
 - 8 CPUs, Intel Xeon 2.27 GHz



	EAM ¹	COMB ²
a_0 (Å)	3.615	3.615
E_{coh} (eV)	-3.54	-3.51
C_{11} (GPa)	170	169
C_{12} (GPa)	123	119
C_{44} (GPa)	76	52
MD Time (seconds. 10^3 atom^{-1} . 10^3 steps^{-1})	2.1	44.8

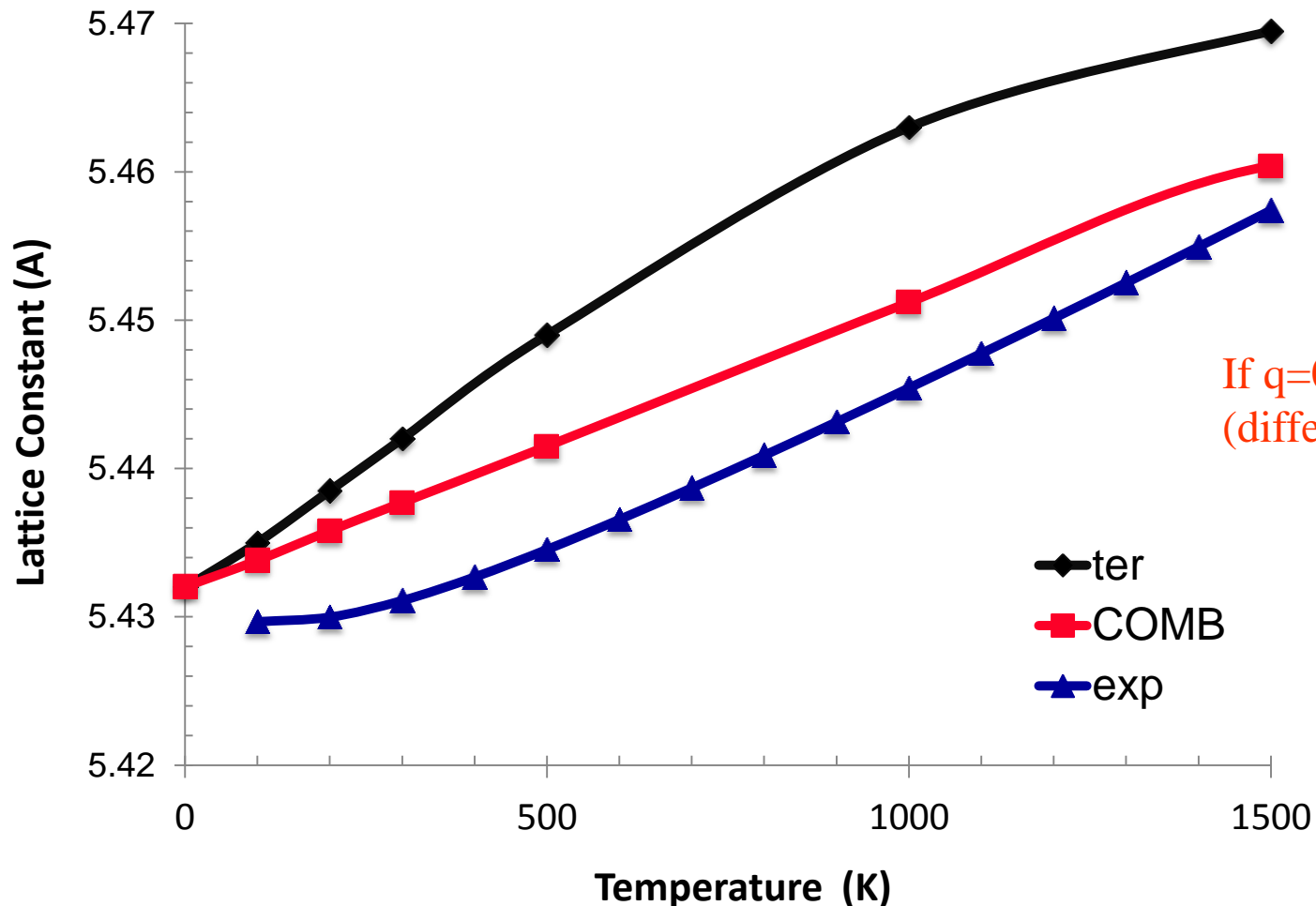
- COMB1 costs ~25 times more than EAM ²

¹Y. Mishin, JM Mehl, DA Papaconstantopoulos, AF Voter, JD Kress, *Phys. Rev. B* 63, 224106 (2001).
²J Yu, SR Phillpot, SB Sinnott, *Phys. Rev. B* 75, 233203 (2007).

Example: Illustration of Costs and Benefits for Si/SiO₂ COMB2

How does COMB do for Si/SiO₂ ?

- Lattice Constant vs. Temperature for Si



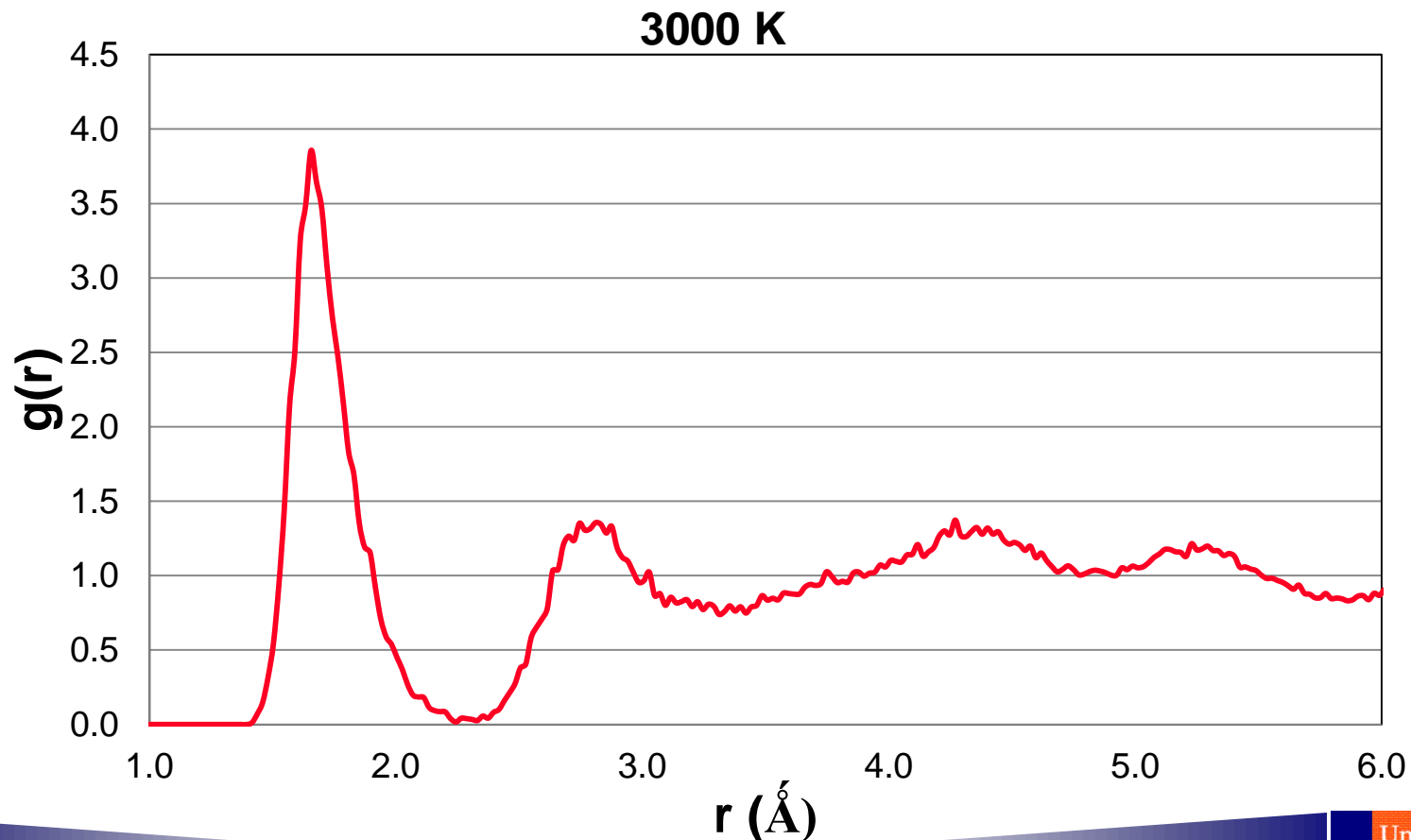
α -Cristobalite surface energies

Surface termination	Surface energy (mJ/m ²)	
	DFT-LDA ^a	COMB
SiO ₂ (α -C):Si	1795	1491
SiO ₂ (α -C):O	1185	1073
SiO ₂ (α -C):OO	917	839

^a VASP calculations, computational set adapted from “K. Nagao, J.B. Neaton, N.W. Ashcroft, *PRB* 68 125403 (2003)”

Amorphous SiO₂

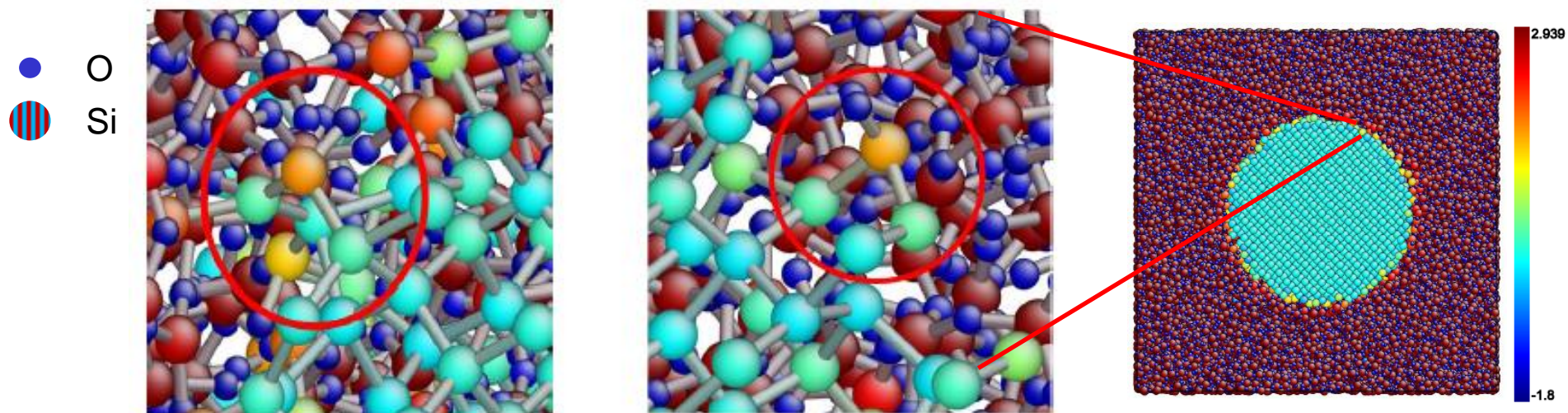
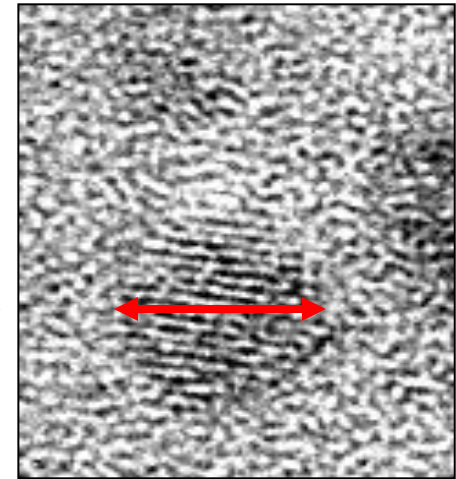
- Amorphous silica is the most stable polymorph
 - Most challenging SiO₂ polymorph to model



Si Nanocrystals Embedded in a-SiO₂

- Si nanocrystals (NCs) emit visible light and the extent of the emission depends on the
 - Size of the Si-NC
 - Structure of the Si-NC/a-SiO₂ interface
 - Silanone bonds (Si=O double bond)

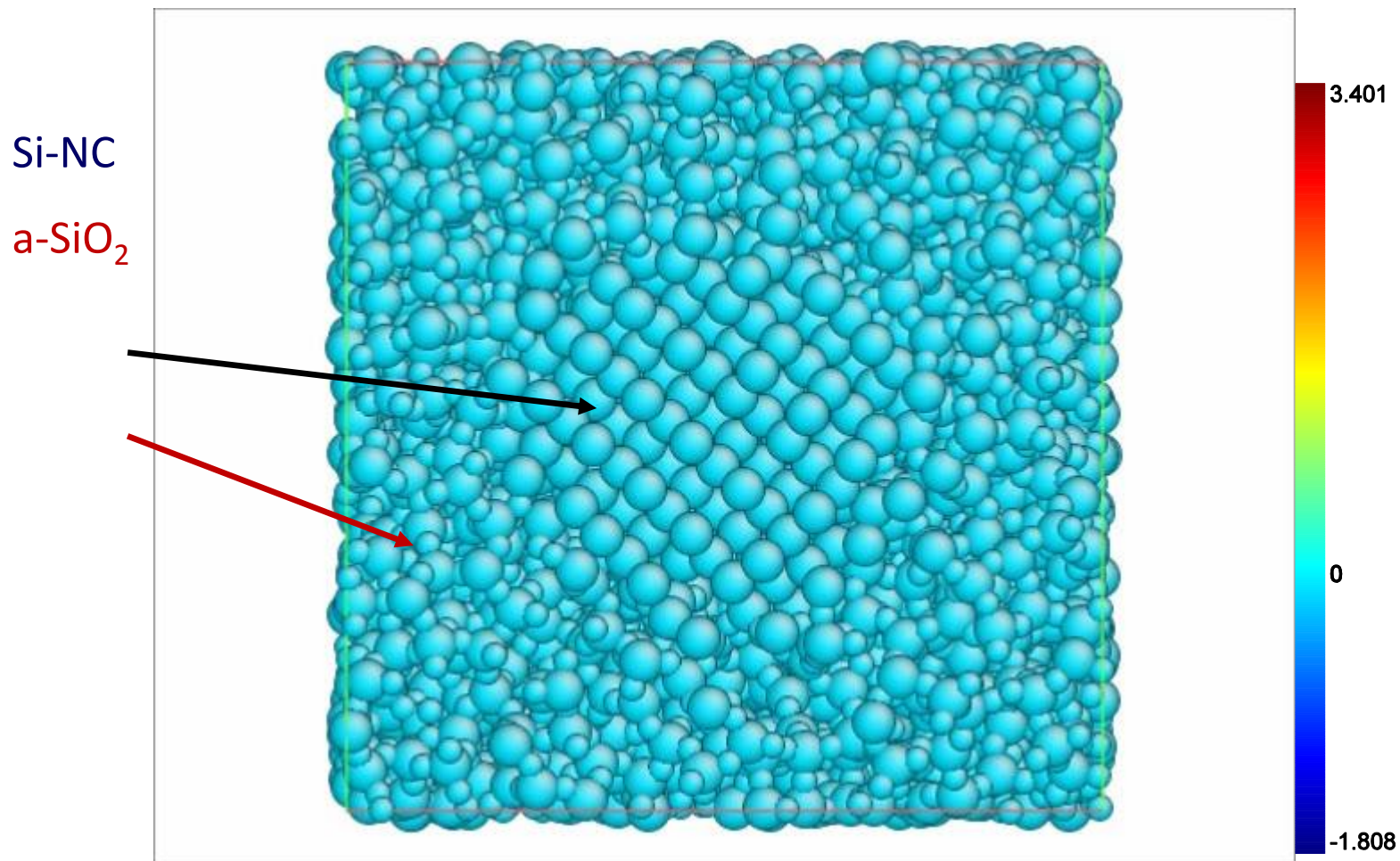
10 nm in diameter



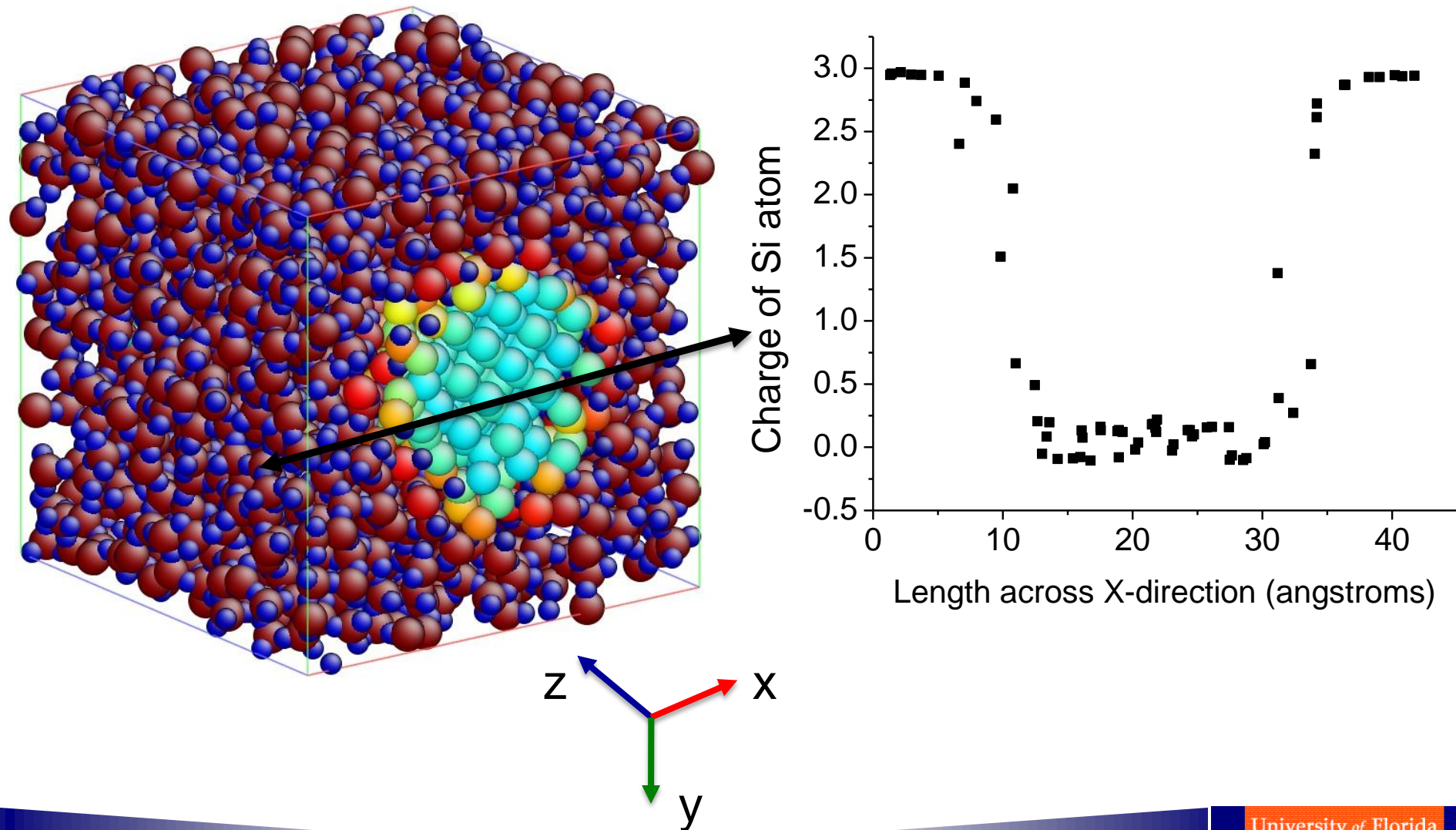
In collaboration with Flyura Djurabekova and Kai Nordlund at the University of Helsinki

F. Djurabekova, M. Backholm, M. Backman, O. H. Pakarinen, J. Keinonen, K. Nordlund, T.-R. Shan, B. D. Devine, and S. B. Sinnott, *Nucl. Instr. Meth. Phys. Res. B* 268 19 3095 (2010).

Variable Charge Equilibration

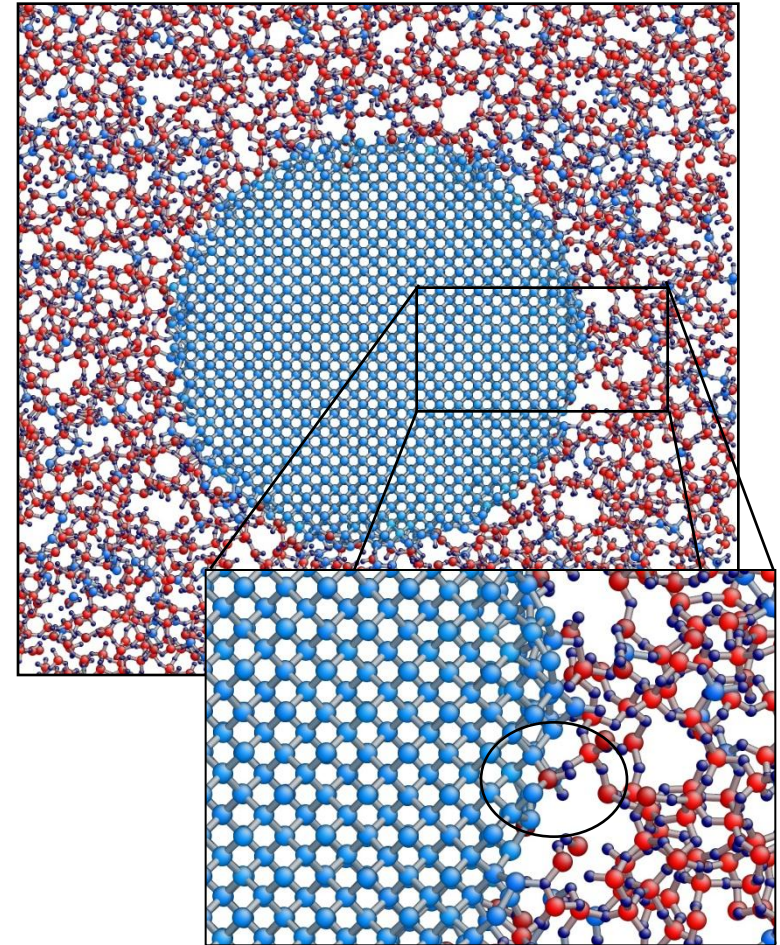
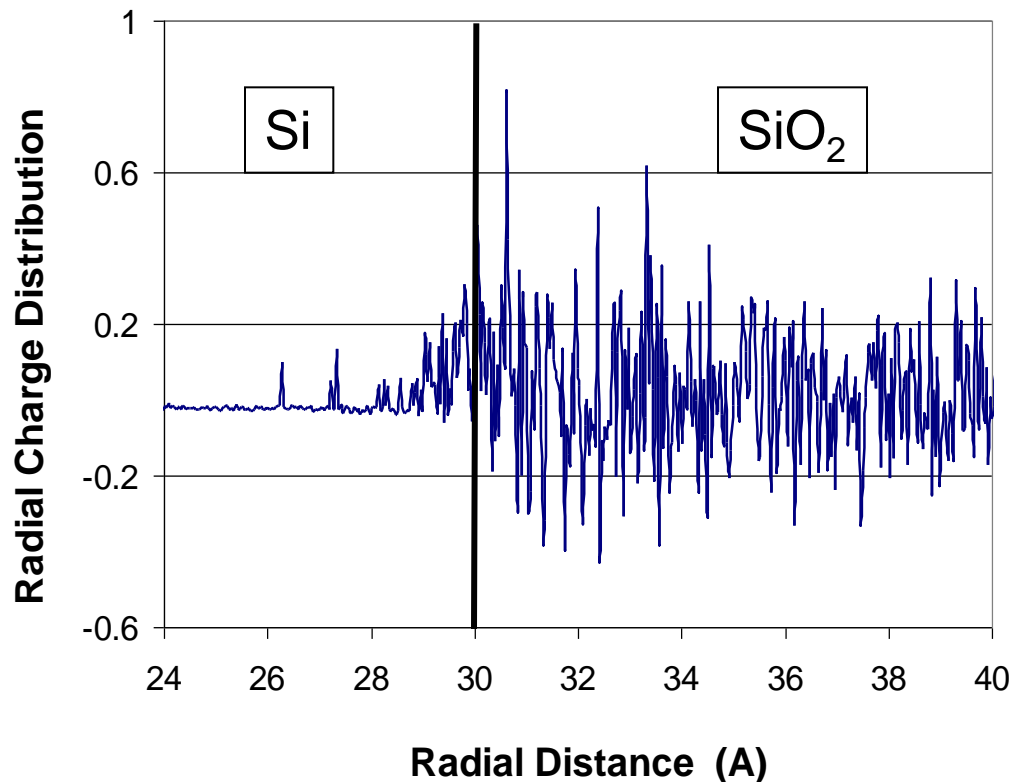


Charge Distribution of a 2 nm NC



Charge Equilibrated MD of nc-Si/SiO₂

Simulations reveal charge spilling and defects at the interface

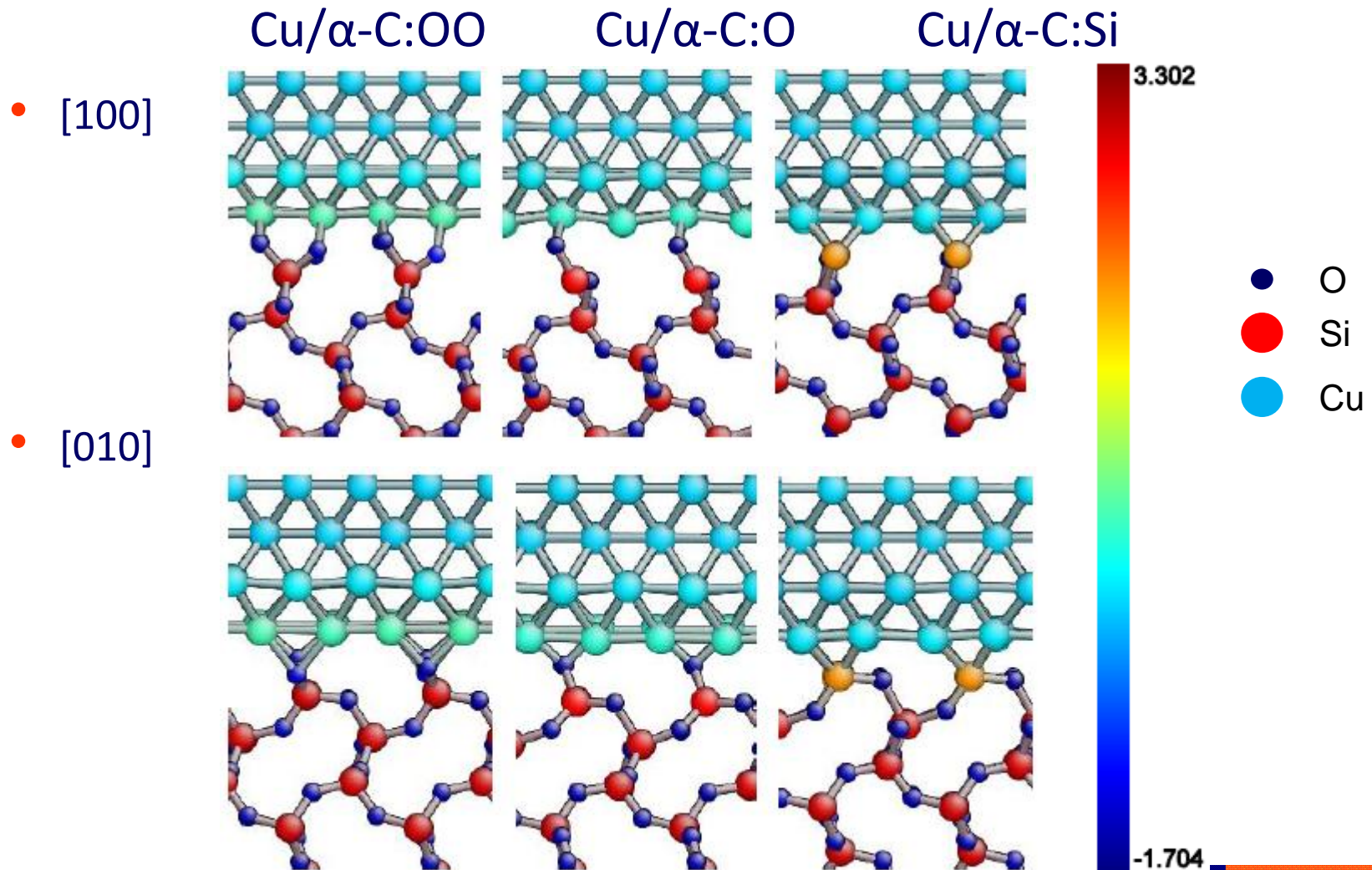


Applications

- Heterogeneous Interfacial Structures

COMB2

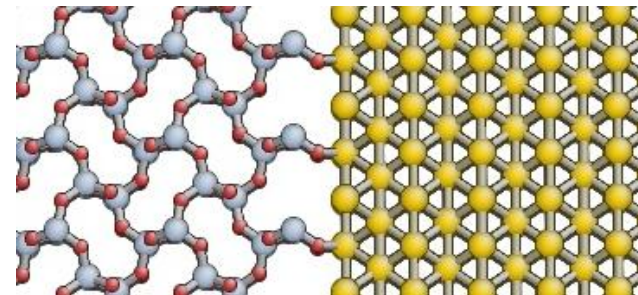
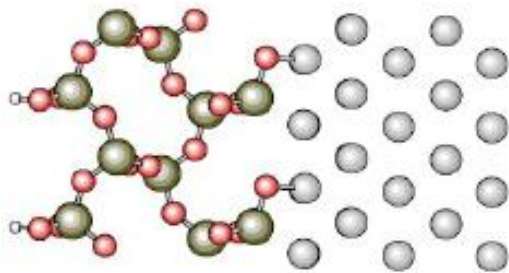
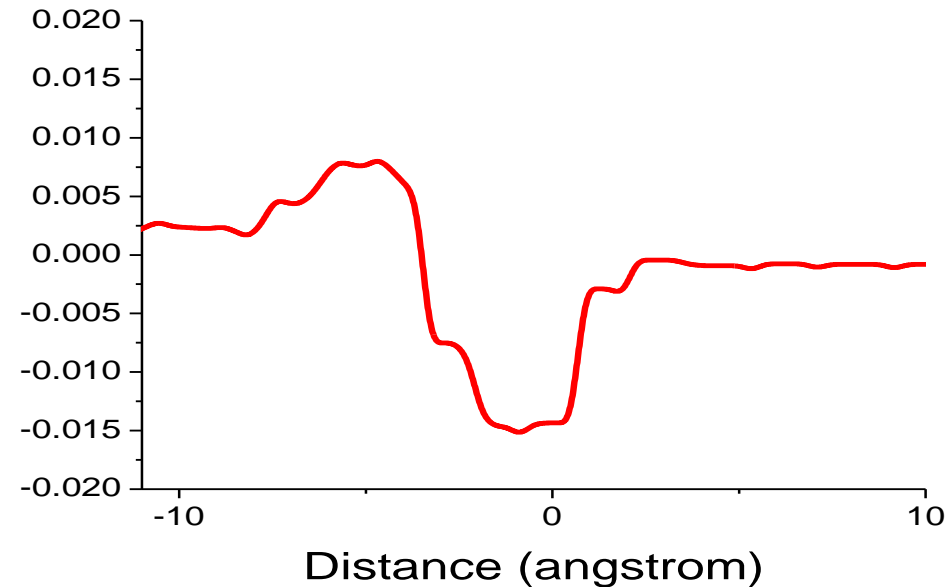
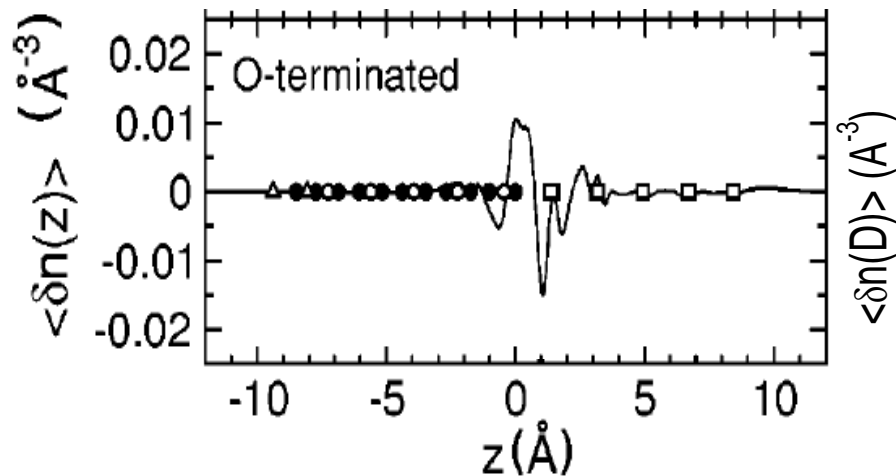
Cu (001)/ α -cristobalite (001) Interfaces



Charge Transfer Across the Interface

- Electron density difference

- $\langle \delta n(z) \rangle = \langle n_{\text{IF}}(z) \rangle - [\langle n_{\text{SiO}_2}(z) \rangle + \langle n_{\text{Cu}}(z) \rangle]$



Cu (001)/ α -cristobalite (001) Interfaces

- Adhesion energy = $(E_{SiO_2} + E_{Cu} - E_{Cu/SiO_2})/A_{IF}$
 - Quantifies the adhesive strength of the interfaces (unit: J/m²)

Type of interface	DFT-LDA ^a	DFT-LDA ^{b, c}	DFT-GGA ^c	COMB ^c
Cu/ α -C:Si	1.406	1.432	1.034	0.864
Cu/ α -C:O	1.555	1.591	1.222	1.734
Cu/ α -C:OO	3.805	3.987	3.601	3.591

- Average interfacial bond lengths *Expt. ~ 4 J/m²*

	DFT-LDA	DFT-GGA	COMB
Cu-O	1.90 Å	1.93 Å	1.86 Å
Cu-Si	2.40 Å	2.47 Å	2.32 Å

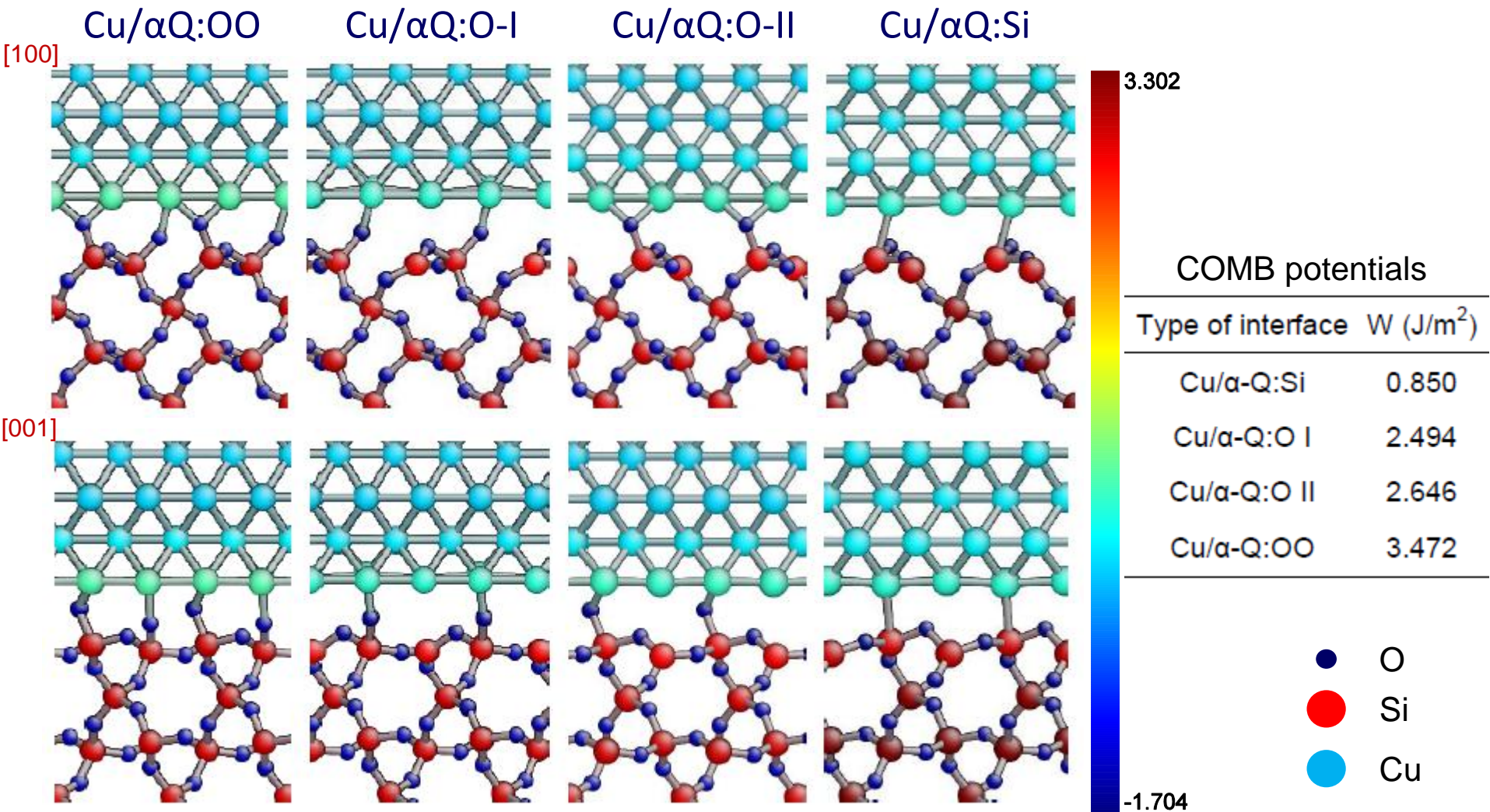
COMB potential reproduces structural and adhesive properties of Cu/ α C

^a K. Nagao, J.B. Neaton, N.W. Ashcroft, *Phys. Rev. B* 68 125403 (2003)

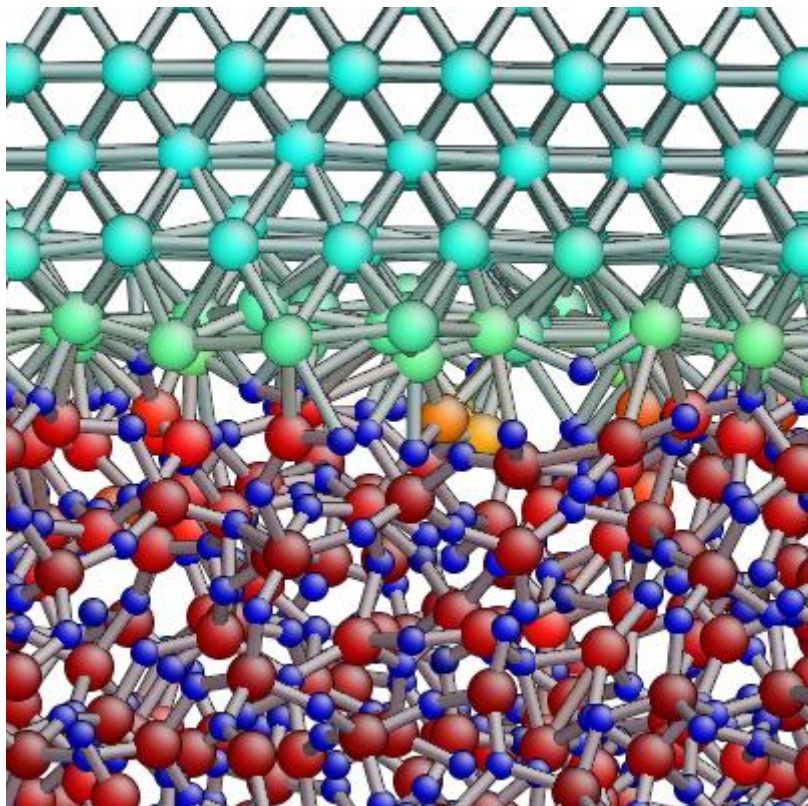
^b VASP calculations with computation details adapted from Ref ^a, except US for Si

^c T.-R. Shan, B. D. Devine, S. Phillpot, S. Sinnott, *Phys. Rev. B* 83 115327 (2011)

Cu (001)/ α -quartz (010) Interfaces



- Structural properties of the interface
 - Oxidation of Cu is limited to the first two Cu layers; formation of Cu₂O



- Introduced O vacancies at the interface
 - 0, 10 and 20 V_O

Type of interface	W (J/m ²)		Cu-O (%)
	Exp	COMB	
Cu/a-SiO ₂ + 0 V _O	0.5 - 1.2 ^a	1.810	22
Cu/a-SiO ₂ + 10 V _O		0.629	13
Cu/a-SiO ₂ + 20 V _O	0.6 - 1.4 ^b	0.289	11

- Cu-O bonds play crucial roles in adhesion of the interface
- Adhesion of Cu/dielectric layer decreases with O defects

^a T. S. Oh, R. M. Cannon, and R. O. Ritchie, *J. Am. Ceram. Soc.* 70, C352 (1987).

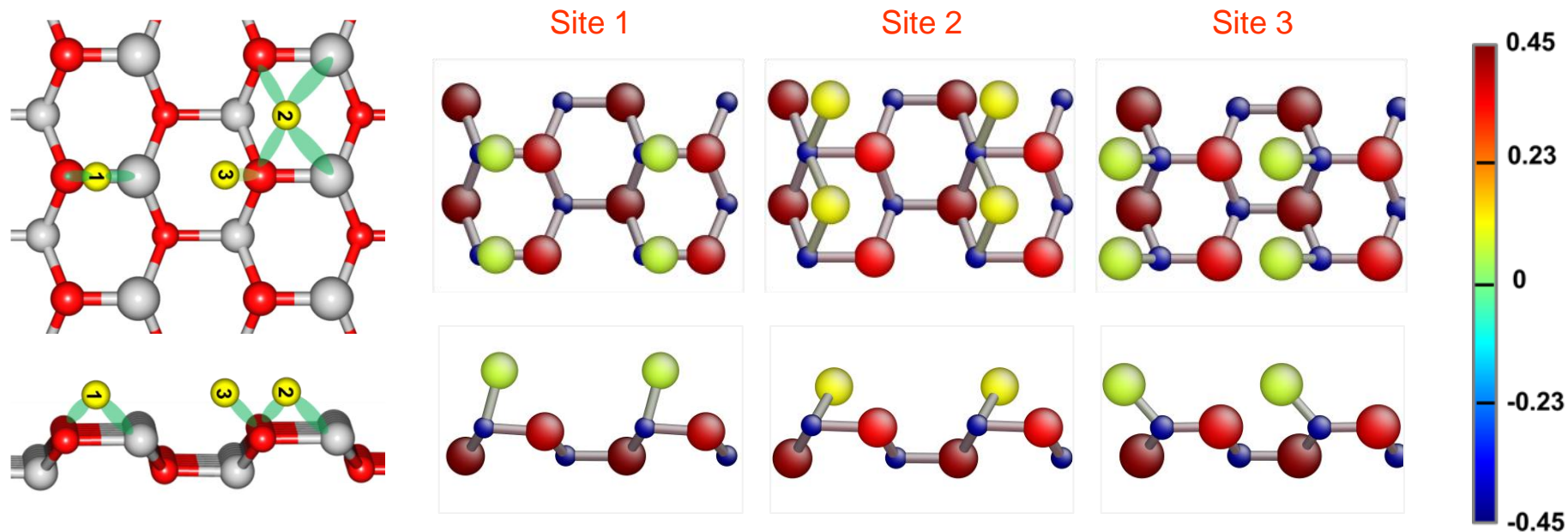
^b M. Z. Pang and S. P. Baker, *J. Mater. Res.* 20, 2420 (2005).

Applications

-Atoms and Clusters on Surfaces

COMB3

Adsorption of Cu adatom on ZnO(10 $\bar{1}0$)



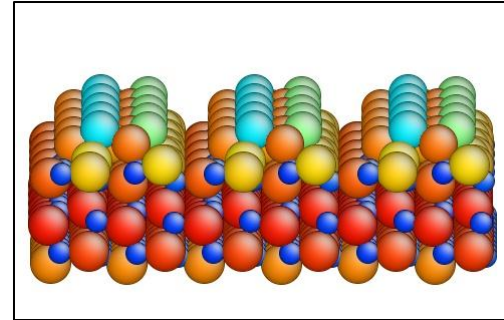
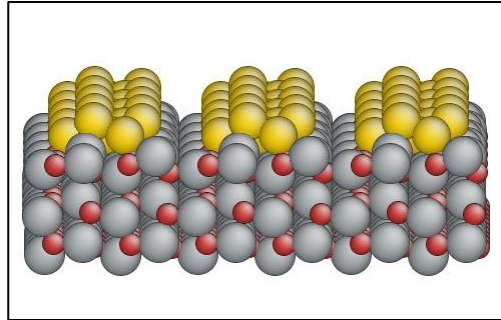
$$E_{\text{ads}} = E_{\text{ZnO}} + E_{\text{Cu}} - E_{\text{Cu/ZnO}}$$

Adsorption E (eV)	Site 1	Site 2	Site 3
DFT-PBE	1.81	1.88	2.09
COMB	1.87 (+3.3%)	1.92 (+2.1%)	1.96 (-6.2%)

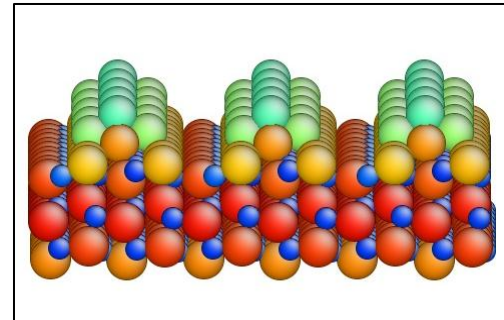
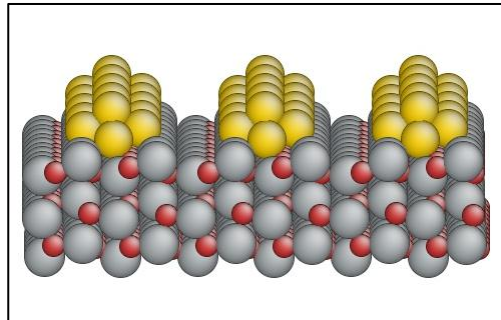
Cu_X Clusters on the ZnO⁻(1010) Surface

X=5

planar



stack

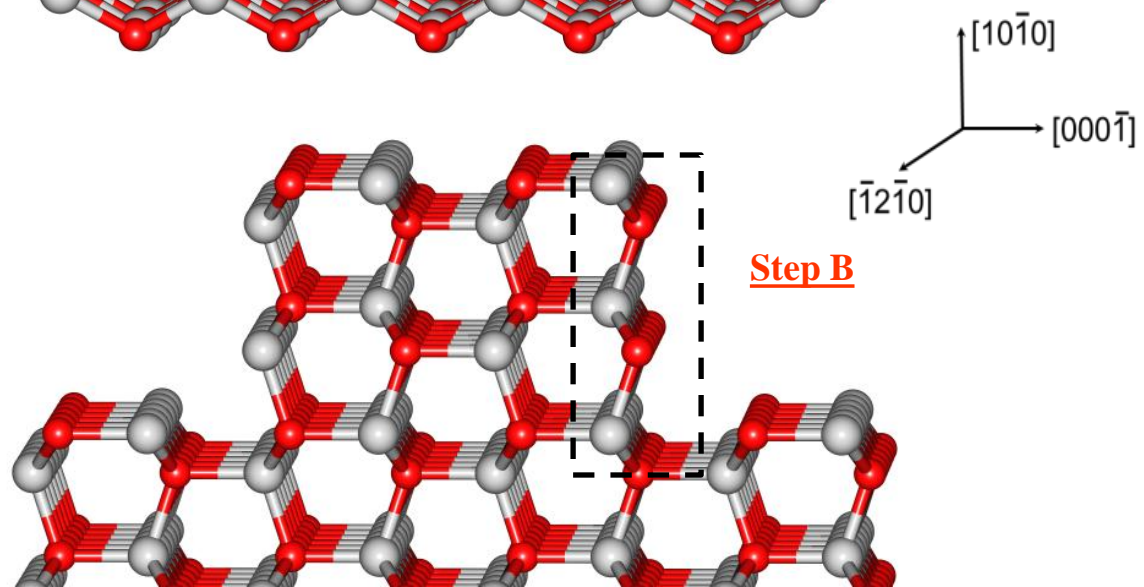
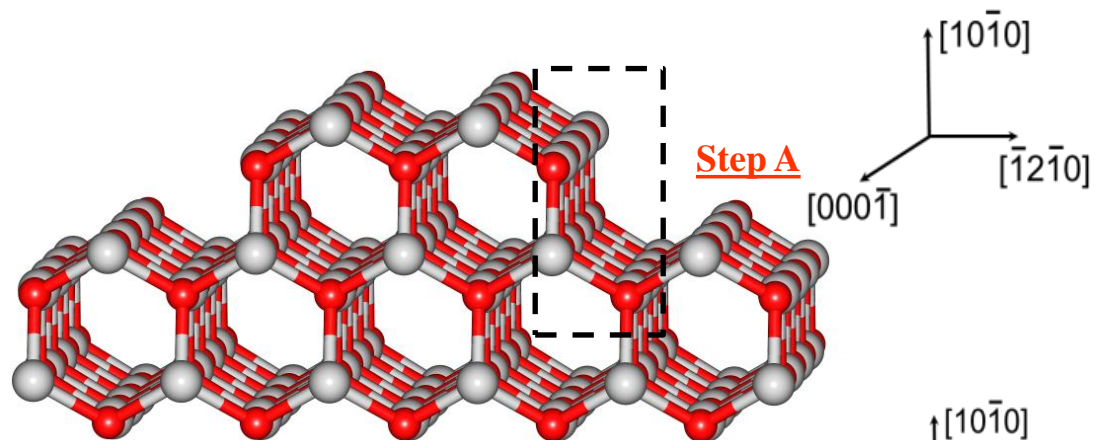
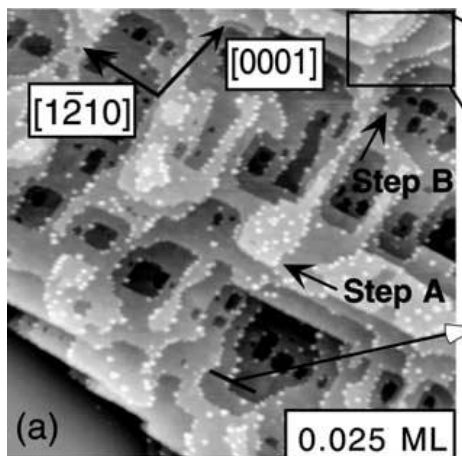
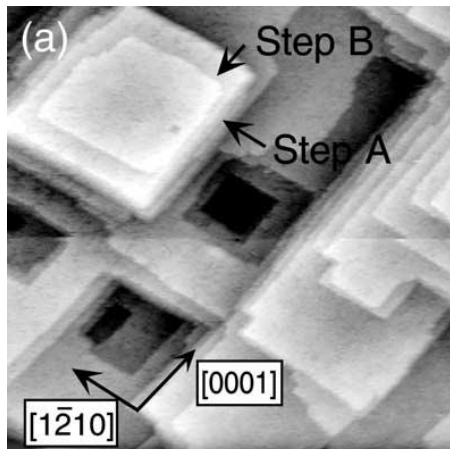


Binding energy (eV)

	X=3		X=4		X=5	
	Row	Stack	Flat	Stack	Planar	Stack
DFT	-2.33	-2.37	-2.28	-2.33	-2.31	-2.35
COMB	-3.40	-3.46	-3.24	-3.89	-3.17	-3.59

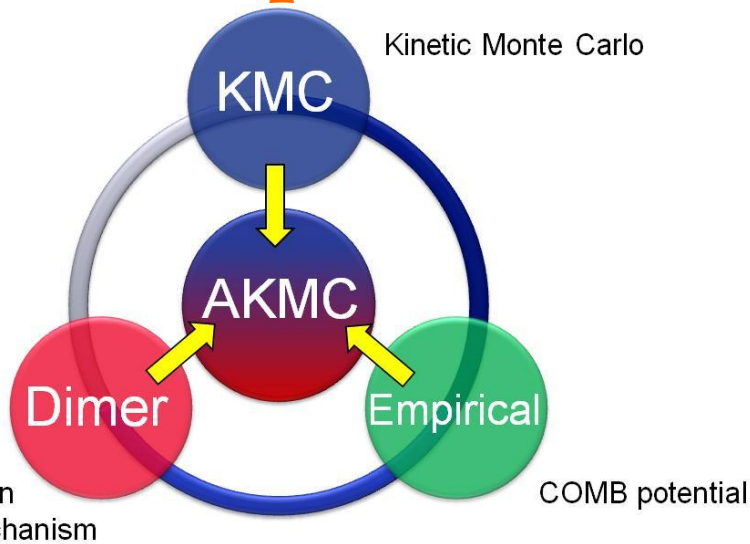
*DFT results courtesy of Xiaowa Nie, Ohio State

Growth of Cu clusters on ZnO surfaces



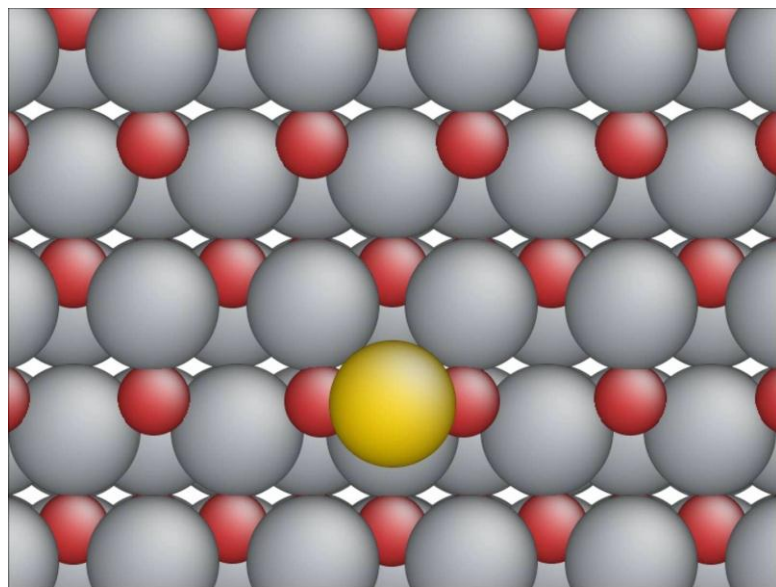
O. Dulub, L. A. Boatner, U. Diebold, Surface Science 504 (2002) 271

Adaptive kinetic Monte Carlo



Dimer method (transition searching):

Using the first derivative of the potential energy and the initial state of the transition to find saddle points.



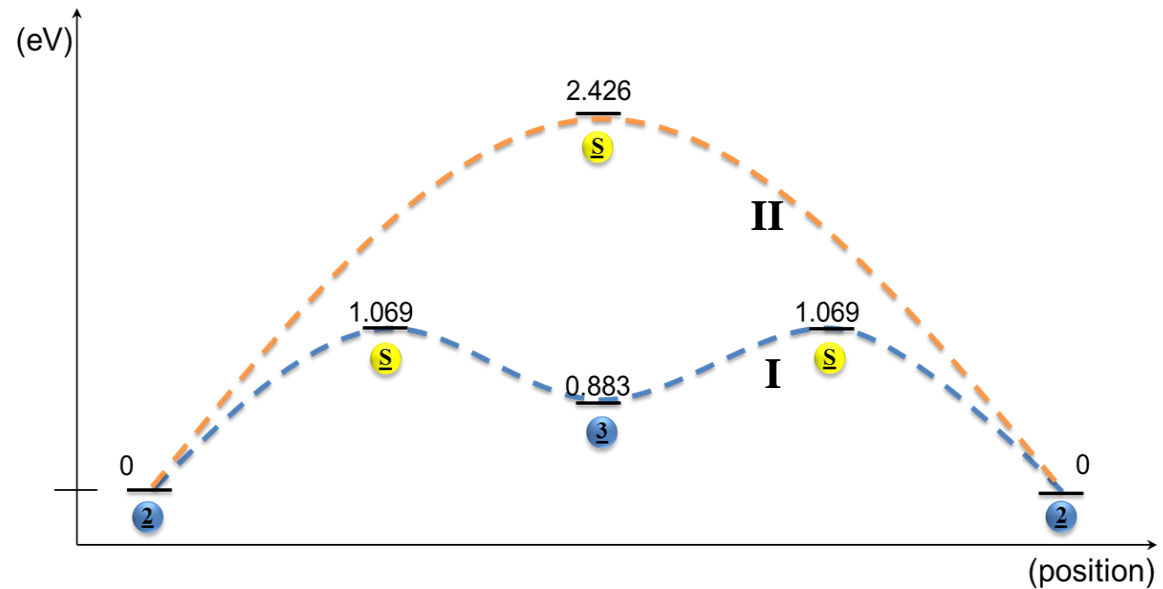
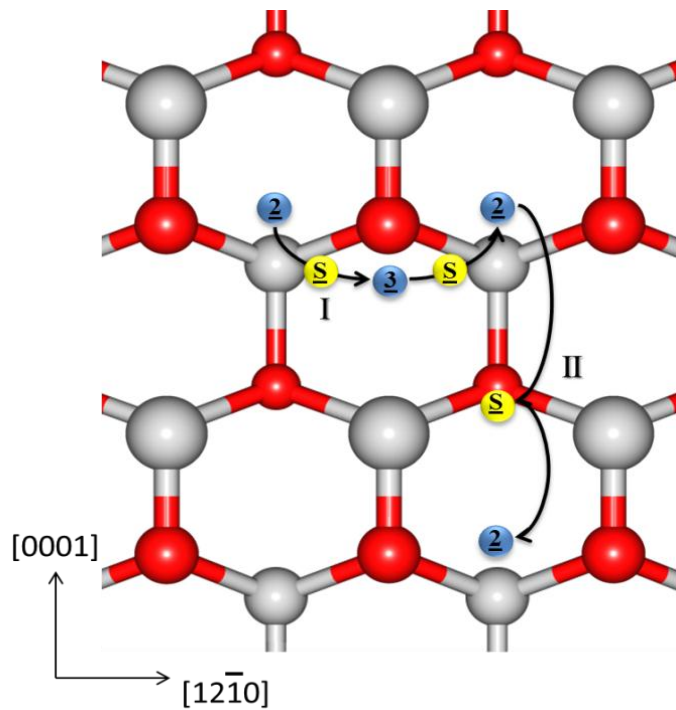
Standard KMC

1. Find low energy saddle point using the dimer method^{1,2}.
2. The rate of each transition path is calculated using HTST. ($r_i = \nu_0 e^{-\Delta E/k_B T}$)
3. Hop to the final state of the chosen process. ($p_i \propto r_i$)
4. Increment time by an average amount Δt . ($\Delta t = -\ln u / \sum r_i$)
5. Repeat from step 1

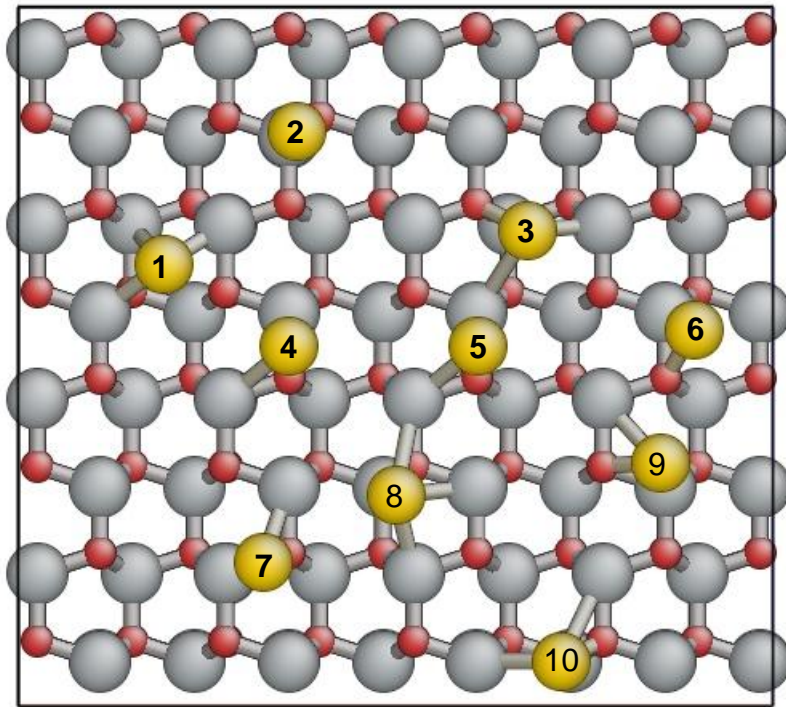
1. G. Henkelman and H. Jonsson, *J. Chem. Phys.* **111**, 7010 (1999)
2. G. Henkelman and H. Jonsson, *J. Chem. Phys.* **115**, 9657 (2001)

Migration barriers of Cu on ZnO(10 $\bar{1}0$)

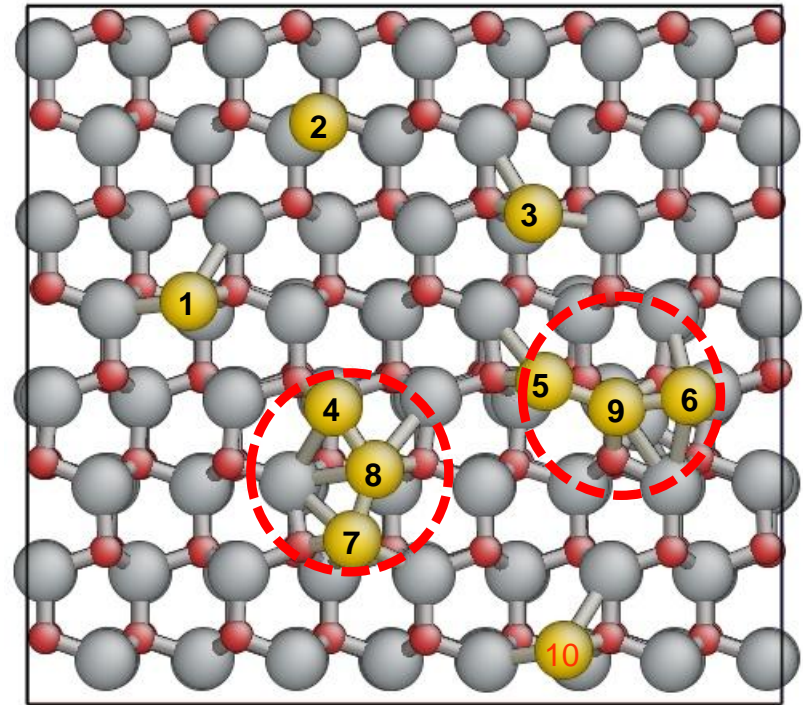
Cu atom migration along $[12\bar{1}0]$ is much easier than along $[0001]$



AKMC: Aggregation of Cu atoms on ZnO(10 $\bar{1}$ 0)



Initial structure
T = 0 ns



After 15 AKMC runs
T = 5 ns

Applications

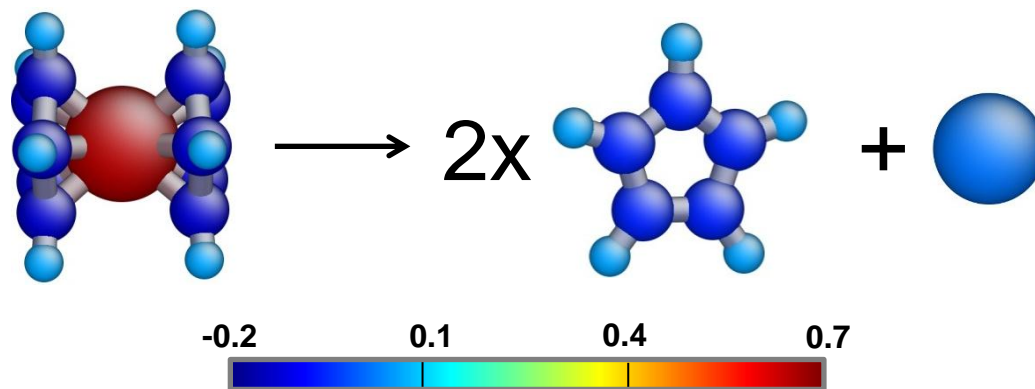
-Surface Chemistry

COMB3

Properties of COMB Potentials

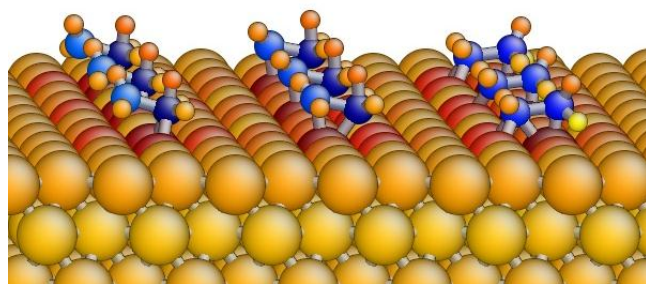
- C/H/Cu

45



Target (kcal mol ⁻¹)	COMB (kcal mol ⁻¹)
122	122

Cu metallocene dissociation

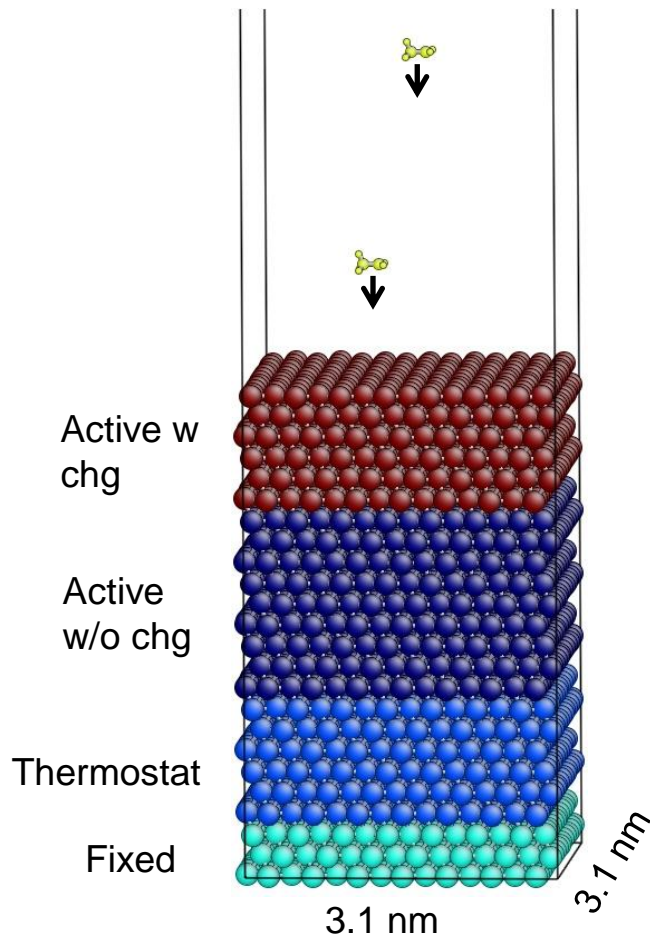


Surfaces	DFT (kcal mol ⁻¹)	COMB (kcal mol ⁻¹)
Cu (100)	-36.2	-46.6 to -24.3
Cu (110)	-39.9	-49.5 to -27.1
Cu (111)	-30.9	-45.3 to -19.7

Ethyl adsorption on Cu surfaces

Xin Li et al., *J Chem Phys* 127, 144710 (2007)

CH₃CH₂ Deposition on the Cu (111) Surface

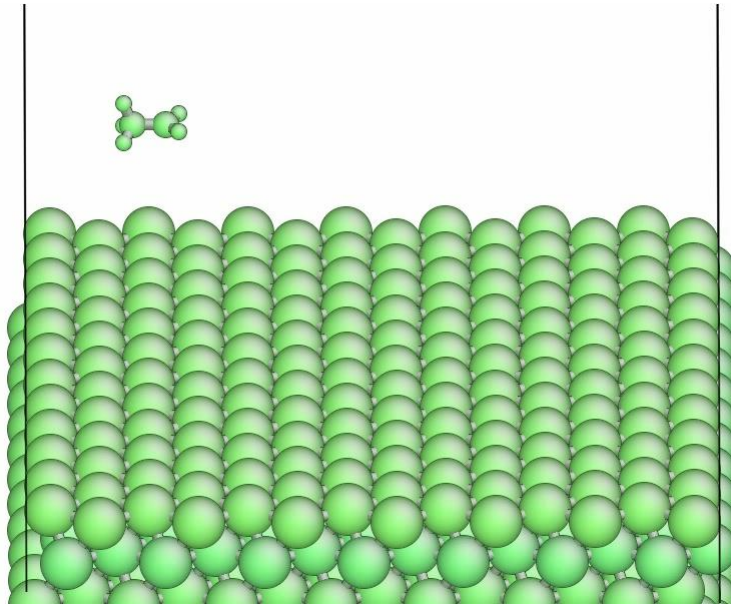


Summary:

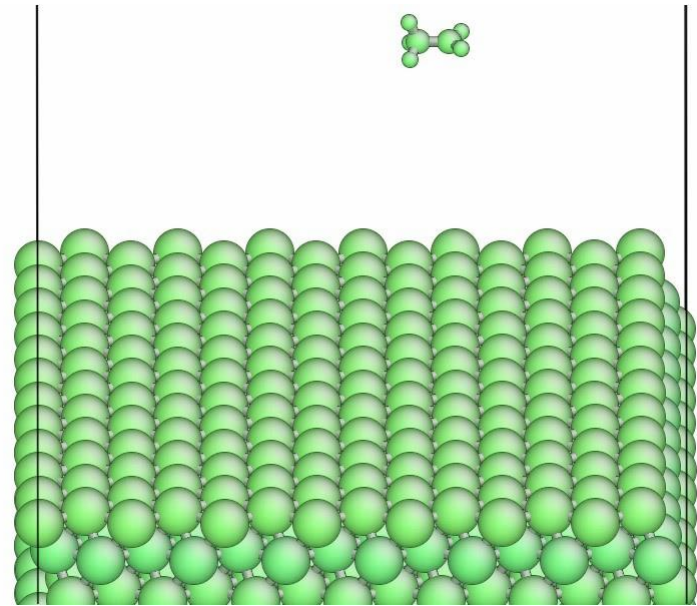
- 12 CH₃CH₂ molecules deposition on Cu(111) surface
- Two incident energy levels
 - 5 eV mol⁻¹
 - 10 eV mol⁻¹
- Molecules are randomly distributed
- The relaxation time between two molecules is 0.5 ps
- Temperature is set to 300K

CH₃CH₂ Deposition on the Cu (111) Surface

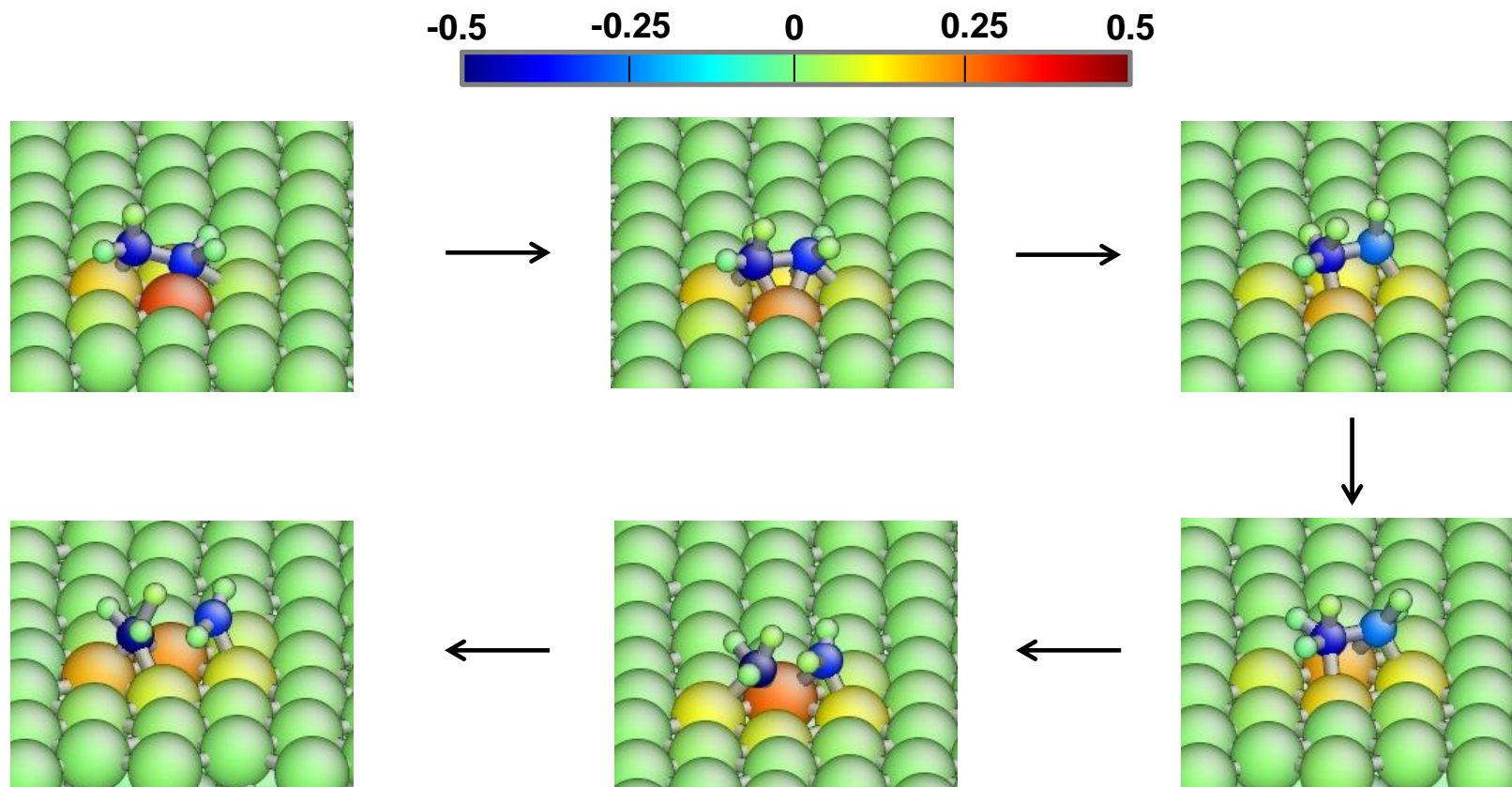
5 eV



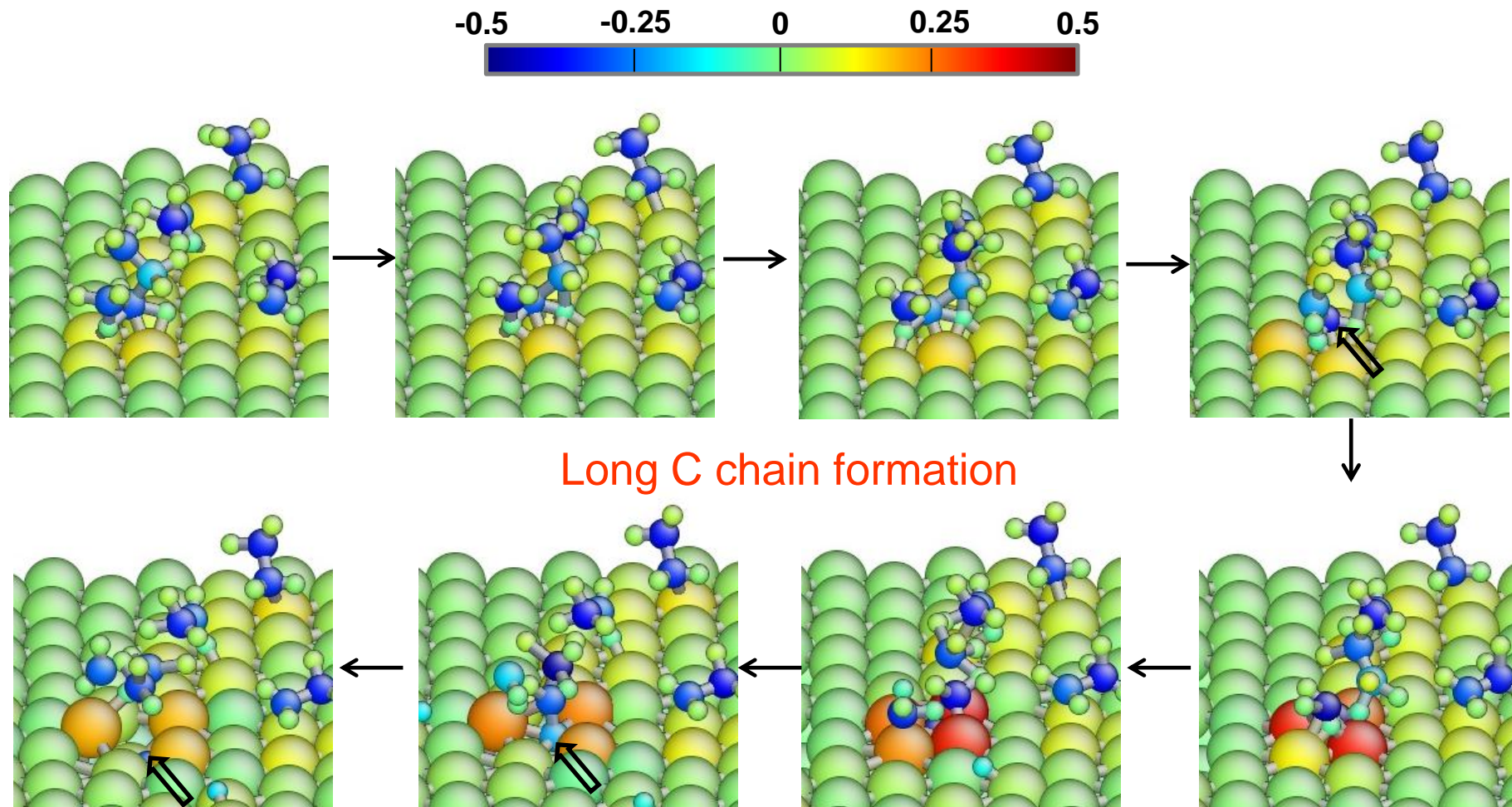
10 eV



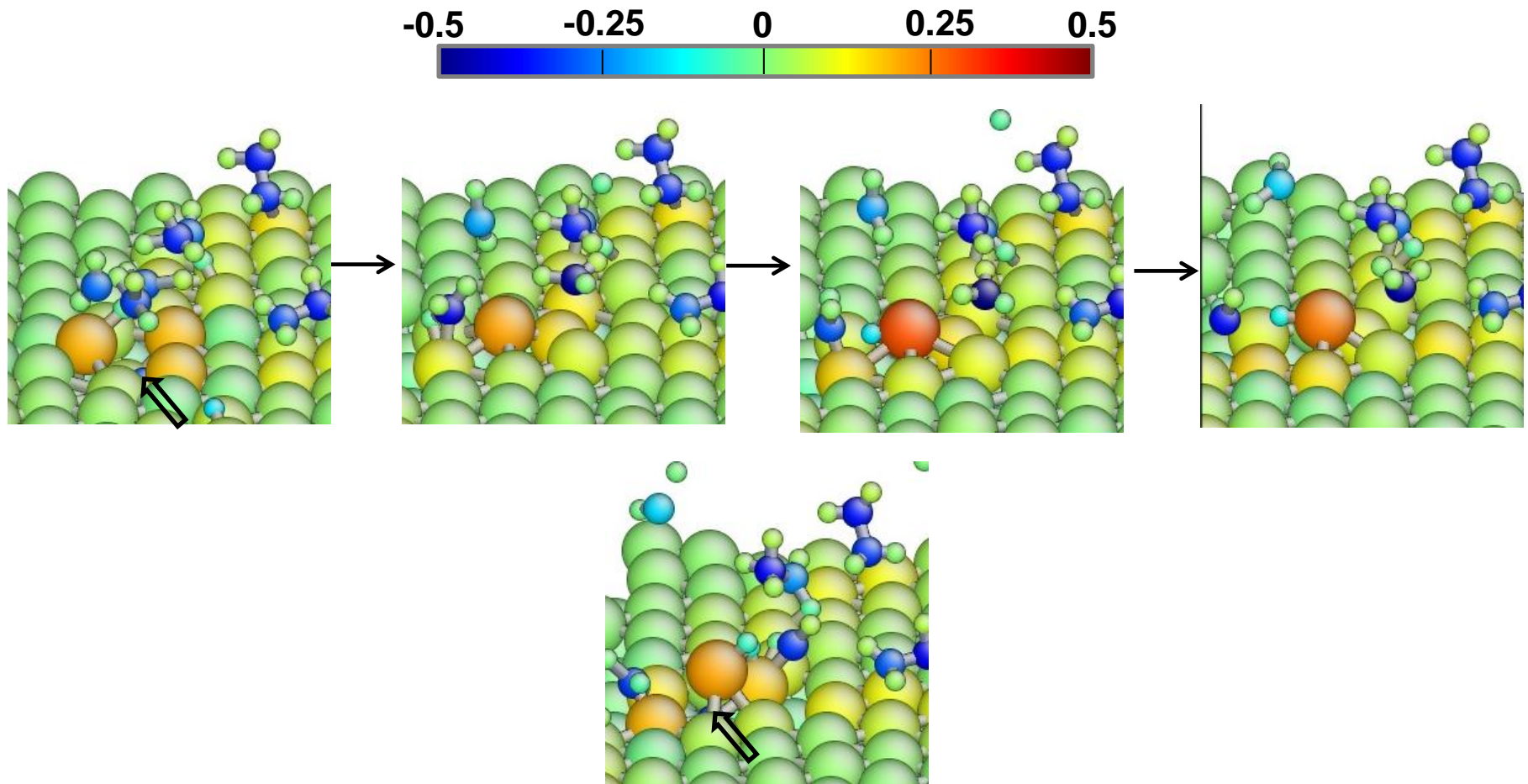
Dissociation of $\text{CH}_3\text{-CH}_2$



Collision-Induced Dissociation Reactions



Displacement of Surface Atoms



Cu^{ko} formation

Applications

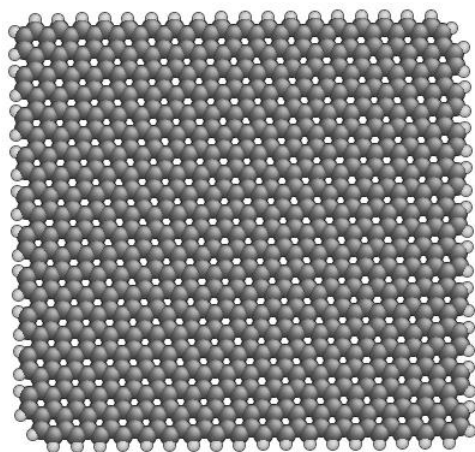
- Graphene Adhesion
to Cu_2O

COMB3

Graphene Adhesion on Cu_2O

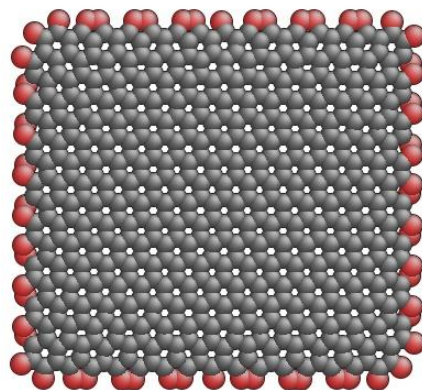
52

796 C atoms



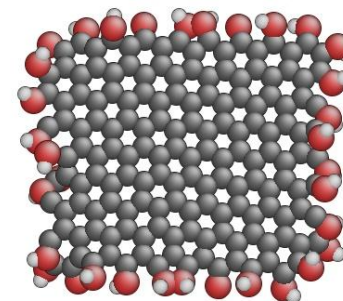
H-Terminated

542 C atoms

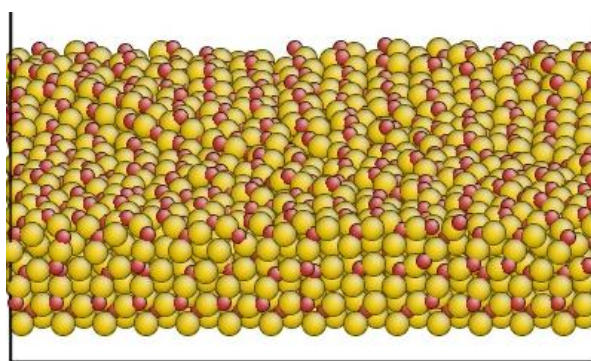


O Terminated

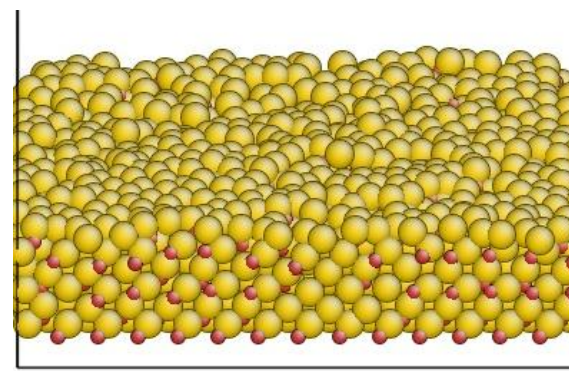
160 C atoms



OH Terminated

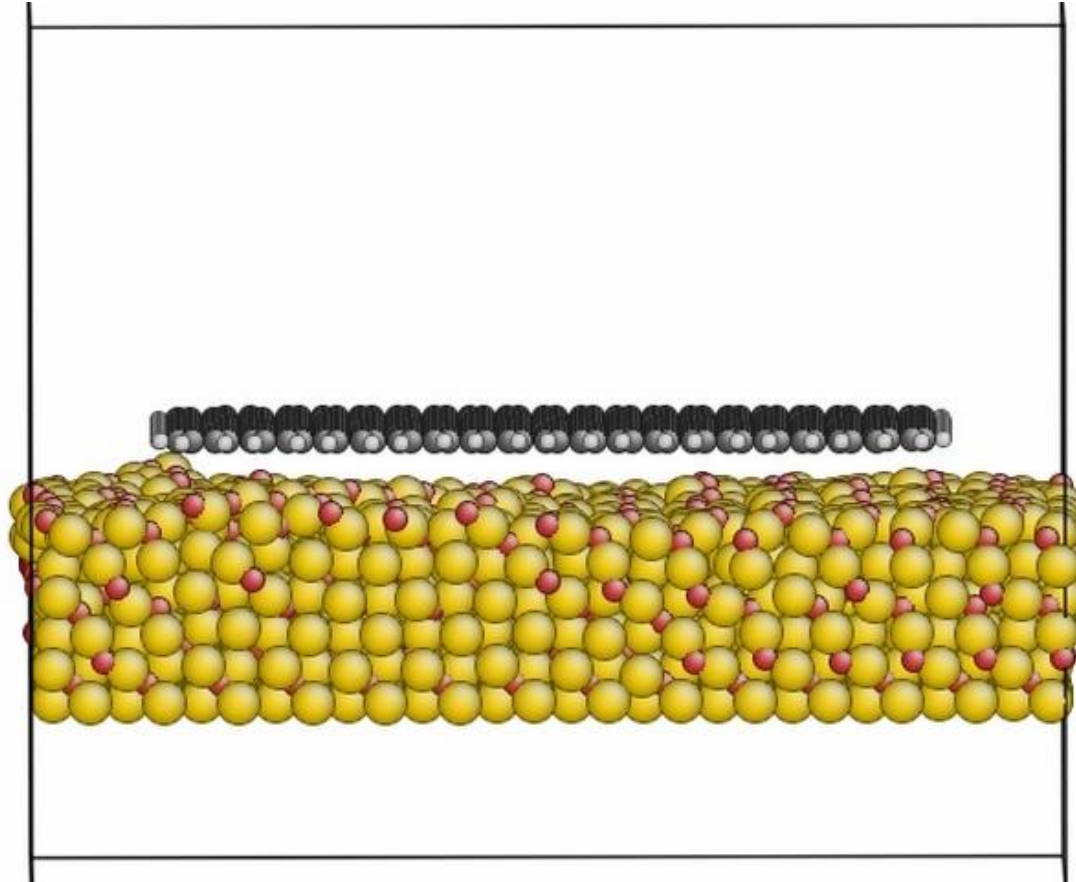


O-Termination



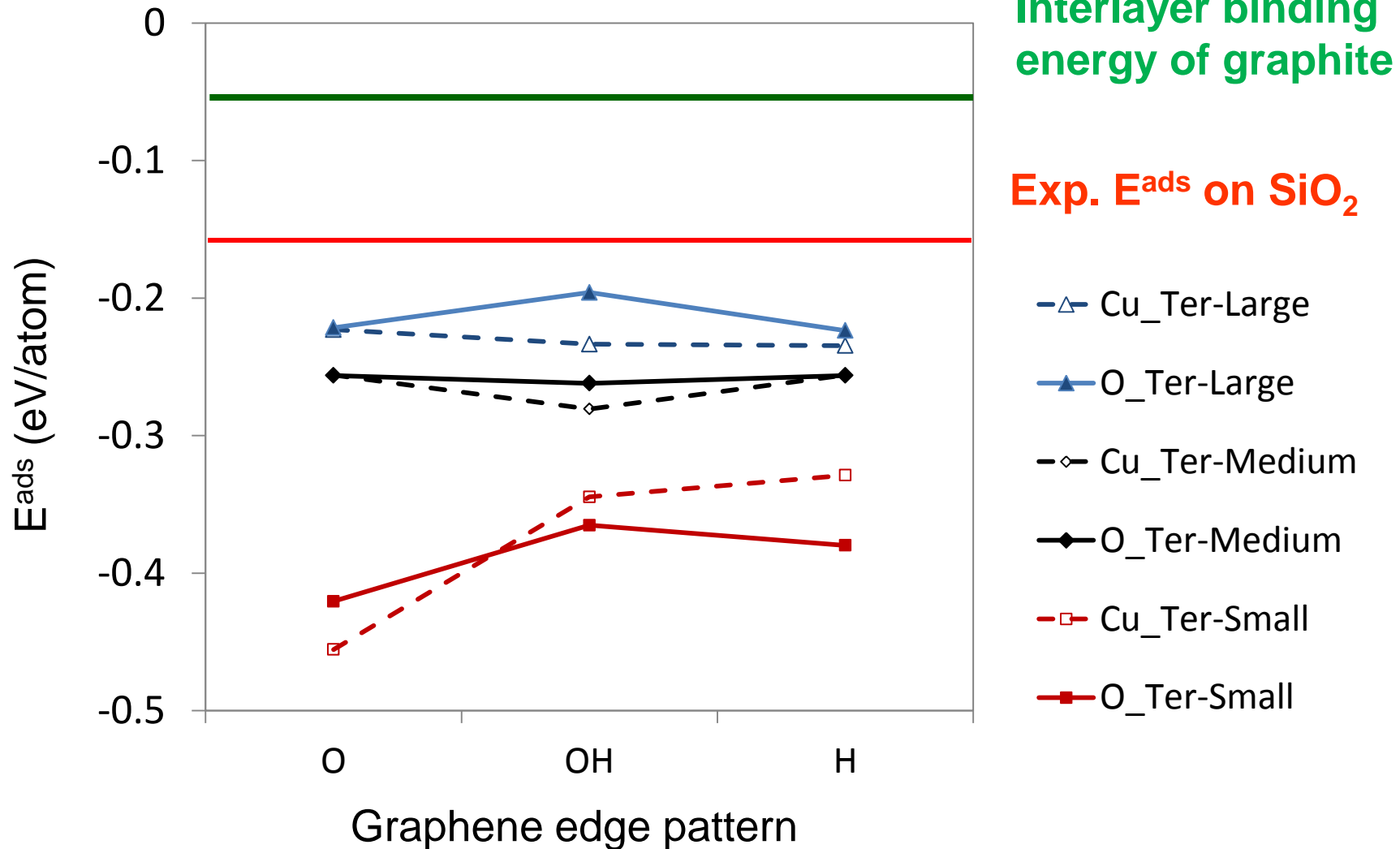
Cu-Termination

Graphene Adhesion on Cu_2O



Graphene Adhesion on Cu_2O

54



Koenig et al. Nature Nano, Sept., 2011.

- Have developed an empirical, variable charge many body (COMB) potential for modeling heterogeneous interfaces
- Successfully applied to atomic-scale simulations of systems consisting of discrete bonding types

