# **Computational Neuroanatomy**

### **Bruce Fischl**

### MGH ATHINOULA A. MARTINOS CENTER Harvard Medical School

### **MIT CSAIL**



# **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of distortion in MRI.
- 4. Linking micro structure to macro structure.

# **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of distortion in MRI.
- 4. Linking micro structure to macro structure.

# Why Is a Model of the Cortical Surface Useful?

#### Local functional organization of cortex is largely 2dimensional!



From (Sereno et al, 1995, Science).

# Why Is Constructing a Model of The Cortical Surface Difficult?

The cortex is highly folded!

- Partial voluming.
- Subject motion.
- Susceptibility artifacts.
- Bias field.
- Tissue inhomogeneities.

Intensity of a tissue class varies as a function of spatial location

# Sources of within-class intensity variation

Partial voluming

a single voxel may contain more than one tissue type.

Bias field

- effective flip angle or sensitivity of receive coil may vary across space.
- Tissue inhomogeneities even within tissue type (e.g. cortical gray matter), intrinsic properties such as T1, PD can vary (up to 20%).

# **T1 weighted MR volume**

### Assigning tissue classes to voxels can be difficult



# Which Surface to Reconstruct?

*Pial surface* is ultimate goal, but pretty much impossible to directly generate a representation of from MRI images (many have tried!).

Alternative: construct an interim representation of the interface between gray matter and white matter, and use it to infer the location of the true cortical surface (Dale and Sereno, 1993).

# Skull Stripping and building of Boundary Element Models



# MRI Segmentation and Surface Reconstruction



# **Topology Correction**

The true topology of the cortical ribbon is that of a sheet (Euler number=1).

We would like the reconstructed gray/white boundary to have spherical topology (Euler number=2), but errors in the segmentation and non-cortical anatomical features of the white matter cause departures from spherical topology ("defects").

# **Typical "Defects"**

Fill Pallidum and Putamen

Cortical Defects

Fill Ventricles and Caudate "spackle" hippocampus

Cut Fornix

# **Topological Defects**



## Standard method\*: shrink wrapping



start with a surface S (e.g. sphere) of known topology find a mapping M:S→C of it to the cortex C that doesn't change its topology (e.g. Davatzikos, 1996; Macdonald 2000)

\*newer volumetric work (Shattuck and Leahy, 2001; Han et al., 2002)

# How to maintain geometric accuracy?

#### **Problems:**

- 1. The initial surface *S* is typically *much* smoother than the target surface *C*. The energy functionals for finding *M* are therefore highly non-convex.
- 2. Local errors that would have given rise to inaccurate segmentation if the topology were not constrained, can cause large scale geometric inaccuracies in the surfaces.

# What Surface Would a Shrink-Wrapping Algorithm Result in?



## **Solution: Manifold Surgery.**



Generate *C*' and find a mapping M<sup>-1</sup> from C' to *S* that is invertible over as much of *C* as possible. Noninvertible regions contain defects!

# Manifold Surgery: Equations

Energy Functional:

$$E = \sum_{i=1}^{F} \left( \frac{\log(1 + e^{-kR_i})}{k} \right)$$



- $R_i$  jacobian at the *i*<sup>th</sup> face in tessellation F number of faces in tessellation
- k positive real constant











# Manifold Surgery: Retessellation

- 1. Mark all triangles that have any edge overlapping any other edge in the tessellation.
- 2. Discard all faces and edges in marked triangles.
- 3. Sort all possible edges by image likelihood (they should go through MR values between gray and white).
- 4. Use a greedy retessellation algorithm: keep adding edges between all vertices in defects until no more can be added without causing an intersection with an existing edge *on the sphere*.
- (Florent Ségonne currently working on using genetic algorithm to evaluate different potential retessellations, but the space is huge!)

## **Manifold Surgery: Results**







# **Surface Inflation**



## White matter and pial surfaces



#### **Gray-white boundary**



#### **Pial surface**



# Surface Flattening – Whole Hemisphere



### Inflated surface with cuts



### Metrically optimal flat map





Borrowed from (Halgren et al., 1999)

## **Talairach Coordinates**

Can mean many things, but most common is linear transform to align input image with a target image that is average of many individuals aligned with the atlas of Talairach and Tournoux (1988).

#### Not Good For Cortex!

- 1. Typical transform is too low dimensional to account for variability in cortical folds.
- 2. Landmarks are subcortical (and far from much of cortex).
- 3. Implicit assumption that 3D metric is appropriate one.

# **Talairach averaging**



Average of 40

Single subject

# How to align different cortical surfaces?



## Surface-Based Coordinate System

Establish a 2-D coordinate system on cortical surface

 Every point in cortex should have a (unique) coordinate
 Every coordinate should refer to a point in cortex

- Inter-subject alignment of cortical folding patterns
- Improve alignment of *functional* areas

## **A Surface-Based Coordinate System**



## **Maximally Isometric Spherical Mapping**



#### **Inflated Surface**



**Transformed Surface** 

## **Spherical Morphing: Equations**

Energy Functional:  $J_c + \lambda_d J_d + \lambda_T J_T$ 

**J**<sub>c:</sub> Correlation error (aligns folding patterns)

 $J_d$ : Metric distortion (constrains allowable shape differences)

 $J_{T:}$  Topology term (forces mapping to be invertible)

## **Spherical Morphing: Equations**

Average Folding Pattern:

$$\overline{C}(\varphi,\theta) = \frac{1}{N} \sum_{i=1}^{N} C_i(\varphi,\theta)$$

Variance of Folding

$$\sigma^{2}(\varphi,\theta) = \frac{1}{N-1} \sum_{i=1}^{N} (C_{i}(\varphi,\theta) - \overline{C}(\varphi,\theta))^{2}$$

Maximum Likelihood Term:

$$J_{c} = \frac{1}{2V} \sum_{\nu=1}^{V} \left( \frac{G_{\alpha} * (C_{\nu} - \overline{C}(\phi(\nu), \theta(\nu)))}{\sigma(\phi(\nu), \theta(\nu))} \right)^{2}$$

Complete Energy Functional:

 $J = J_c + \lambda_T J_T + \lambda_d J_d$
#### **Inter-Subject Morphing**



#### **Individual Subject**





#### **Surface-Based Averaging**



Average surface created from 30 subjects

# **Applications**

- Increased statistical power for inter-subject averaging
- Automatic functional/anatomical labeling
- Inter-subject averaging of morphometric properties
- Statistical analysis of morphometric properties
  - aging
  - neurodegenerative diseases
  - longitudinal studies of structural changes
  - hemispheric asymmetry

# **Applications**

- Increased statistical power for inter-subject averaging
- Automatic functional/anatomical labeling
- Inter-subject averaging of morphometric properties
- Statistical analysis of morphometric properties
  - aging
  - neurodegenerative diseases
  - longitudinal studies of structural changes
  - hemispheric asymmetry

#### Inter-Subject Averaging of Activations







#### Talairach Average

**Spherical Average** 

# **Applications**

- Increased statistical power for inter-subject averaging
- Automatic functional/anatomical labeling
- Inter-subject averaging of morphometric properties
- Statistical analysis of morphometric properties
  - aging
  - neurodegenerative diseases
  - longitudinal studies of structural changes
  - hemispheric asymmetry

# **Applications**

- Increased statistical power for inter-subject averaging
- Automatic functional/anatomical labeling
- Inter-subject averaging of morphometric properties
- Statistical analysis of morphometric properties
  - aging
  - neurodegenerative diseases
  - longitudinal studies of structural changes
  - hemispheric asymmetry

#### **Cortical Parcellation: Manual vs. Automated**



#### Manual Parcellation Automatic Parcellation

Thanks to Christophe Destrieux for this slide.

# **Applications**

- Increased statistical power for inter-subject averaging
- Automatic functional/anatomical labeling
- Inter-subject averaging of morphometric properties
- Statistical analysis of morphometric properties
  - aging
  - neurodegenerative diseases
  - longitudinal studies of structural changes
  - hemispheric asymmetry

# **Applications**

- Increased statistical power for inter-subject averaging
- Automatic functional/anatomical labeling
- Inter-subject averaging of morphometric properties
- Statistical analysis of morphometric properties
  - aging
  - neurodegenerative diseases
  - longitudinal studies of structural changes
  - hemispheric asymmetry



Courtesy of Drs. Randy Buckner and David Salat

## **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of distortion in MRI.
- 4. Linking micro structure to macro structure.

## **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of distortion in MRI.
- 4. Linking micro structure to macro structure.

## **Whole-Brain Segmentation**

Goal: Segment T1-weighted MRI into anatomically and semantically meaningful structures (e.g. caudate, putamen, etc...).

#### **Requirements:**

- Insensitive to pathology.
- Insensitive to varying pulse sequences.

Prerequisite: registration with anatomically meaningful space (e.g. Talairach)

## Why Segmentation is Hard!



#### **Inter-subject Registration**

Goal: align functionally homologous points across subjects (e.g. hippocampus with hippocampus, amygdala with amygdala, etc...).

**Problem: this information is in general unavailable** 

Typical solution: align image intensities and hope this results in alignment of function/structure as well.

### What does Mean-Squared Error Estimation mean from a Probabilistic Perspective?

Find *f* that minimizes  $\iiint (I(f(\mathbf{r})) - T(\mathbf{r}))^2 d\mathbf{r}$ (*T* is target image, *I* is input image, *r* is spatial coordinate)

Assume 
$$\log(p(I | f, T)) = \iiint - (I(f(\mathbf{r})) - T(\mathbf{r}))^2 d\mathbf{r}$$

**Then:**  $p(I | f, T) = \prod e^{-(I(f(\mathbf{r})) - T(\mathbf{r}))^2}$ 

 $\rightarrow f$  is the maximum likelihood solution assuming the image noise can be modeled as a set of IID random variables with means T(r) and equal (unit) variances.

#### Mean-squared Error Registration: Low Quality Data

I(r)







#### **Mean-squared Error Registration**

Anatomy is variable, particularly in cases of pathology\*

 $\rightarrow$  A given spatial location may contain a different tissue class in different types of subjects!



\* Thanks to Marilyn Albert and Ron Killiany for providing this data.

# Segmentation-based Registration

Find the transformation that maximizes the probability that each point in the individual is drawn from *one* of the tissue classes in the template.

Find the *L* that maximizes the probability of observing image *I* given the segmentation *C*:

$$L = \arg \max p(I | L, C)$$

How do we find the segmentation C?

# Segmentation-based Registration

Problem of finding *L* is highly overdetermined (many, many more data points than parameters to solve for).

Can assume *C* in certain atlas locations (a few thousand) where prior probabilities are high, and use them to find *L* using a *global* search (local minima/maxima not a problem).

#### **Atlas Points After Registration**





- Cerebellar cortex
  Cerebellar WM
  4th ventricle
  RH cerebral WM
- LH cerebral WM
  Hippocampus
  - LH pallidum
  - Thalamus

- Cerebral cortexMisc.
- Lateral ventricle
- Caudate

#### Segmentation-based Registration: Results



Normal



### Segmentation Results: CMA Labeling





Cerebellar cortex
 Cerebellar WM
 4th ventricle
 RH cerebral WM



- Cerebral cortex
  Misc.
  - Lateral ventricle
- Caudate



## **Tissue Segmentation**

Given a transform *f* into an atlas space, *C* can be estimated using a Maximum a Posteriori (MAP) approach: what is the most likely tissue classification *C* given the observed image *I*, the transformation *f*, and prior information about *C*?

$$C = \arg \max_{C'} p(C' | I, f)$$
$$p(C' | I, f) \sim p(I | C', f) p(C')$$

What prior information p(C) can we use to constrain the allowable segmentations?

## **Tissue Segmentation**

The probability distribution of each voxel is modeled as an independent *nonstationary* Gaussian (because it is a function of r):

$$p(I \mid f, C) = \prod_{\mathbf{r} \in R} p(I(\mathbf{r}) \mid f, C(\mathbf{r}), \mathbf{r})$$

Forward Model of Image Formation:

$$p(I(\mathbf{r}) \mid f, C(\mathbf{r}) = c, \mathbf{r}) = \frac{1}{\sigma_c(f(\mathbf{r}))\sqrt{2\pi}} \exp(-\frac{(I(\mathbf{r}) - \mu_c(f(\mathbf{r})))^2}{\sigma_c(f(\mathbf{r}))^2})$$

Note: can make  $\mu_c(f(\mathbf{r}))$  a function of MR parameters and embed physics of imaging into forward model (more later)

#### **Gibbs Priors: Motivation**

What is the probability that cortical gray matter occurs inferior to hippocampus?



## **Markov Random Fields**

- Modeling the segmentation as a *Markov Random Field (MRF)* means:
- p(C(r)|the rest of the labels) = p(C(r)|labels in a neighborhood around r)

## **Segmentation: MRF**

Problem: the segmentation is fractured because no spatial smoothness constraints are encoded in model.

Solution: incorporate prior probability of one tissue class being the neighbor of another into model:

 $p(C) \propto \prod_{\mathbf{r} \in R} p(C(\mathbf{r}) | \mathbf{r}) \prod_{\mathbf{r}_i \in N(\mathbf{r})} p(C(\mathbf{r}_i) | C(\mathbf{r}), i, \mathbf{r}, \mathbf{r}_i)$ 

## **Segmentation: MRF**

 $p(C(r_i)|C(r), I, r, r_i)$  encodes the probability that tissue class  $C(r_i)$  occurs at spatial location  $r_i$  when tissue class C(r) occurred at r. The segmentation is thus modeled as an *anisotropic* nonstationary *MRF*.



#### **Segmentation: MRF**



**Preliminary Segmentation** 



**Final Segmentation** 



### Segmentation with MRF: Fly Through



Cerebellar cortex
 Cerebellar WM
 4th ventricle
 RH cerebral WM



Cerebral cortex
 Misc.
 Lateral ventricle
 Caudate



### **Volume Differences Predictive of AD**



Data courtesy of Drs Marilyn Albert Ron Killiany

# Optimizing CNR for Segmentation

**Problem:** CNR varies over brain because of intrinsic tissue property inhomogeneities, bias fields, etc....

Global CNR dramatically underestimates true CNR. Need a local measure that reflects the true difficulty of the segmentation problem.

Solution: Use atlas to compute local segmentation ambiguity and integrate across brain.

#### **Estimation of Intrinsic Tissue Parameters**



#### Inverse Bloch Eq.





#### **Estimated T<sub>1</sub> values**

 $S(TR, TE, \alpha, T_1, T_2^*, P) = \frac{P \sin(k(\mathbf{r})\alpha)}{k(\mathbf{r})} (\frac{1 - e^{-TR/T_1}}{1 - \cos(k(\mathbf{r})\alpha)} e^{-TR/T_1}) e^{-TE/T_2^*}$ 

# Pulse Sequence Independent Segmentation



Test-retest structure volumes measured from three separate datasets (dark, medium and light bars) acquired on the same subject. Each dataset had different acquisition parameters (LV=lateral ventricle, HP=hippocampus, TH=thalamus, CA=caudate, PU=putamen, PA=pallidum, AM=amygdala).
**Sequence Optimization**  $M = \arg\min A(M) = \iiint \sum_{c_1 \neq c_2 \neq c_2} \sum_{c_2 \neq c_2 \neq c_2} \frac{1}{2} (p(c_1 \mid c_2, M) + p(c_2 \mid c_1, M))$  $p(c_1 | c_2, M) = \iint p(c_1) p(I | c_1, M) p(I | c_2, M) d\mathbf{I}$  $p(I | c_1, M) \sim N(\hat{\mu}_{c_1}(M), \hat{\Sigma}_{c_1}(M))$  $\hat{\mu}_{c}(M) = S(M_{\text{predicted}}, \beta(M_{\text{training}}, \mu_{c}))$  $\hat{\Sigma}_{c}(M) = J_{\text{predicted}} (J_{\text{training}}^{+} \Sigma_{c} J_{\text{training}}^{+T}) J_{\text{predicted}}^{T} + \lambda I d$ 

Where  $J_i$  is the Jacobian of  $S(M_i, \beta)$ , and  $A^+$  and  $A^T$  are the pseudoinverse and transpose of A respectively.

# Predicting Means and Covariances



 $\hat{\mu}_{c}(M) = S(M_{\text{predicted}}, \beta(M_{\text{training}}, \mu_{c}))$  $\hat{\Sigma}_{c}(M) = J_{\text{predicted}}(J_{\text{training}}^{+} \Sigma_{c} J_{\text{training}}^{+T}) J_{\text{predicted}}^{T} + \lambda Id$ 

Where M<sub>i</sub> are the MR pulse parameters used in acquisition i.

#### Ambiguity for 2 flip angles (2 flash scans, TR=20ms, TE=3ms, 18 subjects)



## Multi-Echo Flash (Andre van der Kouwe and Anders Dale)



#### TR=20 msec, 2ms esp, flip angle=5°, BW=651 Hz/voxel



TR=20 msec, flip angle=30°, BW=651 Hz/voxel

## T2\* decay at 5<sup>o</sup> (left) and 30<sup>o</sup> (right)

50

300



FLASH Simulation, TR=20ms, TE=3ms GM T2\*≈75 ms (dotted), WM T2\*≈55 ms (solid)

# T2\* Decay with Echo Time (5° left, 30° right, 65ms echo train)



## **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of Variance in MRI.
- 4. Linking macro and microstructure.

## **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of Variance in MRI.
- 4. Linking macro and microstructure.

## **Sources of Variance in MRI**

- 1. Slice positioning
- 2. Subject motion
- 3. MRI distortions
  - Gradient Nonlinearities
  - Bias fields
  - Susceptibility effects
- 4. Hardware/Software changes.

# Longitudinal Analysis (baseline)



# Longitudinal Analysis (600 days)



### Auto Slice Registration: prescribing where slices should be placed without human intervention



is not a second s

Dale / Van der Kouwe / Schmitt MGH / Cortechs / Siemens

#### Real-Time Motion Correction with Cloverleaf Navigators





Average No motion correction

Average (equal weight) Real-time motion corr.

Average (MSE weighted) Real-time motion corr.

Thanks to Andre van der Kouwe for this slide.

#### Gradient Distortions: Between Scanner Variance Without Correction (Scanner A)



Brain Morphometry BIRN: MGH, BWH, Duke, UCSD, UCI, UCLA, JHU

#### Gradient Distortions: Between Scanner Variance Without Correction (Scanner B)



Brain Morphometry BIRN: MGH, BWH, Duke, UCSD, UCI, UCLA, JHU

#### **Spatial Distortion due to Magnetic Susceptibility (B<sub>0</sub>) Pulse-Sequence Dependence (S/I readout direction)**



#### **Spatial Distortion due to Magnetic Susceptibility (B<sub>0</sub>) Pulse-Sequence Dependence (I/S readout direction)**



## **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of distortion in MRI.
- 4. Linking micro structure to macro structure.

## **Talk Outline**

- 1. Cortical Analysis.
- 2. Subcortical Analysis.
- 3. Sources of distortion in MRI.
- 4. Linking micro structure to macro structure.

# Histology in Alzheimer's disease

#### CONTROL

AD



Nissl Stain

thioflavin S (neurofibrillary tangles and neuritic plaques)

Thanks to Brad Hyman and Jean Augustinack for this slide.

# **Temporal Lobe Fly-Through**



100 $\mu$ m isotropic MR, 7T, TR=20msec, TE=7.8msec,  $\alpha$ =23° (synthesized)

## **Entorhinal Islands with MRI!**



1mm

## **Areal border detection**



c.f. (Schleicher et al, 1999)

## Towards MR Histology and Stereology



MRI

**Block Face** 

Nissl Stain

Joint work with Jean Augustinack, Larry Wald, Matt Frosch, Megan Blackwell, Chris Wiggins, David Salat and Andre van der Kouwe



# **Using In-vivo Functional Data to Look for Histological Boundaries**

#### FFA probability map



#### Predicted FFA border



Joint work with Mona Spiridon, Nancy Kanwisher, Jean Augustinack, Becca Schwarzlose, Megan Blackwell and Brian T. Quinn.

## **Acknowledgements & Disclosures**

MGH Andre van der Kouwe **David Salat Stephan Heckers Diana Rosas** Larry Wald **Graham Wiggins Jorge Jovicich David Kennedy Chris Wiggins Nikos Makris** Megan Blackwell Jean Augustinack UC San Diego **Anders Dale Marty Sereno** Johns Hopkins University

**Marilyn Albert** 





Washington University **Randy Buckner Siemens Medical Systems Franz Schmitt Cortechs Labs, Inc Gen-Nan Chen** Mukund Balasubramanian **Georgetown University Tom Zeffiro Guinevere Eden** Peter E. Turkeltaub MIT **Florent Ségonne Polina Golland** Peng Yu **Nancy Kanwisher Mona Spiridon** 

> NATIONAL FOUNDATION FOR Functional Brain Imaging

