

LEARNING REPRESENTATIONS OF SEQUENCES

IPAM GRADUATE SUMMER SCHOOL ON DEEP LEARNING

GRAHAM TAYLOR

SCHOOL OF ENGINEERING
UNIVERSITY OF GUELPH

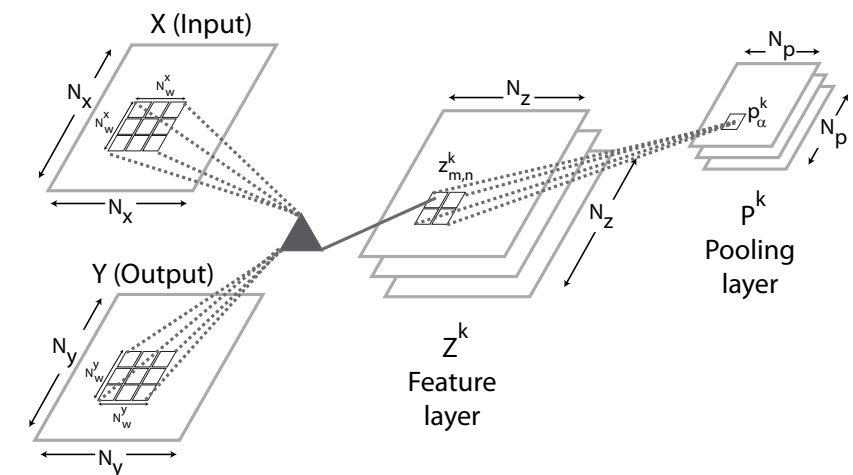
Papers and software available at: <http://www.uoguelph.ca/~gwtaylor>

OVERVIEW: THIS TALK

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Learning Representations of Sequences / G Taylor

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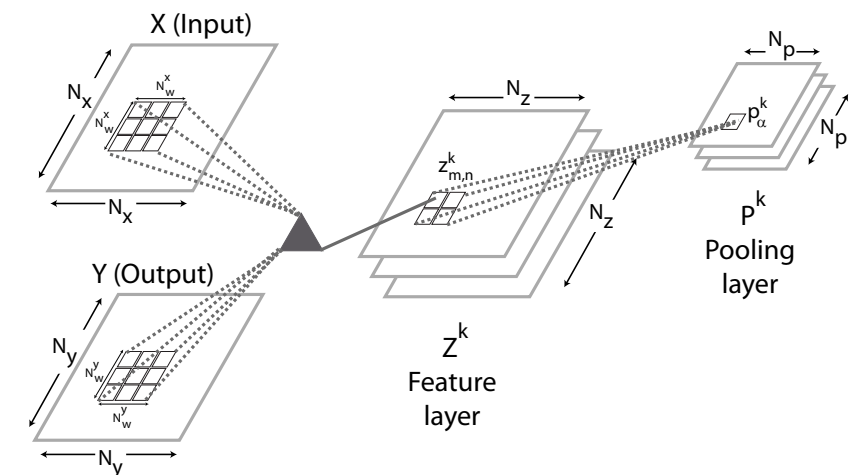
- Learning representations of **temporal data**:
 - existing methods and challenges faced
 - recent methods inspired by deep learning and representation learning



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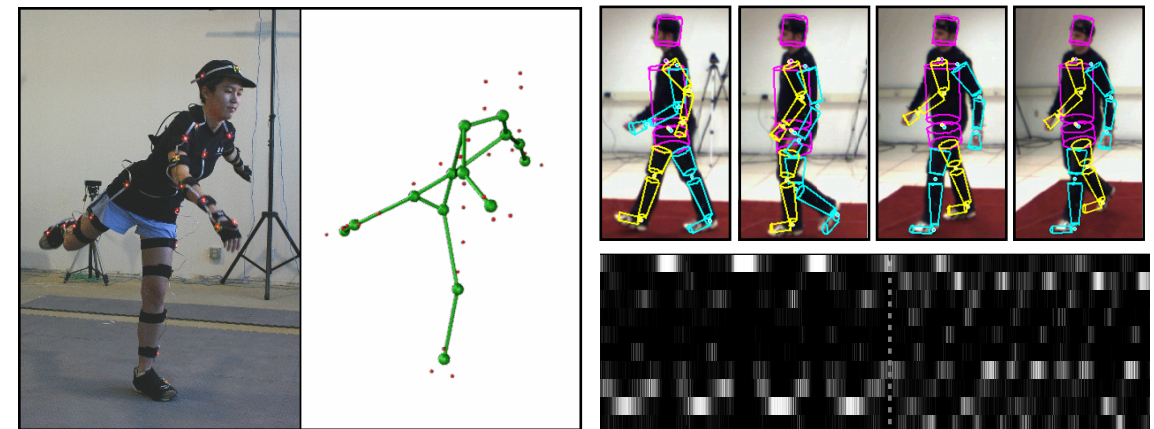
- Learning representations of **temporal data**:

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- Applications: in particular, modeling **human pose and activity**

- highly structured data: e.g. motion capture
- weakly structured data: e.g. video



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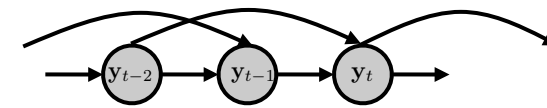
OUTLINE

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OUTLINE

Learning representations from sequences

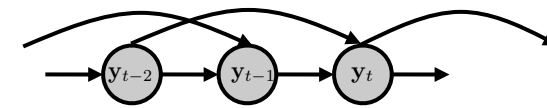
Existing methods, challenges



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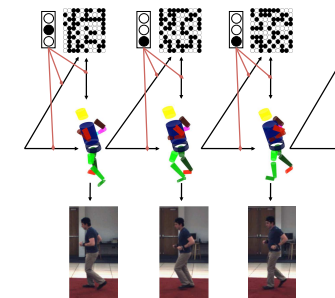
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Composable, distributed-state models for sequences

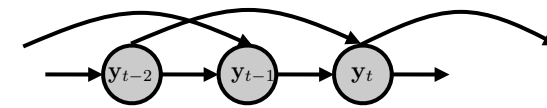
Conditional Restricted Boltzmann Machines and their variants



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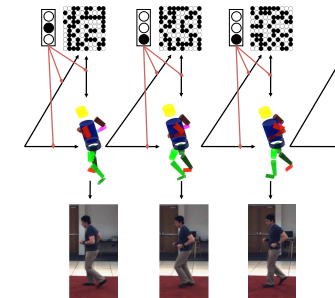
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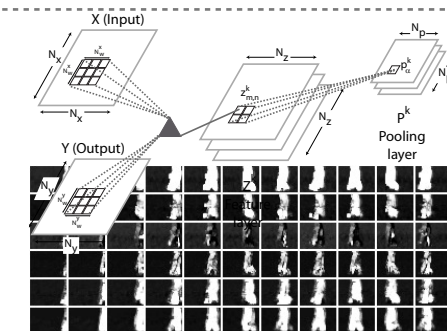
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Conditional Restricted Boltzmann Machines and their variants



Using learned representations to analyze video

A brief and (incomplete) survey of deep learning for activity recognition

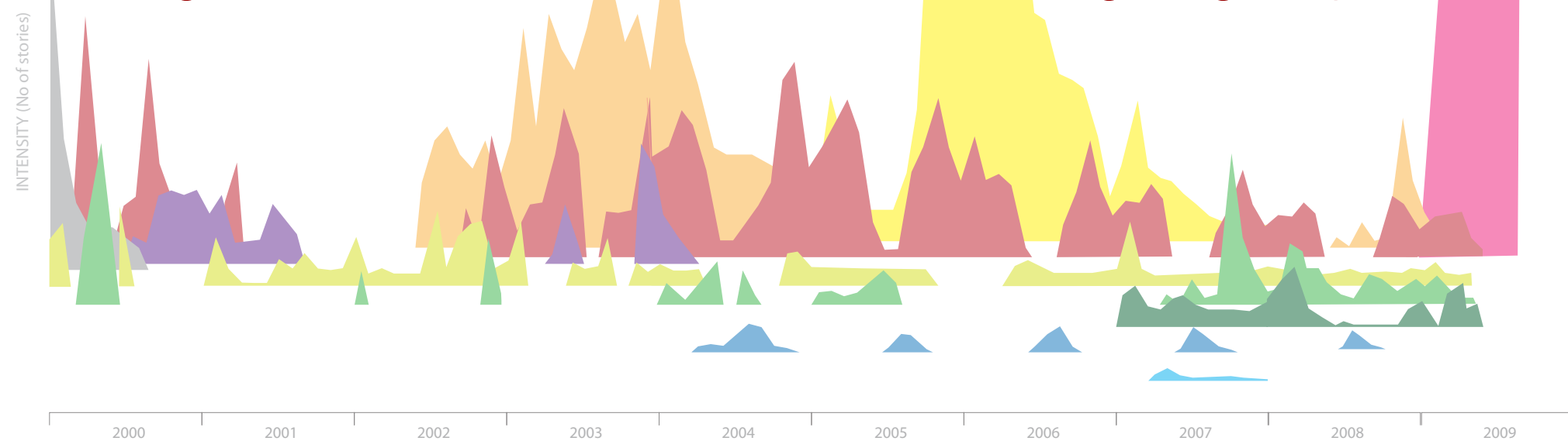


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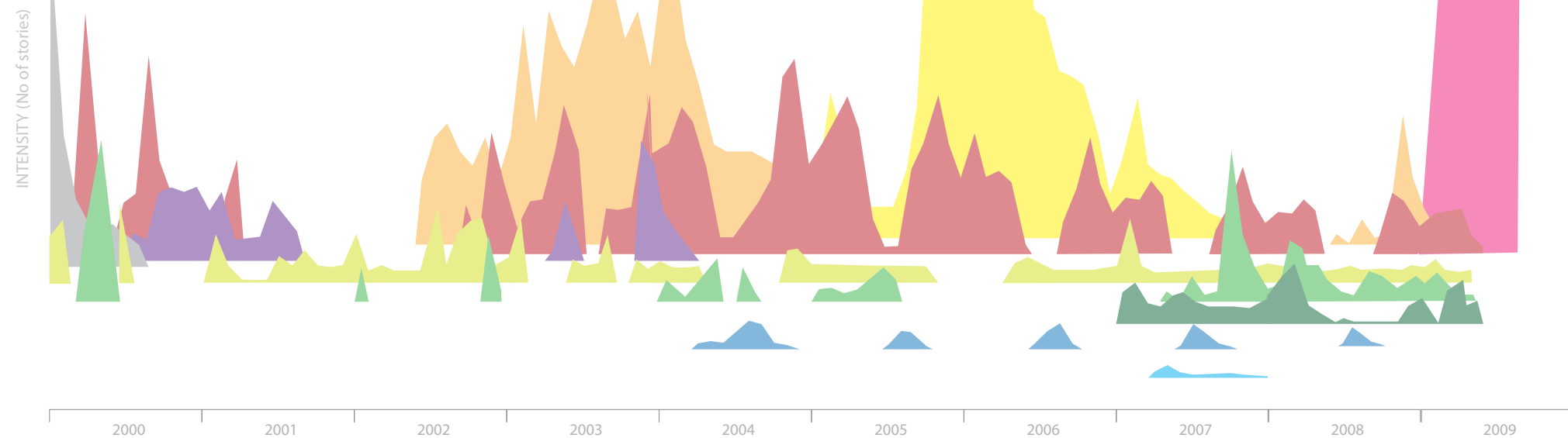
TIME SERIES DATA

- Time is an integral part of many human behaviours (motion, reasoning)
- In building statistical models, **time is sometimes ignored, often problematic**
- Models that **do** incorporate dynamics fail to account for the fact that data is often **high-dimensional, nonlinear, and contains long-range dependencies**



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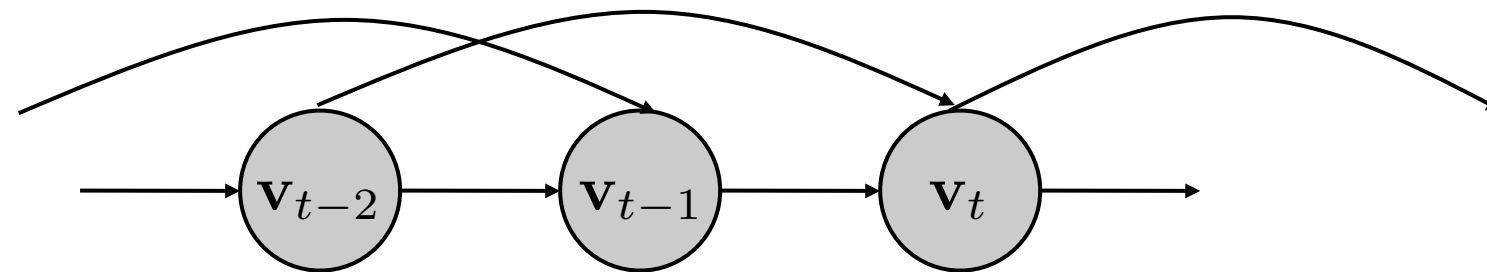
Today we will discuss a number of models that have been developed to address these challenges.

VECTOR AUTOREGRESSIVE MODELS

$$\mathbf{v}_t = \mathbf{b} + \sum_{m=1}^M A_m \mathbf{v}_{t-m} + \mathbf{e}_t$$

- Have dominated statistical time-series analysis for approx. 50 years
- Can be fit easily by least-squares regression
- Can fail even for simple nonlinearities present in the system
 - but many data sets can be modeled well by a linear system
- Well understood; many extensions exist

MARKOV (“N-GRAM”) MODELS



- Fully observable
- Sequential observations may have nonlinear dependence
- Derived by assuming sequences have **Markov property**:

$$p(\mathbf{v}_t | \{\mathbf{v}_1^{t-1}\}) = p(\mathbf{v}_t | \{\mathbf{v}_{t-N}^{t-1}\})$$

- This leads to joint: $p(\{\mathbf{v}_1^T\}) = p(\{\mathbf{v}_1^N\}) \prod_{t=N+1}^T p(\mathbf{v}_t | \{\mathbf{v}_{t-N}^{t-1}\})$
- Number of parameters **exponential** in N !

EXPONENTIAL INCREASE IN PARAMETERS

$$|\theta| = Q^{N+1}$$

Here, $Q = 3$

$p(a a)$	$p(b a)$	$p(c a)$
$p(a b)$	$p(b b)$	$p(c b)$
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1st order Markov ($N = 1$)

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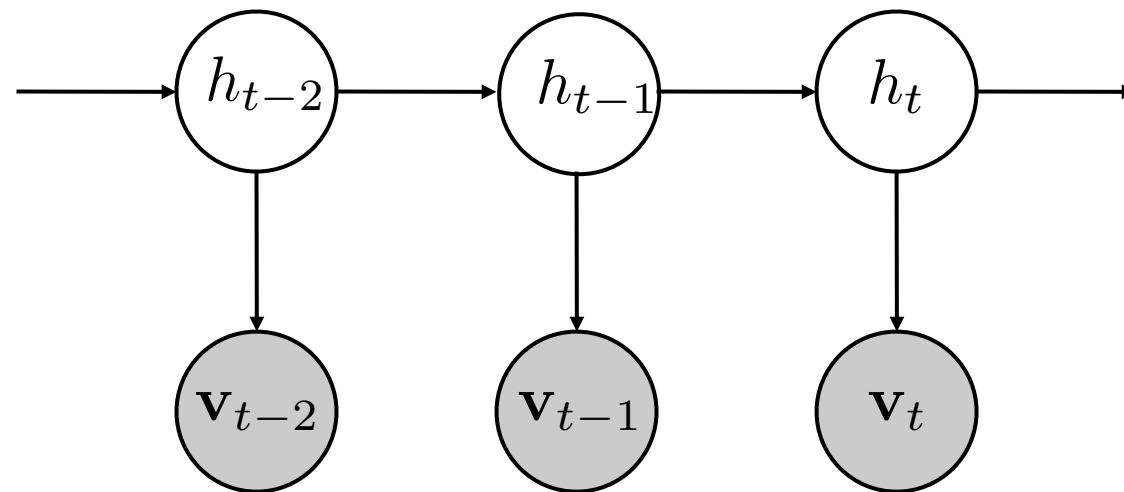
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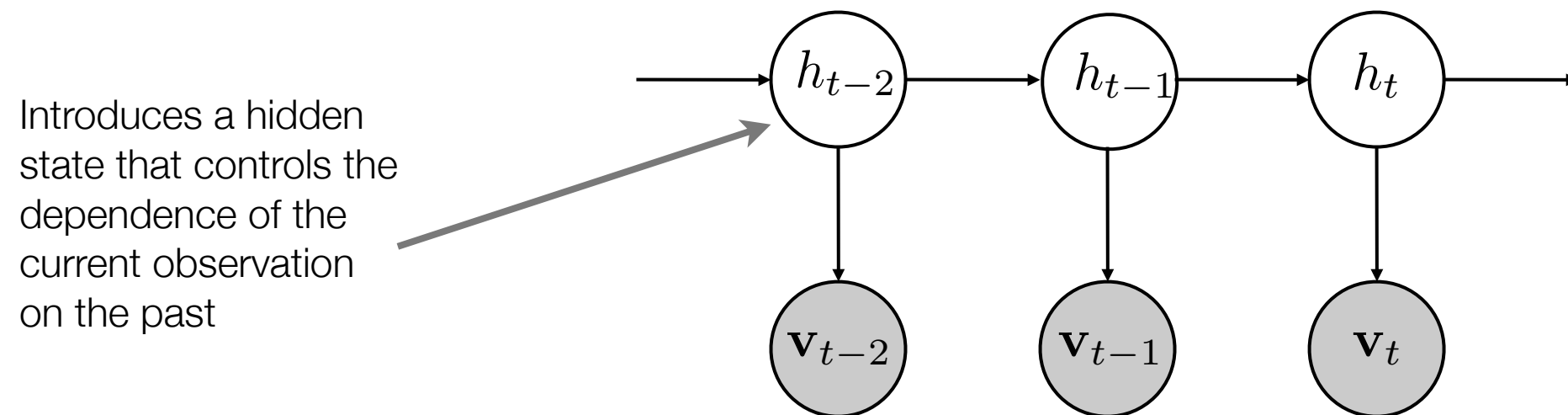
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2nd order Markov ($N = 2$)

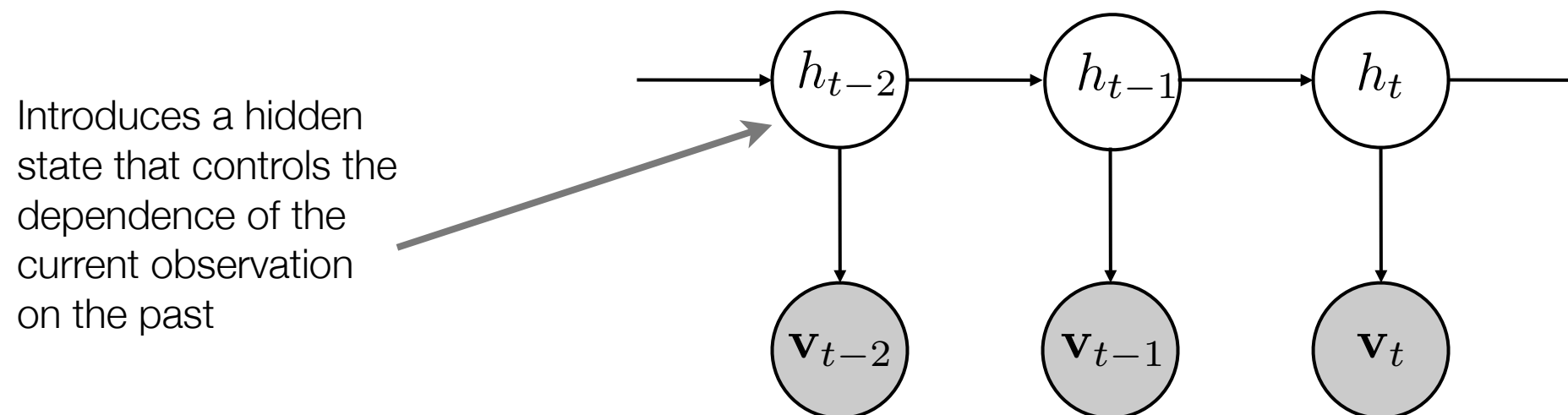
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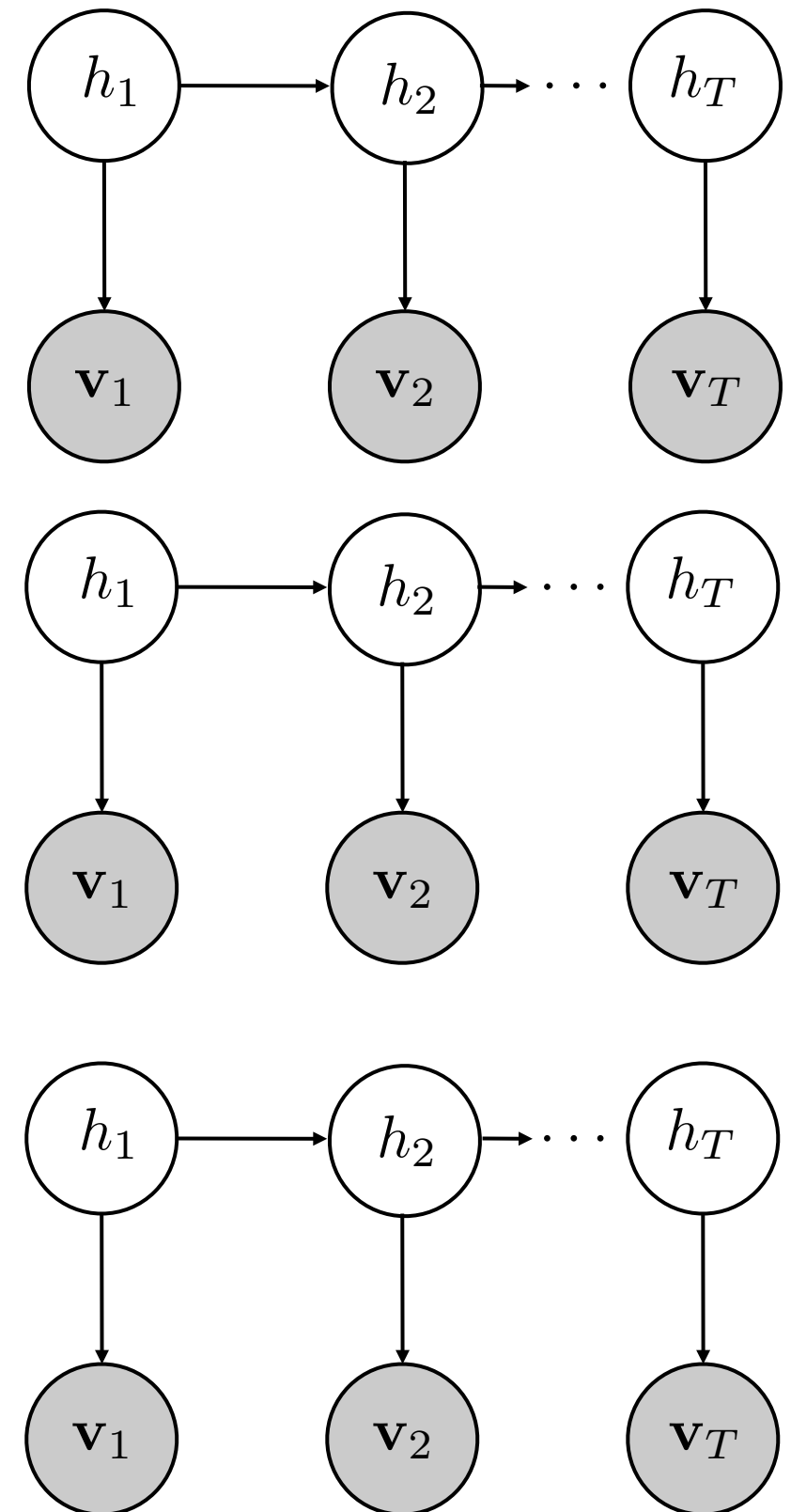


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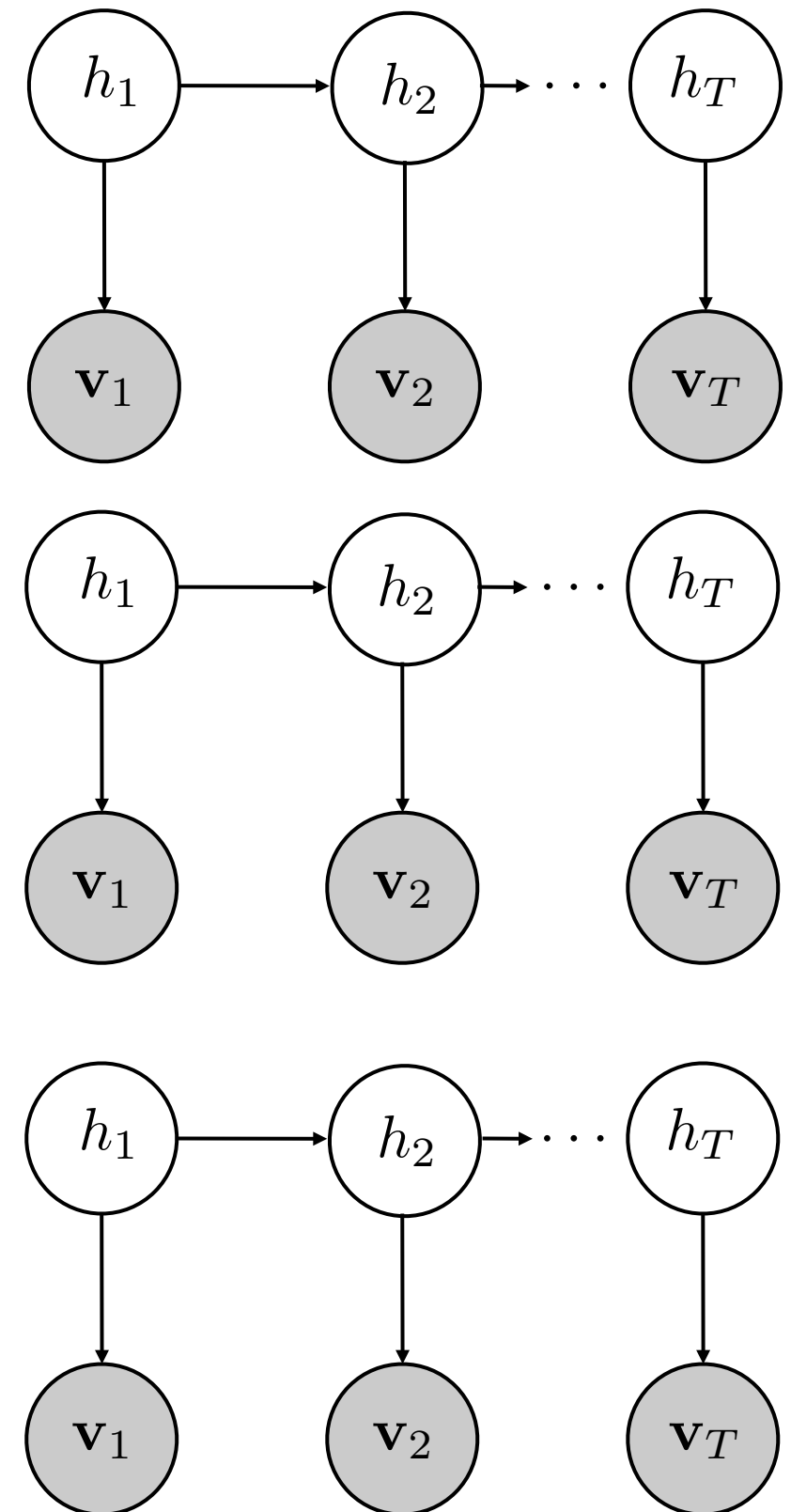
- Successful in speech & language modeling, biology
- Defined by **3 sets of parameters**:
 - Initial state parameters, π
 - Transition matrix, A
 - Emission distribution, $p(\mathbf{v}_t|h_t)$
- Factored joint distribution:
$$p(\{h_t\}, \{\mathbf{v}_t\}) = p(h_1)p(\mathbf{v}_1|h_1) \prod_{t=2}^T p(h_t|h_{t-1})p(\mathbf{v}_t|h_t)$$

INFERENCE AND LEARNING



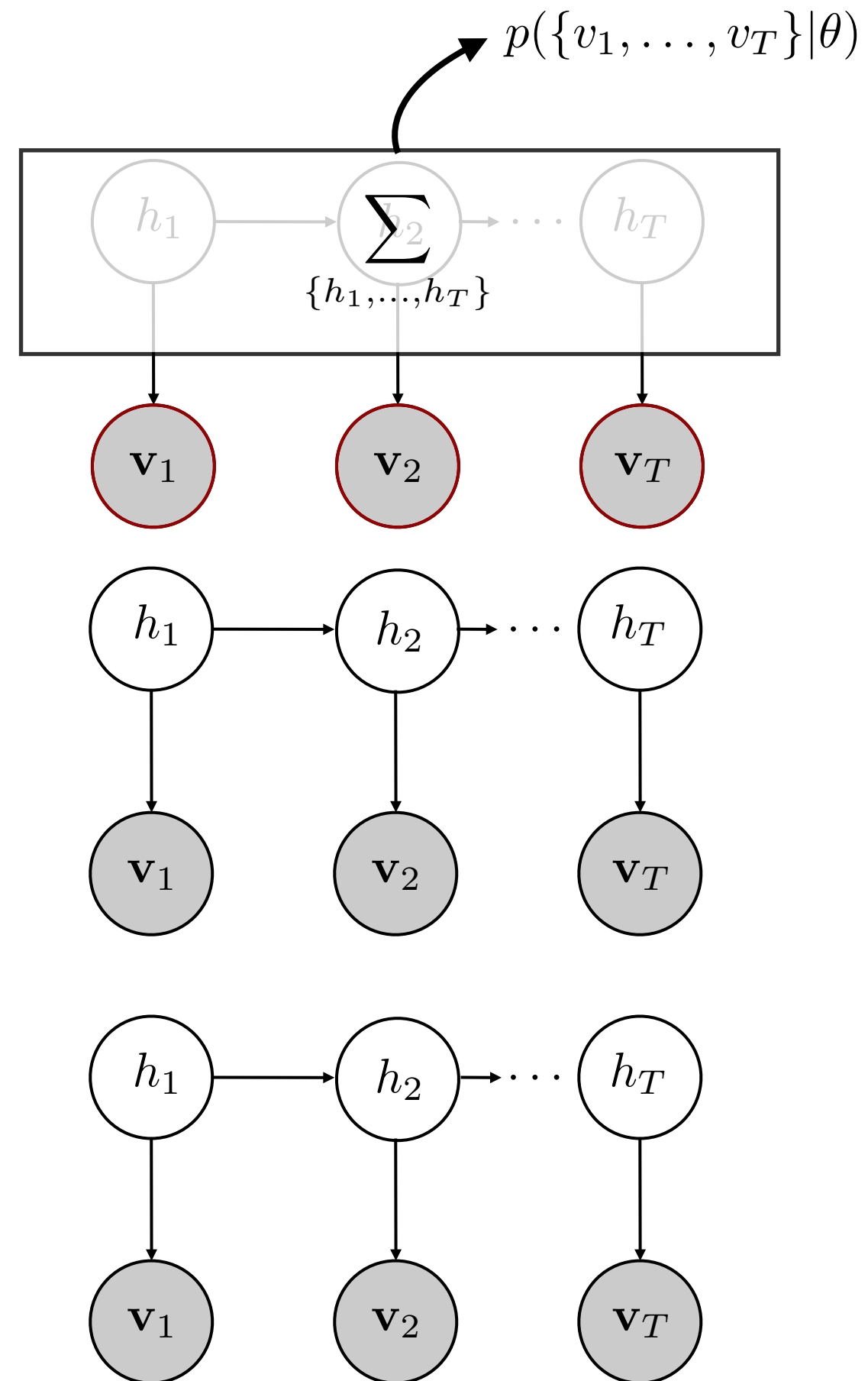
INFERENCE AND LEARNING

- Typically three tasks we want to perform in an HMM:



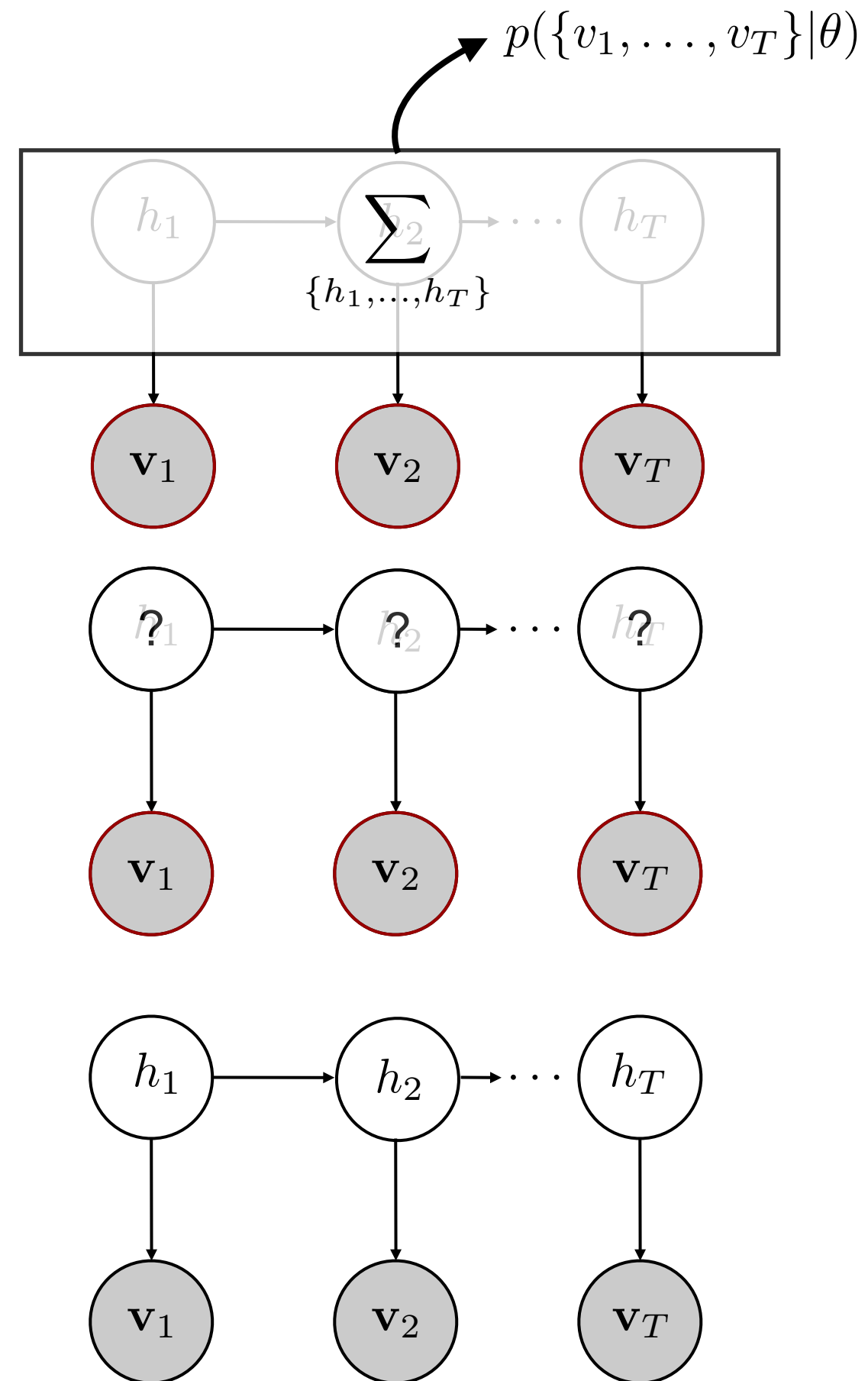
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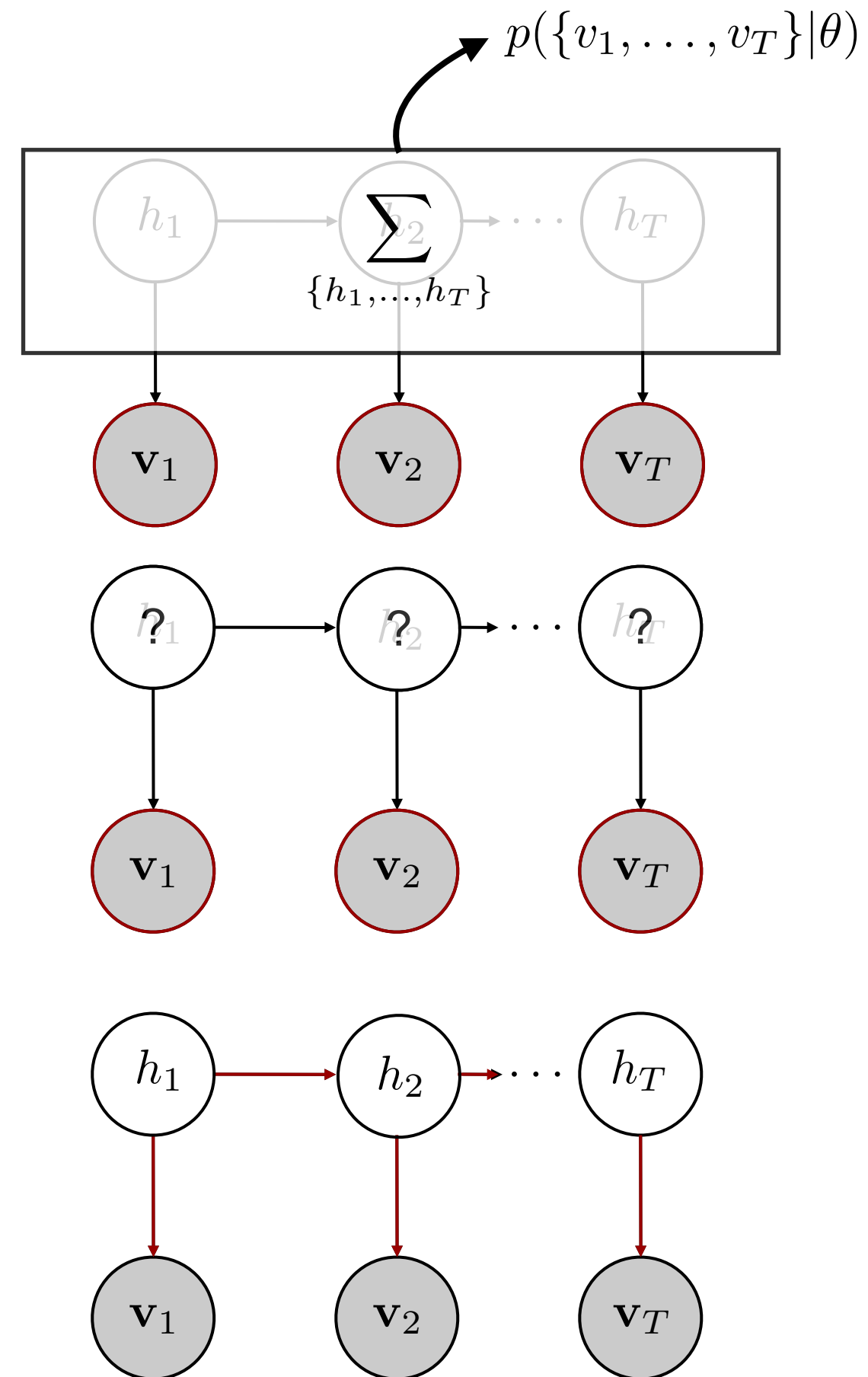
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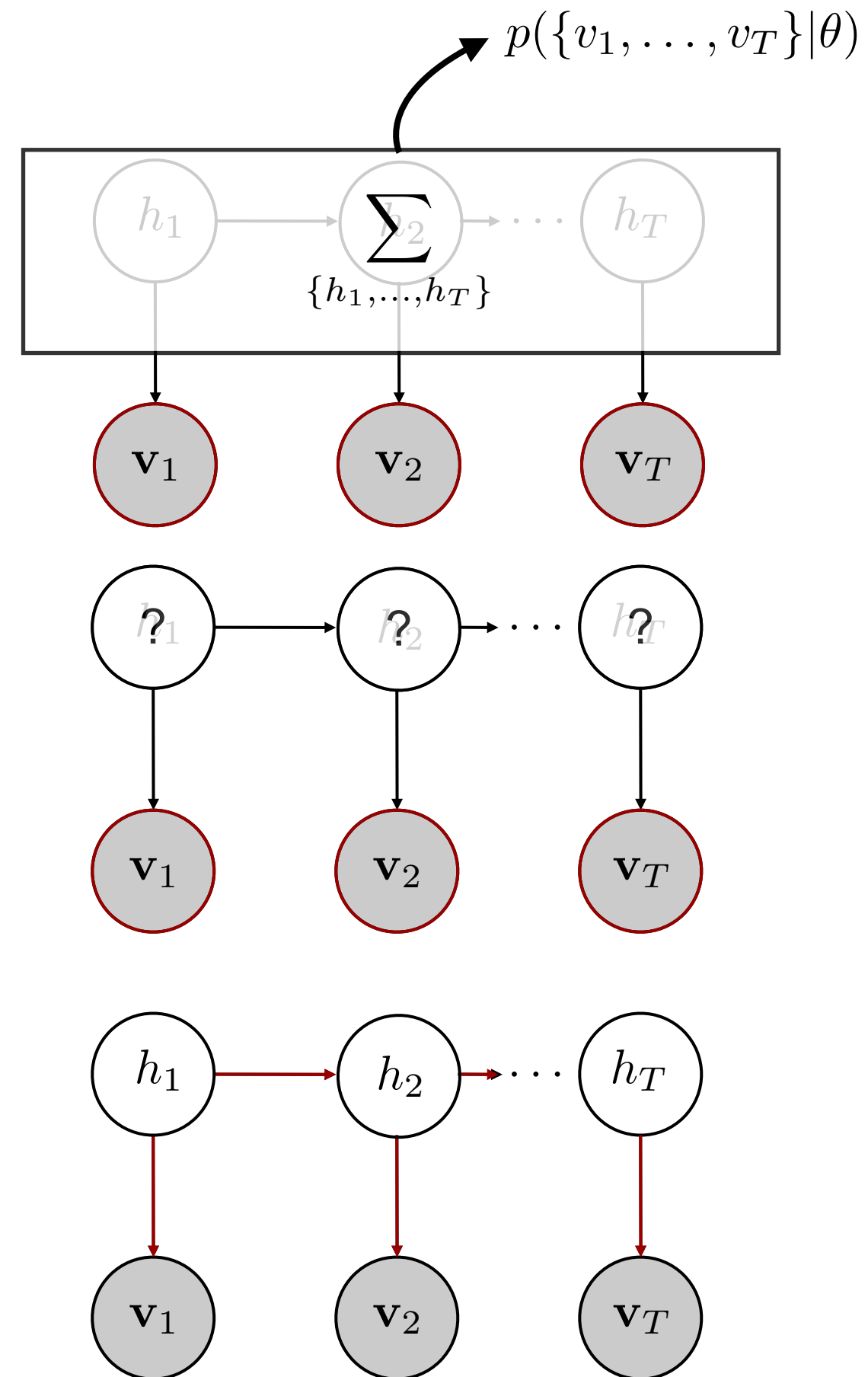
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- Typically three tasks we want to perform in an HMM:
 - Likelihood estimation
 - Inference
 - Learning
- All are exact and tractable due to the simple structure of the HMM



LIMITATIONS OF HMMS

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LIMITATIONS OF HMMS

- Many high-dimensional data sets contain rich componential structure

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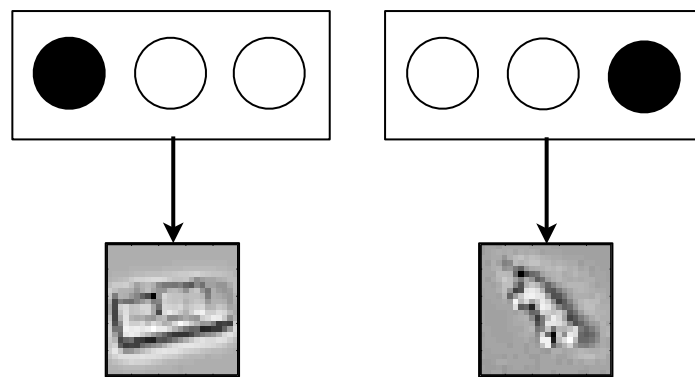
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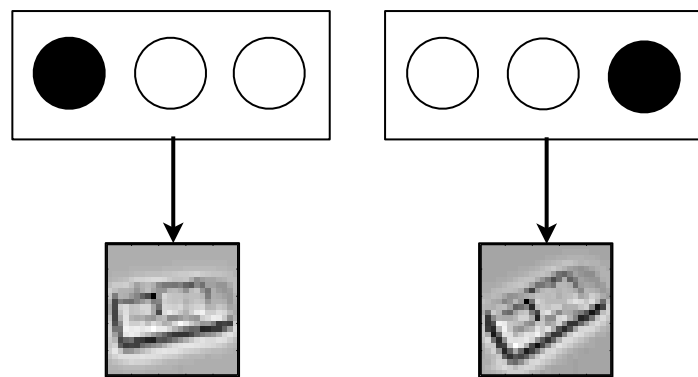
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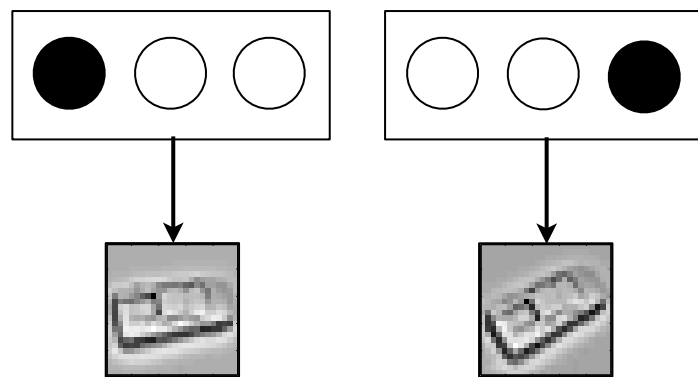
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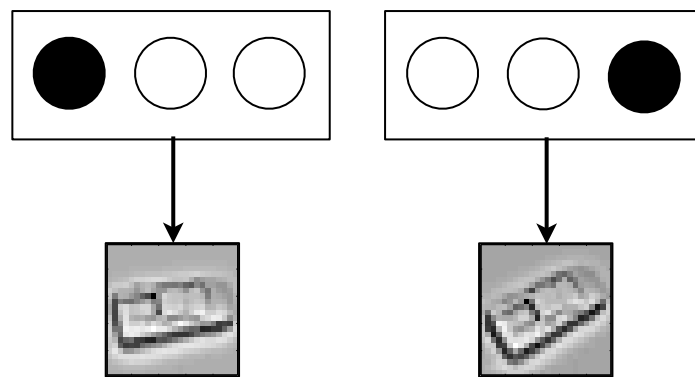
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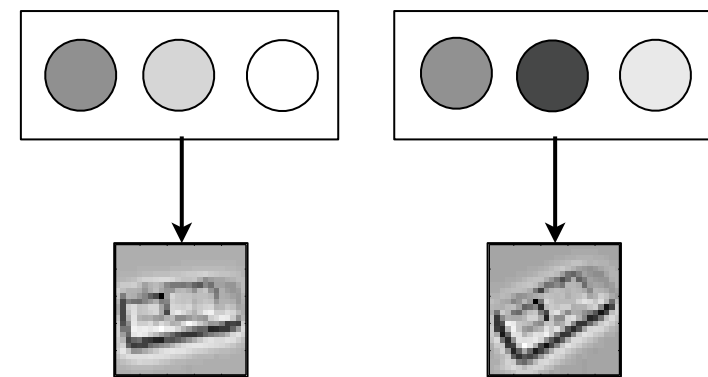
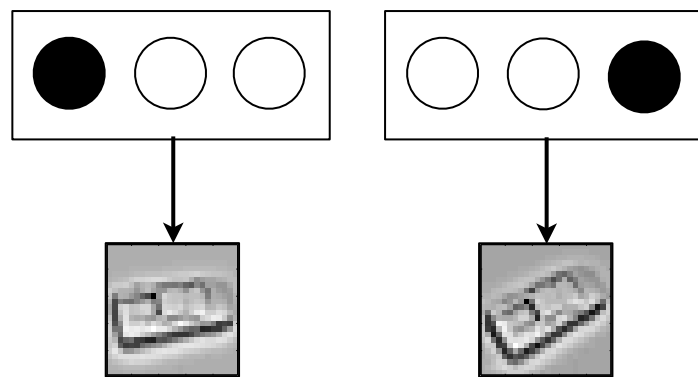
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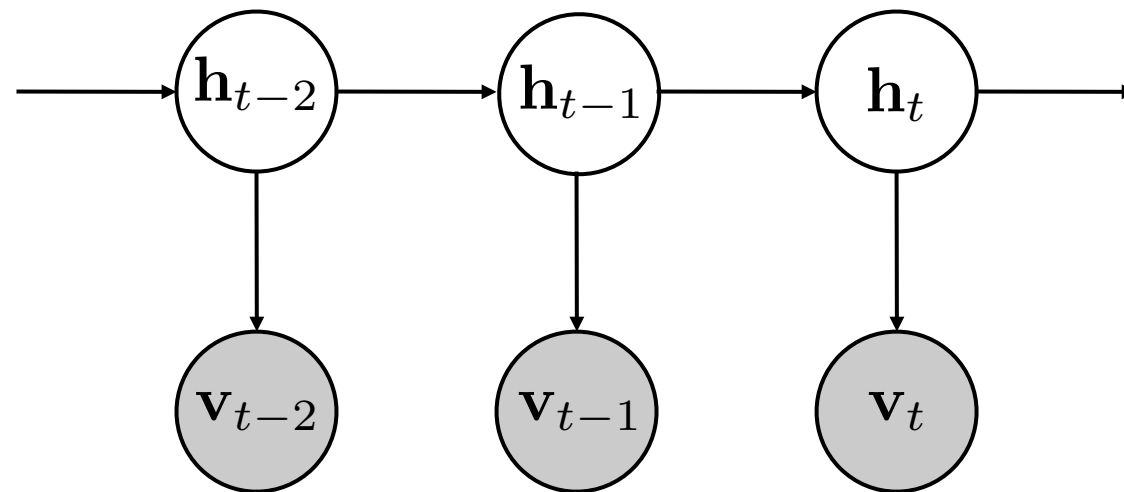


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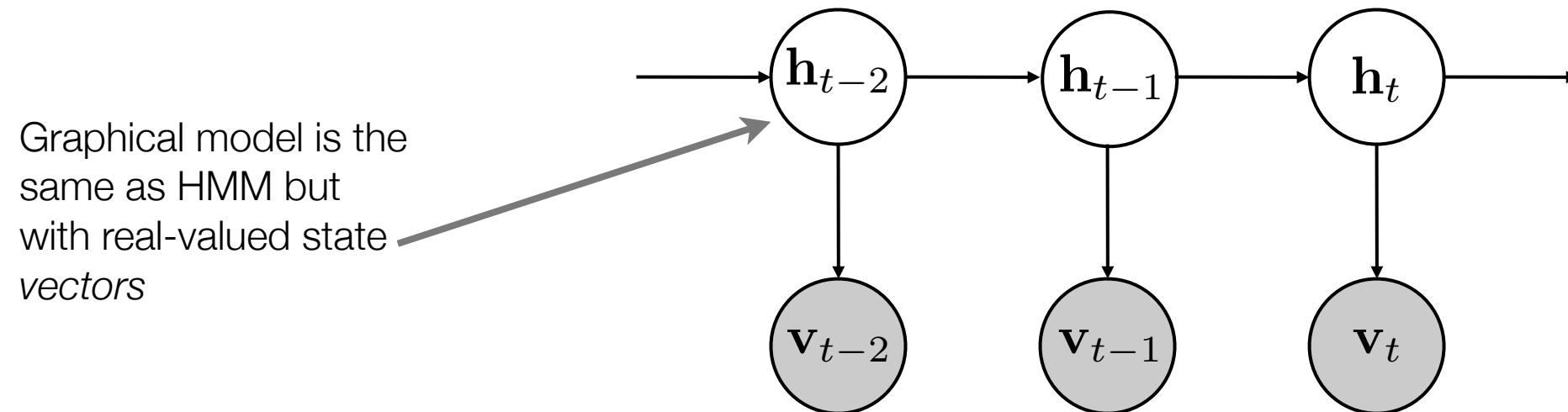
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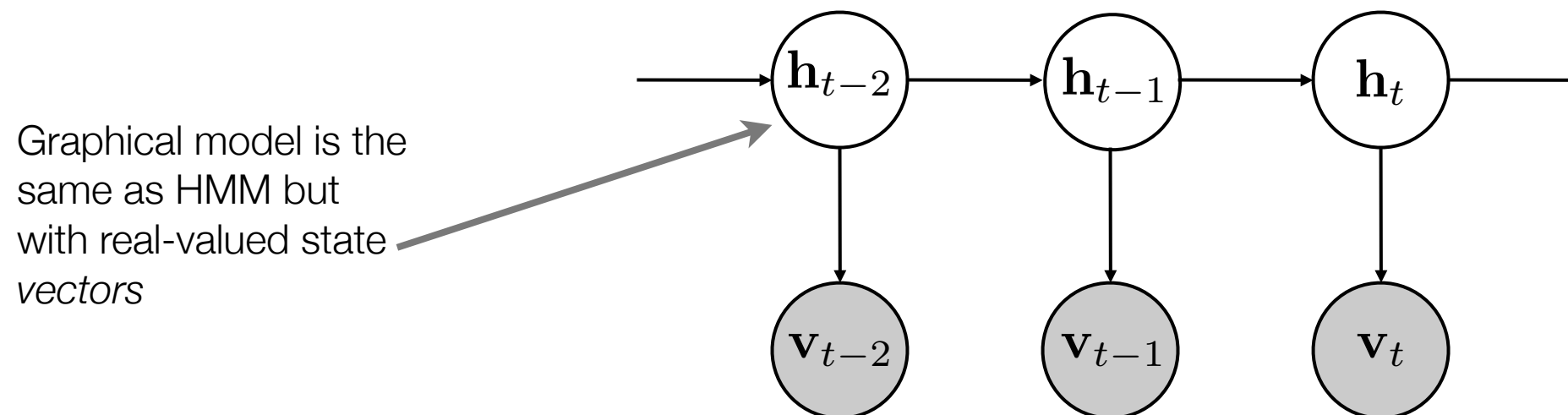
LINEAR DYNAMICAL SYSTEMS



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LINEAR DYNAMICAL SYSTEMS



- Characterized by linear-Gaussian dynamics and observations:

$$p(\mathbf{h}_t | \mathbf{h}_{t-1}) = \mathcal{N}(\mathbf{h}_t; A\mathbf{h}_{t-1}, Q) \quad p(\mathbf{v}_t | \mathbf{h}_t) = \mathcal{N}(\mathbf{v}_t; C\mathbf{h}_t, R)$$

- Inference is performed using Kalman smoothing (belief propagation)
- Learning can be done by EM
- Dynamics, observations may also depend on an observed input (control)

LATENT REPRESENTATIONS FOR REAL-WORLD DATA

Data for many real-world problems (e.g. vision, motion capture) is high-dimensional, containing complex non-linear relationships between components

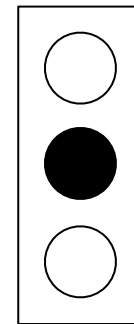
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Hidden Markov Models

Pro: complex, nonlinear emission model

Con: single K -state multinomial represents entire history



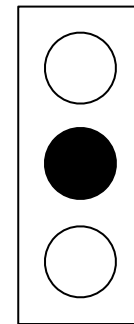
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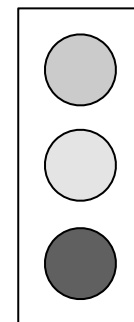
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Linear Dynamical Systems

Pro: state can convey much more information

Con: emission model constrained to be linear



LEARNING DISTRIBUTED REPRESENTATIONS

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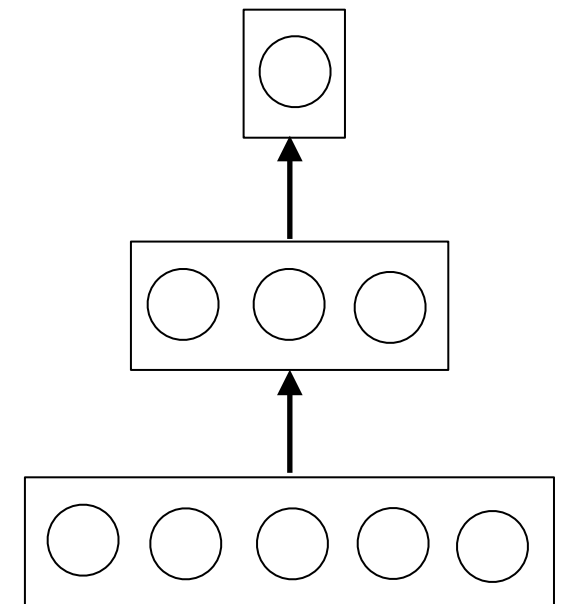
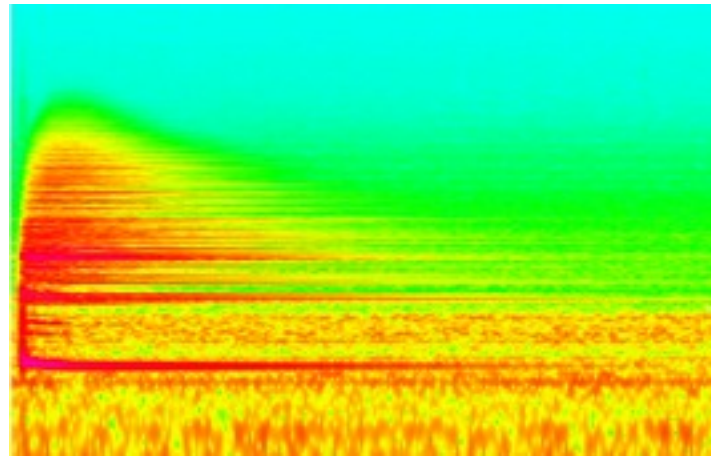
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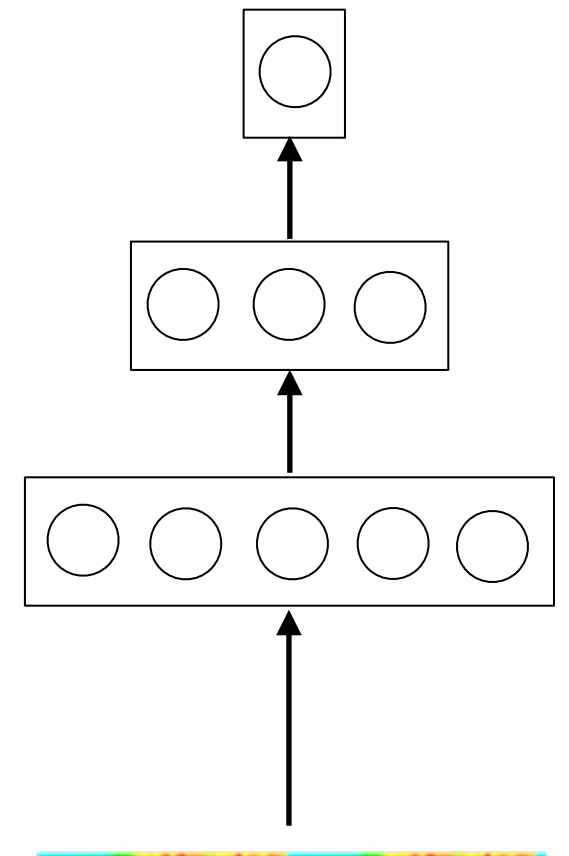
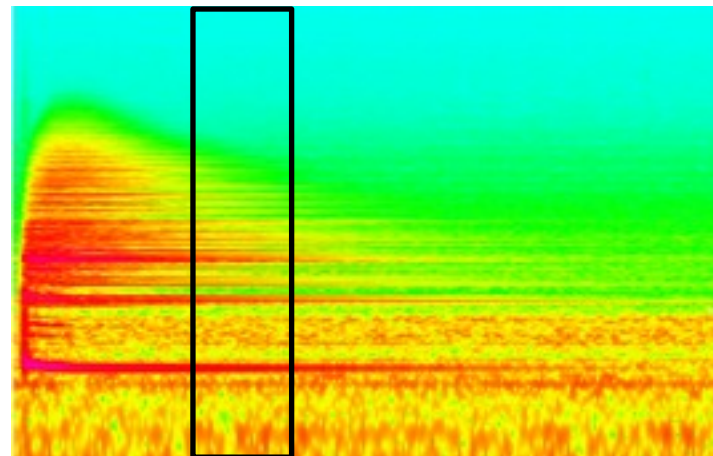
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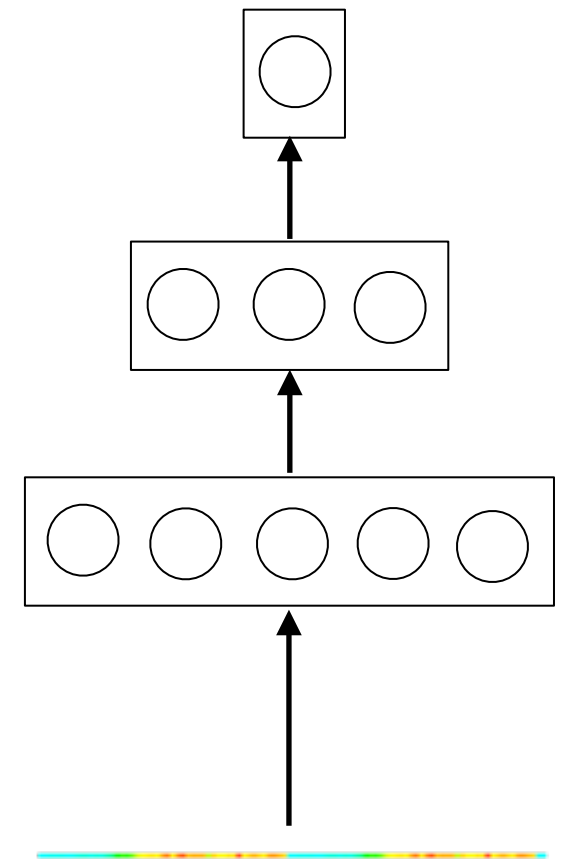
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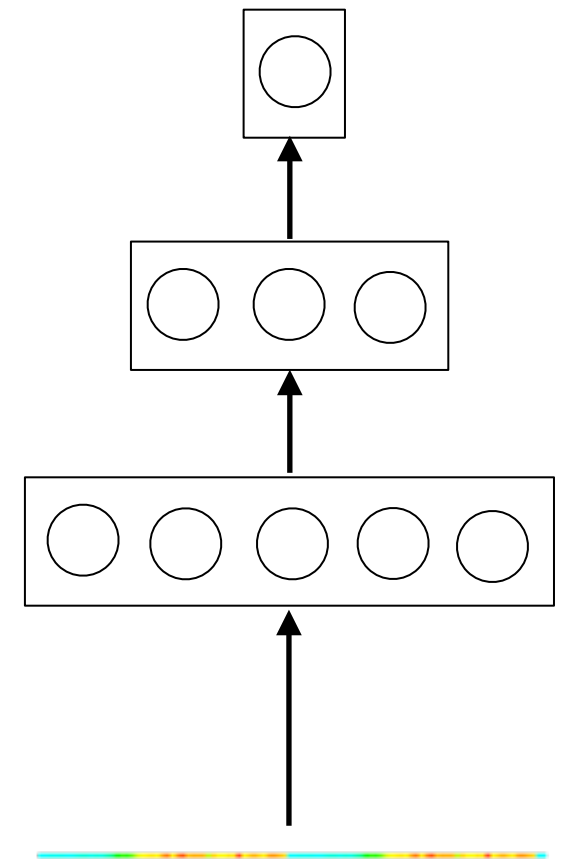
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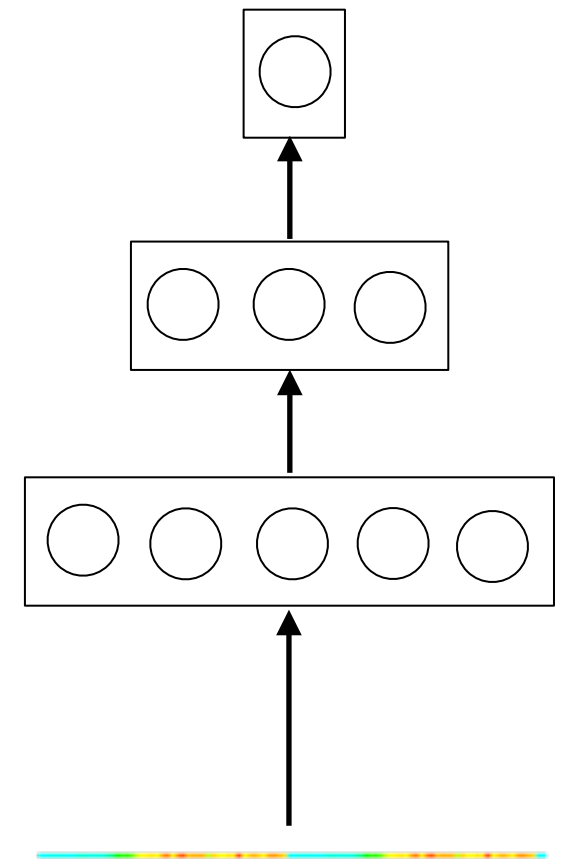
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 - Cannot process inputs of differing length
 - Cannot distinguish between absolute and relative position



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- Simple idea: spatial representation of time:
 - Need a buffer; not biologically plausible
 - Cannot process inputs of differing length
 - Cannot distinguish between absolute and relative position
- This motivates an **implicit** representation of time in connectionist models where time is represented by its effect on processing



A RICH HISTORY

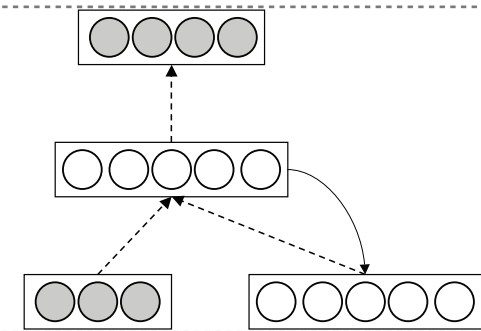
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A RICH HISTORY

Elman networks

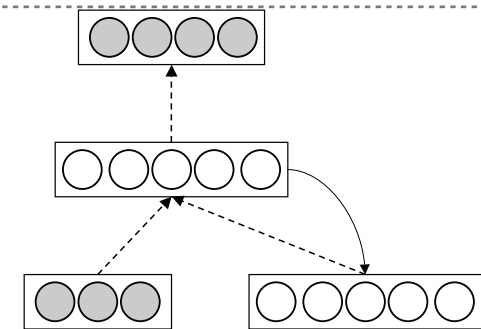
Time-delayed “context” units, truncated BPTT.
(Elman, 1990), (Jordan, 1986)



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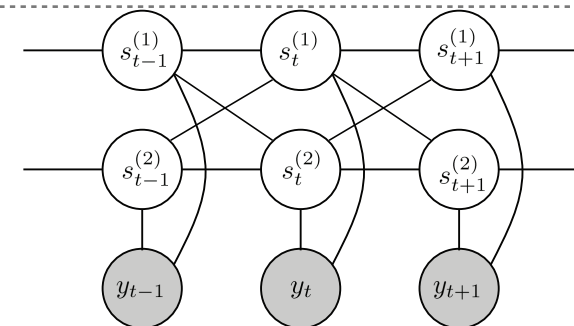
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Mean-field Boltzmann Machines through Time

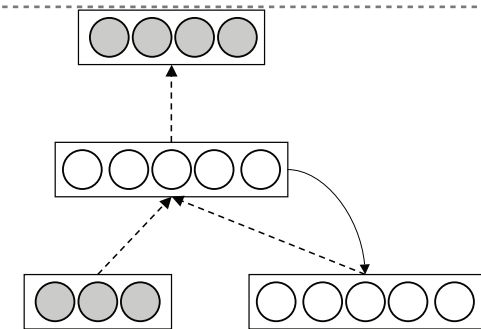
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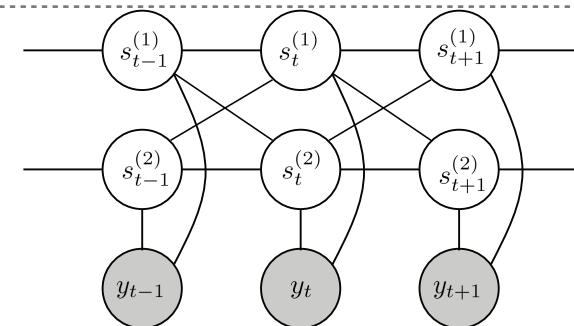
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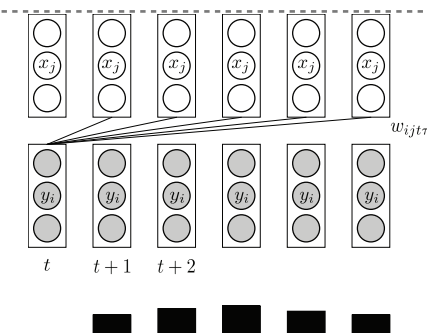
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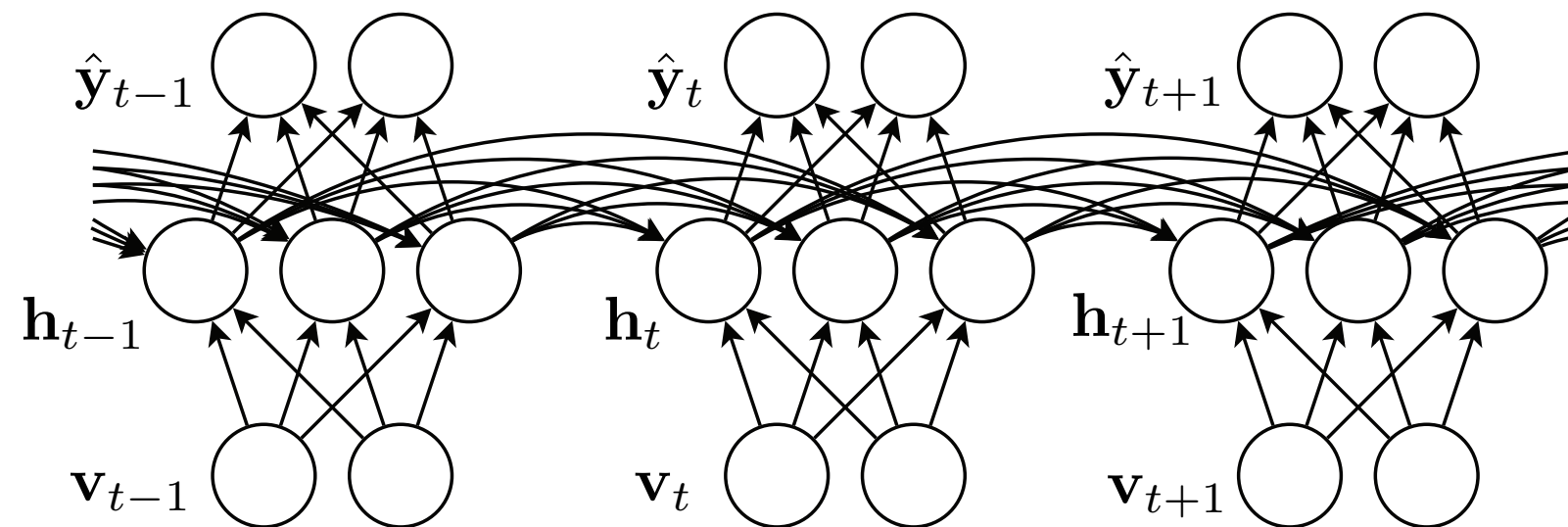


Spiking Boltzmann Machines

Hidden-state dynamics and smoothness constraints on observed data.
(Hinton and Brown, 2000)



RECURRENT NEURAL NETWORKS



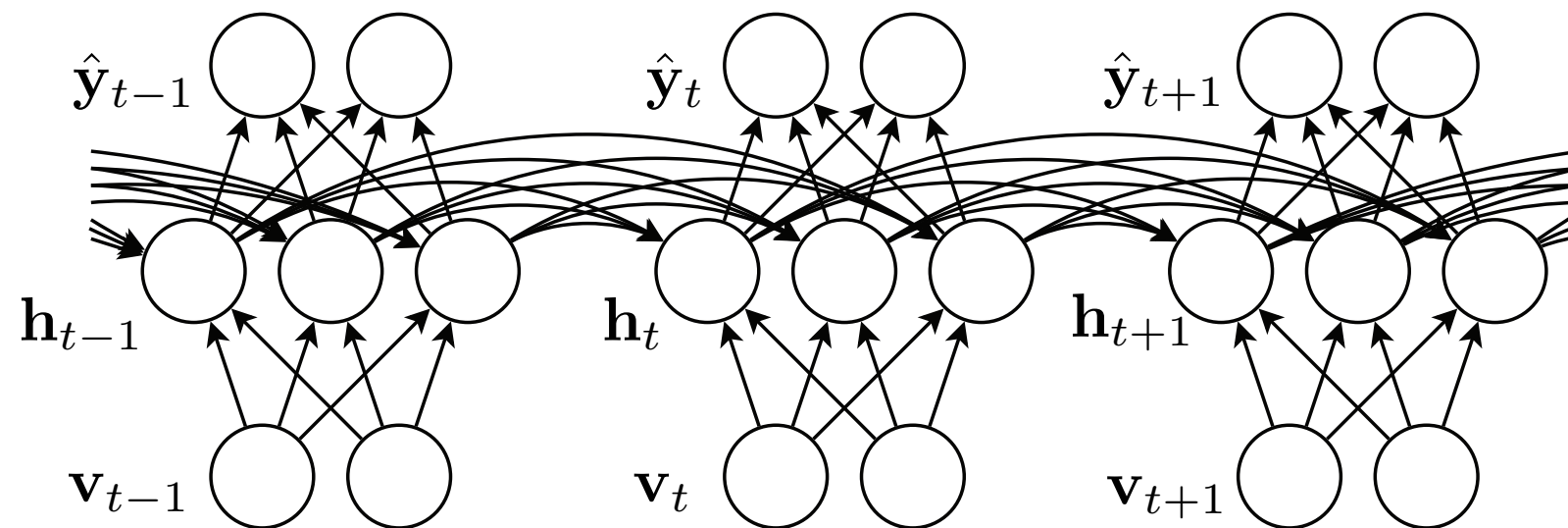
$$\begin{aligned}\mathbf{x}_t &= W^{hv}\mathbf{v}_t + W^{hh}\mathbf{h}_{t-1} + \mathbf{b}_h \\ h_{j,t} &= f(x_{j,t}) \\ \mathbf{s}_t &= W^{yh}\mathbf{h}_t + \mathbf{b}_y \\ \hat{y}_{k,t} &= g(s_{k,t})\end{aligned}$$

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(Figure from Martens and Sutskever)

RECURRENT NEURAL NETWORKS



- Neural network replicated in time

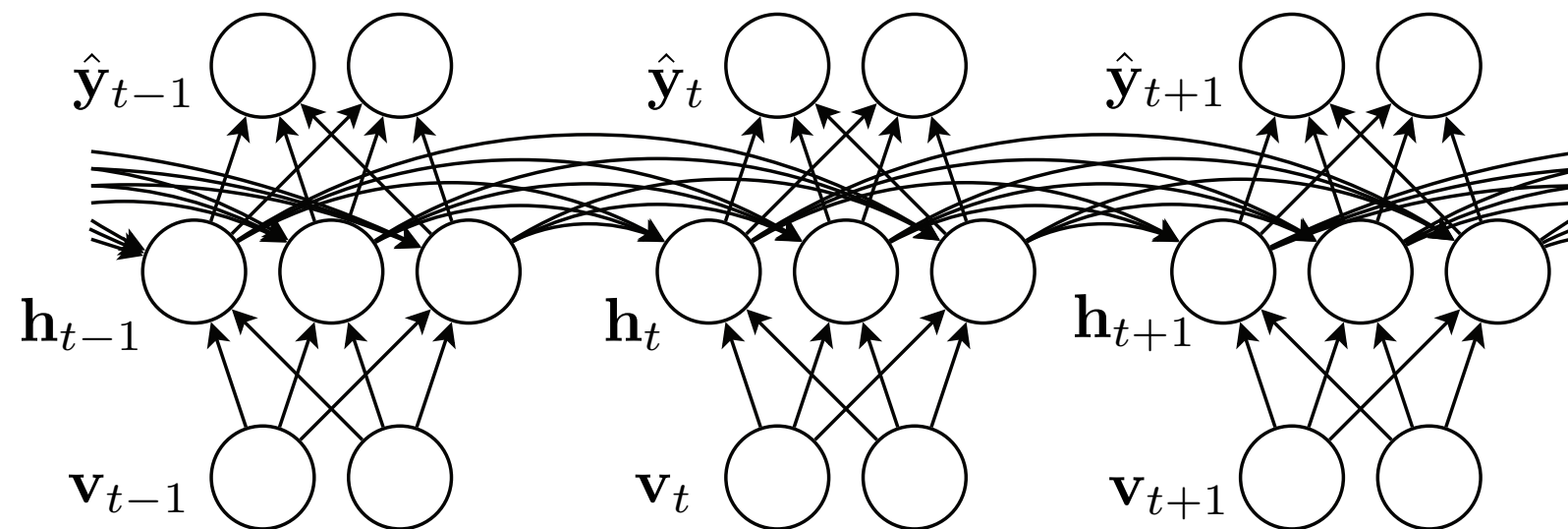
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(Figure from Martens and Sutskever)

RECURRENT NEURAL NETWORKS



- Neural network replicated in time
- At each step, receives input vector, updates its internal representation via nonlinear activation functions, and makes a prediction:

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TRAINING RECURRENT NEURAL NETWORKS

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TRAINING RECURRENT NEURAL NETWORKS

- Possibly high-dimensional, distributed, internal representation and nonlinear dynamics allow model, in theory, model complex time series

TRAINING RECURRENT NEURAL NETWORKS

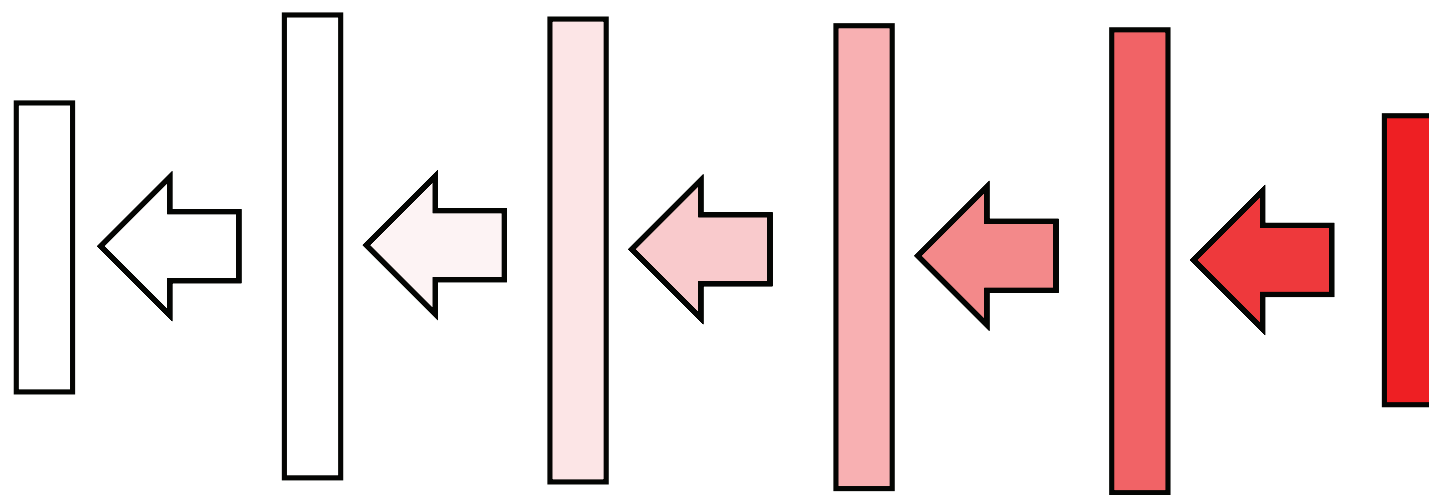
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(Figure adapted from James Martens)

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 - Much work in the 1990's focused on identifying and addressing these issues: none of these methods were widely adopted
- Best-known attempts to resolve the problem of RNN training:
 - Long Short-term Memory (LSTM) (Hochreiter and Schmidhuber 1997)
 - Echo-State Network (ESN) (Jaeger and Haas 2004)

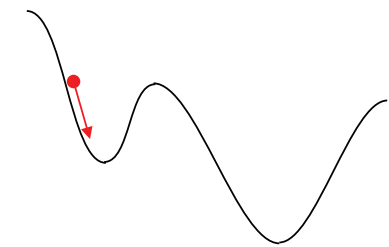
FAILURE OF GRADIENT DESCENT

Two hypotheses for why gradient descent fails for NN:

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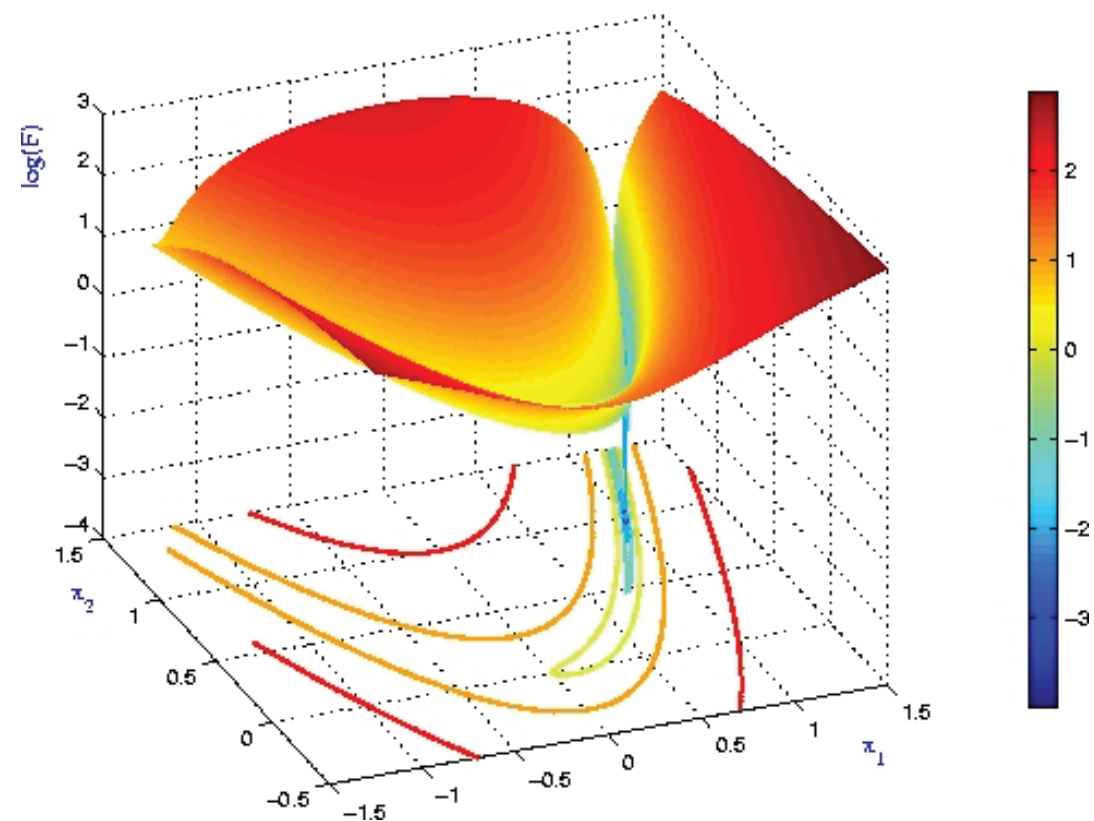
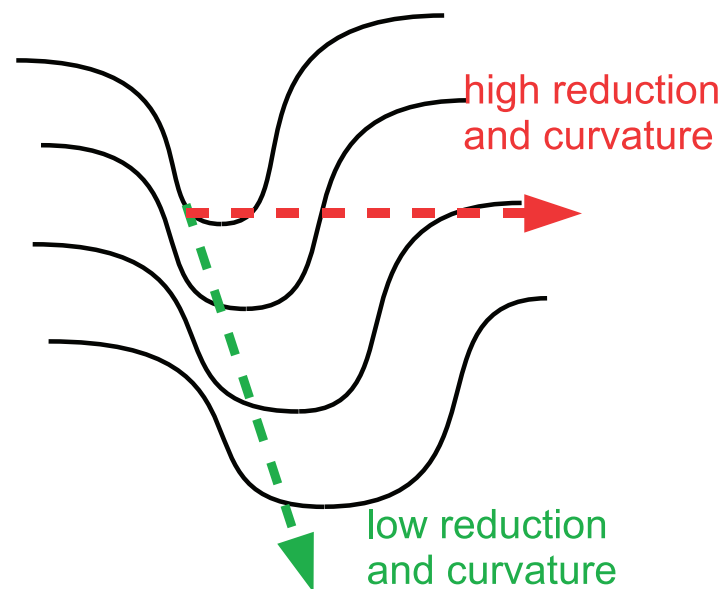


FAILURE OF GRADIENT DESCENT

Two hypotheses for why gradient descent fails for NN:

- increased frequency and severity of bad local minima
- pathological curvature, like the type seen in the Rosenbrock function:

$$f(x, y) = (1 - x)^2 + 100(y - x^2)^2$$



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(Figures from James Martens)

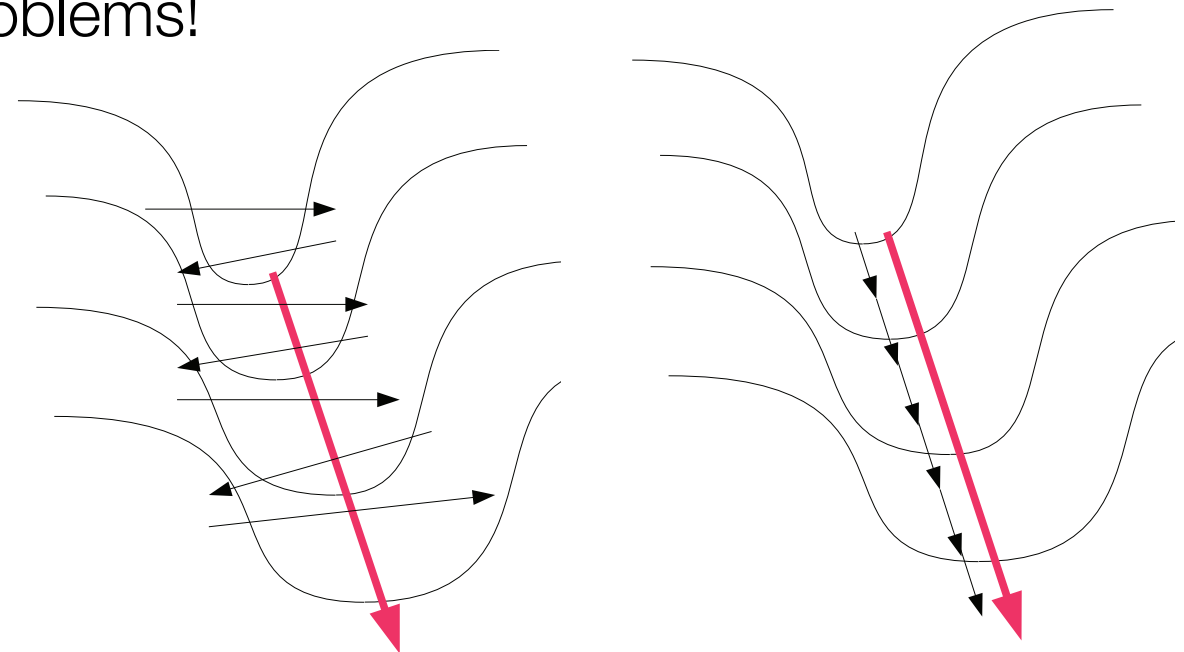
SECOND ORDER METHODS

- Model the objective function by the local approximation:

$$f(\theta + p) \approx q_\theta(p) \equiv f(\theta) + \Delta f(\theta)^T p + \frac{1}{2} p^T B p$$

where p is the search direction and B is a matrix which quantifies curvature

- In Newton's method, B is the Hessian matrix, H
- By taking the curvature information into account, Newton's method “rescales” the gradient so it is a much more sensible direction to follow
- Not feasible for high-dimensional problems!



HESSIAN-FREE OPTIMIZATION

Based on exploiting two simple ideas (and some additional “tricks”):

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RNN demo code (using Theano): <http://github.com/gwtaylor/theano-rnn>

GENERATIVE MODELS WITH DISTRIBUTED STATE

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GENERATIVE MODELS WITH DISTRIBUTED STATE

- Many sequences are high-dimensional and have complex structure
 - music, human motion, weather/climate data
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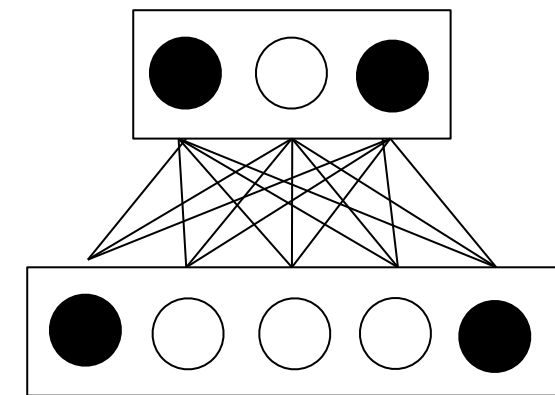
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- Generative models (like Restricted Boltzmann Machines) can capture complex distributions
- Use binary hidden state and gain the best of HMM & LDS:
 - the nonlinear dynamics and observation model of the HMM without the limited hidden state
 - the efficient, expressive state of the LDS without the linear-Gaussian restriction on dynamics and observations

DISTRIBUTED BINARY HIDDEN STATE

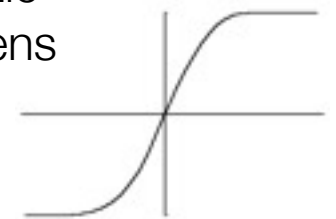
- Using distributed binary representations for hidden state in directed models of time series makes inference difficult. But we can:
 - Use a Restricted Boltzmann Machine (RBM) for the interactions between hidden and visible variables. A factorial posterior makes inference and sampling easy.
 - Treat the visible variables in the previous time slice as additional **fixed** inputs

Hidden variables (factors) at time t



Visible variables (observations) at time t

One typically uses binary logistic units for both visibles and hiddens



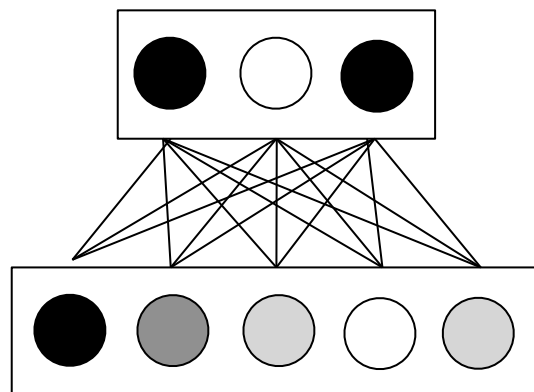
$$p(h_j = 1|\mathbf{v}) = \sigma(b_j + \sum_i v_i W_{ij})$$

$$p(v_i = 1|\mathbf{h}) = \sigma(b_i + \sum_j h_j W_{ij})$$

MODELING OBSERVATIONS WITH AN RBM

- So the distributed binary latent (hidden) state of an RBM lets us:
 - Model complex, nonlinear dynamics
 - Easily and exactly infer the latent binary state given the observations
- But RBMs treat data as static (i.i.d.)

Hidden variables (factors) at time t

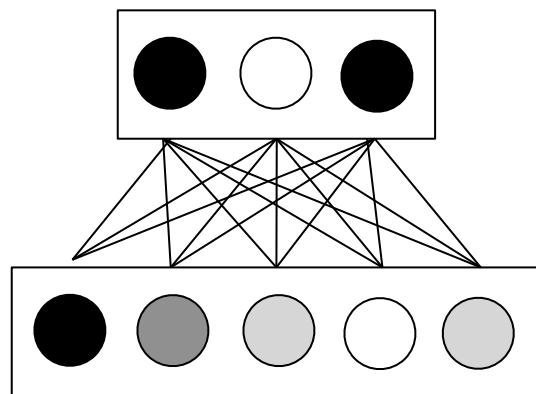


Visible variables (joint angles) at time t

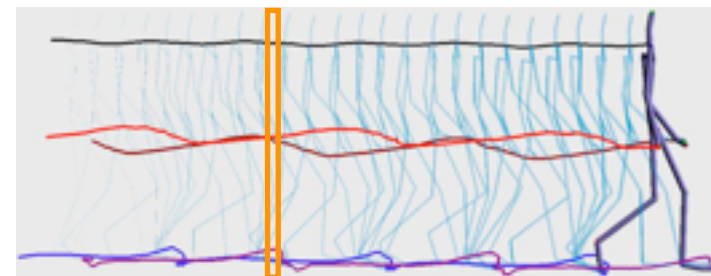
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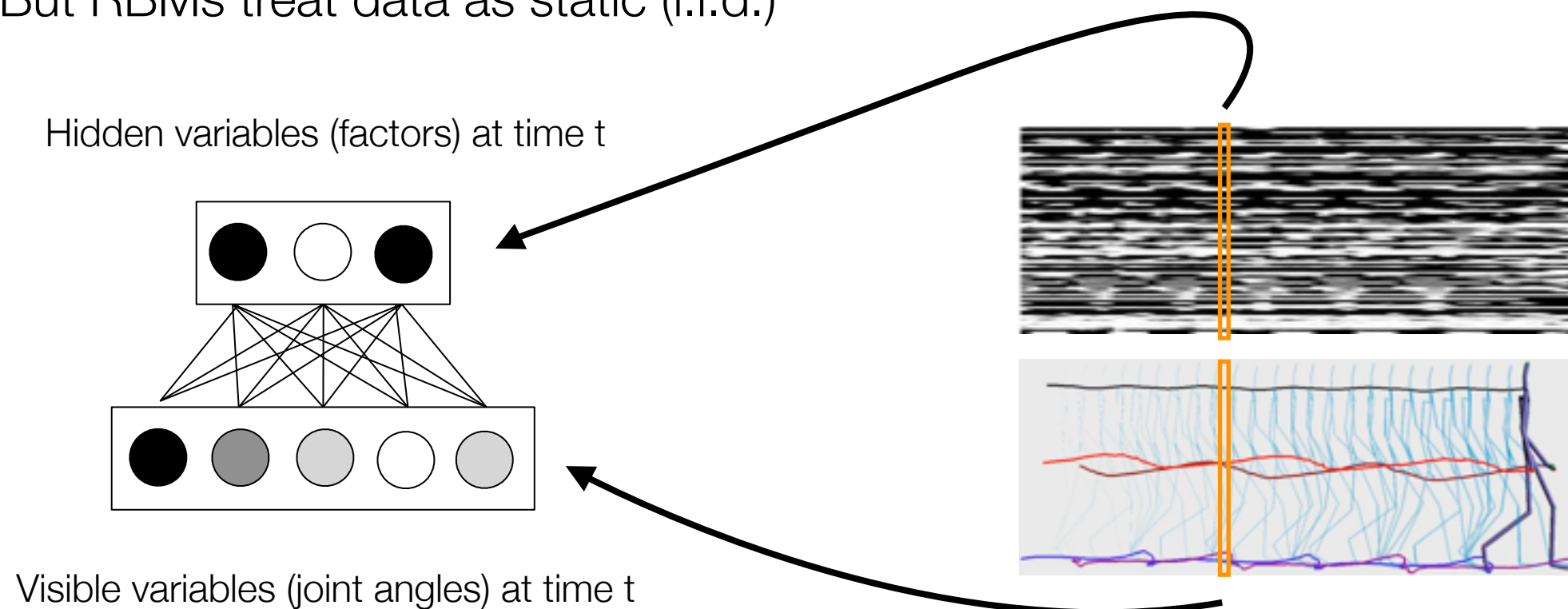


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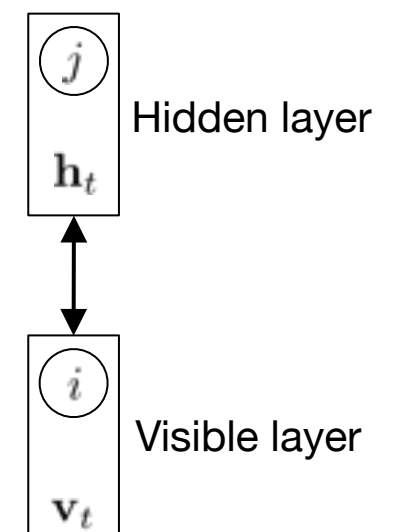
CONDITIONAL RESTRICTED BOLTZMANN MACHINES

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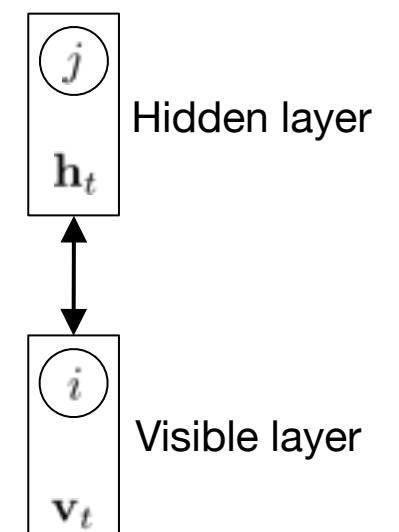
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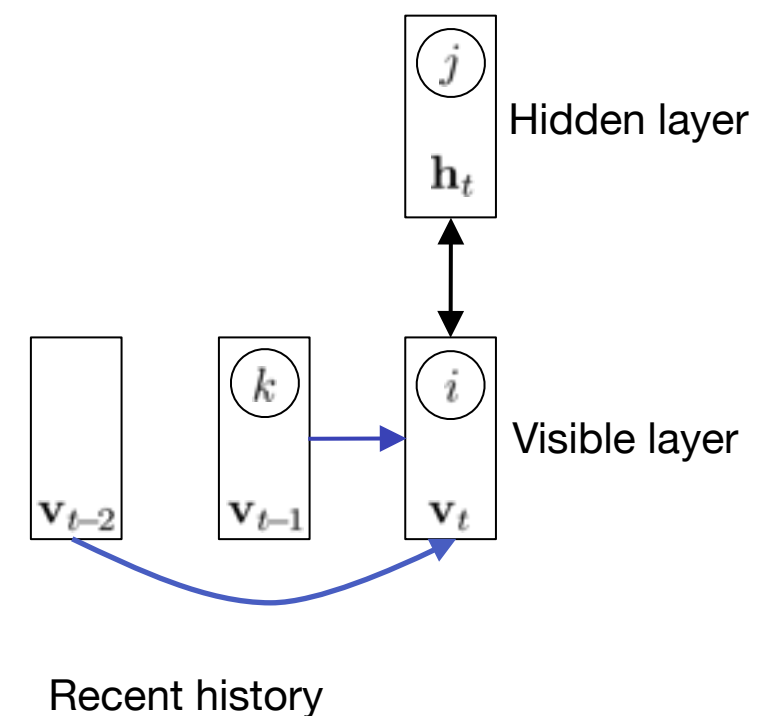
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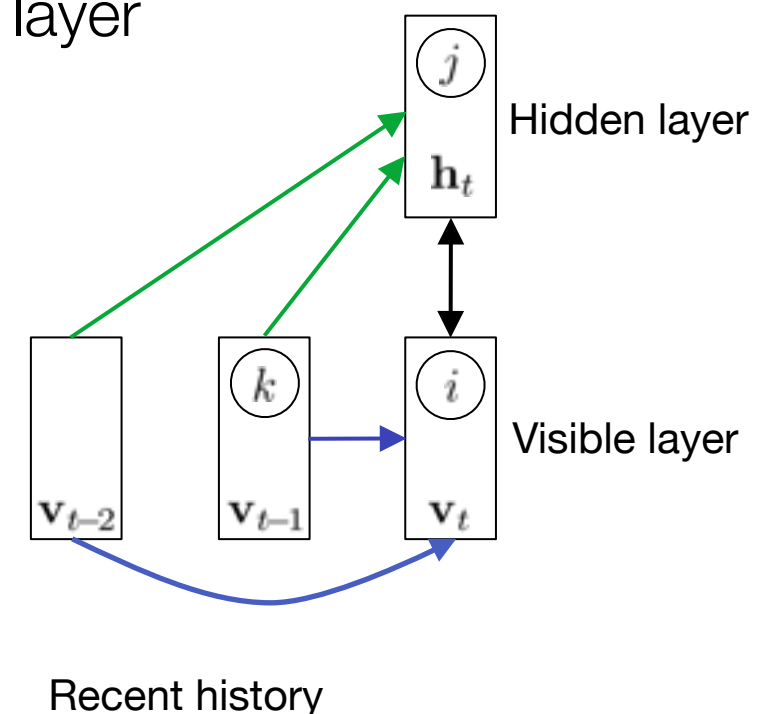
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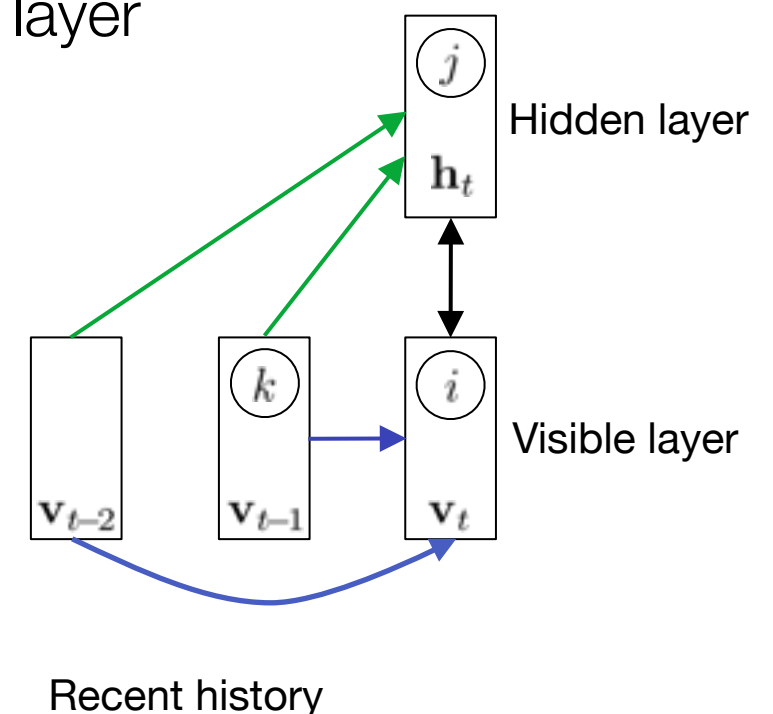
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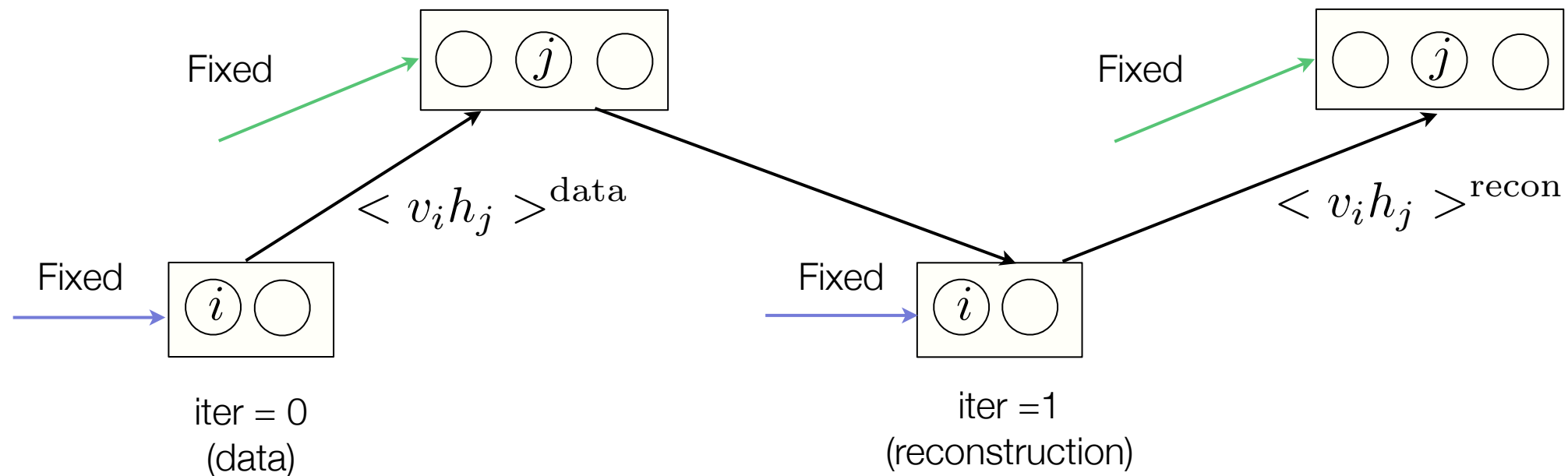
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 - History can also influence dynamics through hidden layer
- Conditioning does not change inference nor learning



CONTRASTIVE DIVERGENCE LEARNING IN A CRBM



- When updating visible and hidden units, we implement directed connections by treating data from previous time steps as a dynamically changing bias
- Inference and learning do not change

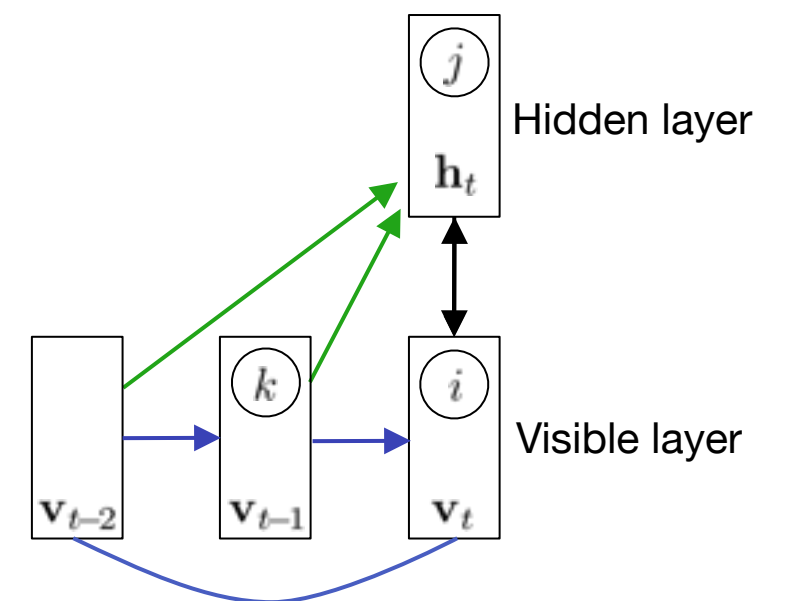
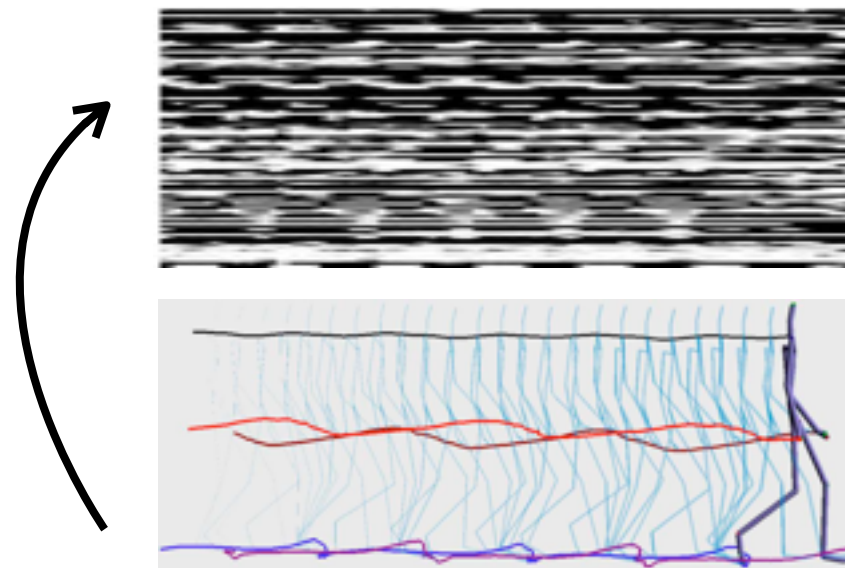
STACKING: THE CONDITIONAL DEEP BELIEF NETWORK

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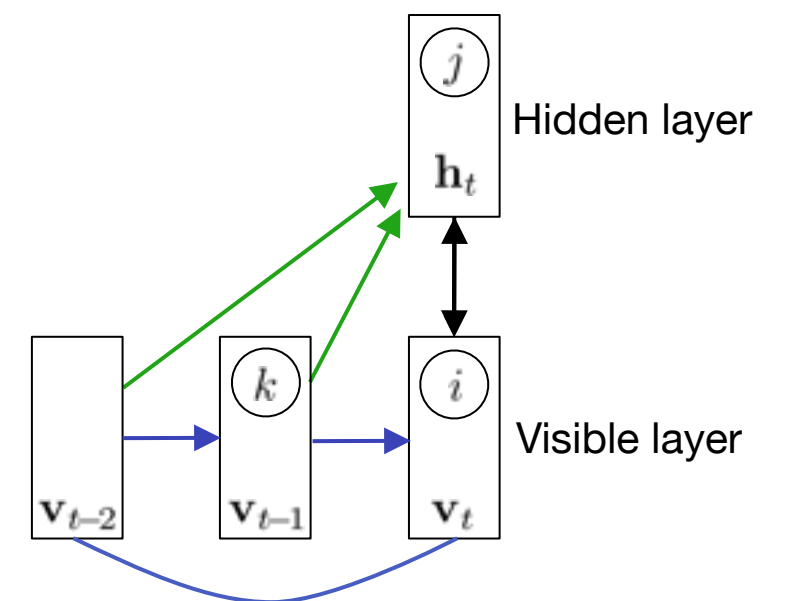
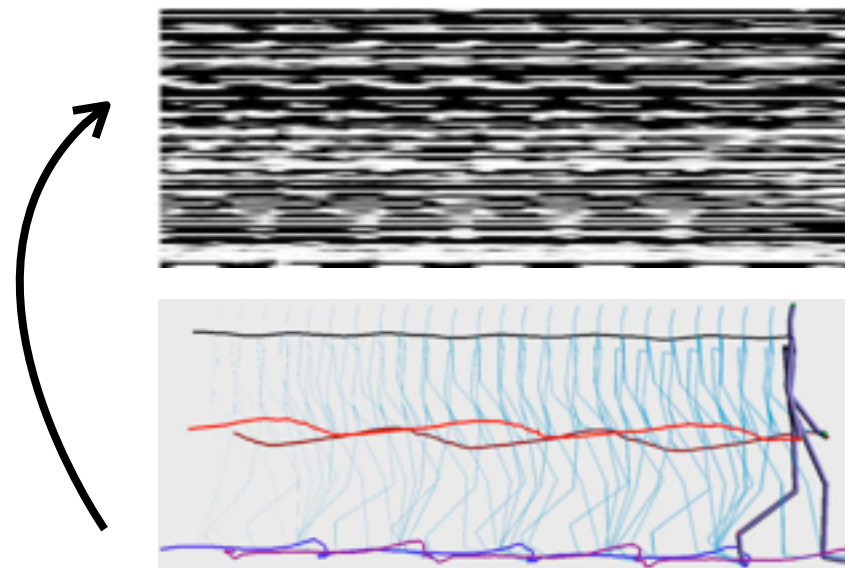
STACKING: THE CONDITIONAL DEEP BELIEF NETWORK

- Learn a CRBM



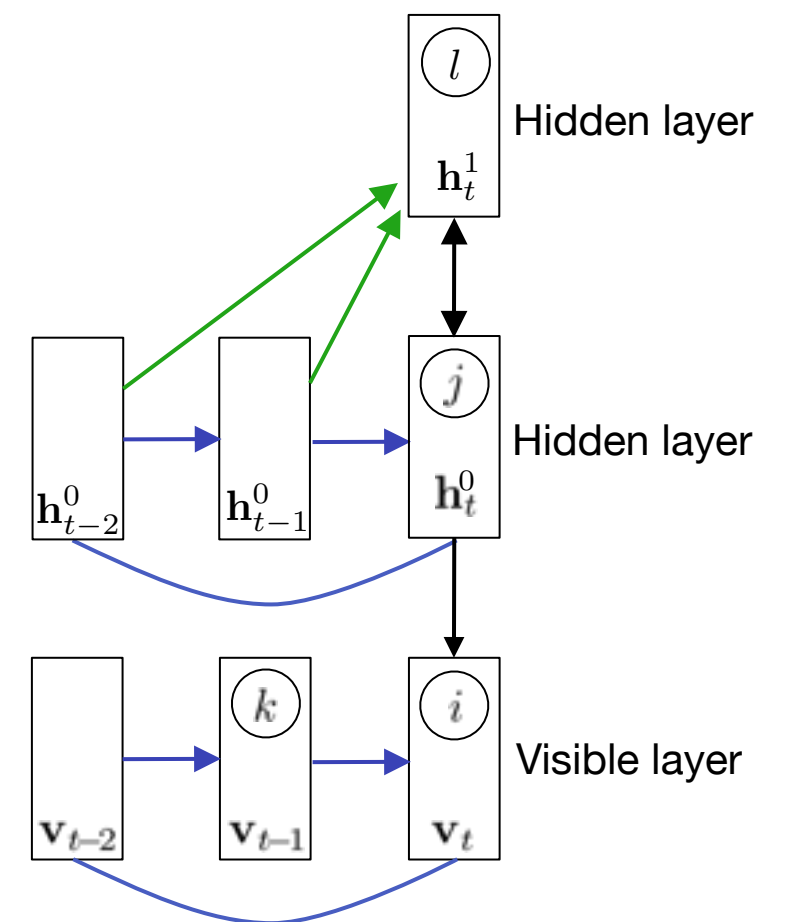
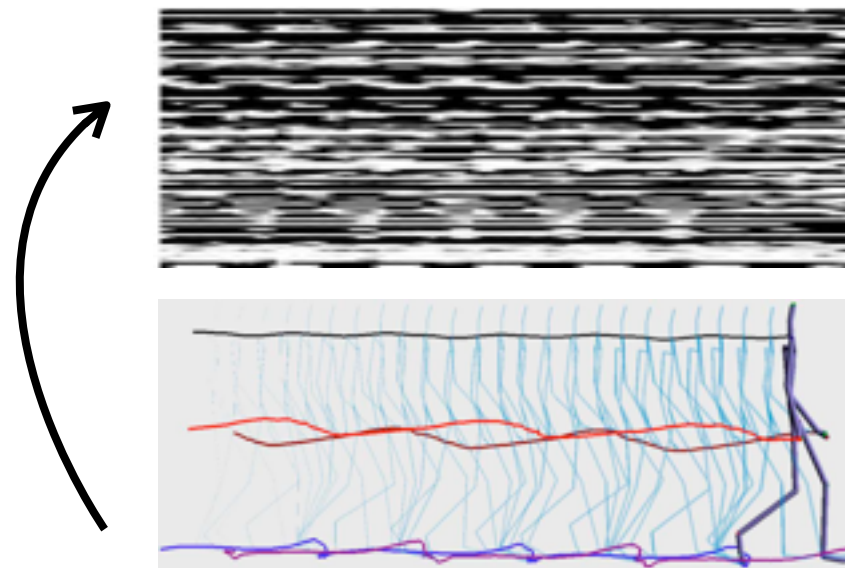
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- Learn a CRBM
- Now, treat the sequence of hidden units as “fully observed” data and train a second CRBM



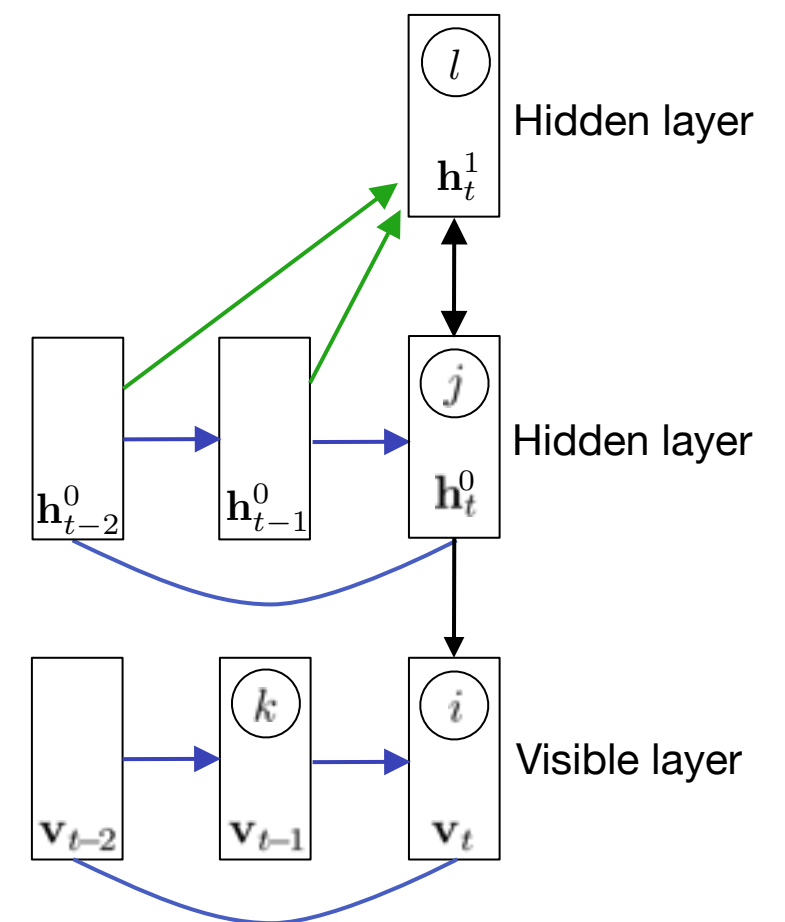
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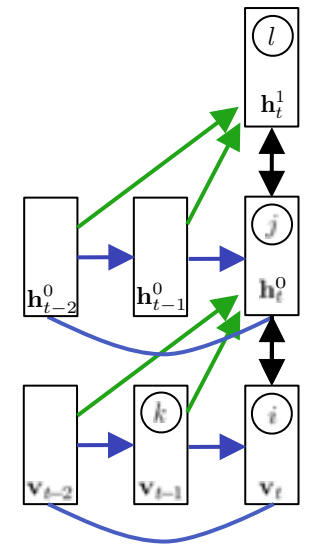
STACKING: THE CONDITIONAL DEEP BELIEF NETWORK

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- The composition of CRBMs is a conditional deep belief net
- It can be fine-tuned generatively or discriminatively



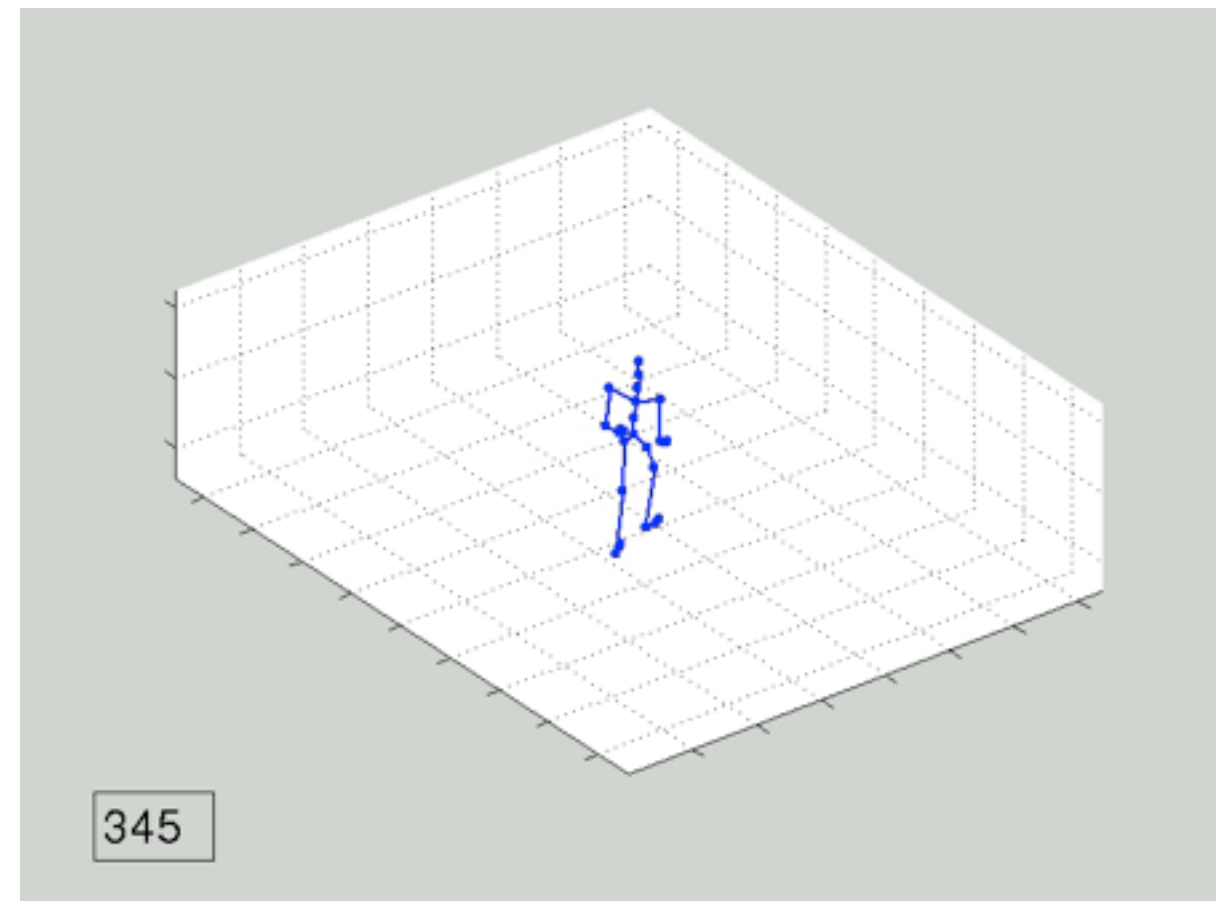
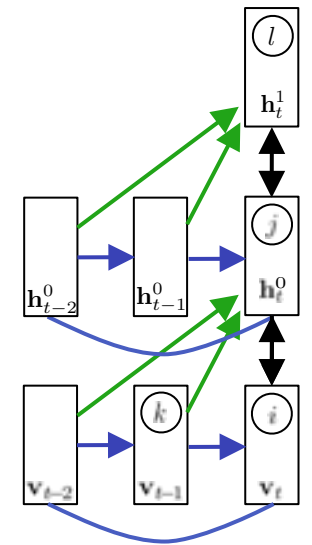
MOTION SYNTHESIS WITH A 2-LAYER CDBN

- Model is trained on ~8000 frames of 60fps data (49 dimensions)
- 10 styles of walking: cat, chicken, dinosaur, drunk, gangly, graceful, normal, old-man, sexy and strong
- 600 binary hidden units per layer
- < 1 hour training on a modern workstation

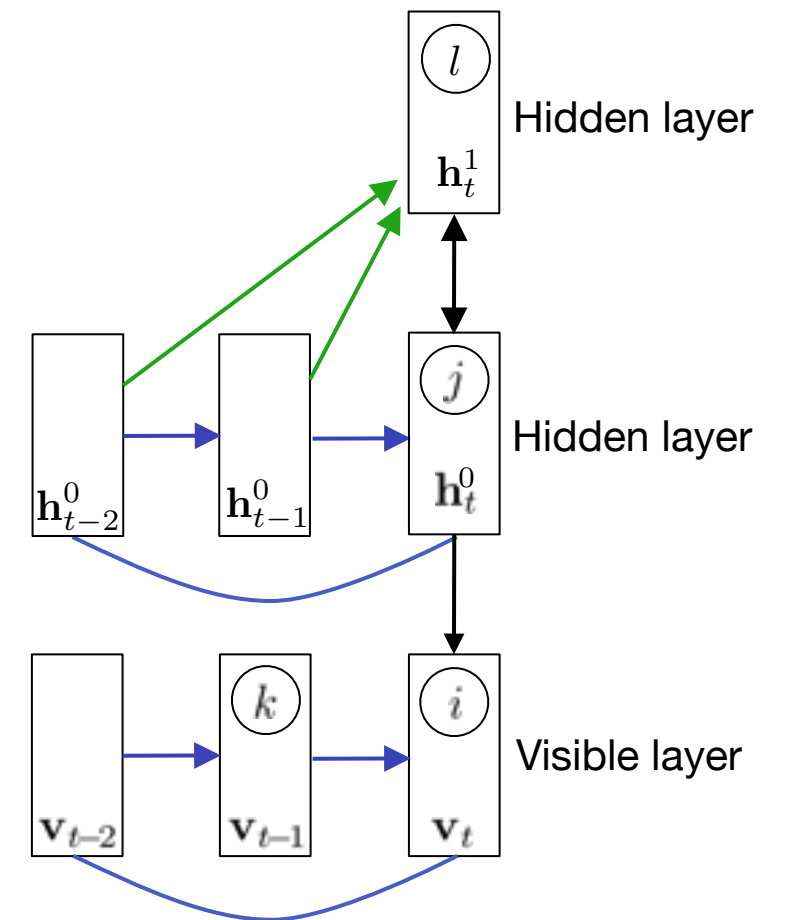


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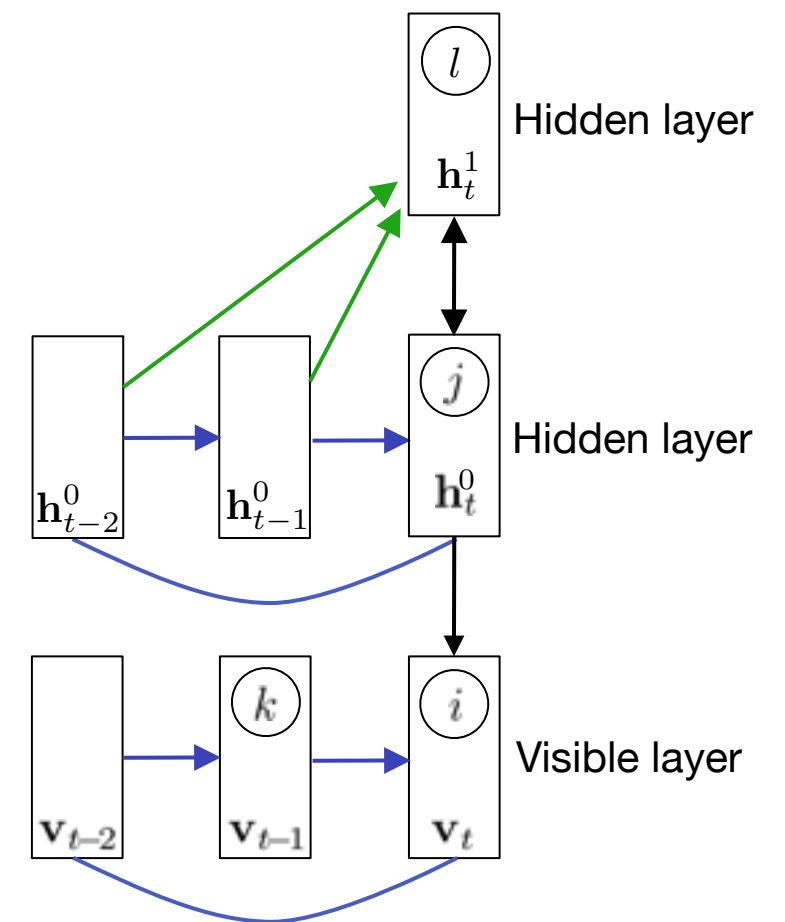


MODELING CONTEXT



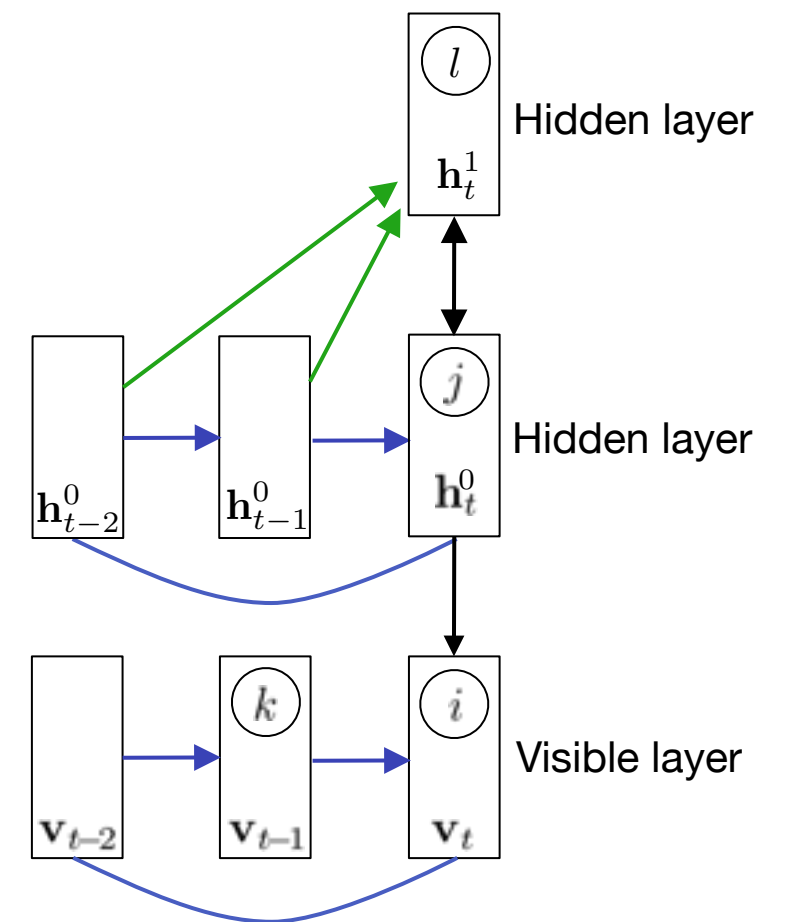
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- A single model was trained on 10 “styled” walks from CMU subject 137



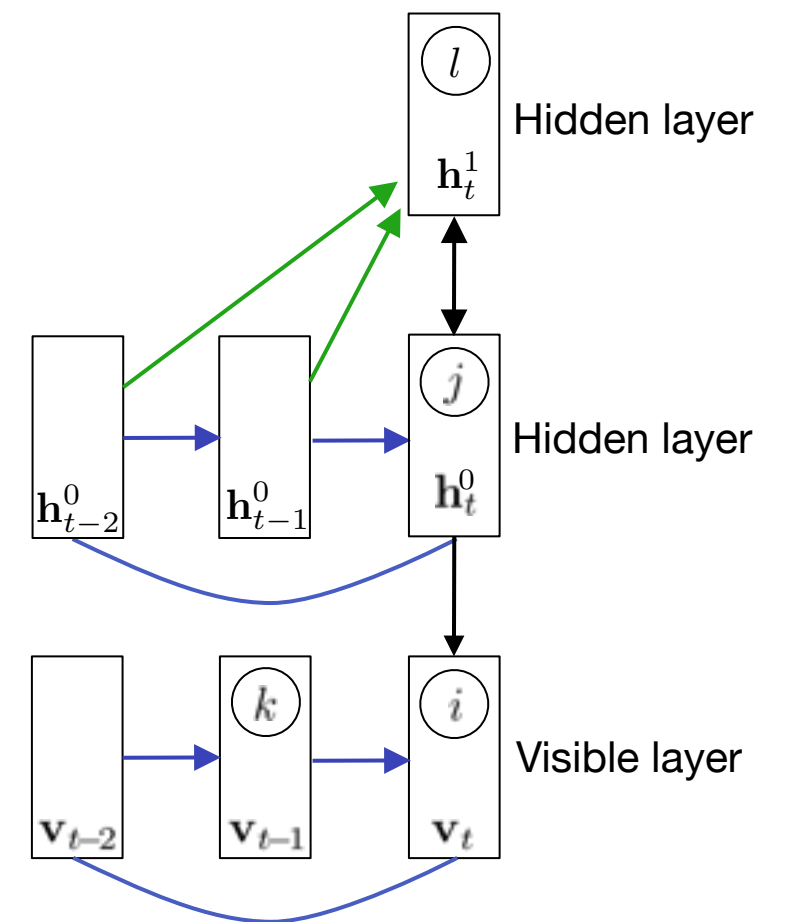
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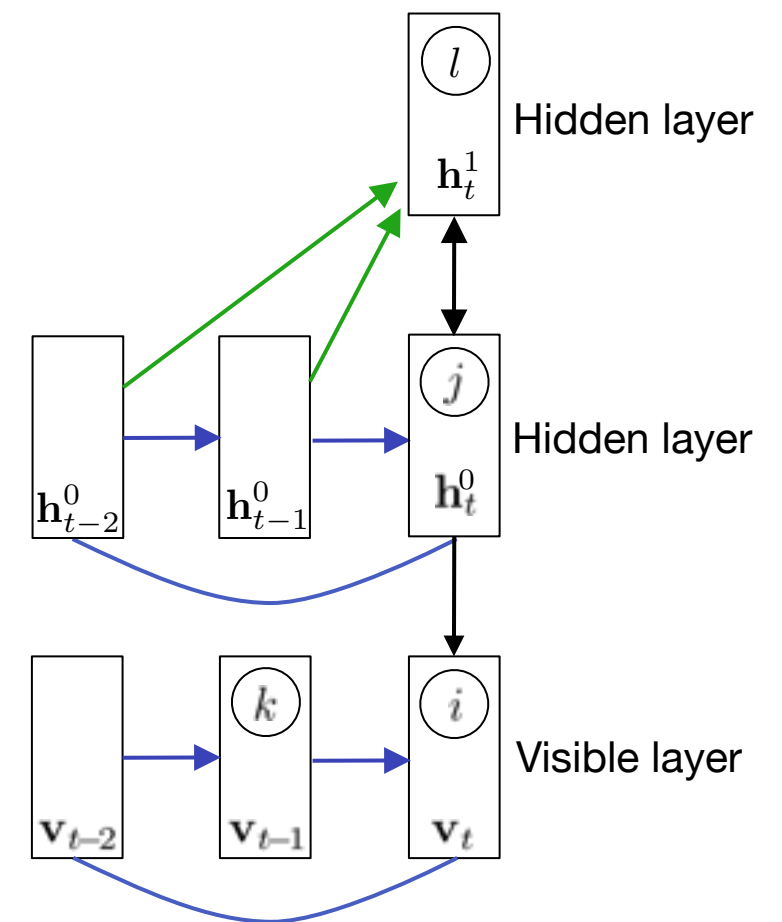
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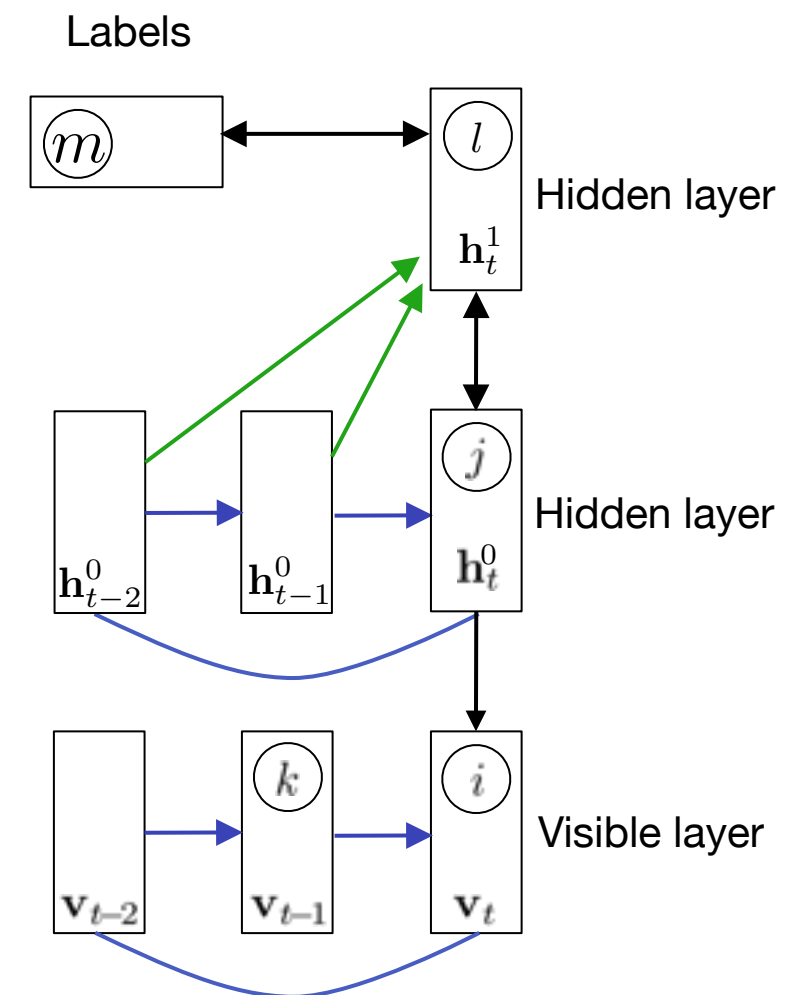
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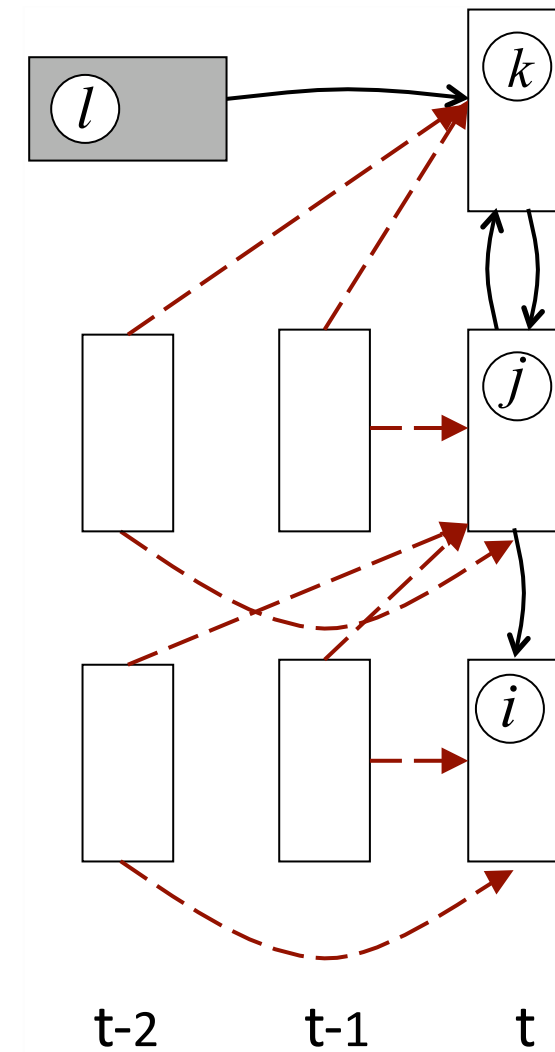
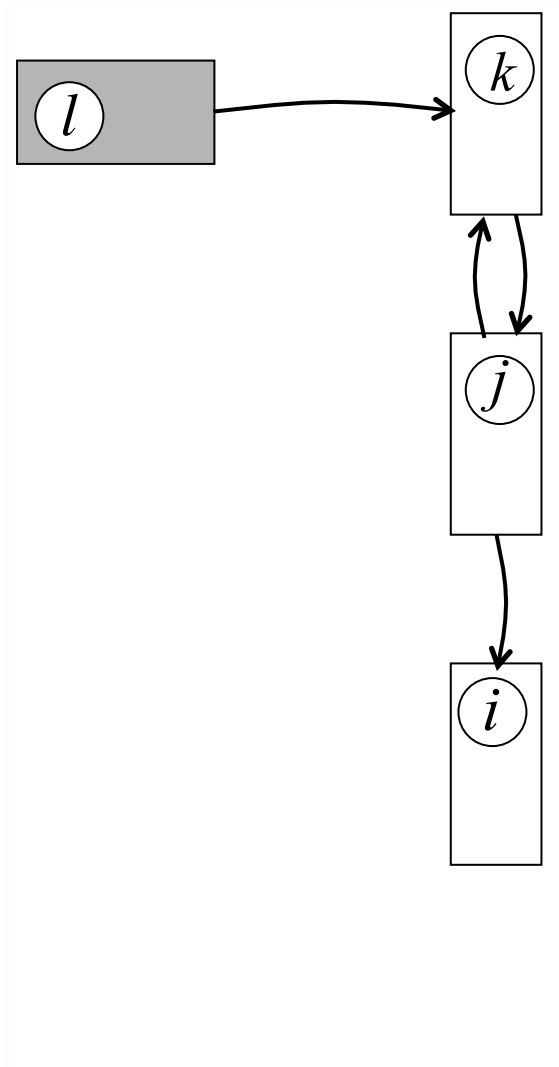


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- The model can generate each style based on initialization
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- How to blend styles?
- Style or person labels can be provided as part of the input to the top layer

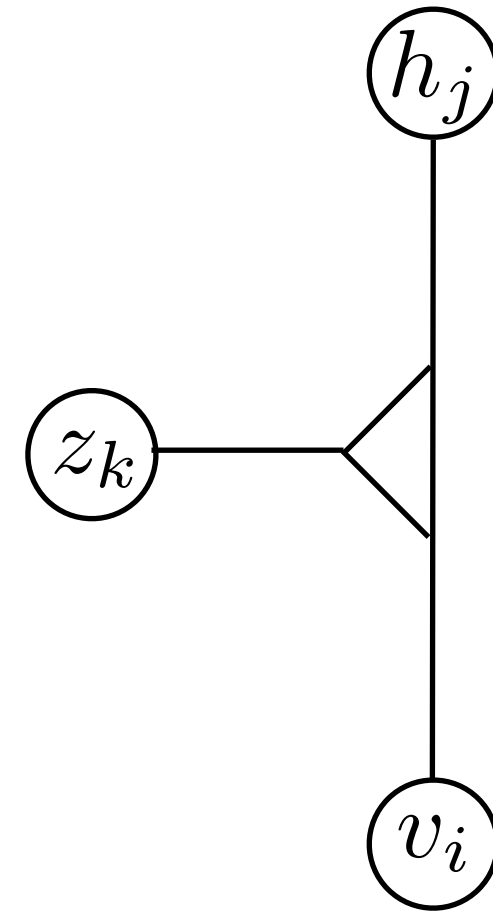


HOW TO MAKE CONTEXT INFLUENCE DYNAMICS?



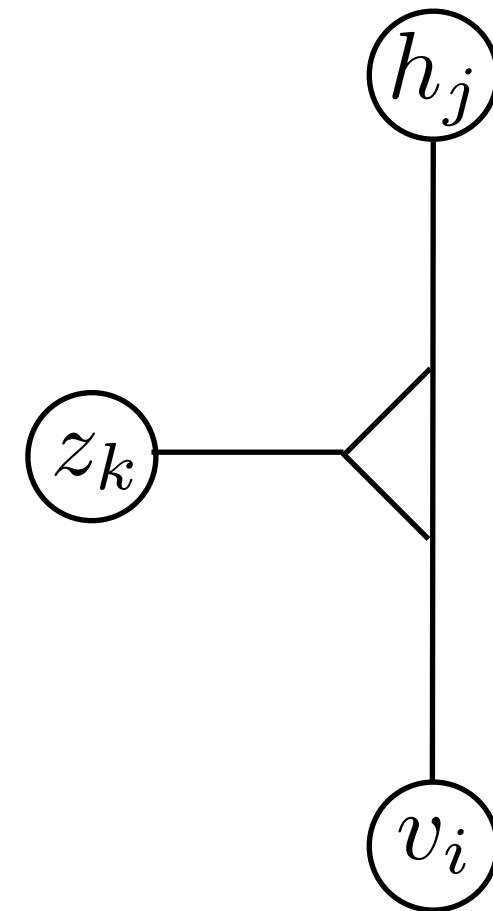
MULTIPLICATIVE INTERACTIONS

- Let latent variables act like *gates*, that dynamically change the connections between other variables
- This amounts to letting variables multiply connections between other variables: *three-way multiplicative interactions*
- Recently used in the context of learning *correspondence* between images (Memisevic & Hinton 2007, 2010) but long history before that



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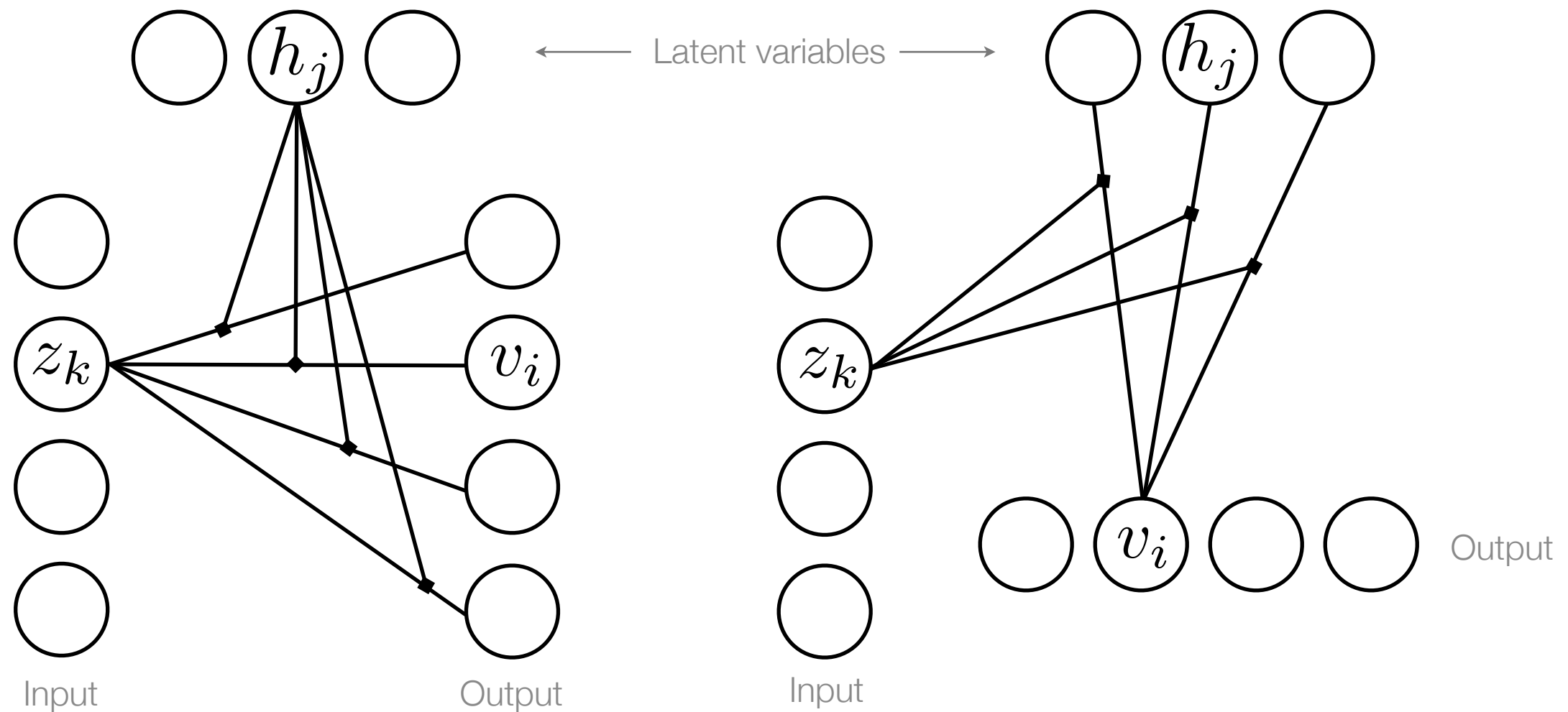
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Roland Memisevic has a nice Tutorial and review paper on the subject:
<http://www.cs.toronto.edu/~rfm/multiview-feature-learning-cvpr/>

GATED RESTRICTED BOLTZMANN MACHINES (GRBM)

Two views: Memisevic & Hinton (2007)

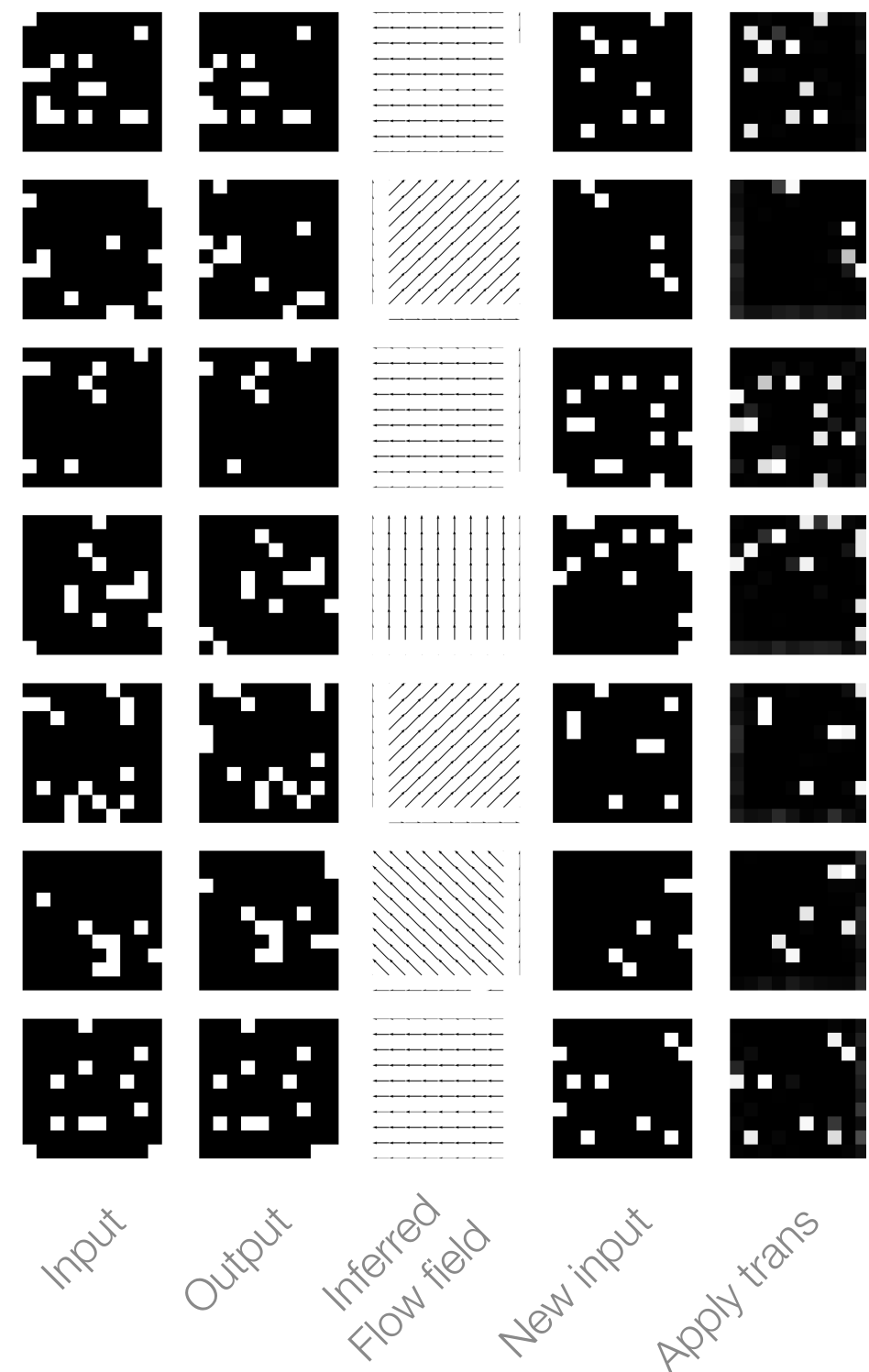


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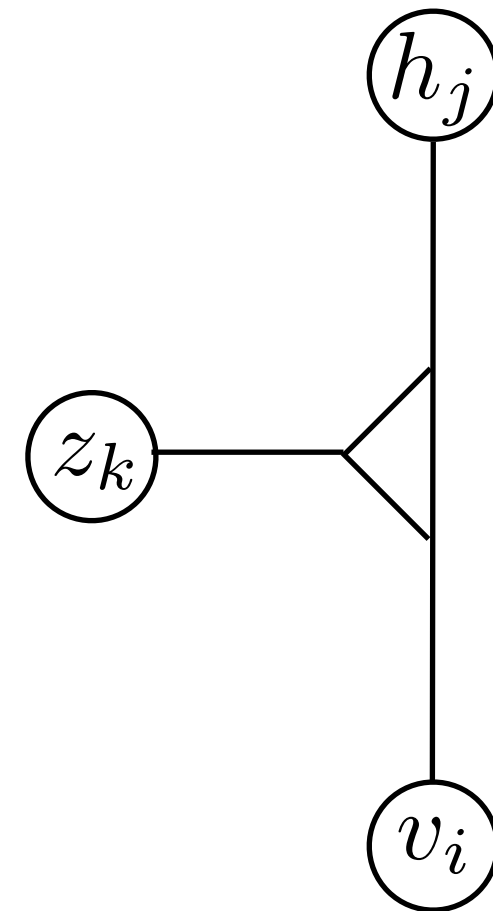
INFERRING OPTICAL FLOW: IMAGE “ANALOGIES”

- Toy images (Memisevic & Hinton 2006)
- No structure in these images, only *how they change*
- Can infer optical flow from a pair of images and apply it to a random image



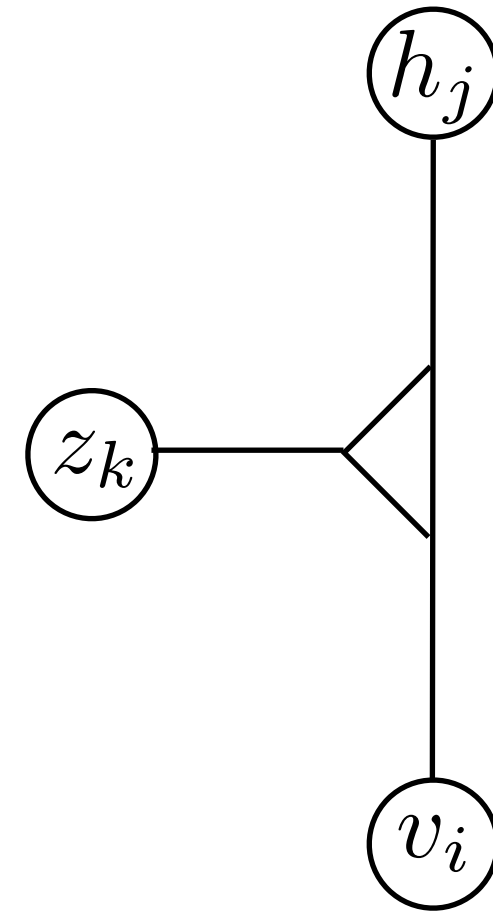
BACK TO MOTION STYLE

- Introduce a set of latent “context” variables whose value is known at training time
- In our example, these represent “motion style” but could also represent height, weight, gender, etc.
- The contextual variables gate every existing pairwise connection in our model



LEARNING AND INFERENCE

- Learning and inference remain almost the same as in the standard CRBM
- We can think of the context or style variables as “blending in” a whole “sub-network”
- This allows us to share parameters across styles but selectively adapt dynamics

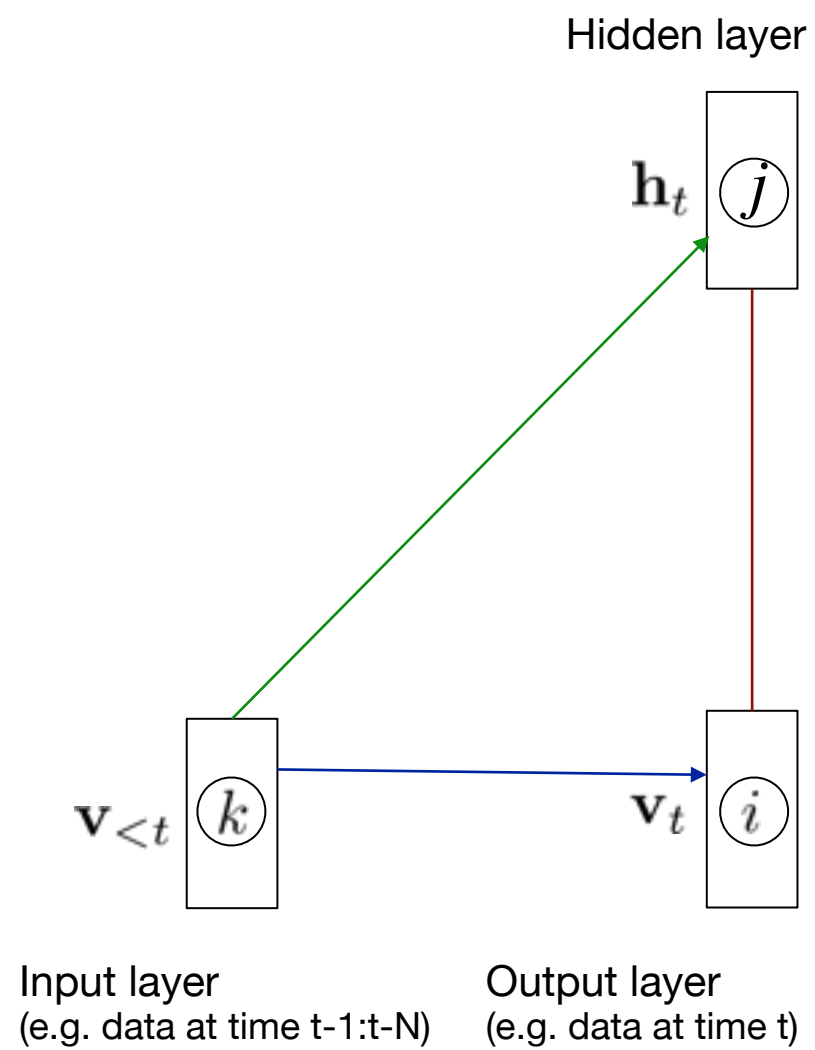


SUPERVISED MODELING OF STYLE

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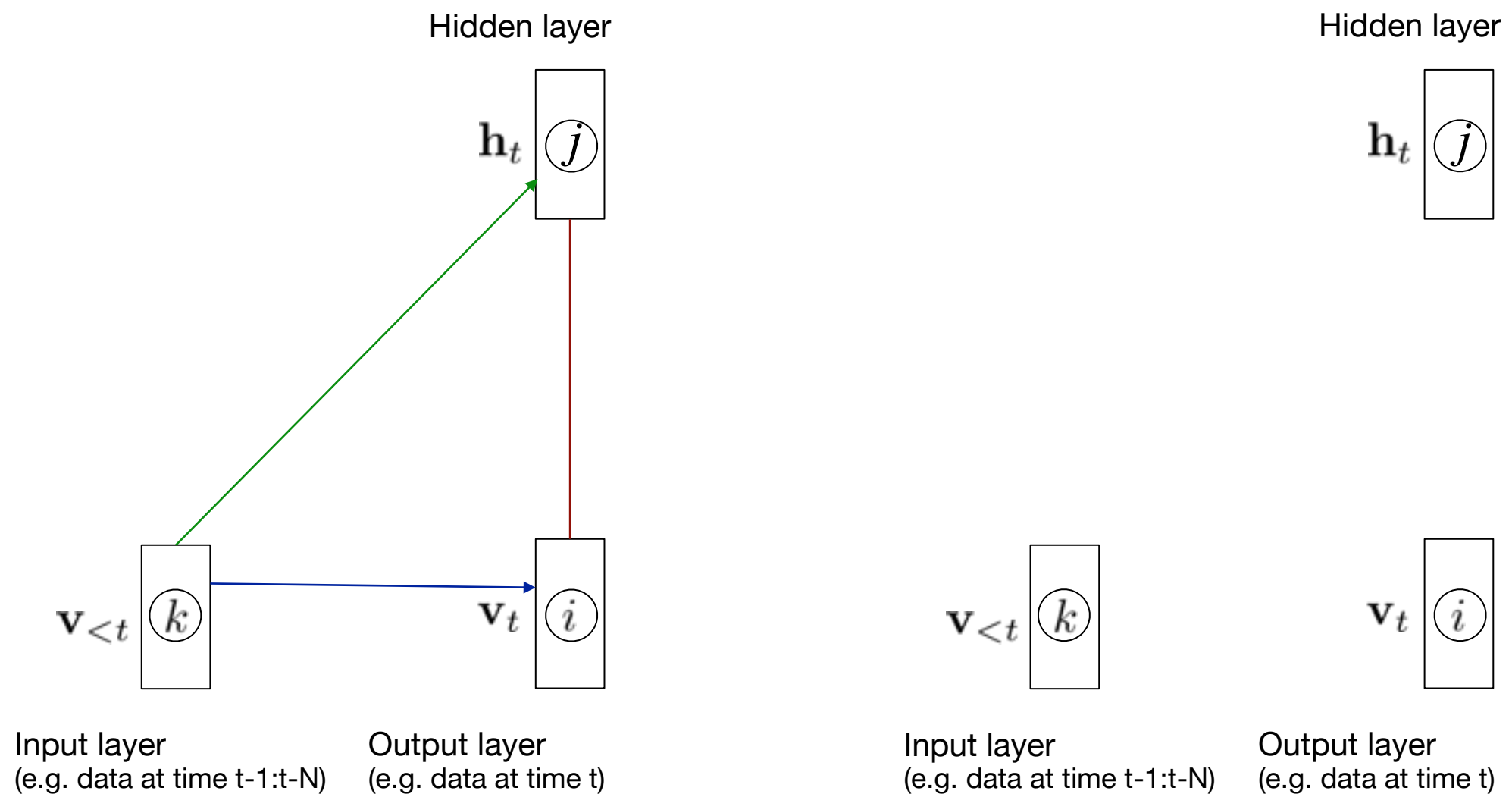


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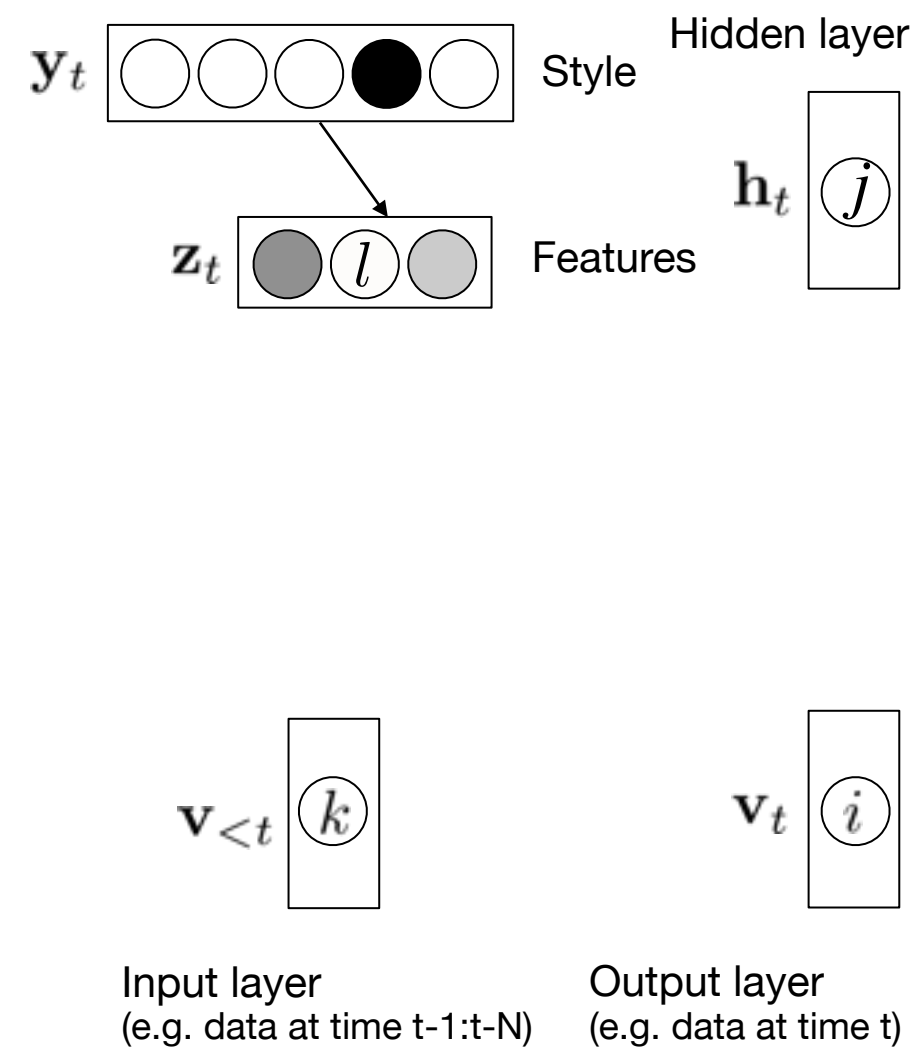
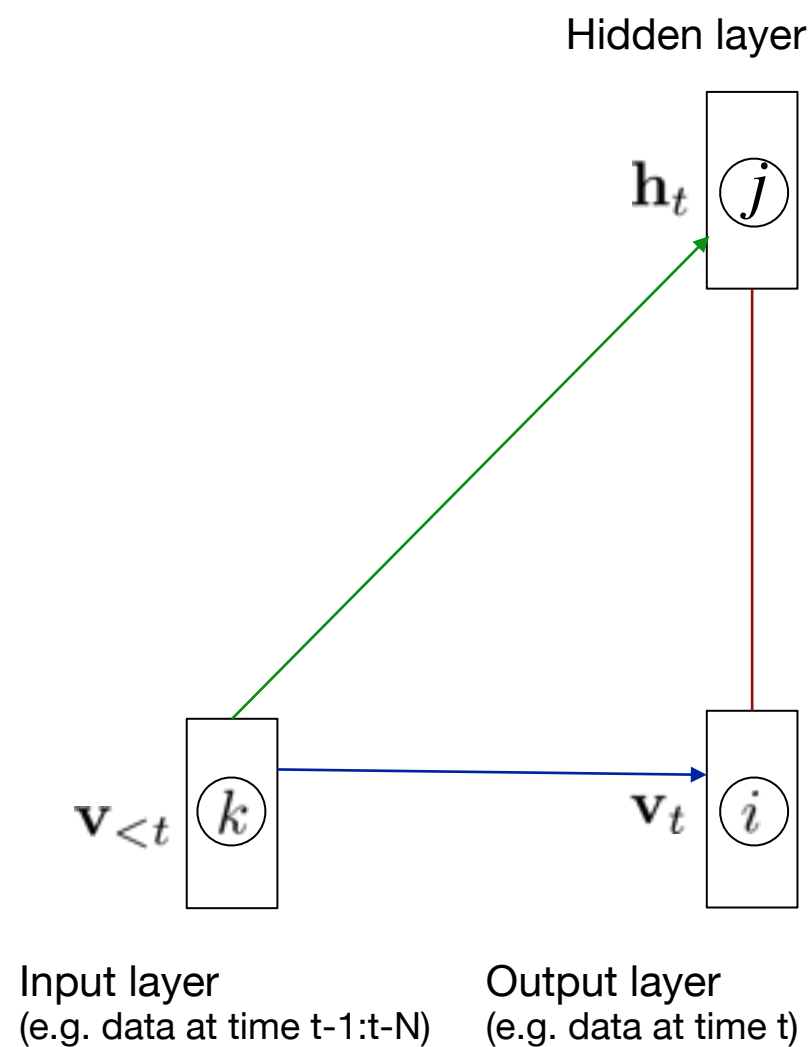


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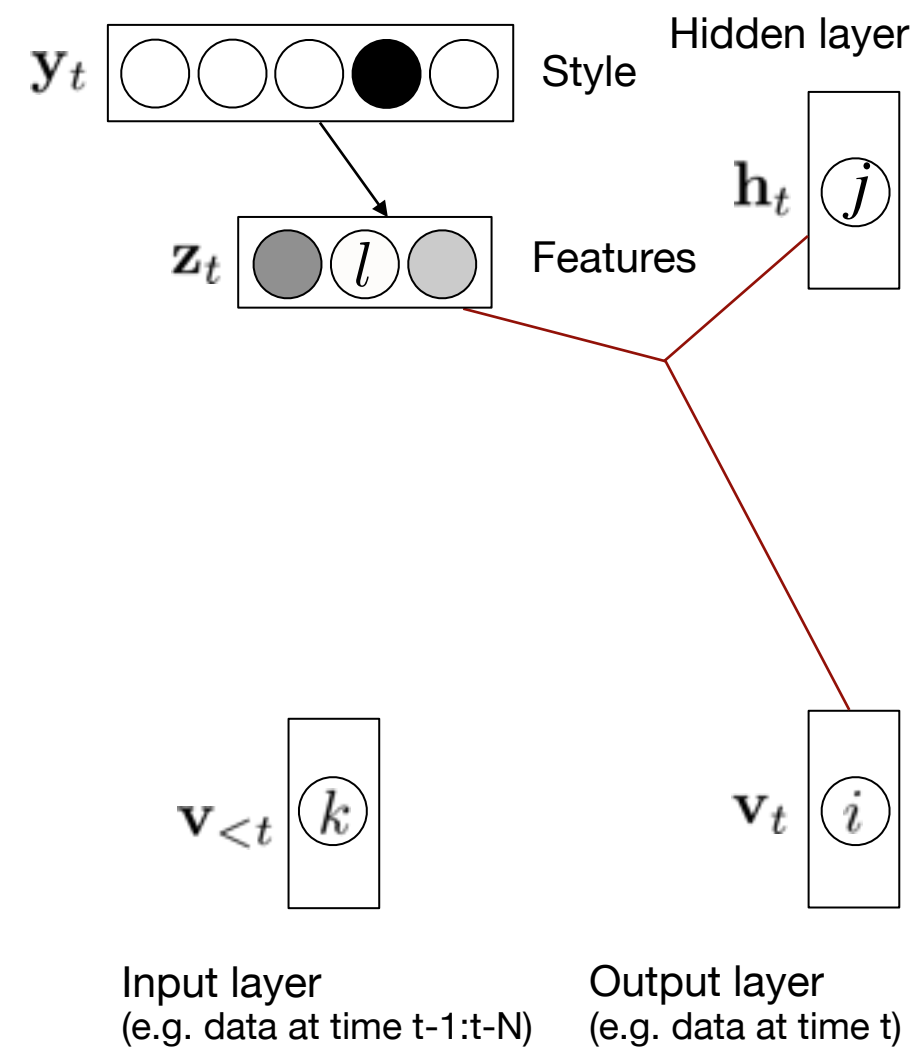
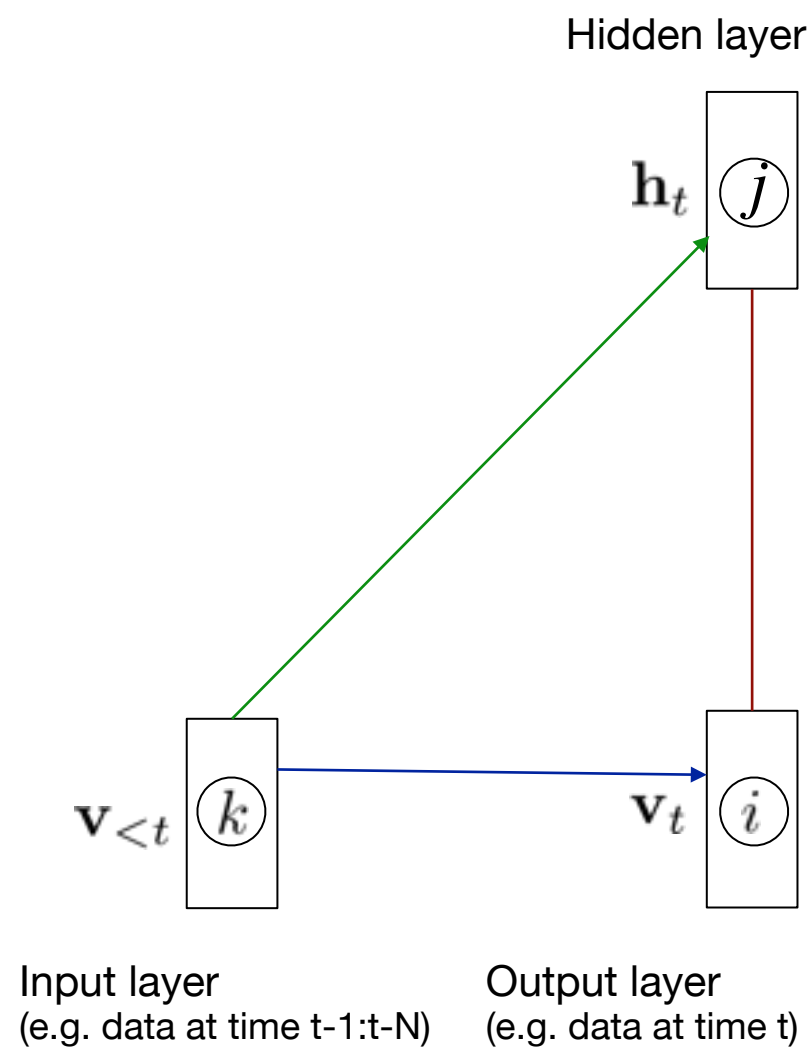


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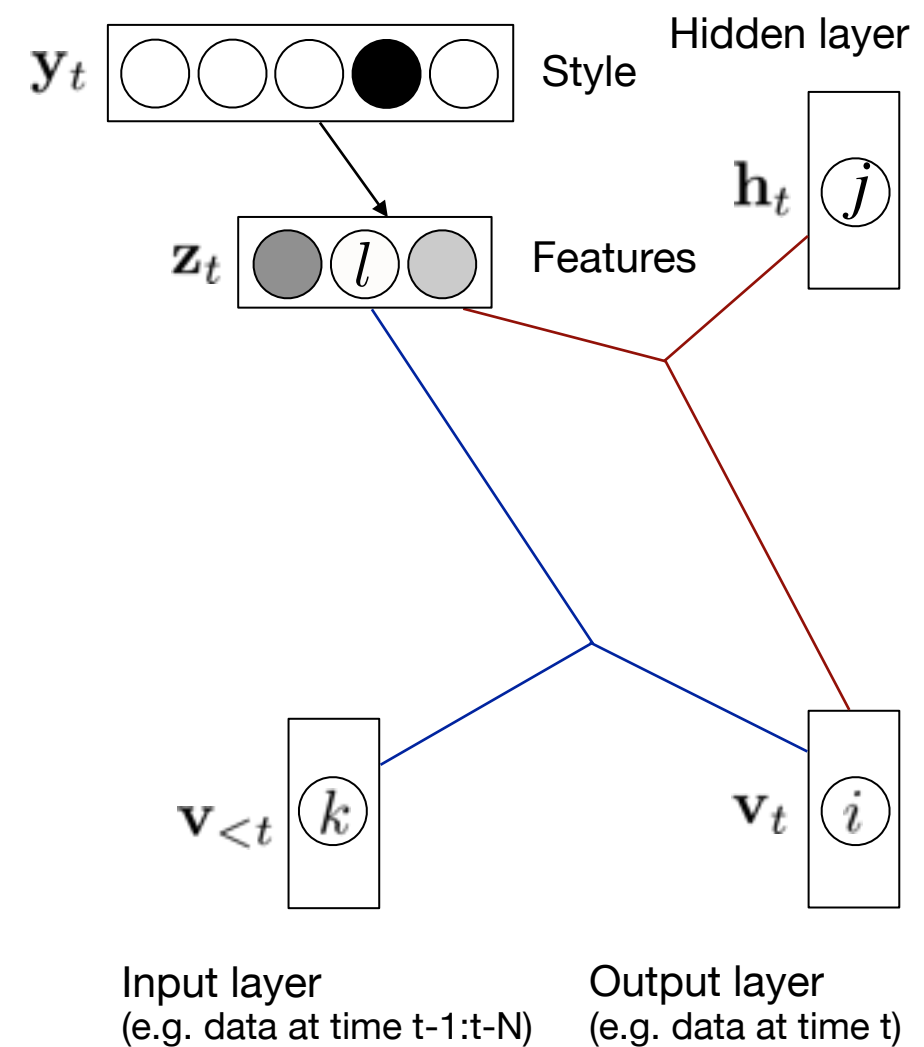
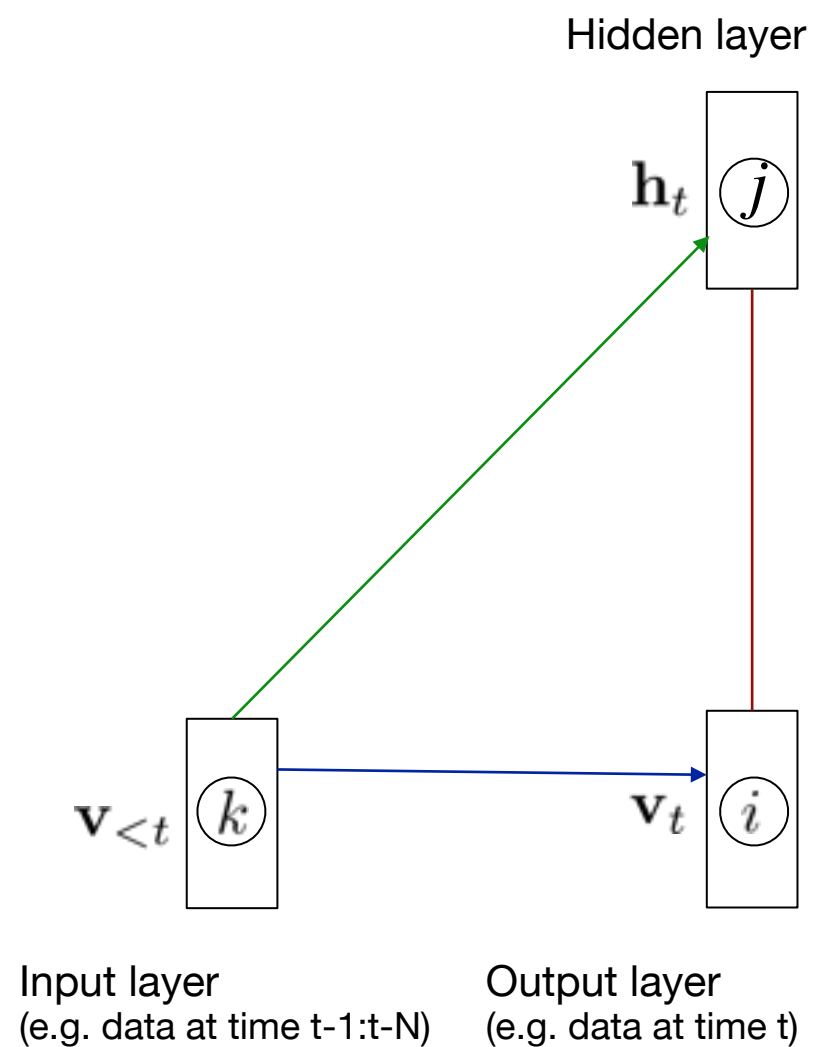


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Learning Representations of Sequences / G Taylor

SUPERVISED MODELING OF STYLE

(Taylor, Hinton and Roweis ICML 2009, JMLR 2011)

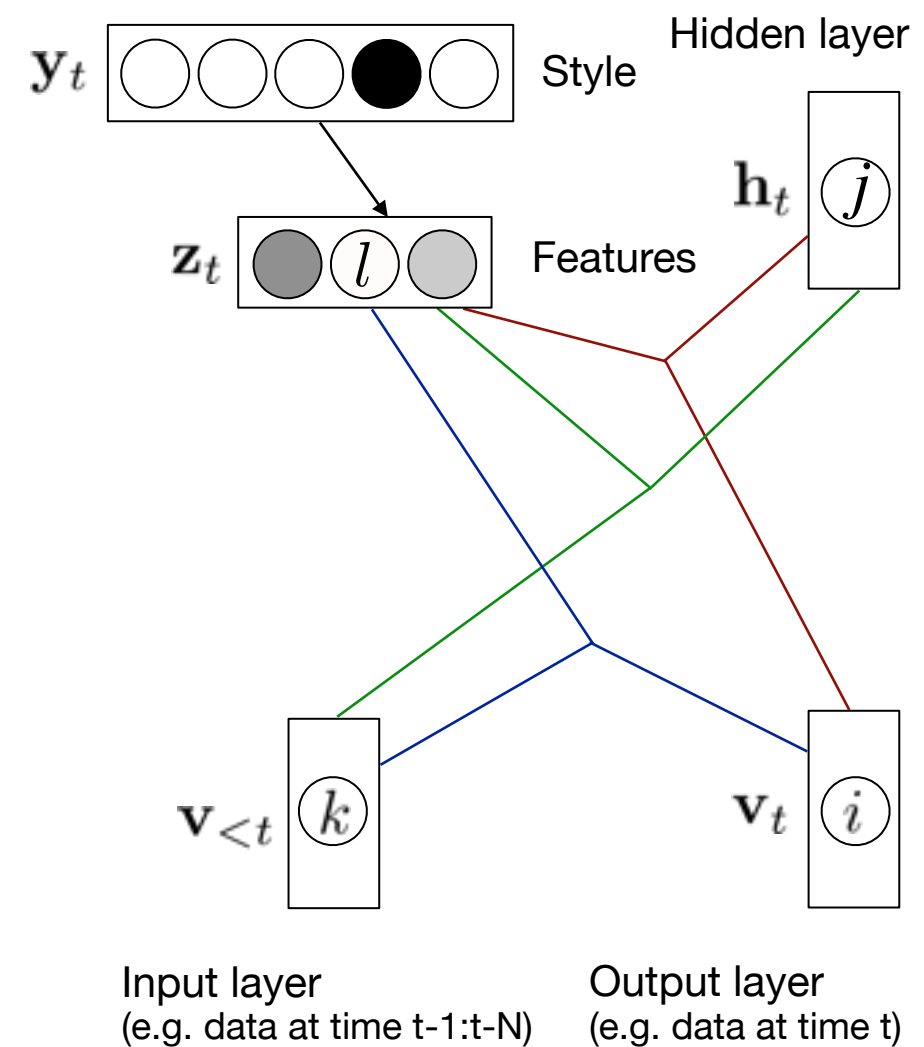
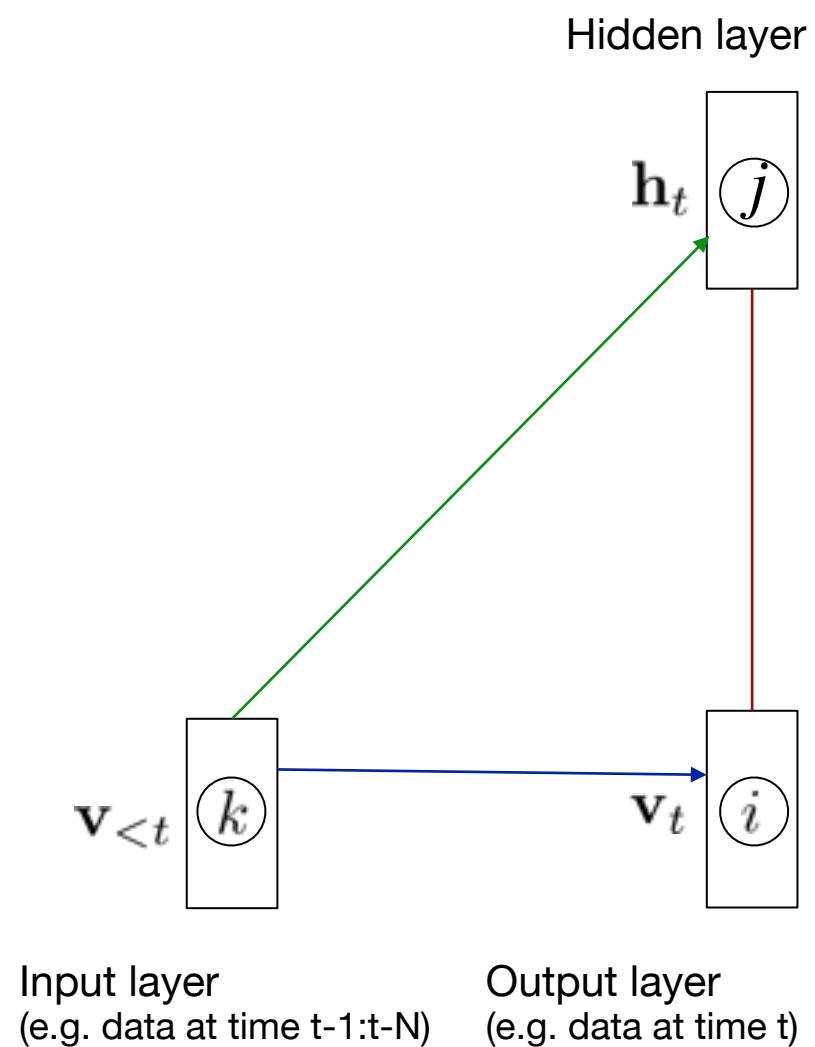


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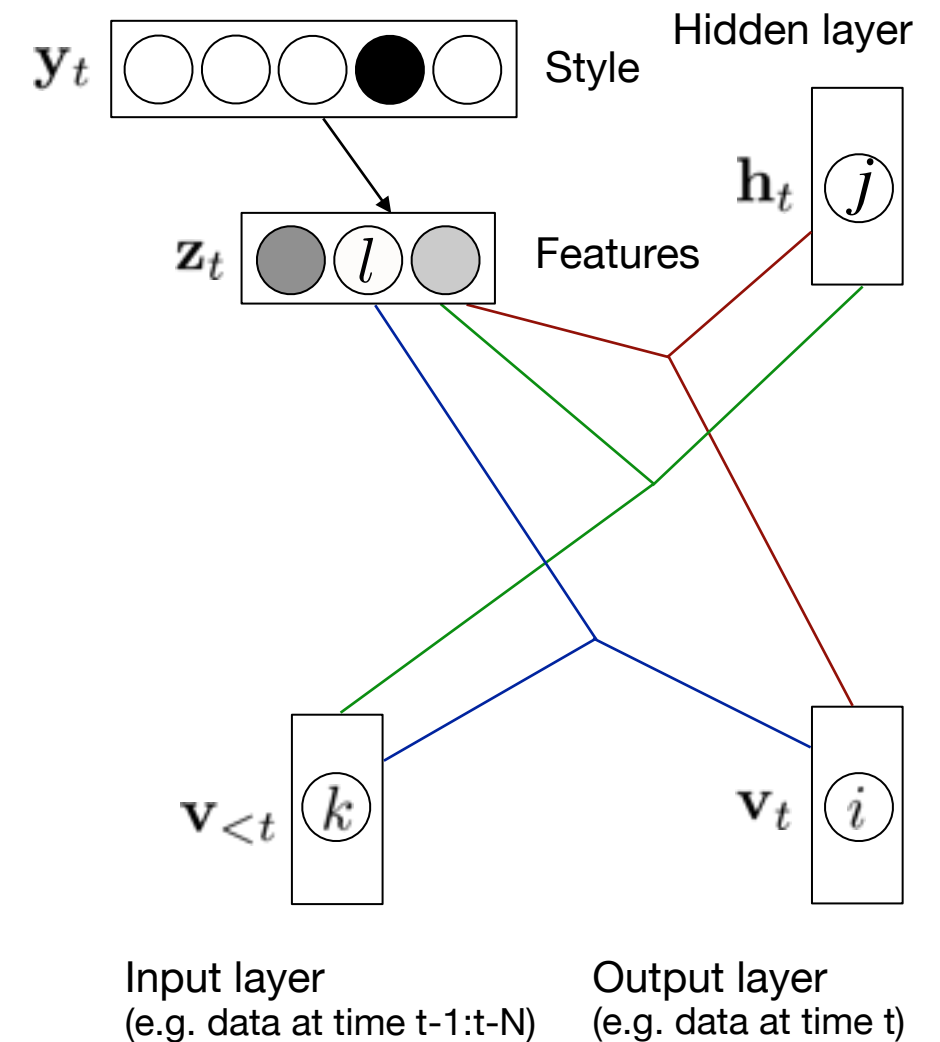


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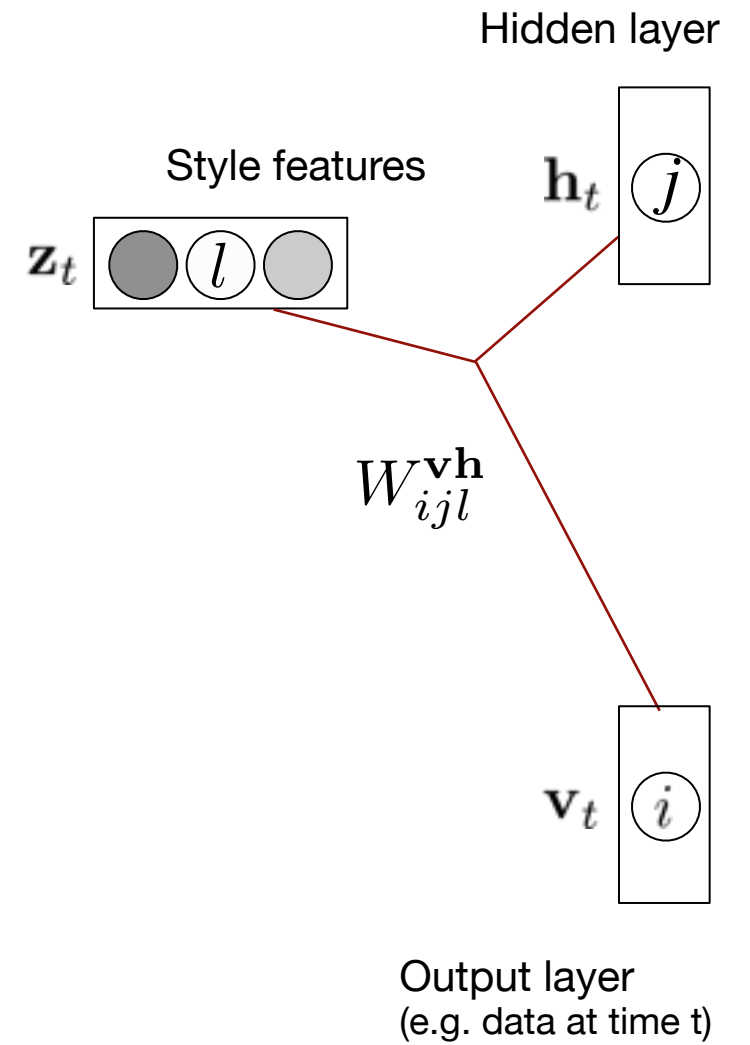
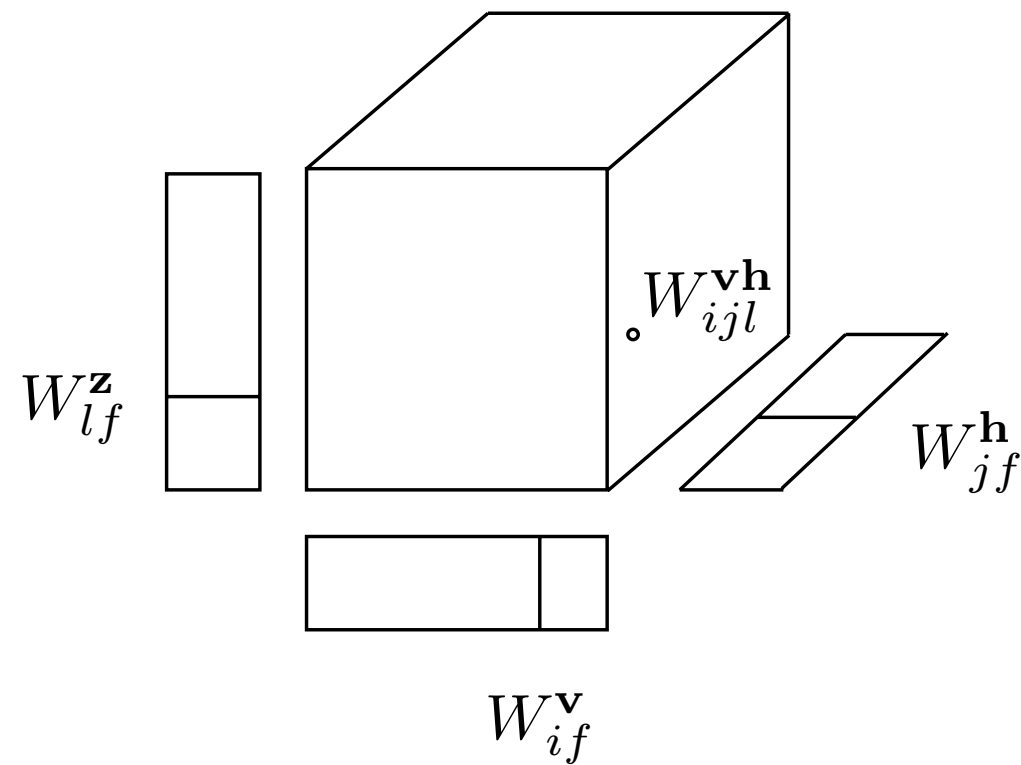
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OVERPARAMETERIZATION

- Note: weight Matrix $W^{\mathbf{v},\mathbf{h}}$ has been replaced by a tensor $W^{\mathbf{v},\mathbf{h},\mathbf{z}}$! (Likewise for other weights)
- The number of parameters is $O(N^3)$ - per group of weights
- More, if we want sparse, overcomplete hidden
- However, there is a simple yet powerful solution!



FACTORING



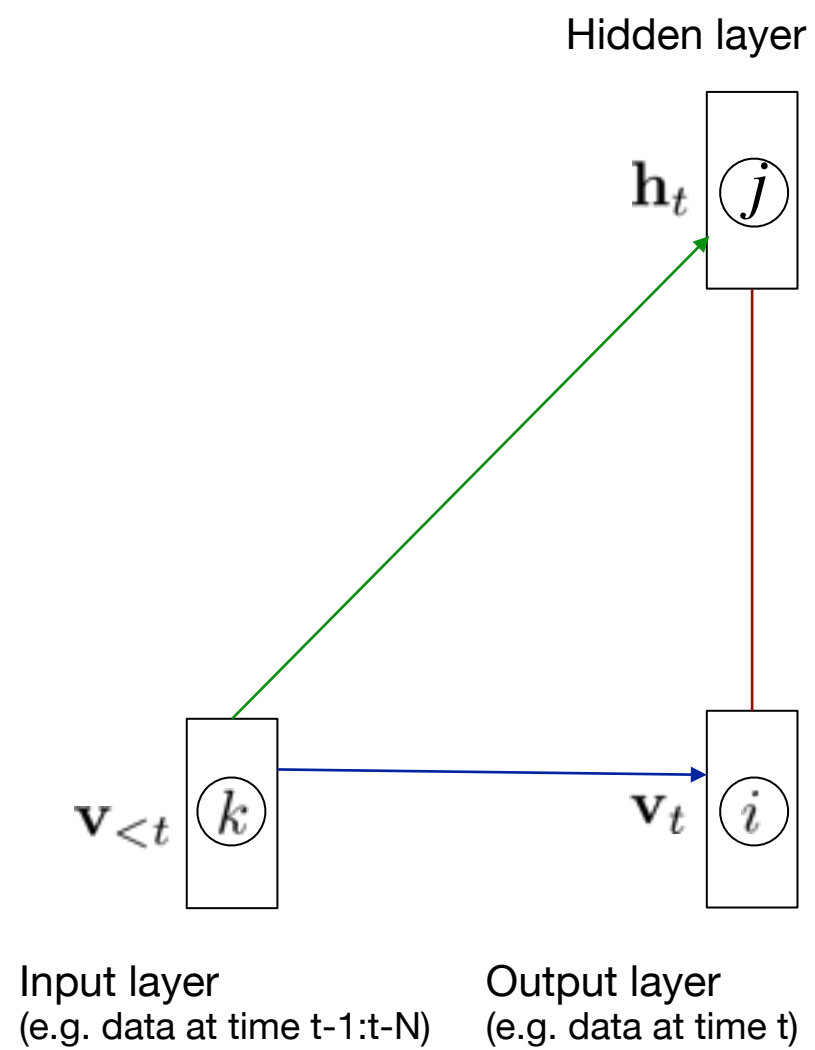
$$W_{ijl}^{vh} = \sum_f W_{if}^v W_{jf}^h W_{lf}^z$$

SUPERVISED MODELING OF STYLE

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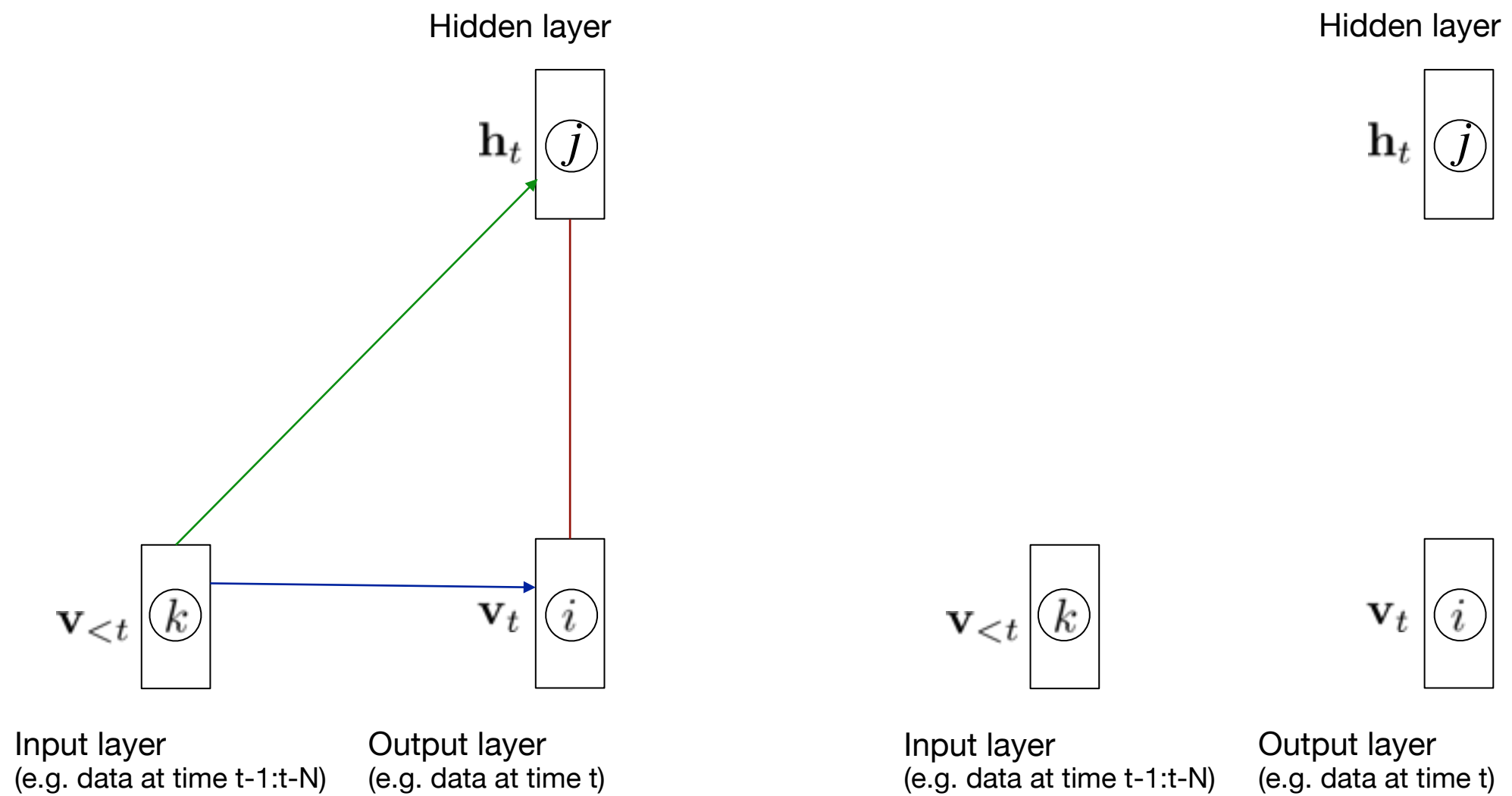


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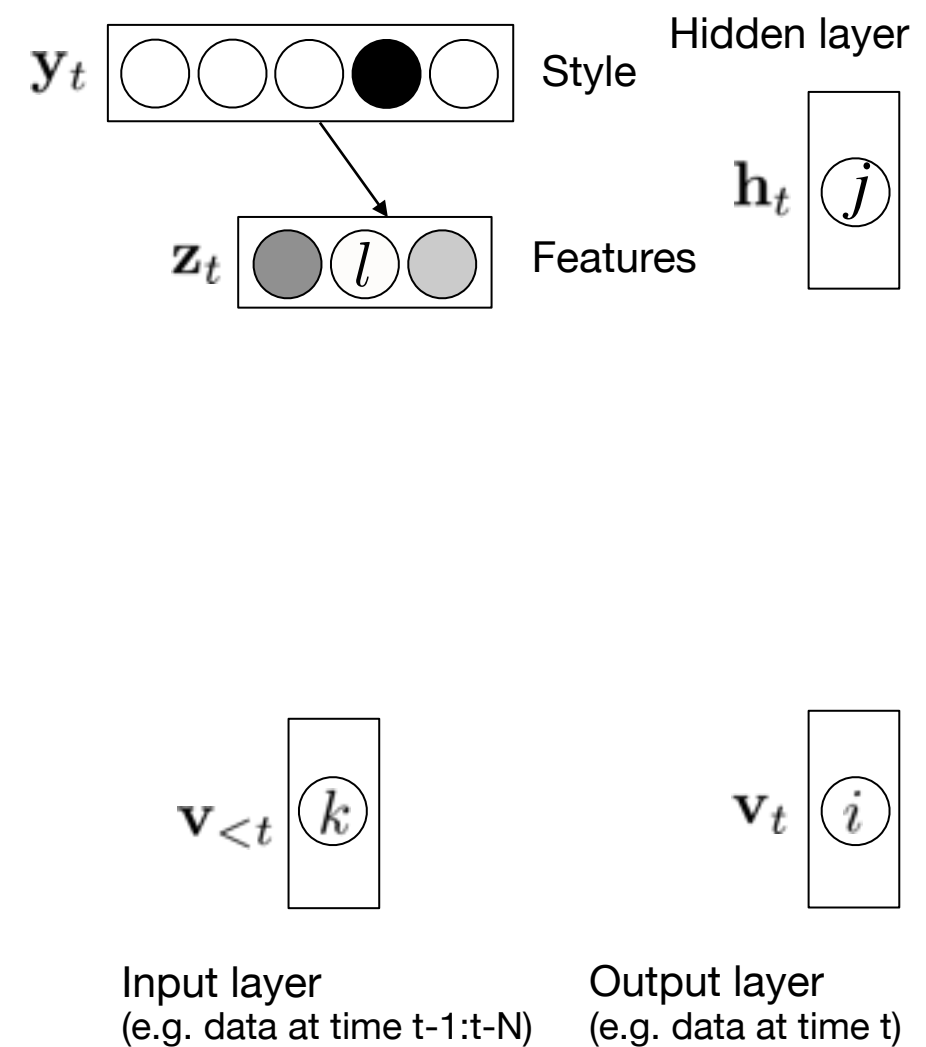
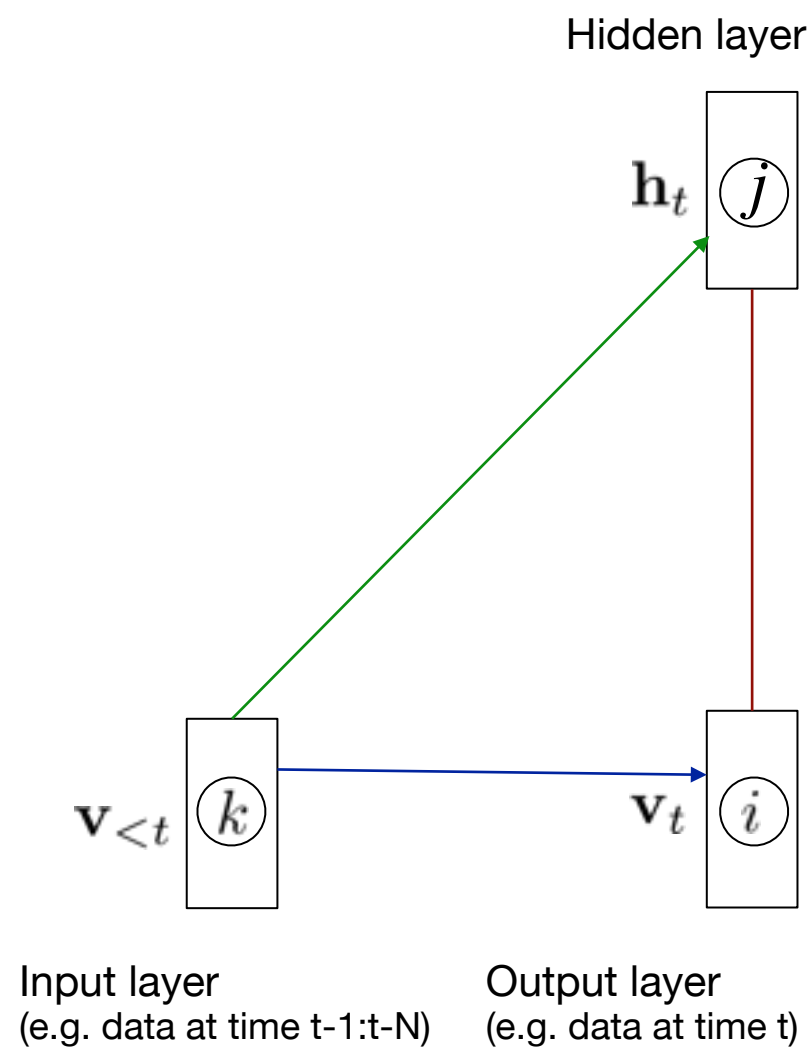


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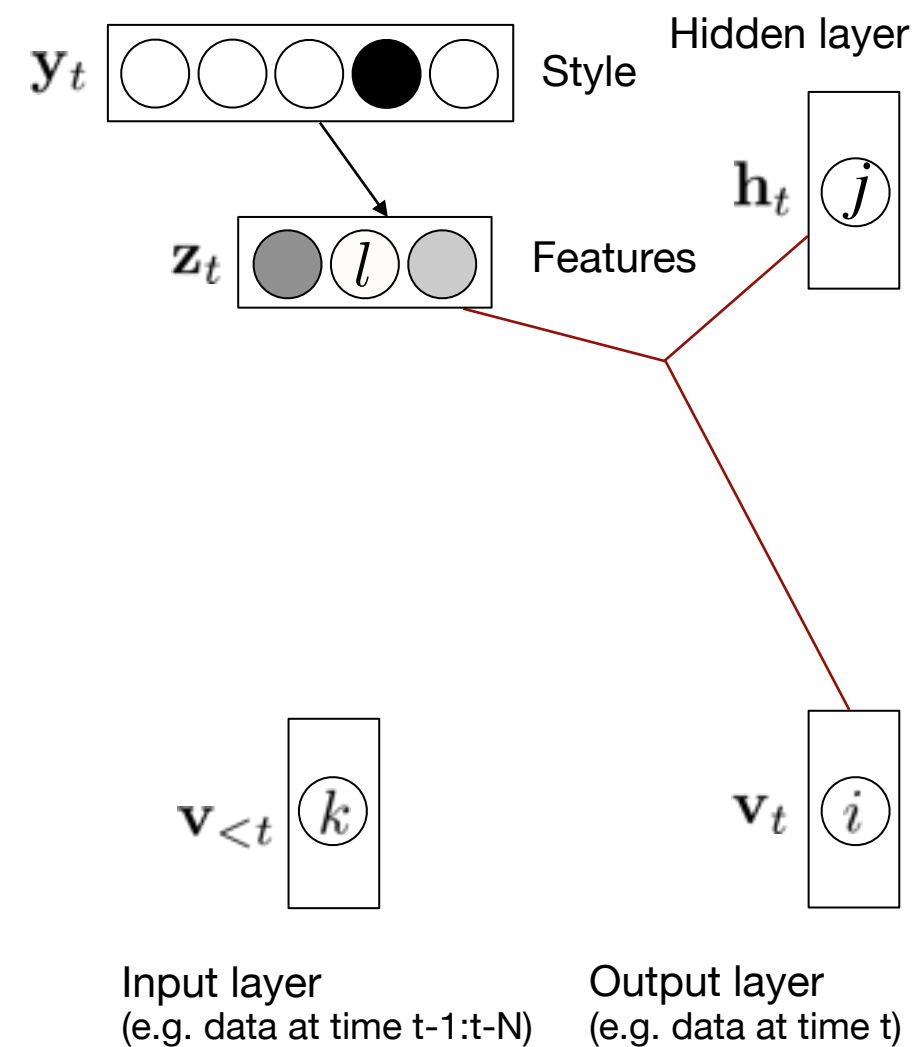
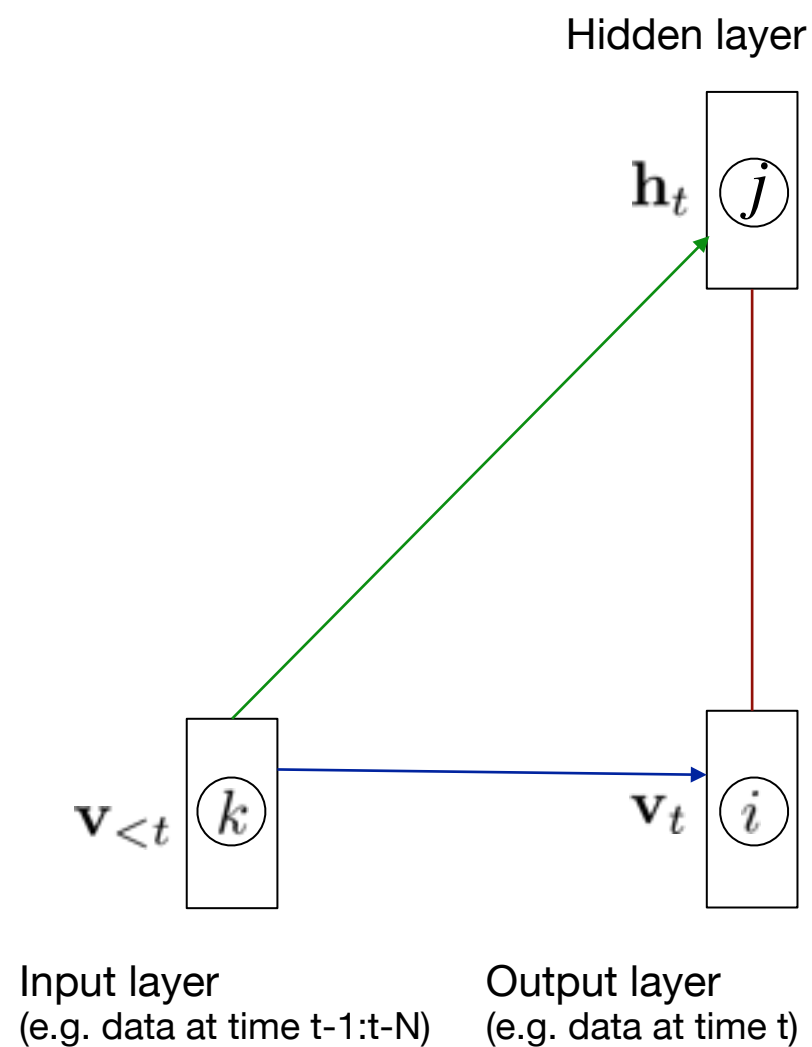


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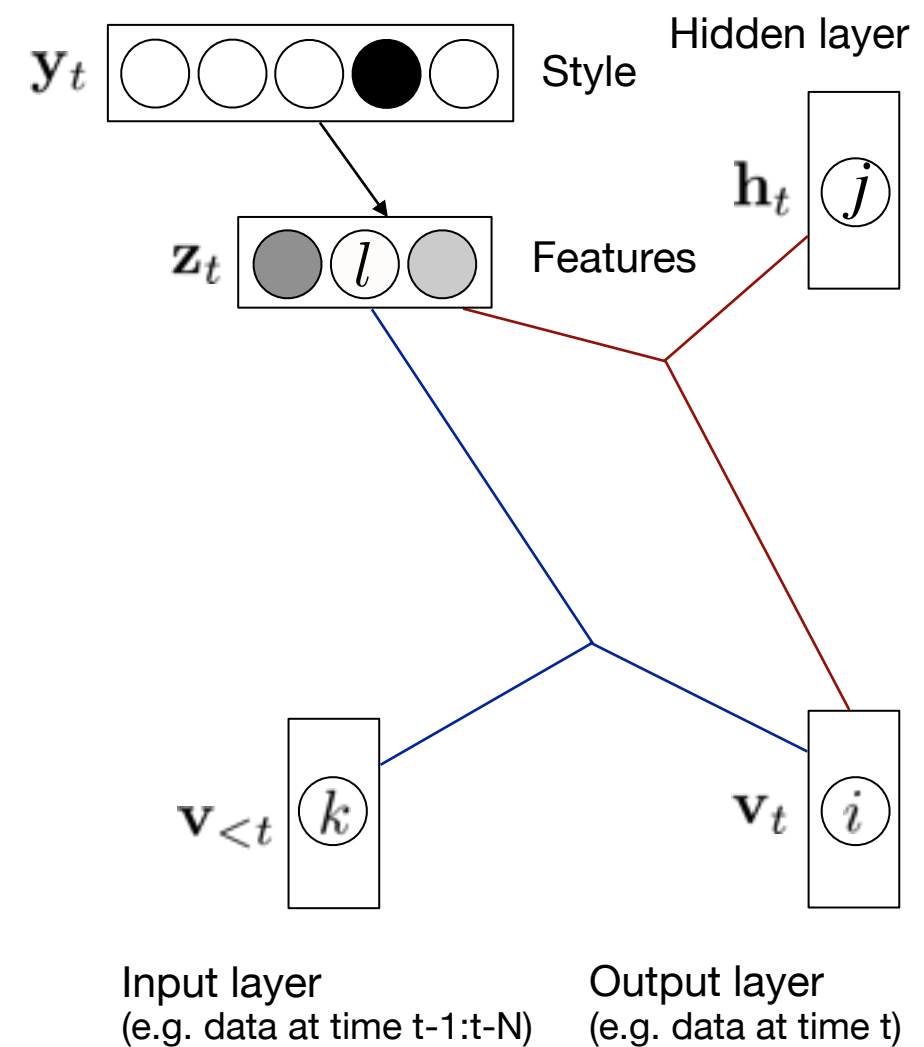
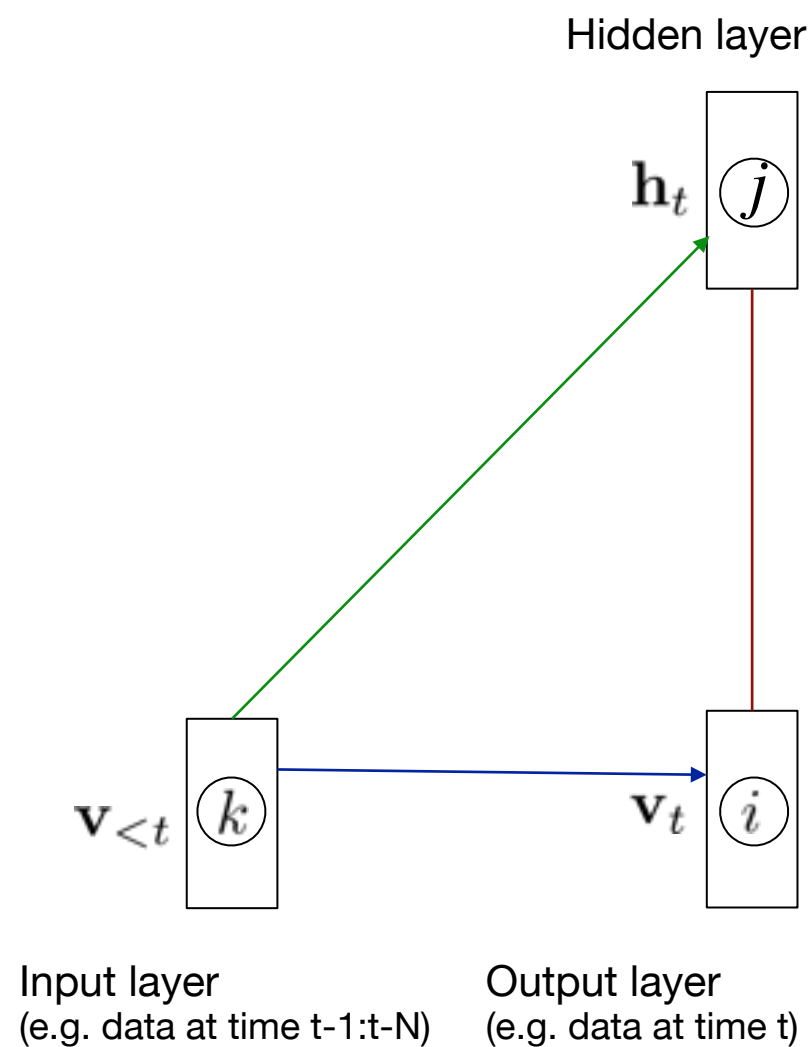


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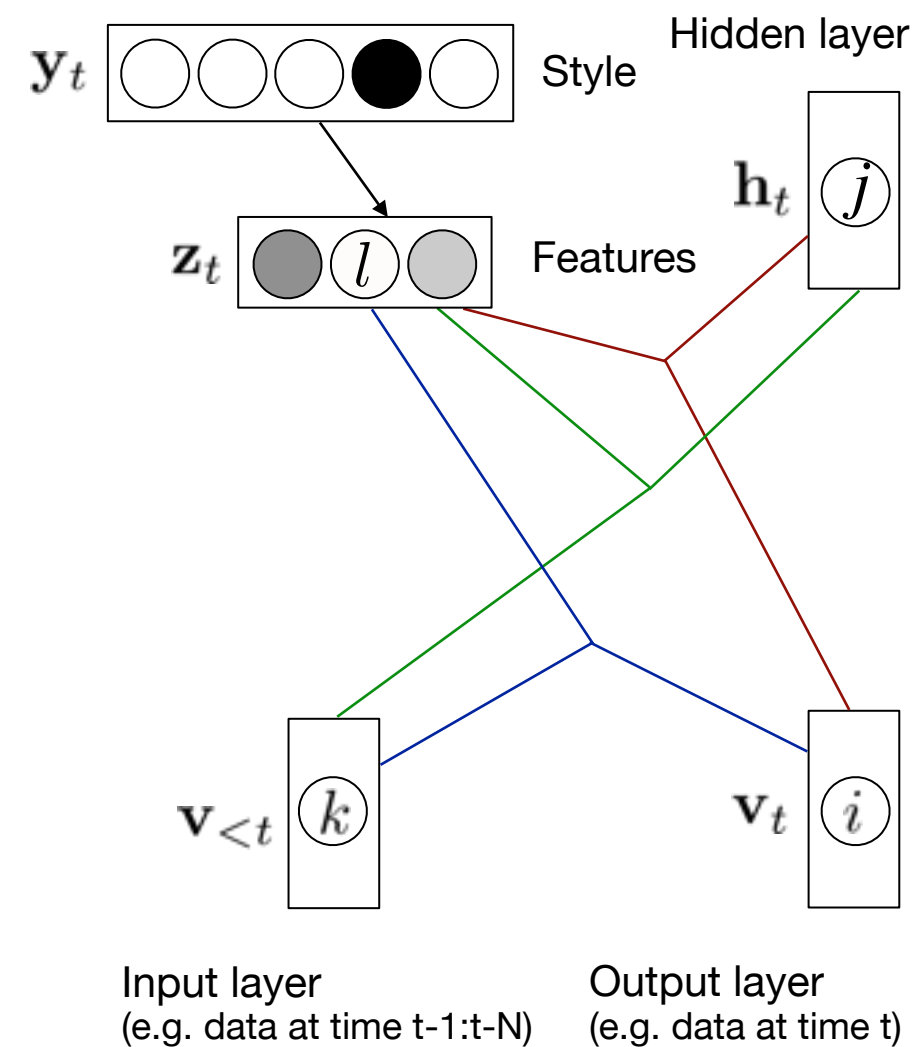
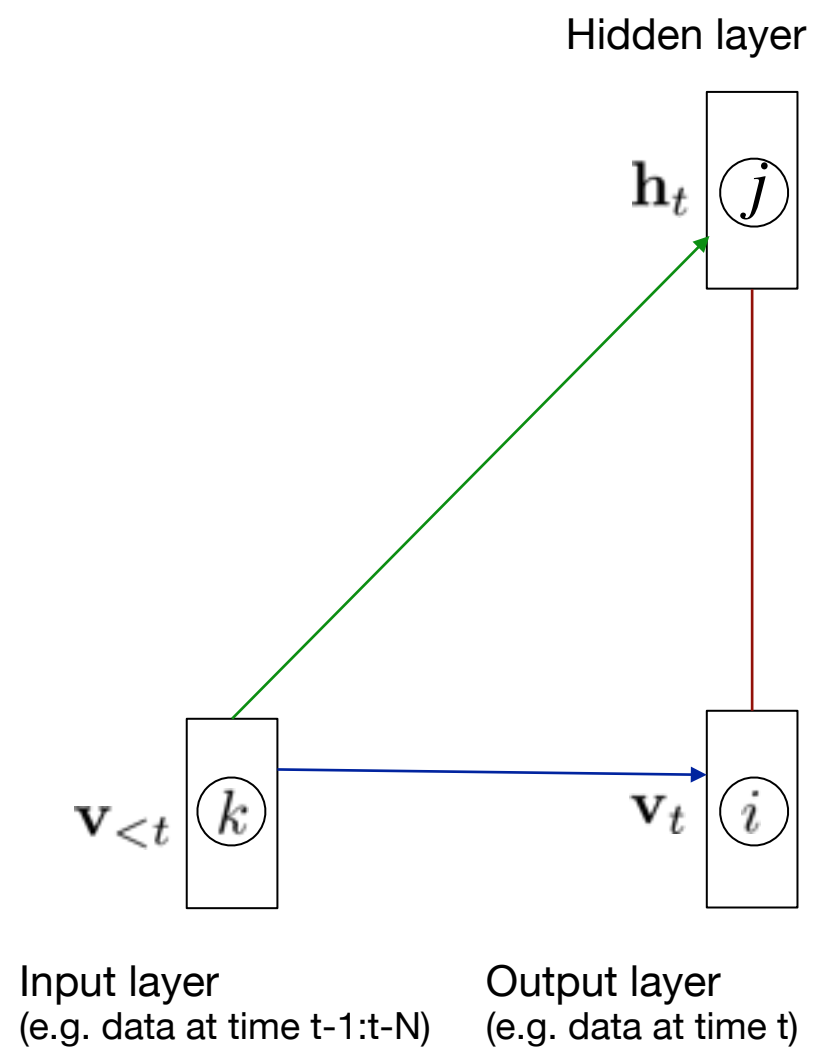


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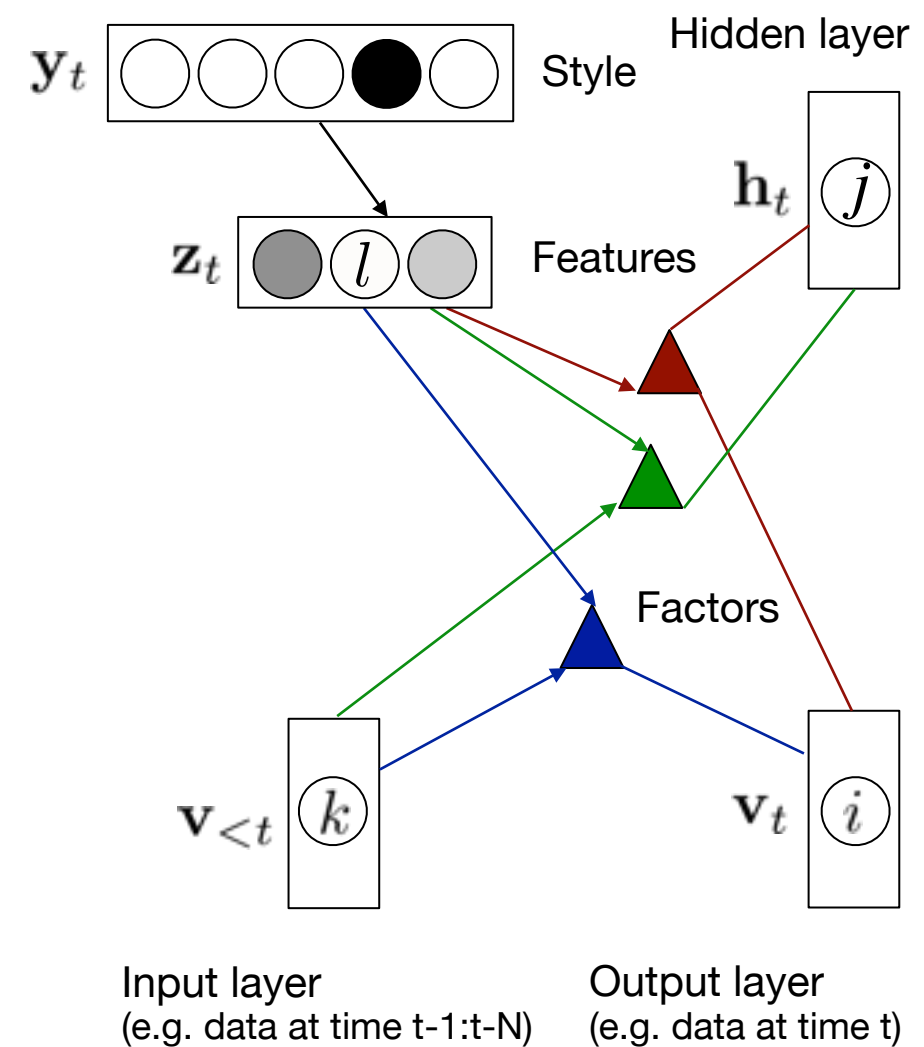
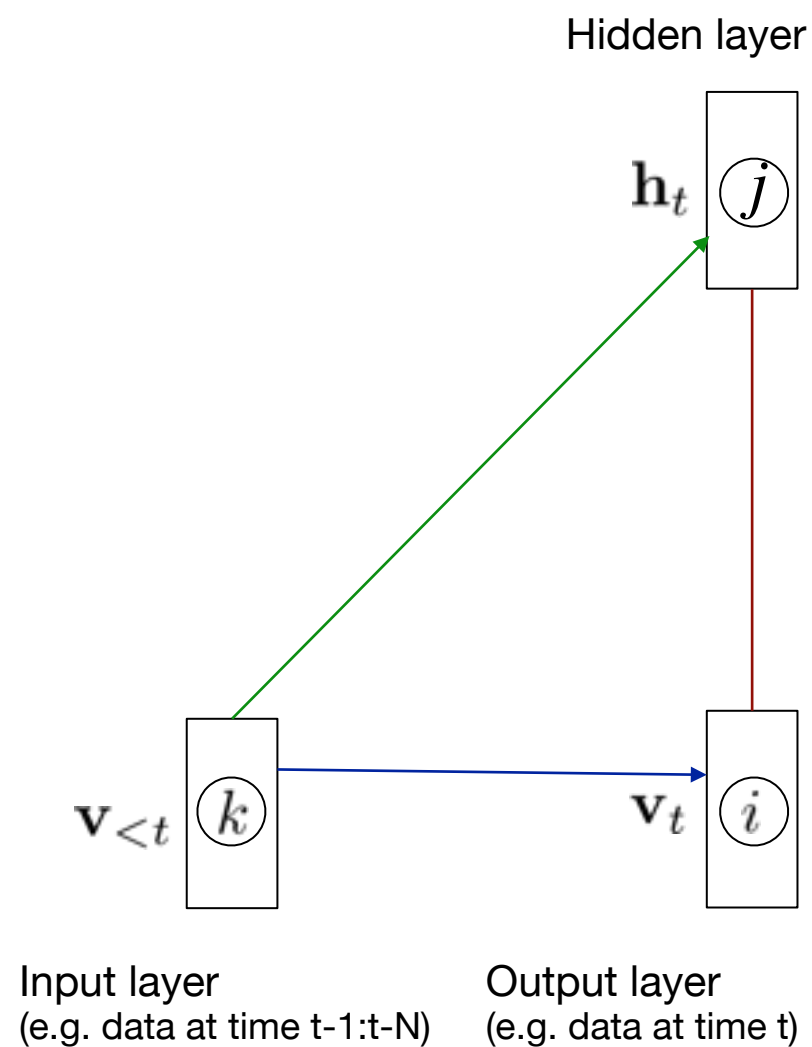


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SUPERVISED MODELING OF STYLE

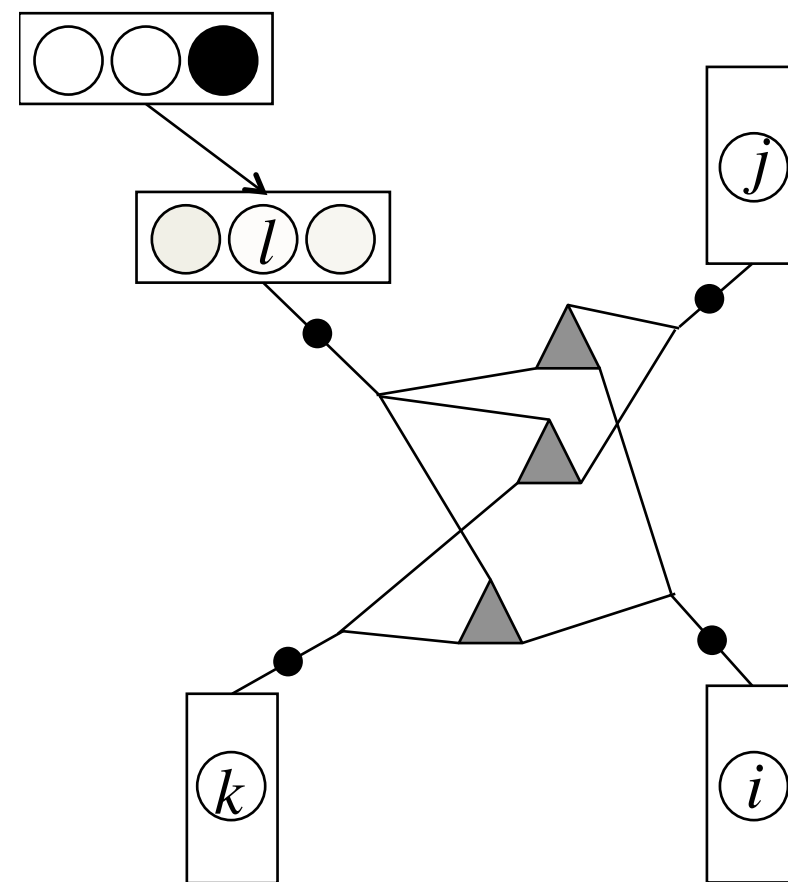
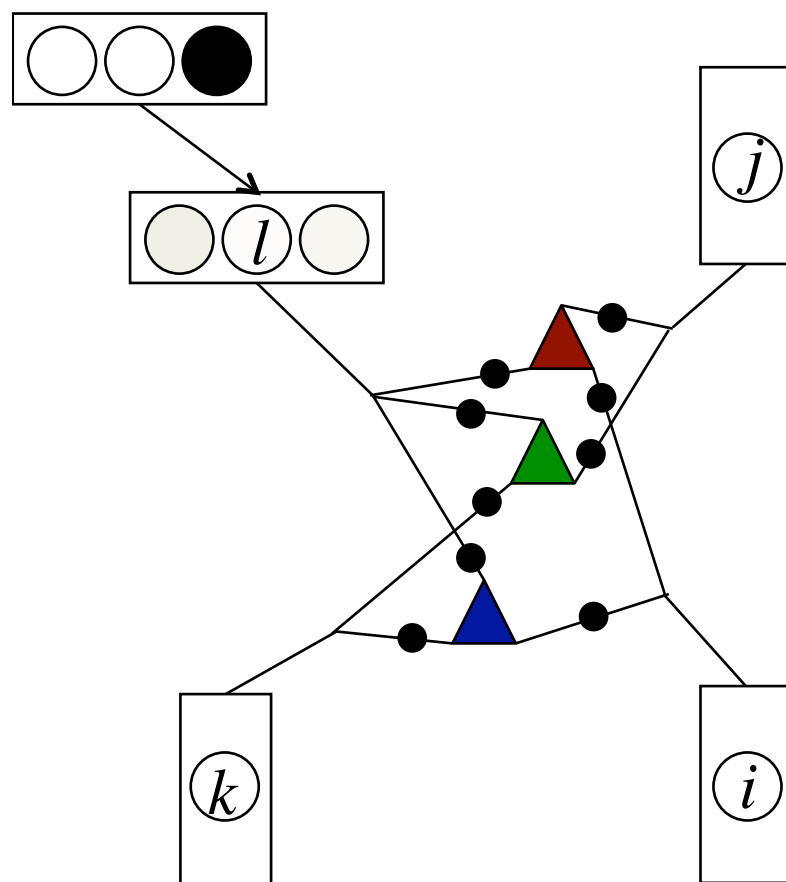
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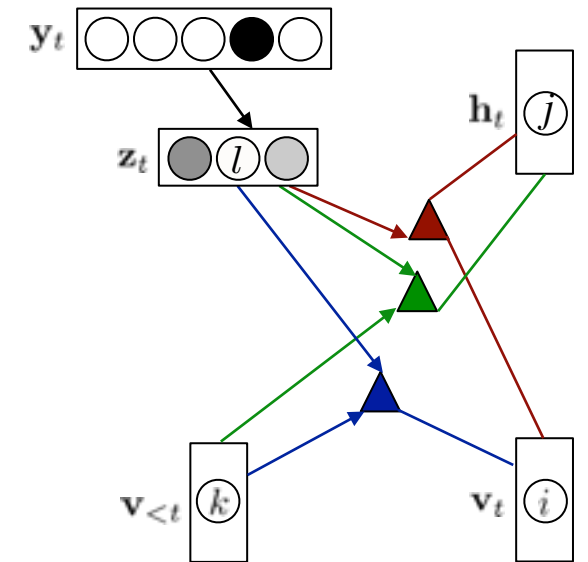
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PARAMETER SHARING



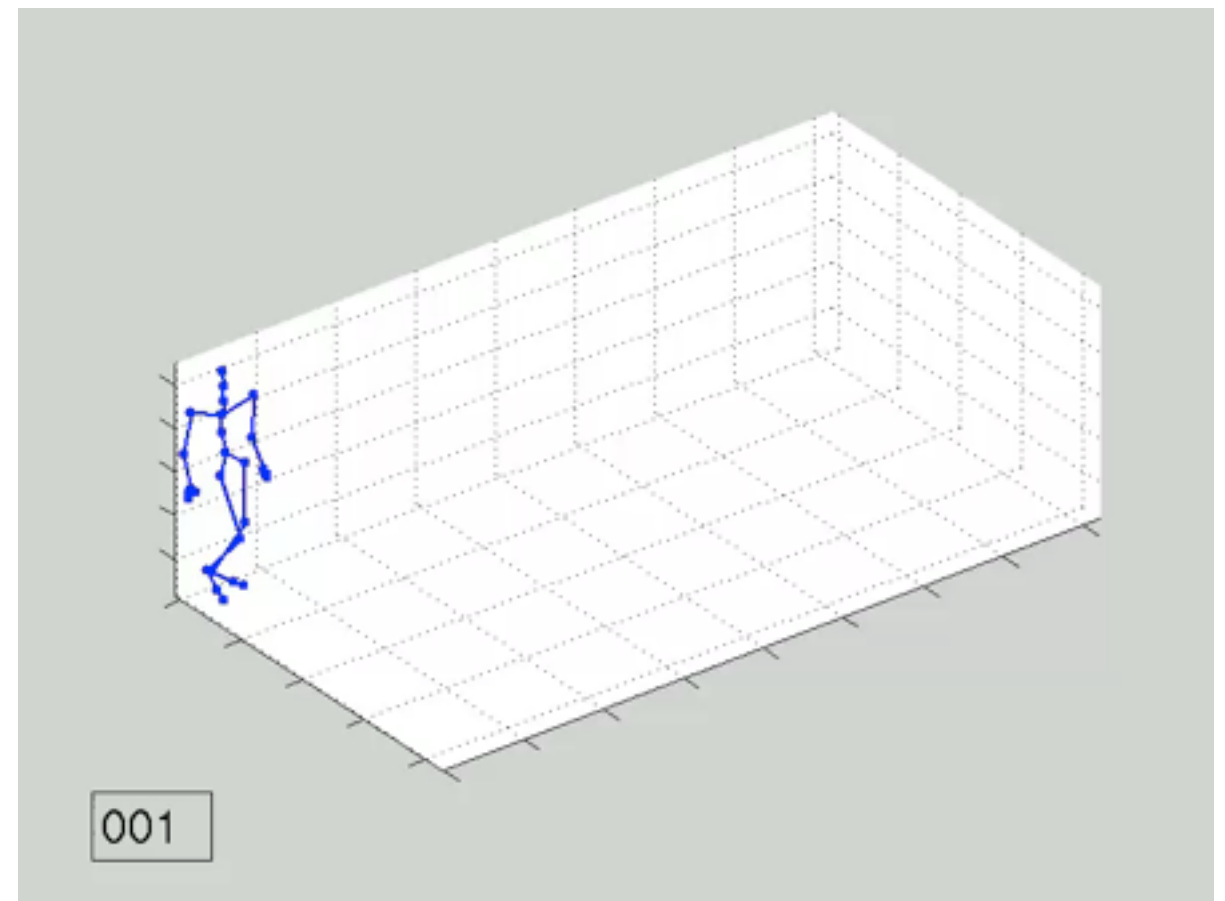
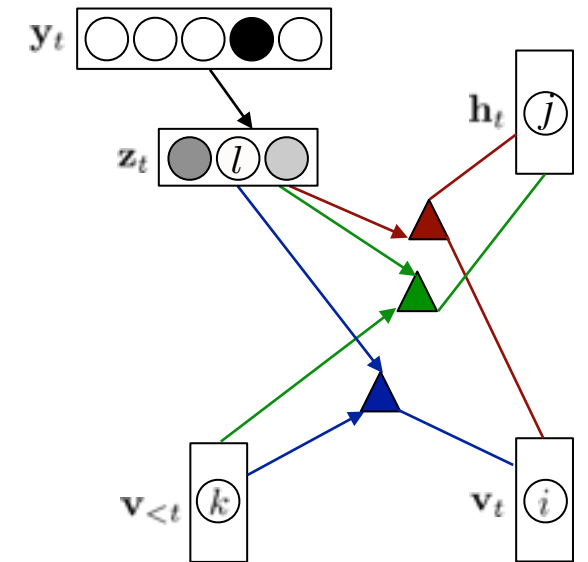
MOTION SYNTHESIS: FACTORED 3RD-ORDER CRBM

- Same 10-styles dataset
- 600 binary hidden units
- 3×200 deterministic factors
- 100 real-valued style features
- < 1 hour training on a modern workstation
- Synthesis is real-time



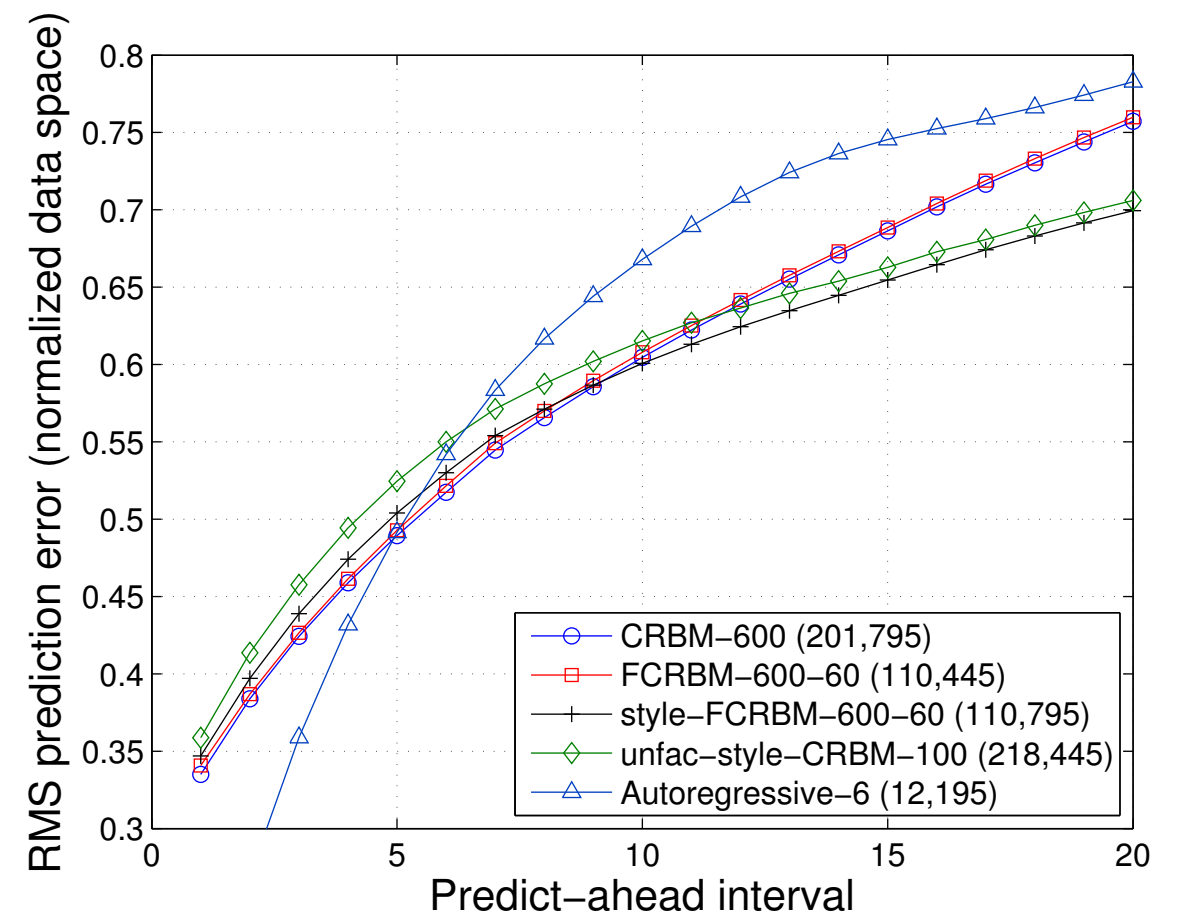
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QUANTITATIVE EVALUATION

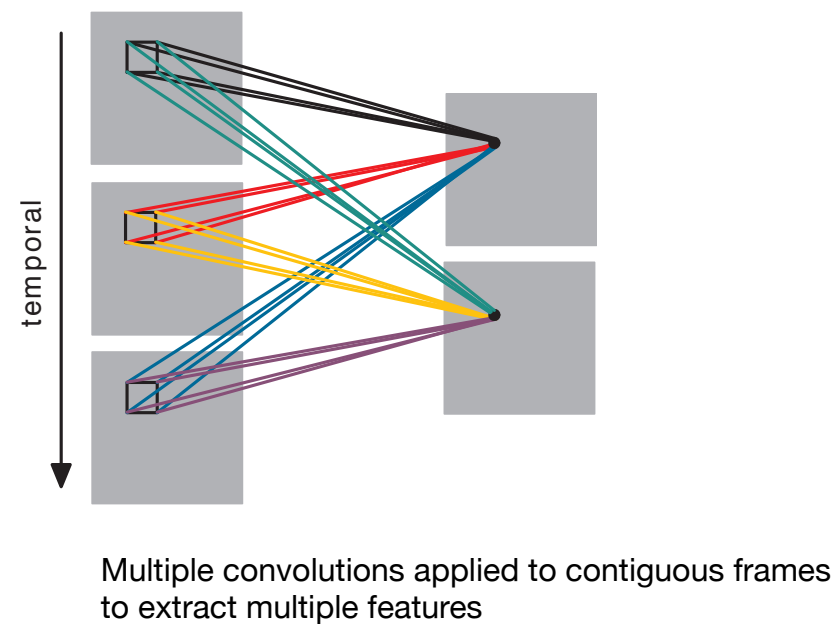
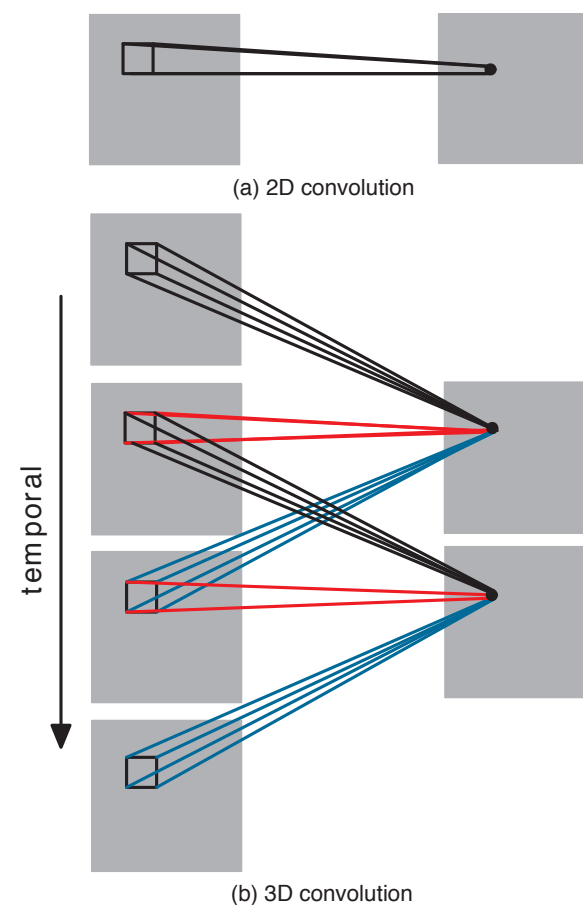
- Not computationally tractable to compute likelihoods
- Annealed Importance Sampling will not work in conditional models (open problem)
- Can evaluate predictive power (even though it has been trained generatively)
- Can also evaluate in denoising tasks



3D CONVNETS FOR ACTIVITY RECOGNITION

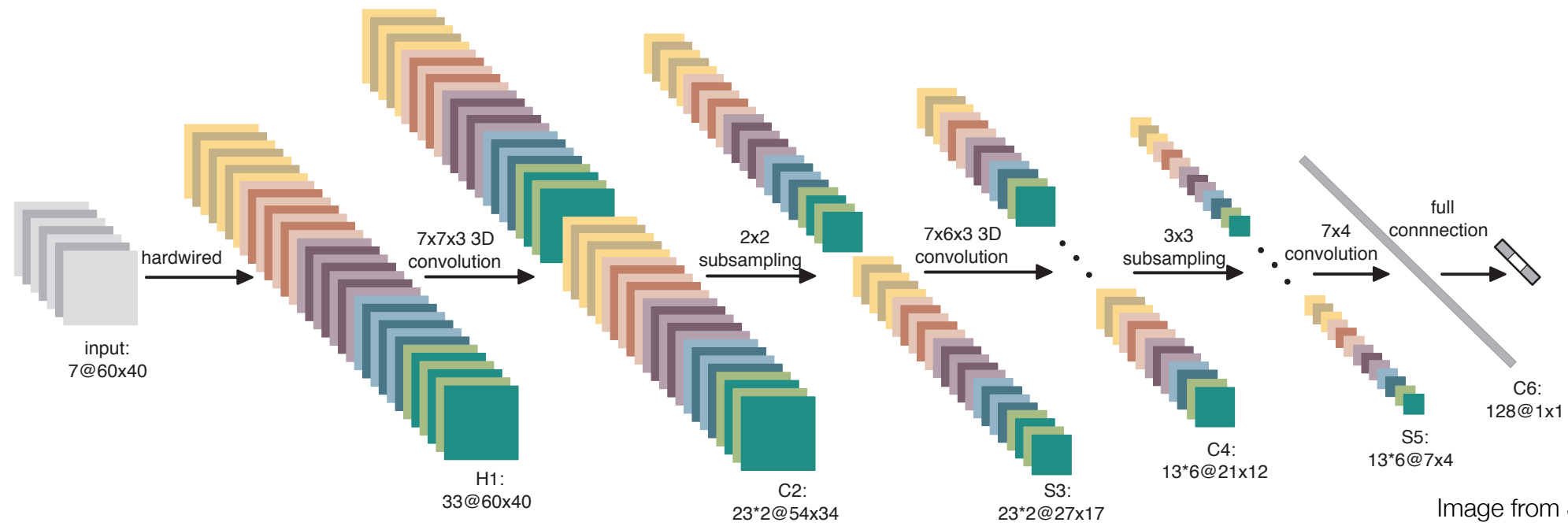
Shuiwang Ji, Wei Xu, Ming Yang, and Kai Yu (ICML 2010)

- One approach: treat video frames as still images (LeCun et al. 2005)
- Alternatively, perform 3D convolution so that discriminative features across space and time are captured



Images from Ji et al. 2010

3D CNN ARCHITECTURE



Hardwired to extract:
 1) grayscale
 2) grad-x
 3) grad-y
 4) flow-x
 5) flow-y

2 different 3D filters
 applied to each of 5
 blocks independently

Subsample
 spatially

3 different 3D filters
 applied to each of 5
 channels in 2 blocks

Two fully-
 connected
 layers

Action units

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Learning Representations of Sequences / G Taylor

3D CONVNET: DISCUSSION

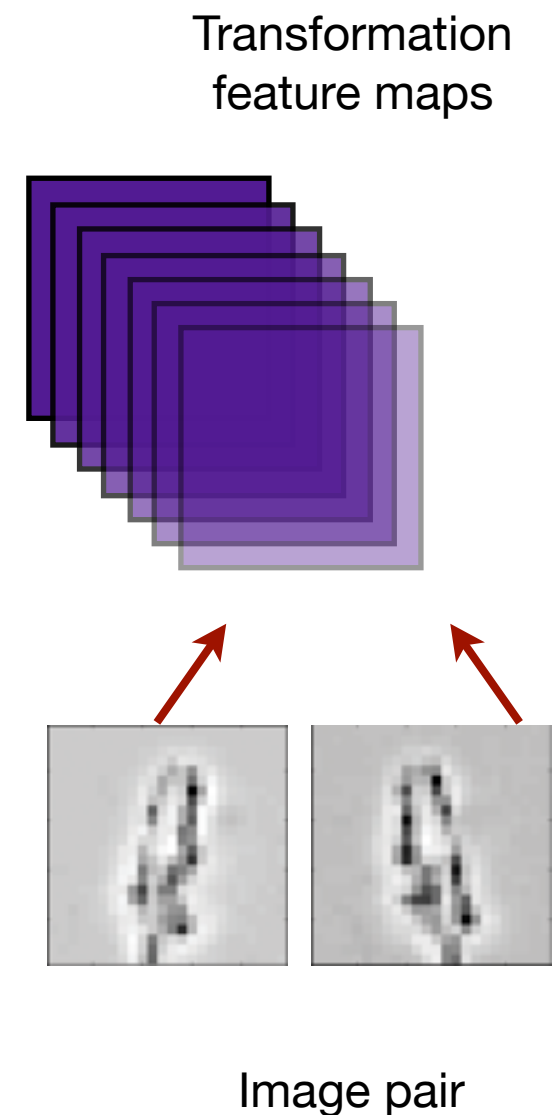
- Good performance on TRECVID surveillance data (*CellToEar*, *ObjectPut*, *Pointing*)
- Good performance on KTH actions (*box*, *handwave*, *handclap*, *jog*, *run*, *walk*)
- Still a fair amount of engineering: person detection (TRECVID), foreground extraction (KTH), hard-coded first layer



Image from Ji et al. 2010

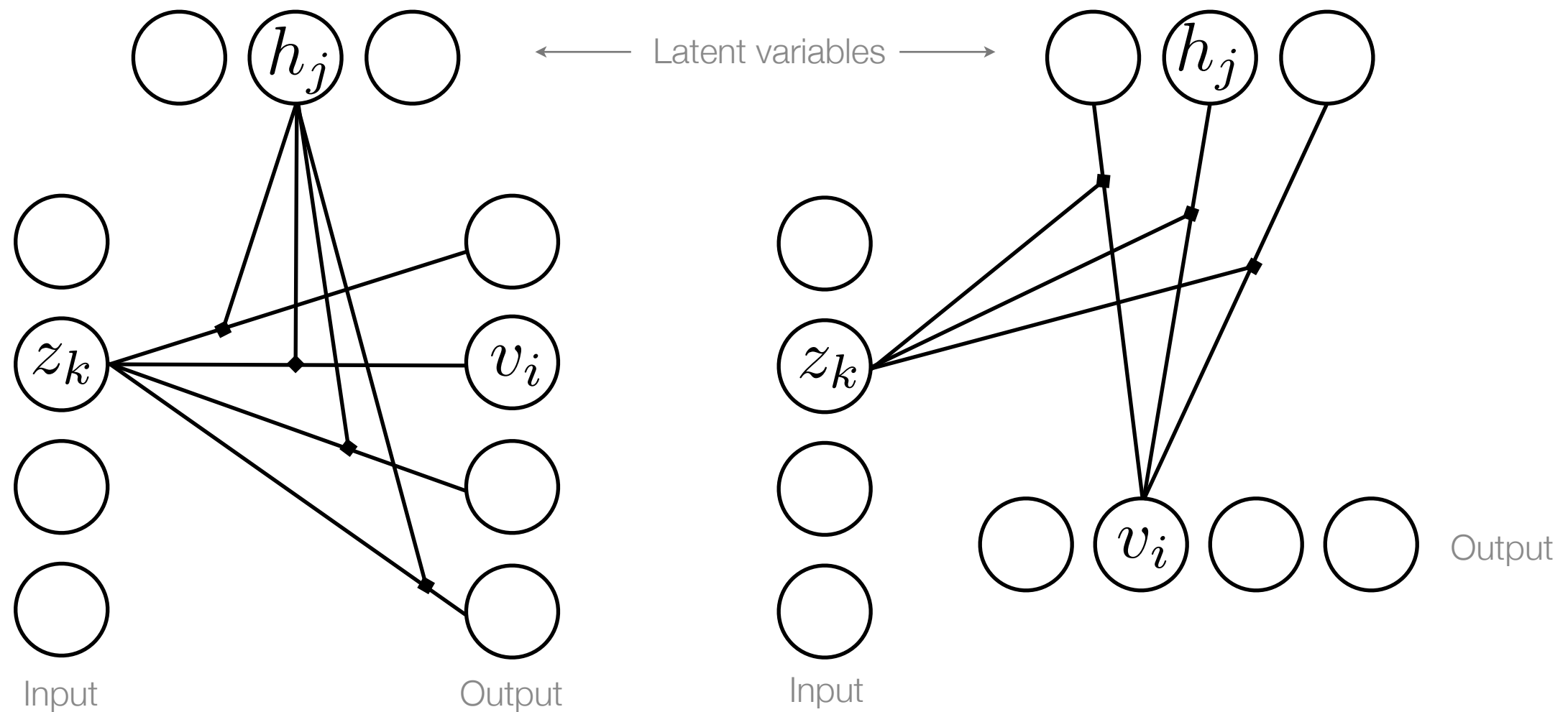
LEARNING FEATURES FOR VIDEO UNDERSTANDING

- Most work on unsupervised feature extraction has concentrated on **static images**
- We propose a model that extracts motion-sensitive features from **pairs of images**
- Existing attempts (e.g. Memisevic & Hinton 2007, Cadieu & Olshausen 2009) ignore the *pictorial* structure of the input
- Thus limited to modeling small image patches



GATED RESTRICTED BOLTZMANN MACHINES (GRBM)

Two views: Memisevic & Hinton (2007)



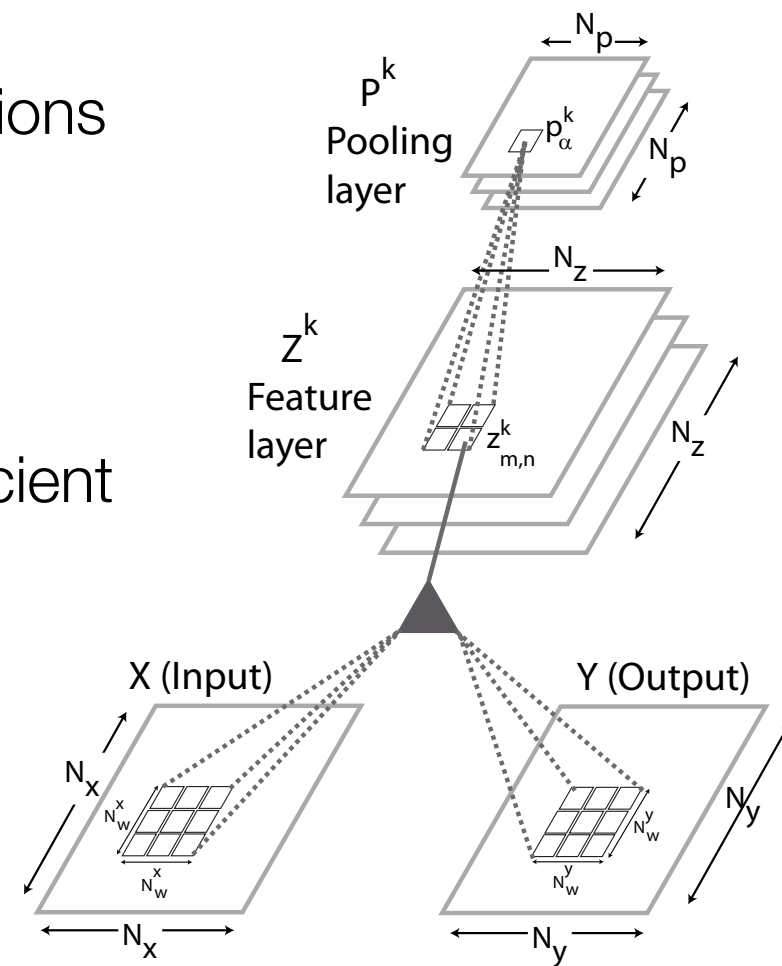
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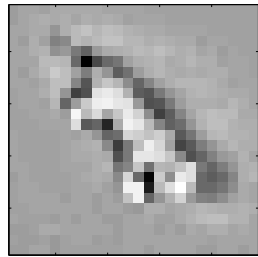
CONVOLUTIONAL GRBM

Graham Taylor, Rob Fergus, Yann LeCun, and Chris Bregler (ECCV 2010)

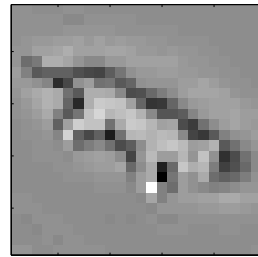
- Like the GRBM, captures third-order interactions
- Shares weights at all locations in an image
- As in a standard RBM, exact inference is efficient
- Inference and reconstruction are performed through convolution operations



MORE COMPLEX EXAMPLE OF “ANALOGIES”



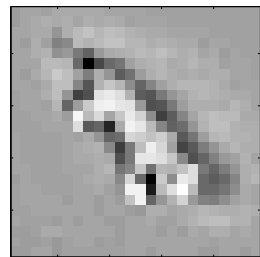
Input



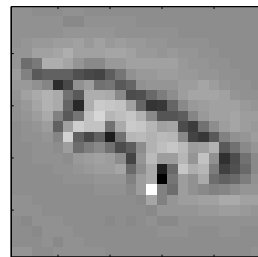
Output

MORE COMPLEX EXAMPLE OF “ANALOGIES”

Feature maps



Input

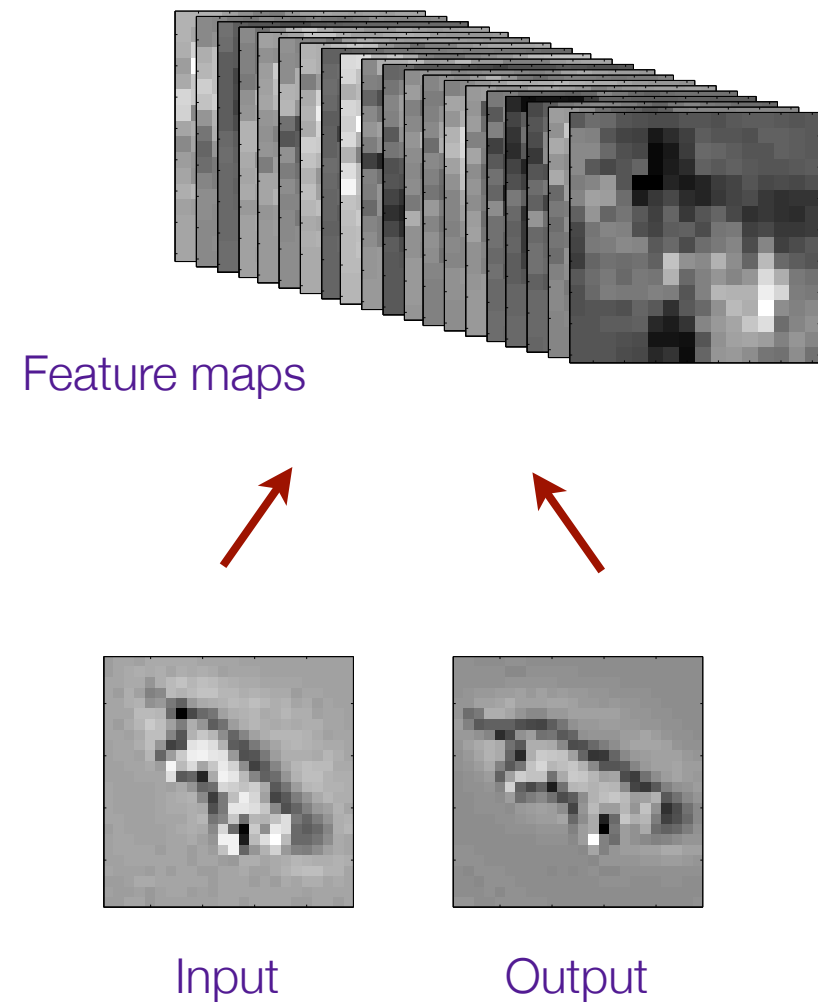


Output

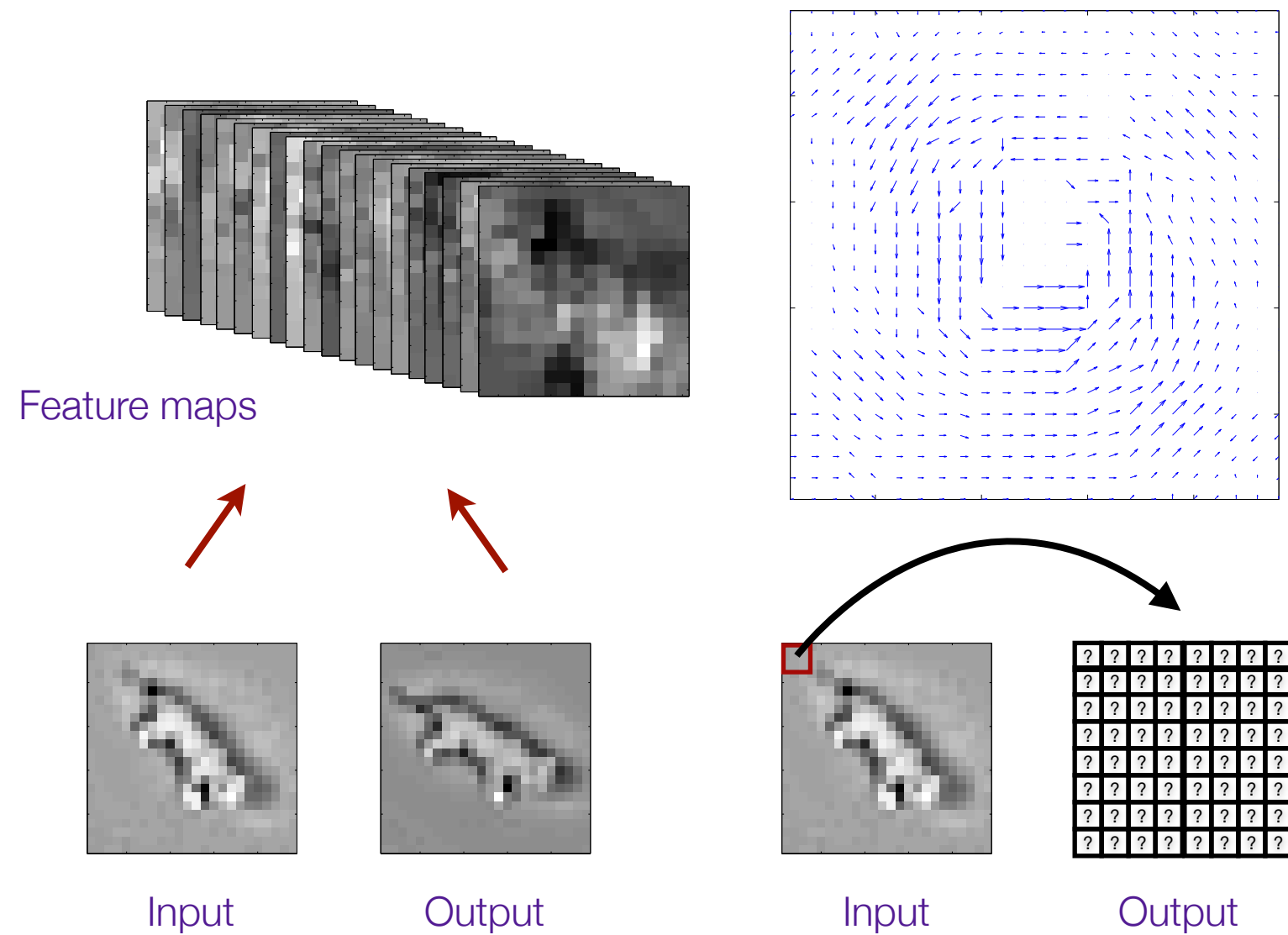
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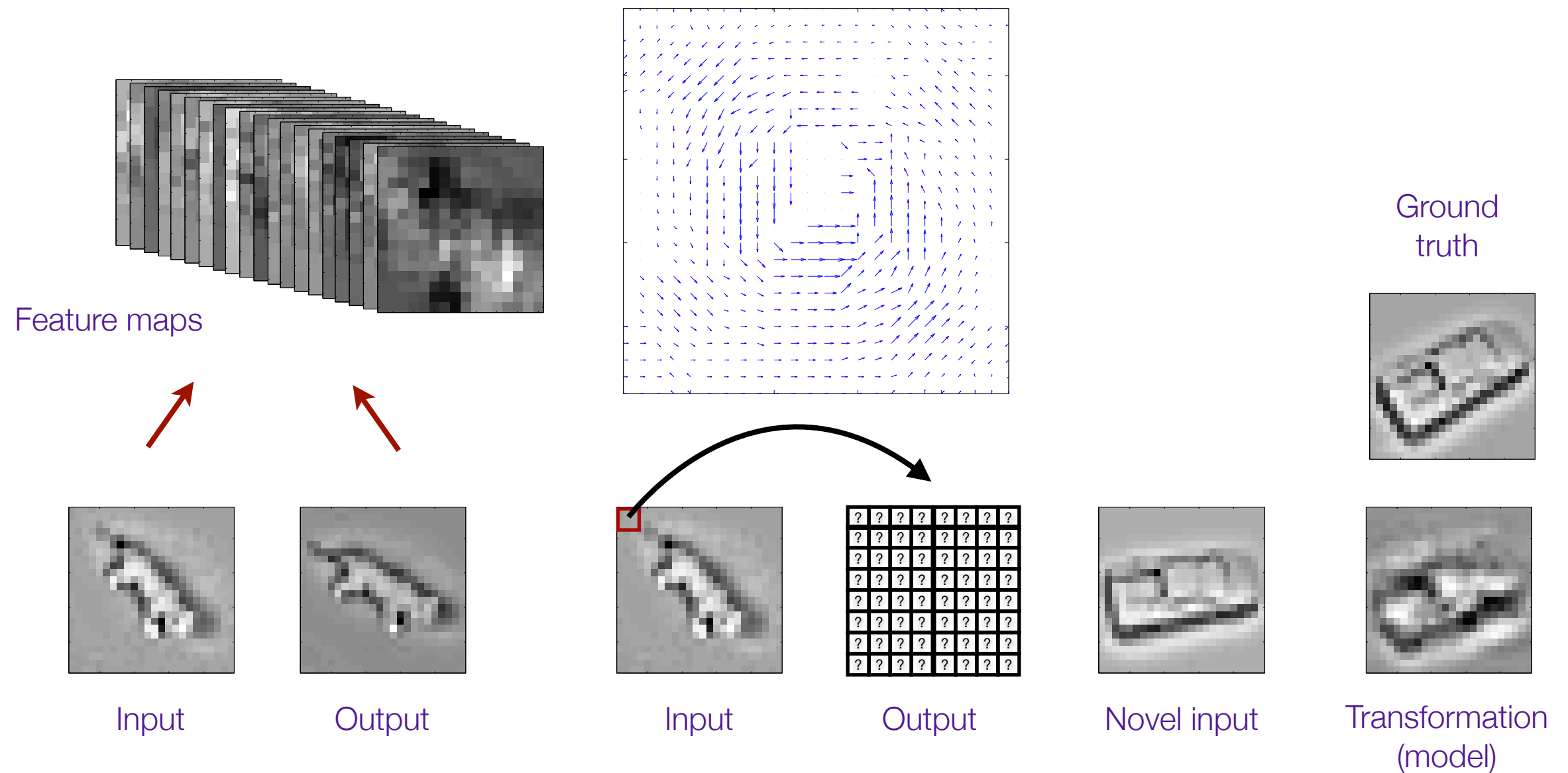
MORE COMPLEX EXAMPLE OF “ANALOGIES”



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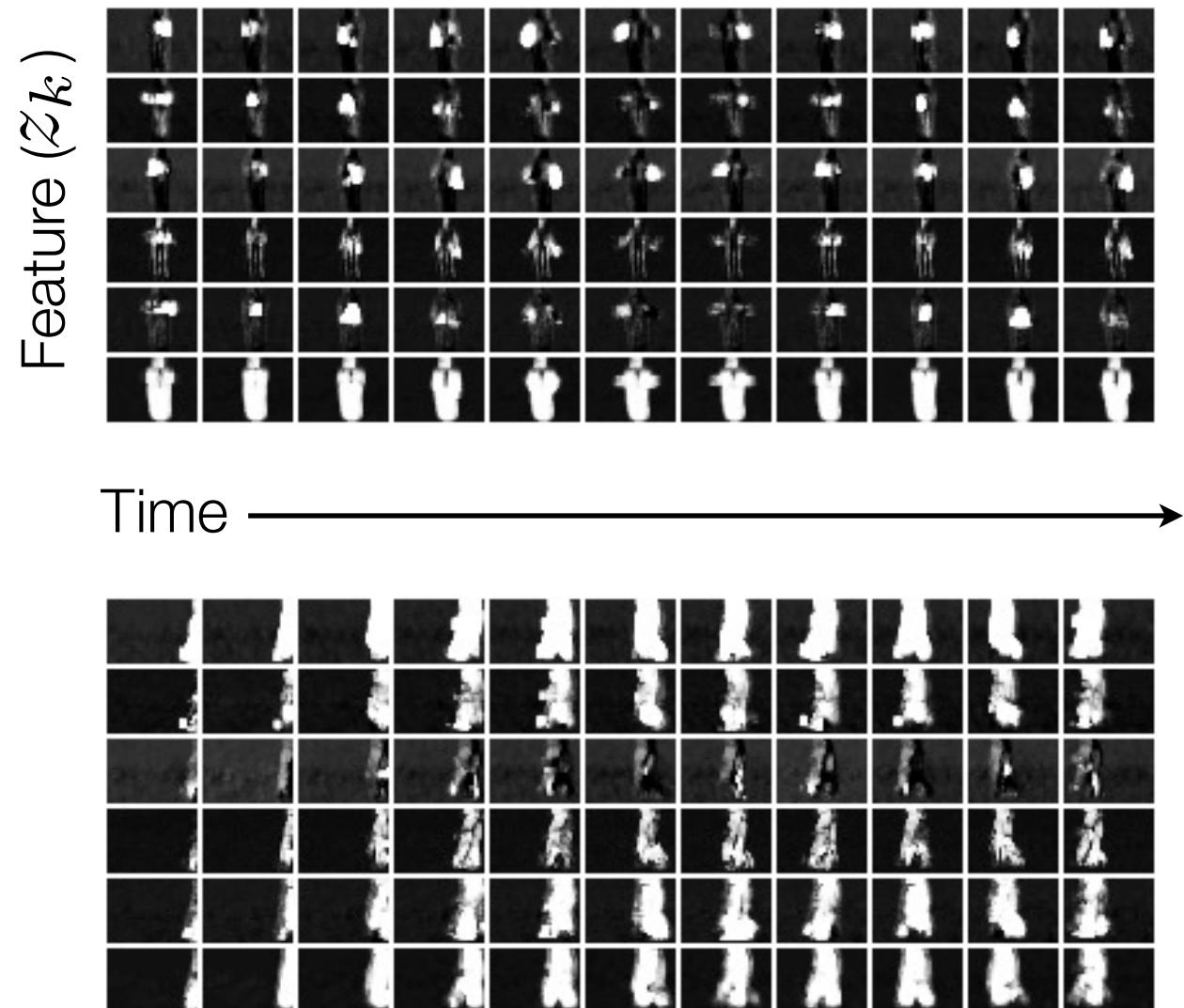


MORE COMPLEX EXAMPLE OF “ANALOGIES”



HUMAN ACTIVITY: KTH ACTIONS DATASET

- We learn 32 feature maps
- 6 are shown here
- KTH contains 25 subjects performing 6 actions under 4 conditions
- Only preprocessing is local contrast normalization
- Motion sensitive features (1,3)
- Edge features (4)
- Segmentation operator (6)



Hand clapping (above); Walking (below)

ACTIVITY RECOGNITION: KTH

Prior Art	Acc (%)	Convolutional architectures	Acc. (%)
HOG3D+KM+SVM	85.3	convGRBM+3D-convnet+logistic reg.	88.9
HOG/HOF+KM+SVM	86.1	convGRBM+3D convnet+MLP	90.0
HOG+KM+SVM	79.0	3D convnet+3D convnet+logistic reg.	79.4
HOF+KM+SVM	88.0	3D convnet+3D convnet+MLP	79.5

- Compared to methods that do not use explicit interest point detection
- State of the art: 92.1% (Laptev et al. 2008) 93.9% (Le et al. 2011)
- Other reported result on 3D convnets uses a different evaluation scheme

ACTIVITY RECOGNITION: HOLLYWOOD 2

- 12 classes of human action extracted from 69 movies (20 hours)
- Much more realistic and challenging than KTH (changing scenes, zoom, etc.)
- Performance is evaluated by mean average precision over classes

Method	Average Prec.
<i>Prior Art (Wang et al. survey 2009):</i>	
HOG3D+KM+SVM	45.3
HOG/HOF+KM+SVM	47.4
HOG+KM+SVM	39.4
HOF+KM+SVM	45.5
<i>Our method:</i>	
GRBM+SC+SVM	46.8



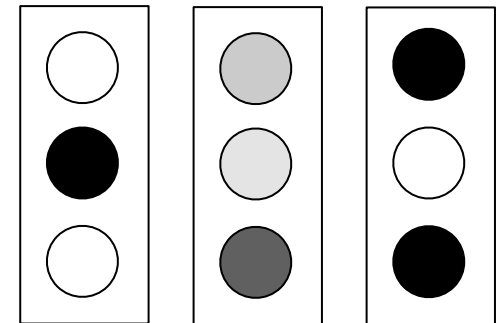
SUMMARY

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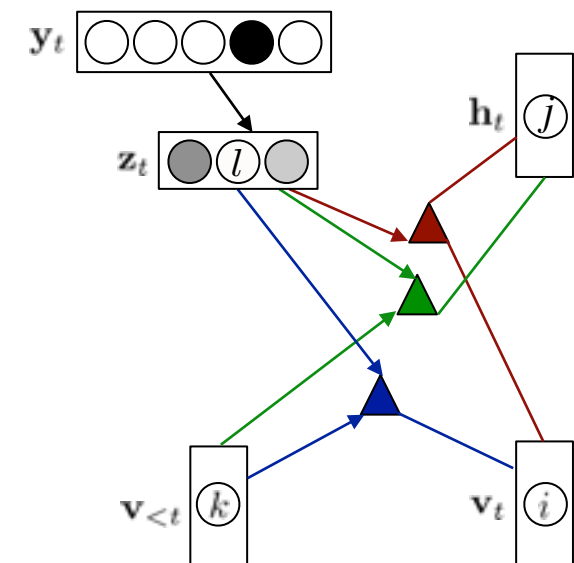
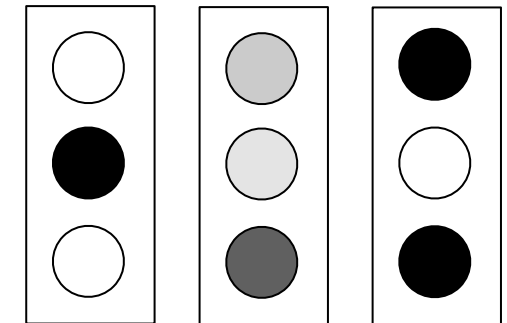
SUMMARY

- Learning distributed representations of sequences



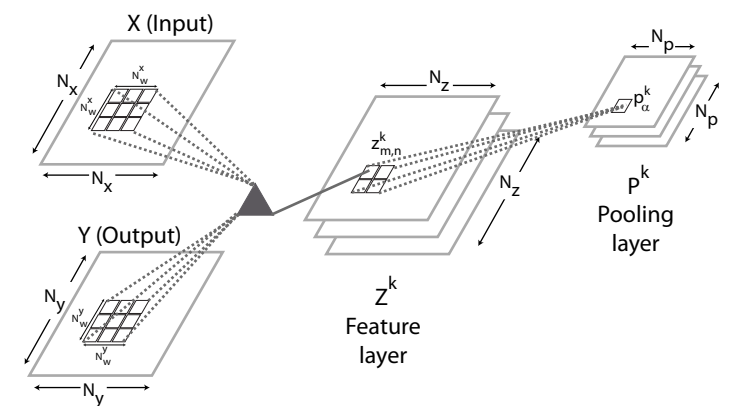
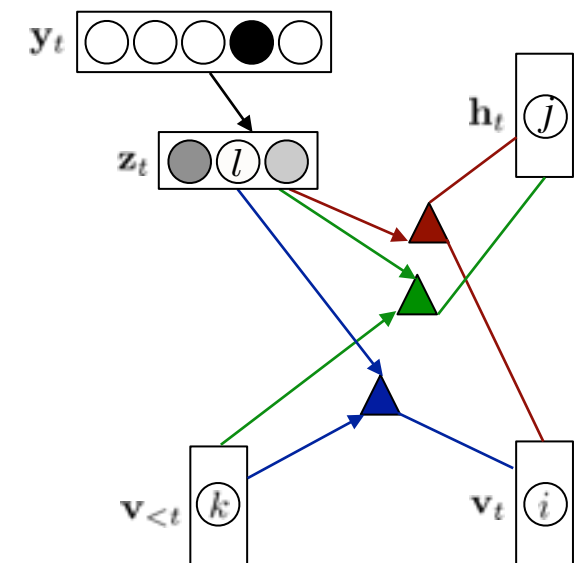
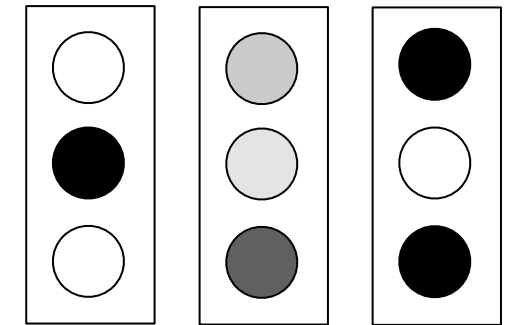
SUMMARY

- Learning distributed representations of sequences
- For high-dimensional, multi-modal data: CRBM, FCRBM



SUMMARY

- Learning distributed representations of sequences
- For high-dimensional, multi-modal data: CRBM, FCRBM
- Activity recognition: 2 methods



The University of Guelph is not in Belgium!

