

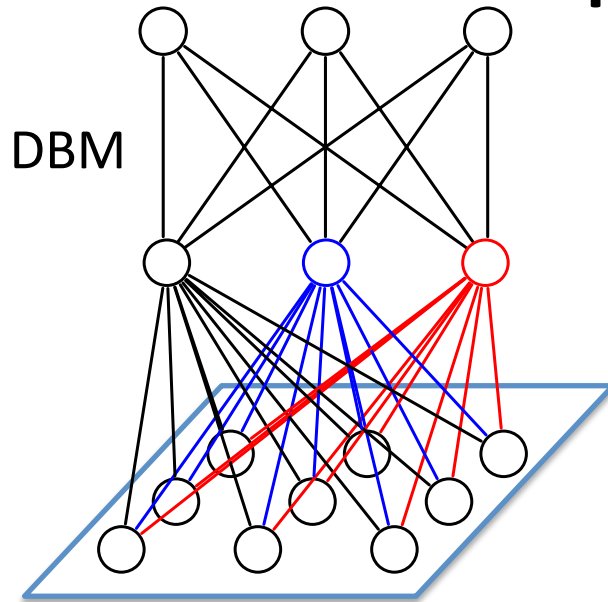
# Advanced Hierarchical Models

Ruslan Salakhutdinov

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Department of Statistics, University of Toronto

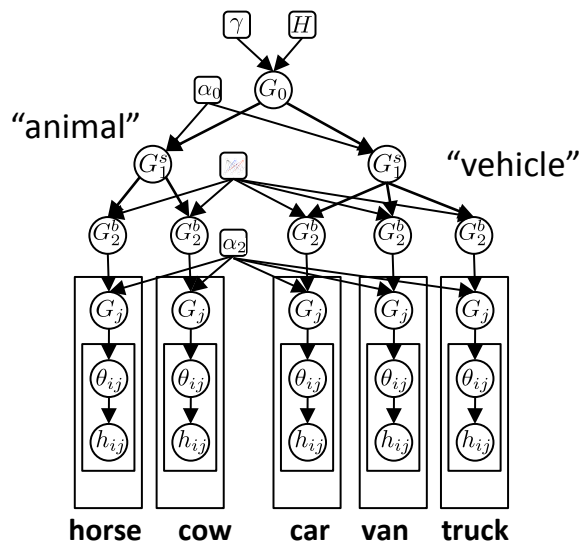


# Talk Roadmap



## Part 2: Advanced Hierarchical Models

- Introduction: Transfer Learning/  
One-Shot Learning.
- Compound Hierarchical Deep Models:
  - Deep Boltzmann Machines.
  - Hierarchical Latent Dirichlet Allocation Model.
- Applications.



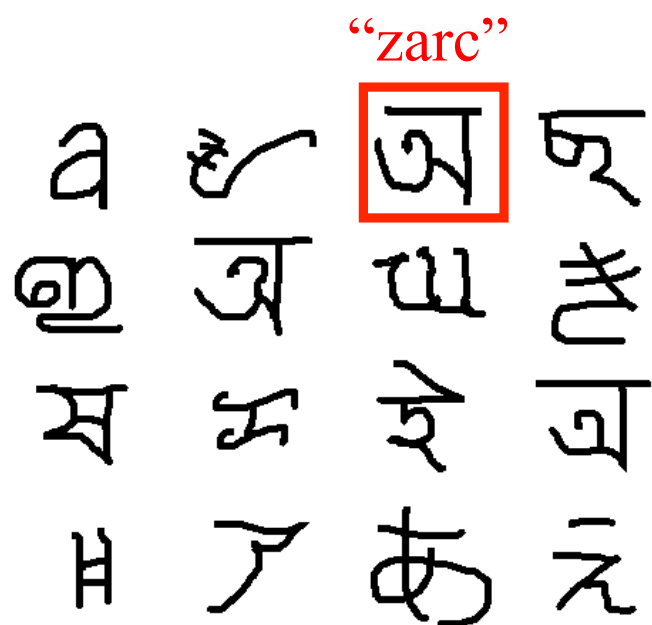
# Motivation

- Learning abstract representations that support transfer to novel tasks, lies at the core of many problems in computer vision, speech perception, natural language processing, and machine learning.
- In many machine learning applications performance is measured using hundreds or thousands of training examples.
- For human learners, a single example of a novel category is often sufficient to make meaningful generalizations to novel instances.

**Goal:** Transfer higher-order knowledge abstracted from previously learned concept to infer parameters of a novel concept from few examples.

# One-shot Learning

(Lake, Salakhutdinov, Gross, Tenenbaum, CogSci 2011)



How can we learn a novel concept – a high dimensional statistical object – from few examples.



# Traditional Supervised Learning



Segway



Motorcycle

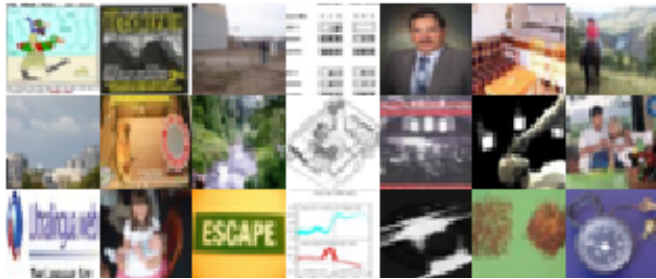
Test:  
What is this?



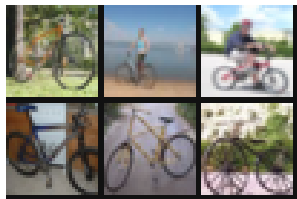
# Learning to Transfer

## Background Knowledge

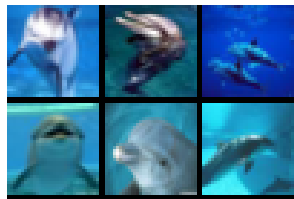
Millions of unlabeled images



Some labeled images



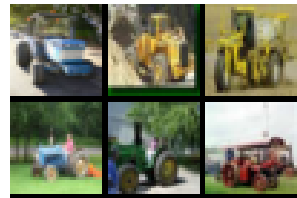
Bicycle



Dolphin



Elephant



Tractor

Learn to Transfer  
Knowledge



Learn novel concept  
from one example

Test:  
What is this?



# Learning to Transfer

## Background Knowledge

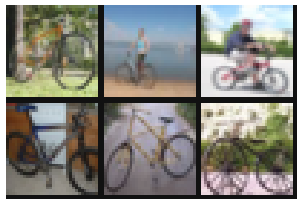
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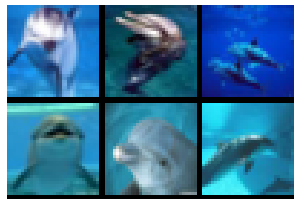
Learn to Transfer Knowledge

Key problem in computer vision, speech perception, natural language processing, and many other domains.

Some labeled images



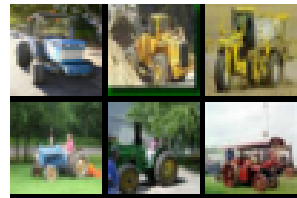
Bicycle



Dolphin



Elephant



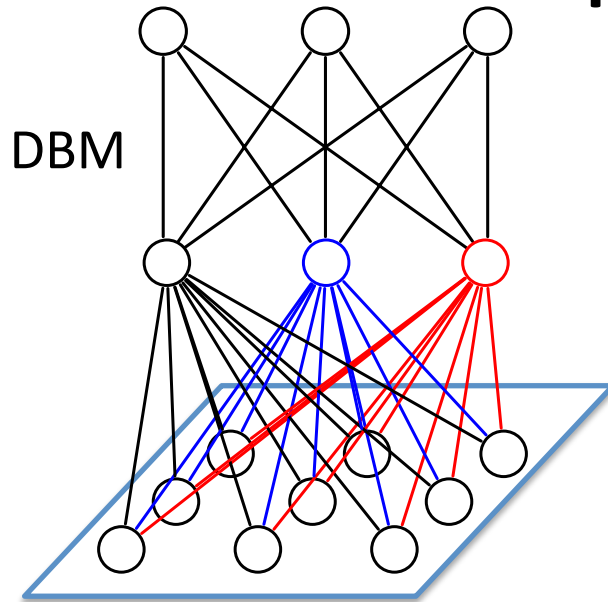
Tractor

Learn novel concept from one example

Test:  
What is this?

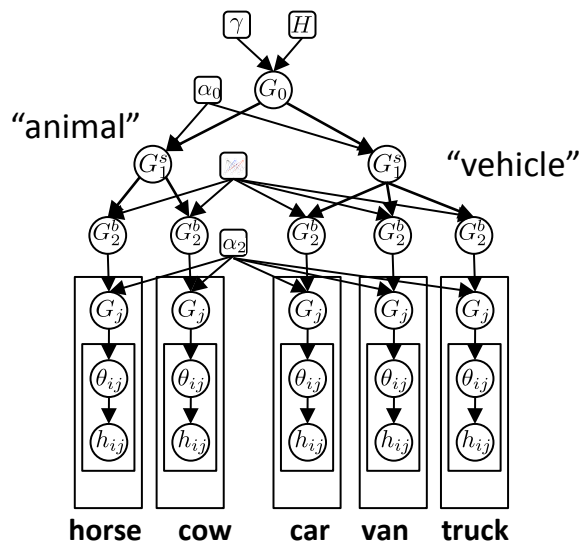


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## Part 2: Advanced Hierarchical Models

- Introduction: Transfer Learning/ One-Shot Learning.
- **Compound Hierarchical Deep Models:**
  - Deep Boltzmann Machines.
  - Hierarchical Latent Dirichlet Allocation Model.
- Applications.
- Conclusions



# Compound Hierarchical-Deep Models

(Salakhutdinov, Tenenbaum, Torralba, 2011)

**This Talk: HD Models:** Compose hierarchical Bayesian models with deep networks, two influential approaches from unsupervised learning

## Deep Networks:

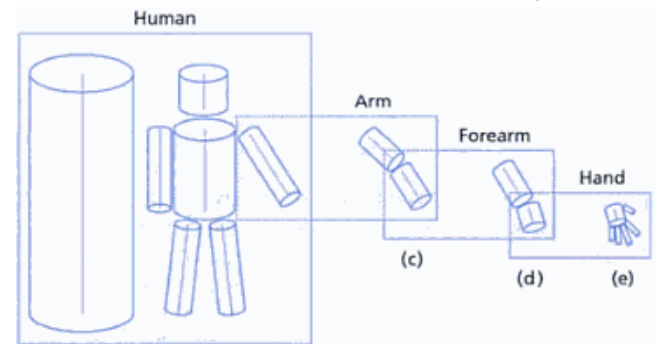
- learn multiple **layers of nonlinearities**.
- trained in unsupervised fashion -- **unsupervised feature learning** – no need to rely on human-crafted input representations.
- **labeled data** is used to slightly adjust the model for a specific task.

## Hierarchical Bayes:

- **explicitly represent category hierarchies** for sharing abstract knowledge.
- explicitly identify only a **small number of parameters** that are relevant to the new concept being learned.

## Deep Nets

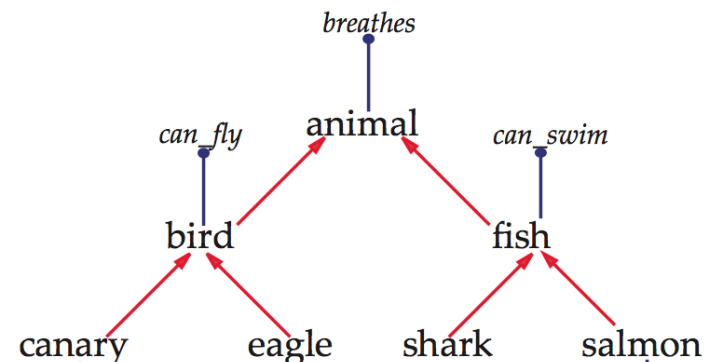
### Part-based Hierarchy



Marr and Nishihara (1978)

## Hierarchical Bayes

### Category-based Hierarchy



Collins & Quillian (1969)

# Motivation for Our Approach

Learning to transfer knowledge:

## Hierarchical

- Super-category: “A segway looks like a funny kind of vehicle”.
- Higher-level features, or parts, shared with other classes:
  - wheel, handle, post
- Lower-level features:
  - edges, composition of edges



Segway

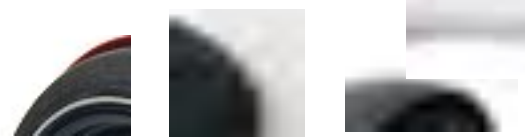
Super-class



Parts



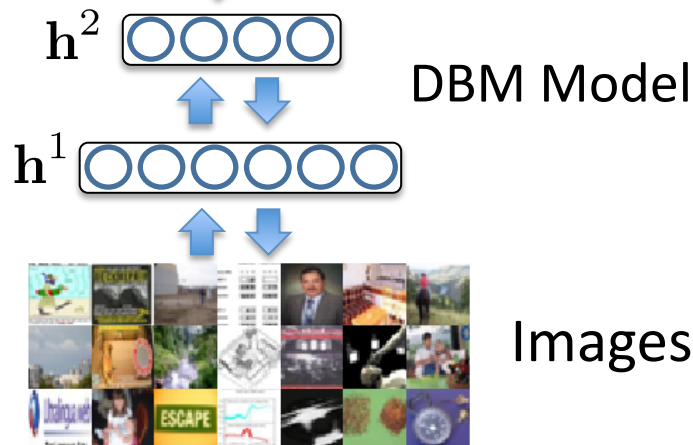
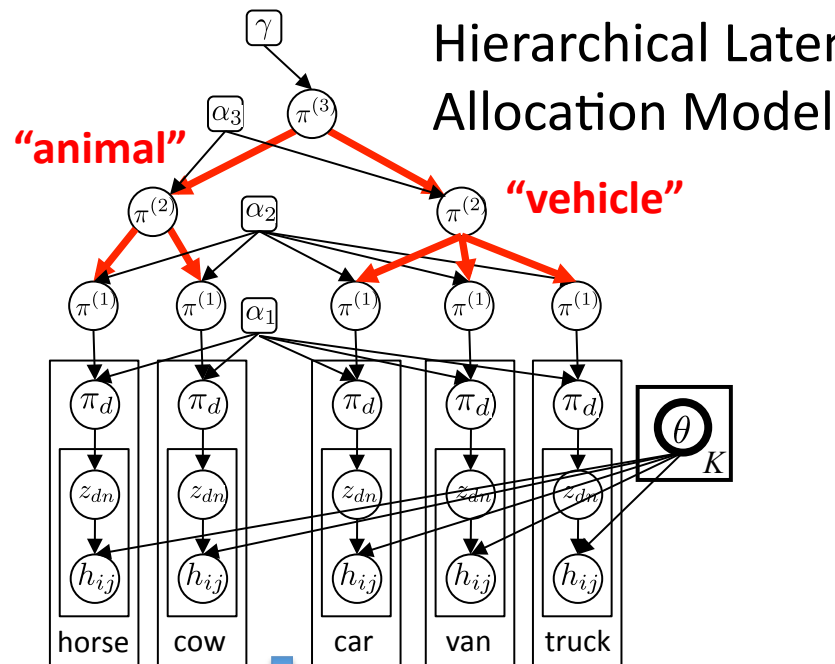
Edges



## Deep

# Hierarchical Generative Model

(Salakhutdinov, Tenenbaum, Torralba, 2011)



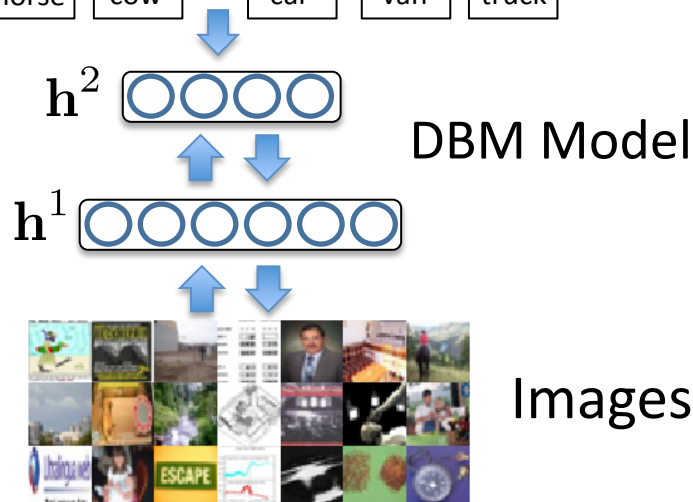
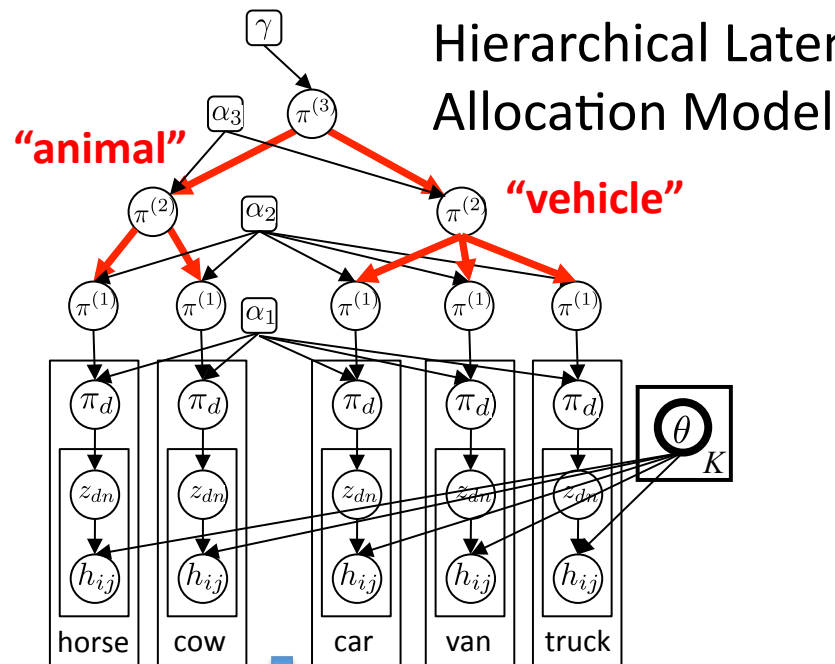
**Lower-level generic features:**

- edges, combination of edges



# Hierarchical Generative Model

(Salakhutdinov, Tenenbaum, Torralba, 2011)



## Hierarchical Organization of Categories:

- express priors on the features that are typical of different kinds of concepts
- modular data-parameter relations

## Higher-level class-sensitive features:

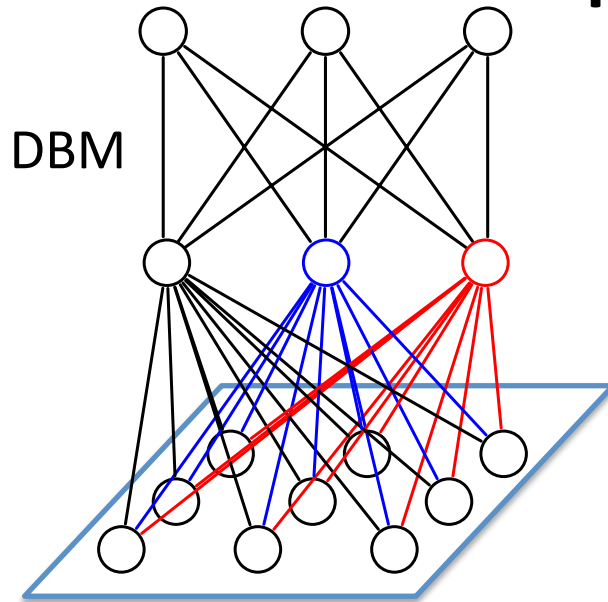
- capture distinctive perceptual structure of a specific concept

## Lower-level generic features:

- edges, combination of edges

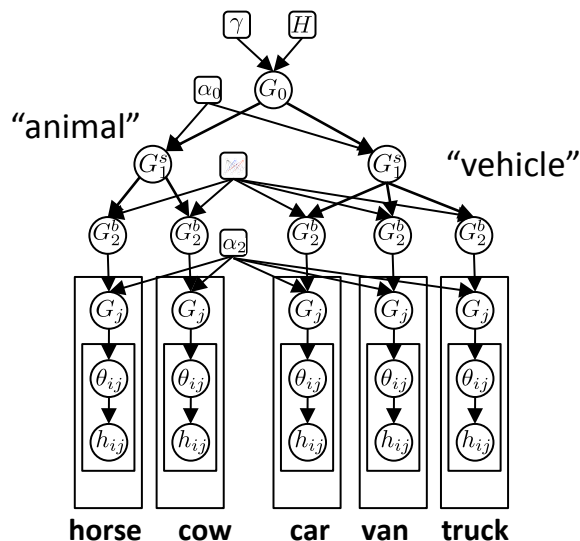


# Talk Roadmap



## Part 2: Advanced Hierarchical Models

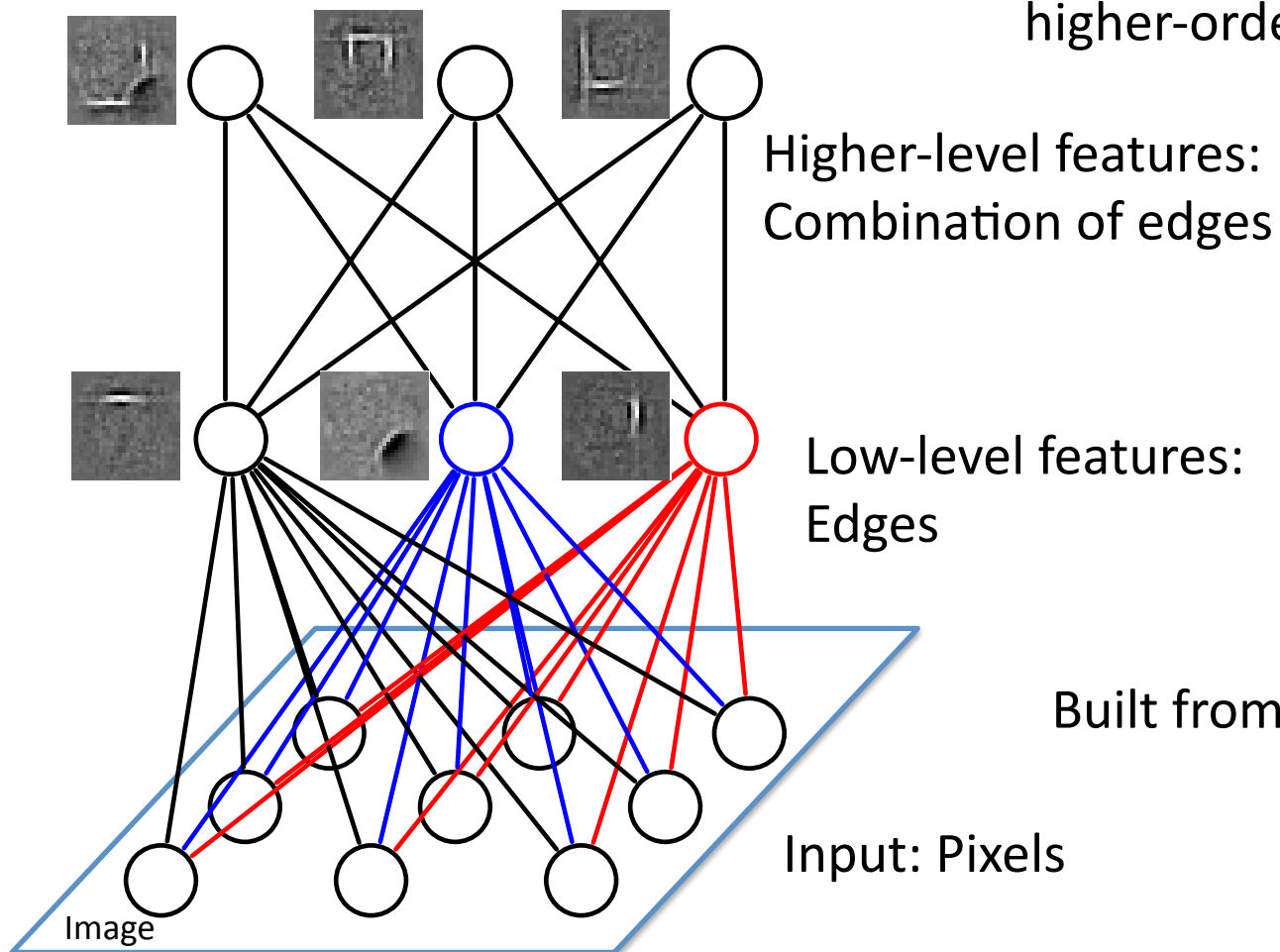
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# Deep Boltzmann Machines

(Salakhutdinov, 2008; Salakhutdinov & Hinton, AI & Statistics 2009)

Internal representations capture  
higher-order statistical structure



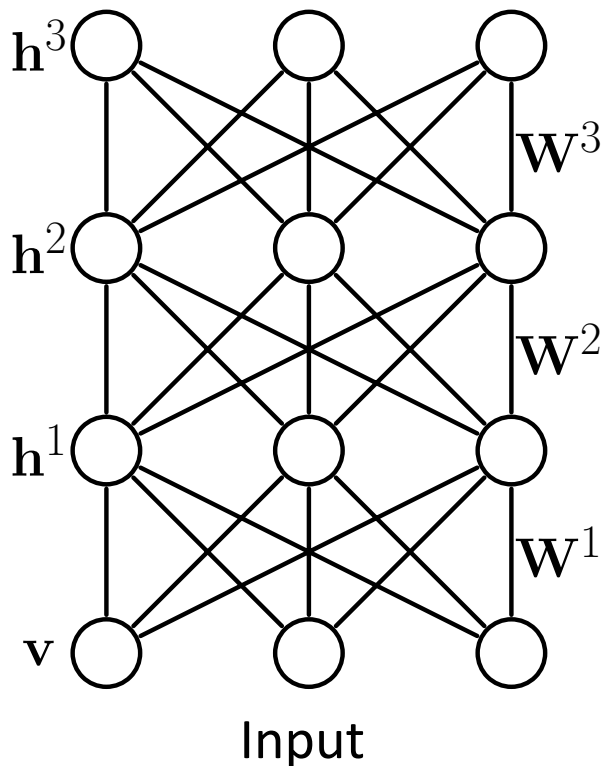
Built from **unlabeled** inputs.

# A Brief Review

$$P_{\theta}(\mathbf{v}) = \frac{P^*(\mathbf{v})}{\mathcal{Z}(\theta)} = \frac{1}{\mathcal{Z}(\theta)} \sum_{\mathbf{h}^1, \mathbf{h}^2, \mathbf{h}^3} \exp \left[ \mathbf{v}^{\top} W^1 \mathbf{h}^1 + \underline{\mathbf{h}^1{}^{\top} W^2 \mathbf{h}^2} + \underline{\mathbf{h}^2{}^{\top} W^3 \mathbf{h}^3} \right]$$

Deep Boltzmann Machine

$\theta = \{W^1, W^2, W^3\}$  model parameters

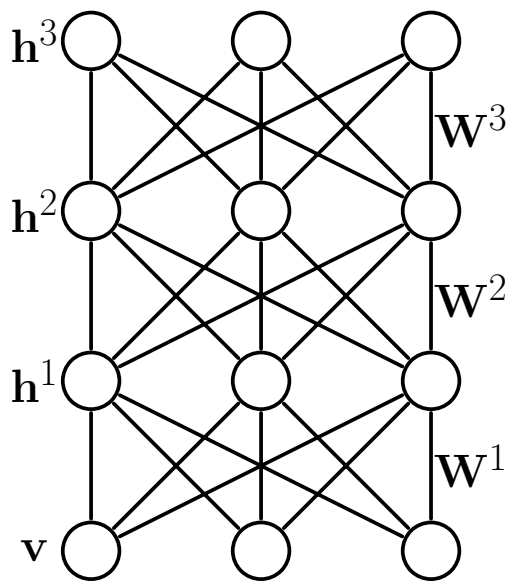


- Dependencies between hidden variables.
- All connections are undirected.
- Bottom-up and Top-down:

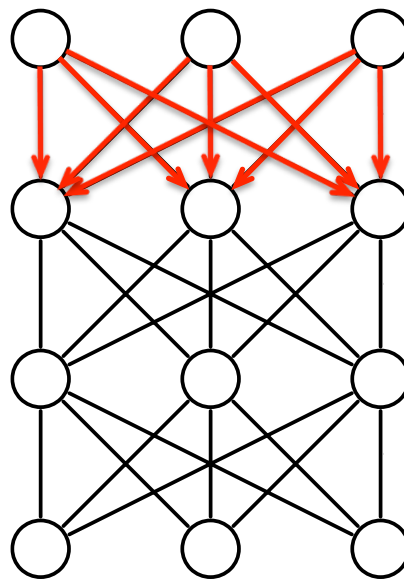
# Decomposition

The joint probability can be decomposed:

$$P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2, \mathbf{h}^3) = \underbrace{P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2 | \mathbf{h}^3)}_{\text{Conditional DBM}} \underbrace{P_{\theta}(\mathbf{h}^3)}_{\text{Prior term}}$$



DBM



Conditional DBM

**Key Idea:** Replace the last term with more structured hierarchical prior.

$$P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2 | \mathbf{h}^3) = \frac{1}{\mathcal{Z}(\theta, \mathbf{h}^3)} \exp \left[ \mathbf{v}^{\top} W^1 \mathbf{h}^1 + \mathbf{h}^1{}^{\top} W^2 \mathbf{h}^2 + \mathbf{h}^2{}^{\top} W^3 \mathbf{h}^3 \right]$$

# Stage-wise Learning

The joint probability can be decomposed:

$$P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2, \mathbf{h}^3) = \underbrace{P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2 | \mathbf{h}^3)}_{\text{Conditional DBM}} \underbrace{P_{\theta}(\mathbf{h}^3)}_{\text{Prior term}}$$

DBMs approximate intractable posterior  $P_{\theta}(\mathbf{h} | \mathbf{v})$  with fully factorized tractable distribution  $Q_{\mu}(\mathbf{h} | \mathbf{v})$ . The variational lower-bound takes form:

$$\log P_{\theta}(\mathbf{v}) \geq \underbrace{\sum_{\mathbf{h}^1, \mathbf{h}^2} Q_{\mu}(\mathbf{h} | \mathbf{v}) \left[ \log P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2 | \mathbf{h}^3) \right]}_{\text{Likelihood term}} + \underbrace{\mathcal{H}(Q_{\mu}(\mathbf{h} | \mathbf{v}))}_{\text{Entropy functional}}$$

$$\mathcal{H}(Q_{\mu}(\mathbf{h} | \mathbf{v})) = \sum_{\mathbf{h}} Q_{\mu}(\mathbf{h} | \mathbf{v}) \log \frac{1}{Q_{\mu}(\mathbf{h} | \mathbf{v})}$$

$$+ \underbrace{\sum_{\mathbf{h}^3} Q_{\mu}(\mathbf{h}^3 | \mathbf{v}) \log P_{\theta}(\mathbf{h}^3)}_{\text{Fit Hierarchical LDA prior}}$$

# Stage-wise Learning

The joint probability can be decomposed:

$$P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2, \mathbf{h}^3) = \underbrace{P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2 | \mathbf{h}^3)}_{\text{Conditional DBM}} \underbrace{P_{\theta}(\mathbf{h}^3)}_{\text{Prior term}}$$

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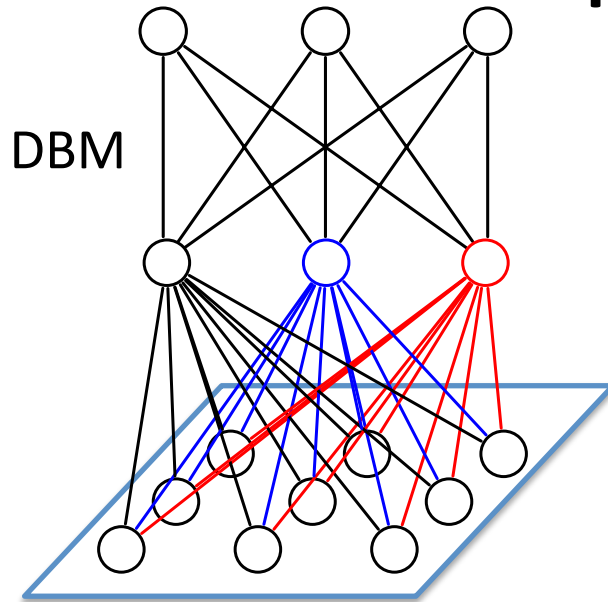
$$\log P_{\theta}(\mathbf{v}) \geq \sum_{\mathbf{h}^1, \mathbf{h}^2} Q_{\mu}(\mathbf{h} | \mathbf{v}) \underbrace{\left[ \log P_{\theta}(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2 | \mathbf{h}^3) \right]}_{\text{Likelihood term}} + \underbrace{\mathcal{H}(Q_{\mu}(\mathbf{h} | \mathbf{v}))}_{\text{Entropy functional}}$$

- Learn DBM.
- Using variational inference, infer the states of the top-level variables and fit an LDA prior.

$$Q_{\mu}(\mathbf{h}^3 | \mathbf{v}) \log P_{\theta}(\mathbf{h}^3)$$

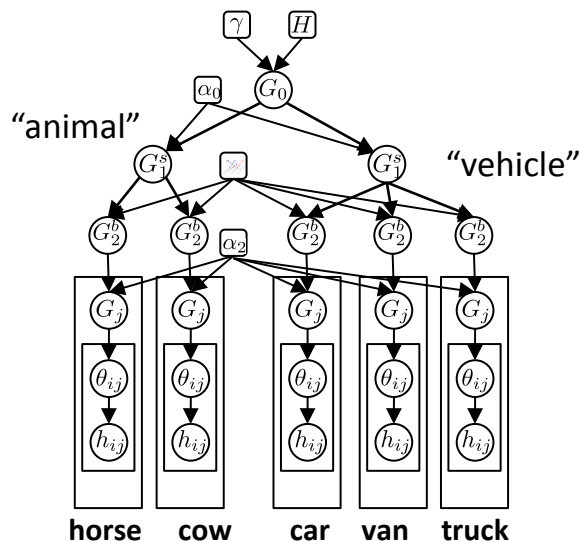
**Fit Hierarchical LDA prior**

# Talk Roadmap

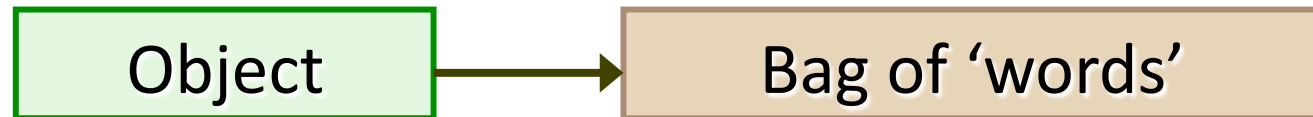


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# Bag of Words Representation





# Analogy to Documents

Of all the sensory impressions proceeding to the brain, the visual impressions are the dominant ones. The world around us is a constant stream of messages that reach the brain through the eyes. The time taken for these messages to be transmitted to the brain is very short. The visual system, the brain, the eye, cell, optical nerve, image Hubel, Wiesel

*message about the image falling on the retina undergoes a step-wise analysis in a system of nerve cells stored in columns*

China is forecasting a trade surplus of \$90bn (£51bn) to \$100bn, a 30% increase on 2004's \$69bn. The government said the surplus would rise to 18% in 2005, a further rise in 2006. China's deliberate policy to boost its surplus is a major factor. Bank of China said the country's domestic demand would boost the country. China's yuan against the dollar by 2.1% in July, but permitted it to trade within a narrow band. The US wants the yuan to be allowed to rise freely. However, Beijing has made it clear it will take its time and tread carefully before allowing the yuan to rise further in value.

**Intuition:** Documents contain multiple topics.

# Latent Dirichlet Allocation

Text  
document

The William Randolph Hearst Foundation will give \$1.25 million to Lincoln Center, Metropolitan Opera Co., New York Philharmonic and Juilliard School. “Our board felt that we had a real opportunity to make a mark on the future of the performing arts with these grants an act every bit as important as our traditional areas of support in health, medical research, education and the social services,” Hearst Foundation President Randolph A. Hearst said Monday in announcing the grants. Lincoln Center’s share will be \$200,000 for its new building, which will house young artists and provide new public facilities. The Metropolitan Opera Co. and New York Philharmonic will receive \$400,000 each. The Juilliard School, where music and the performing arts are taught, will get \$250,000. The Hearst Foundation, a leading supporter of the Lincoln Center Consolidated Corporate Fund, will make its usual annual \$100,000 donation, too.

Discovered  
topics

| “Arts”  | “Budgets”  | “Children” | “Education” |
|---------|------------|------------|-------------|
| NEW     | MILLION    | CHILDREN   | SCHOOL      |
| FILM    | TAX        | WOMEN      | STUDENTS    |
| SHOW    | PROGRAM    | PEOPLE     | SCHOOLS     |
| MUSIC   | BUDGET     | CHILD      | EDUCATION   |
| MOVIE   | BILLION    | YEARS      | TEACHERS    |
| PLAY    | FEDERAL    | FAMILIES   | HIGH        |
| MUSICAL | YEAR       | WORK       | PUBLIC      |
| BEST    | SPENDING   | PARENTS    | TEACHER     |
| ACTOR   | NEW        | SAYS       | BENNETT     |
| FIRST   | STATE      | FAMILY     | MANIGAT     |
| YORK    | PLAN       | WELFARE    | NAMPHY      |
| OPERA   | MONEY      | MEN        | STATE       |
| THEATER | PROGRAMS   | PERCENT    | PRESIDENT   |
| ACTRESS | GOVERNMENT | CARE       | ELEMENTARY  |
| LOVE    | CONGRESS   | LIFE       | HAITI       |

Blei, et al. 2003

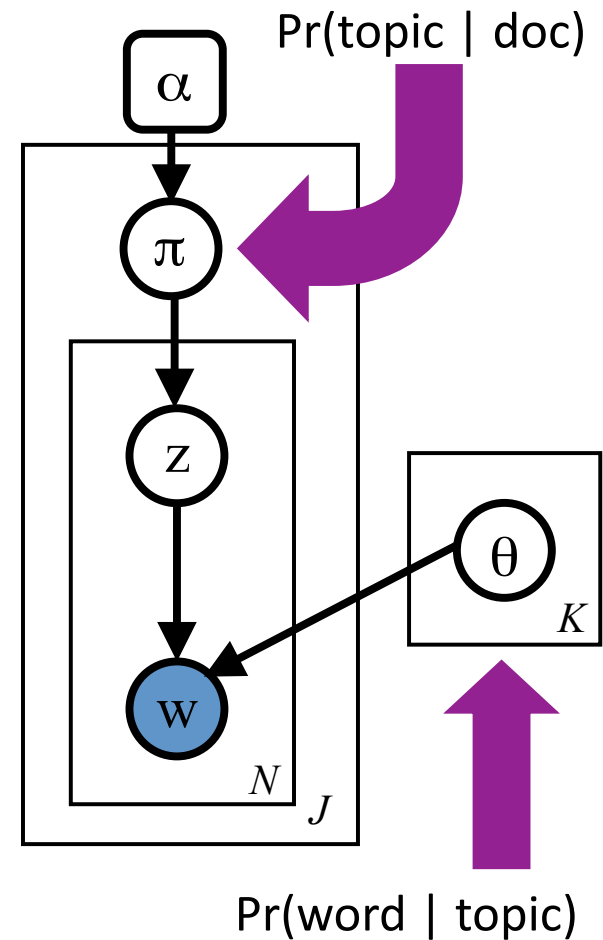
# Latent Dirichlet Allocation

Generative Process:  $w \sim \text{LDA}$

Draw each topic  $\theta_k \sim \text{Dir}(\eta)$  for  $k = 1 \dots, K$

For each document:

- Draw topic proportions  $\pi_d \sim \text{Dir}(\alpha)$
- For each word:
  - Draw topic indicator  $z_{d,n} \sim \text{Mult}(\pi_d)$
  - Draw word  $w_{d,n} \sim \text{Mult}(\theta_{z_{d,n}})$



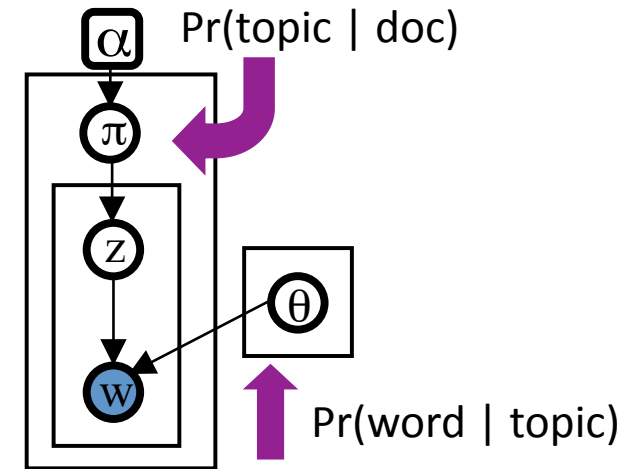
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| "Arts"  | "Budgets"  | "Children" | "Education" |
|---------|------------|------------|-------------|
| NEW     | MILLION    | CHILDREN   | SCHOOL      |
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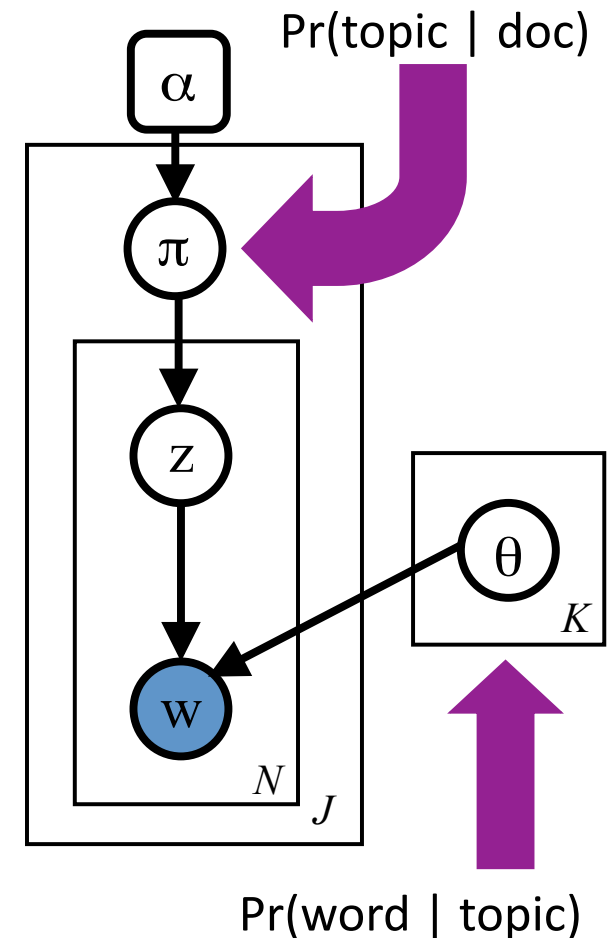
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**Remember:** compound HD model:

$\mathbf{h}^3 \sim \text{LDA prior}$

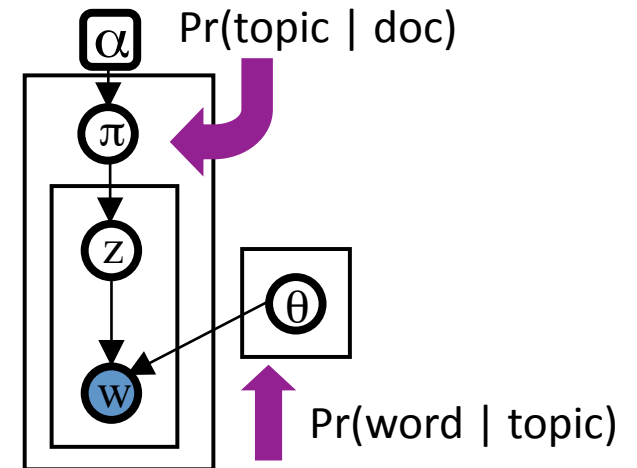
Words  $\Leftrightarrow$  activations of DBM's top-level units.  
Topics  $\Leftrightarrow$  distributions over top-level units, or higher-level parts.



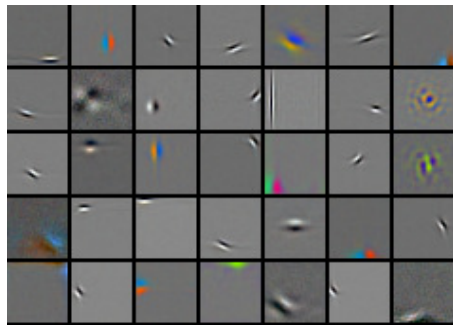
# Intuition

$\mathbf{h}^3 \sim \text{LDA prior}$

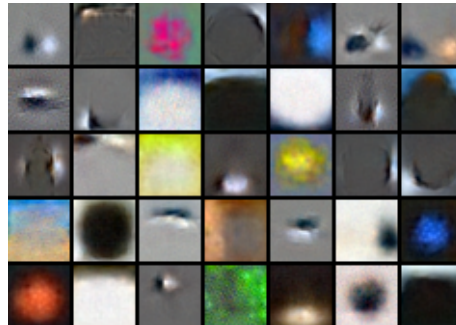
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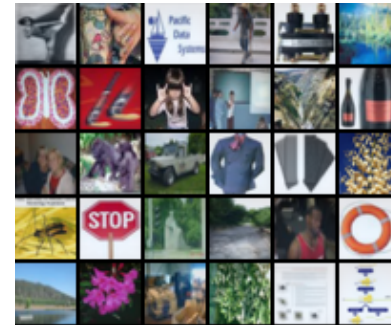
DBM generic features:  
**Words**



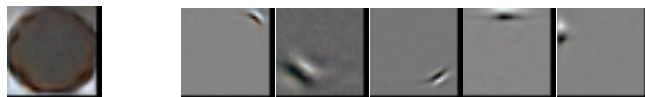
LDA high-level features:  
**Topics**



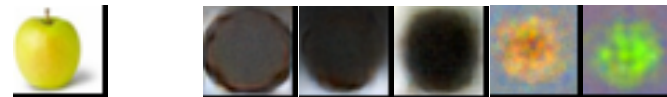
Images  
**Documents**



**Each topic is made up of words.**

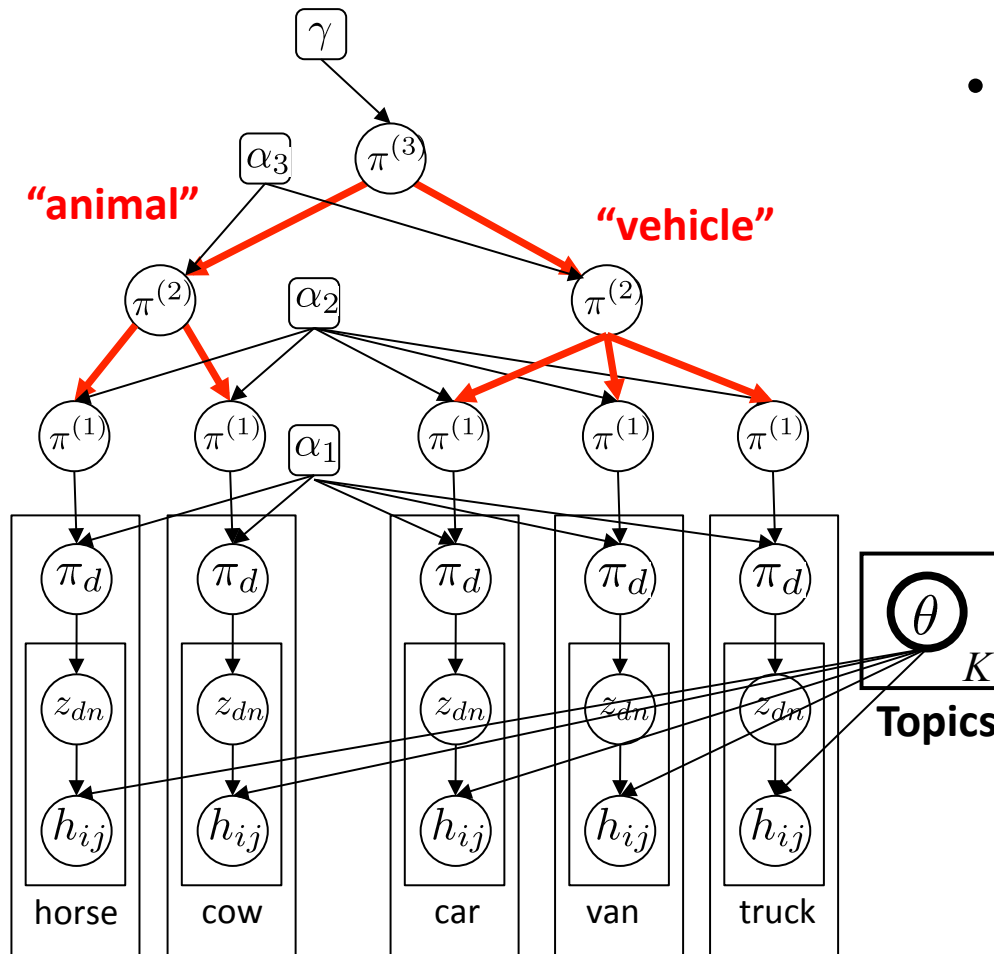


**Each document is made up of topics.**



# Hierarchical LDA

## Modeling Super-Category Structure



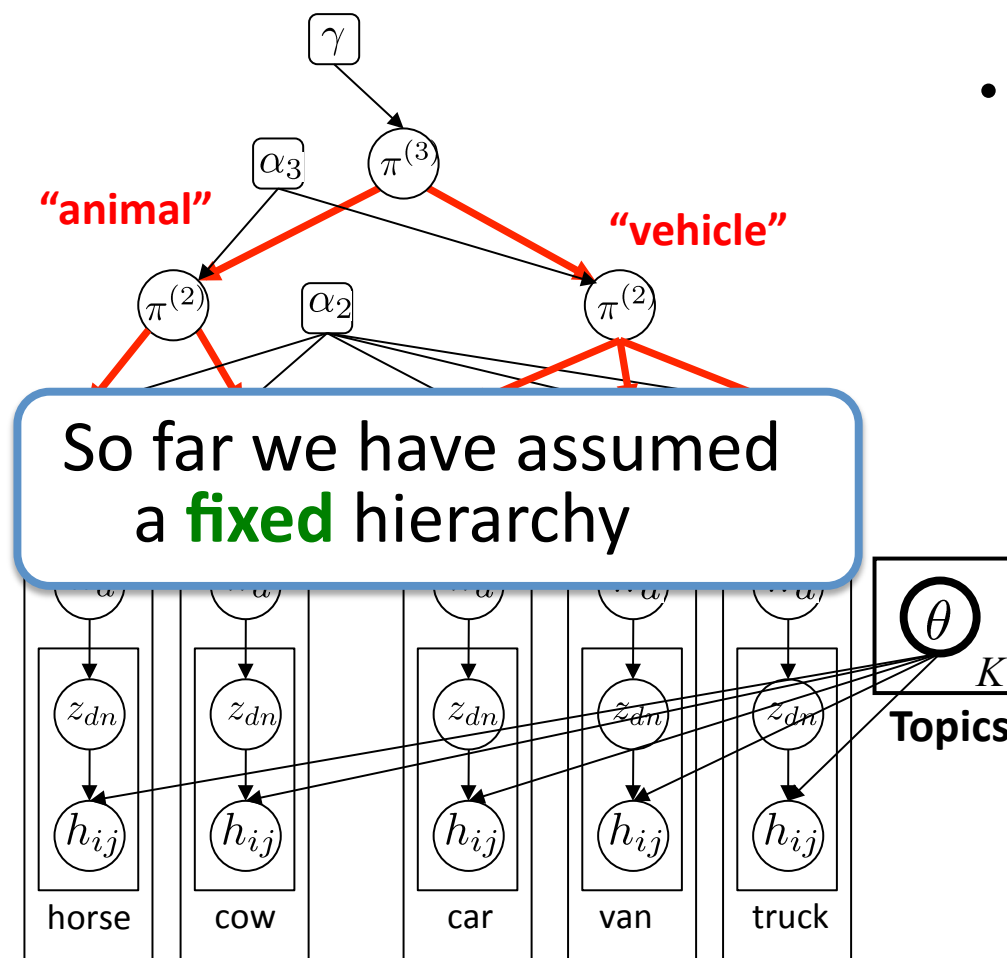
- Draw **global** topic proportions:  $\pi^{(3)} \sim \text{Dir}(\gamma)$
- Draw **super-class specific** topic proportions:  
 $\pi^{(2)} | \pi^{(3)} \sim \text{Dir}(\alpha^{(3)} \pi^{(3)})$
- Draw **class-class specific** topic proportions:  
 $\pi^{(1)} | \pi^{(2)} \sim \text{Dir}(\alpha^{(2)} \pi^{(2)})$ 
  - Draw **document specific** topic proportions:  
 $\pi_d | \pi^{(1)} \sim \text{Dir}(\alpha^{(1)} \pi^{(1)})$

Nonparametric extension:

**Hierarchical Dirichlet Process (HDP).**

# Hierarchical LDA

## Modeling Super-Category Structure



- Draw **global** topic proportions:  $\pi^{(3)} \sim \text{Dir}(\gamma)$
- Draw **super-class specific** topic proportions:  
 $\pi^{(2)} | \pi^{(3)} \sim \text{Dir}(\alpha^{(3)} \pi^{(3)})$
- Draw **class-class specific** topic proportions:  
 $\pi^{(1)} | \pi^{(2)} \sim \text{Dir}(\alpha^{(2)} \pi^{(2)})$
- Draw **document specific** topic proportions:  
 $\pi_d | \pi^{(1)} \sim \text{Dir}(\alpha^{(1)} \pi^{(1)})$

Nonparametric extension:

**Hierarchical Dirichlet Process (HDP).**



# Modeling the Number of Super-Categories

Place Chinese Restaurant Process (CRP) Prior over the number of super-classes.

CRP defines a distribution on partition of integers.

Generating from  $\text{CRP}(\alpha)$ :

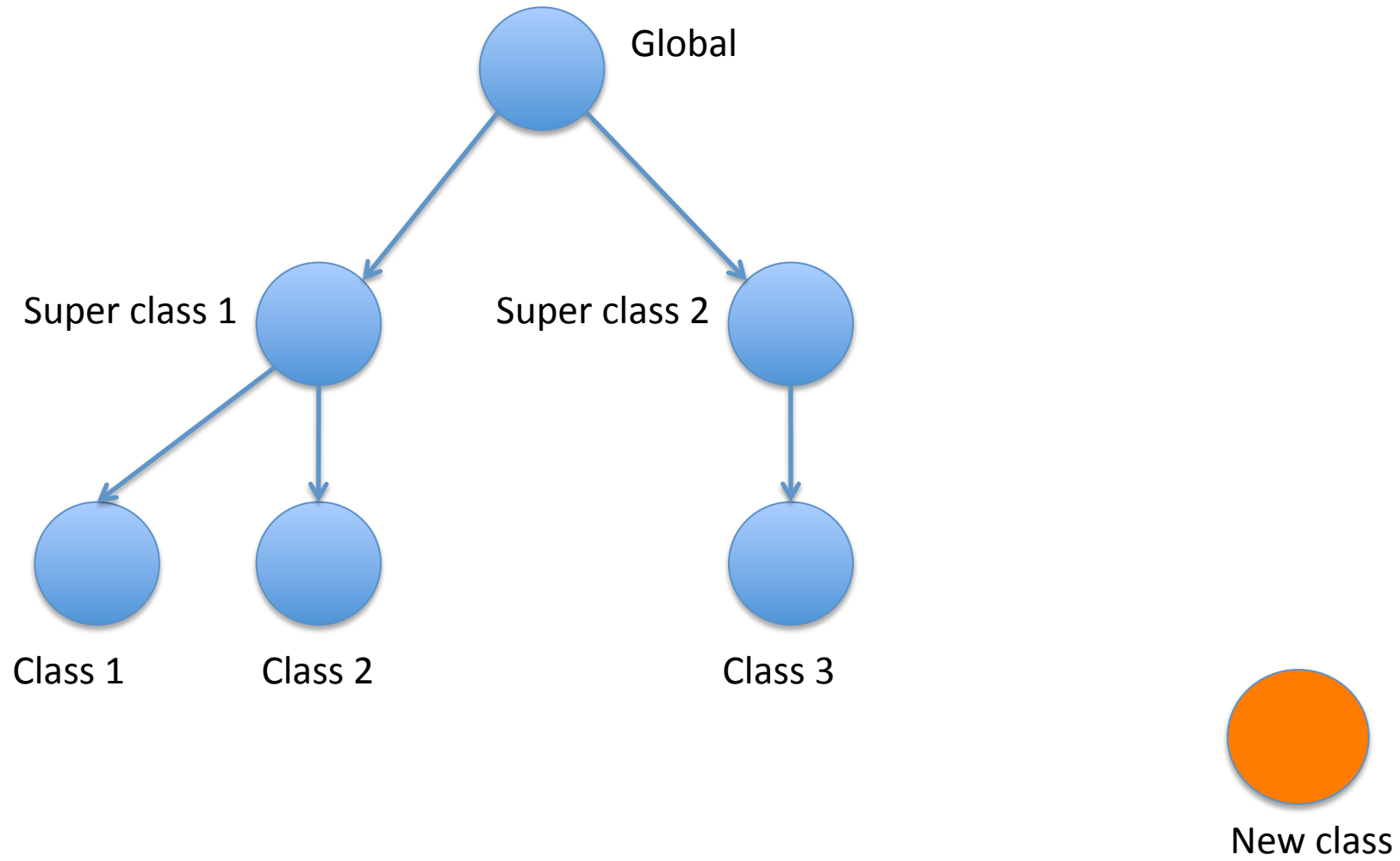
Customers enter a restaurant with an unbounded number of tables, where the  $n^{\text{th}}$  customer occupies a table  $k$  drawn from:

$$P(z_n = k | z_1, \dots, z_{n-1}) = \begin{cases} \frac{n^k}{n-1+\alpha} & n^k > 0 \\ \frac{\alpha}{n-1+\alpha} & k \text{ is new} \end{cases}$$

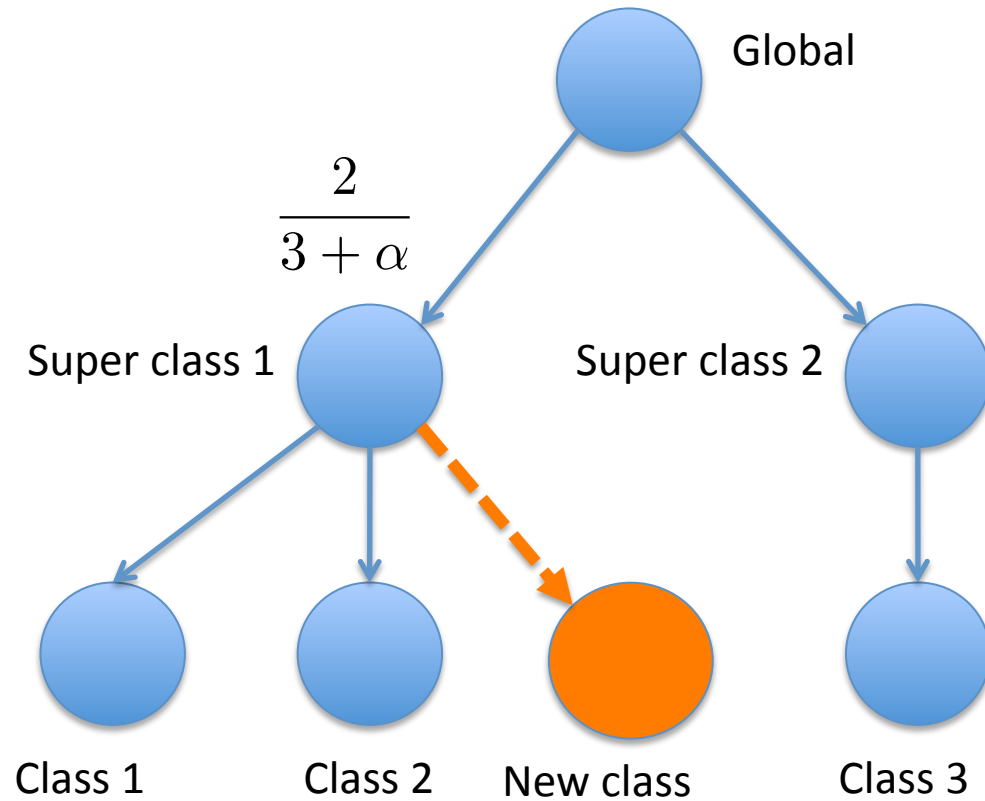
where  $n^k$  is the number of previous customers at table  $k$  and  $\alpha$  is the concentration parameter.

Customers  $\Leftrightarrow$  integers, tables  $\Leftrightarrow$  clusters.

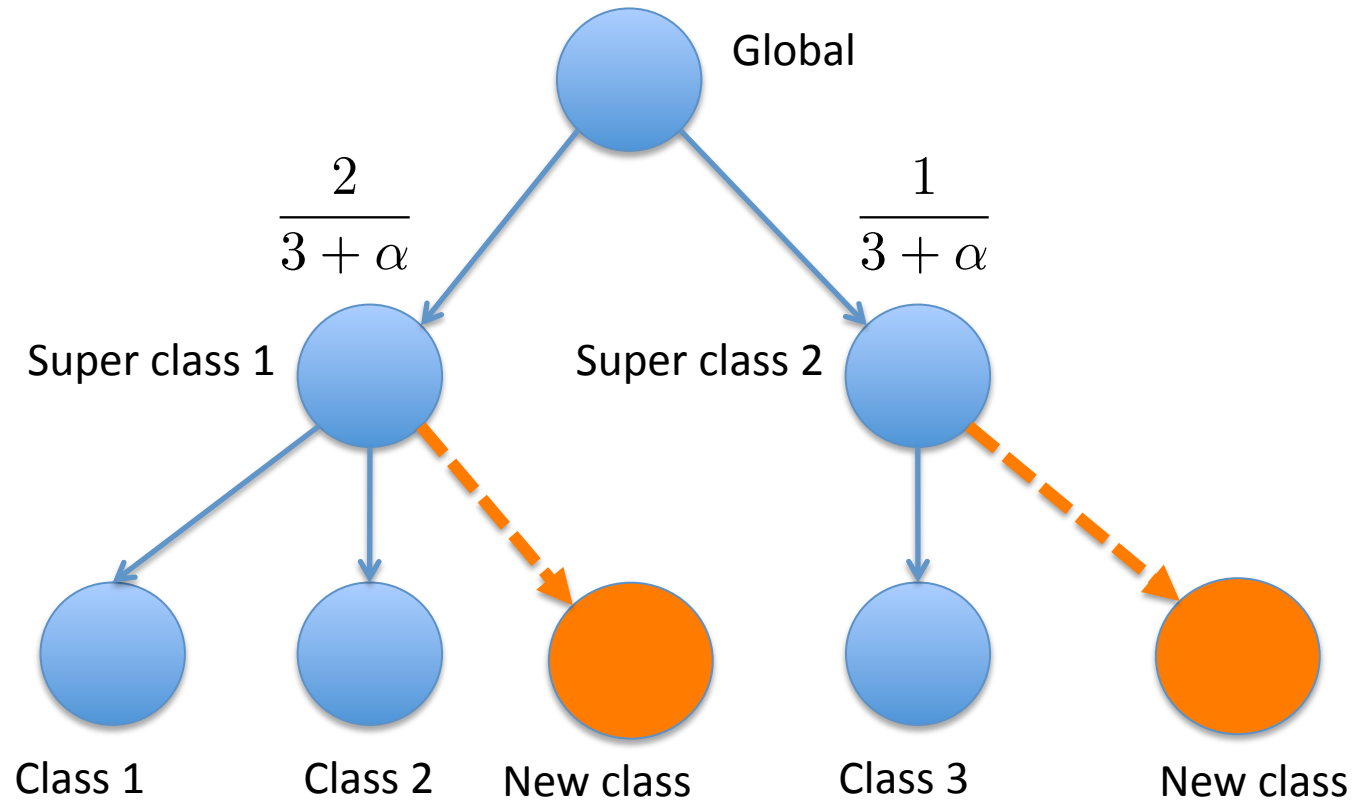
# Modeling the Hierarchy



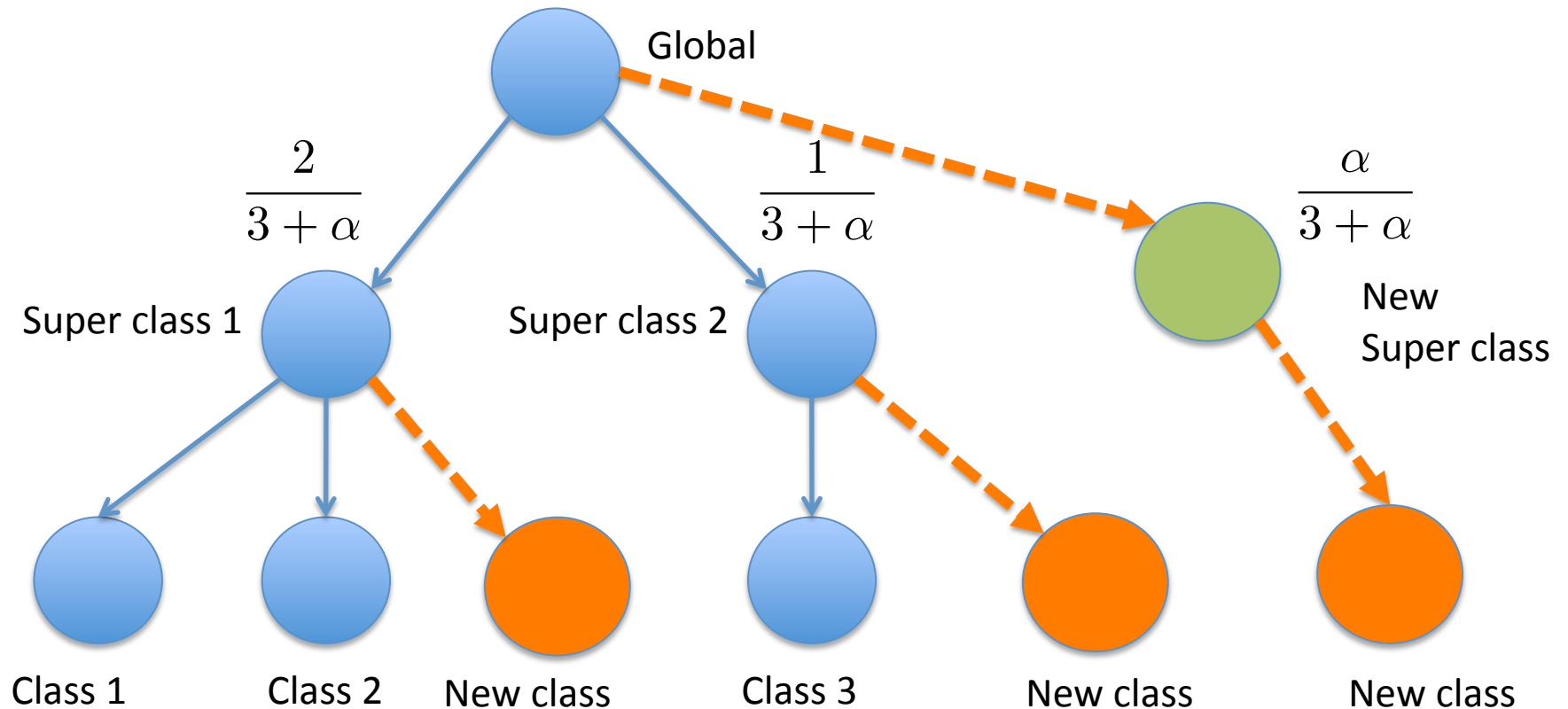
# Modeling the Hierarchy



# Modeling the Hierarchy



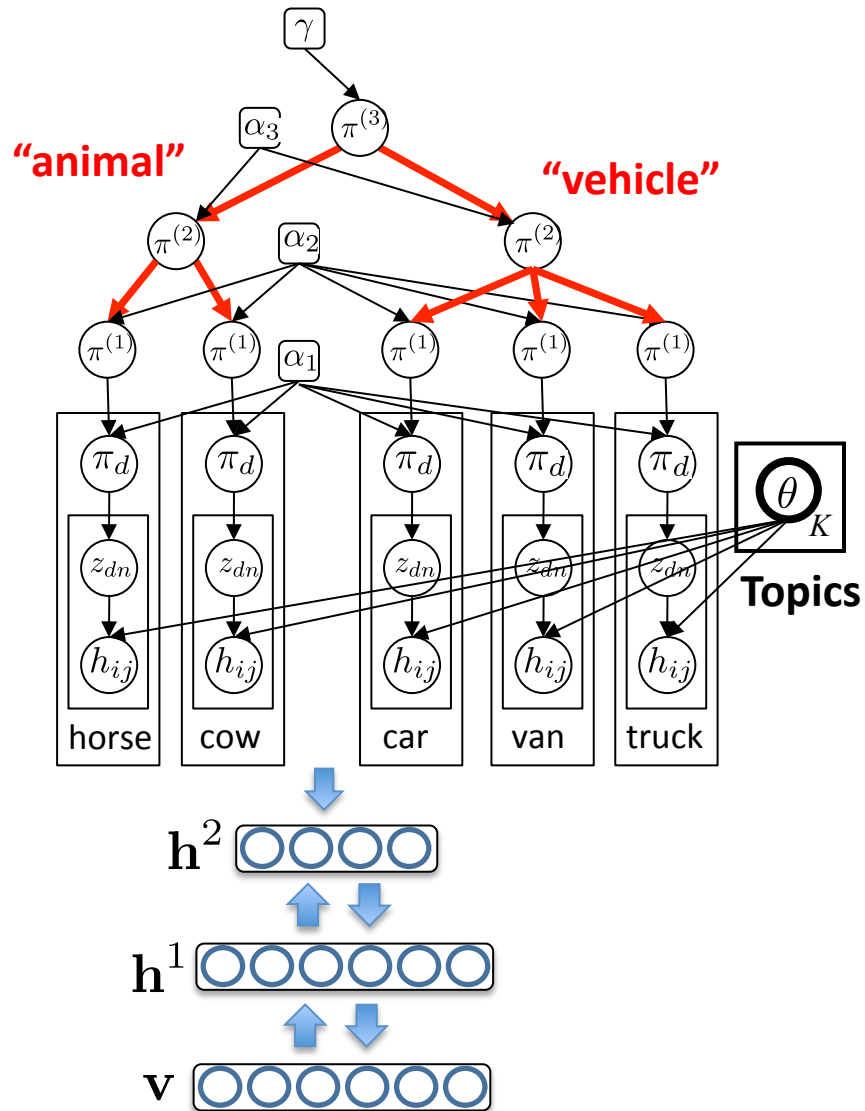
# Modeling the Hierarchy



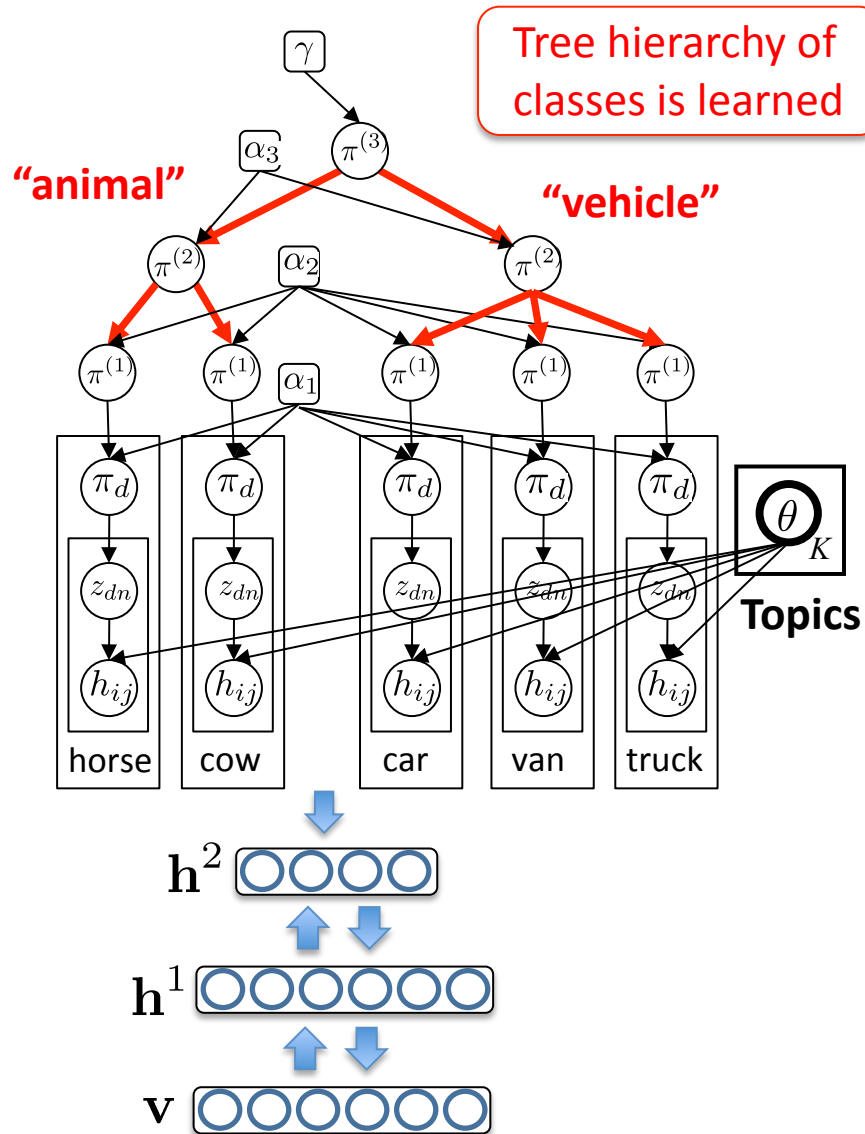
Expected number of clusters:  $O(\alpha \log n)$

The nested CRP, nCRP, extends CRP to nested sequence of partitions, one for each level of the tree (Blei et.al. NIPS 2003).

# Hierarchical Deep Model

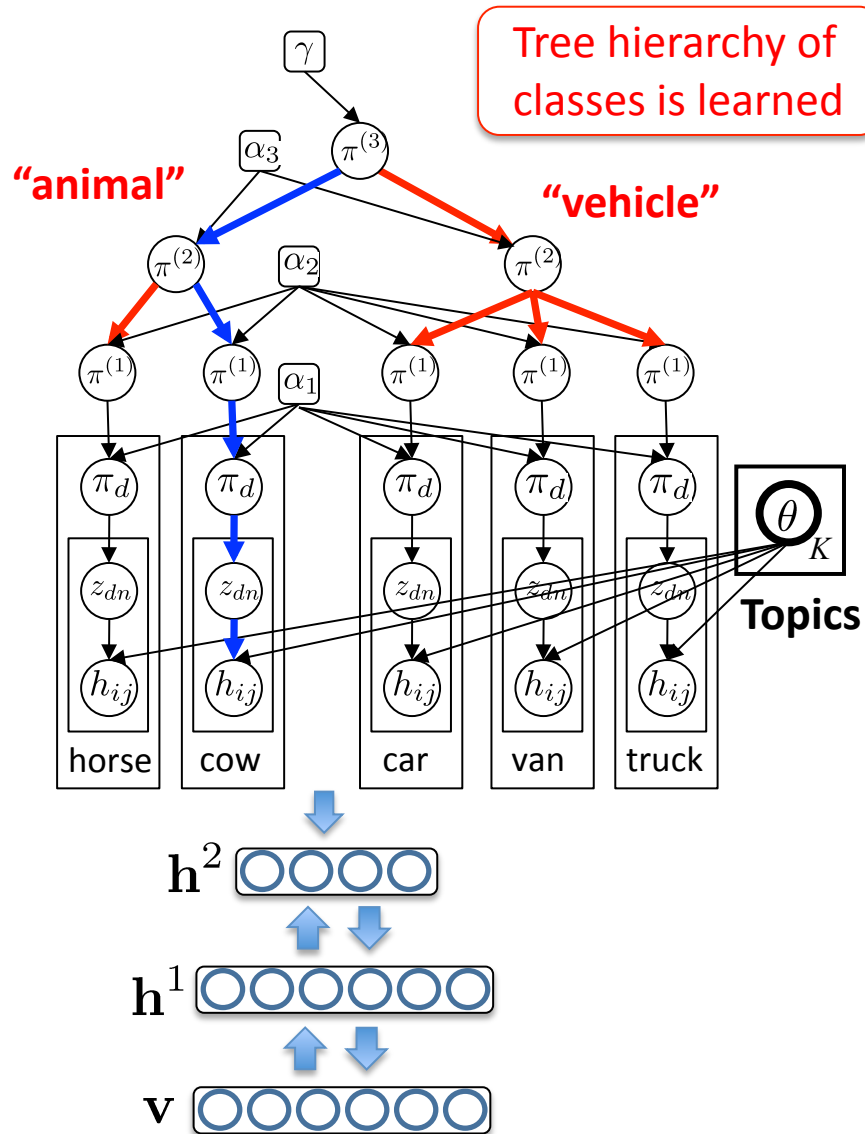


# Hierarchical Deep Model



$\mathbf{z} \sim \text{nCRP}$  (**Nested Chinese Restaurant Process**)  
 prior: a nonparametric prior over tree structures.

# Hierarchical Deep Model

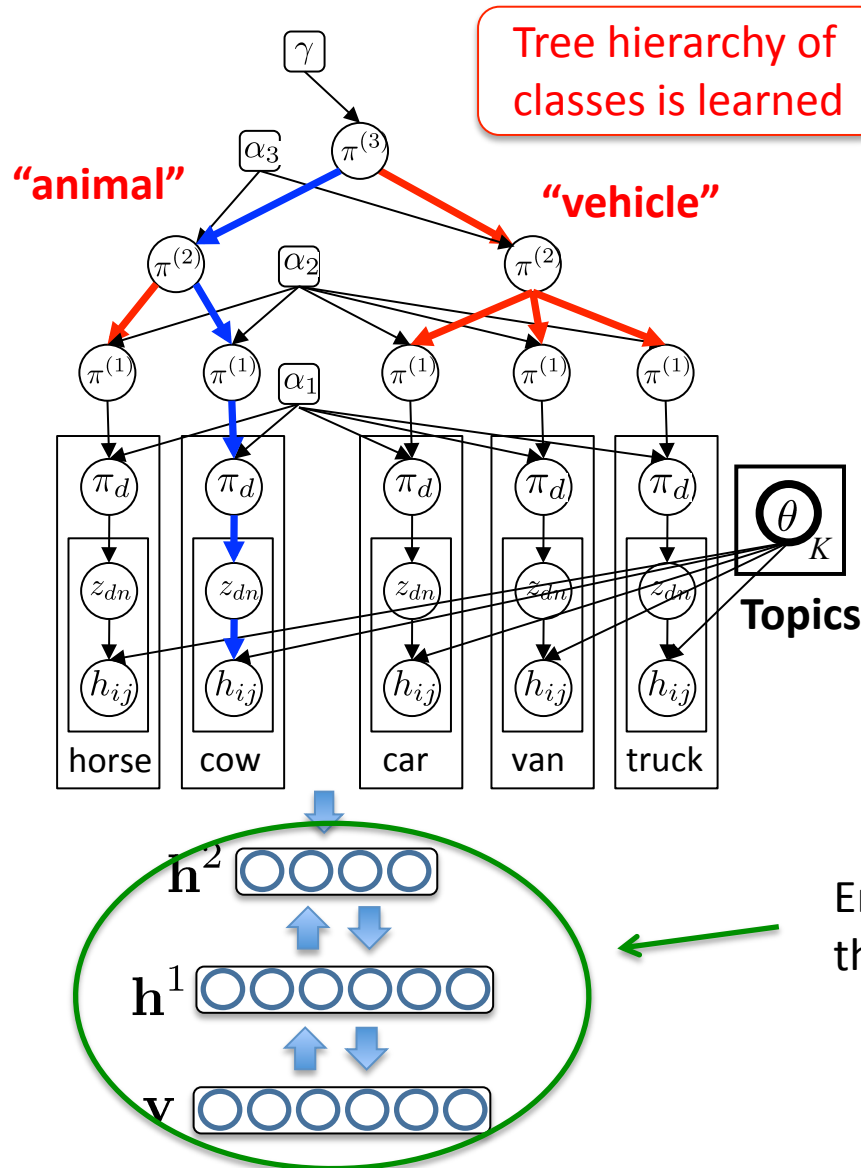


$z \sim \text{nCRP}$  (**Nested Chinese Restaurant Process**)  
prior: a nonparametric prior over tree structures.

$h^3 | z \sim \text{HDP}$  (**Hierarchical Dirichlet Process**) prior:  
a nonparametric prior allowing categories to share higher-level features, or parts.



# Hierarchical Deep Model



Tree hierarchy of classes is learned

"animal"

"vehicle"

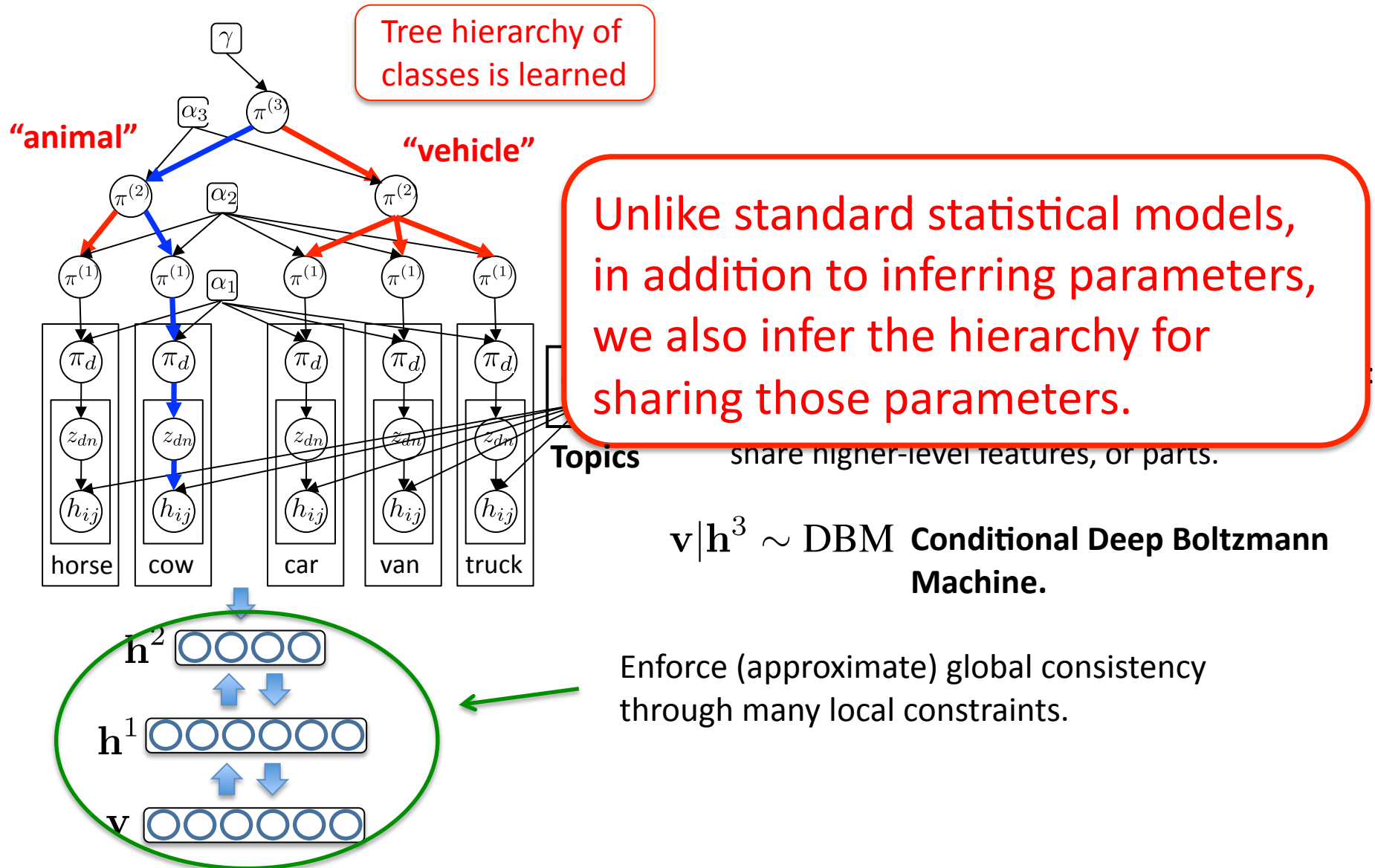
$z \sim \text{nCRP}$  (**Nested Chinese Restaurant Process**)  
prior: a nonparametric prior over tree structures

$h^3 | z \sim \text{HDP}$  (**Hierarchical Dirichlet Process**) prior:  
a nonparametric prior allowing categories to share higher-level features, or parts.

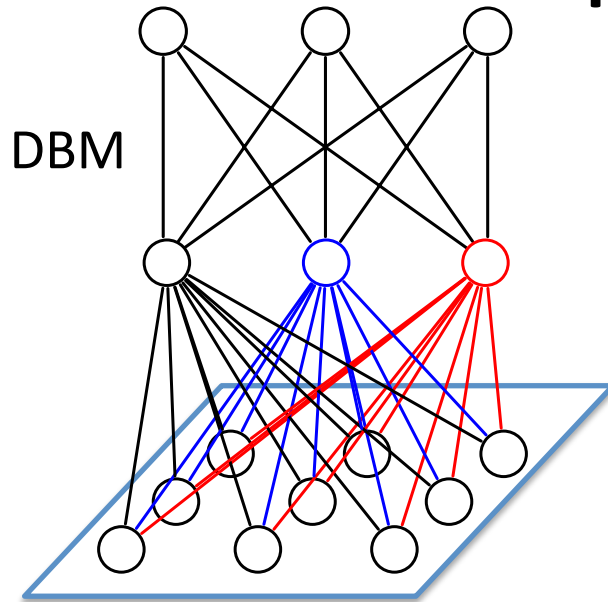
$v | h^3 \sim \text{DBM}$  **Conditional Deep Boltzmann Machine.**

Enforce (approximate) global consistency through many local constraints.

# Hierarchical Deep Model

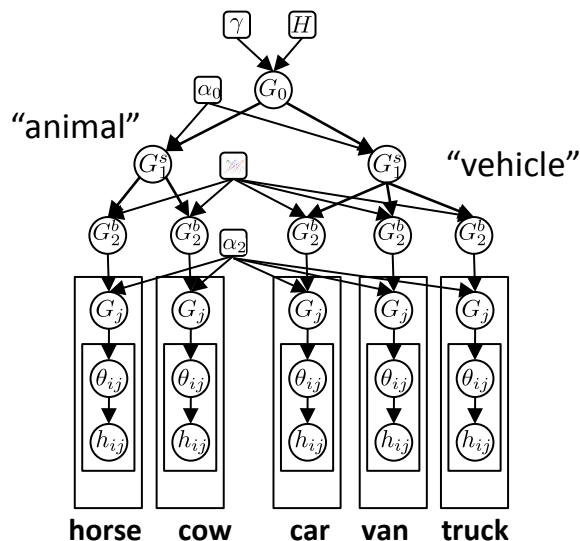


# Talk Roadmap

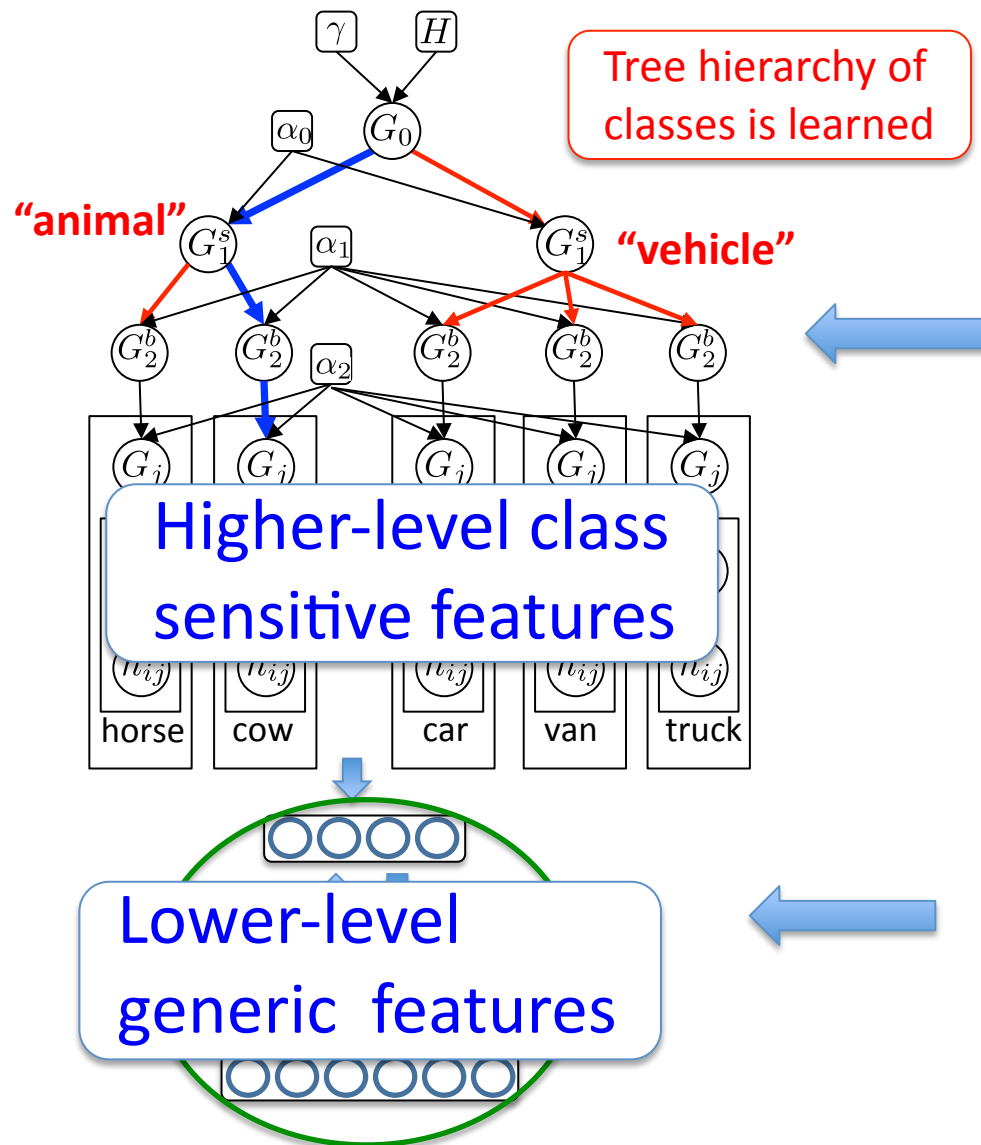


## Part 2: Advanced Hierarchical Models

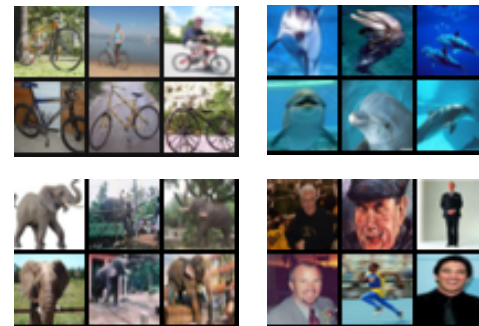
- Introduction: Transfer Learning/ One-Shot Learning.
- Compound Hierarchical Deep Models:
  - Deep Boltzmann Machines.
  - Hierarchical Latent Dirichlet Allocation Model.
- Applications.
- Conclusions



# CIFAR Object Recognition

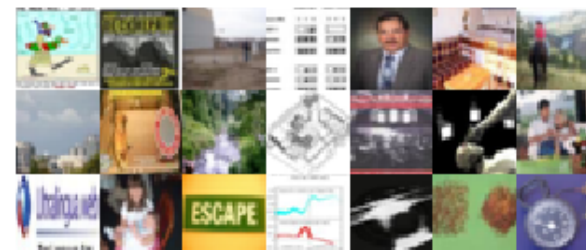


50,000 images of 100 classes



**Inference:** Markov chain Monte Carlo

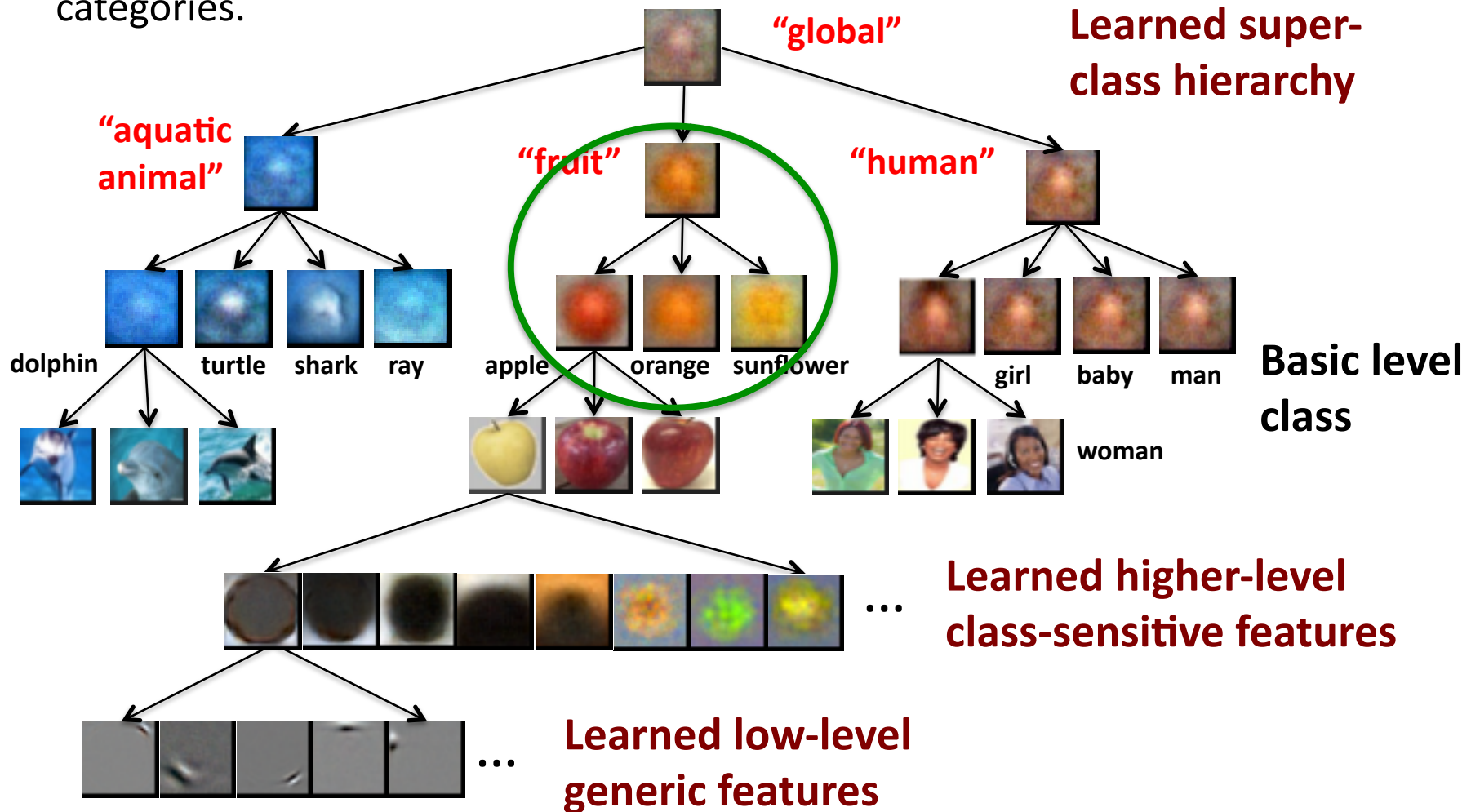
4 million unlabeled images



32 x 32 pixels x 3 RGB

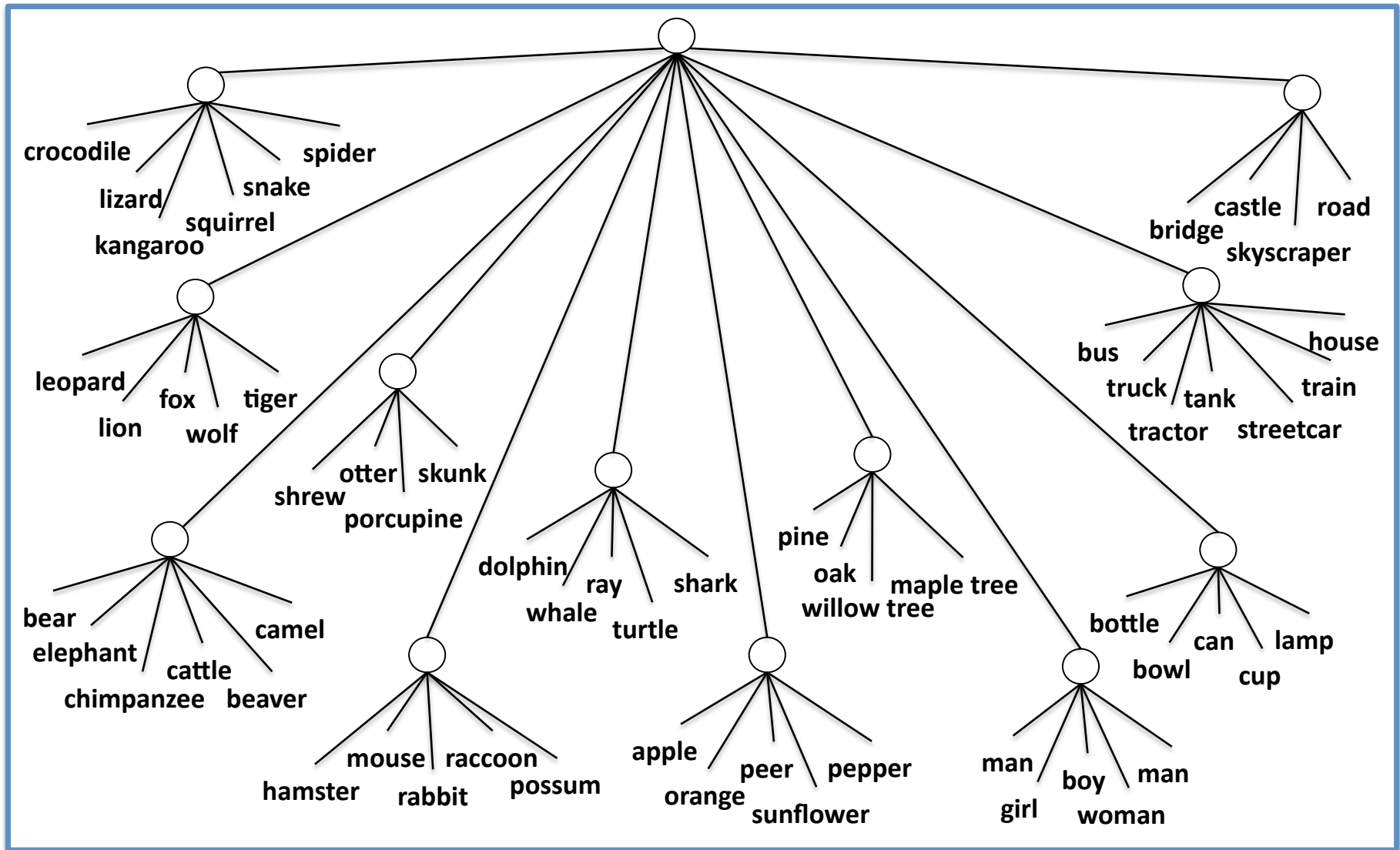
# Learning to Learn

The model learns how to share the knowledge across many visual categories.

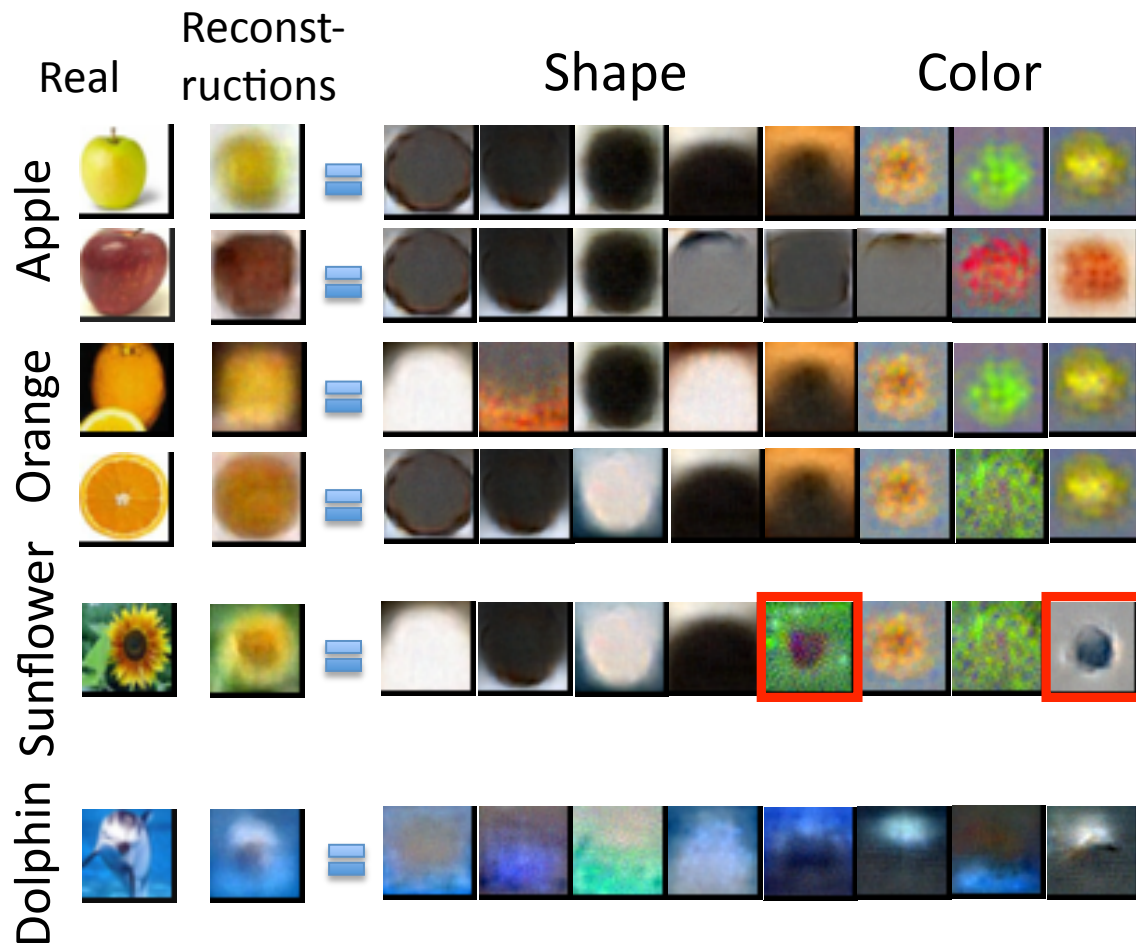


# Learning to Learn

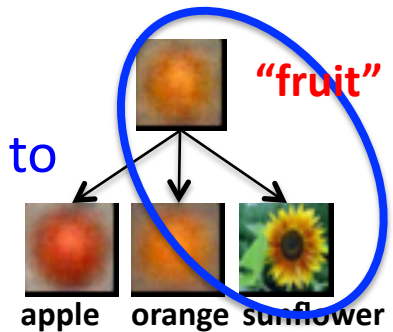
The model learns how to share the knowledge across many visual



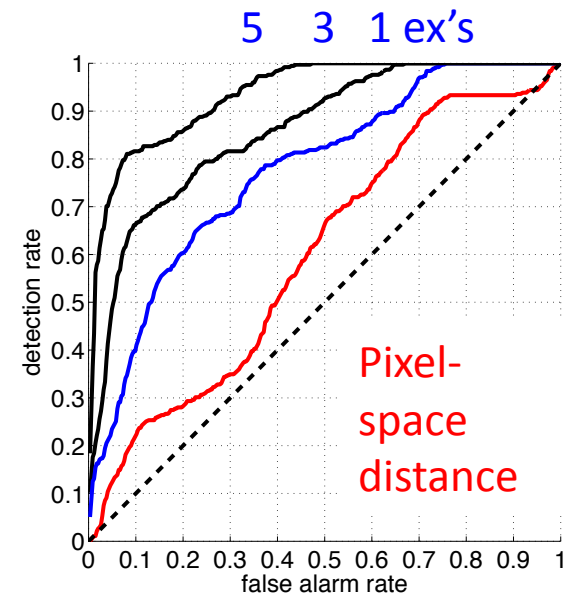
# Sharing Features



Learning to Learn



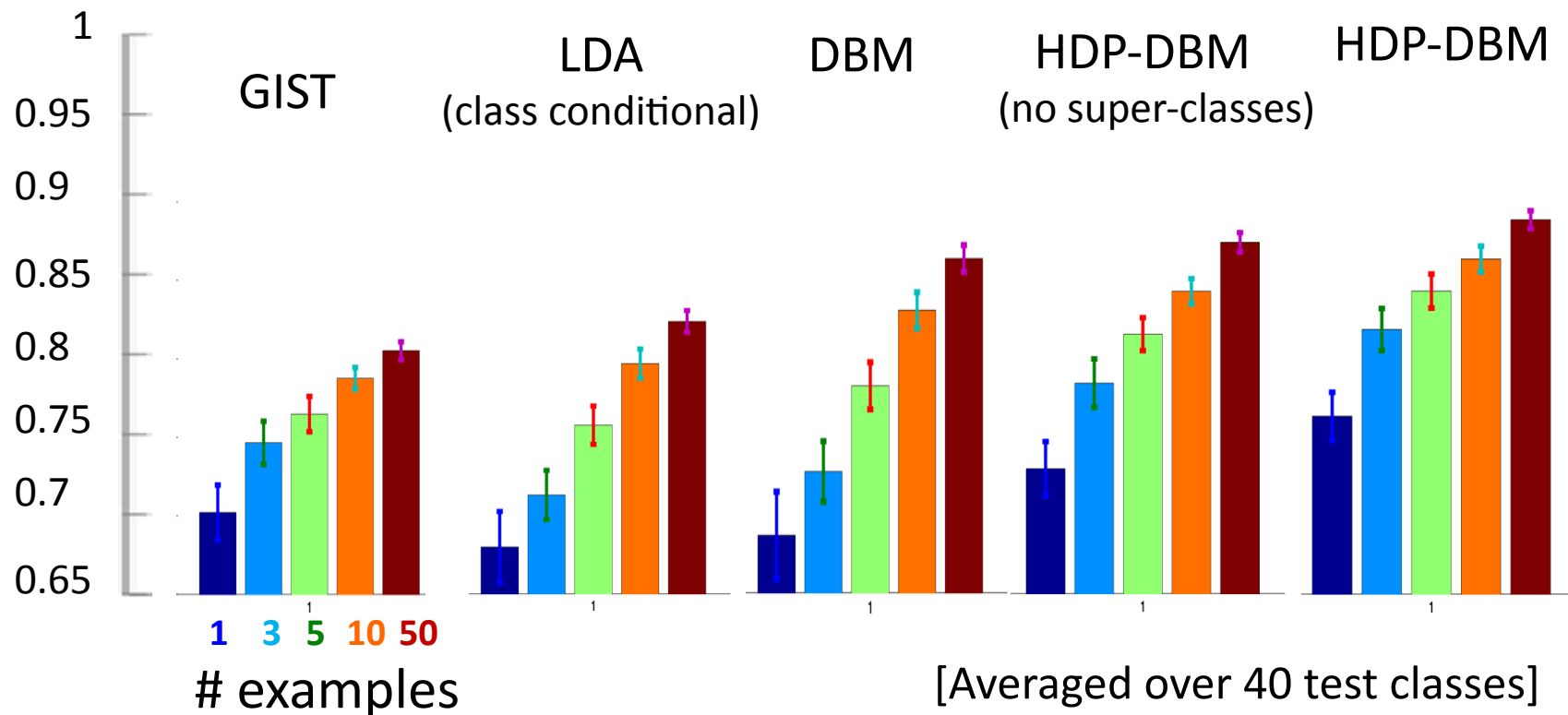
Sunflower ROC curve



**Learning to Learn:** Learning a hierarchy for sharing parameters – rapid learning of a novel concept.

# Object Recognition

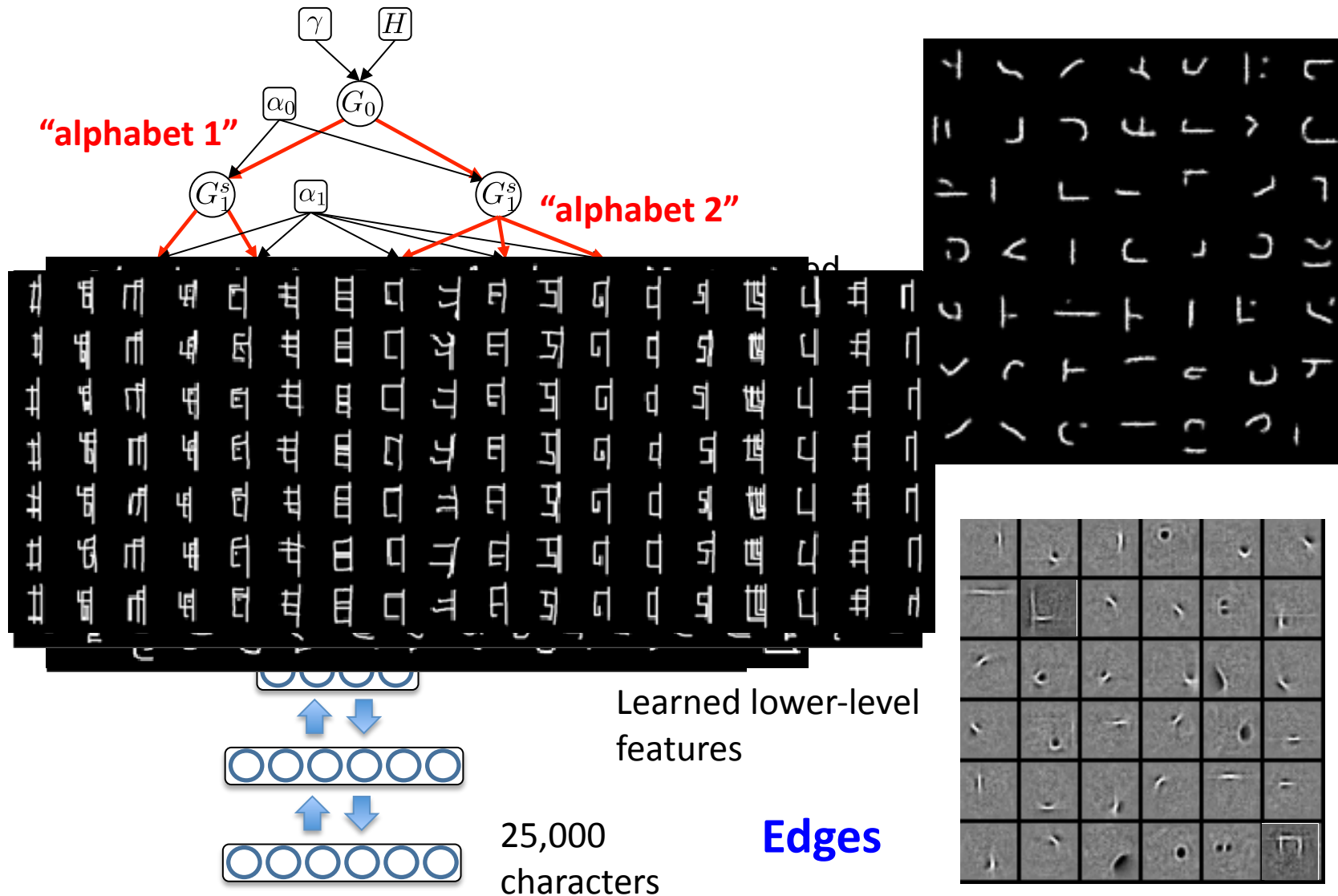
Area under ROC curve for same/different  
(1 new class vs. 99 distractor classes)



**Our model outperforms standard computer vision features (e.g. GIST).**

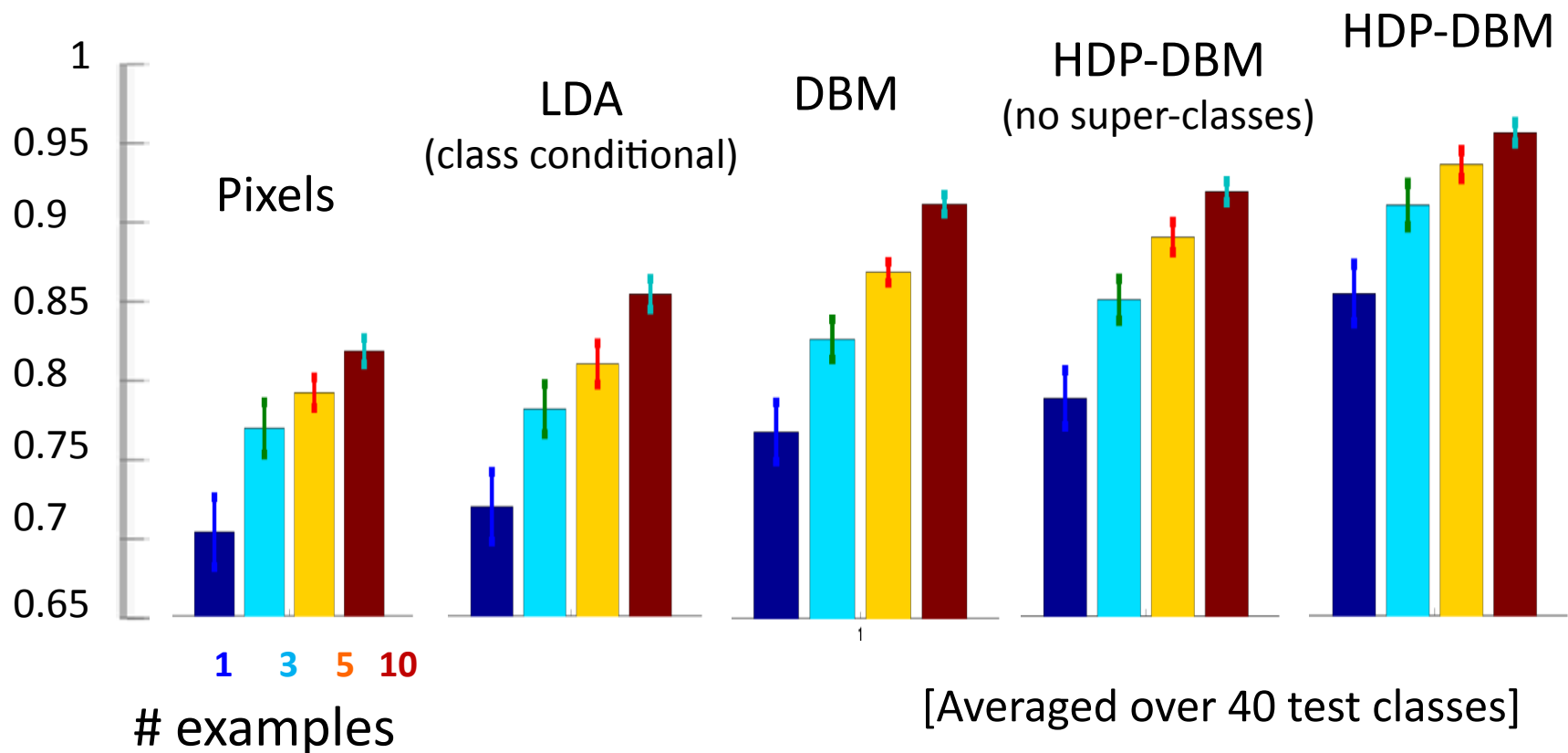


# Handwritten Character Recognition

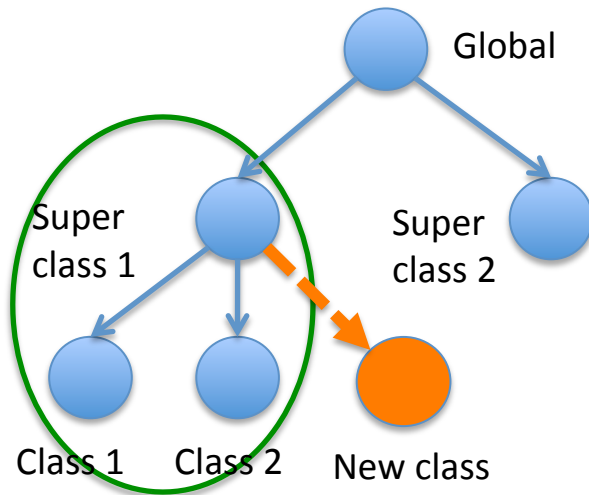


# Handwritten Character Recognition

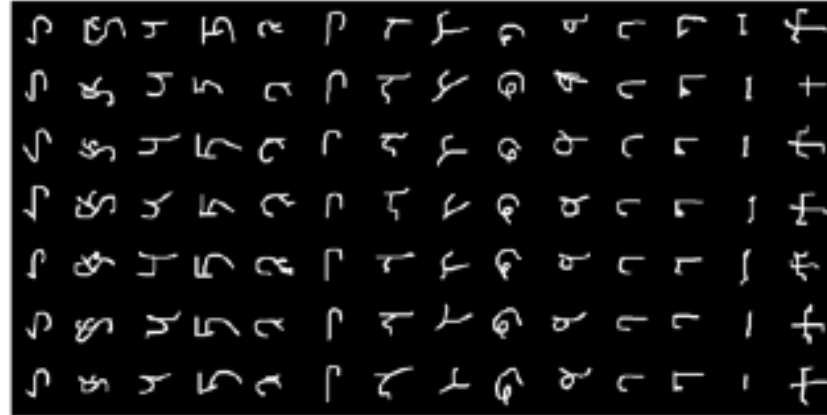
Area under ROC curve for same/different  
(1 new class vs. 1000 distractor classes)



# Simulating New Characters



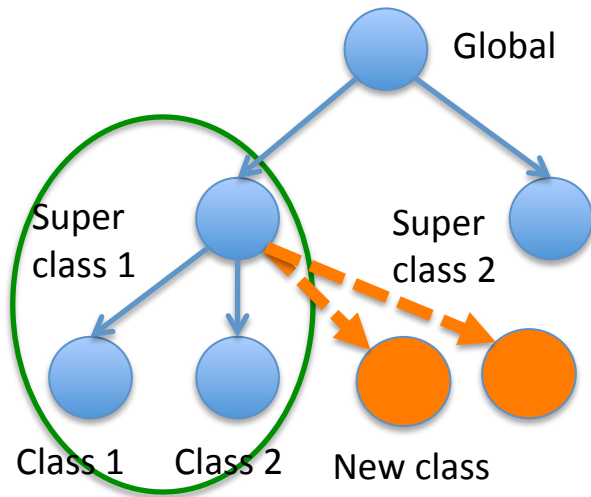
Real data within super class



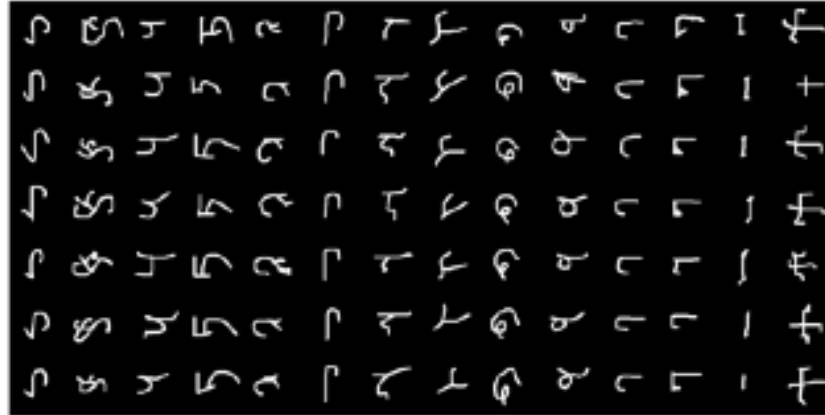
Simulated new characters



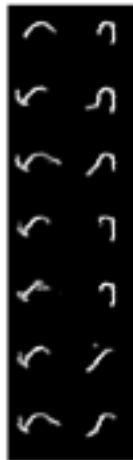
# Simulating New Characters



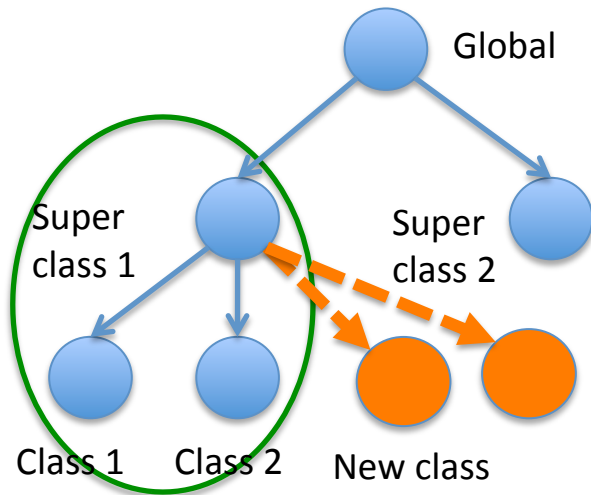
Real data within super class



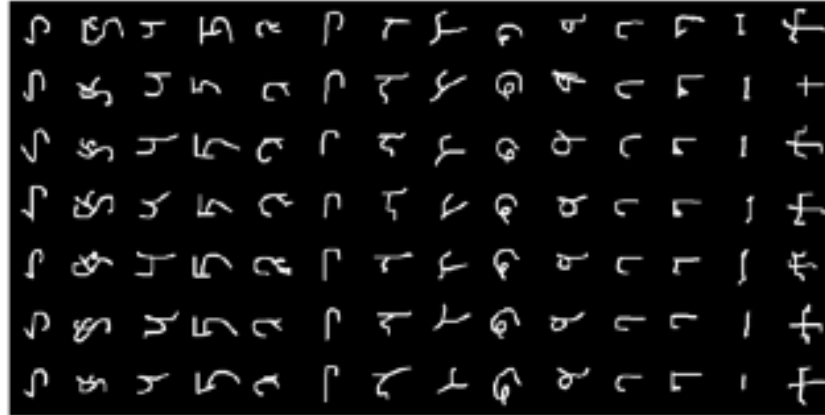
Simulated new characters



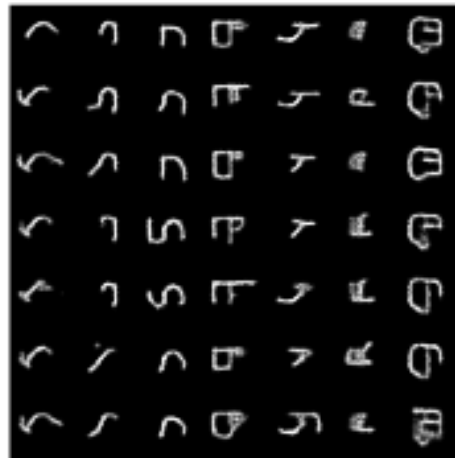
# Simulating New Characters



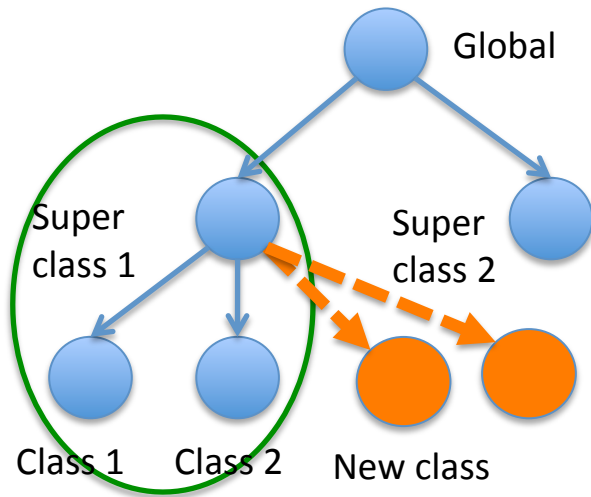
Real data within super class



Simulated new characters



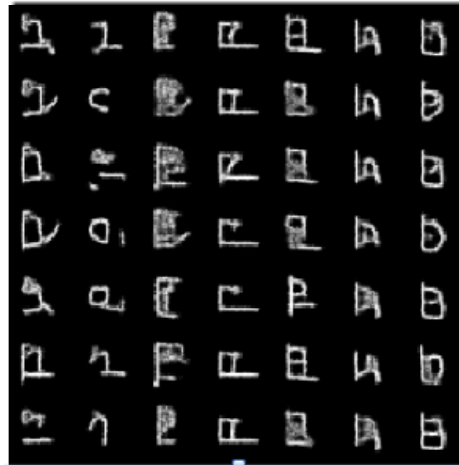
# Simulating New Characters



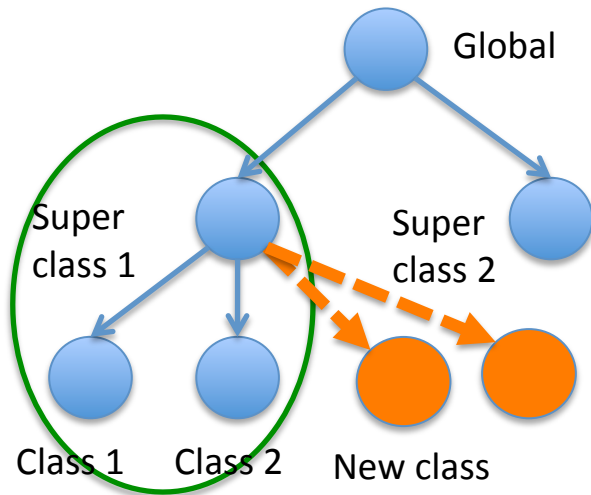
Real data within super class



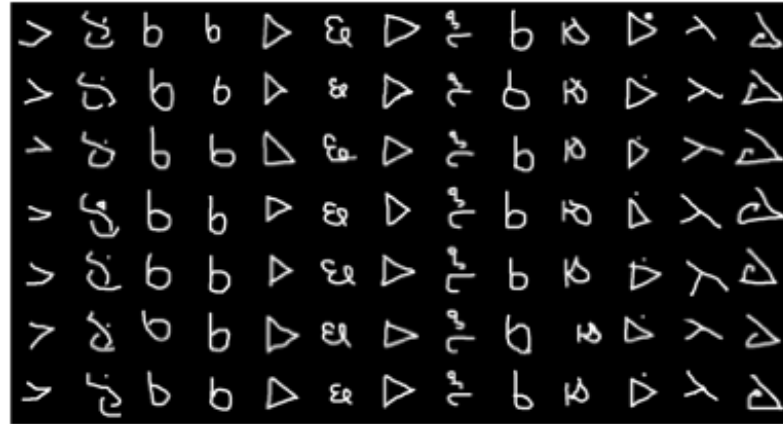
Simulated new characters



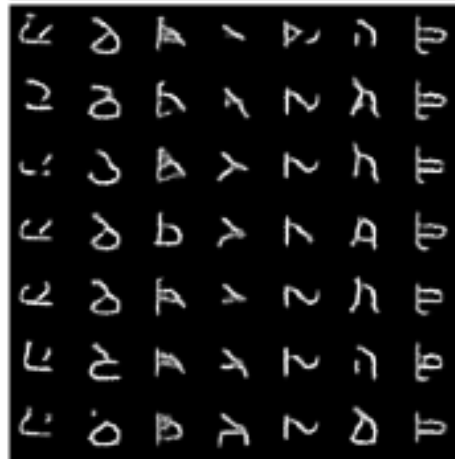
# Simulating New Characters



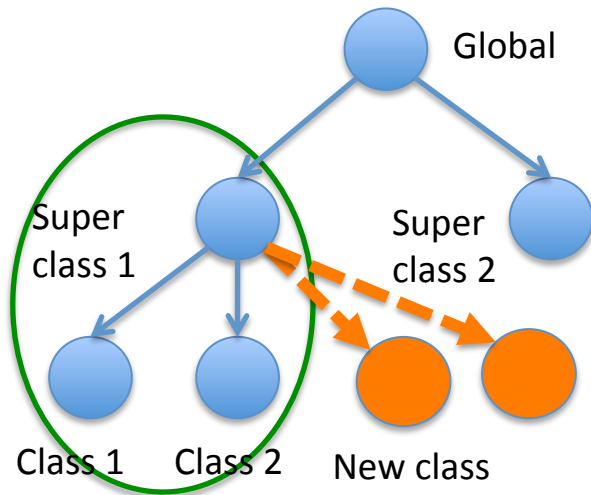
Real data within super class



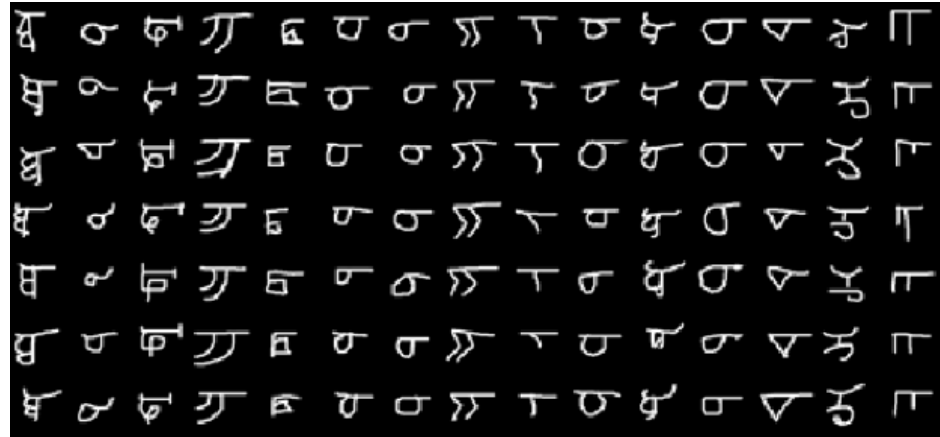
Simulated new characters



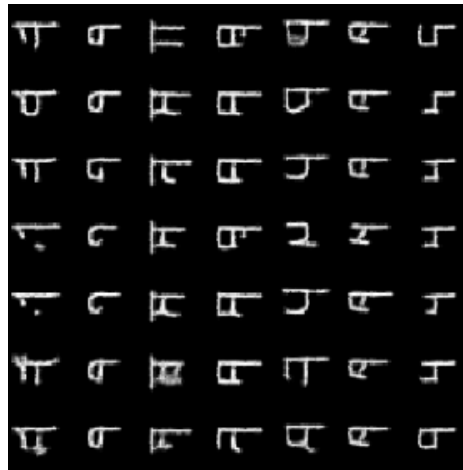
# Simulating New Characters



Real data within super class



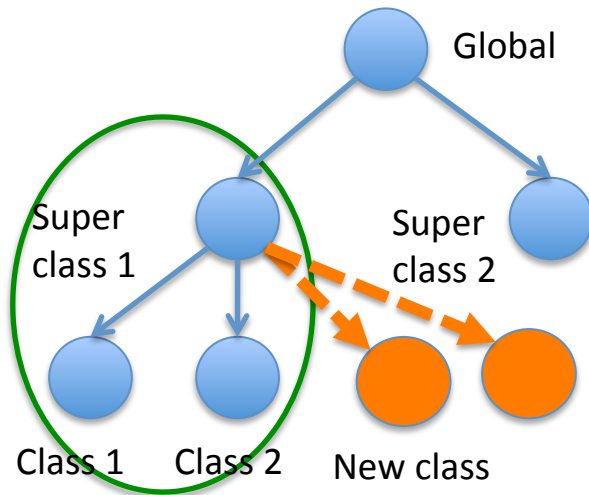
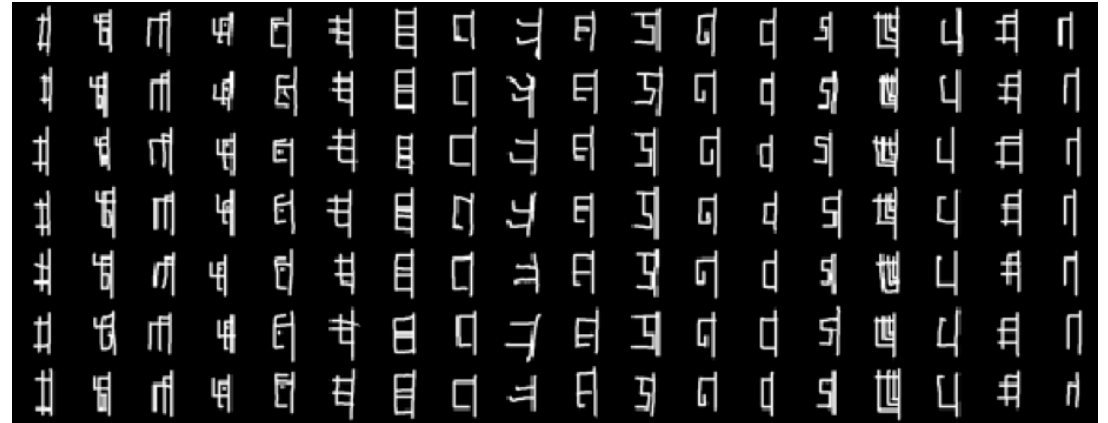
Simulated new characters



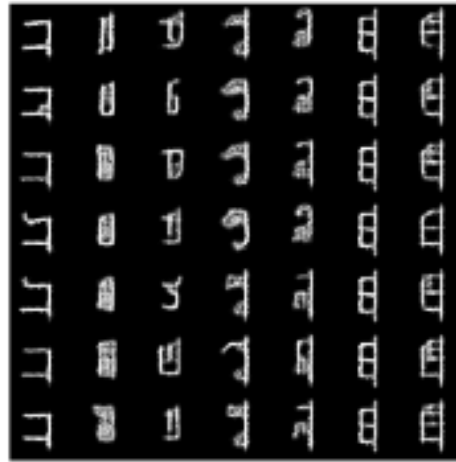


# Simulating New Characters

Real data within super class



Simulated new characters



# Learning from very few examples

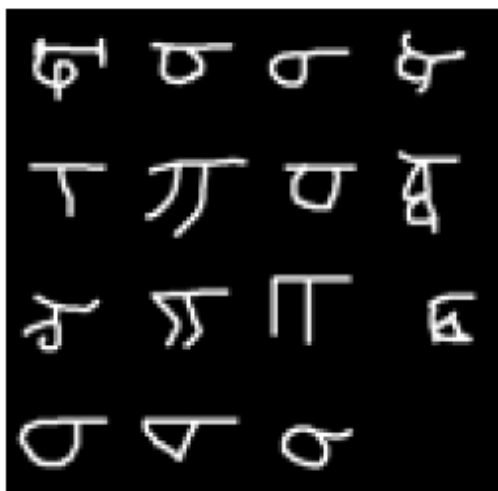
3 examples of  
a new class



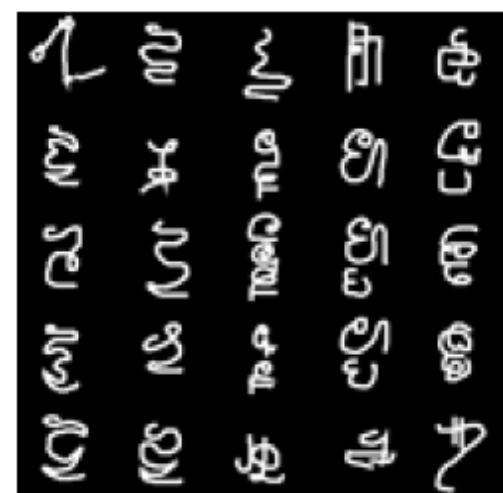
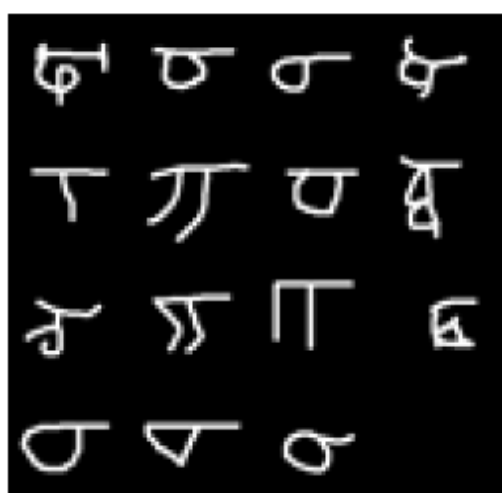
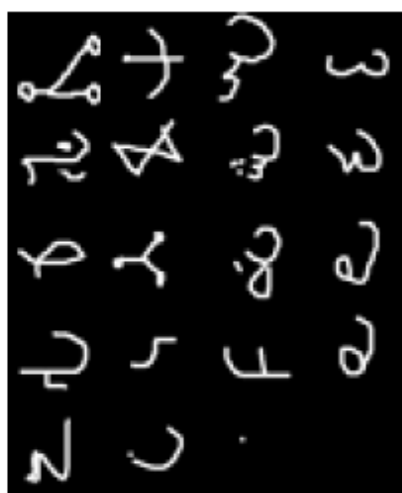
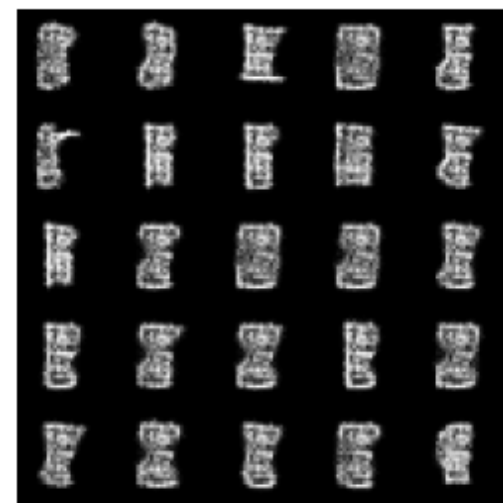
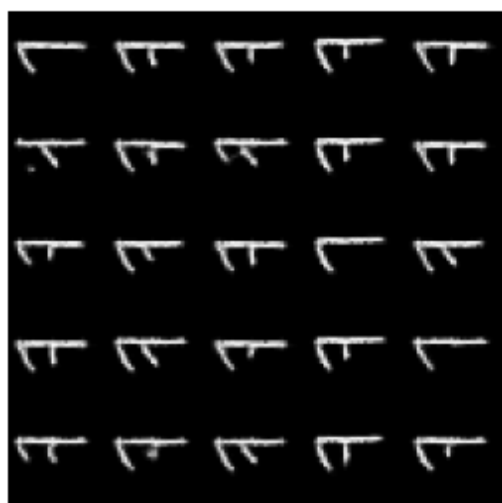
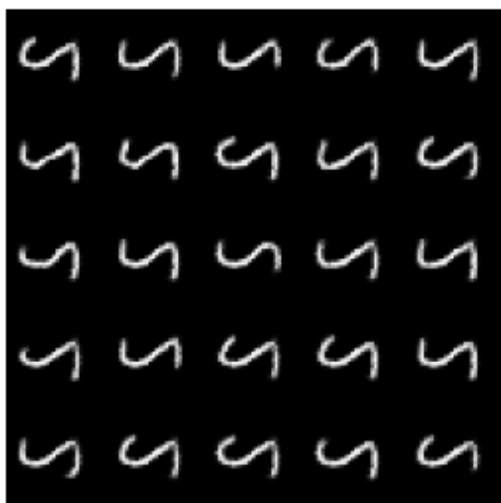
Conditional samples  
in the same class



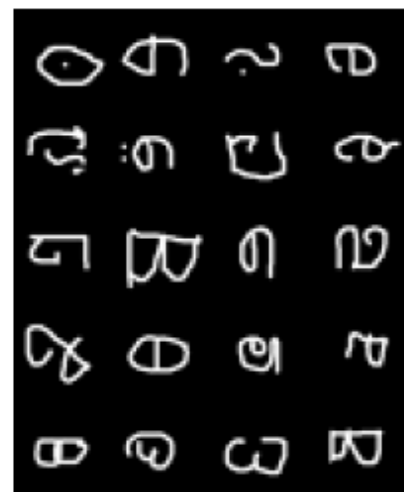
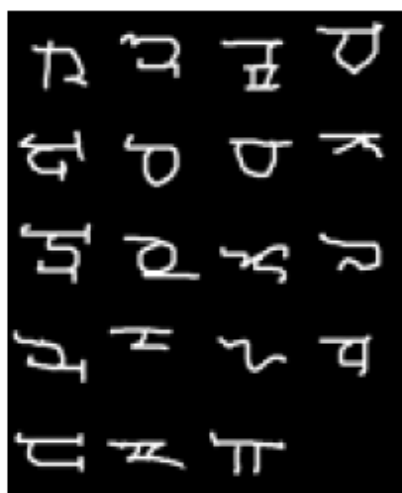
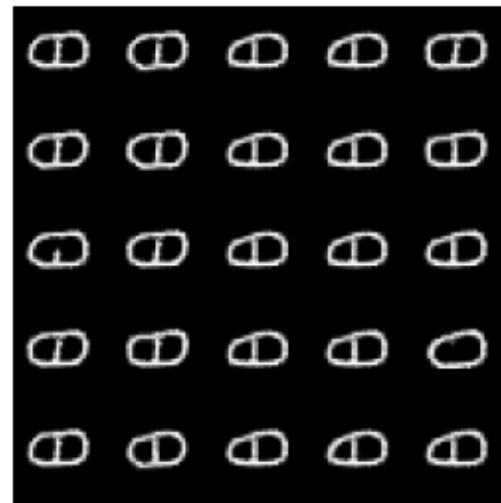
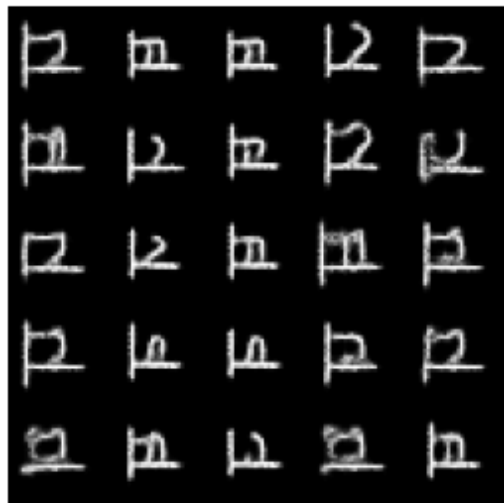
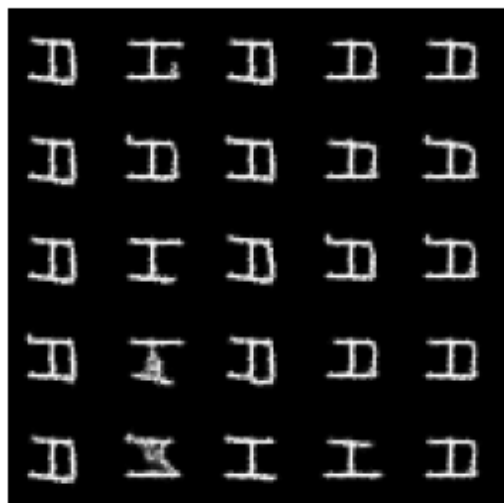
Inferred super-class



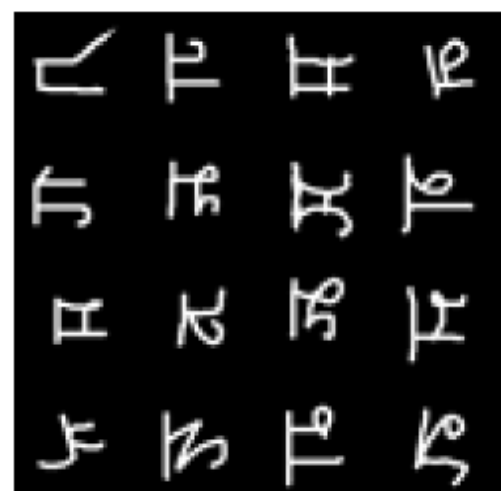
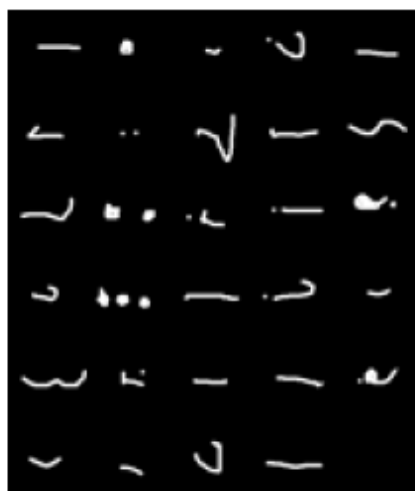
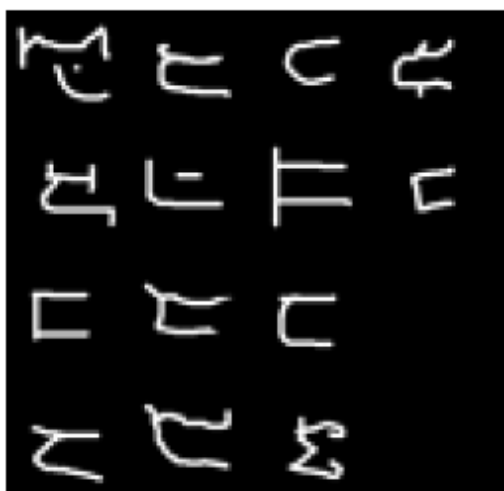
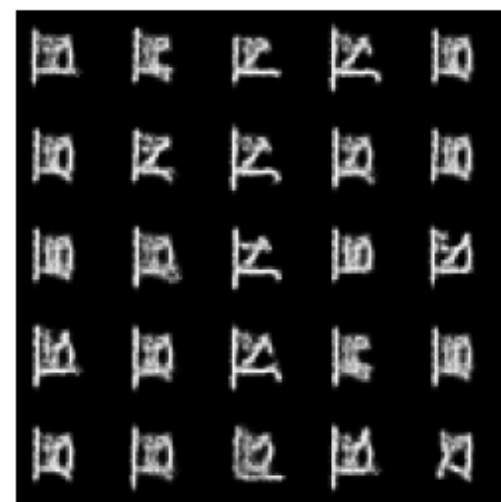
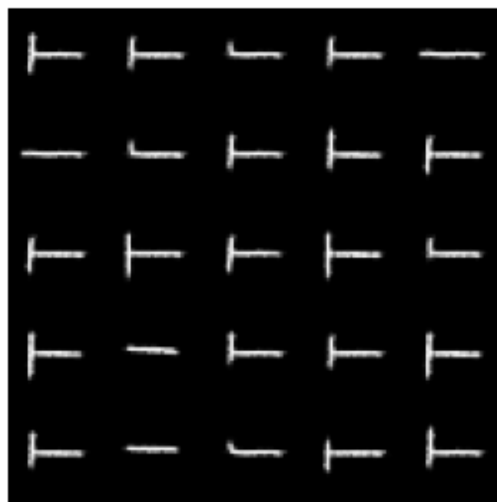
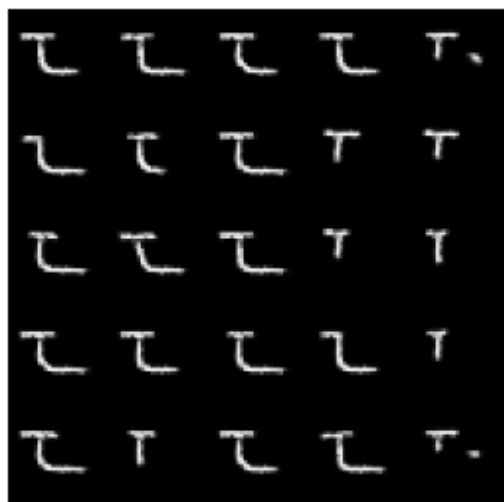
# Learning from very few examples



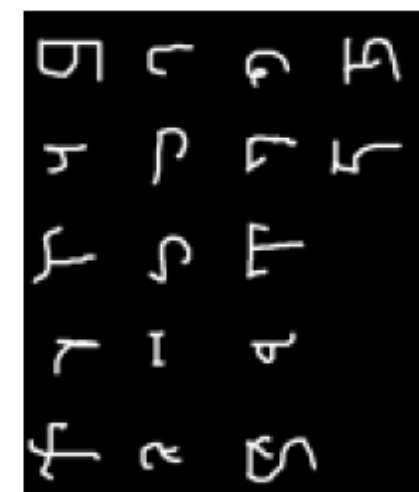
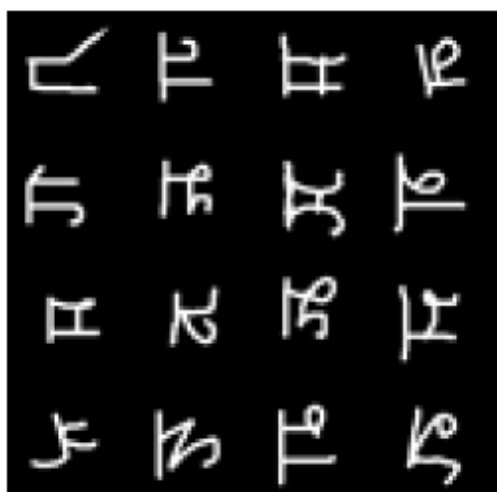
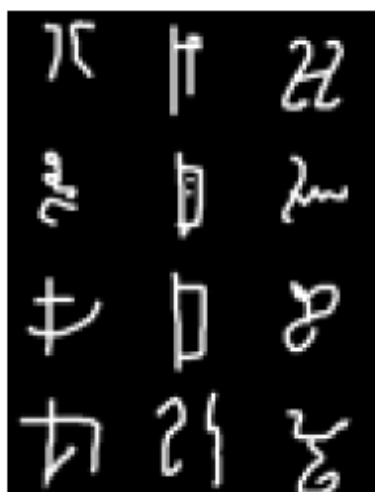
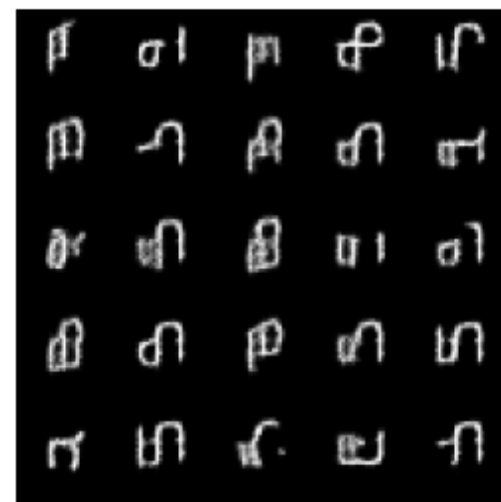
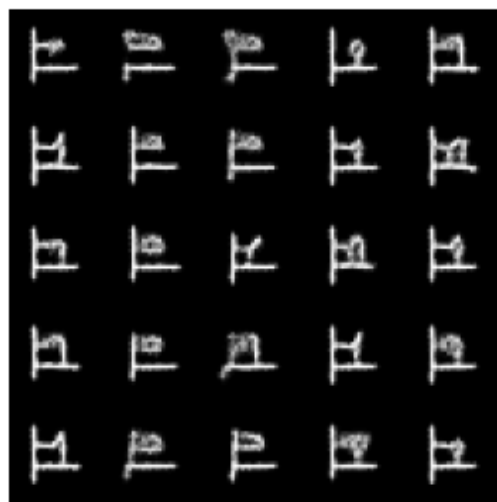
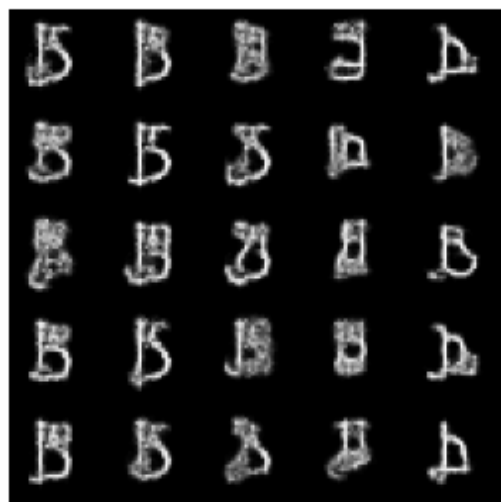
# Learning from very few examples



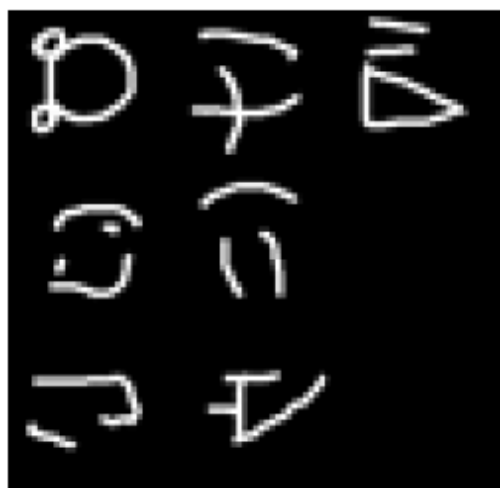
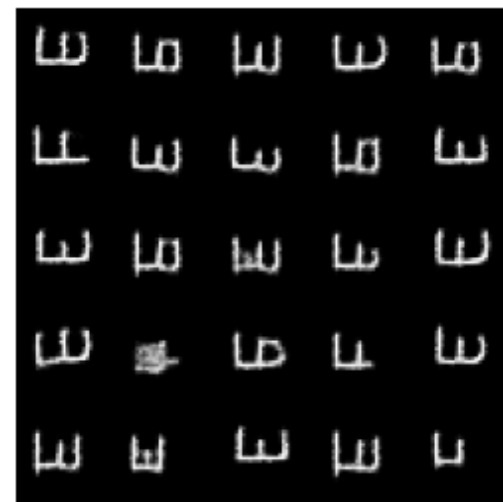
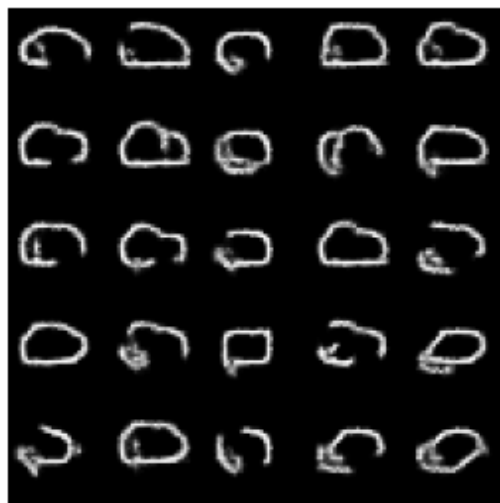
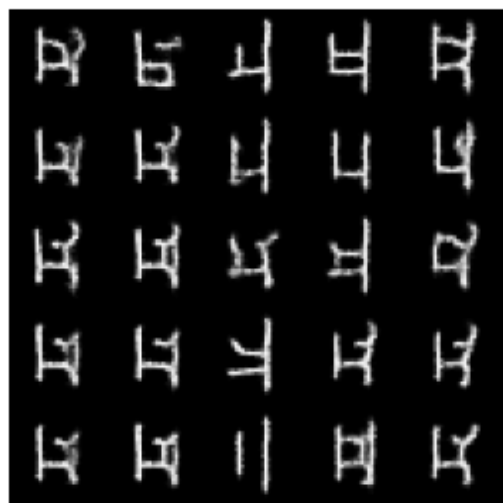
# Learning from very few examples



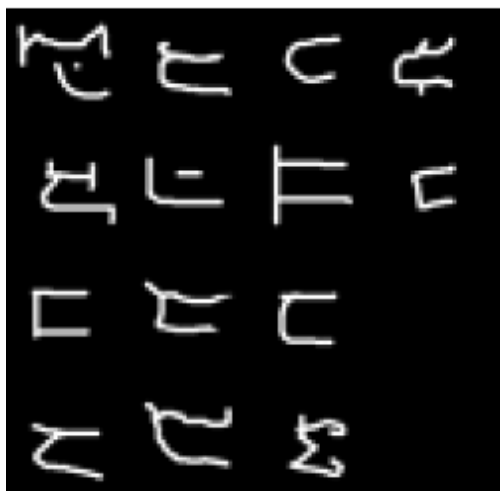
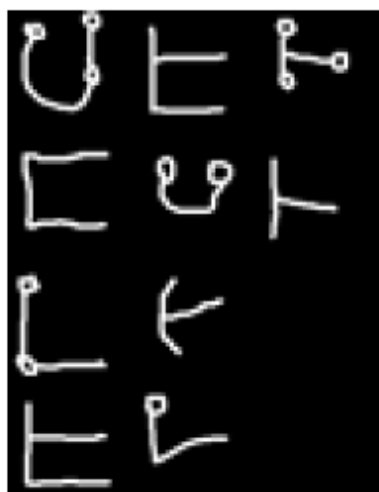
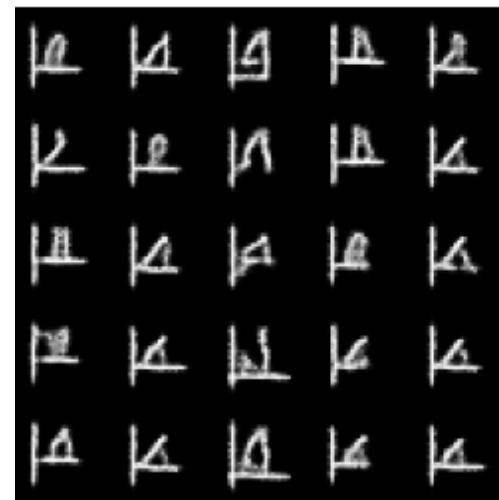
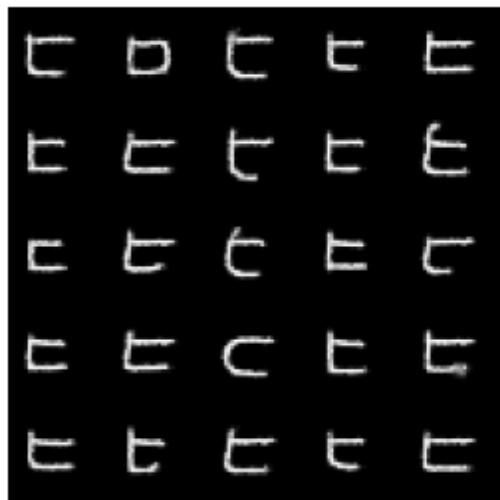
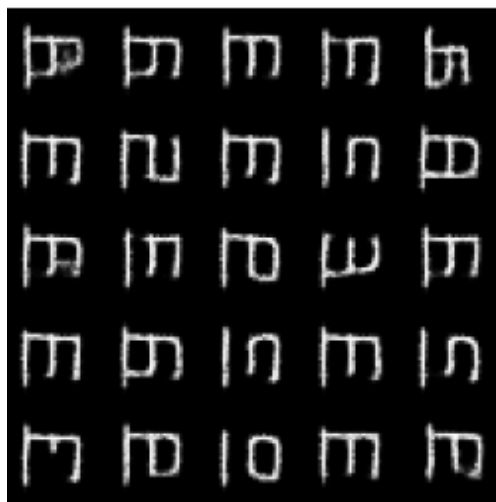
# Learning from very few examples



# Learning from very few examples

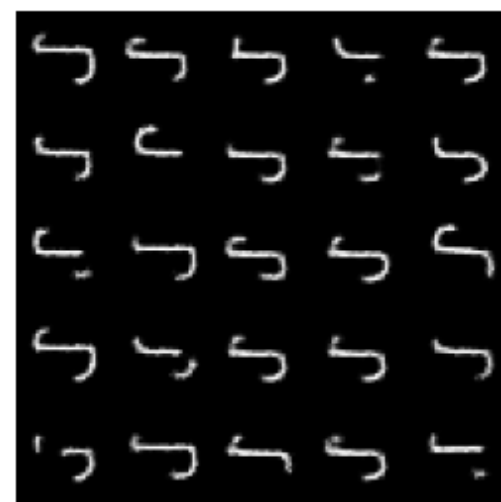
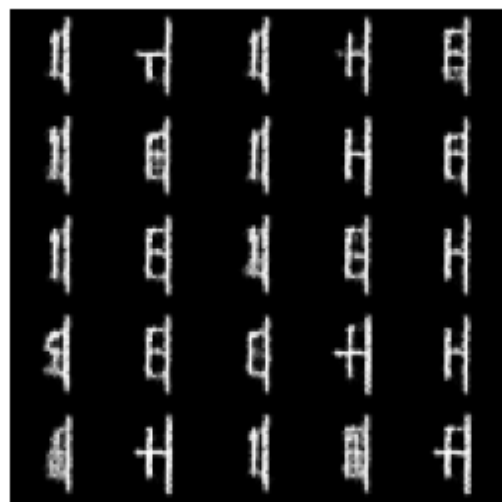
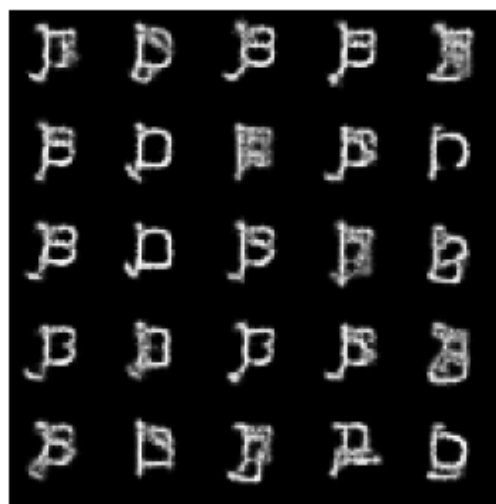


# Learning from very few examples

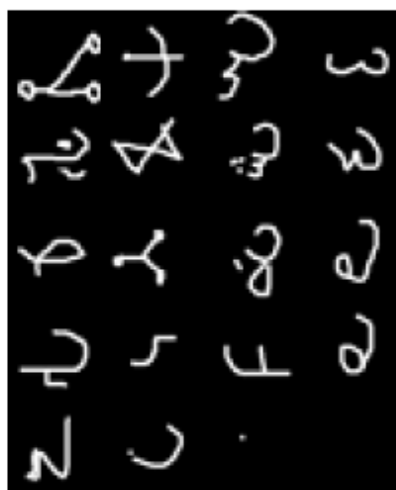
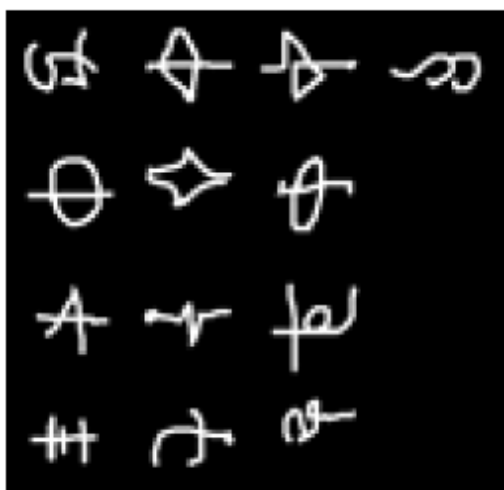
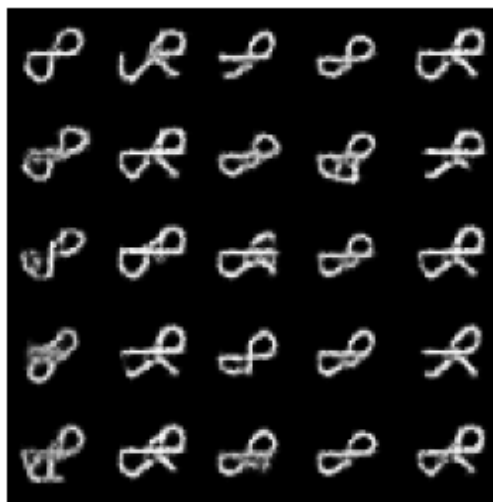
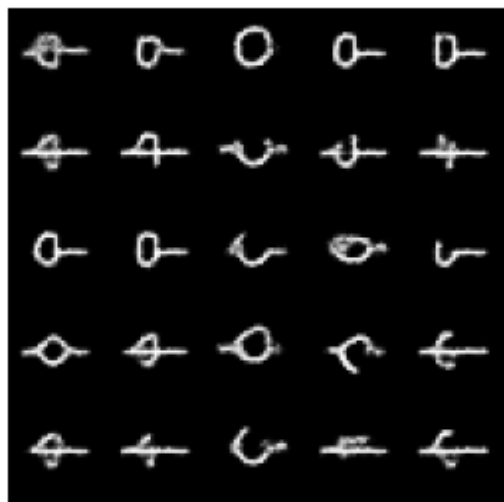




# Learning from very few examples

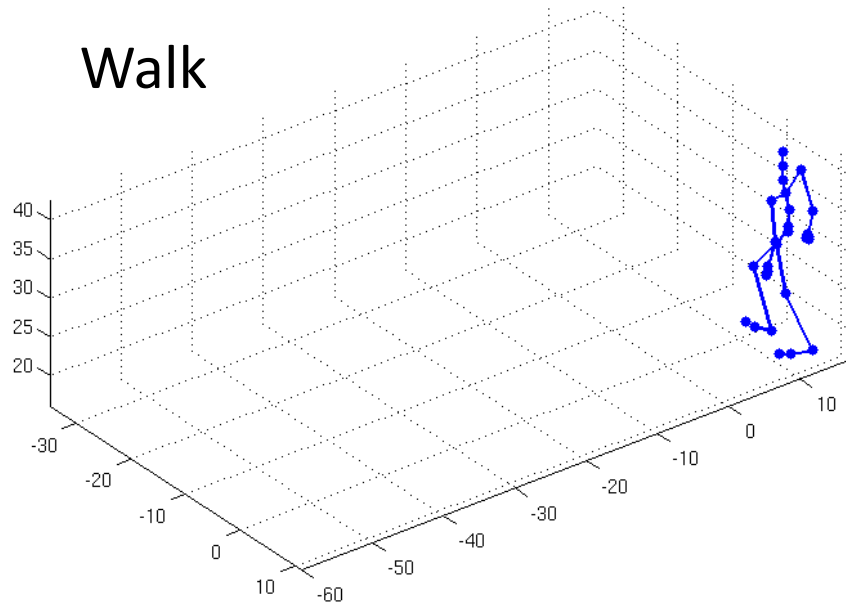


# Learning from very few examples

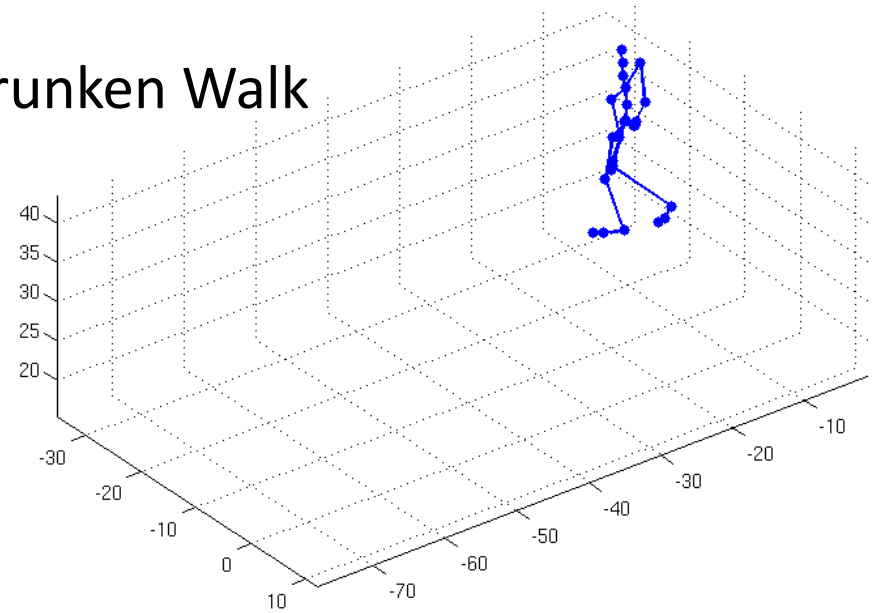


# Motion Capture

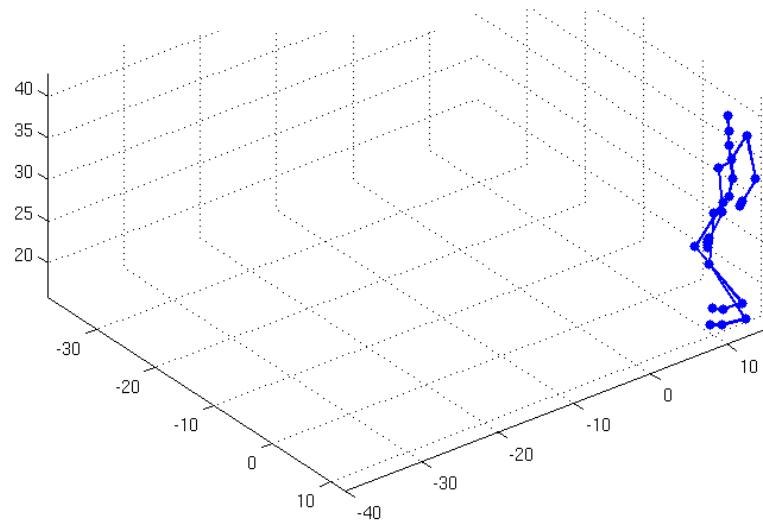
Walk



Drunken Walk

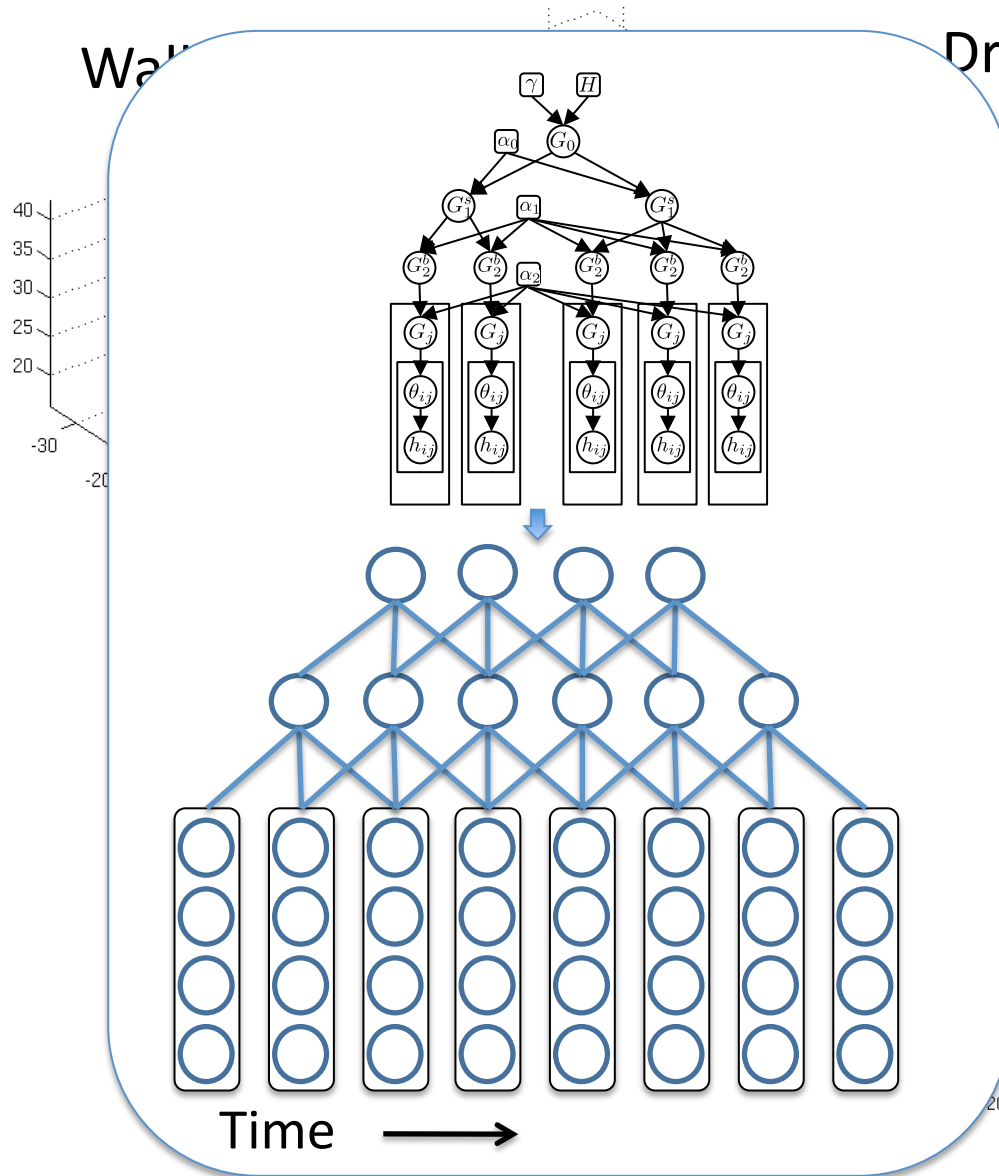


Sexy Walk

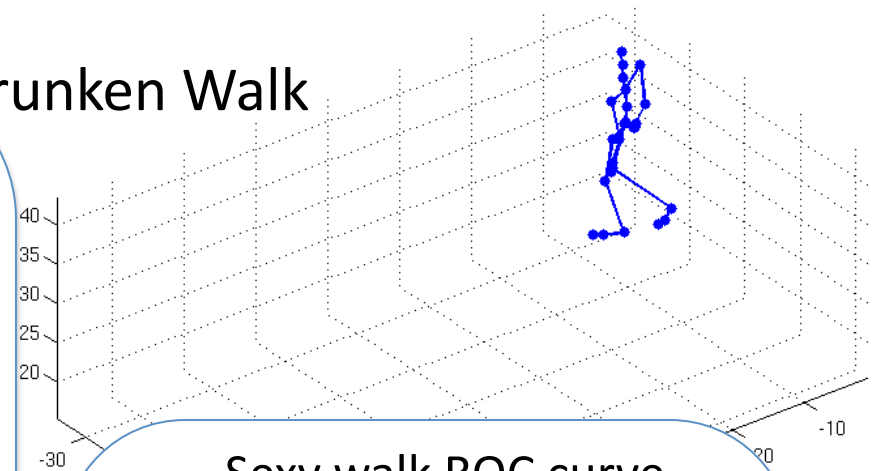


# Motion Capture

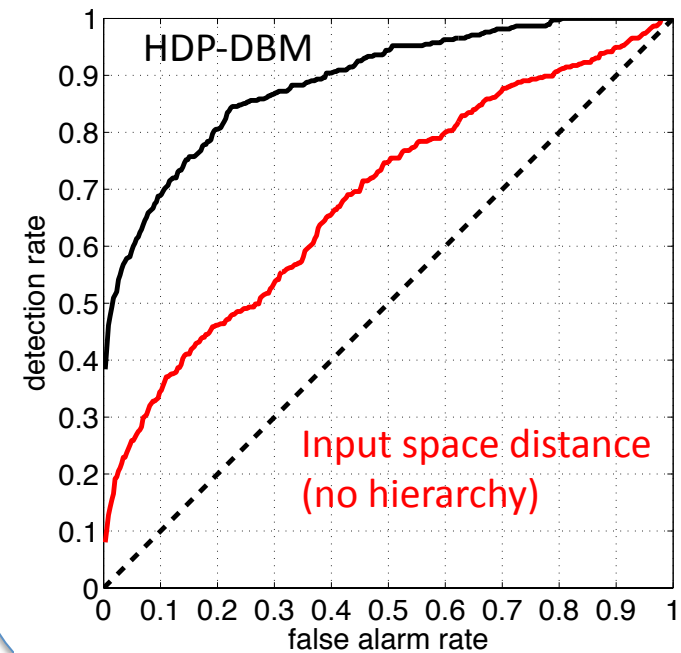
Walk



Drunken Walk



Sexy walk ROC curve

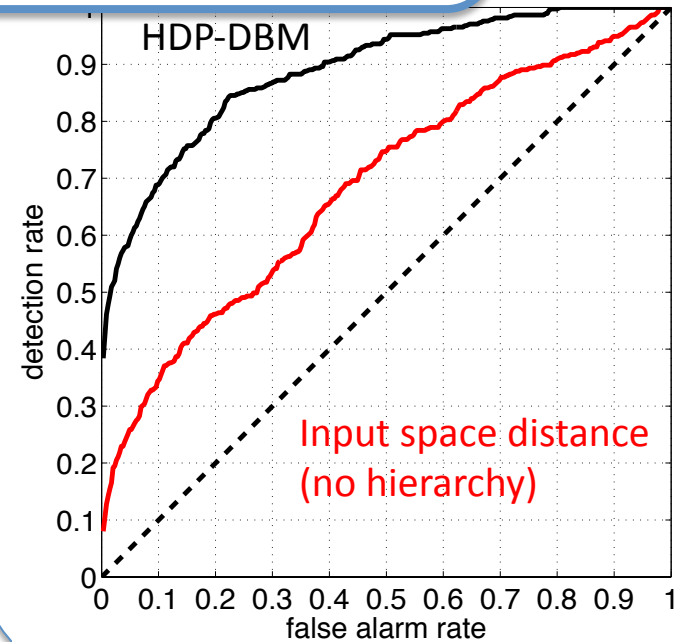
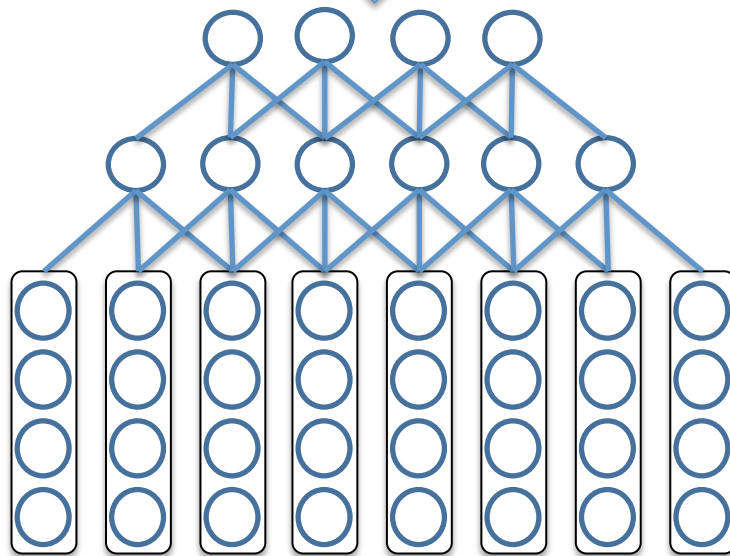


# Motion Capture

Walk

Drunken Walk

The same model can be applied to speech, text, video, or any other high-dimensional data.



# Other Hierarchical Models

At a minimum, object categorization requires information about

- category mean (prototype)
- variances along each dimension (similarity metric)



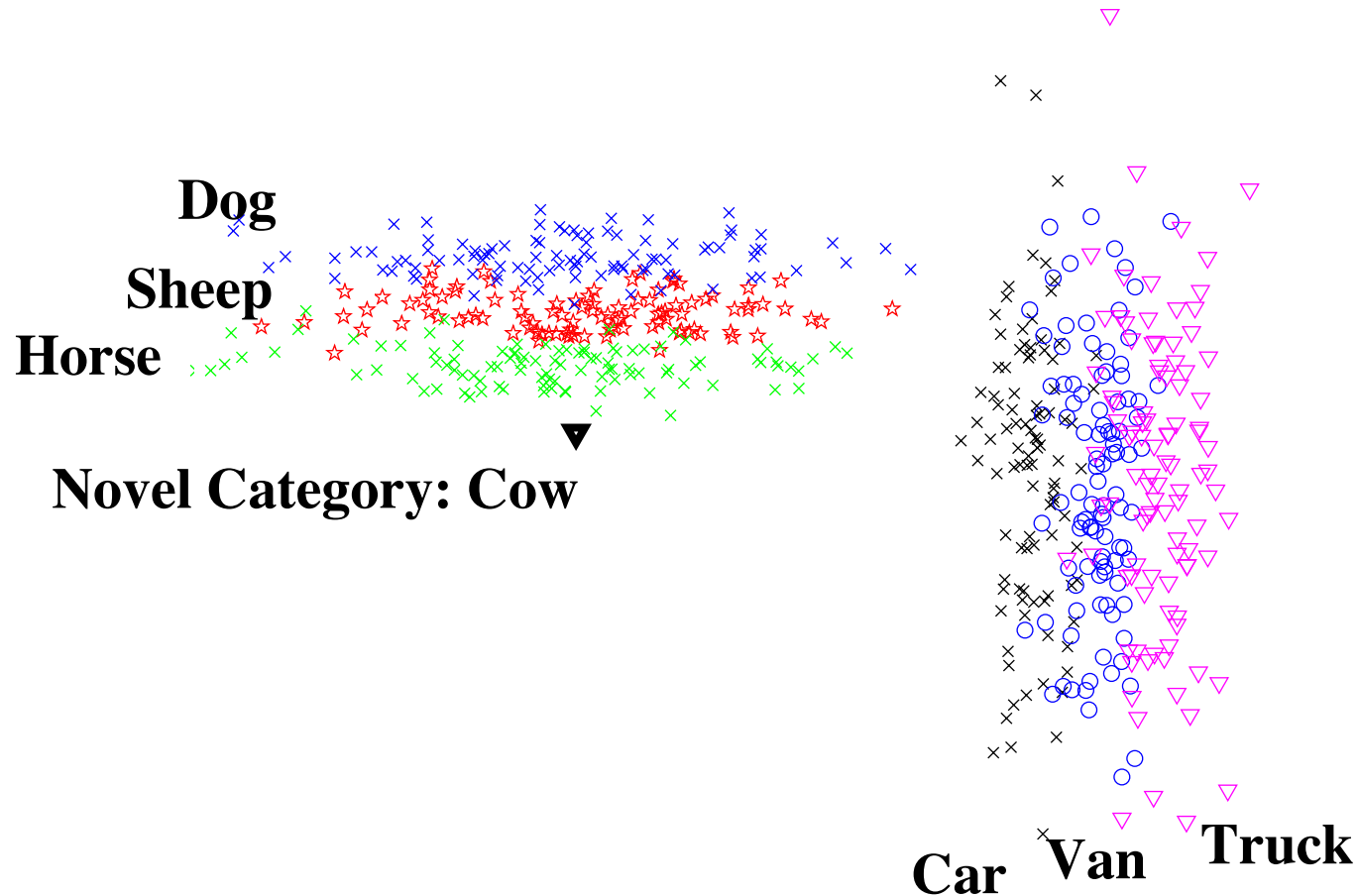
Color features vary strongly, whereas shape features vary weakly.



A single example provides some information about the prototype, but not about the variances.

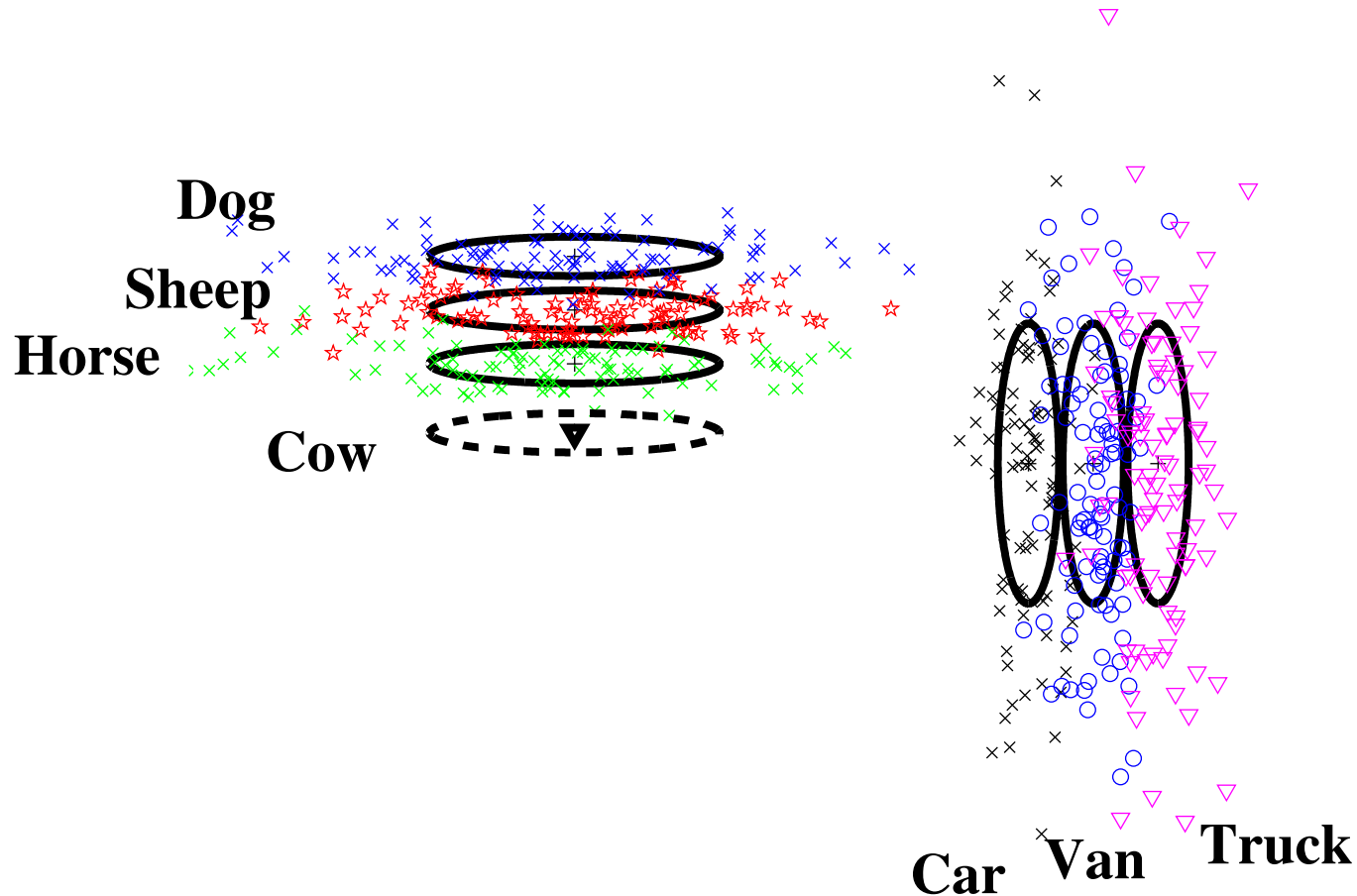
# Learning Class-Specific Similarity Metrics

(Salakhutdinov, Tenenbaum, & Torralba, 2010)



# Learning Class-Specific Similarity Metrics

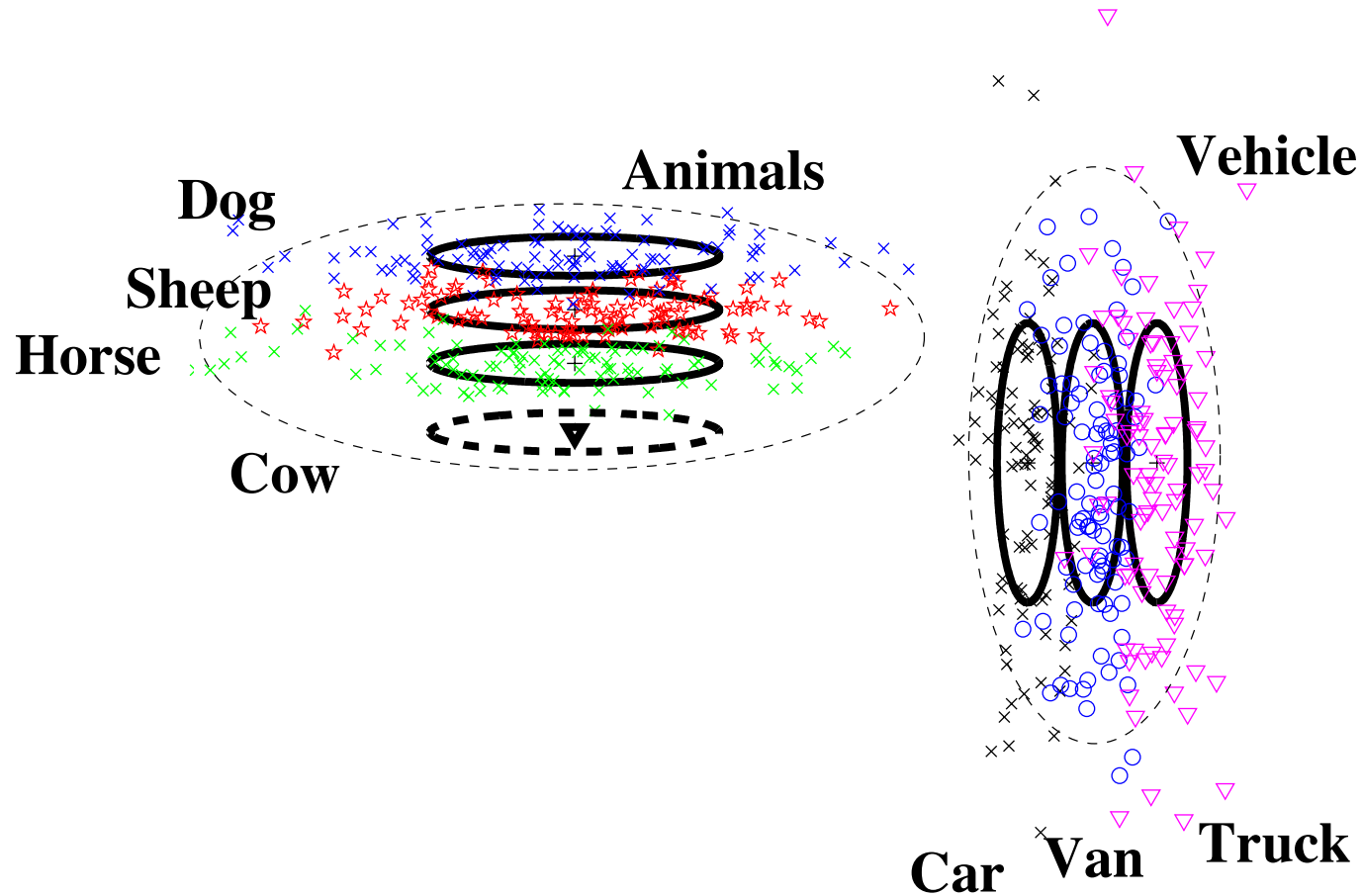
(Salakhutdinov, Tenenbaum, & Torralba, 2010)





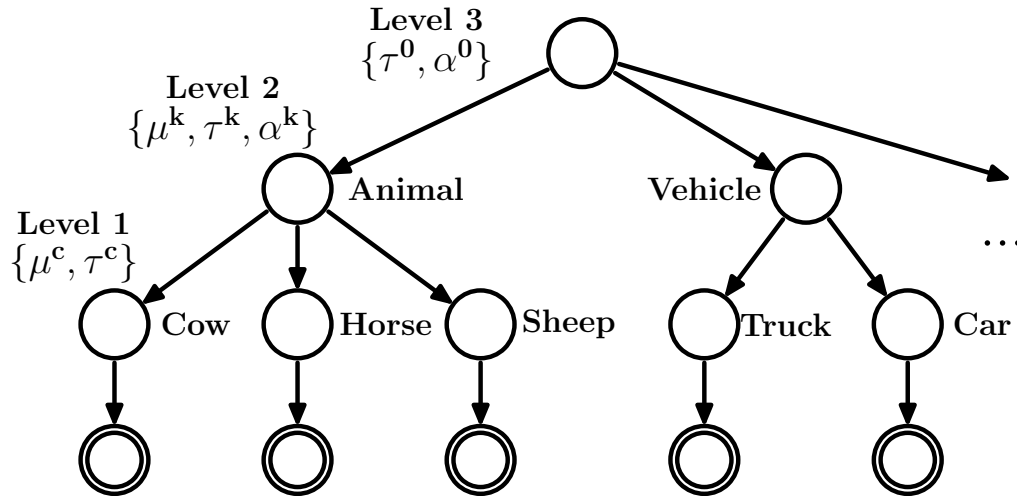
# Learning Class-Specific Similarity Metrics

(Salakhutdinov, Tenenbaum, & Torralba, 2010)



In order to transfer appropriate similarity metric, the model needs to discover how to group related categories into super-categories.

# Hierarchical Bayes



- Probabilistic linear model with Gaussian observation noise:

$$P(x|z = c) = N(\mu^c, 1/\tau^c)$$

- Place a conjugate Normal-Gamma prior over the means and precision parameters:

$$P(\mu^c, \tau^c) = \mathcal{N}(\mu^k 1/(\nu\tau^c))\Gamma(\alpha^k, \tau^k)$$

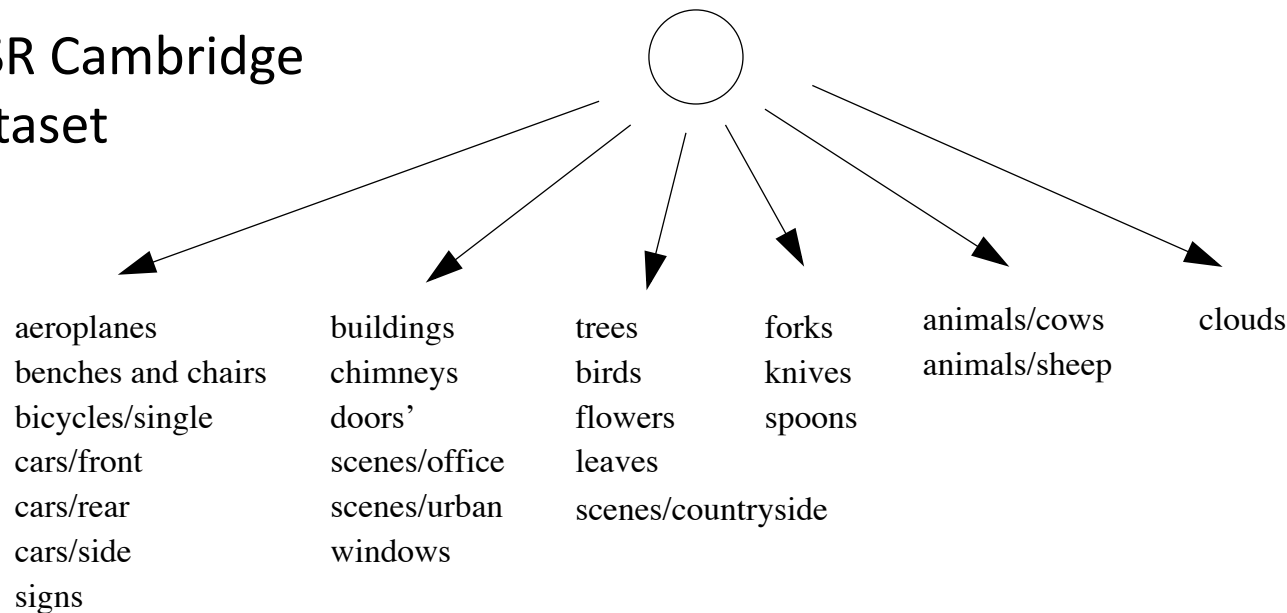
**Hierarchical Prior.**

As before, infer the hierarchy.

# Image Retrieval

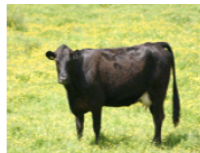
(Salakhutdinov, Tenenbaum, & Torralba, 2010)

## MSR Cambridge Dataset



## Retrieved images with our model

### Query image



Given only one  
examples of a cpw



## Nearest neighbor

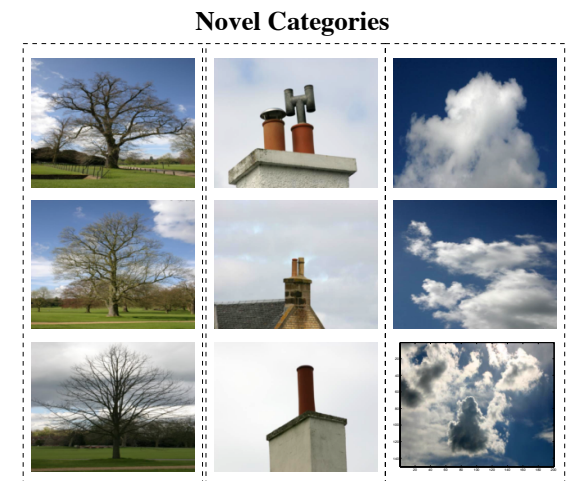
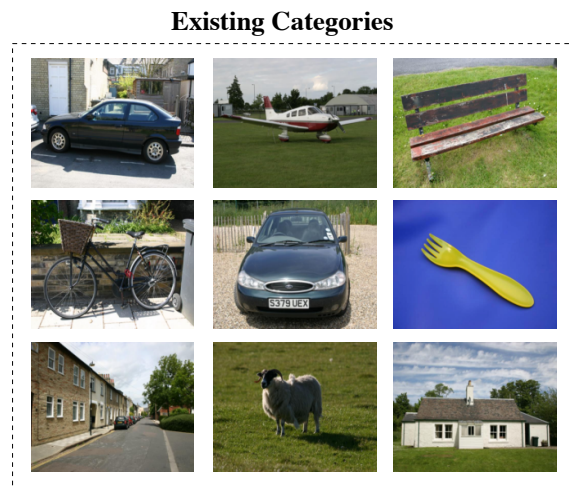
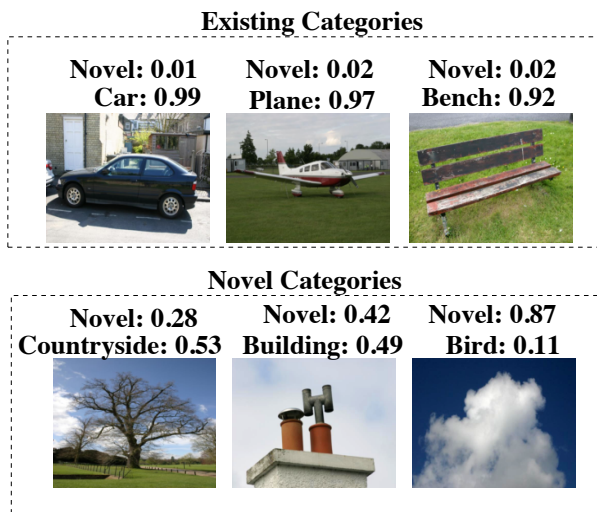


# Unsupervised Category Discovery

(Salakhutdinov, Tenenbaum, & Torralba, 2010)

Can we discover when the model has encountered novel categories, and how can we break up new instances into novel categories?

The test set consists of **many unlabeled examples from an unknown number of basic-level classes.**



With 18 unlabeled test images the model correctly places nine familiar images in nine different basic-level categories, while also correctly forming three novel categories with 3 examples each.

# Object Detection Challenge

Consider challenging object detection task.



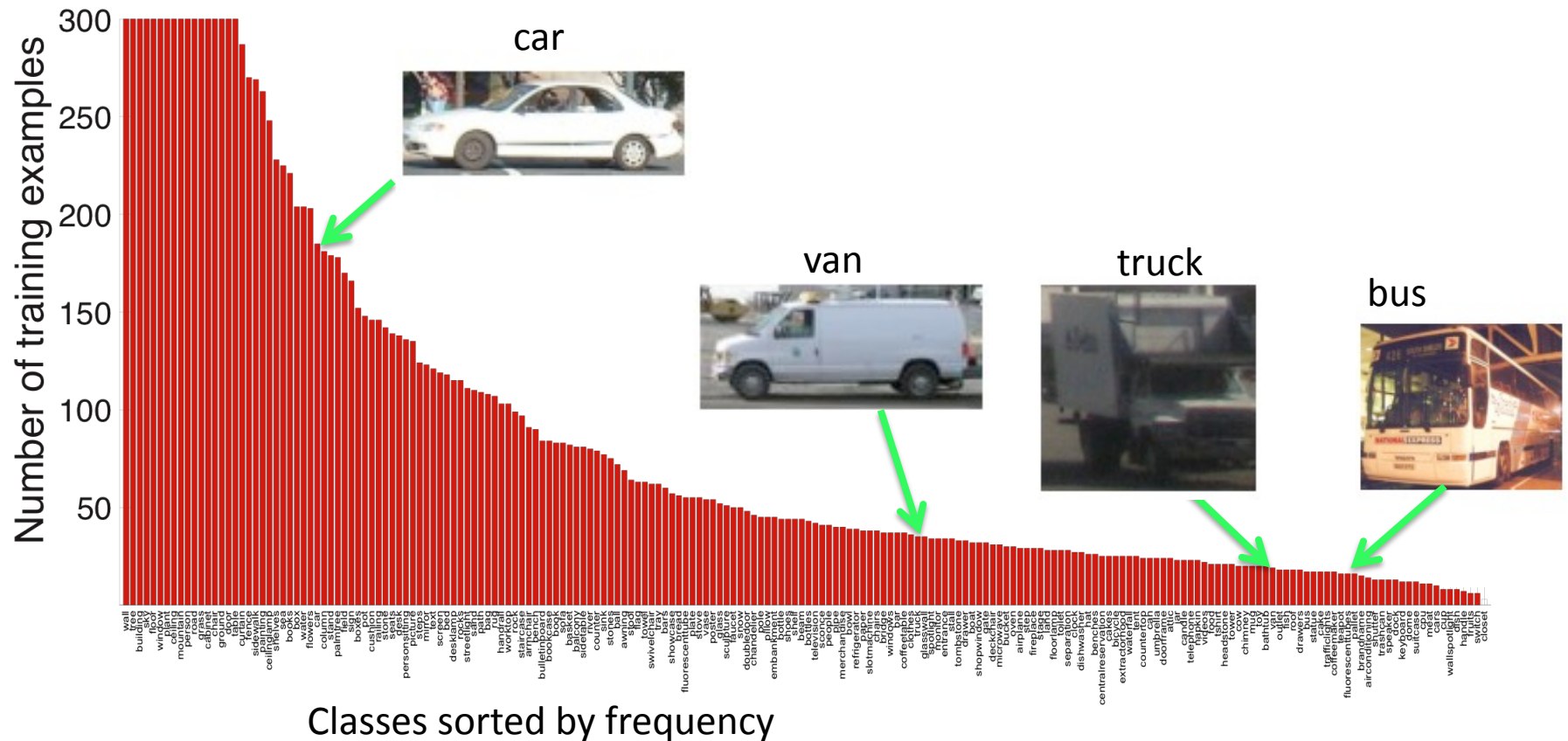
By looking at the output of a detector, can you guess which object is it trying to detect?

Slide credit: Antonio Torralba

# Learning from Few Examples

(Salakhutdinov, Torralba, & Tenenbaum, CVPR 2011)

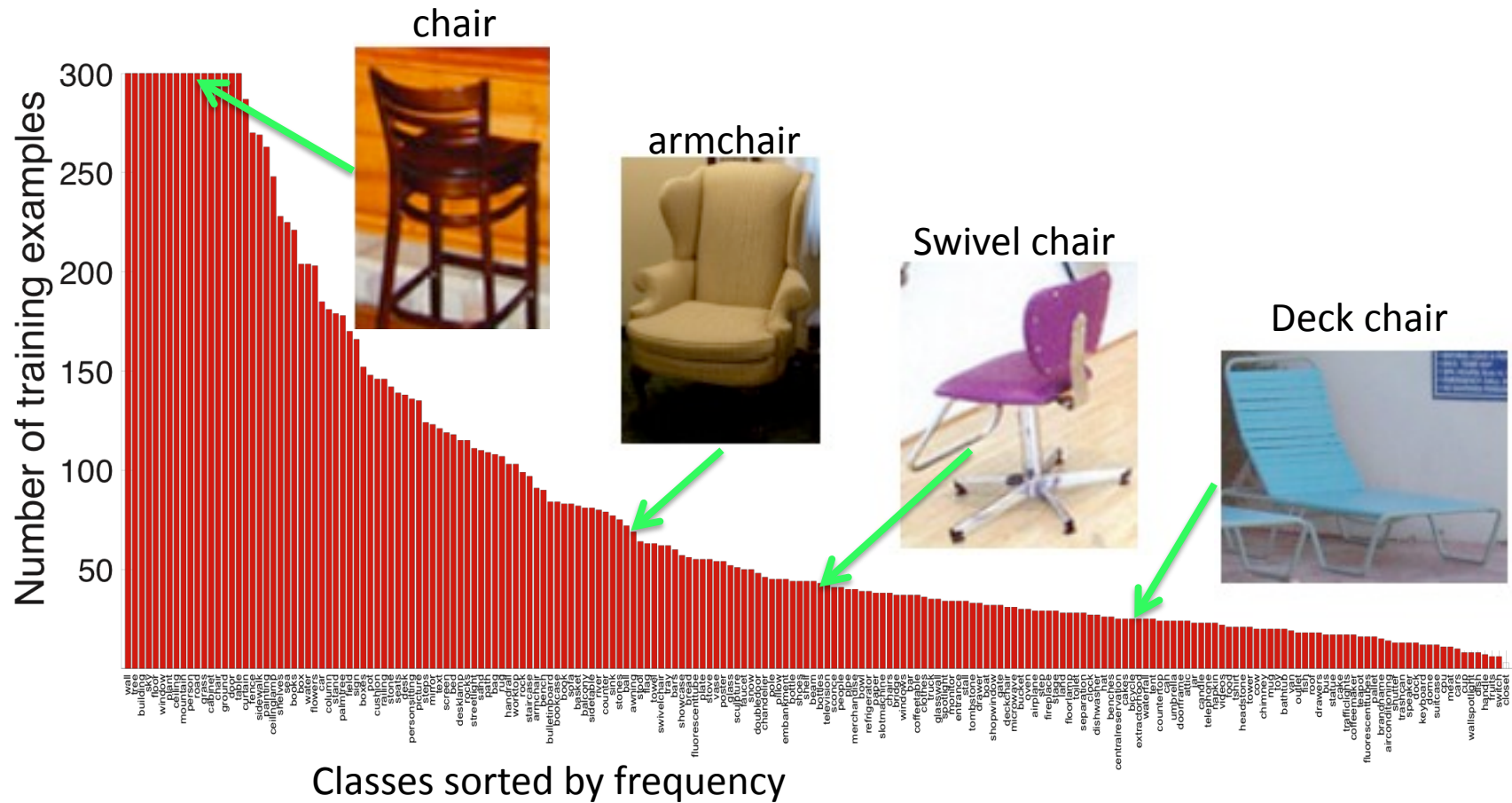
## SUN database



Rare objects are similar to frequent objects

# Learning from Few Examples

(Salakhutdinov, Torralba, & Tenenbaum, CVPR 2011)





# Generative Model of Classifier Parameters

(Salakhutdinov, Torralba, & Tenenbaum, CVPR 2011)

Many state-of-the-art object detection systems use sophisticated models, based on multiple parts with separate appearance and shape components.

$$y = \beta^{\top} \Phi(\mathbf{x})$$



Detect objects by testing sub-windows and scoring corresponding test patches with a linear function.

**We can define hierarchical prior over parameters of discriminative model and learn the hierarchy.**

**Image Specific:** concatenation of the HOG feature pyramid at multiple scales.

Felzenszwalb, McAllester & Ramanan, 2008

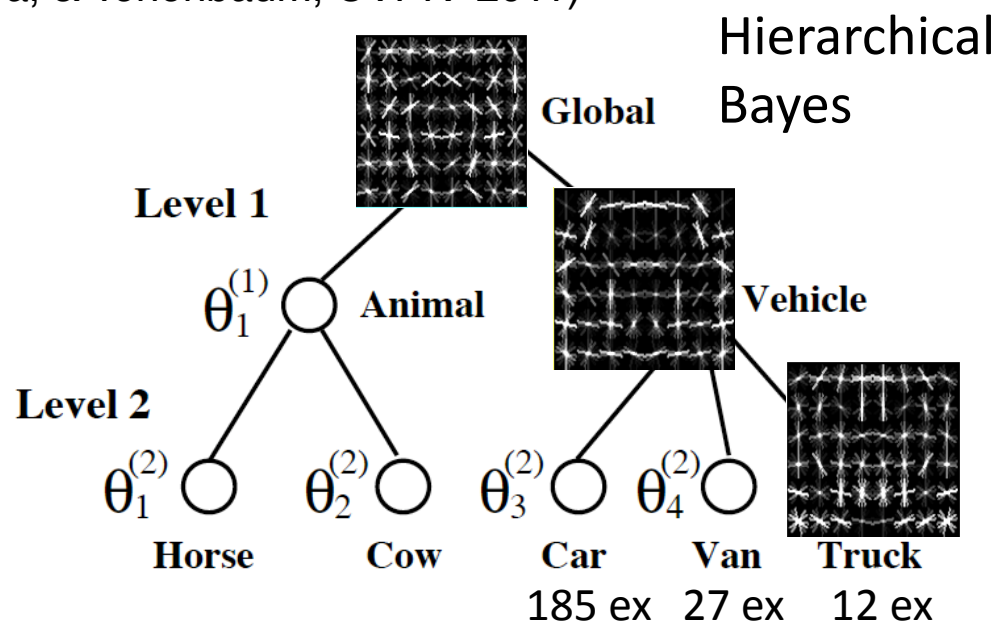


# Generative Model of Classifier Parameters

(Salakhutdinov, Torralba, & Tenenbaum, CVPR 2011)

By learning hierarchical structure, we can improve the current state-of-the-art.

Sun Dataset: 32,855 examples of 200 categories



## Hierarchical Model



## Single Class

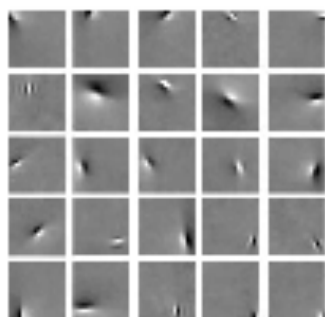




# Generative Model of Matrix Factorizations

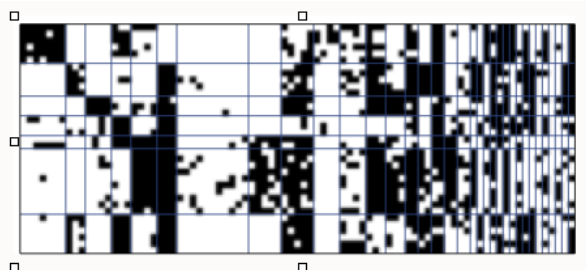
Grosse, Salakhutdinov, Freeman, and Tenenbaum, 2011

Image bases



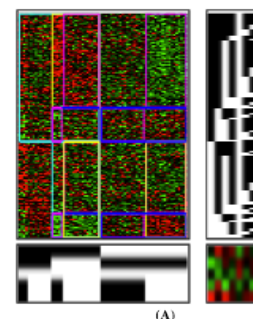
Karklin and Lewicki (2009)

Relational data



Kemp et.al. (2006)

Gene expression data



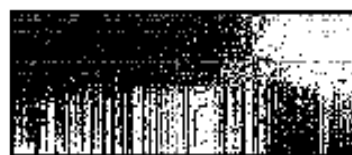
Meeds et al. (2007)

How can we automatically choose the right structure from raw data?

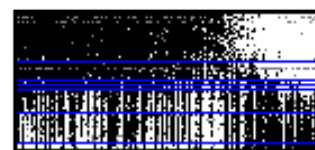
Context free grammar:

- |                 |                                      |     |
|-----------------|--------------------------------------|-----|
| low-rank        | $G \rightarrow GG + G$               | (1) |
| clustering      | $G \rightarrow MG + G \mid GM^T + G$ | (2) |
|                 | $M \rightarrow MG + G$               | (3) |
| linear dynamics | $G \rightarrow CG + G \mid GC^T + G$ | (4) |
|                 | $C \rightarrow CG + G$               | (5) |
| sparsity        | $G \rightarrow \exp(G) \circ G$      | (6) |
| binary factors  | $G \rightarrow BG + G \mid GB^T + G$ | (7) |
|                 | $M \rightarrow B$                    | (8) |

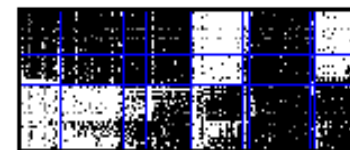
US Senate votes:



(a) Level 1:  $GG + G$



(b) Level 2:  $(MG + G)G + G$



(c) Level 3:  $(MG + G)(GM^T + G) + G$

Evolution of structure discovery

# Multi-Modal Input

Learning systems that combine multiple input domains

Images



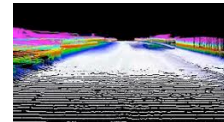
Text & Language



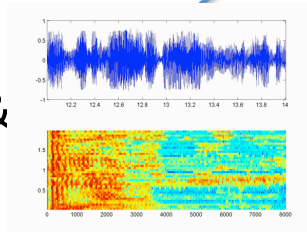
Video



Laser scans



Speech &  
Audio

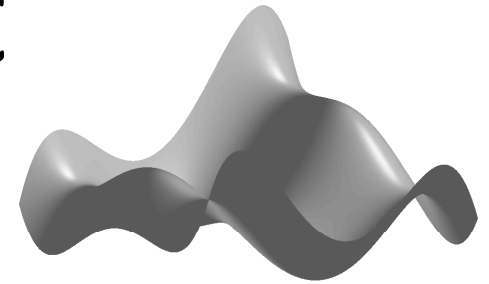


Time series  
data

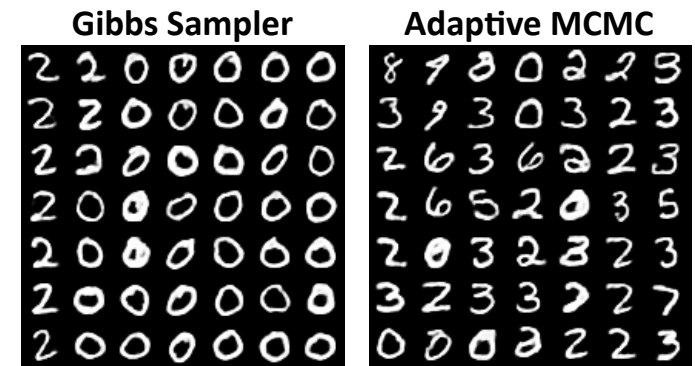
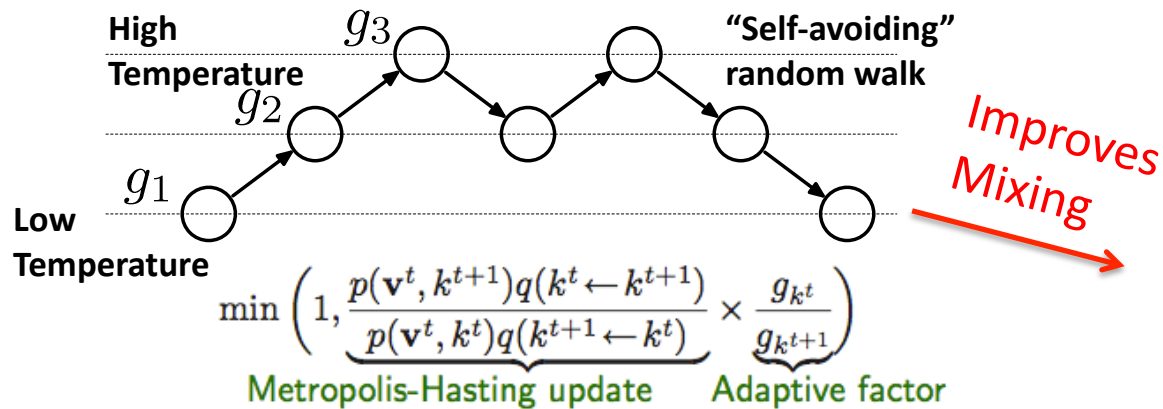
Develop learning systems that come closer to displaying human like intelligence

**One of Key Challenges:**  
Inference

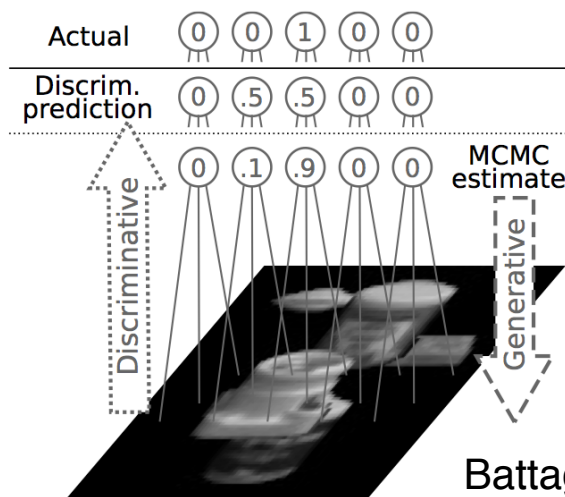
# Inference with MCMC



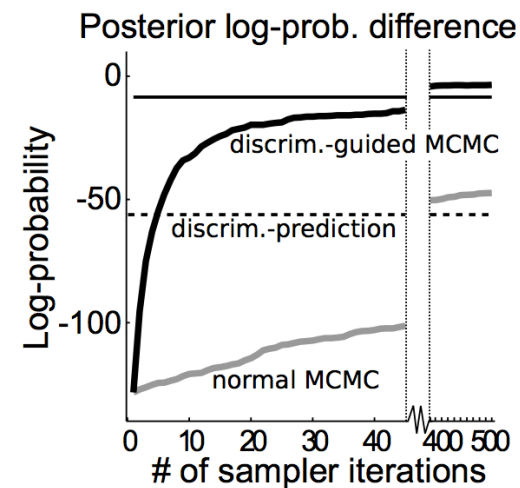
## Adaptive Markov Chain Monte Carlo for Hierarchical Generative Models (Salakhutdinov, ICML 2010):



## Data-Driven MCMC for Hierarchical Models:



Faster Convergence

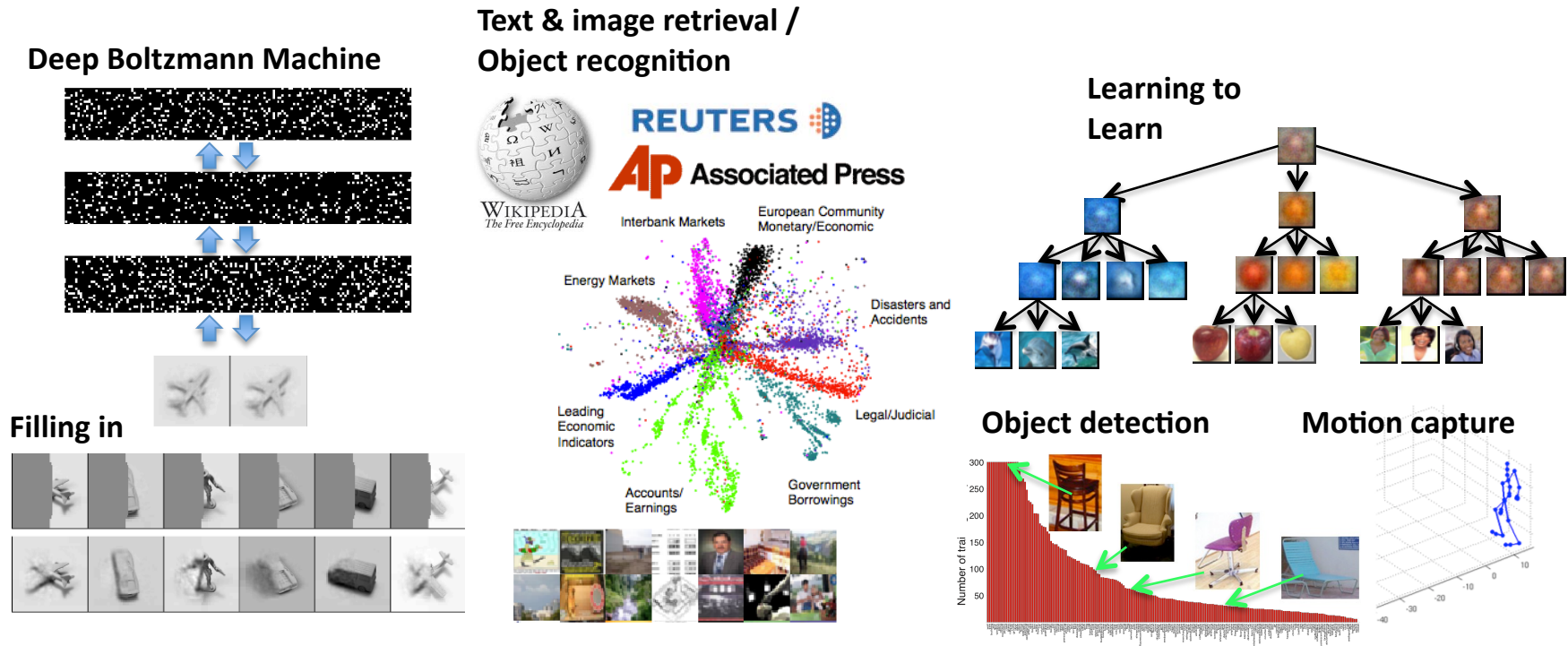


Battaglia, Salakhutdinov, Goodman, Torralba & Tenenbaum, 2011



# Recap

- Efficient learning algorithms for Hierarchical Generative Models.



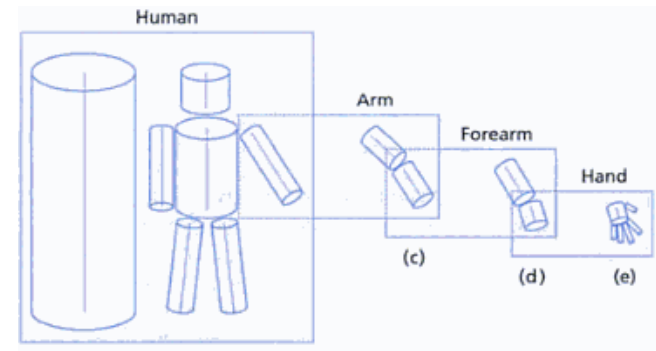
- Deep generative models can improve current state-of-the-art in many application domains:
  - Object recognition and detection, text and image retrieval, handwritten character recognition, motion capture, and others.

# Summary

Compose hierarchical Bayesian models with deep networks for transfer learning / one-shot learning.

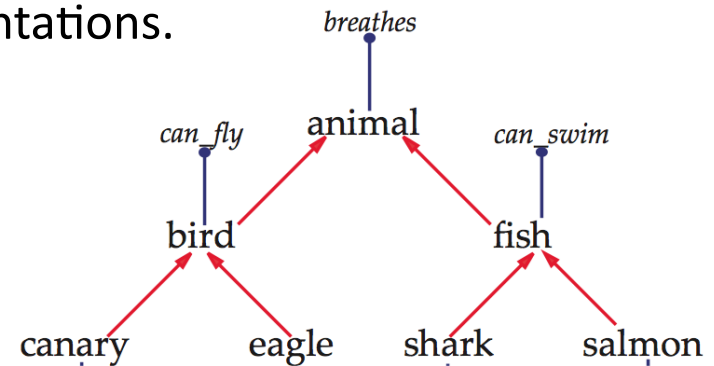
## Deep Networks: Learning Part-based Hierarchy:

- multiple **layers of nonlinearities**.
- **distributed representations**.
- **unsupervised learning of generic features** -- no need to rely on human-crafted input representations.



## Hierarchical Bayes: Learning Category Hierarchy:

- **explicitly learn category hierarchies** for sharing abstract knowledge.
- **modular data-parameter relations**.
- higher-level **class sensitive features**.



**One of Key Challenges:**  
Inference

Thank you