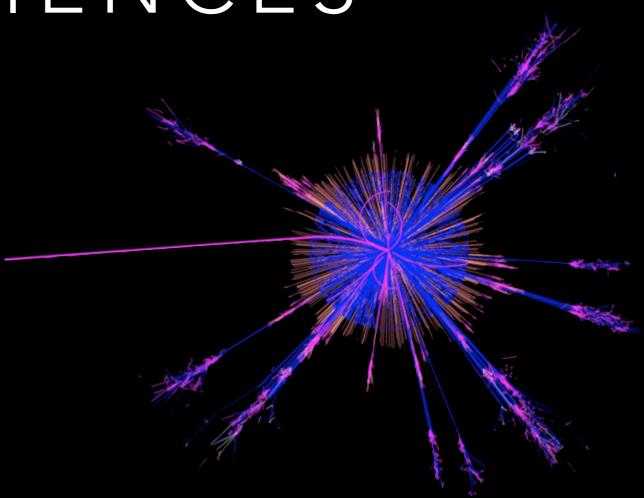


DEEP LEARNING IN THE

PHYSICAL SCIENCES

@KyleCranmer

New York University
Department of Physics
Center for Data Science
CILVR Lab

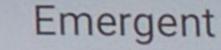


Reductionist Emergent mechanistic models descriptive models clear causal structure unclear causal structure ecology astrophysics nuclear & particle health physics documents climate language cosmology perception connectome lattice protein folding psychology simulations quantum chemistry systems biology

Reductionist | Company |

mechanistic models clear causal structure Maybe AI should start with problems where causal structure is clear and mechanistic models are available?







descriptive models unclear causal structure

ecology

nuclear & particle physics

cosmology

astrophysics

climate

connectome

health

documents

language

perception

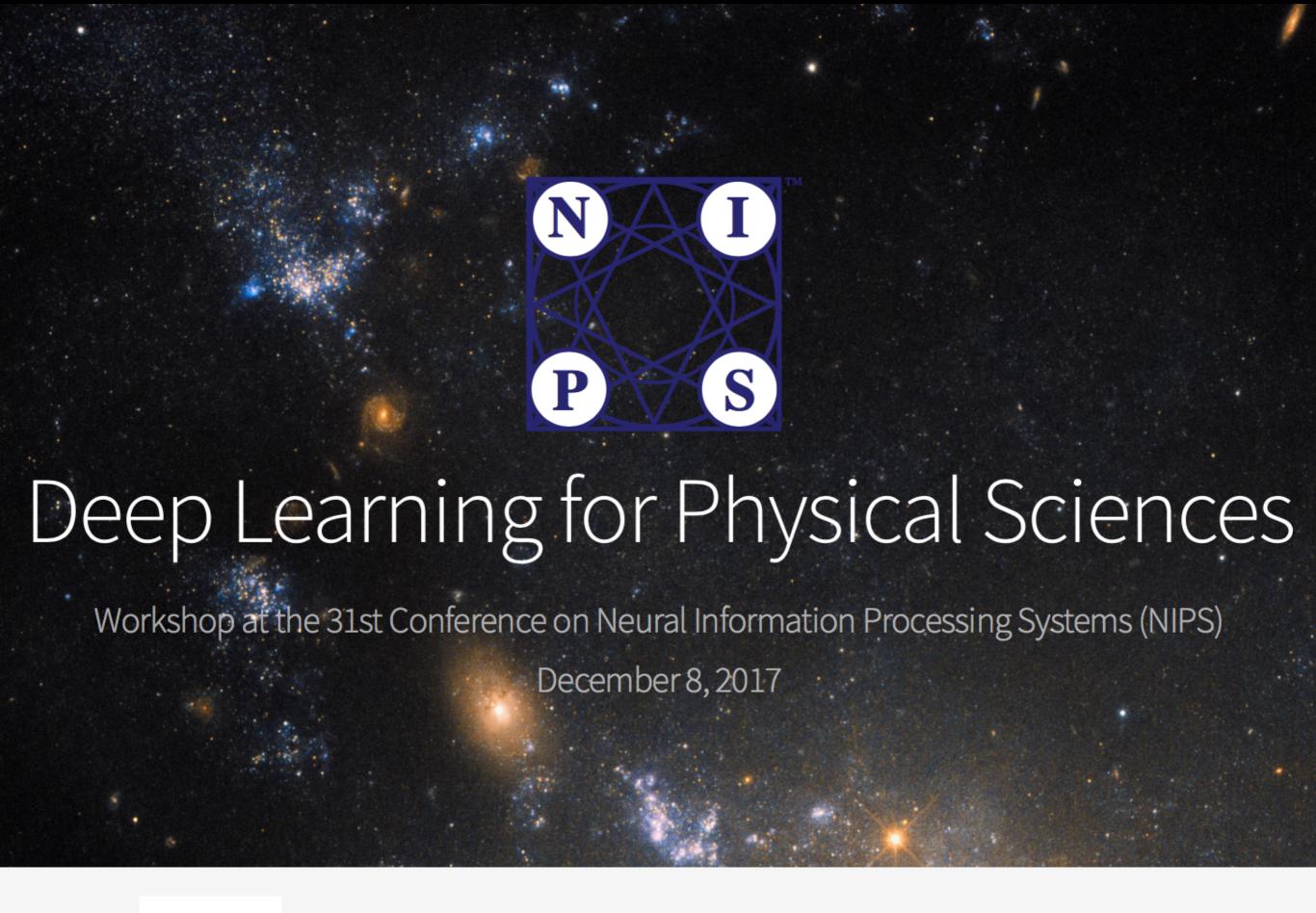
lattice simulations

protein folding

quantum chemistry

systems biology

psychology



About Schedule Call for papers Organizers Location

PANEL DISCUSSION

Moderator: Kyle Cranmer (New York University)

Iain Murray (University of Edinburgh)

Max Welling (University of Amsterdam)

Juan Carrasquilla (D-Wave Systems / Vector Institute for Artificial Intelligence)

Gilles Louppe (University of Liège)

George Dahl (Google Brain)

Anatole von Lilienfeld (University of Basel)

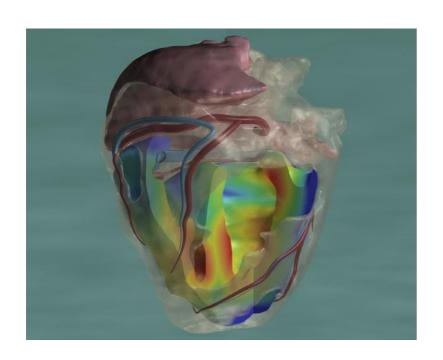
- 1. There is a lot of low hanging fruit, we can use M.L. to
 - improve what we normally do
 - speed up accelerate what we normally do

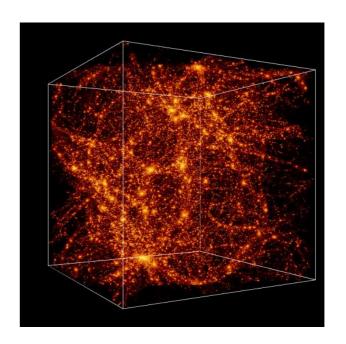
- 2. More profound changes to how we approach physics
 - new capabilities to be exploited
 - attack previously intractable problems

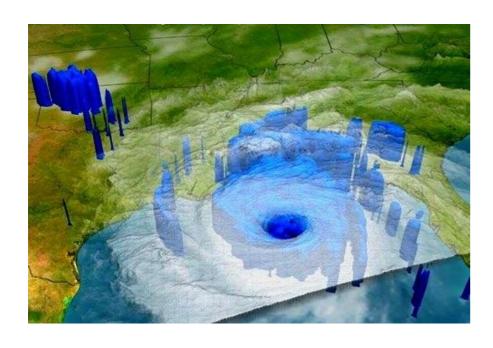


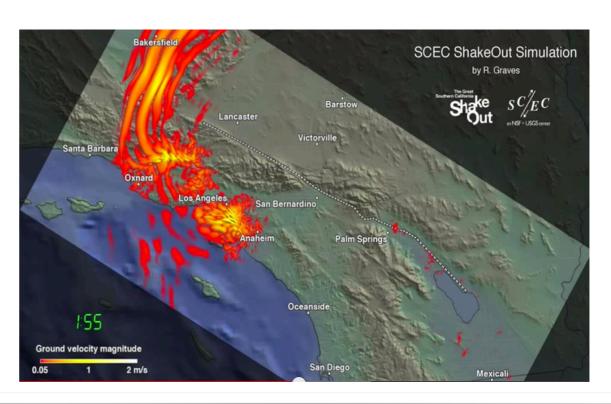
Max Welling

Generative Models: Simulators









Simulators can produce labeled training data for supervised learning

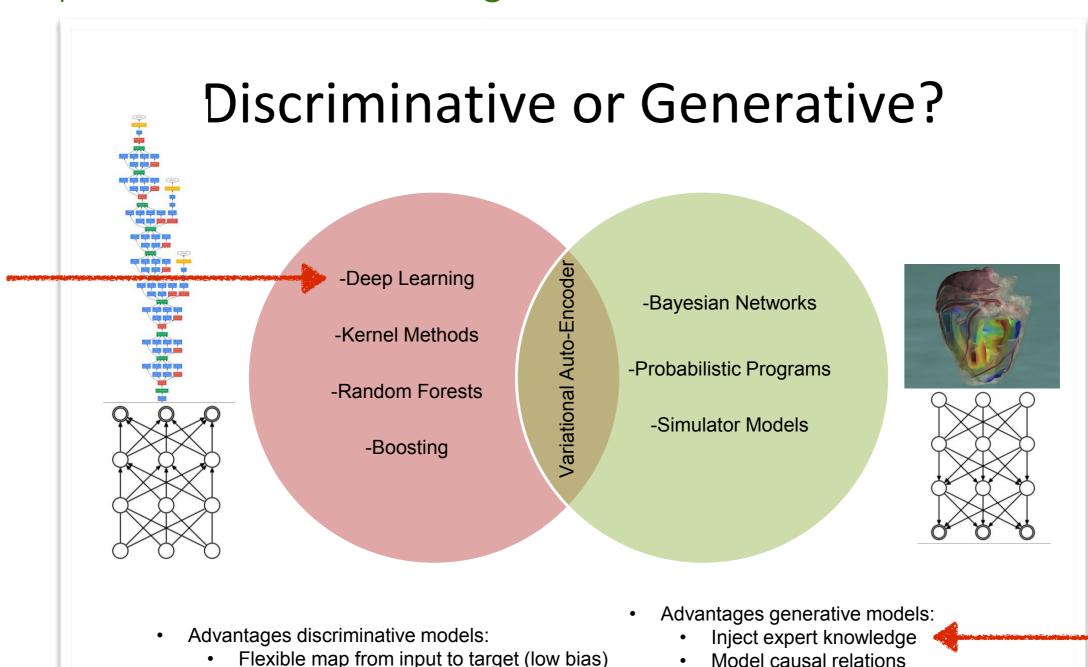
(note: some simulation are very computationally expensive)

PHYSICS AT THE INTERSECTION

We can leverage both the power of deep learning and inject our expert / domain knowledge



Max Welling



Interpretable

Data efficient

More robust to domain shift

Facilitate un/semi-supervised learning

Efficient training algorithms available

Very successful and accurate!

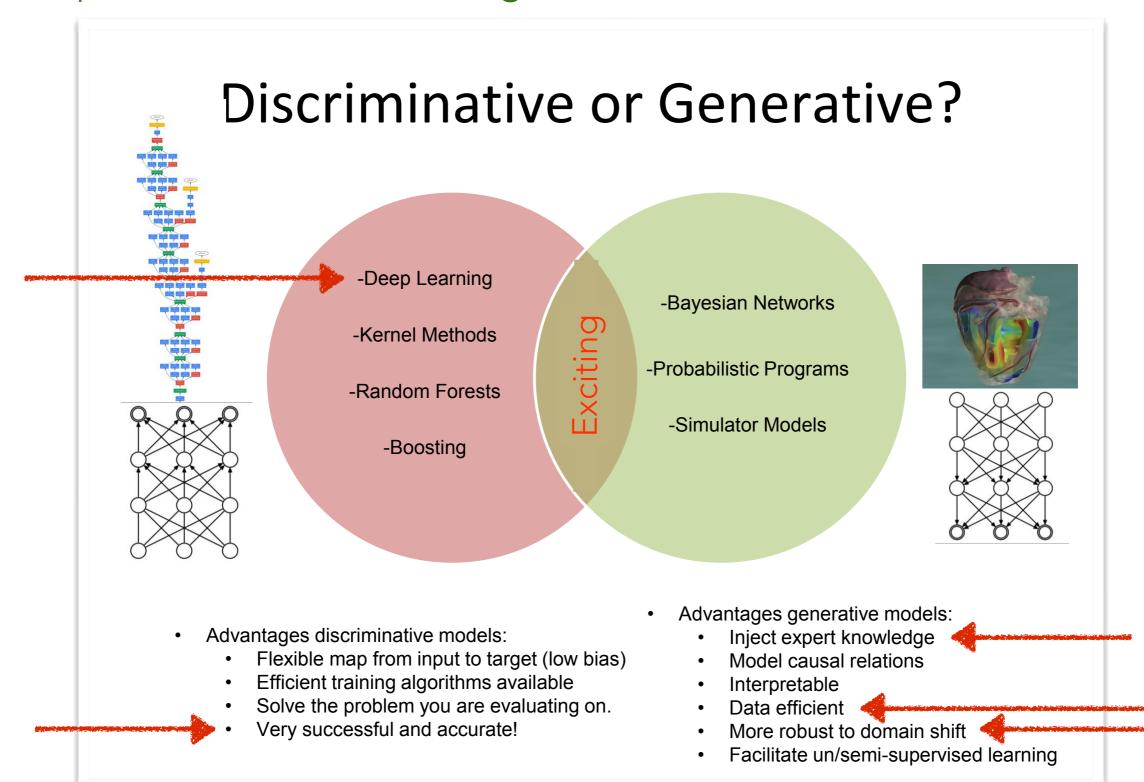
Solve the problem you are evaluating on.

PHYSICS AT THE INTERSECTION

We can leverage both the power of deep learning and inject our expert / domain knowledge



Max Welling



NOTATION / TERMINOLOGY

forward modeling generation simulation

PREDICTION

 $p(x, z | \theta, \vee)$

Z

x
observed data
simulated data

θ parameters of interest

v nuisance parameters latent variables

INFERENCE

inverse problem
measurement
parameter estimation

Quiz:

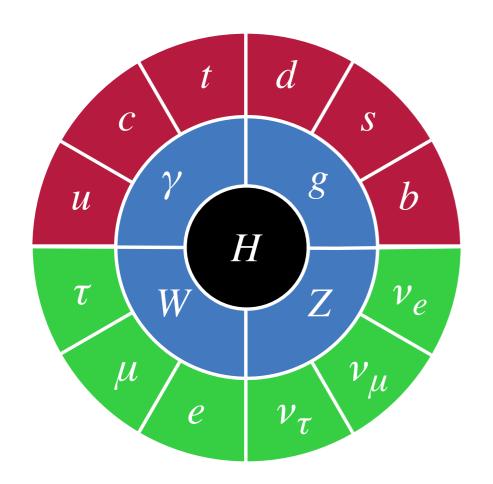
The Standard Model has 19 parameters.

The LHC has collected 10¹⁵ collisions.

Is this a parametric or non-parametric problem?

PARTICLE PHYSICS: 19 PARAMETERS

$$\mathcal{L}_{SM} = \underbrace{\frac{1}{4} \mathbf{W}_{\mu\nu} \cdot \mathbf{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} G^a_{\mu\nu} G^{\mu\nu}_a}_{\text{kinetic energies and self-interactions of the gauge bosons}} \\ + \underbrace{\bar{L} \gamma^{\mu} (i \partial_{\mu} - \frac{1}{2} g \tau \cdot \mathbf{W}_{\mu} - \frac{1}{2} g' Y B_{\mu}) L + \bar{R} \gamma^{\mu} (i \partial_{\mu} - \frac{1}{2} g' Y B_{\mu}) R}_{\text{kinetic energies and electroweak interactions of fermions}} \\ + \underbrace{\frac{1}{2} \left| (i \partial_{\mu} - \frac{1}{2} g \tau \cdot \mathbf{W}_{\mu} - \frac{1}{2} g' Y B_{\mu}) \phi \right|^2 - V(\phi)}_{W^{\pm}, Z, \gamma, \text{and Higgs masses and couplings}} \\ + \underbrace{\frac{g''(\bar{q} \gamma^{\mu} T_a q) G^a_{\mu}}{(\bar{q} \gamma^{\mu} T_a q) G^a_{\mu}}}_{\text{interactions between quarks and gluons}} + \underbrace{\frac{(G_1 \bar{L} \phi R + G_2 \bar{L} \phi_c R + h.c.)}{(G_1 \bar{L} \phi R + G_2 \bar{L} \phi_c R + h.c.)}}_{\text{fermion masses and couplings to Higgs}}$$



Symbol	Description	Value
<i>m</i> _e	Electron mass	511 keV
m_{μ}	Muon mass	105.7 MeV
m _τ	Tau mass	1.78 GeV
<i>m</i> _u	Up quark mass	1.9 MeV
m_{d}	Down quark mass	4.4 MeV
<i>m</i> s	Strange quark mass	87 MeV
<i>m</i> _c	Charm quark mass	1.32 GeV
<i>m</i> _b	Bottom quark mass	4.24 GeV
<i>m</i> _t	Top quark mass	172.7 GeV
$ heta_{12}$	CKM 12-mixing angle	13.1°
$ heta_{23}$	CKM 23-mixing angle	2.4°
<i>θ</i> 13	CKM 13-mixing angle	0.2°
δ	CKM CP-violating Phase	0.995
<i>g</i> ₁	U(1) gauge coupling	0.357
<i>g</i> ₂	SU(2) gauge coupling	0.652
<i>g</i> ₃	SU(3) gauge coupling	1.221
$ heta_{ extsf{QCD}}$	QCD vacuum angle	~0
V	Higgs vacuum expectation value	246 GeV
<i>m</i> _H	Higgs mass	125 GeV

$$\mathcal{L}_{SM} = \underbrace{\frac{1}{4} \mathbf{W}_{\mu\nu} \cdot \mathbf{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} G^a_{\mu\nu} G^{\mu\nu}_a}_{a}$$

kinetic energies and self-interactions of the gauge bosons

+
$$\bar{L}\gamma^{\mu}(i\partial_{\mu} - \frac{1}{2}g\tau \cdot \mathbf{W}_{\mu} - \frac{1}{2}g'YB_{\mu})L + \bar{R}\gamma^{\mu}(i\partial_{\mu} - \frac{1}{2}g'YB_{\mu})R$$

kinetic energies and electroweak interactions of fermions

+
$$\underbrace{\frac{1}{2} \left| \left(i \partial_{\mu} - \frac{1}{2} g \tau \cdot \mathbf{W}_{\mu} - \frac{1}{2} g' Y B_{\mu} \right) \phi \right|^{2} - V(\phi)}_{}$$

 W^{\pm}, Z, γ , and Higgs masses and couplings

+
$$g''(\bar{q}\gamma^{\mu}T_aq)G^a_{\mu}$$
 + $(G_1\bar{L}\phi R + G_2\bar{L}\phi_c R + h.c.)$
interactions between quarks and gluons fermion masses and couplings to Higgs

1) We begin with Quantum Field Theory

$$\mathcal{L}_{SM} = \underbrace{\frac{1}{4} \mathbf{W}_{\mu\nu} \cdot \mathbf{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} G^a_{\mu\nu} G^{\mu}_a}_{a}$$

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kinetic energies and electroweak interactions of fermions

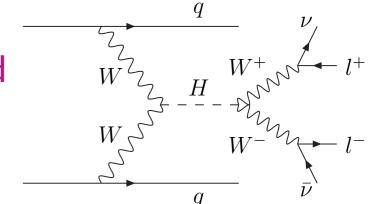
+
$$\underbrace{\frac{1}{2} \left| \left(i \partial_{\mu} - \frac{1}{2} g \tau \cdot \mathbf{W}_{\mu} - \frac{1}{2} g' Y B_{\mu} \right) \phi \right|^{2} - V(\phi)}_{}$$

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interactions between quarks and gluons fermion masses and couplings to Higgs

1) We begin with Quantum Field Theory

2) Theory gives detailed prediction for highenergy collisions



hierarchical: $2 \rightarrow O(10) \rightarrow O(100)$ particles

$$\mathcal{L}_{SM} = \underbrace{\frac{1}{4} \mathbf{W}_{\mu\nu} \cdot \mathbf{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} G^a_{\mu\nu} G^{\mu\nu}_a}_{a}$$

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kinetic energies and electroweak interactions of fermions

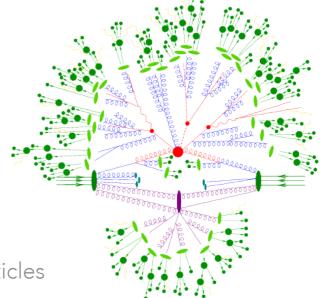
+
$$\underbrace{\frac{1}{2} \left| \left(i \partial_{\mu} - \frac{1}{2} g \tau \cdot \mathbf{W}_{\mu} - \frac{1}{2} g' Y B_{\mu} \right) \phi \right|^{2} - V(\phi)}_{}$$

 W^{\pm}, Z, γ , and Higgs masses and couplings

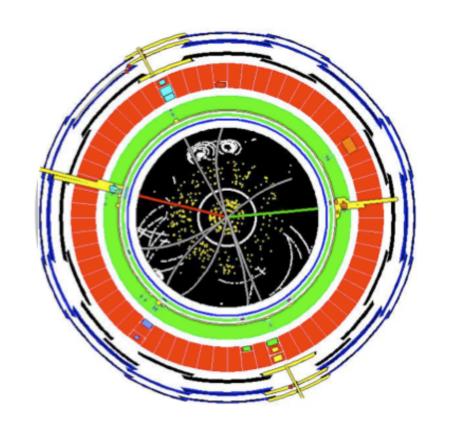
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$$g''(\bar{q}\gamma^{\mu}T_aq)G^a_{\mu}$$
 + $(G_1\bar{L}\phi R + G_2\bar{L}\phi_c R + h.c.)$
interactions between quarks and gluons fermion masses and couplings to Higgs



2) Theory gives detailed prediction for highenergy collisions



hierarchical: $2 \rightarrow O(10) \rightarrow O(100)$ particles



3) The interaction of outgoing particles with the detector is simulated.

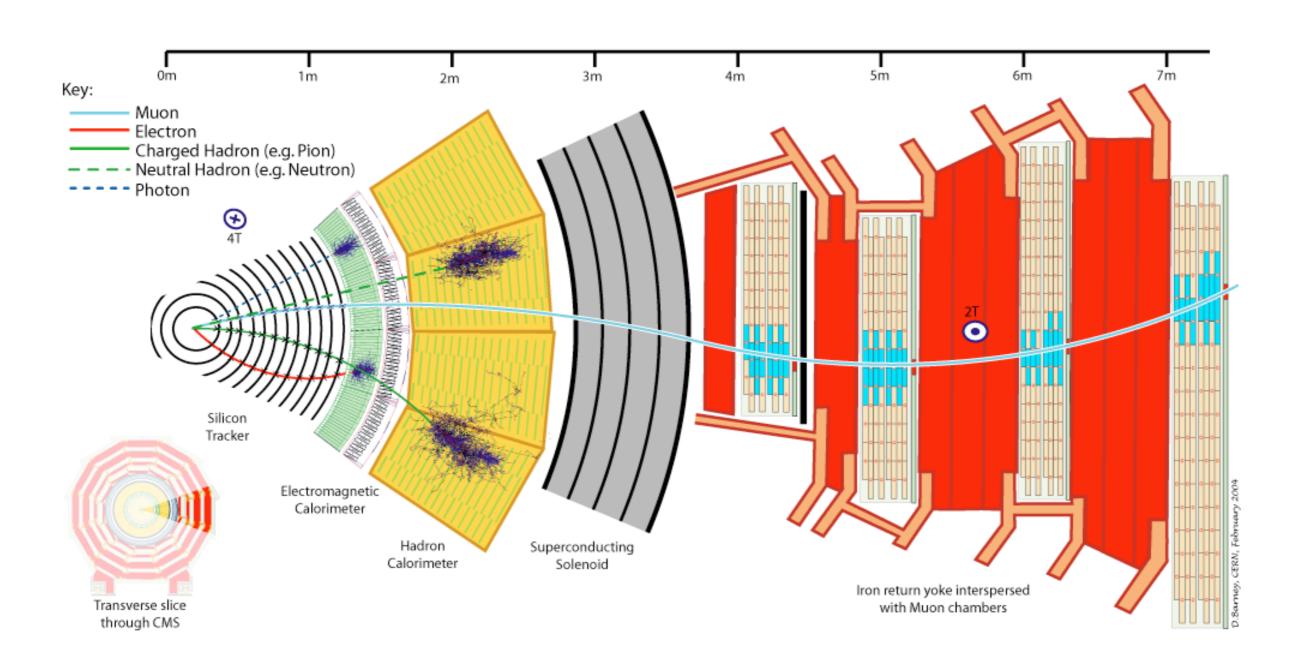
>100 million sensors

DETECTOR SIMULATION

Conceptually: Prob(detector response | particles)

Implementation: Monte Carlo integration over micro-physics

Consequence: evaluation of the likelihood is intractable



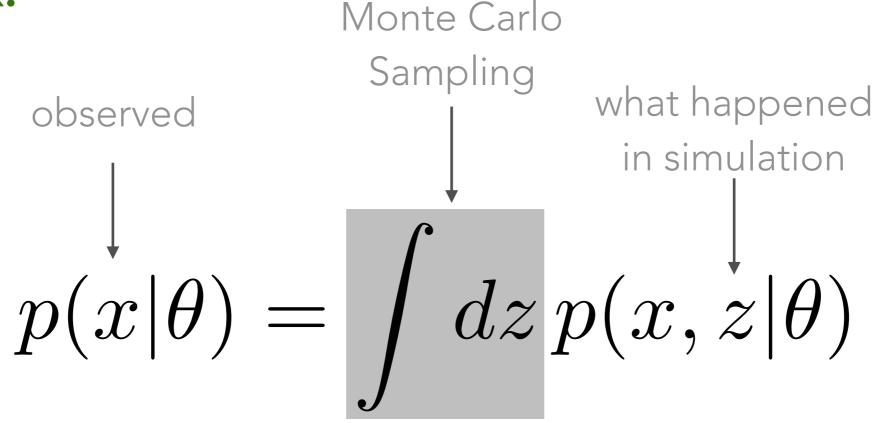
DETECTOR SIMULATION

Conceptually: Prob(detector response | particles)

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The Crux:



Parametric:

- num parameters < num data points
- model is highly constrained & tractable

Parametric:

- num parameters < num data points
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Non-Parametric

- num parameters > num data points
- model is very flexible, but tractable

Parametric:

- num parameters < num data points
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Non-Parametric

- num parameters > num data points
- model is very flexible, but tractable

Implicit Models / Simulation-based inference / Likelihood-free inference

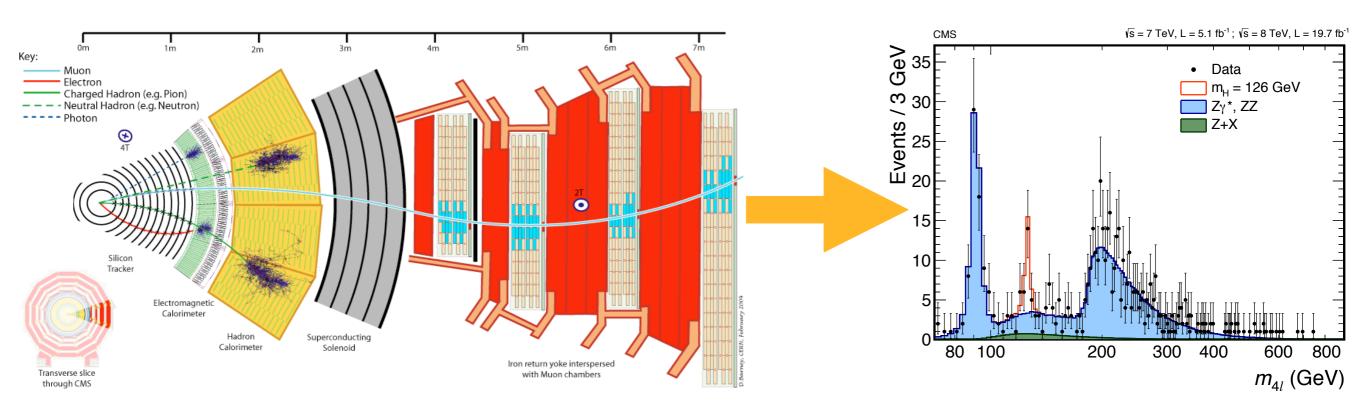
- num parameters of simulator < num data points
- but data distribution is very complicated and density is intractable
 - hard to identify the relevant "degrees of freedom" in the data (sufficient statistics)
- model is highly constrained, but hard to leverage that structure
 - deep learning can help! learn a surrogate that captures relevant aspects of $p(x|\theta)$

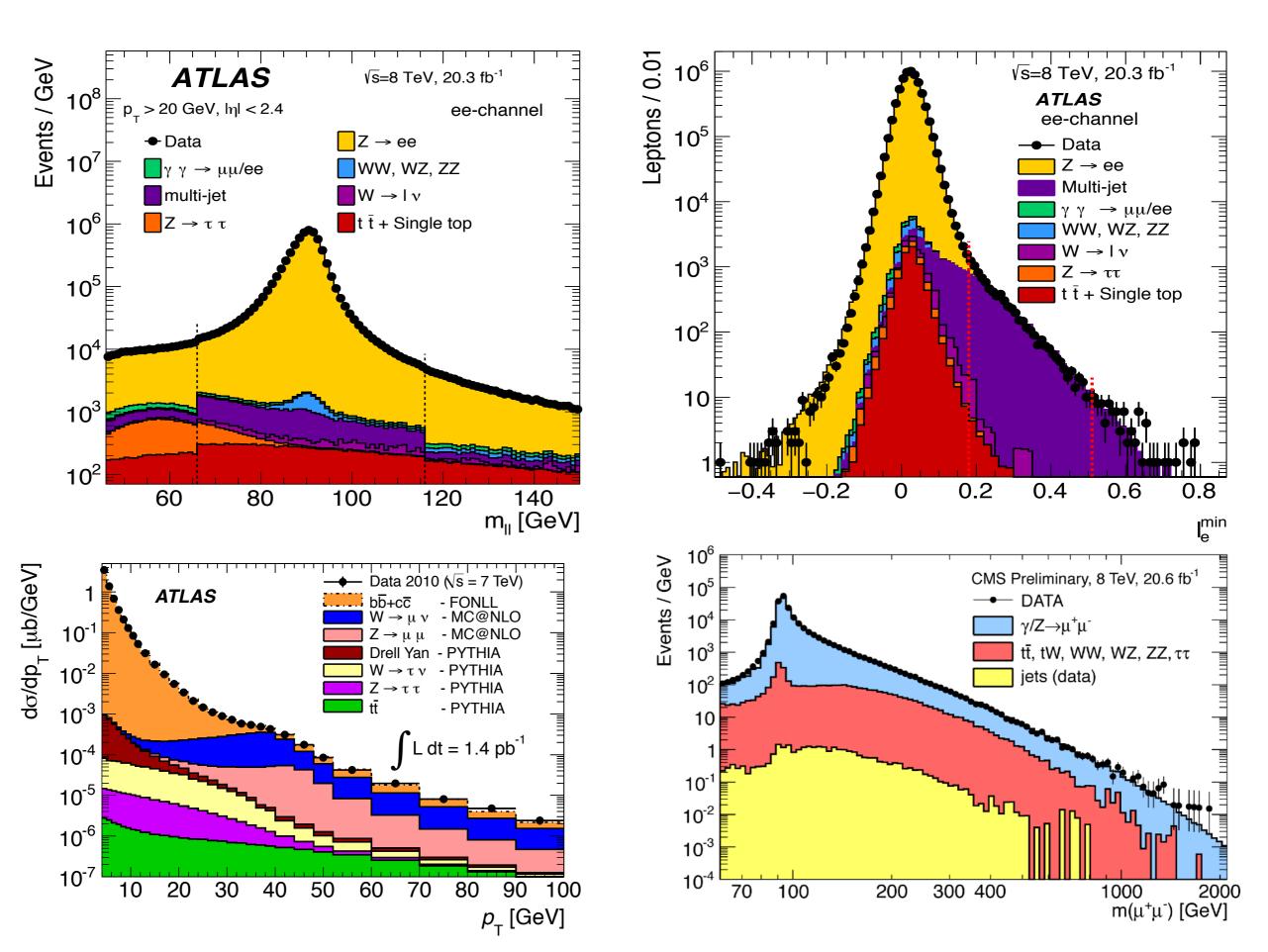
The Traditional Approach

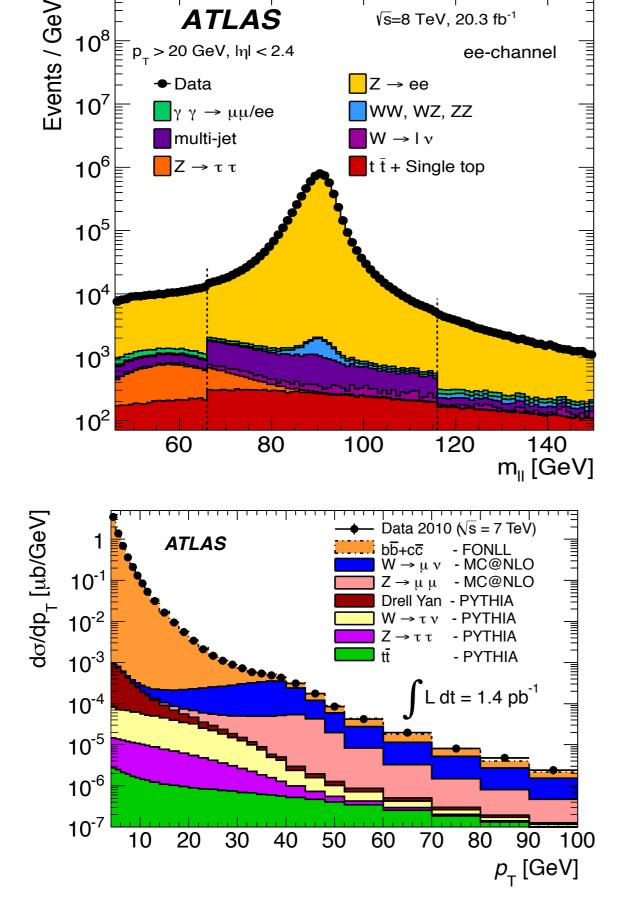
108 SENSORS → 1 REAL-VALUED QUANTITY

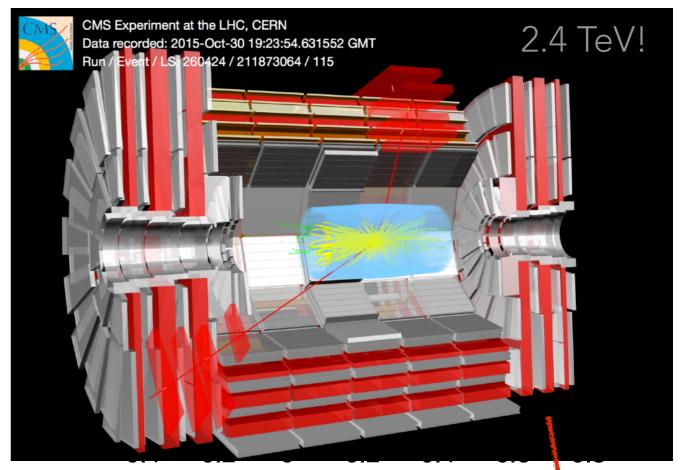
Most measurements and searches for new particles at the LHC are based on the distribution of a single variable / feature / summary statistic

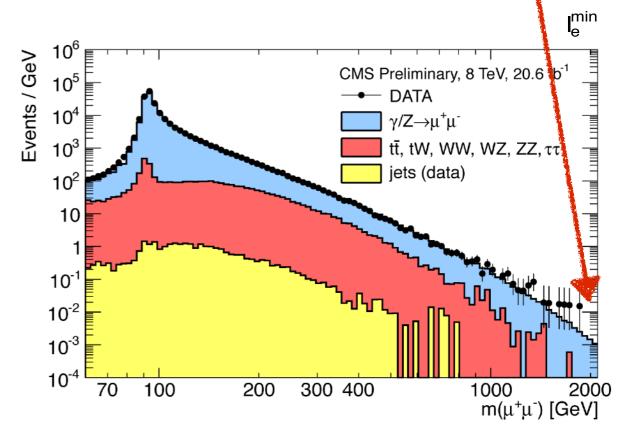
- choosing a good variable (feature engineering) is a task for a skilled physicist and tailored to the goal of measurement or new particle search
- likelihood $p(x|\theta)$ approximated using histograms (univariate density estimation)





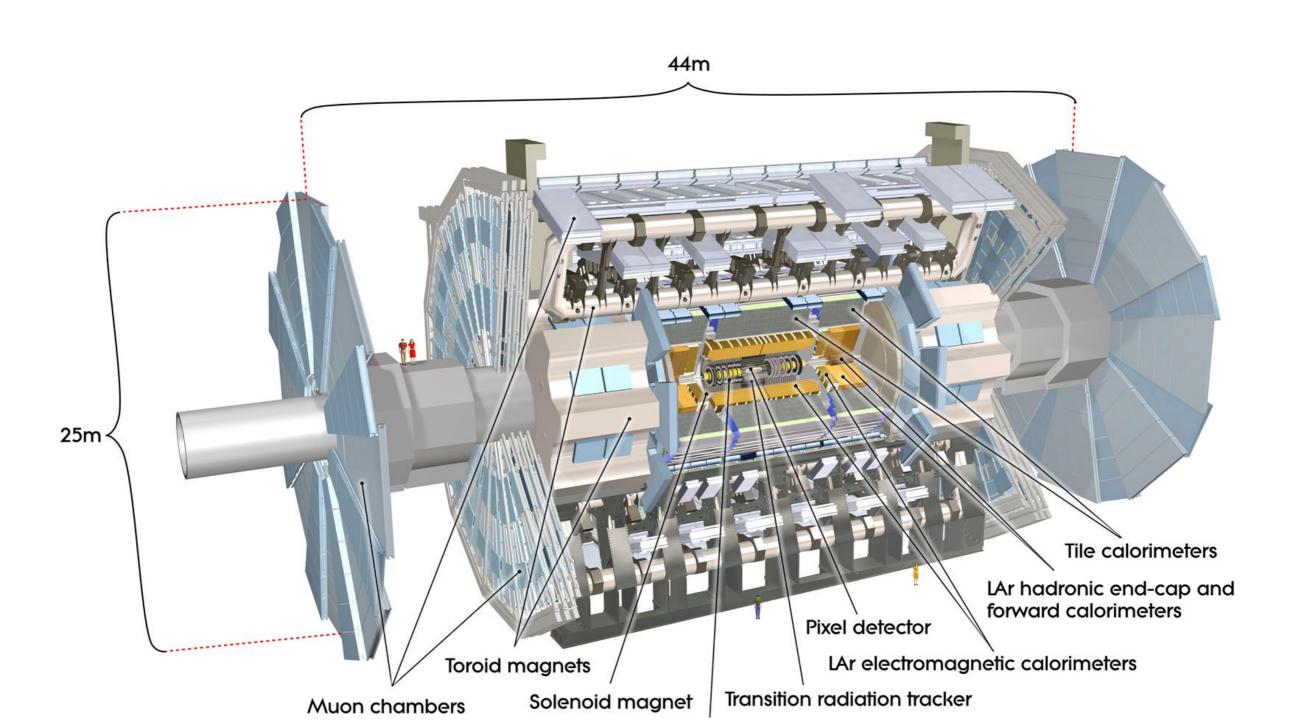






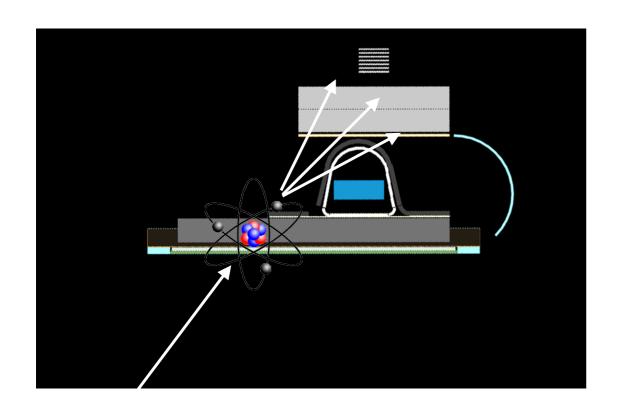
Detector is 44m long

• Detector resolves details at <mm scale; Simulation accurate!



Detector is 44m long

• Detector resolves details at <mm scale; Simulation accurate!



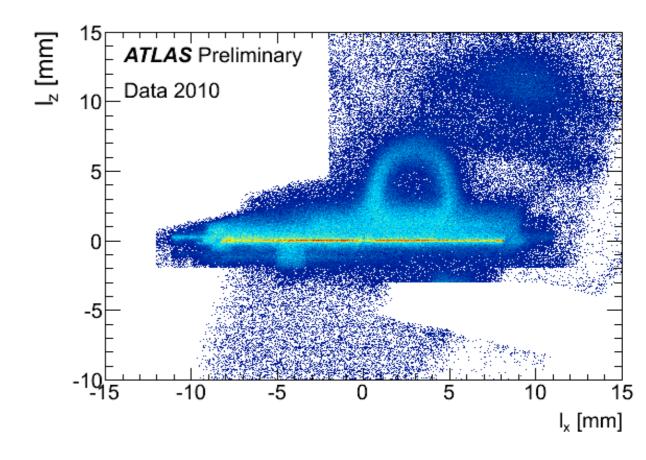
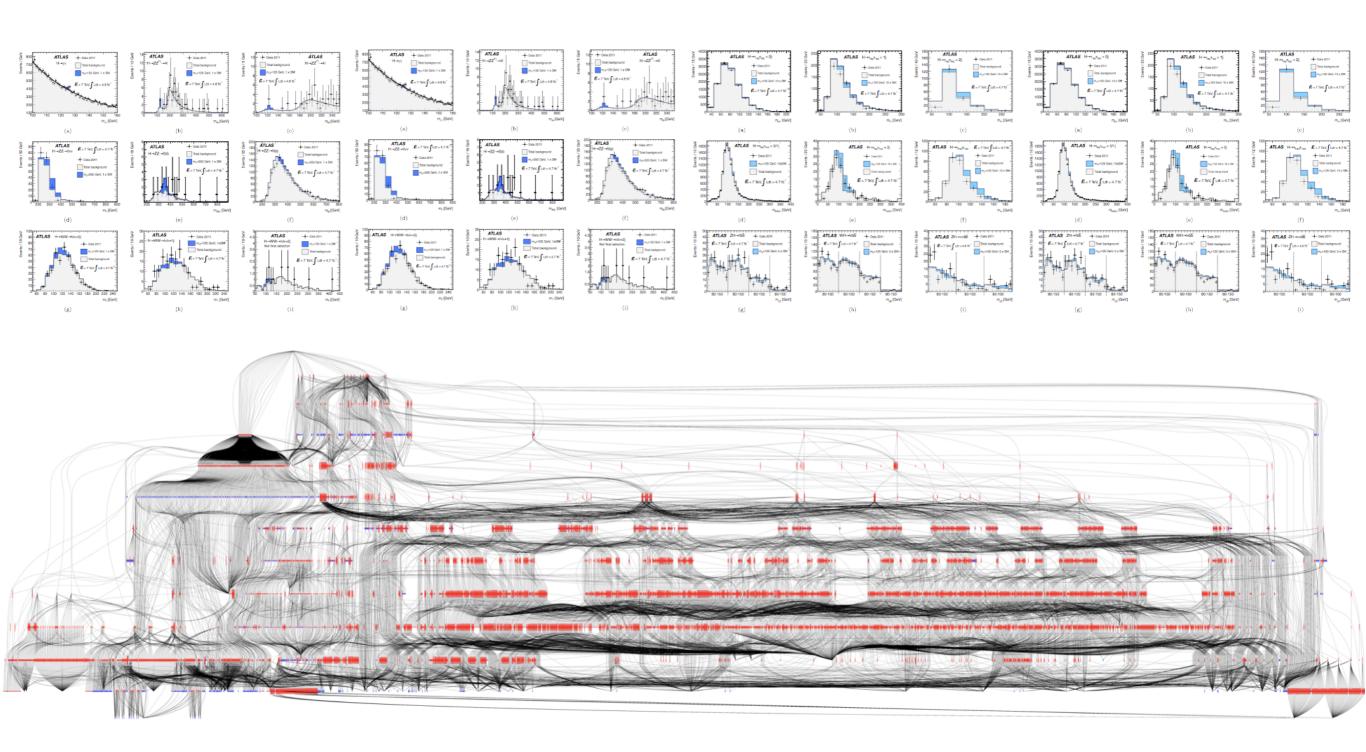


Figure:

ATLAS pixel model as described in simulation (left), tomography from vertices built from tracks for hadronic interactions (right)

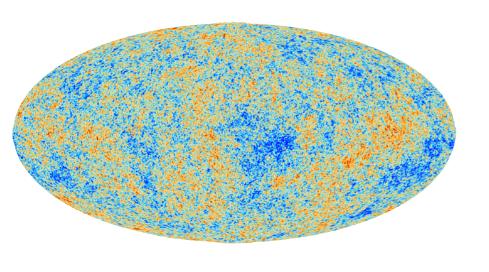
Slide Credit: A. Salzburger (CERN)

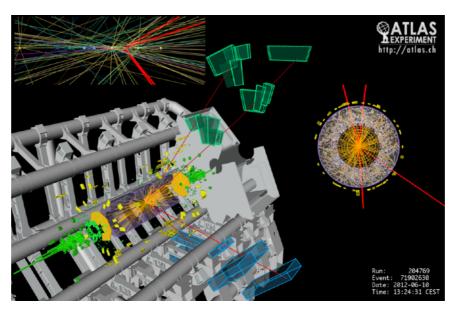
THE DISCOVERY OF THE HIGGS BOSON

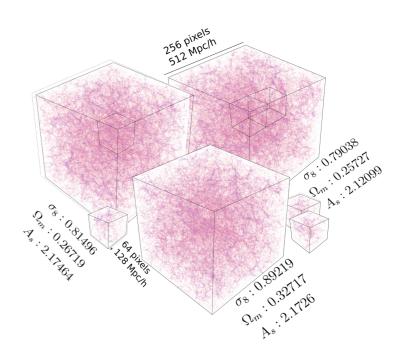


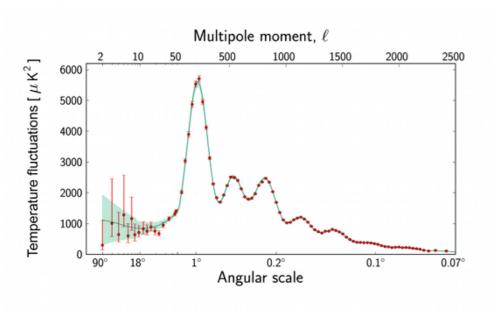
$$\mathbf{f}_{\text{tot}}(\mathcal{D}_{\text{sim}}, \mathcal{G}|\boldsymbol{\alpha}) = \prod_{c \in \text{channels}} \left[\text{Pois}(n_c|\nu_c(\boldsymbol{\alpha})) \prod_{e=1}^{n_c} f_c(x_{ce}|\boldsymbol{\alpha}) \right] \cdot \prod_{p \in \mathbb{S}} f_p(a_p|\alpha_p)$$

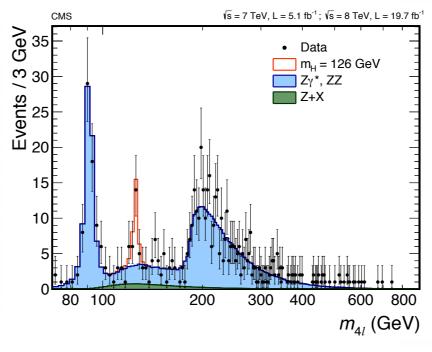
SIMULATION → TEMPLATE

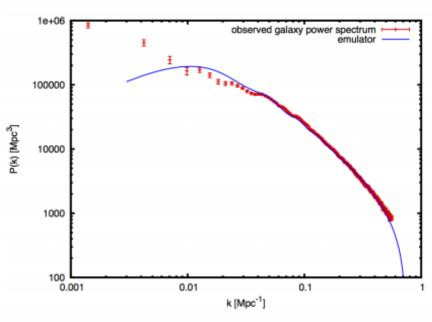












The Problem:

This doesn't scale if \mathbf{x} is high dimensional!

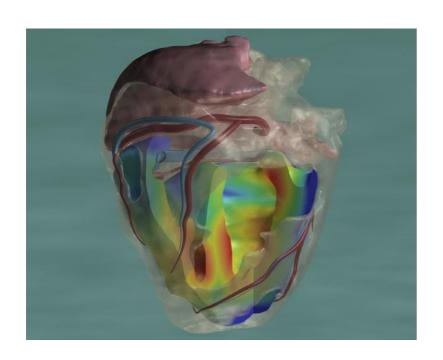
How much are we loosing in feature engineering?

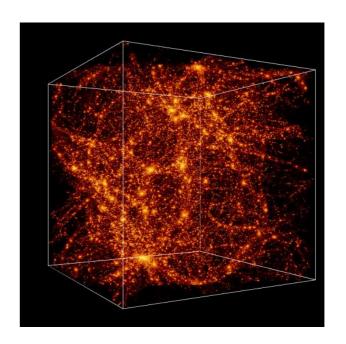
What if we don't know how to design a good feature?

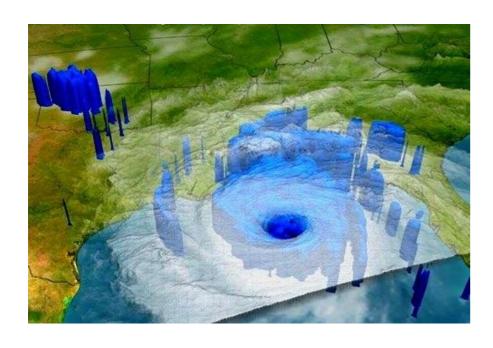


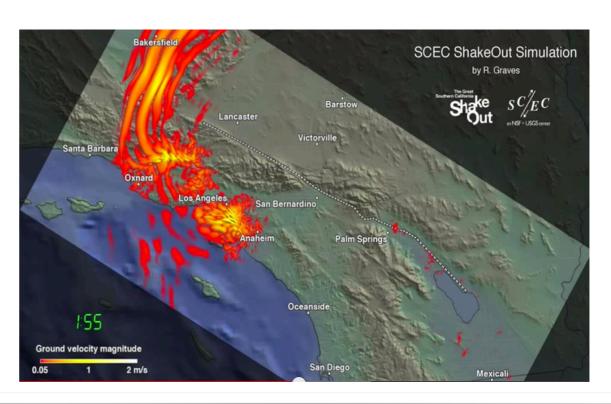
Max Welling

Generative Models: Simulators

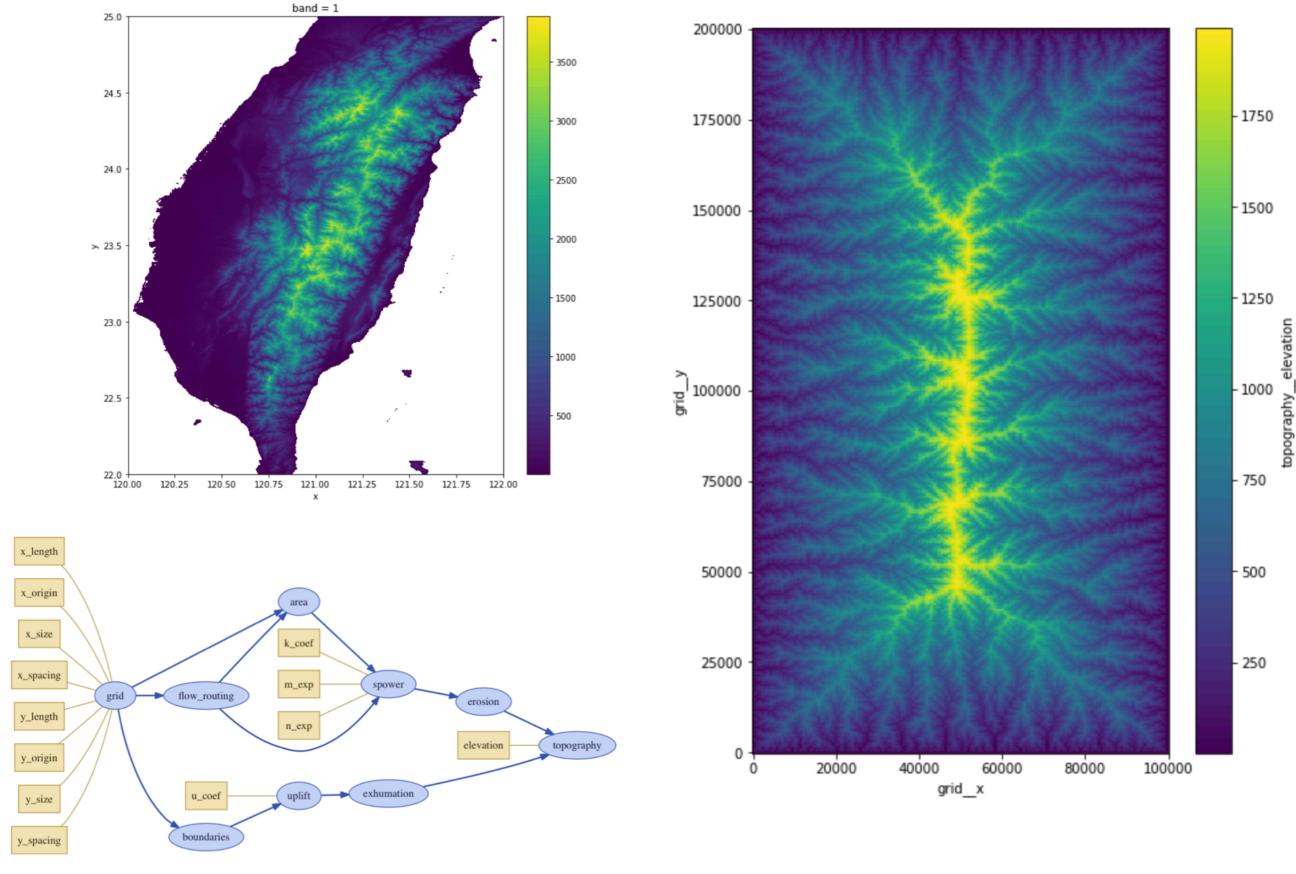




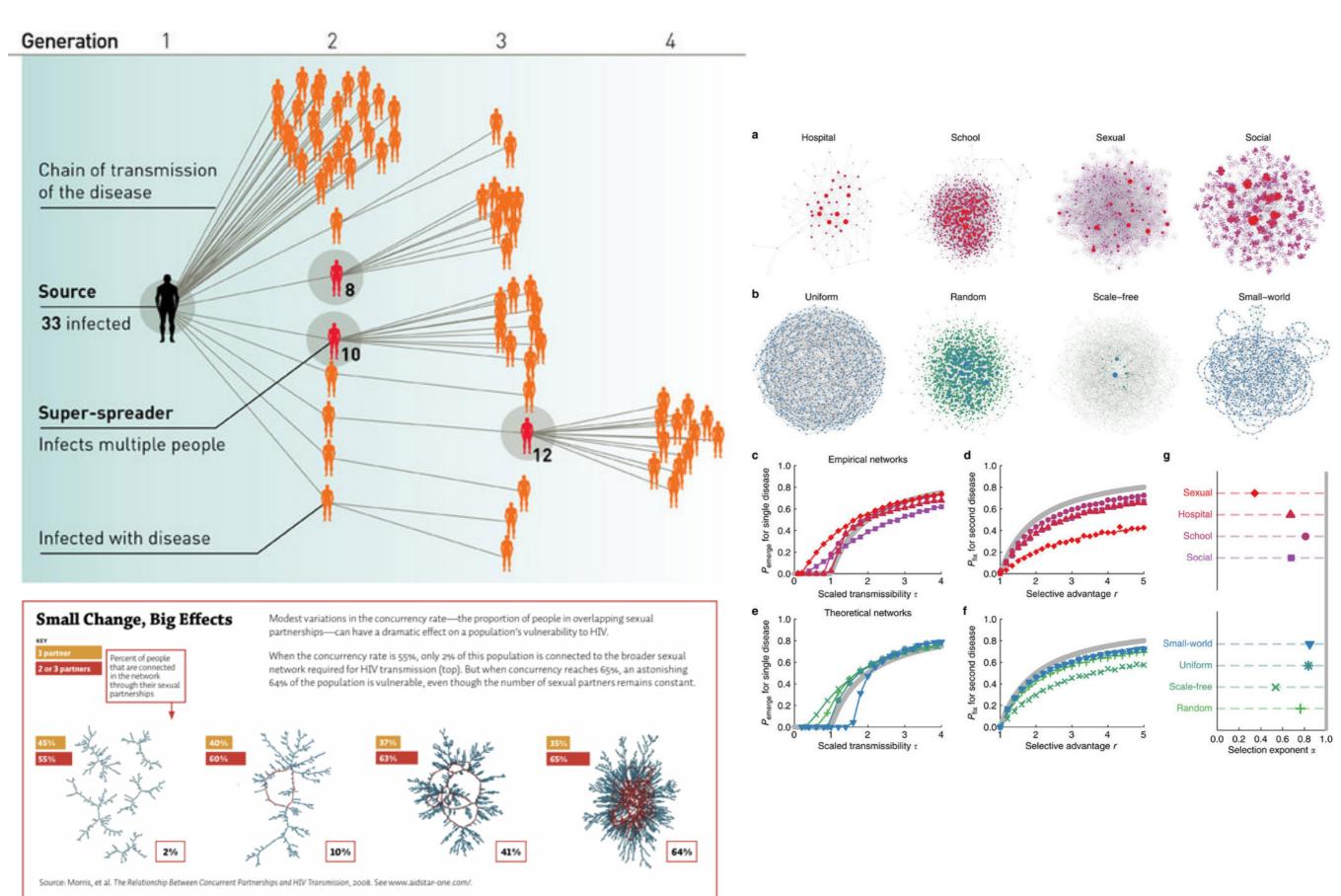




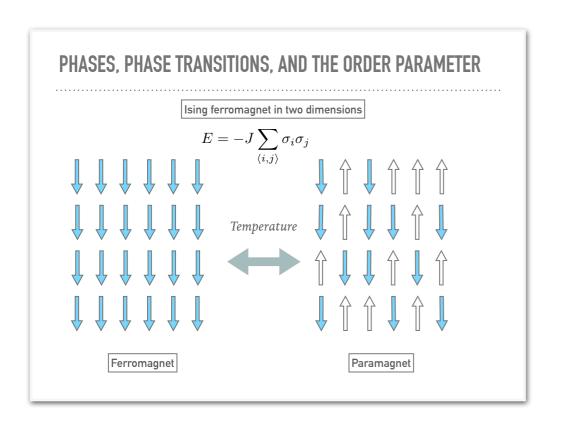
COMPUTATIONAL TOPOGRAPHY

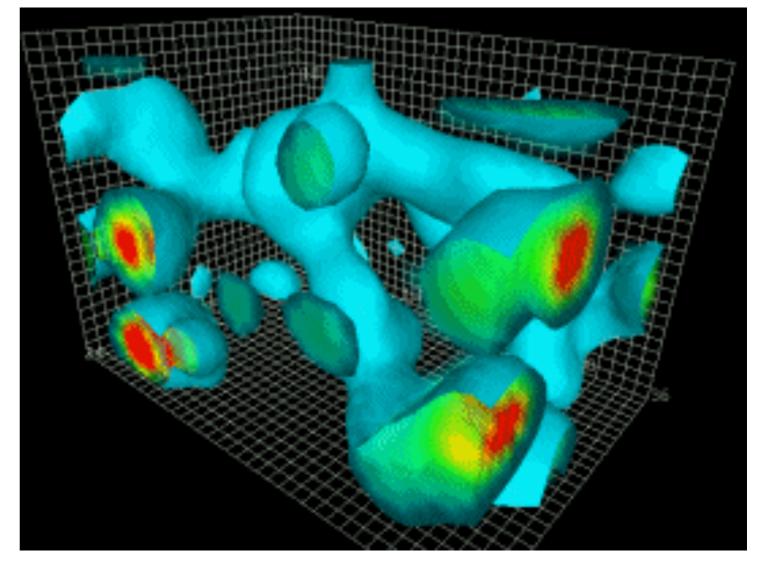


EPIDEMIOLOGY & POPULATION GENETICS

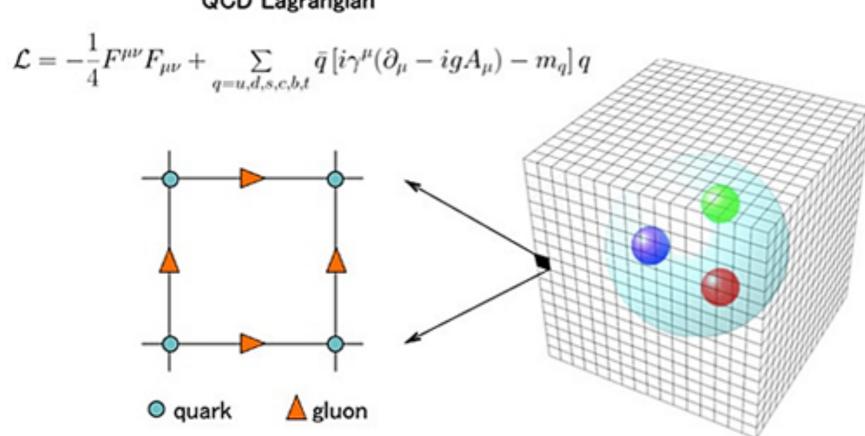


LATTICE FIELD THEORY

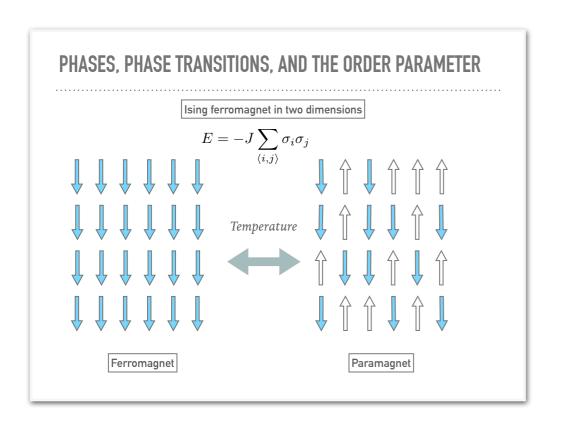


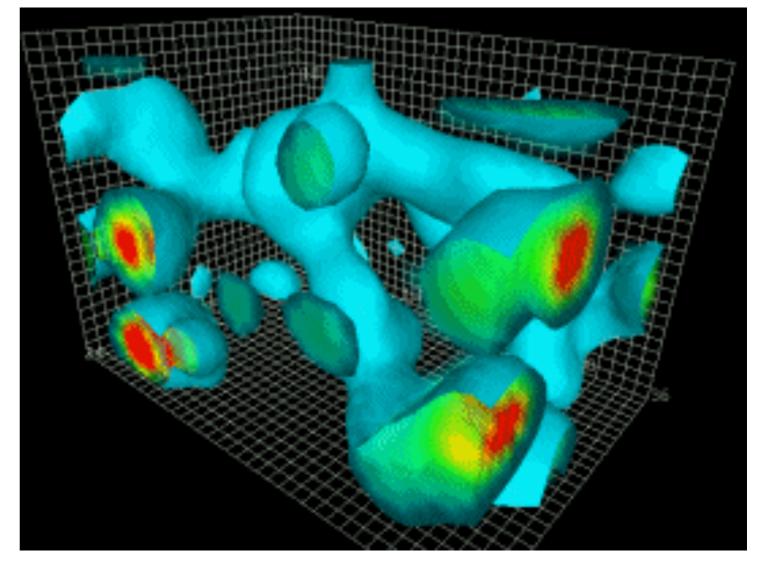


QCD Lagrangian

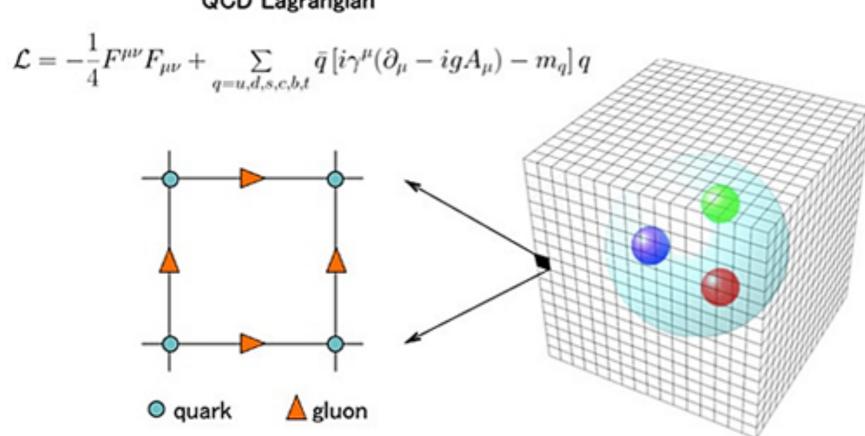


LATTICE FIELD THEORY



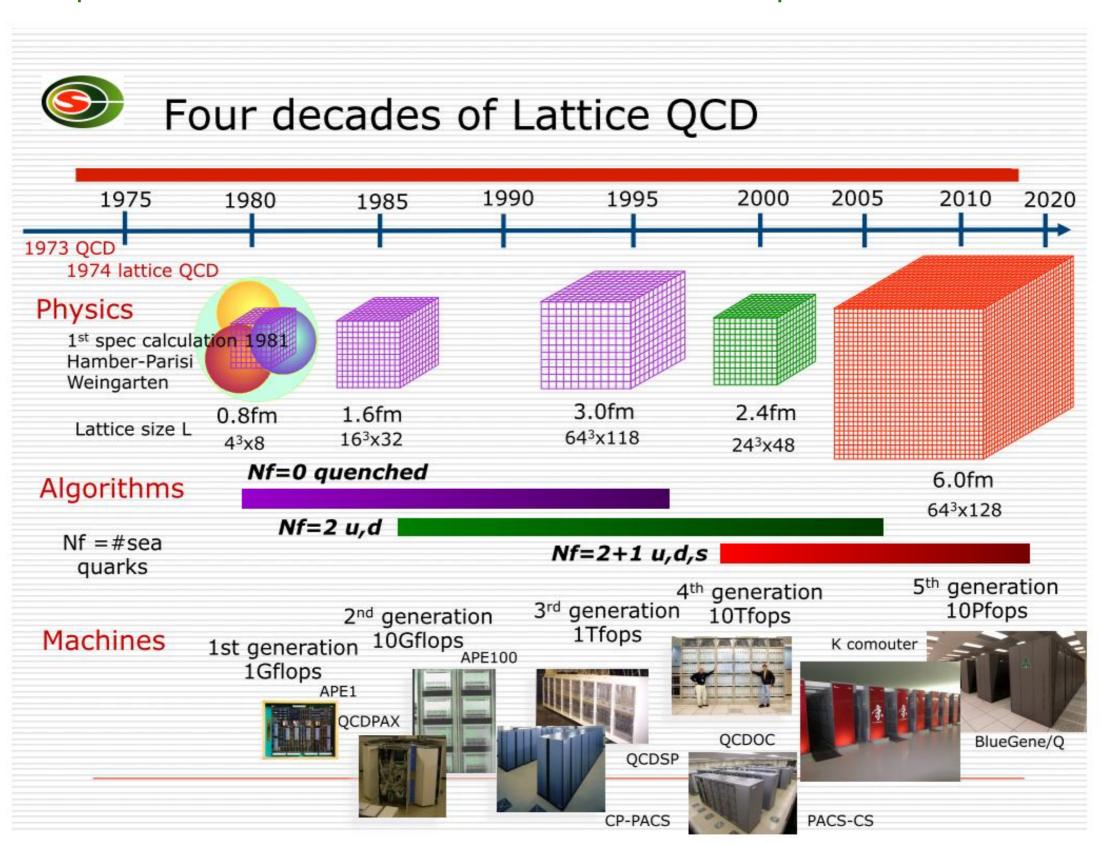


QCD Lagrangian



LATTICE QCD

Very expensive simulations, ~1000 examples with $x \in \mathbb{R}^{10^9}$



ICML 2017 Workshop on Implicit Models

Workshop Aims

Probabilistic models are an important tool in machine learning. They form the basis for models that generate realistic data, uncover hidden structure, and make predictions. Traditionally, probabilistic models in machine learning have focused on prescribed models. Prescribed models specify a joint density over observed and hidden variables that can be easily evaluated. The requirement of a tractable density simplifies their learning but limits their flexibility --- several real world phenomena are better described by simulators that do not admit a tractable density. Probabilistic models defined only via the simulations they produce are called implicit models.

Arguably starting with generative adversarial networks, research on implicit models in machine learning has exploded in recent years. This workshop's aim is to foster a discussion around the recent developments and future directions of implicit models.

Implicit models have many applications. They are used in ecology where models simulate animal populations over time; they are used in phylogeny, where simulations produce hypothetical ancestry trees; they are used in physics to generate particle simulations for high energy processes. Recently, implicit models have been used to improve the state-of-the-art in image and content generation. Part of the workshop's focus is to discuss the commonalities among applications of implicit models.

Of particular interest at this workshop is to unite fields that work on implicit models. For example:

- **Generative adversarial networks** (a NIPS 2016 workshop) are implicit models with an adversarial training scheme.
- Recent advances in **variational inference** (a NIPS 2015 and 2016 workshop) have leveraged implicit models for more accurate approximations.
- **Approximate Bayesian computation** (a NIPS 2015 workshop) focuses on posterior inference for models with implicit likelihoods.
- Learning implicit models is deeply connected to two sample testing, density ratio and density difference estimation.

We hope to bring together these different views on implicit models, identifying their core challenges and combining their innovations.

WHY SCIENTISTS SHOULD CARE

Many areas of science have simulations based on some well-motivated mechanistic model.

However, the aggregate effect of many interactions between these low-level components leads to an intractable inverse problem.

The developments in machine learning and AI have the potential to effectively bridge the microscopic - macroscopic divide & aid in the inverse problem.

- they can provide effective statistical models that describe macroscopic phenomena that are tied back to the low-level microscopic (reductionist) model
- generative models and likelihood-free inference are two particularly exciting areas

GOALS

DEFINE THE MILESTONES THAT WILL ASSIST WITH REACHING YOUR GOALS

OBJECTIVES

DECIDE THE PLAN OF ACTION TO ACHIEVE YOUR OBJECTIVES

STRATEGIES

IDENTIFY THE TOOLS YOU WILL USE TO IMPLEMENT YOUR STRATEGIES

TACTICS

GOALS & STRATEGIES

Goals:

• Use machine learning to do better science

Strategies:

- Import domain knowledge into models (inductive bias)
- Export knowledge from learned models
- Leverage machine learning for intractable inverse problems
- Incorporate traditional scientific concerns into the learning paradigm
 - include impact of domain shift / systematics uncertainties into objective
 - maintain an actionable, scientifically-useful notion of "interpretability"
 - use real-world data for training when possible
 - be data efficient
- Modify codebase to facilitate use of these techniques

STRATEGIES & TACTICS

Strategy: Import domain knowledge into models

- Tactic: exploit symmetries in the data
- Tactic: exploit geometric structure of the data
- Tactic: exploit causal structure of the generative process
- Tactic: exploit hierarchical / compositional structure
- **Tactic**: exploit Markov property of the generative process
- Tactic: exploit tangent space of statistical manifold

Strategy: Export knowledge from learned models

• Tactic: learnable components that can be interpreted

Strategy: maintain an actionable, scientifically-useful notion of "interpretability"

• **Tactic:** compose model from reusable components that perform a specific task and can be individually characterized & validated

STRATEGIES & TACTICS

Strategy: Leverage machine learning for intractable inverse problems

- Tactic: Use the likelihood ratio trick to convert a discriminative classifier into a density ratio
- Tactic: Use autoregressive models & normalizing flows for conditional density estimation
- Tactic: Use universal probabilistic programming
- Tactic: Approximate gradients of non-differentiable, black-box models (AVO, RELAX, ...)

Strategy: include impact of systematics uncertainties into objective

- Tactic: Design loss functions more relevant to scientific goals
- Tactic: Adversarial training for continuous domain adaptation & fairness ("learning to pivot")

Strategy: use real-world data for training when possible

• Tactic: Weakly supervised learning

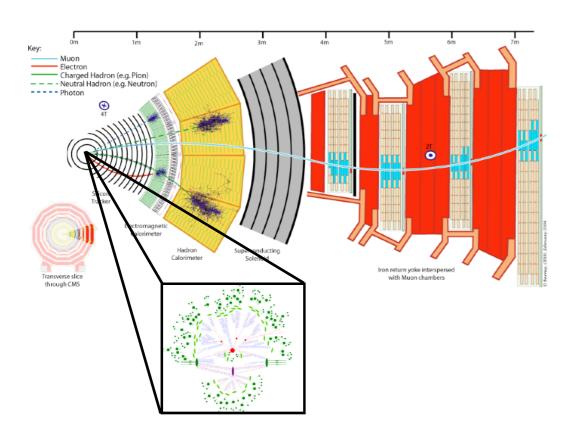
Strategy: be data efficient

• Tactic: exploiting domain knowledge can dramatically reduce number of parameters

TACTICS FOR INTRACTABLE INVERSE PROBLEMS

Use simulator

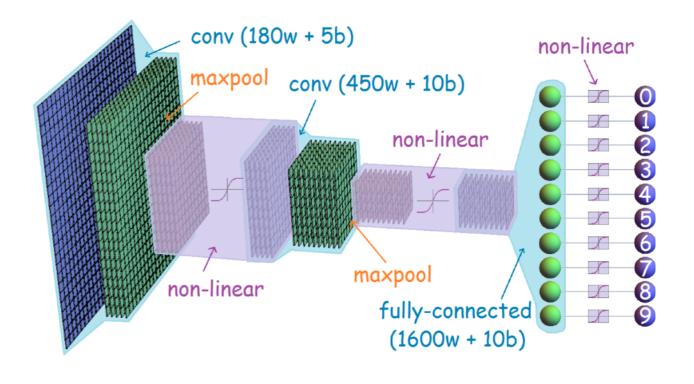
(much more efficiently)



- Approximate Bayesian Computation (ABC)
- Probabilistic Programming
- Adversarial Variational Optimization (AVO)

Learn simulator

(with deep learning)



- Generative Adversarial Networks (GANs), Variational Auto-Encoders (VAE)
- Likelihood ratio from classifiers (CARL)
- Autoregressive models, Normalizing Flows

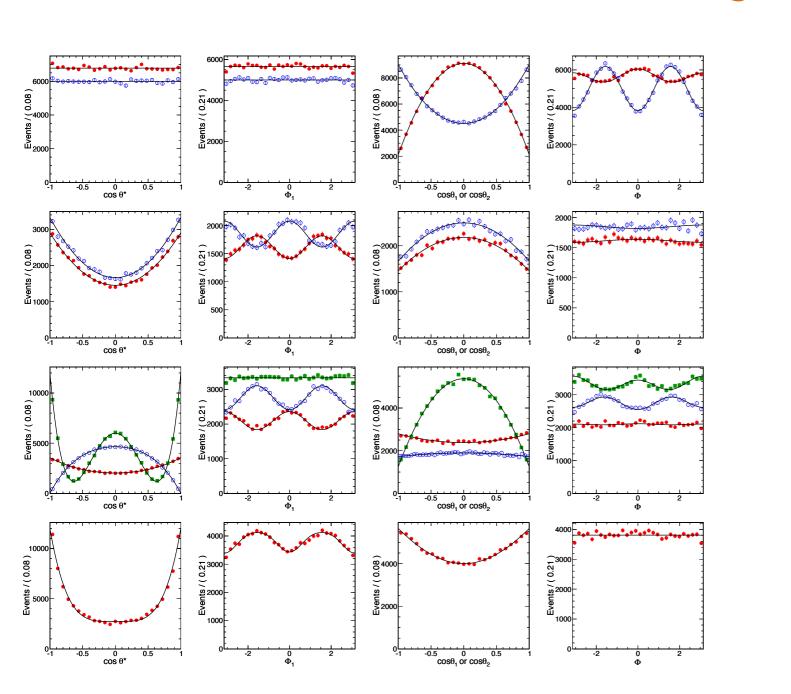
Example:

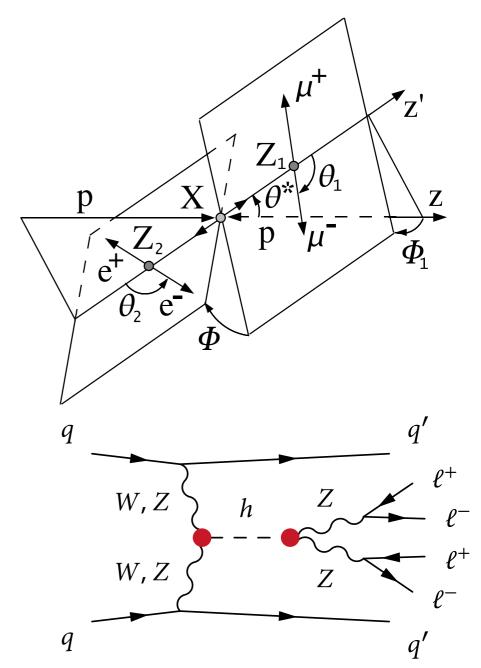
More Powerful Higgs Measurements

HIGH DIMENSIONAL EXAMPLE

When looking for deviations from the standard model Higgs, we would like to look at all sorts of kinematic correlations

 \bullet thus each observation \mathbf{x} is high-dimensional





EXTENDING THE LIKELIHOOD RATIO TRICK

A binary classifier approximates

$$s(x) = \frac{p(x|H_1)}{p(x|H_0) + p(x|H_1)}$$

Which is one-to-one with the likelihood ratio

$$\frac{p(x|H_1)}{p(x|H_0)} = 1 - \frac{1}{s(x)}$$

Can do the same thing for any two points θ_0 & θ_1 in parameter space Θ . I call this a **parametrized classifier**

$$s(x; \theta_0, \theta_1) = \frac{p(x|\theta_1)}{p(x|\theta_0) + p(x|\theta_1)}$$

CALIBRATING THE LIKELIHOOD-RATIO TRICK

The intractable likelihood ratio based on high-dimensional features x is:

$$\frac{p(x|\theta_0)}{p(x|\theta_1)}$$

We can show that an equivalent test can be made from 1-D projection

$$\frac{p(x|\theta_0)}{p(x|\theta_1)} = \frac{p(s(x;\theta_0,\theta_1)|\theta_0)}{p(s(x;\theta_0,\theta_1)|\theta_1)}$$

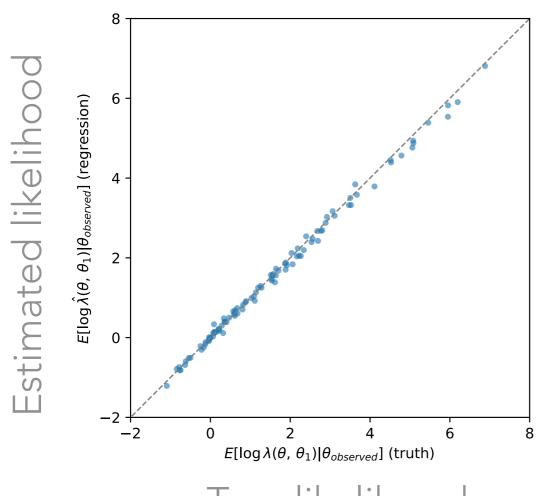
if the scalar map s: $X \to \mathbb{R}$ has the same level sets as the likelihood ratio

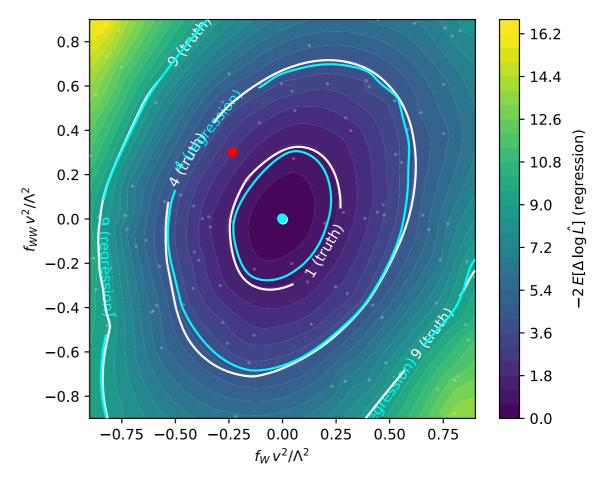
$$s(x; \theta_0; \theta_1) = \text{monotonic}[p(x|\theta_0)/p(x|\theta_1)]$$

Estimating the density of $s(x; \theta_0, \theta_1)$ via the simulator calibrates the ratio.

MACHINE LEARNING THE HIGGS EFFECTIVE FIELD THEORY

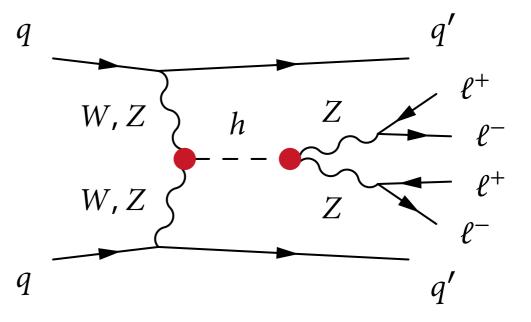
(based on a 16-D observation **x**)





True likelihood

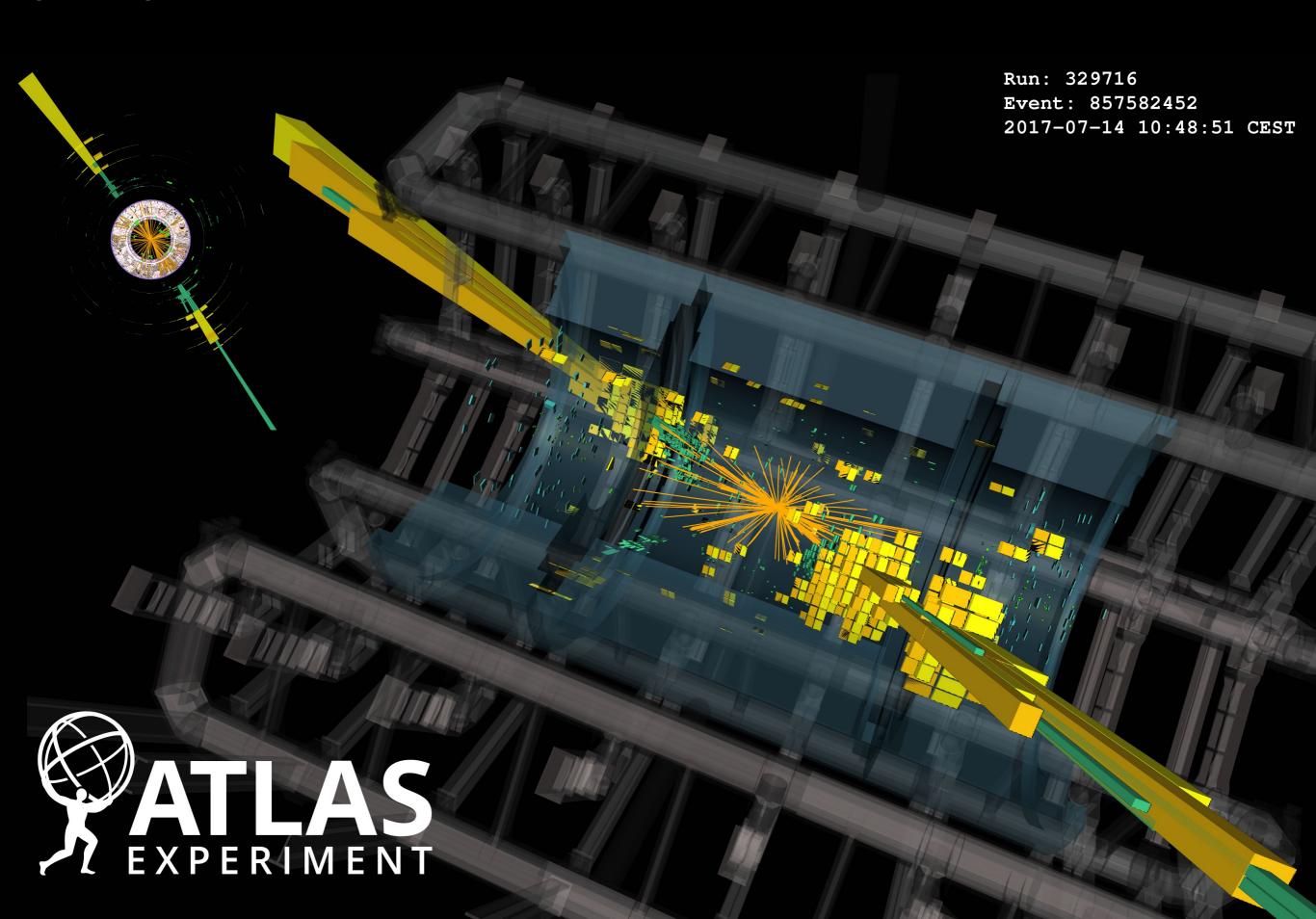
Equivalent to 3x more data!



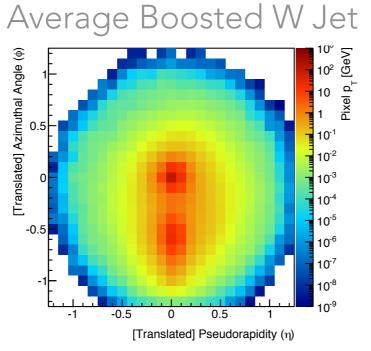
Example:

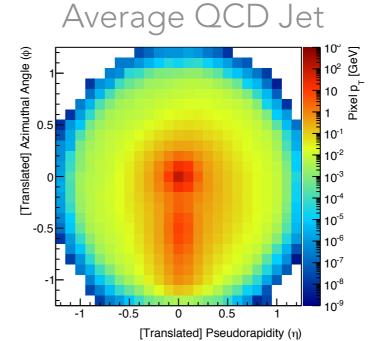
Jet Classification

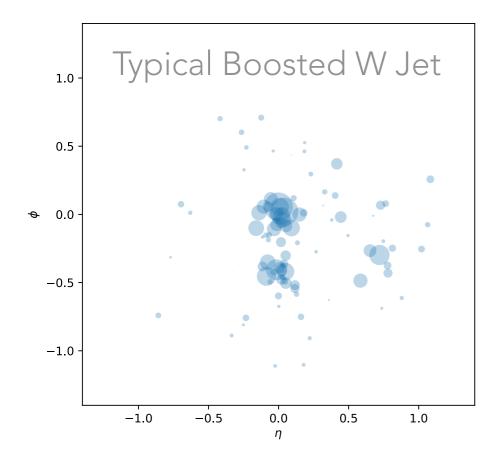
JETS

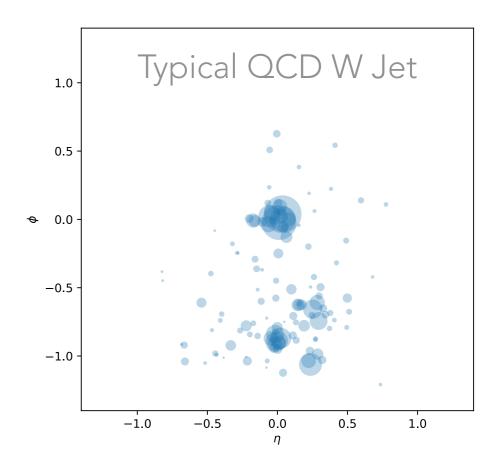


CLASSIFICATION

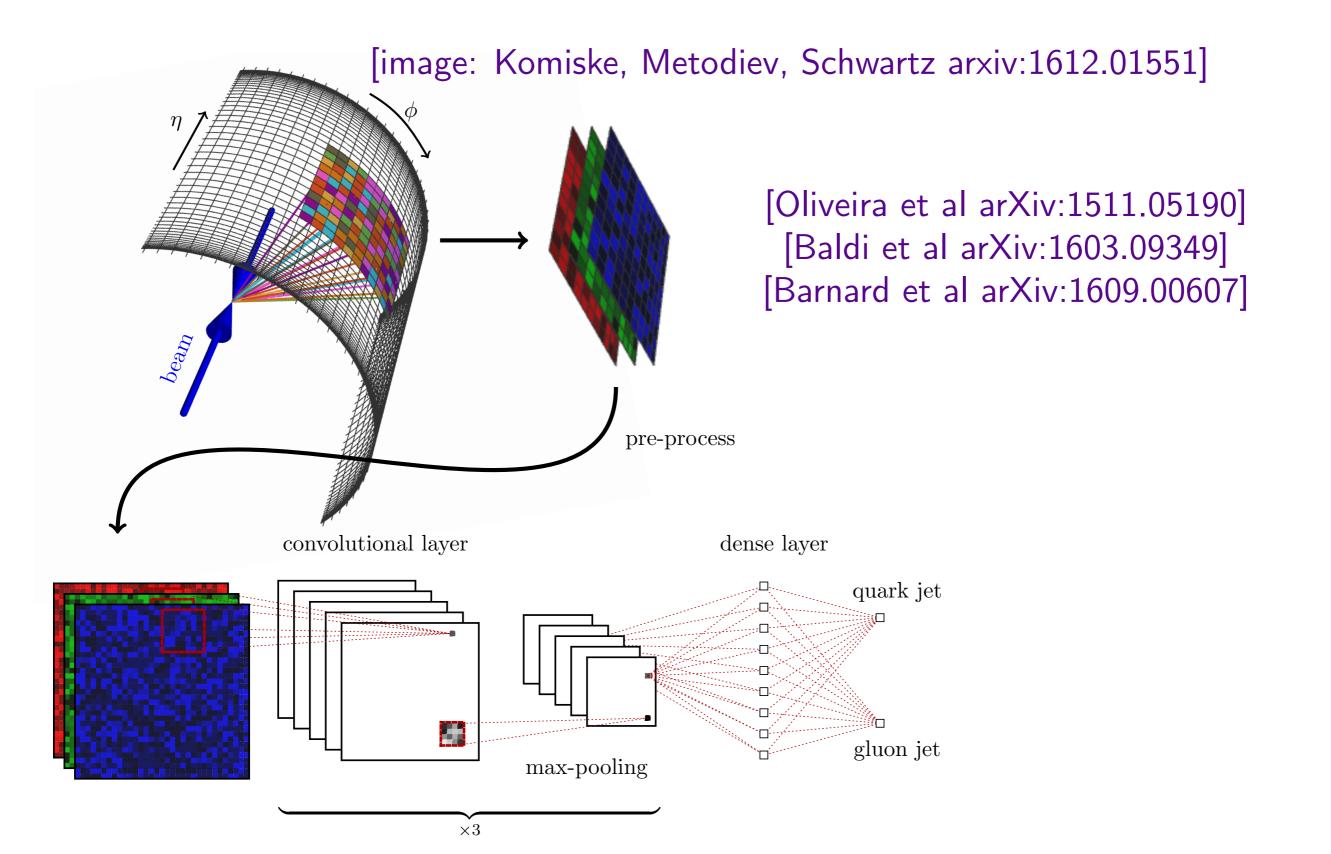




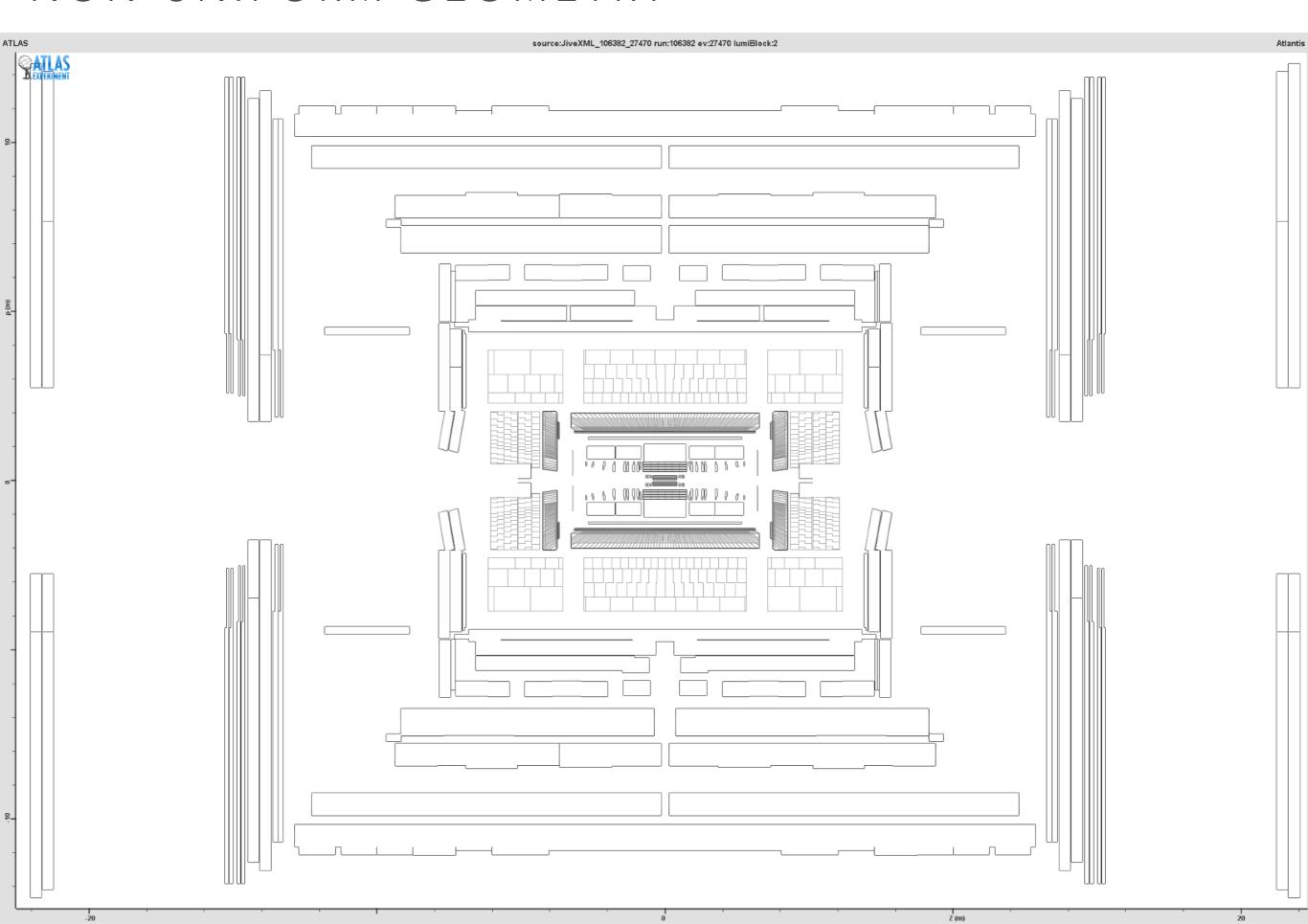




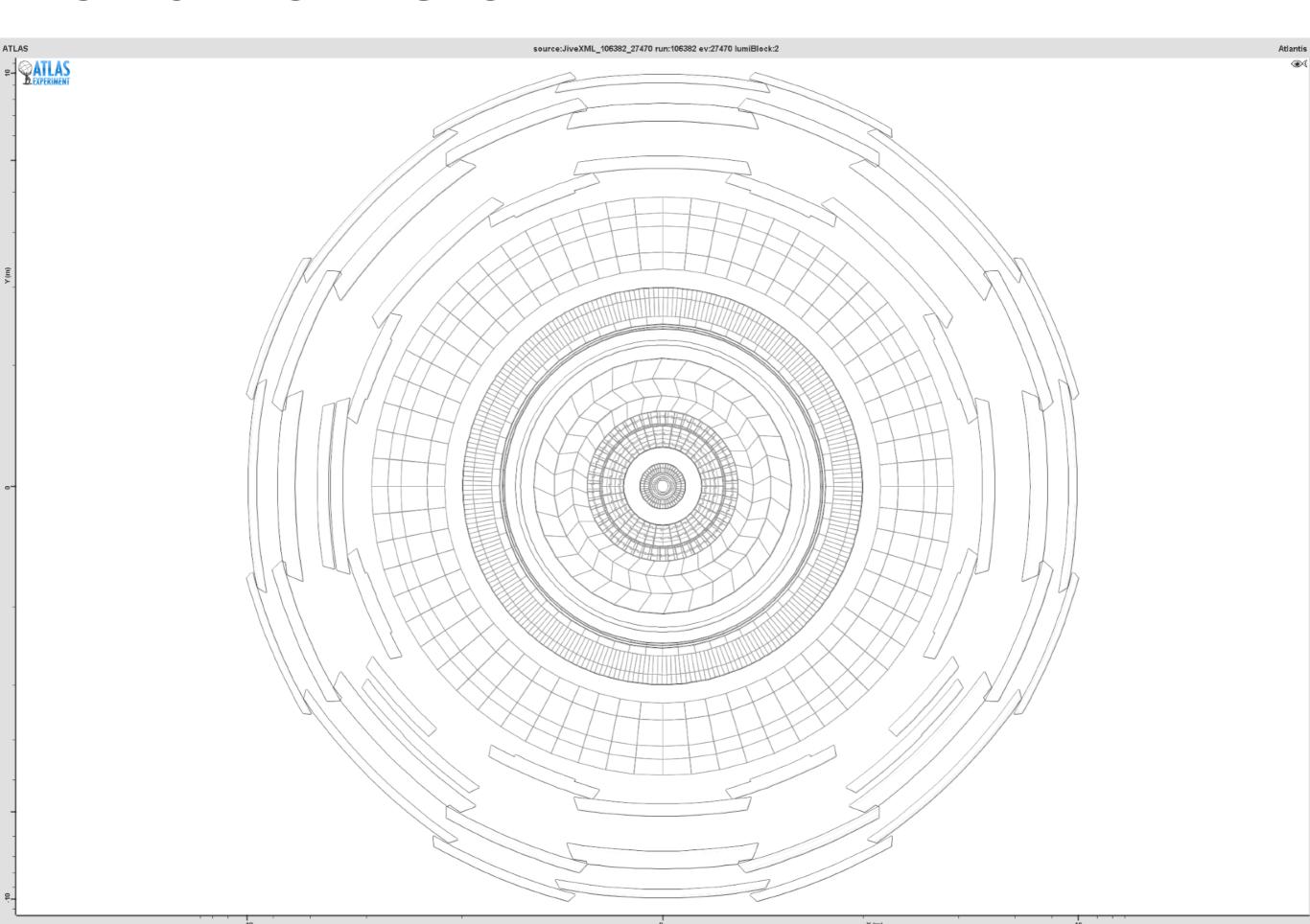
JET IMAGES



NON-UNIFORM GEOMETRY



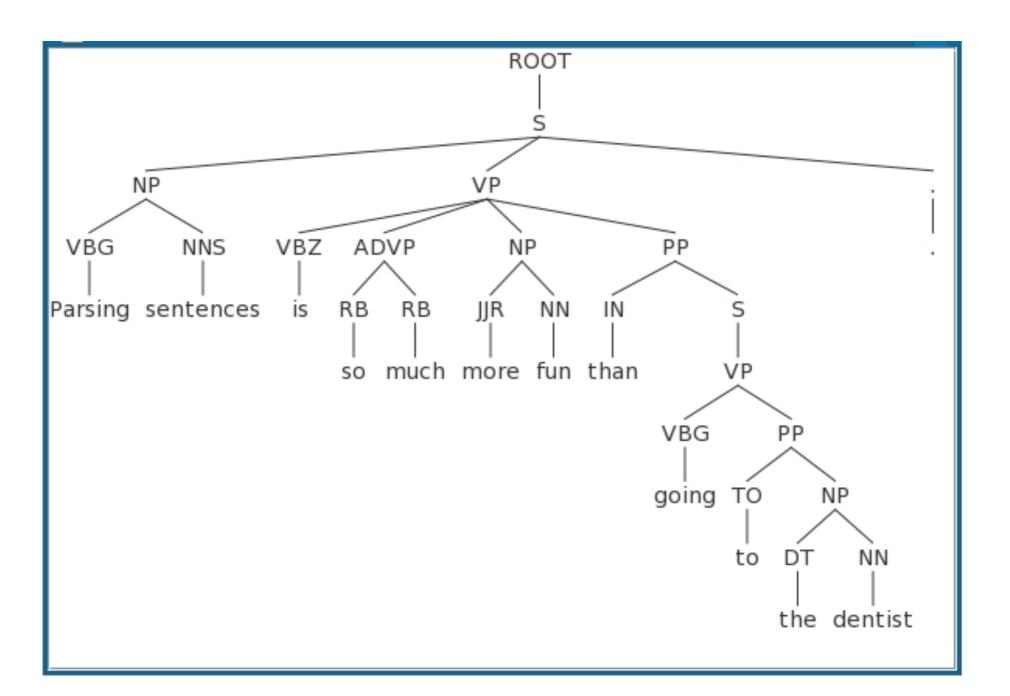
NON-UNIFORM GEOMETRY



FROM IMAGES TO SENTENCES

Recursive Neural Networks showing great performance for Natural Language Processing tasks

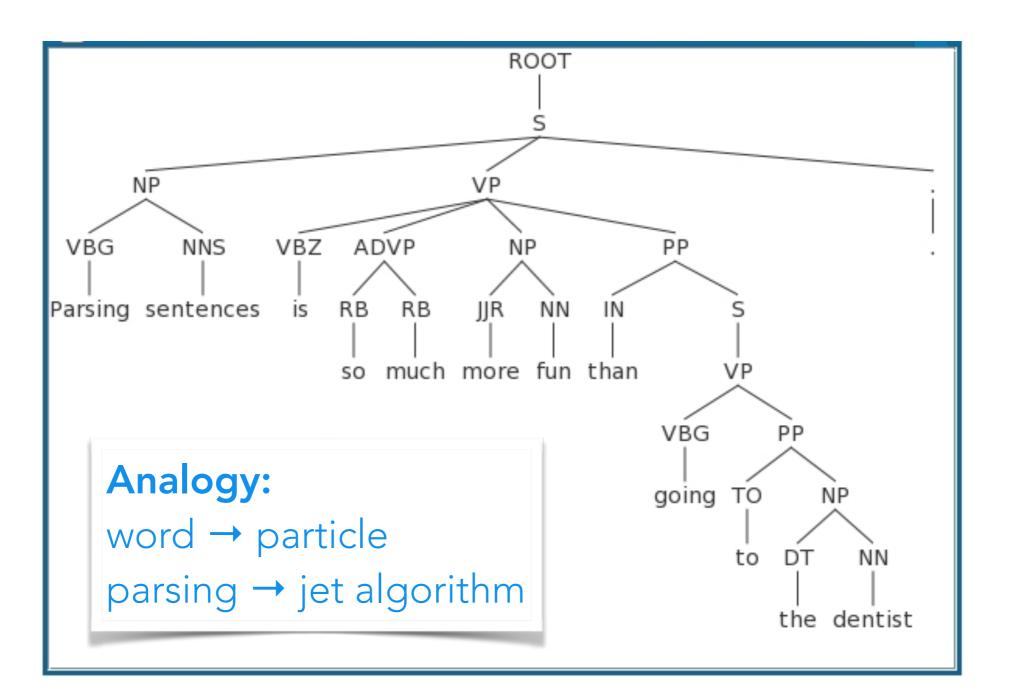
neural network's topology given by parsing of sentence!



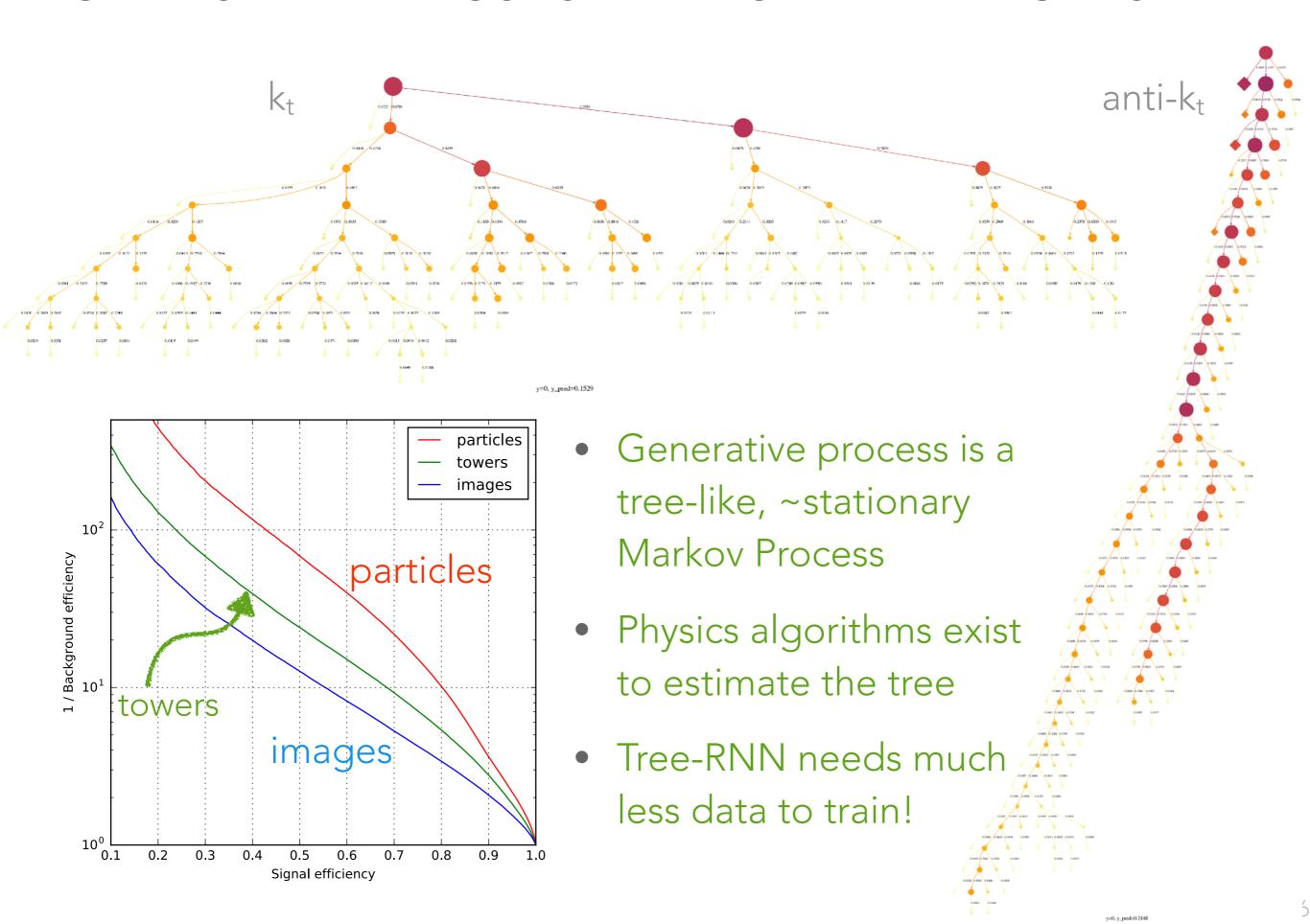
FROM IMAGES TO SENTENCES

Recursive Neural Networks showing great performance for Natural Language Processing tasks

neural network's topology given by parsing of sentence!



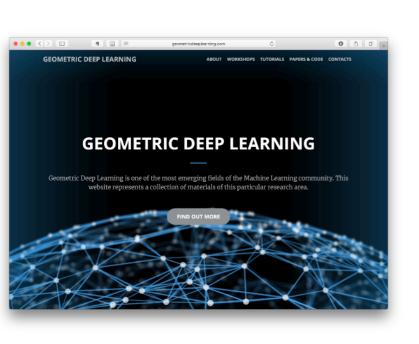
QCD-INSPIRED RECURSIVE NEURAL NETWORKS



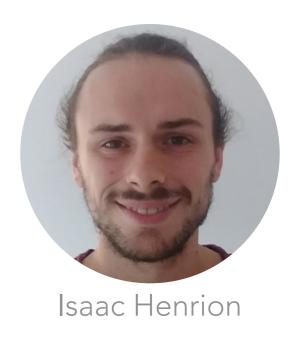
Neural Message Passing for Jet Physics

Isaac Henrion, Johann Brehmer, Joan Bruna, Kyunghyun Cho, Kyle Cranmer, Gilles Louppe, Gaspar Rochette

Courant Institute & Center for Data Science





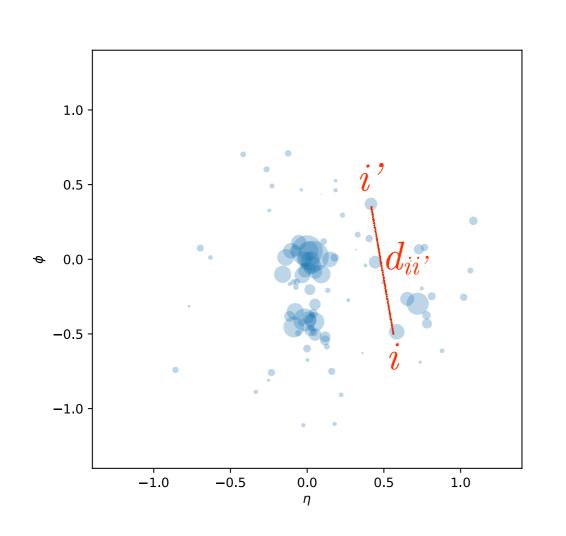


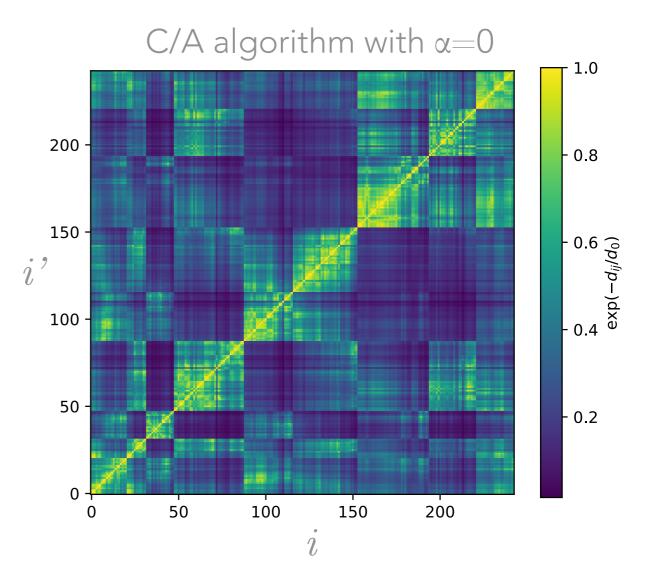
Paper: https://dl4physicalsciences.github.io/files/nips_dlps_2017_29.pdf
Talk: https://dl4physicalsciences.github.io/files/nips_dlps_2017_slides_henrion.pdf

JETS AS A GRAPH

Using message passing neural networks over a fully connected graph on the particles

- Two approaches for adjacency matrix for edges
 - **import** physics knowledge by using metric of jet algorithms $d_{ii'}^{\alpha} = \min(p_{ti}^{2\alpha}, p_{ti'}^{2\alpha}) \frac{\Delta R_{ii'}^2}{R^2}$
 - learn adjacency matrix and **export** new jet algorithm





1/FPR @ TPR = 50%		
Model	Iterations	$R_{\epsilon=50\%}$
Rec-NN (no gating)	1	70.4 ± 3.6
Rec-NN (gating)	1	83.3 ± 3.1
MPNN (directed)	1	89.4 ± 3.5
MPNN (directed)	2	$\textbf{98.3} \pm \textbf{4.3}$
MPNN (directed)	3	85.9 ± 8.5
MPNN (identity)	3	74.5 ± 5.2
Relation Network	1	67.7 ± 6.8

Significant improvement on W vs. QCD jet classification!

This is with a learned adjacency matrix

- what did it learn? Is that adjacency matrix useful?
- we are working MPNN with QCD-motivated adjacency matrix

Example:

Optimizing Non-Differentiable Simulators

NEW! AVO

Adversarial Variational Optimization of Non-Differentiable Simulators

Gilles Louppe¹ and Kyle Cranmer¹

New York University

Complex computer simulators are increasingly used across fields of science as generative models tying parameters of an underlying theory to experimental observations. Inference in this setup is often difficult, as simulators rarely admit a tractable density or likelihood function. We introduce Adversarial Variational Optimization (AVO), a likelihood-free inference algorithm for fitting a non-differentiable generative model incorporating ideas from empirical Bayes and variational inference. We adapt the training procedure of generative adversarial networks by replacing the differentiable generative network with a domain-specific simulator. We solve the resulting non-differentiable minimax problem by minimizing variational upper bounds of the two adversarial objectives. Effectively, the procedure results in learning a proposal distribution over simulator parameters, such that the corresponding marginal distribution of the generated data matches the observations. We present results of the method with simulators producing both discrete and continuous data.

catch me

if you can

Leo is G

Tom is D

Similar to W-GAN setup, but instead of using a neural network as the generator, use the actual simulation (eg. Pythia, GEANT)

Continue to use a neural network discriminator / critic.

Difficulty: the simulator isn't differentiable, but there's a **trick**!

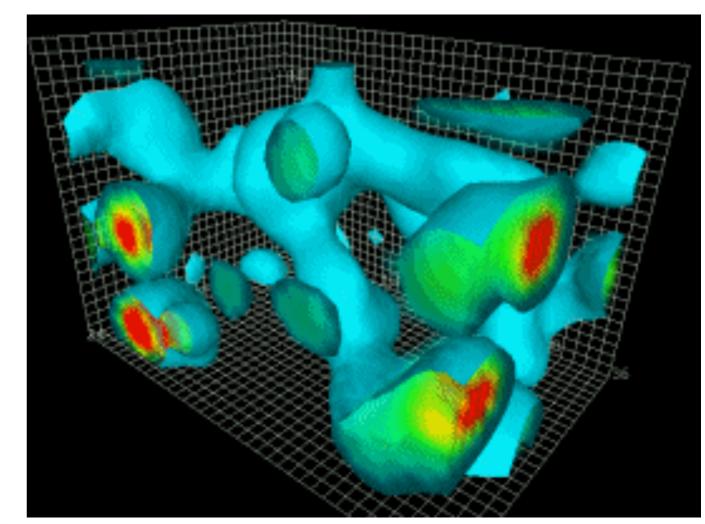
Allows us to efficiently fit / tune simulation with stochastic gradient techniques!

Example:

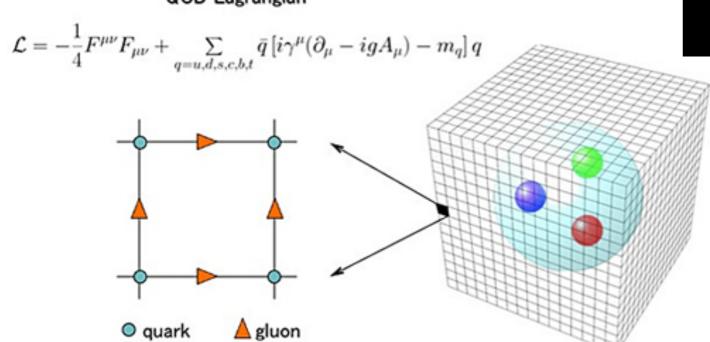
Lattice Field Theory

LATTICE QUANTUM CHROMO DYNAMICS

Very expensive simulations, ~1000 examples with $x \in \mathbb{R}^{10^9}$

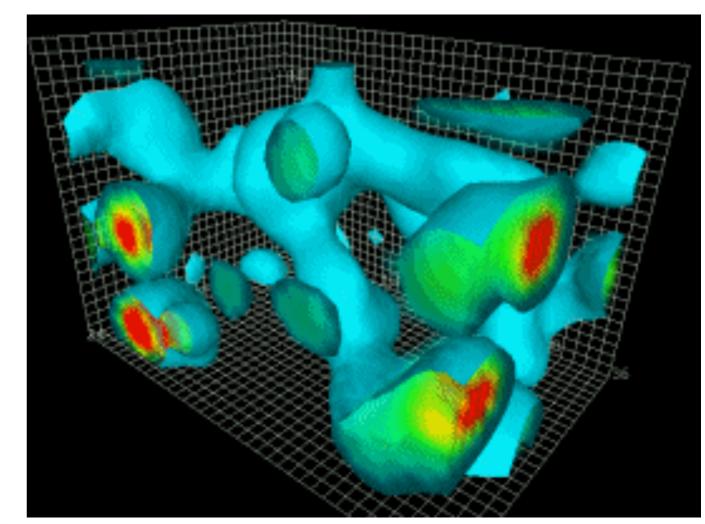


QCD Lagrangian

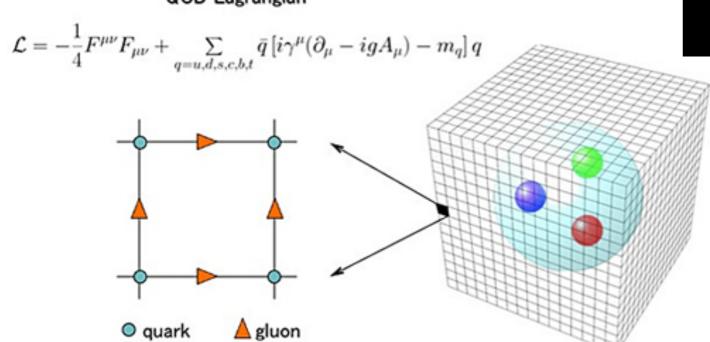


LATTICE QUANTUM CHROMO DYNAMICS

Very expensive simulations, ~1000 examples with $x \in \mathbb{R}^{10^9}$



QCD Lagrangian



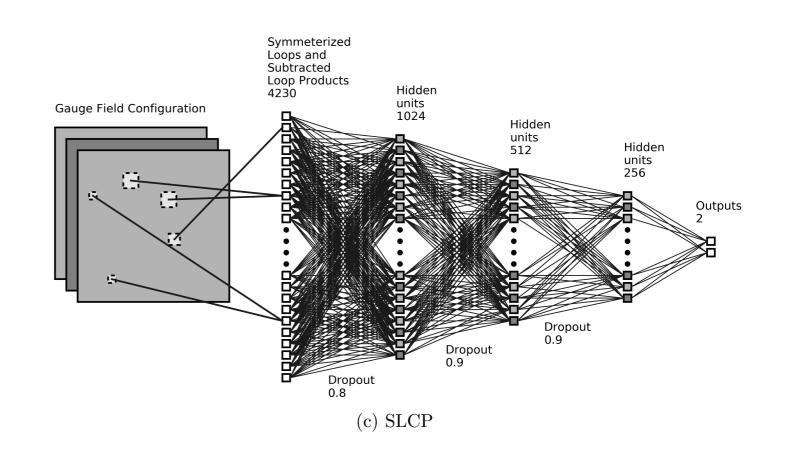
LATTICE QCD

Each of the 10^7 lattice locations has data $x_i \in \mathbb{R}^{32}$ with non-trivial data with continuous local symmetry.

- space-time translation invariance → convolutional architecture
- local gauge symmetry → design group-invariant convolutional filters
- coarse graining & renormalization group → hierarchical convolutions shared weights
- few very, large training examples → rethink minibatching & SGD

Bonus:

Network discovered something unexpected, a feature that has a long auto-correlation time.



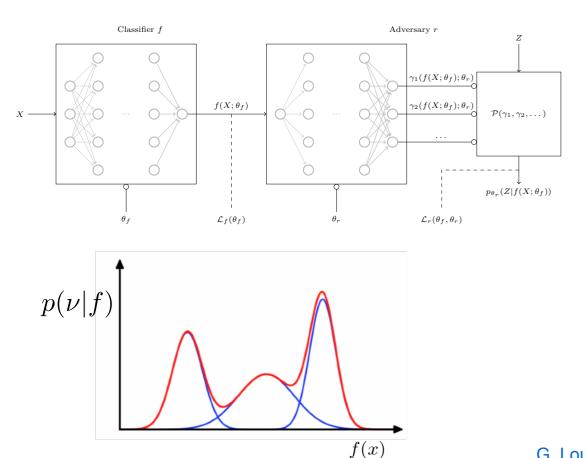
Example:

Systematics Uncertainty
Continuous Domain Adaptation
Fairness on Continuous Attributes

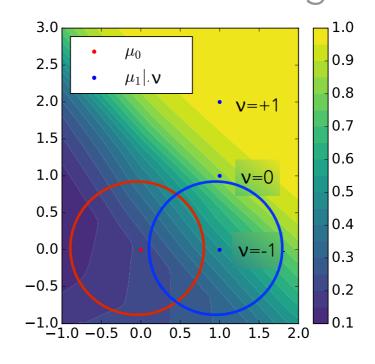
LEARNING TO PIVOT WITH ADVERSARIAL NETWORKS

Typically classifier f(x) trained to minimize loss L_f .

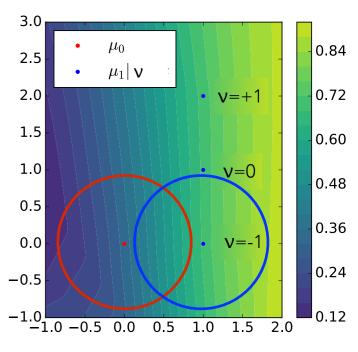
- want classifier output to be insensitive to systematics (nuisance parameter v)
- introduce an adversary \mathbf{r} that tries to predict \mathbf{v} based on \mathbf{f} .
- setup as a minimax game:

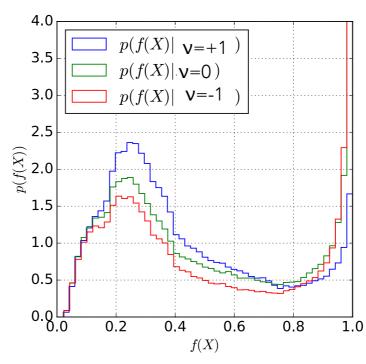


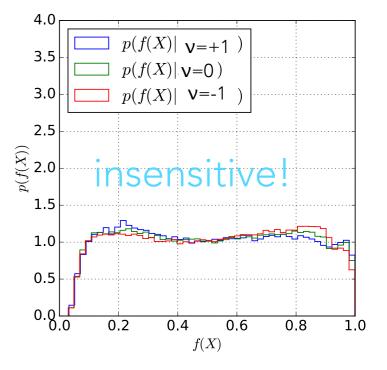
normal training



adversarial training



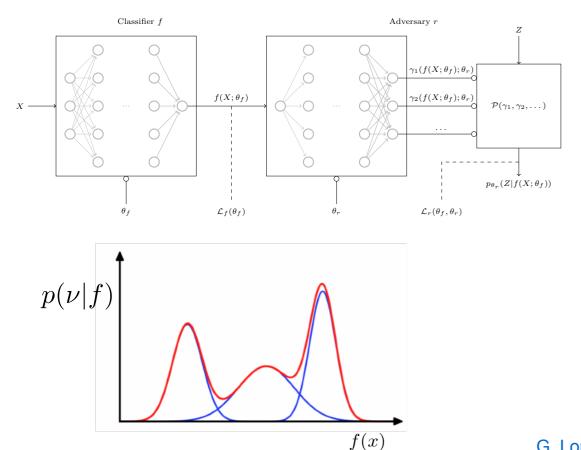




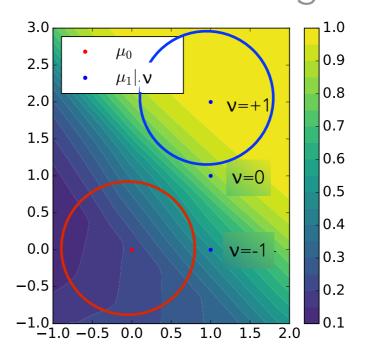
LEARNING TO PIVOT WITH ADVERSARIAL NETWORKS

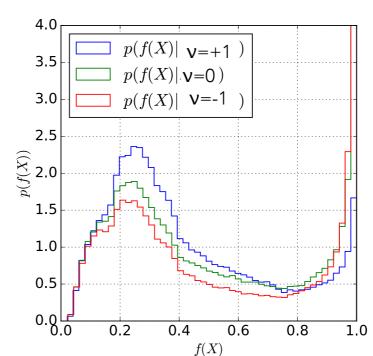
Typically classifier f(x) trained to minimize loss L_f .

- want classifier output to be insensitive to systematics (nuisance parameter v)
- introduce an **adversary r** that tries to predict **v** based on f.
- setup as a minimax game:

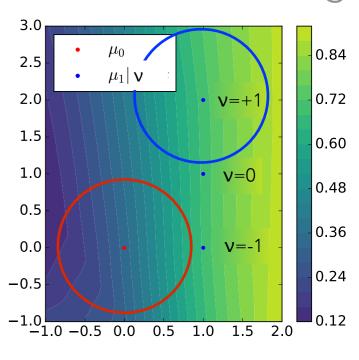


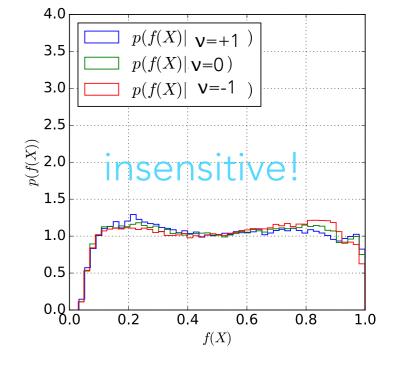
normal training





adversarial training



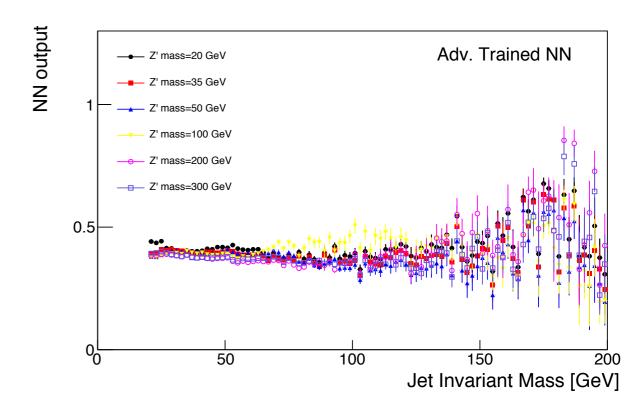


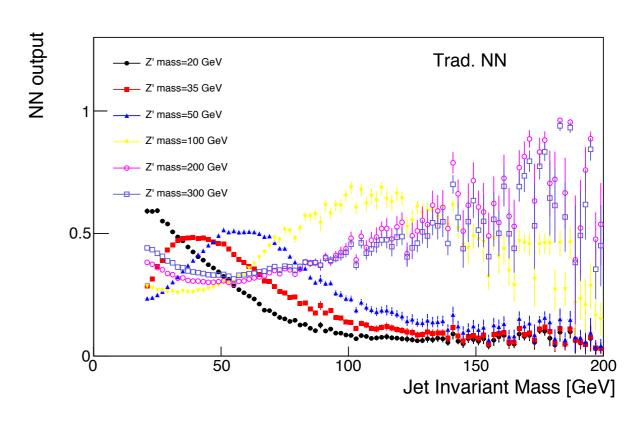
K.C, J. Pavez, and G. Louppe, arXiv:1506.02169 P. Baldi, K.C, T. Faucett, P. Sadowski, D. Whiteson arXiv:1601.07913 G. Louppe, M. Kagan, K.C, arXiv:1611.01046 Shimmin, et. al. arXiv:1703.03507

Adversarial approach of "Learning to Pivot" can also be used to train a classifier that is independent from some other continuous variable.

 fairness to continuous attribute

 motivation for doing this is related to robustnesss to uncertainties and interpretability





Example:

Reusable components

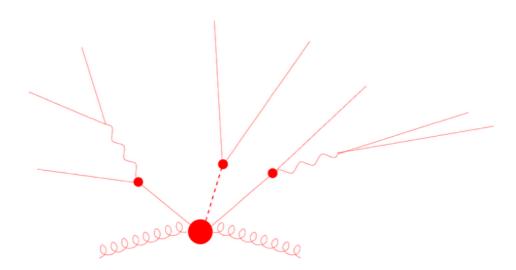
"Of course, particle physicists are among the first to realize that nature is compositional."

- YANN LECUN

"The world is compositional, or there is a god"

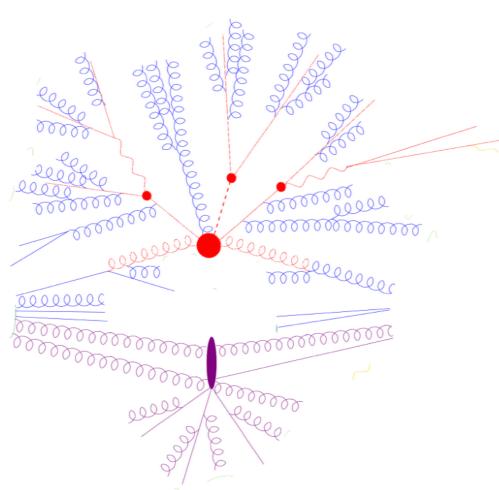
- JASON EISNER

pencil & paper calculable from first principles $p(z_1 \mid \theta)$

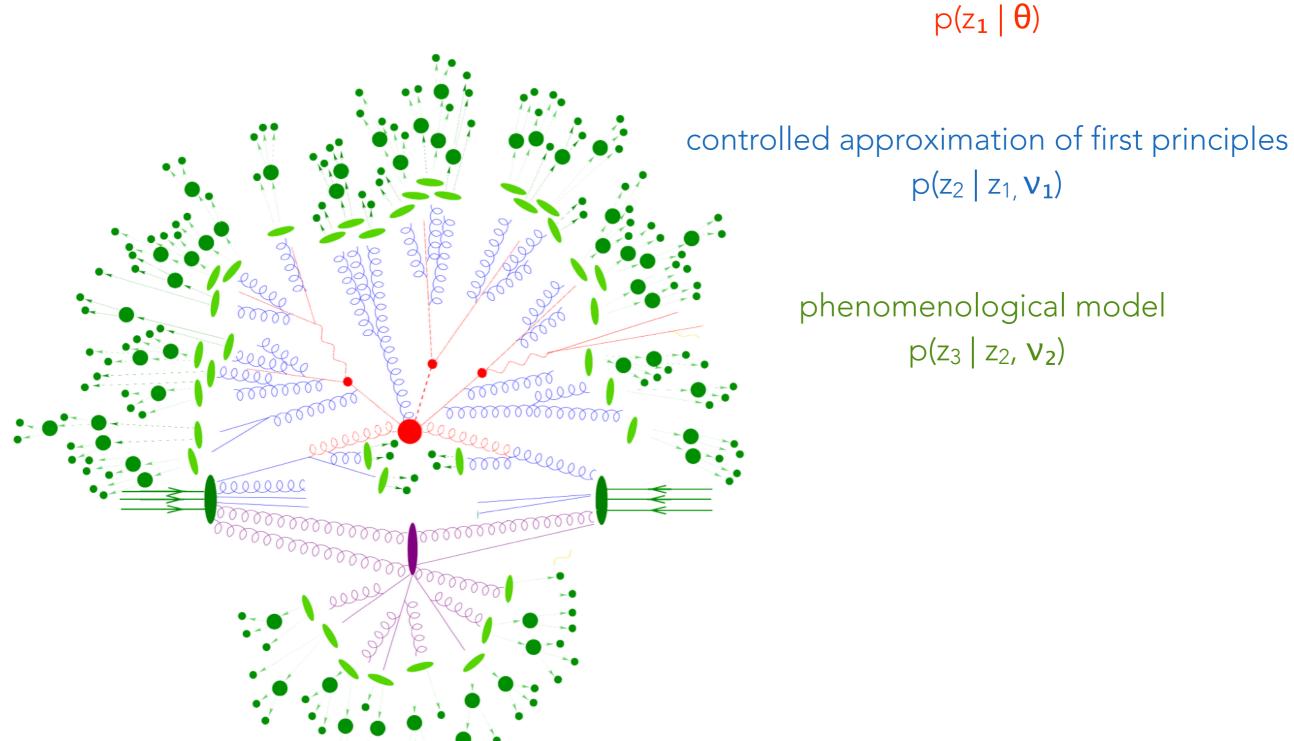


pencil & paper calculable from first principles $p(z_1 \mid \boldsymbol{\theta})$

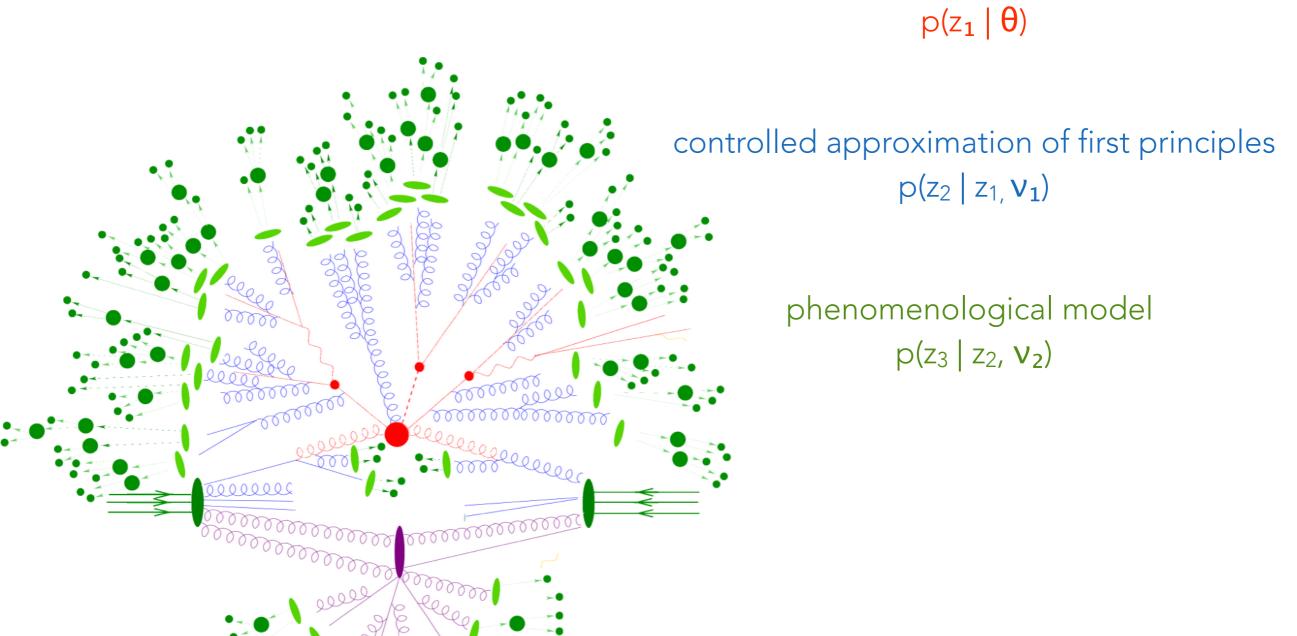
controlled approximation of first principles $p(z_2 \mid z_1, \nu_1)$



pencil & paper calculable from first principles $p(z_1 \mid \theta)$

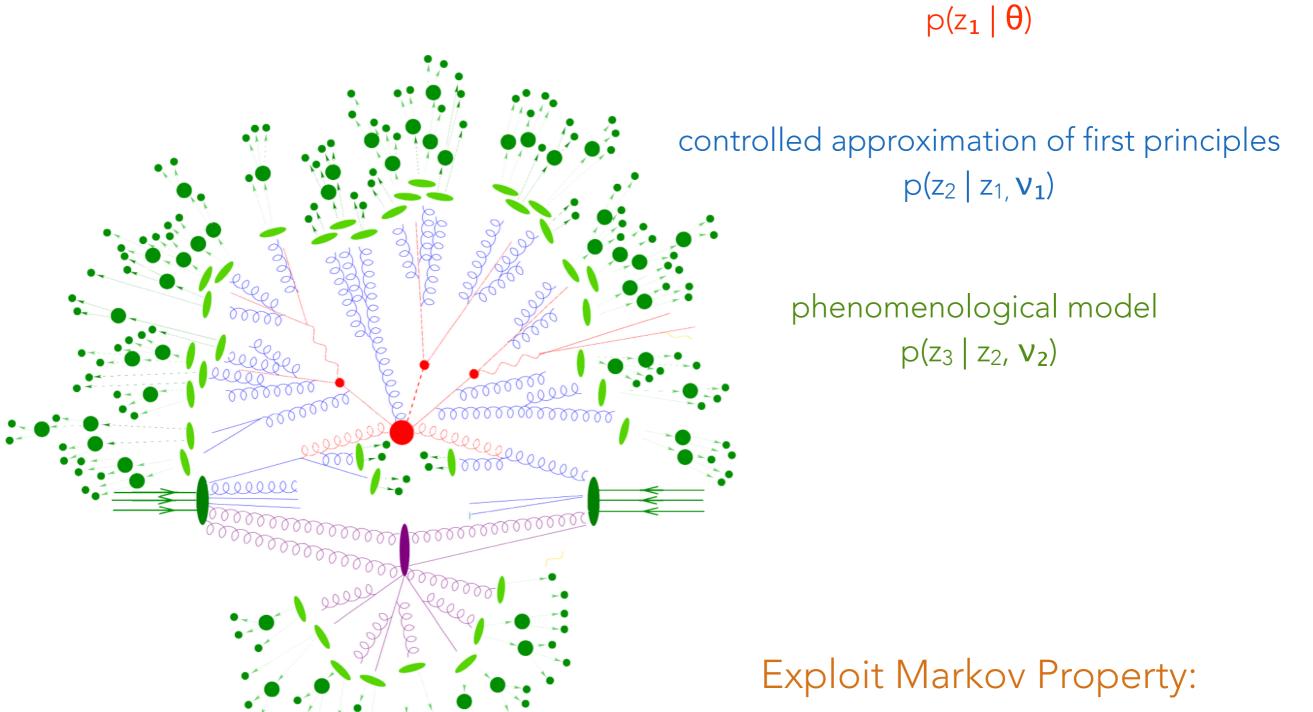


pencil & paper calculable from first principles $p(z_1 \mid \theta)$

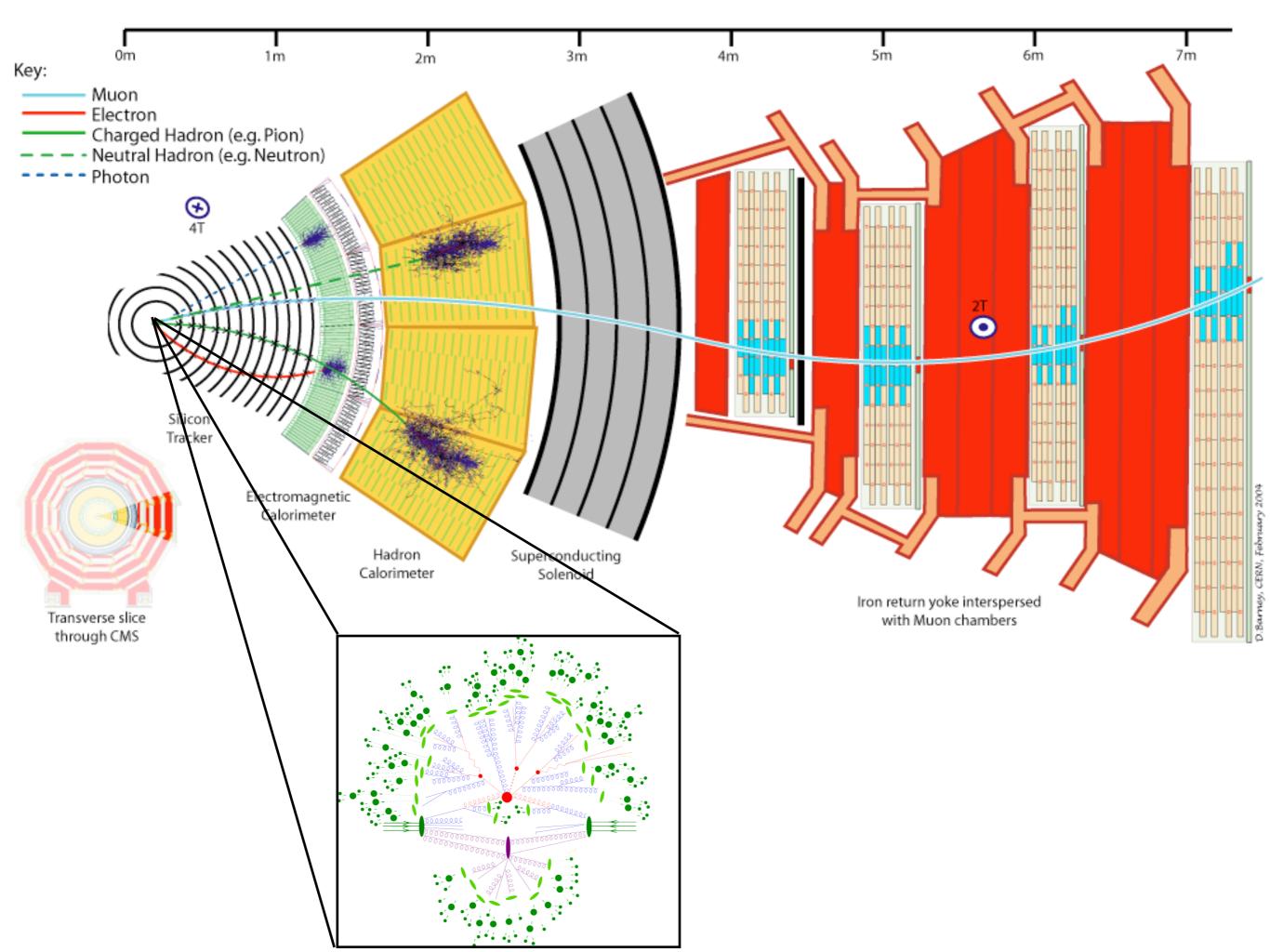


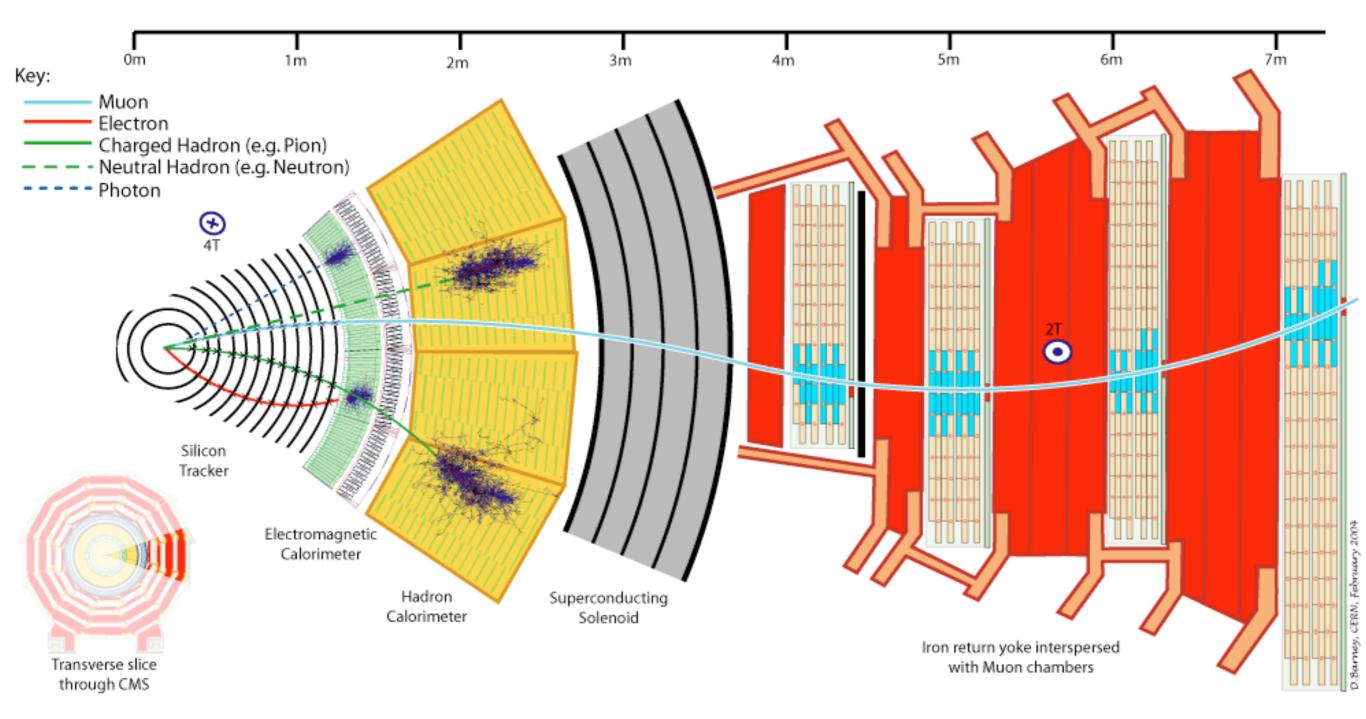
Exploit Markov Property:

pencil & paper calculable from first principles $p(z_1 \mid \theta)$



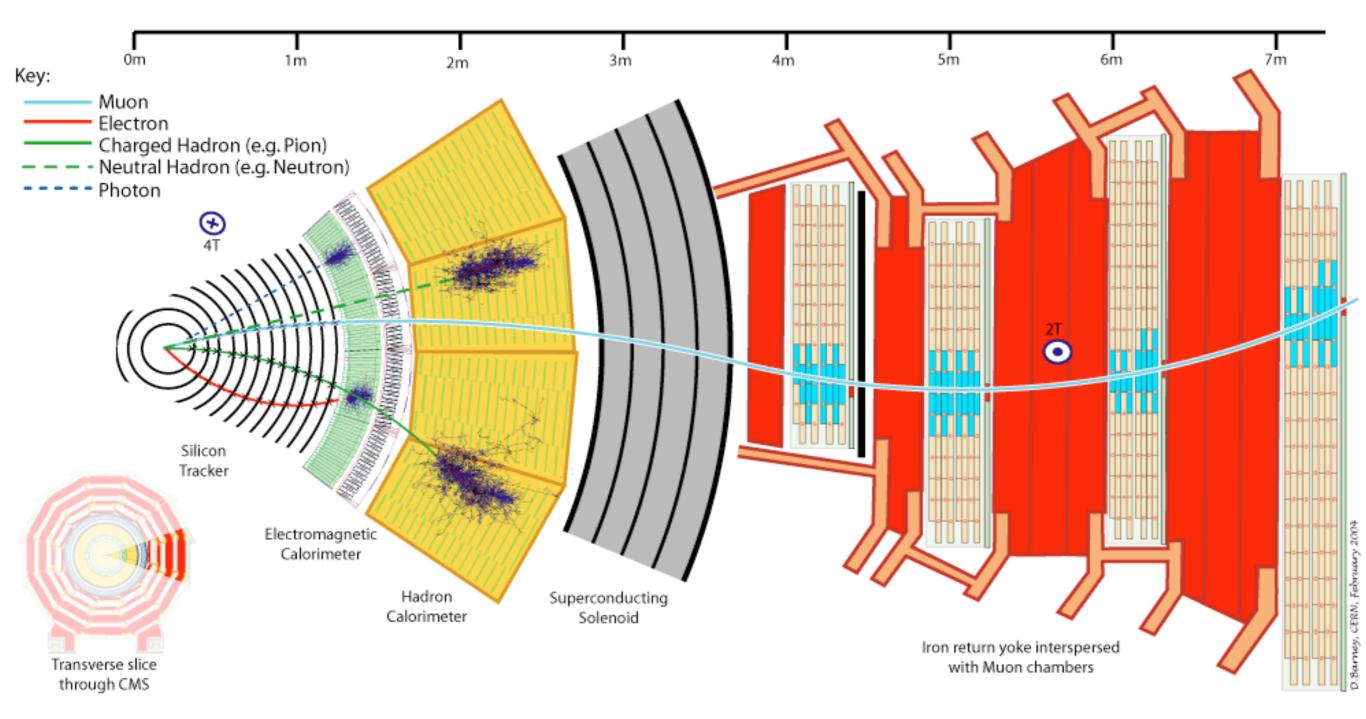
 $p(x|\theta) = \int p(x | z_3, v_3) p(z_3 | z_2, v_2) p(z_2 | z_1, v_1) p(z_1 | \theta) dz$





Detector Simulation $p(x \mid z_3, v_3)$:

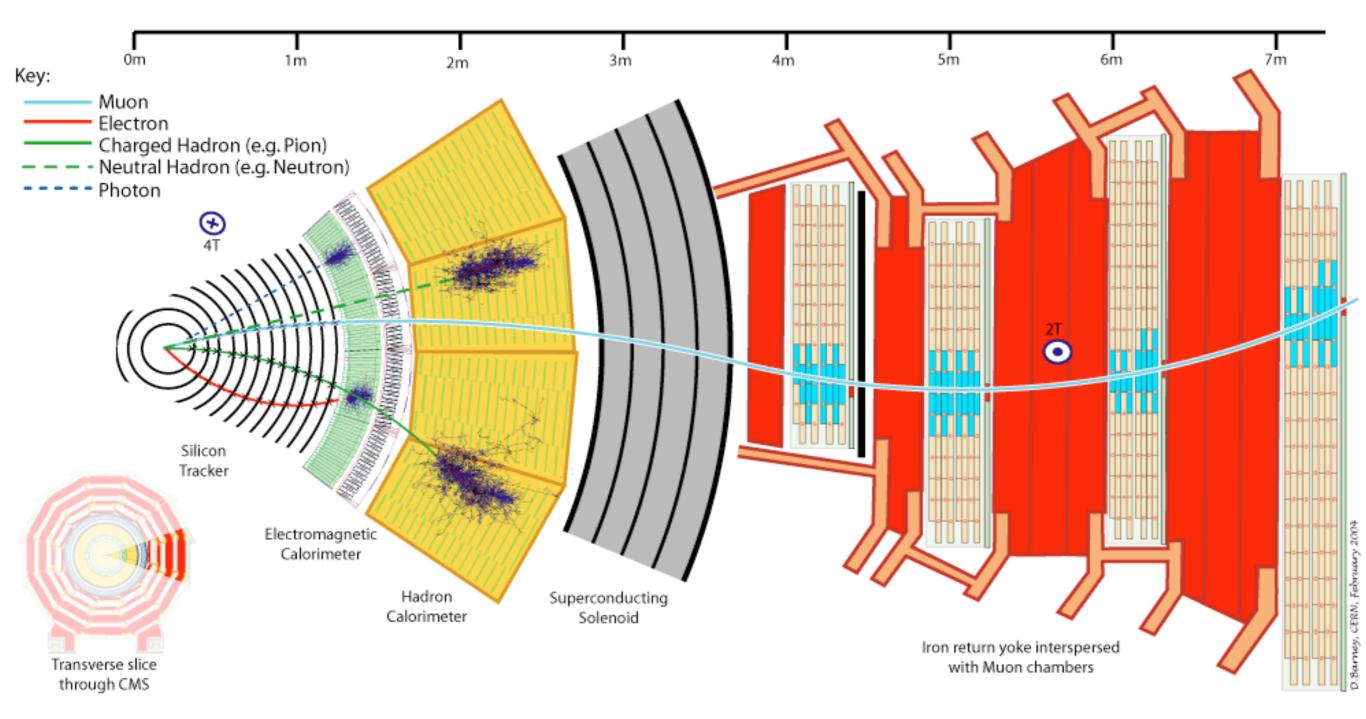
- detailed engineering (CAD)
- in situ measurements of temperature, magnetic field, alignment, calibration constants
- first-principles description of interaction of particles with matter
- look up tables of measured interaction of particles with matter



Detector Simulation $p(x \mid z_3, v_3)$:

- detailed engineering (CAD)
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Exploit Markov Property:

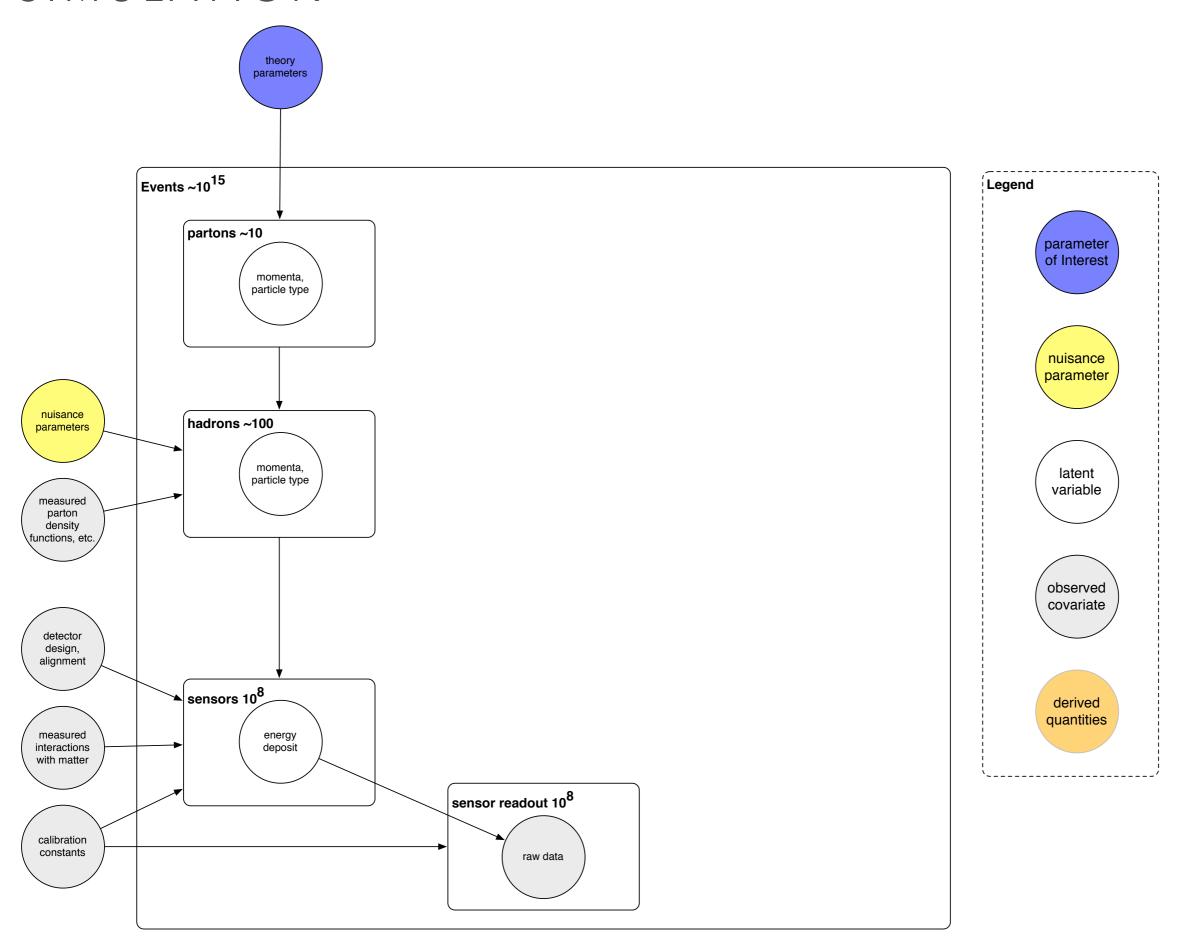


Detector Simulation $p(x \mid z_3, v_3)$:

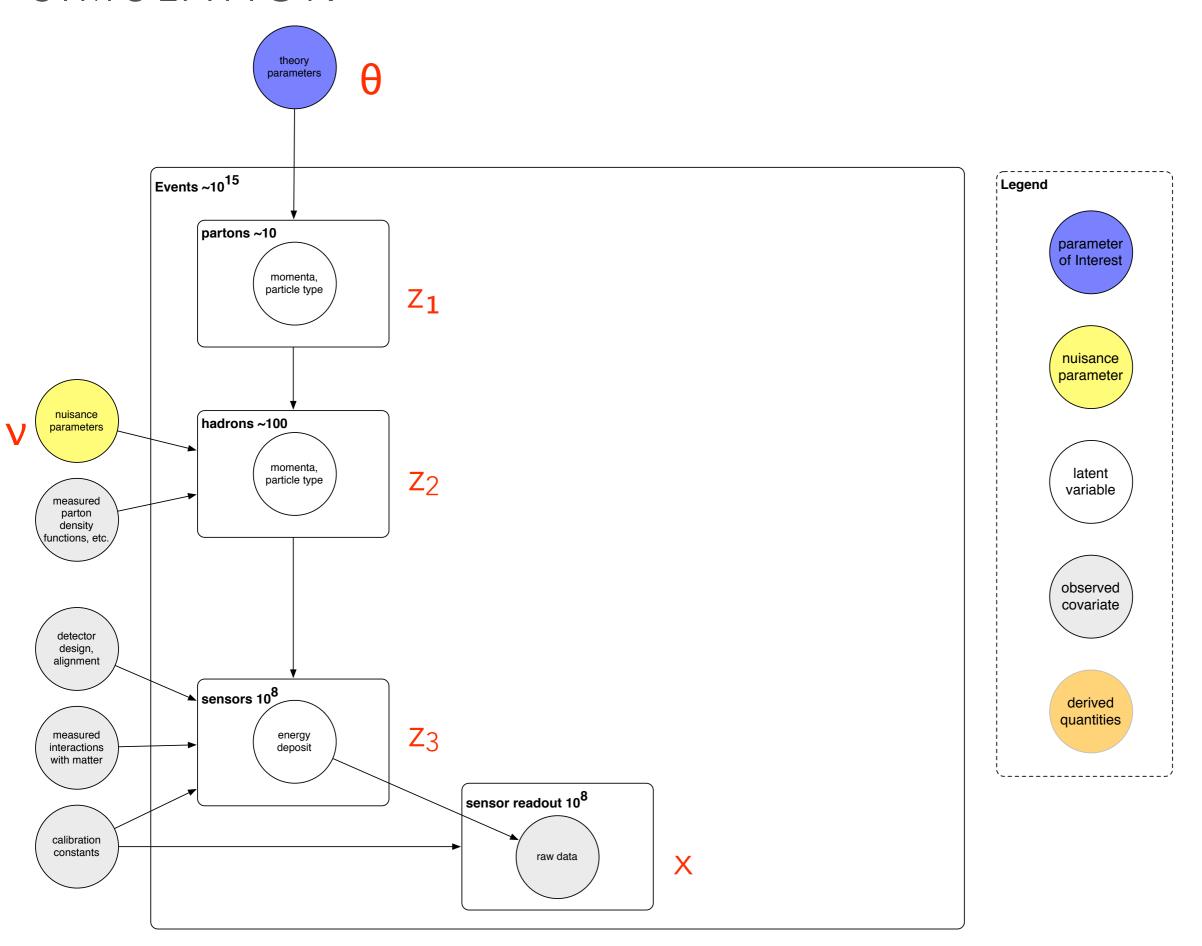
- detailed engineering (CAD)
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- first-principles description of interaction of particles with matter
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Exploit Markov Property: $p(x|\theta) = \int p(x|z_3, v_3) p(z_3|z_2, v_2) p(z_2|z_1, v_1) p(z_1|\theta) dz$

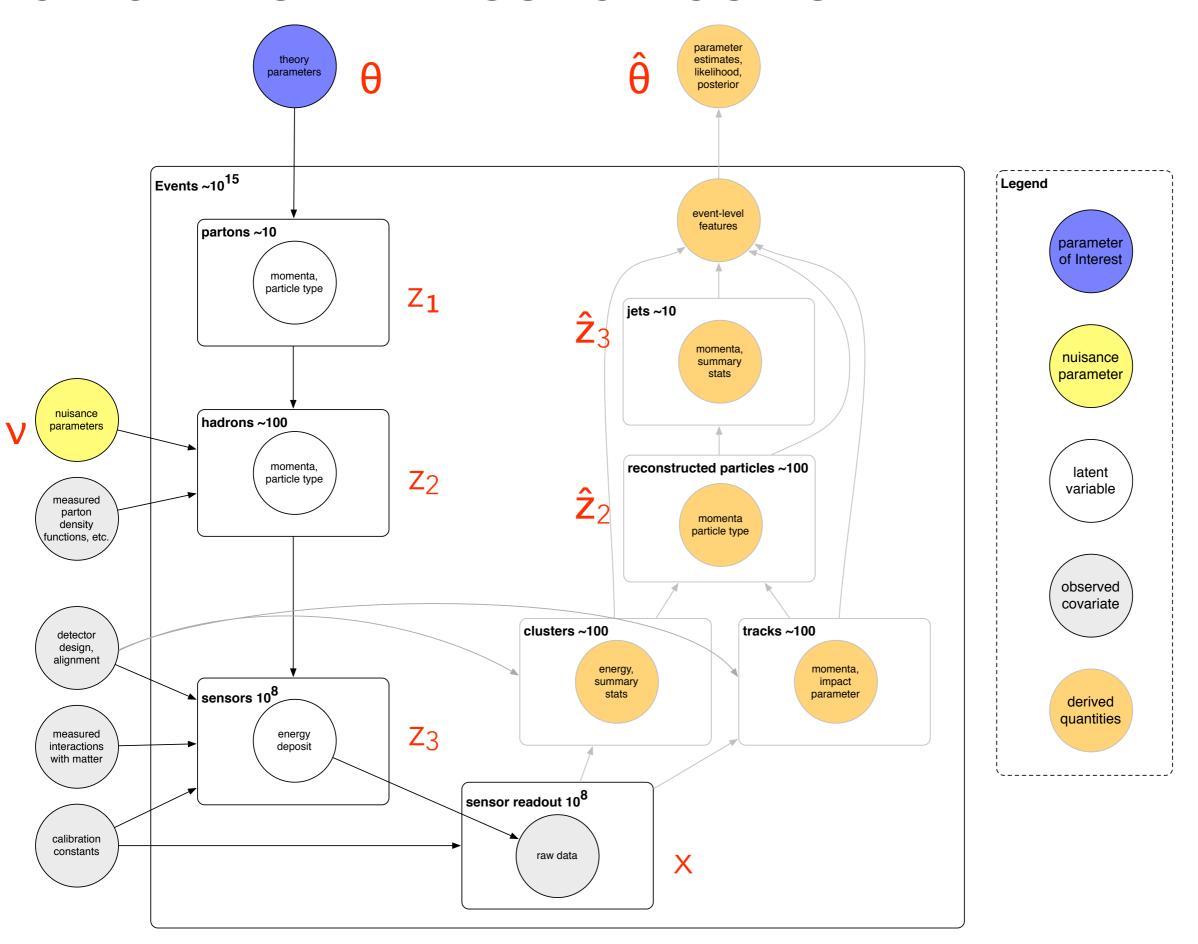
SIMULATION



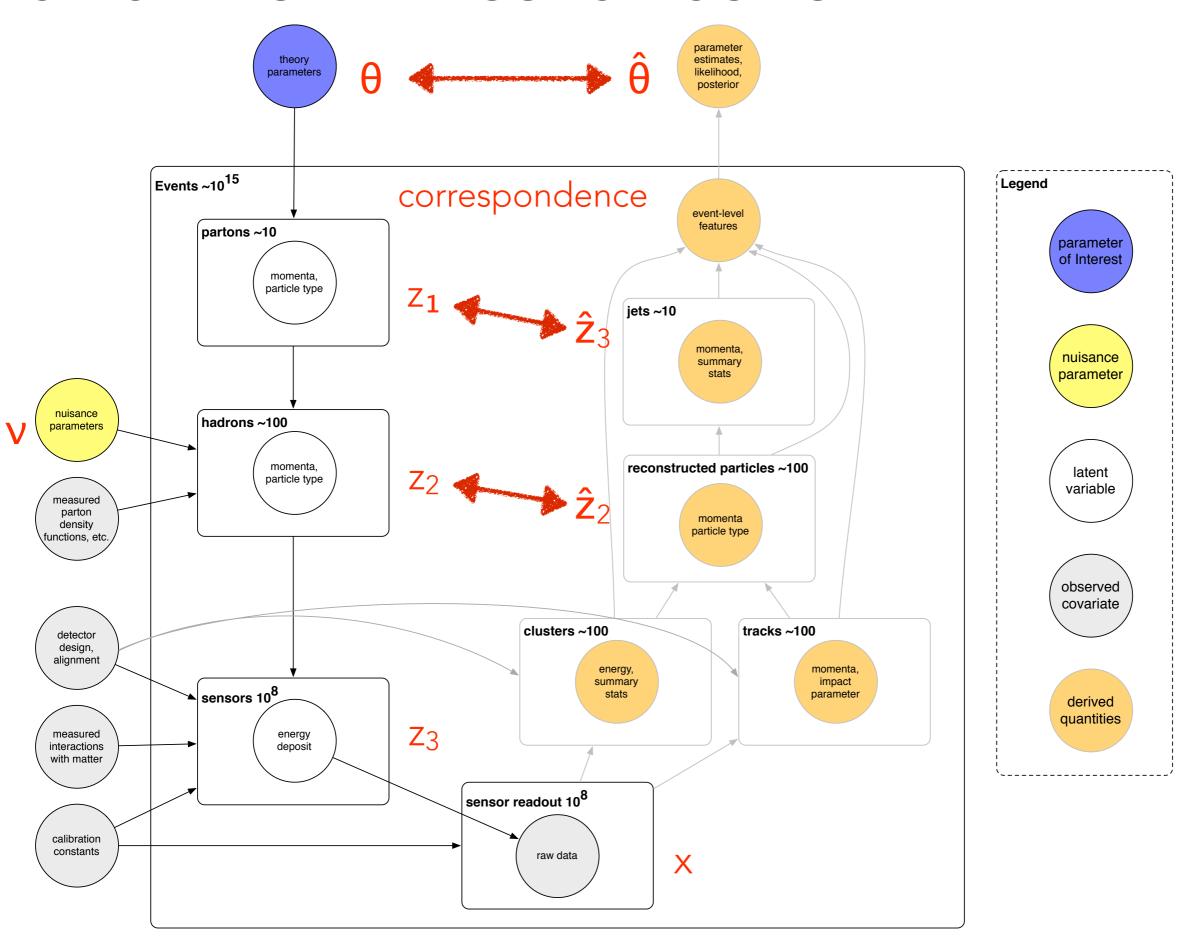
SIMULATION



SIMULATION + RECONSTRUCTION



SIMULATION + RECONSTRUCTION



COMPOSITION & REDUCTIONISM

The traditional reconstruction algorithms can be seen as attempt to invert the generative process (point estimate / regression)

- generative model: $\theta \rightarrow z_1 \rightarrow z_2 \rightarrow z_2 \rightarrow x$
- Sequential Inversion: $x \to \hat{z}_3(x) \to \hat{z}_2(\hat{z}_3) \to \hat{z}_1(\hat{z}_2)$

Key points:

- can characterize & validate $p(\hat{z}_1 \mid z_1)$, $p(\hat{z}_2 \mid z_2)$, $p(\hat{z}_3 \mid z_3)$ with simulation
- these components are reusable (transfer learning)
 - e.g. an algorithm that looks for electrons in the data (segmentation & classification) and estimates their energy and momentum (regression).
- Provides a notion of "interpretable" that is practical and actionable
- Composition is at the heart of the reductionist paradigm of science

COMPOSITION OF REUSABLE COMPONENTS

How do these fit together?

Combine many of these ideas:

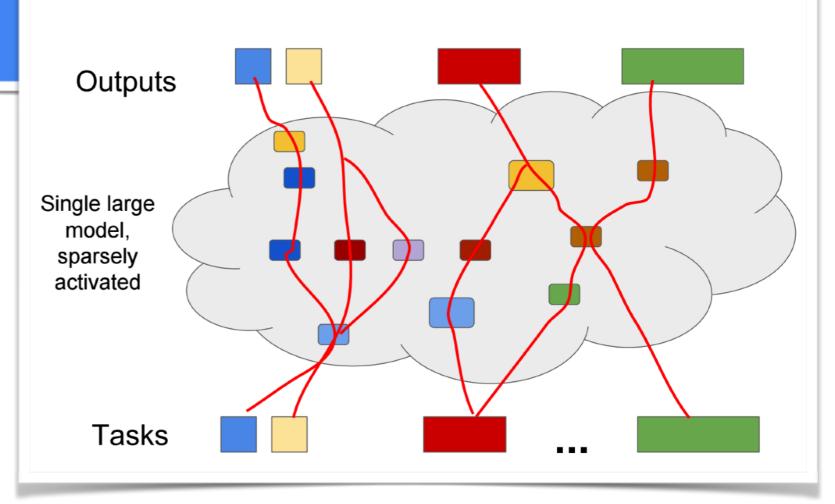
Large model, but sparsely activated
Single model to solve many tasks (100s to 1Ms)

Dynamically learn and grow pathways through large model
Hardware specialized for ML supercomputing

ML for efficient mapping onto this hardware



Google



DIFFERENTIABLE REDUCTIONISM

The reconstruction algorithms can be seen as attempt to invert the generative process (point estimate / regression) sequentially

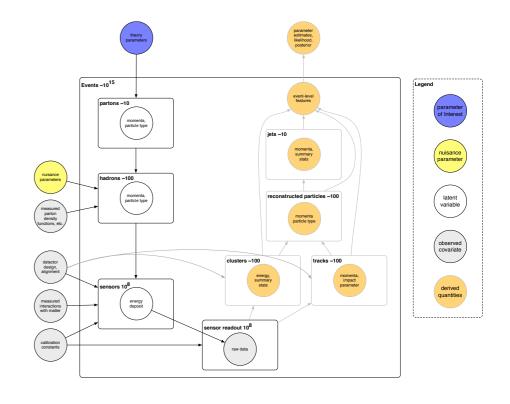
- generative model: $\theta \rightarrow z_1 \rightarrow z_2 \rightarrow z_2 \rightarrow x$
- Sequential Inversion: $x \to \hat{z}_3(x) \to \hat{z}_2(\hat{z}_3) \to \hat{z}_1(\hat{z}_2)$

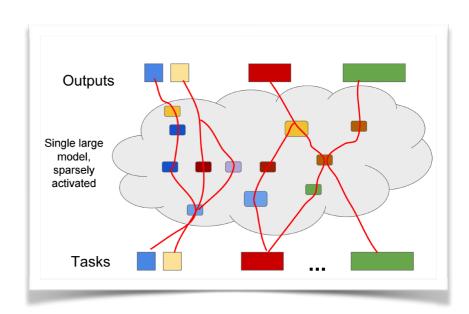
Currently both generative model and inversion algorithms involve handengineered, code not developed for auto-diff / back propagation (effectively not differentiable)

big gain from just reimplementing what we have in a Differentiable
 Programming framework

We can keep the compositional structure and gradually enhance each of the stages of the with deep learning components

- A high-level form of inductive bias (innate structure) on the networks
- jointly optimize & borrow power from all the tasks that use a certain component
 - maintain ability to characterize, validate, and interpret individual components
- transition from deterministic point estimate to probabilistic components for improved uncertainty estimation





CONCLUSION

The developments in machine learning have the potential to effectively bridge the microscopic - macroscopic divide & aid in the inverse problem.

- leverage expert knowledge of the generative process
- learn surrogates that extract relevant features for inference task

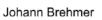
Several strategies to incorporate domain knowledge into the model

- starting point: migrate current code bases to differentiable programming framework
- gradually replace components with deep learning

Helpful to establish more actionable notions of "interpretability"

COLLABORATORS







Kyunghyun Cho



Joan Bruna



Brenden Lake



Meghan Frate



Juan Pavez



Tilman Plehn





Isaac Henrion



Lukas Heinrich



Heiko Müller



Tim Head



Michael Kagan



David Rousseau



Peter Sadowski



Daniel Whiteson



Pierre Baldi



Lezcano Casado



Atılım Güneş Baydin University of Oxford



Prabhat NERSC, Berkeley Lab



Wahid Bhimji NERSC, Berkeley Lab



Frank Wood University of Oxford



Phiala Shanahan



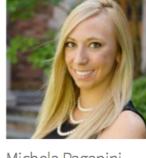
William Detmold



Karen Ng



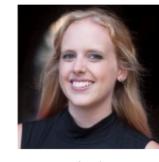
Tuan Anh Le



Michela Paganini Yale University



Daniela Huppenkothen New York University



Savannah Thais Yale University



Ruth Angus Columbia University

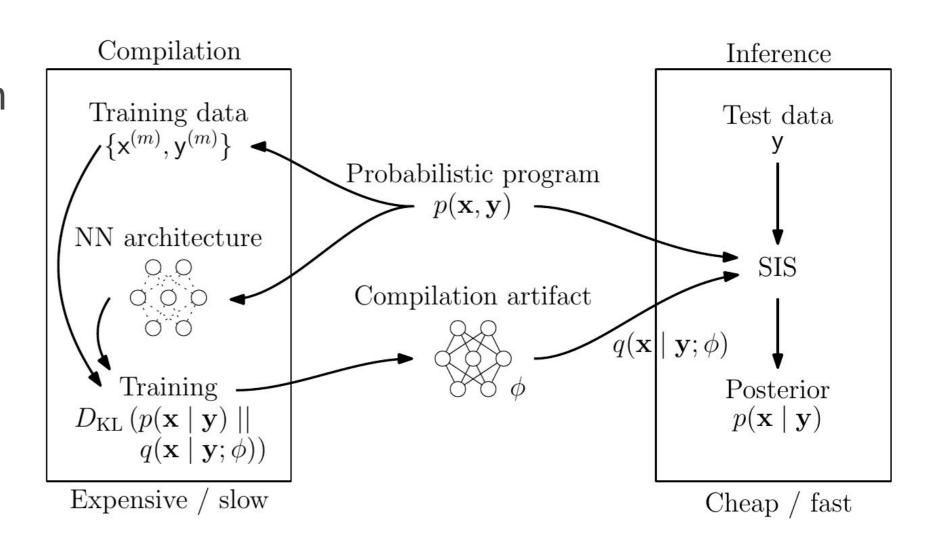
Backup

PROB PROG: HOW DOES IT WORK?

In short: hijack the random number generators and use NN's to perform a *very* smart type of importance sampling

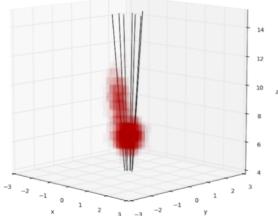
Input: an inference problem denoted in a universal PPL (Anglican, CPProb)

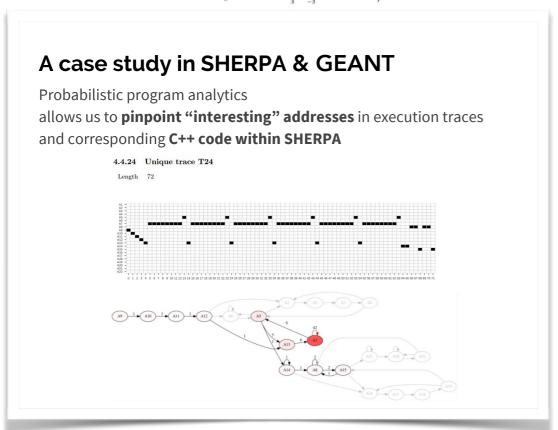
Output: a trained inference network, or "compilation artifact" (Torch, PyTorch)



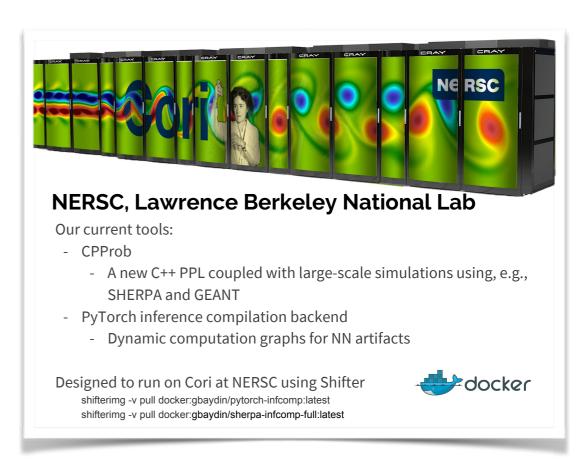
IN PROGRESS: C++, SHERPA, GEANT4

Mario Lezcano Casado, Atılım Güneş Baydin, Tuan Anh Le, Frank Wood* Department of Engineering Science University of Oxford {lezcano,gunes,tuananh,fwood}@robots.ox.ac.uk Lukas Heinrich, Gilles Louppe, Kyle Cranmer Department of Physics & Center for Data Science New York University {kyle.cranmer,lukas.heinrich,g.louppe}@cern.ch Wahid Bhimji, Prabhat Karen Ng Lawrence Berkeley National Laboratory {wbhimji,prabhat}@lbl.gov karen.y.ng@intel.com





Probabilistic programming with C++ Our new tool: CPProb https://github.com/probprog/cpprob Instrumenting C++ code to allow tools like SHERPA and GEANT run with inference compilation void linear_regression(const std::array<std::pair<RealType, RealType>, N> & points) { using boost::random::normal_distribution; auto normal = normal_distribution</ri> const auto a = cpprob::sample(normal, true); const auto b = cpprob::sample(normal, true); for (const auto & point : points) { auto likelihood = normal_distribution<RealType>{a * point.first + b, 1}; cpprob::predict(a); cpprob::predict(b); SHERPA::Hadron_Decays::Treat(ATOOLS::Blob_List*, double&)+0x709 SHERPA::Event_Handler::IterateEventPhases(SHERPA::eventtype::code&, double&)+0x1b2 SHERPA::Event_Handler::GenerateHadronDecayEvent(SHERPA::eventtype::code&)+0x979



GANS FOR PHYSICS

CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters with Generative Adversarial Networks

Michela Paganini^{a,b}, Luke de Oliveira^a, and Benjamin Nachman^a

 $\textit{E-mail:} \verb| michela.paganini@yale.edu|, | lukedeoliveira@lbl.gov|, | bnachman@cern.ch| | lukedeoliveira@lbl.gov|, | lukedeoliveira@lb$

Creating Virtual Universes Using Generative Adversarial Networks

Mustafa Mustafa*¹, Deborah Bard¹, Wahid Bhimji¹, Rami Al-Rfou², and Zarija Lukić¹

¹Lawrence Berkeley National Laboratory, Berkeley, CA 94720 ²Google Research, Mountain View, CA 94043

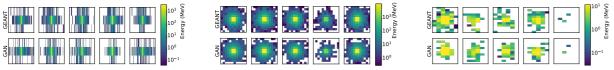


Figure 9: Five randomly selected e^+ showers per calorimeter layer from the training set (top) and the five nearest neighbors (by euclidean distance) from a set of CALOGAN candidates.

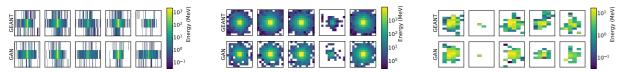


Figure 10: Five randomly selected γ showers per calorimeter layer from the training set (top) and the five nearest neighbors (by euclidean distance) from a set of CALOGAN candidates.

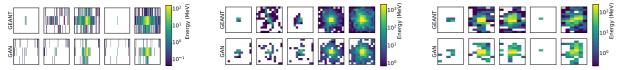
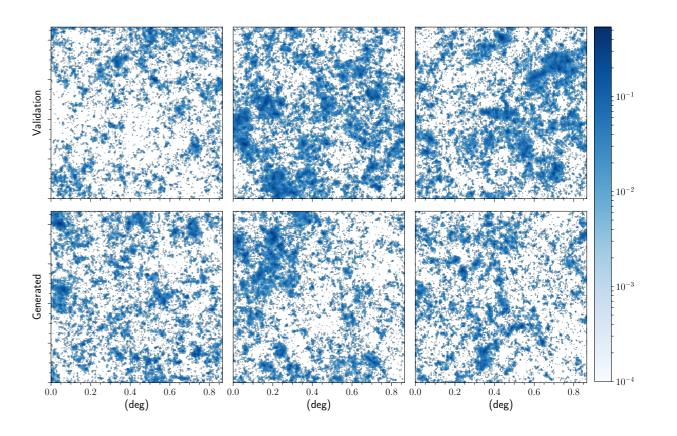


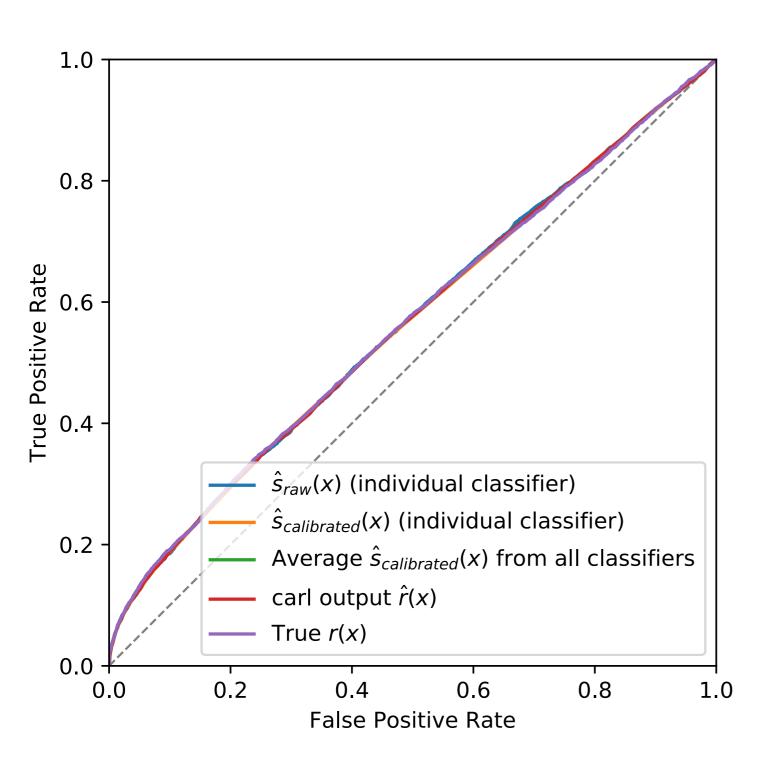
Figure 11: Five randomly selected π^+ showers per calorimeter layer from the training set (top) and the five nearest neighbors (by euclidean distance) from a set of CALOGAN candidates.

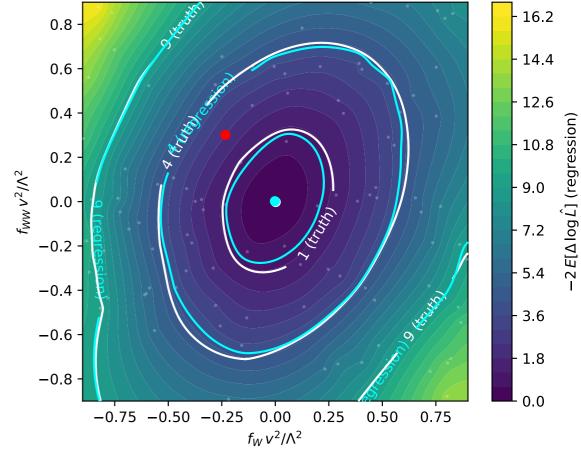


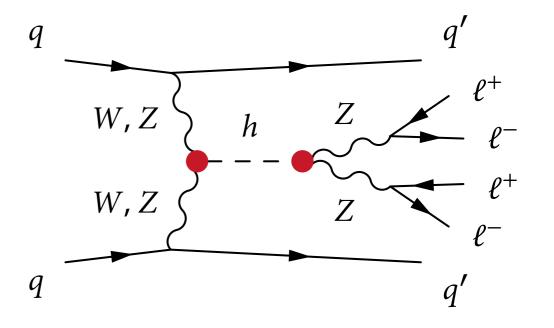
^aLawrence Berkeley National Laboratory, 1 Cyclotron Rd, Berkeley, CA, 94720, USA

^bDepartment of Physics, Yale University, New Haven, CT 06520, USA

SEPARABILITY

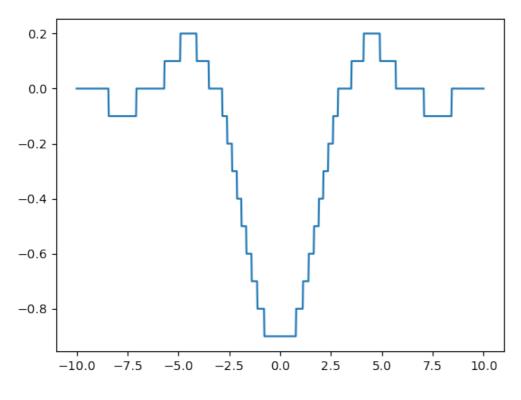




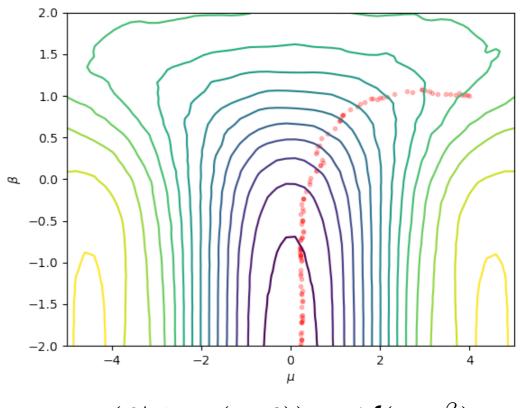


VARIATIONAL OPTIMIZATION

$$\min_{\boldsymbol{\theta}} f(\boldsymbol{\theta}) \leq \mathbb{E}_{\boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi})}[f(\boldsymbol{\theta})] = U(\boldsymbol{\psi})$$
$$\nabla_{\boldsymbol{\psi}} U(\boldsymbol{\psi}) = \mathbb{E}_{\boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi})}[f(\boldsymbol{\theta})\nabla_{\boldsymbol{\psi}} \log q(\boldsymbol{\theta}|\boldsymbol{\psi})]$$



Piecewise constant $-\frac{\sin(\mathbf{x})}{\mathbf{x}}$



$$q(\boldsymbol{\theta}|\boldsymbol{\psi} = (\mu, \beta)) = \mathcal{N}(\mu, e^{\beta})$$

ADVERSARIAL VARIATIONAL OPTIMIZATION



Like a GAN, but generative model is non-differentiable and the parameters of simulator have meaning

- Replace the generative network with a non-differentiable forward simulator $g(\mathbf{z}; \boldsymbol{\theta})$.
- With VO, optimize upper bounds of the adversarial objectives:

$$U_d = \mathbb{E}_{\boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi})}[\mathcal{L}_d] \tag{1}$$

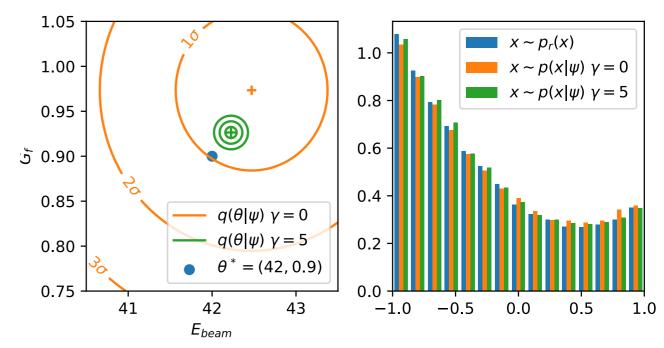
$$U_g = \mathbb{E}_{\boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi})}[\mathcal{L}_g] \tag{2}$$

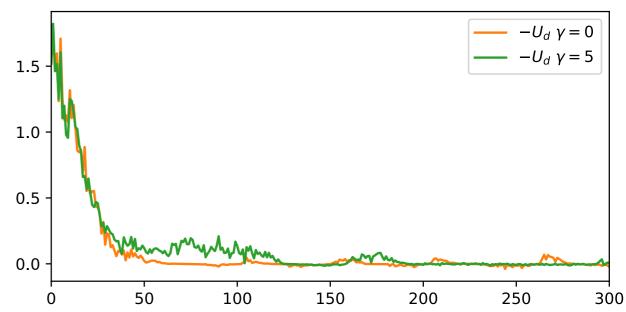
respectively over ϕ and ψ .

Effectively sampling from marginal model

$$\mathbf{x} \sim q(\mathbf{x}|\boldsymbol{\psi}) \equiv \boldsymbol{\theta} \sim q(\boldsymbol{\theta}|\boldsymbol{\psi}), \mathbf{z} \sim p(\mathbf{z}|\boldsymbol{\theta}), \mathbf{x} = g(\mathbf{z};\boldsymbol{\theta})$$

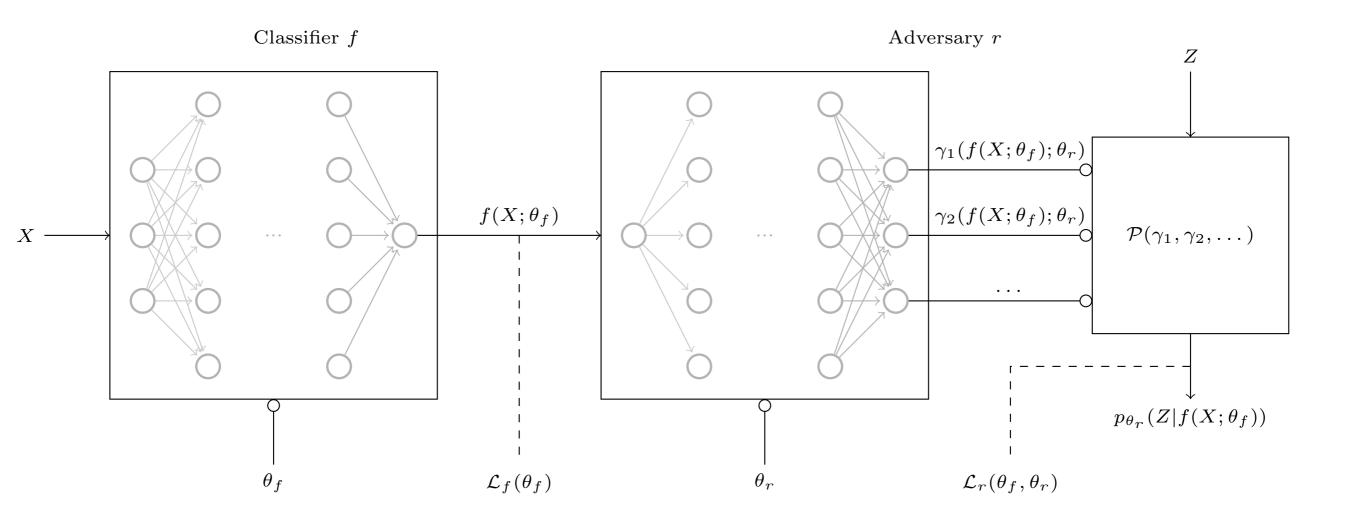
We use Wasserstein distance, as in WGAN





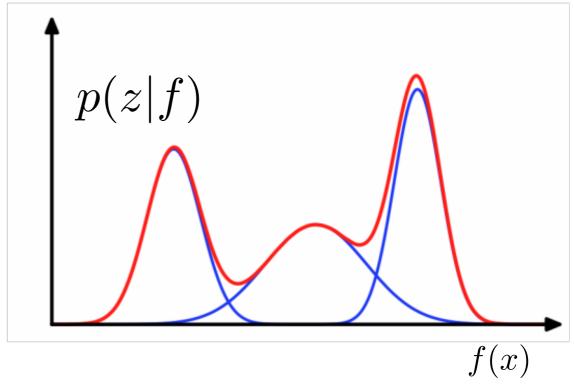
G. Louppe & K.C. arXiv:1707.07113

THE ADVERSARIAL MODEL



the $\gamma_1, \gamma_2, \ldots$ are the mean, standard deviation, and amplitude for the Gaussian Mixture Model.

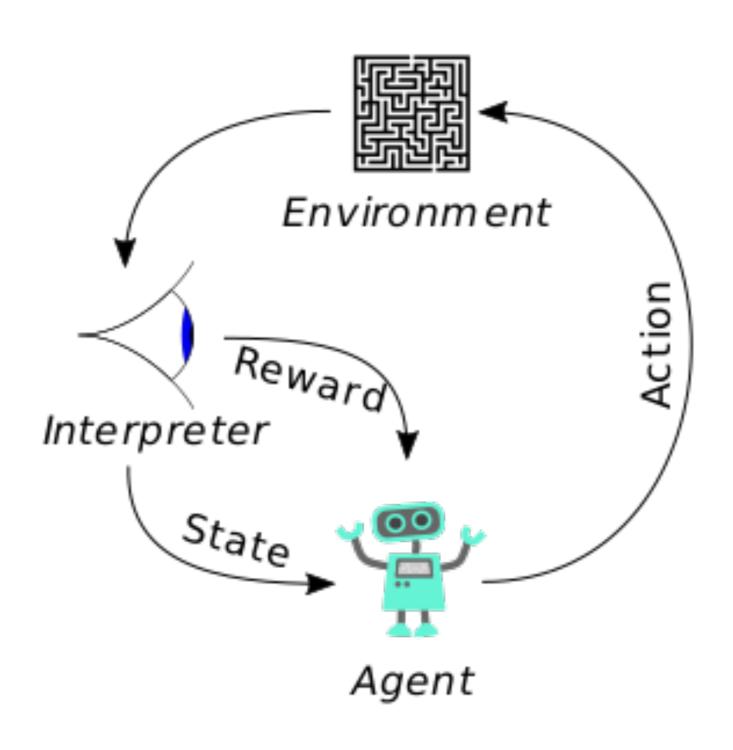
• the neural network takes in f and predicts $\gamma_1, \gamma_2, ...$



Reinforcement / Active Learning + Likelihood Free Inference

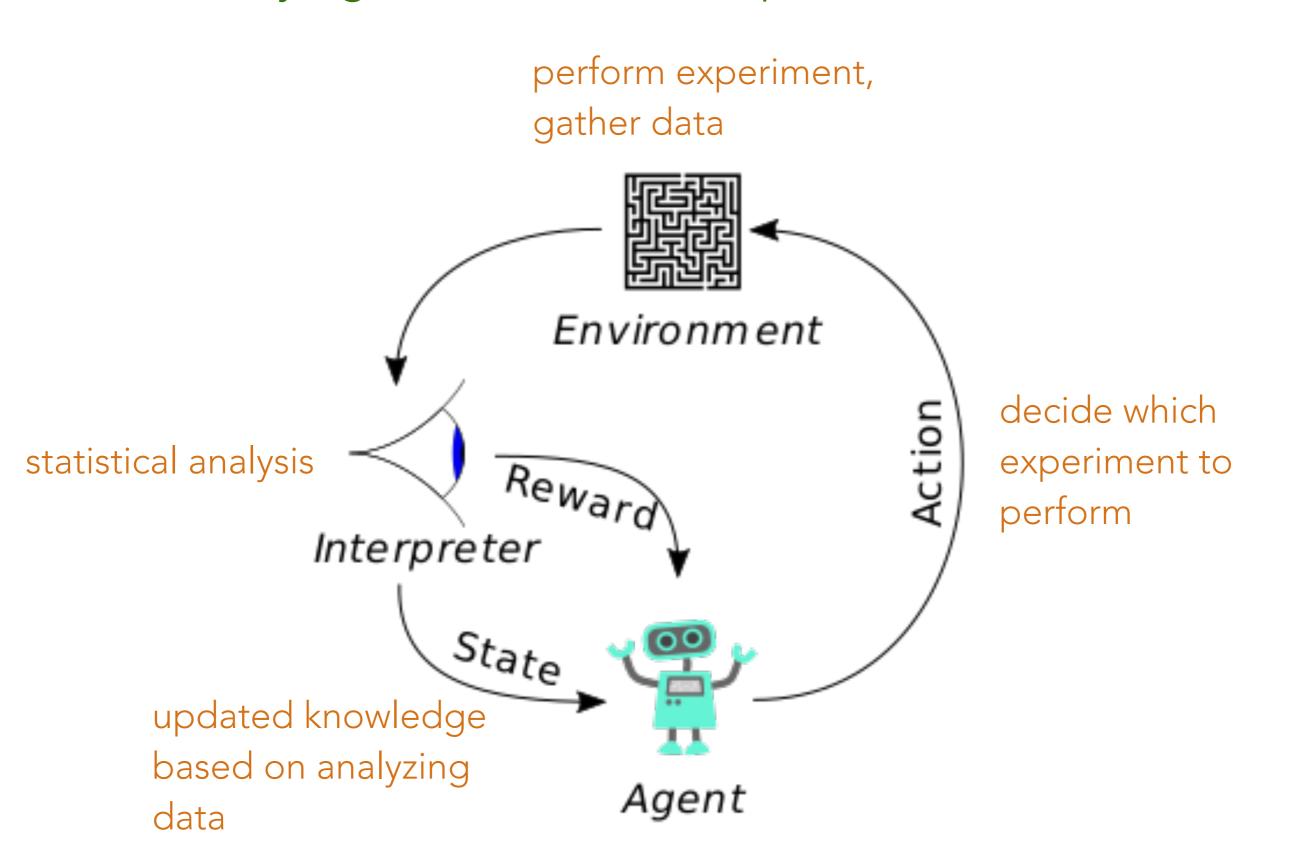
REINFORCEMENT LEARNING & SCIENTIFIC METHOD

Scientist trying to decide what experiment to do next



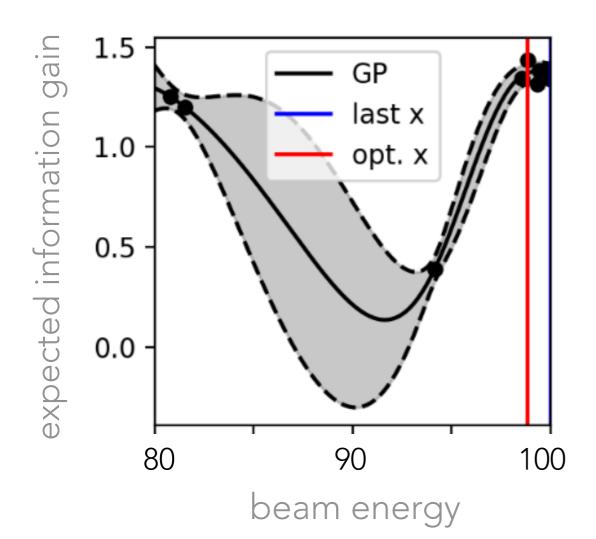
REINFORCEMENT LEARNING & SCIENTIFIC METHOD

Scientist trying to decide what experiment to do next



Proof-of-principle algorithm can:

- measure parameter of theory (eg. Weinberg angle in Standard Model of particle Physics) from raw data
- optimize experiment (eg. beam energy) for most sensitive measurement



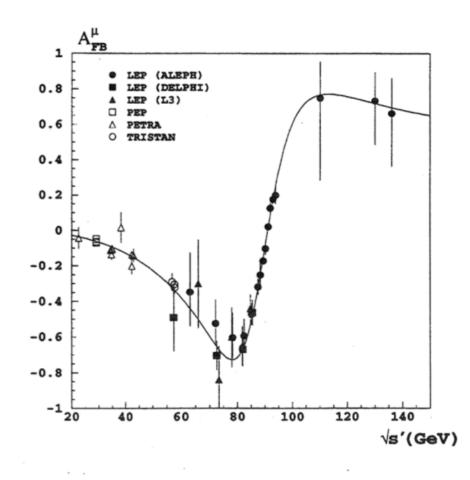
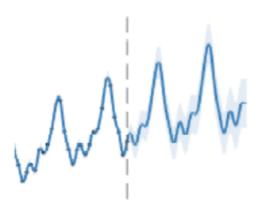


Figure 2: Measured forward-backward asymmetries of muon-pair production compared with the model independent fit results.

PHYSICS-AWARE MACHINE LEARNING

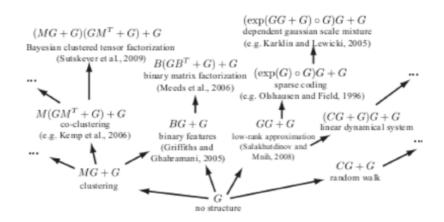
Physics goes into the construction of a "Kernel" that defines M.L. model

 Vocabulary of kernels + grammar for composition = powerful modeling



Structure Discovery in Nonparametric Regression through Compositional Kernel Search

David Duvenaud, James Robert Lloyd, Roger Grosse, Joshua B. Tenenbaum, Zoubin Ghahramani *International Conference on Machine Learning, 2013* pdf | code | poster | bibtex



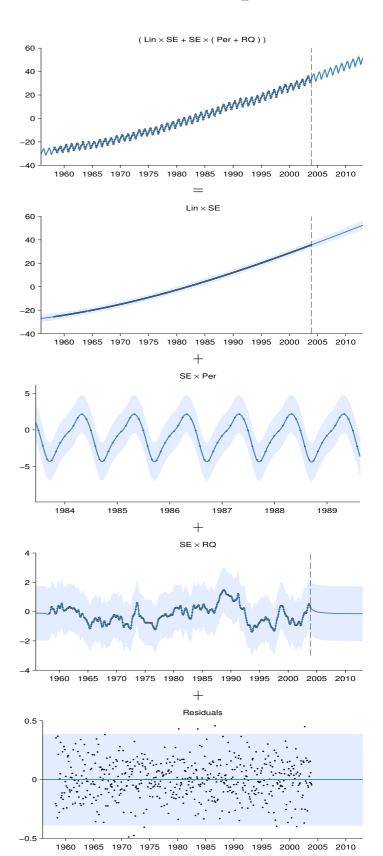
Exploiting compositionality to explore a large space of model structures

Roger Grosse, Ruslan Salakhutdinov, William T.
Freeman, Joshua B. Tenenbaum

Conference on Uncertainty in Artificial Intelligence, 2012

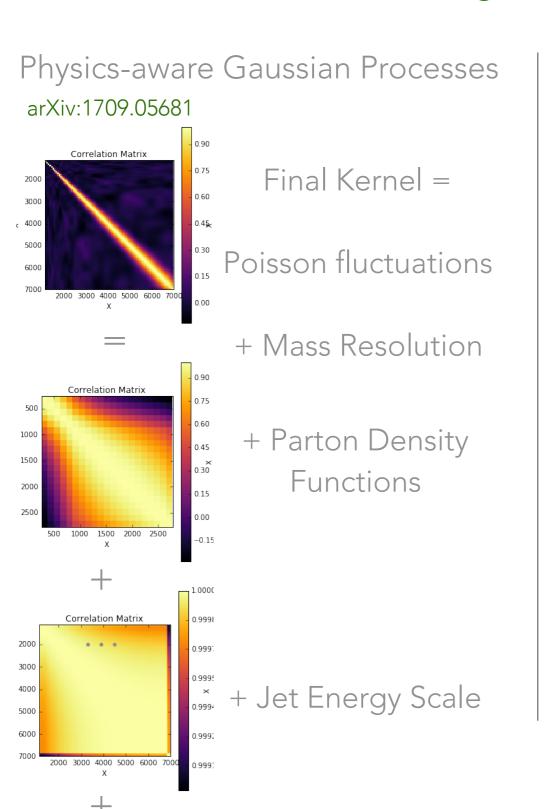
pdf | code | bibtex

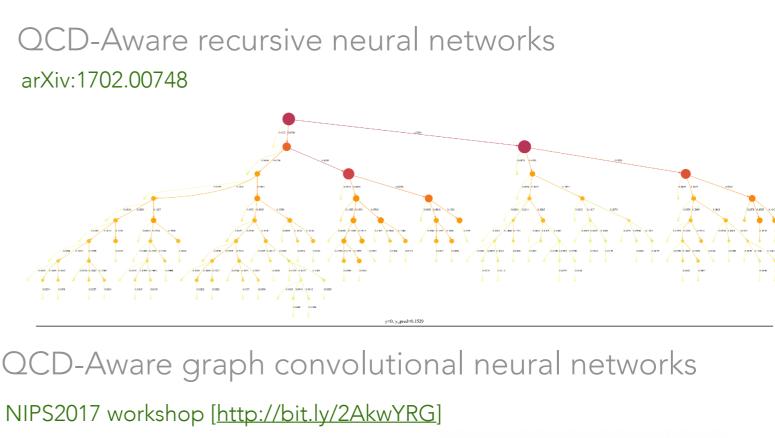
Mauna Loa atmospheric CO₂

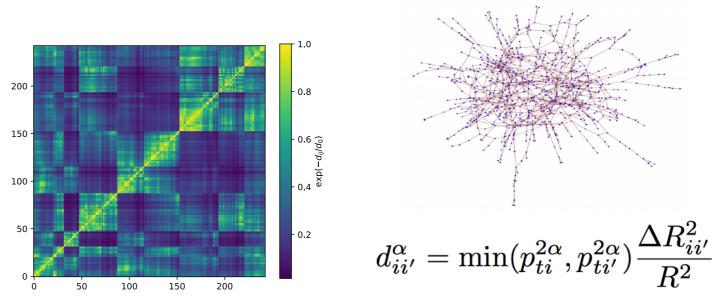


PHYSICS-AWARE MACHINE LEARNING

We can **inject** our knowledge of physics into the machine learning models! We can **extract** knowledge learned from the data!

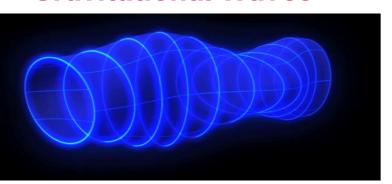


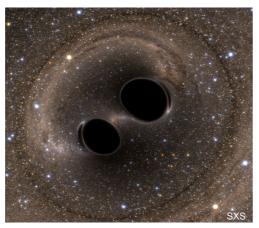


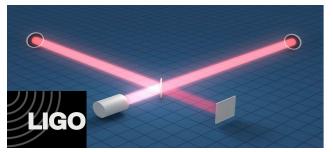


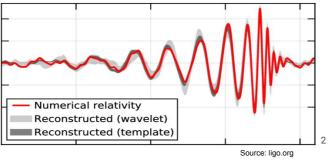
GRAVITATIONAL WAVES & NEUTRINOS

Gravitational Waves









Convolutional Neural Networks Applied to Neutrino Events in a Liquid Argon Time Projection Chamber

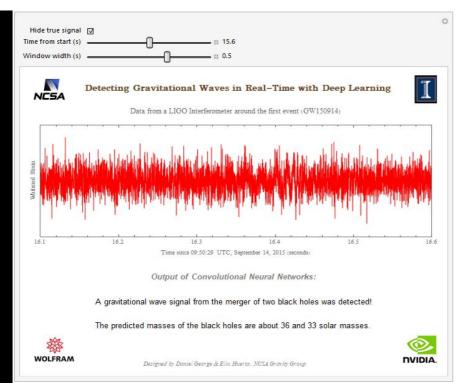
MicroBooNE Collaboration

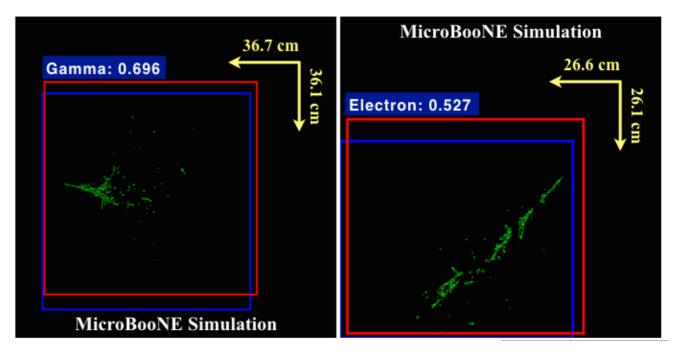
Live Demo: www.tiny.cc/DLGW Detecting GW150914 Data not included in training Trained with only non-spinning, non-eccentric simulations ~1s to analyze 4096s of data.

Masses correct within error bars

No False Alarms with two

detectors!





JUAN CARRASQUILLA @ NIPS



Juan Carrasquilla

RESTRICTED BOLTZMANN MACHINE WAVE FUNCTION

RBM probability distribution:

$$p_{\lambda}(\boldsymbol{\sigma}) = e^{\sum_{j} b_{j}^{\lambda} \sigma_{j} + \sum_{i} \log \left(1 + e^{c_{i}^{\lambda} + \sum_{j} W_{ij}^{\lambda} \sigma_{j}} \right)}$$

RBM wavefunction:

$$\psi_{\lambda,\mu}(\sigma) = \sqrt{\frac{p_{\lambda}(\sigma)}{Z_{\lambda}}} e^{i\phi_{\mu}(\sigma)}$$
 $\phi_{\mu} = \log p_{\mu}$

Widespread use of RBMs to solve many-body physics:

Variational ansatz for quantum wave-functions (Carleo & Troyer, Science 2017)

Exact representation of topological states (Deng, Li & Das Sarma, arXiv 2016)

Accelerate Monte Carlo simulations (Huang & Wang, PRB 2017)

Topological quantum error correction (GT & Melko, PRL)

and more . . .

But other choices for the neural network are also possible (CNN, MLP etc)

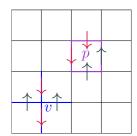
Torlai, Mazzola, Carrasquilla, Troyer, Melko and Carleo 1703:05334

NEURAL-NETWORK QUANTUM STATE TOMOGRAPHY FOR LARGE MANY-BODY SYSTEMS

NEURAL-NETWORK QUANTUM STATE TOMOGRAPHY FOR LARGE MANY-BODY SYSTEMS

KITAEV'S TORIC CODE GROUND STATE

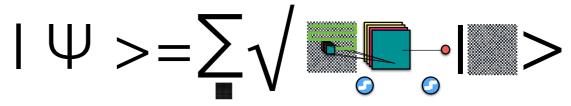
$$H = -J_p \sum_{p} \prod_{i \in p} \sigma_i^z - J_v \sum_{v} \prod_{i \in v} \sigma_i^x$$



$$|\Psi_{\text{TC}}\rangle \propto \lim_{\beta \to \infty} \sum_{\sigma_1, ..., \sigma_N} e^{\frac{\beta}{2}J\sum_p \prod_{i \in p} \sigma_i^z} |\sigma_1, ..., \sigma_N\rangle$$

PEPS: F. Verstraete, M. M. Wolf, D. Perez-Garcia, J. I. Cirac Phys. Rev. Lett. 96, 220601 (2006).

$$O_{\text{cold}}(\sigma_1, ..., \sigma_N) \propto \lim_{\beta \to \infty} \exp \beta J \sum_{p} \prod_{i \in p} \sigma_i^z$$



J. Carrasquilla and R. G. Melko. Nature Physics 13, 431–434 (2017) Dong-Ling Deng et al Phys. Rev. X 7, 021021 (2017) Jing Chen, Song Cheng, Haidong Xie, Lei Wang, Tao Xiang arXiv:1701.04831 RBMs

GENERATIVE MODELS FOR CALIBRATION

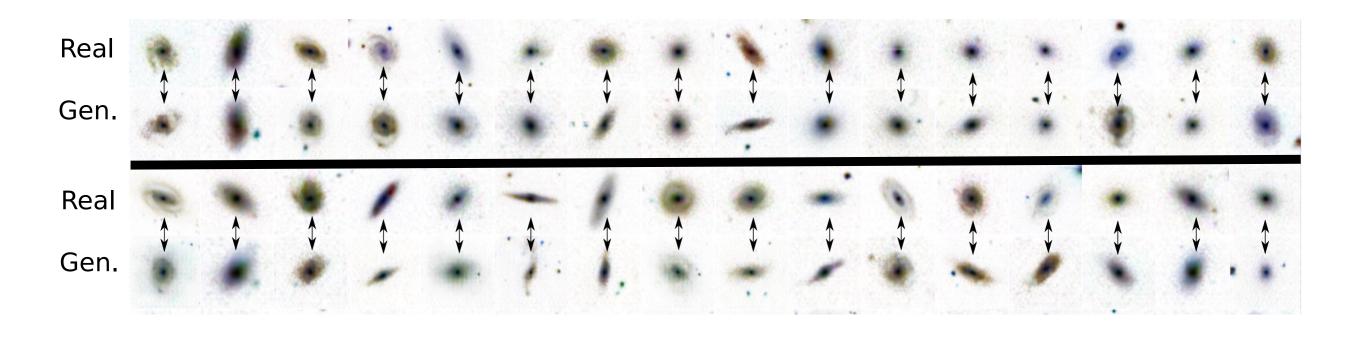
Use of generative models of galaxy images to help calibrate down-stream analysis in next-generation surveys.

Enabling Dark Energy Science with Deep Generative Models of Galaxy Images

Siamak Ravanbakhsh¹, François Lanusse², Rachel Mandelbaum², Jeff Schneider¹, and Barnabás Póczos¹

¹School of Computer Science, Carnegie Mellon University ²McWilliams Center for Cosmology, Carnegie Mellon University

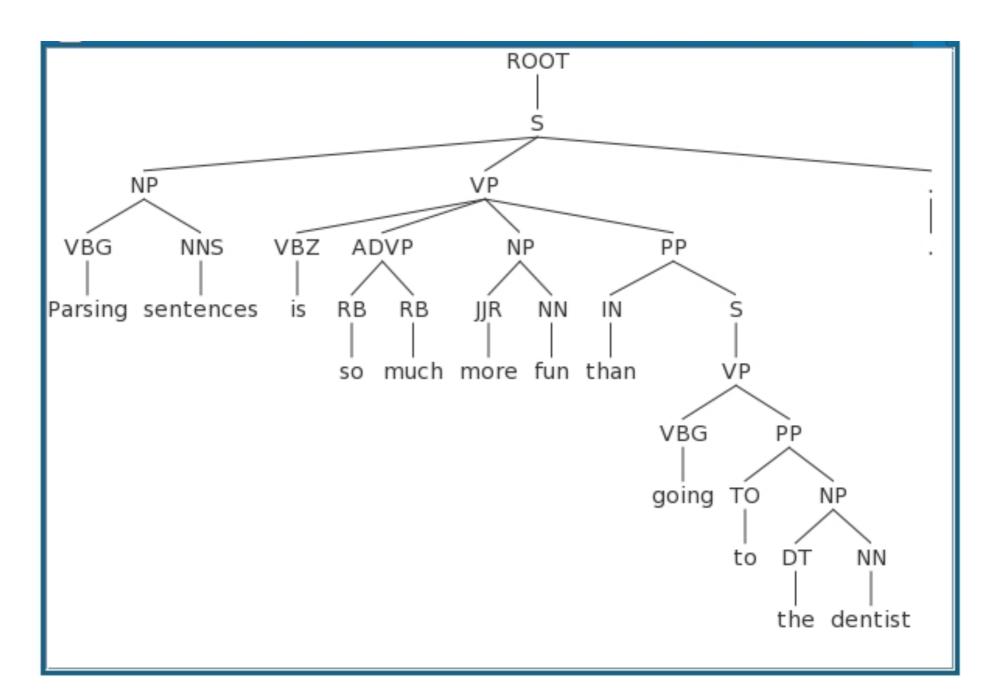
Abstract—Understanding the nature of dark energy, the mysterious force driving the accelerated expansion of the Universe, is a major challenge of modern cosmology. The next generation of cosmological surveys, specifically designed to address this issue, rely on accurate measurements of the apparent shapes of distant galaxies. However, shape measurement methods suffer from various unavoidable biases and therefore will rely on a precise calibration to meet the accuracy requirements of the science analysis. This calibration process remains an open challenge as it requires large sets of high quality galaxy images. To this end, we study the application of deep conditional generative models in generating realistic galaxy images. In particular we consider variations on conditional variational autoencoder and introduce a new adversarial objective for training of conditional generative networks. Our results suggest a reliable alternative to the acquisition of expensive high quality observations for generating the calibration data needed by the next generation of cosmological surveys.



FROM IMAGES TO SENTENCES

Recursive Neural Networks showing great performance for Natural Language Processing tasks

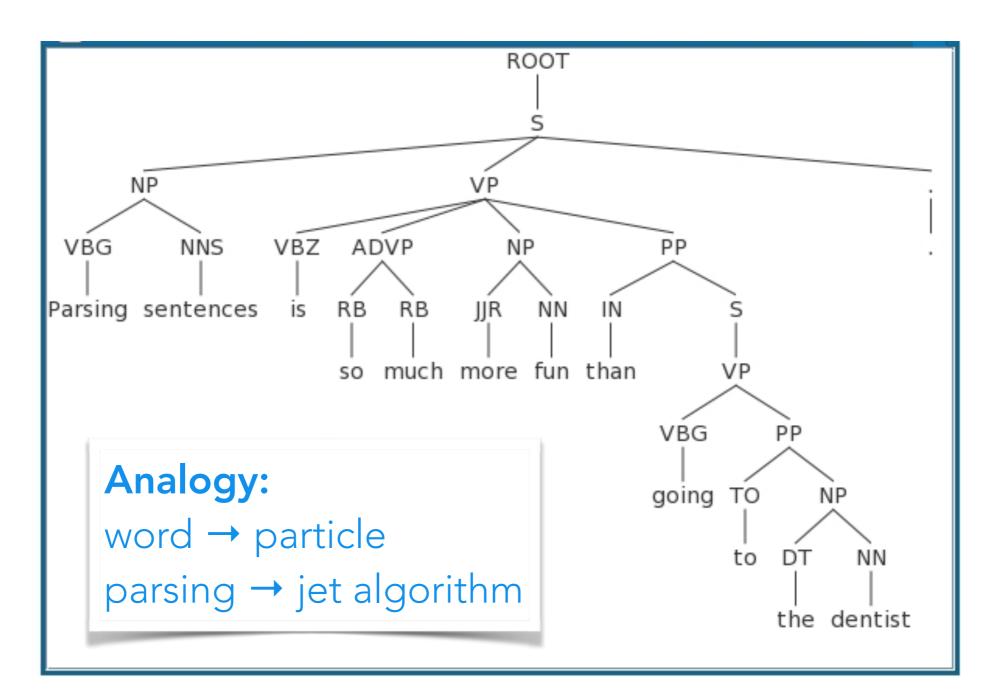
neural network's topology given by parsing of sentence!

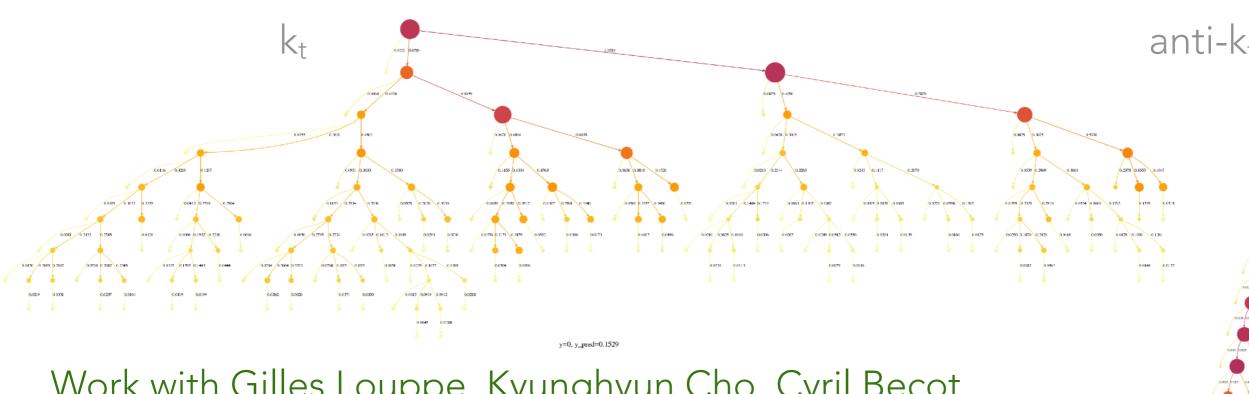


FROM IMAGES TO SENTENCES

Recursive Neural Networks showing great performance for Natural Language Processing tasks

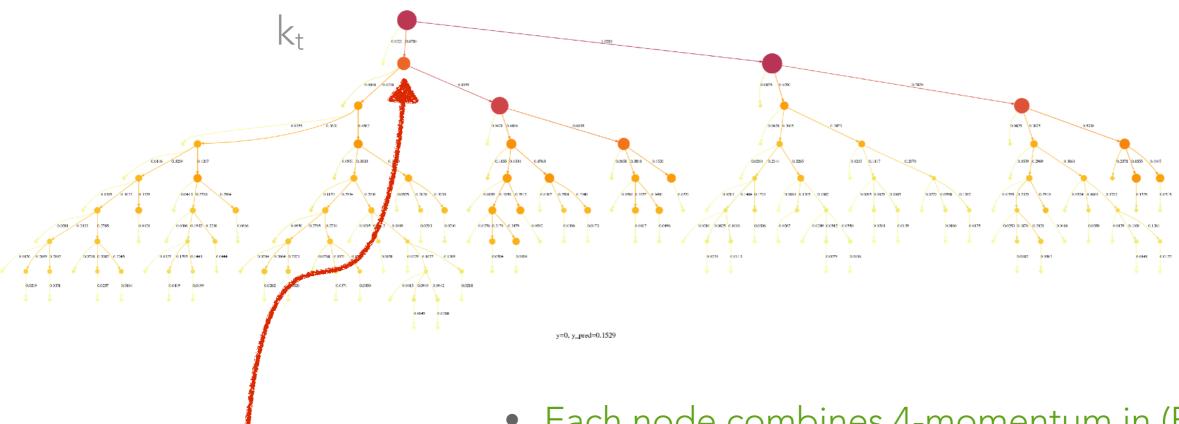
neural network's topology given by parsing of sentence!





Work with Gilles Louppe, Kyunghyun Cho, Cyril Becot

- Use sequential recombination jet algorithms to provide network topology (on a per-jet basis)
- path towards ML models with good physics properties
- Top node of recursive network provides a fixed-length embedding of a jet that can be fed to a classifier



$$\mathbf{h}_{k}^{\text{jet}} = \begin{cases} \mathbf{u}_{k} & \text{if } k \text{ is a leaf} \\ \mathbf{z}_{H} \odot \tilde{\mathbf{h}}_{k}^{\text{jet}} + \mathbf{z}_{L} \odot \mathbf{h}_{k_{L}}^{\text{jet}} + & \text{otherwise} \\ \hookrightarrow \mathbf{z}_{R} \odot \mathbf{h}_{k_{R}}^{\text{jet}} + \mathbf{z}_{N} \odot \mathbf{u}_{k} & \\ \mathbf{u}_{k} = \sigma \left(W_{u} g(\mathbf{o}_{k}) + b_{u} \right) \end{cases}$$

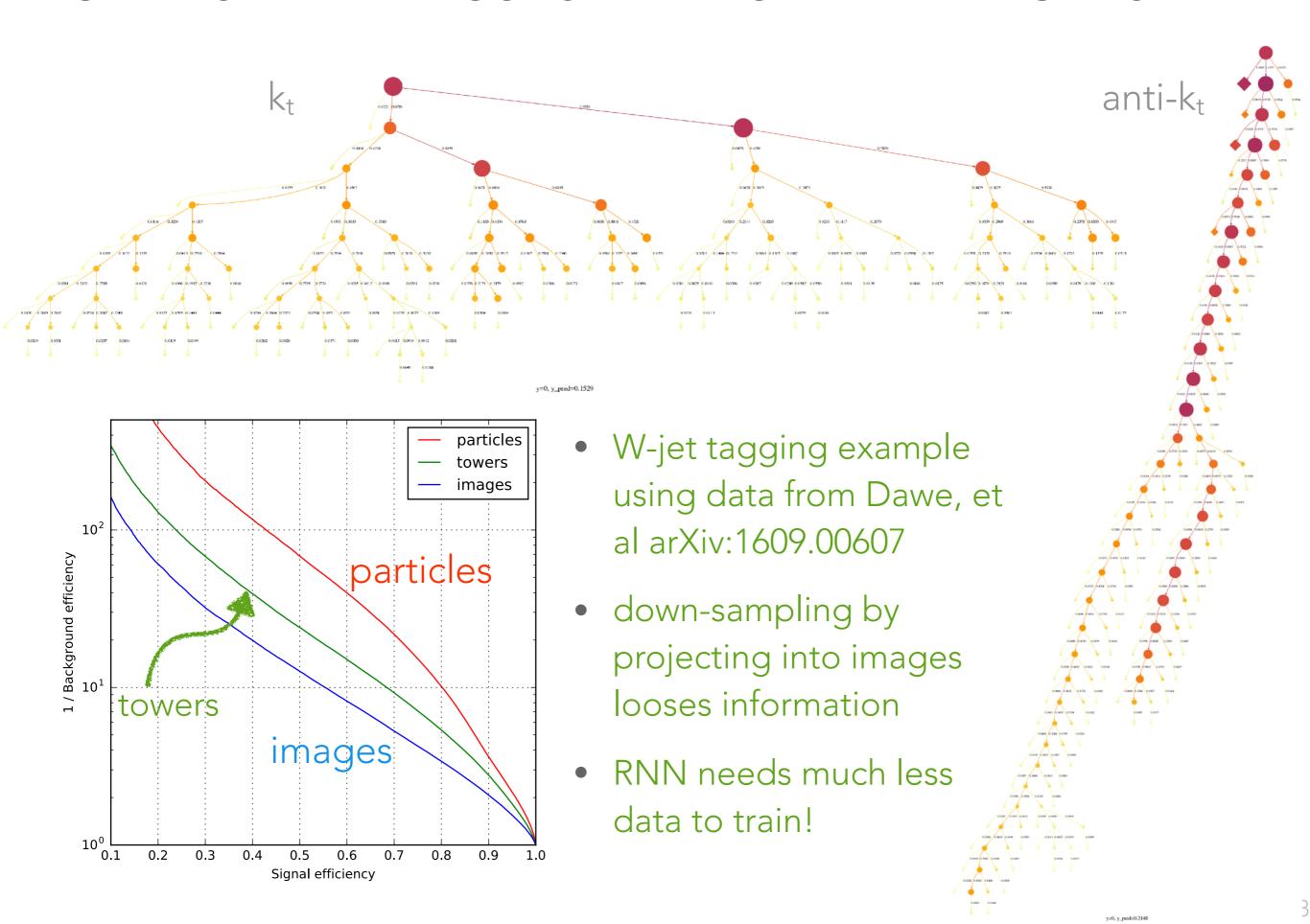
$$\mathbf{o}_k = \begin{cases} \mathbf{v}_{i(k)} & \text{if } k \text{ is a leaf} \\ \mathbf{o}_{k_L} + \mathbf{o}_{k_R} & \text{otherwise} \end{cases}$$

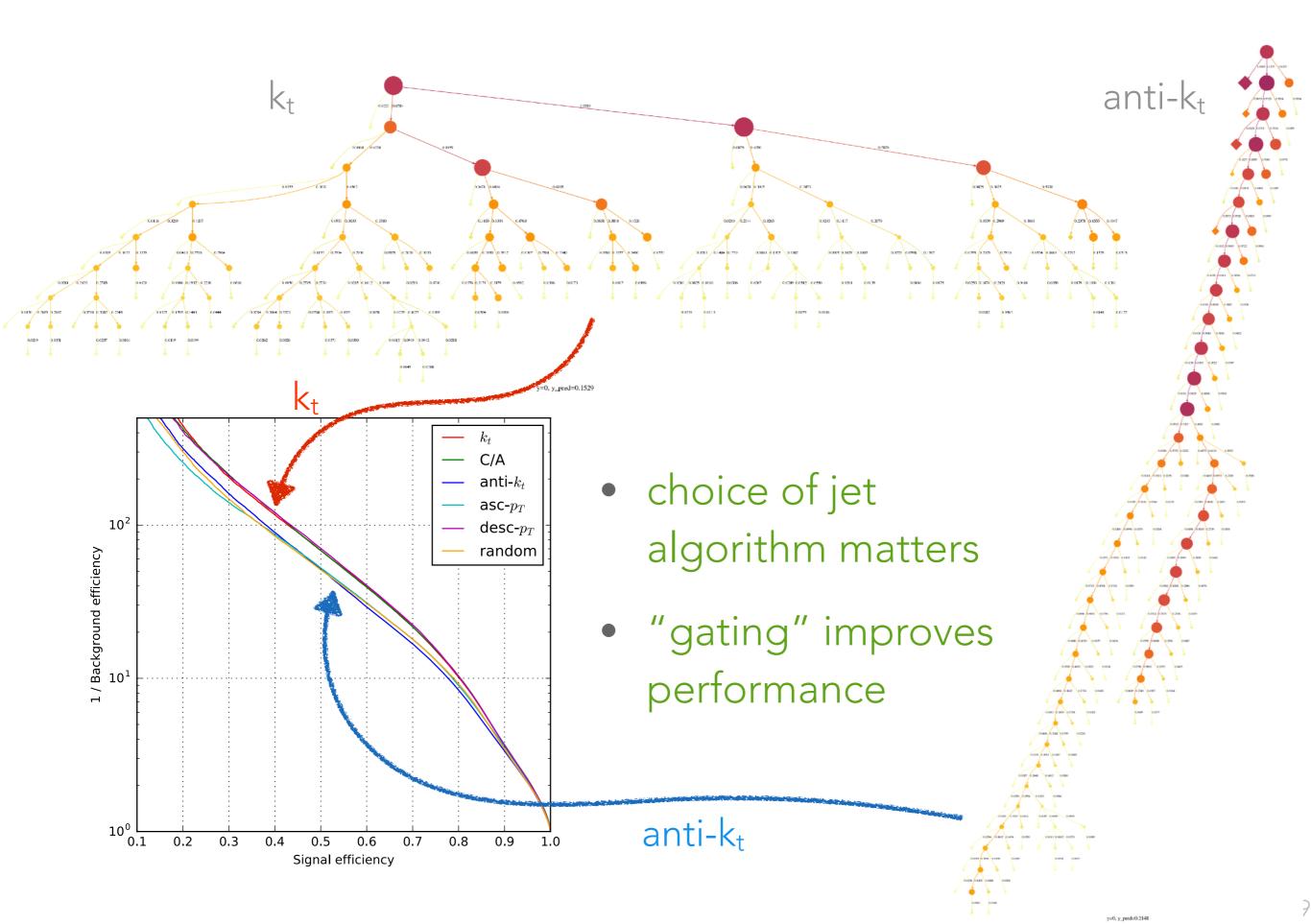
$$\tilde{\mathbf{h}}_{k}^{\text{jet}} = \sigma \left(W_{\tilde{h}} \begin{bmatrix} \mathbf{r}_{L} \odot \mathbf{h}_{k_{L}}^{\text{jet}} \\ \mathbf{r}_{R} \odot \mathbf{h}_{k_{R}}^{\text{jet}} \\ \mathbf{r}_{N} \odot \mathbf{u}_{k} \end{bmatrix} + b_{\tilde{h}} \right)$$

$$\begin{bmatrix} \mathbf{z}_{H} \\ \mathbf{z}_{L} \\ \mathbf{z}_{R} \\ \mathbf{z}_{N} \end{bmatrix} = \operatorname{softmax} \left(W_{z} \begin{bmatrix} \tilde{\mathbf{h}}_{k}^{\text{jet}} \\ \mathbf{h}_{k_{L}}^{\text{jet}} \\ \mathbf{h}_{k_{R}}^{\text{jet}} \\ \mathbf{u}_{k} \end{bmatrix} + b_{z} \right)$$

$$\begin{bmatrix} \mathbf{r}_L \\ \mathbf{r}_R \\ \mathbf{r}_N \end{bmatrix} = \text{sigmoid} \left(W_r \begin{bmatrix} \mathbf{h}_{k_L}^{\text{jet}} \\ \mathbf{h}_{k_R}^{\text{jet}} \\ \mathbf{u}_k \end{bmatrix} + b_r \right)$$

- Each node combines 4-momentum in (E-scheme recombination of o_k) and a non-linear transformation of hidden state of children h_{kL} , $h_{kR} \in \mathbb{R}^{40}$
- Recursively applied (shared weights, Markov)
- "gating" allows for weighting of information of L/R children and for to flow directly along one branch





JET-LEVEL CLASSIFICATION RESULTS

TABLE I. Summary of jet classification performance for several approaches applied either to particle-level inputs or towers from a DELPHES simulation.

	Input	Architecture	ROC AUC	$R_{\epsilon=50\%}$	
-	Projected into images				
	towers	MaxOut	0.8418	_	
	towers	k_t	0.8321 ± 0.0025	$\big 12.7\pm0.4\big $	
	towers	k_t (gated)	0.8277 ± 0.0028	12.4 ± 0.3	
Without image preprocessing					
	towers	$ au_{21}$	0.7644	6.79	
	towers	$mass + \tau_{21}$	0.8212	11.31	
	towers	k_t	0.8807 ± 0.0010	$ \ 24.1 \pm 0.6\ $	
	towers	C/A	0.8831 ± 0.0010	$ \ 24.2\pm0.7\ $	
	towers	anti- k_t	0.8737 ± 0.0017	$ \ 22.3 \pm 0.8\ $	
	towers	$\operatorname{asc-}p_T$	0.8835 ± 0.0009	$ig 26.2\pm0.7 ig $	
	towers	$\operatorname{desc-}p_T$	0.8838 ± 0.0010	$ \ 25.1 \pm 0.6\ $	
	towers	random	0.8704 ± 0.0011	$ \ 20.4 \pm 0.3\ $	
Ī	particles	k_t	0.9185 ± 0.0006	68.3 ± 1.8	
	particles	C/A	0.9192 ± 0.0008	$ 68.3 \pm 3.6 $	
	particles	anti- k_t	0.9096 ± 0.0013	$ 51.7 \pm 3.5 $	
	particles	$\operatorname{asc-}p_T$	0.9130 ± 0.0031	$ 52.5 \pm 7.3 $	
	particles	$\operatorname{desc-}p_T$	0.9189 ± 0.0009	$ig 70.4\pm3.6ig $	
	particles	random	0.9121 ± 0.0008	$ 51.1 \pm 2.0 $	
With gating (see Appendix A)					
	towers	k_t	0.8822 ± 0.0006	25.4 ± 0.4	
	towers	C/A	0.8861 ± 0.0014	$ 26.2 \pm 0.8 $	
	towers	anti- k_t	0.8804 ± 0.0010	$ 24.4 \pm 0.4 $	
	towers	$\operatorname{asc-}p_T$	0.8849 ± 0.0012	$ \ 27.2 \pm 0.8 \ $	
	towers	$\operatorname{desc-}p_T$	0.8864 ± 0.0007	$ig 27.5\pm0.6 ig $	
	towers	random	0.8751 ± 0.0029	$ \ 22.8 \pm 1.2\ $	
	particles	k_t	0.9195 ± 0.0009	74.3 ± 2.4	
	particles	C/A	$\textbf{0.9222}\pm\textbf{0.0007}$	81.8 ± 3.1	
	particles	anti- k_t	0.9156 ± 0.0012	$ 68.3 \pm 3.2 $	
	particles	$\operatorname{asc-}p_T$	0.9137 ± 0.0046	$ 54.8 \pm 11.7 $	
	particles	$\operatorname{desc-}p_T$	0.9212 ± 0.0005	$ig 83.3\pm3.1ig $	
	particles	random	0.9106 ± 0.0035	50.7 ± 6.7	

When working on images:

 recursive network has similar performance to previous approaches

Improved performance when working with calo towers without image pre-processing

• loss of information depends on details of calorimeter, pixelation, etc.

Working on truth-level particles led to a significant improvement

 generically expect information from tracking, particle flow, etc. to be somewhere between towers and truth particle-level Introduction Jet Physics Previous work Proposed model Experiments Conclusions

Neural Message Passing for Jet Physics

Isaac Henrion, Johann Brehmer, Joan Bruna, Kyunghyun Cho, Kyle Cranmer, Gilles Louppe, Gaspar Rochette

Courant Institute & Center for Data Science



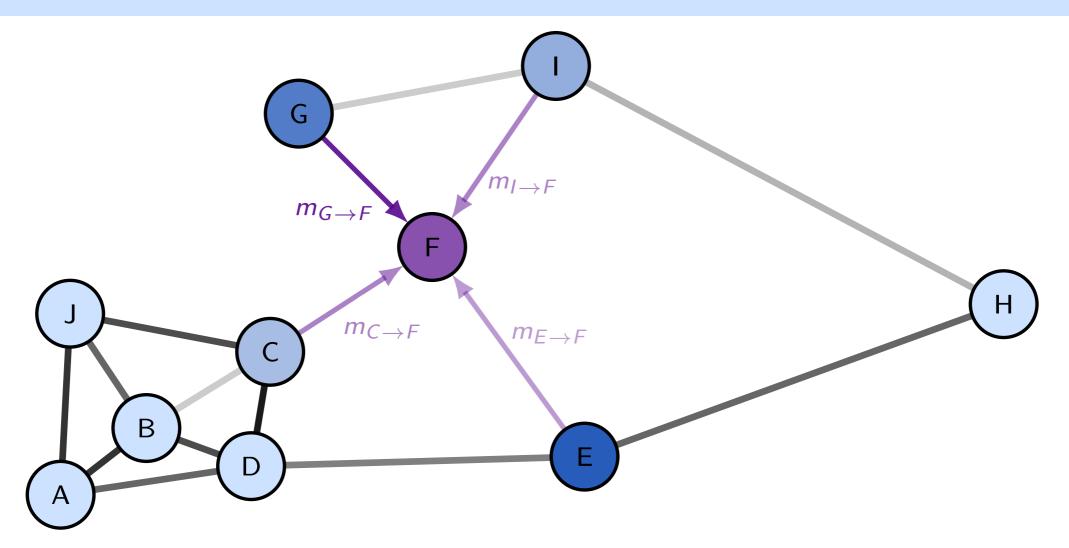
Paper: https://dl4physicalsciences.github.io/files/nips_dlps_2017_29.pdf
Talk: https://dl4physicalsciences.github.io/files/nips_dlps_2017_slides_henrion.pdf

Message Passing Neural Network

```
Algorithm 1 Message passing neural network
Require: N \times D nodes x, adjacency matrix A
   \mathbf{h} \leftarrow \mathsf{Embed}(\mathbf{x})
   for t = 1, \ldots, T do
         \mathbf{m} \leftarrow \mathsf{Message}(A, \mathbf{h})
         \mathbf{h} \leftarrow \text{VertexUpdate}(\mathbf{h}, \mathbf{m})
   end for
   \mathbf{r} = \mathsf{Readout}(\mathbf{h})
   return Classify(r)
```

Adjacency matrix generalizes receptive field of convolution kernel Vertex Update like pooling Iterations like layers of a CNN

Graph neural networks



$$ilde{m}_{j}^{t} = f(h_{j}^{t-1})$$
 $m_{j o i}^{t} = \sigma(A_{ij} \tilde{m}_{j}^{t})$
 $h_{i}^{t} = \mathsf{GRU}(h_{i}^{t-1}, \Sigma_{j} m_{j o i}^{t})$

Message Passing Neural Network

```
Algorithm 2 Message passing neural network
Require: N \times D array of jet constituents x
    \mathbf{h} \leftarrow \mathsf{Embed}(\mathbf{x})
    for t = 1, \ldots, T do
         A \leftarrow AdjacencyMatrix_t(\mathbf{h})
         \mathbf{m} \leftarrow \mathsf{Message}_t(A, \mathbf{h})
         \mathbf{h} \leftarrow \mathsf{VertexUpdate}_t(\mathbf{h}, \mathbf{m})
    end for
    \mathbf{r} = \mathsf{Readout}(\mathbf{h})
    return Classify(r)
```

Difference from Alg 1:

new weights for each iteration (layer) of message passing

Introduction Jet Physics Previous work Proposed model Experiments Conclusions

A problem with the adjacency matrix

Question

Where does adjacency matrix come from?

Answer 1

Use a physics-inspired adjacency matrix.

BONUS: import physics knowledge

Answer 2

Learn the adjacency matrix from the data.

BONUS: export physics algorithm

Very interesting:

adjacency matrix can be **interpreted** like a kT, C/A, anti-kT Once learned, can **export** the adjacency function for other uses Provides bi-directional **interface** between ML and jet physics.

Learning the adjacency matrix

$$F(h, h') = v^{\top}(h+h') + b$$
 $s_{ij}^{t} = F(h_i^{t-1}, h_j^{t-1})$

$$A_{ij}^{t} = \frac{\exp\{s_{ij}^{t}\}}{\sum_{k} \exp\{s_{ik}^{t}\}}$$
 (directed)

$$A_{\text{sym}} = \frac{1}{2} \left(A + A^{\top} \right)$$
 (undirected)

This is a simple starting point, not motivated by physics

Classification results

1/FP	PR @ TPR	= 50%
Model	Iterations	$R_{\epsilon=50\%}$
Rec-NN (no gating)	1	70.4 ± 3.6
Rec-NN (gating)	1	$\textbf{83.3} \pm \textbf{3.1}$
MPNN (directed)	1	89.4 ± 3.5
MPNN (directed)	2	$\textbf{98.3} \pm \textbf{4.3}$
MPNN (directed)	3	85.9 ± 8.5
MPNN (identity)	3	74.5 ± 5.2
Relation Network	1	67.7 ± 6.8

Significant improvement on W vs. QCD tagging!

This is with a learned adjacency matrix what did it learn? Is that adjacency matrix useful? we are working MPNN with QCD-motivated adjacency matrix