

# Uncertainty in an Unknown World

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# Outline

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Objects, existence, identity, uncertainty

Examples

First-order probabilistic languages

BLOG

- example BLOG models
- semantics (briefly)
- inference (briefly)

Random comments on prior knowledge

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# Existence, Identity, Uncertainty

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The world has individual objects in it

Raw data provide propositional observations (e.g., pixels, text strings)  
not necessarily direct observations of the objects

Postulating *existence* of objects is the first step

Ascertaining *identity* of objects is important for:

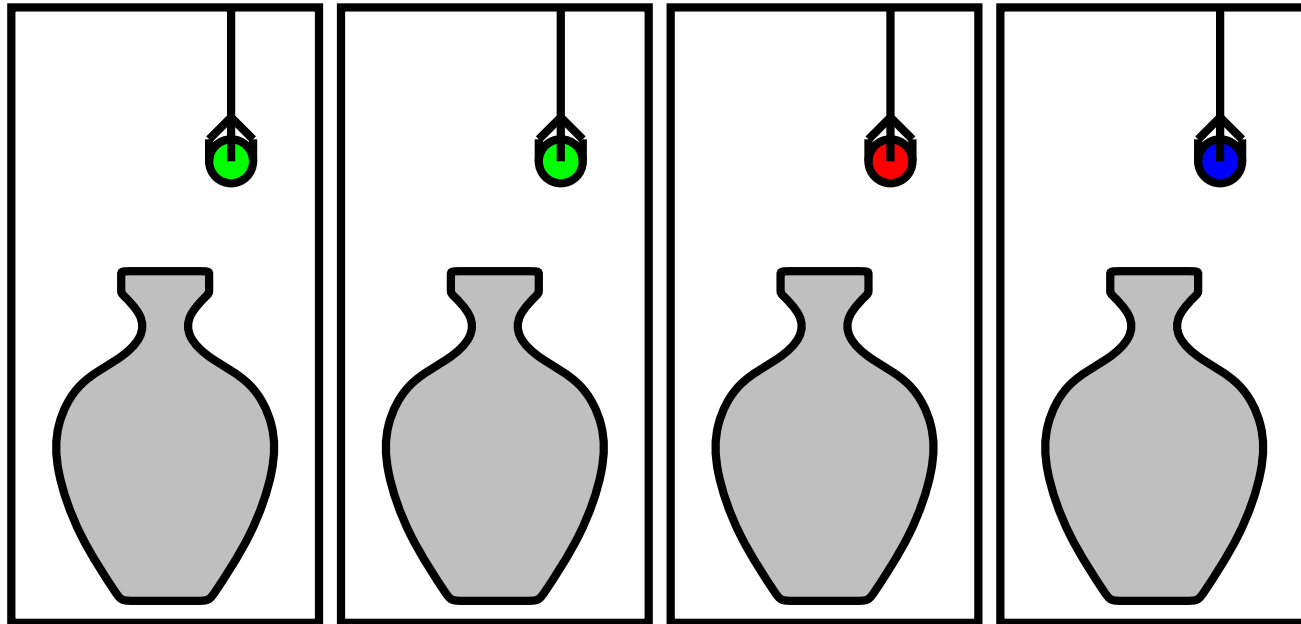
- ◇ Accumulation of knowledge (e.g., tracking systems, databases)
- ◇ Certain relations (ownership, marriage, ...)
- ◇ Navigation (places), counting, etc.

Uncertainty is inevitable

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# Urns and balls

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Repeat:

shake the urn, pick out one ball, examine colour, replace

How many balls are there in the urn?

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# Urns and balls

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$N$  balls, prior distribution  $P(N)$

True colours  $C_1, \dots, C_N$ , identical priors  $P(C_i)$

$k$  observations, observed colours  $\mathbf{O} = O_1, \dots, O_k$

Assignment  $\omega = \{\mathbf{B}_1, \dots, \mathbf{B}_m\}$  where each  $\mathbf{B}_i$  is the set of observations purportedly generated by a single real ball:



Sensor model  $P(O_j | C_{\omega_j})$

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# Counting the balls

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$$\begin{aligned}P(N \mid \mathbf{O}) &= \alpha P(N) P(\mathbf{O} \mid N) \\&= \alpha P(N) \sum_{\omega} P(\omega \mid N) P(\mathbf{O} \mid N, \omega) \\&= \alpha P(N) \sum_{\omega} P(\omega \mid N) P(\mathbf{O} \mid \omega) \\&= \alpha P(N) \sum_{\omega} \frac{N!}{(N-m)!} \left(\frac{1}{N}\right)^k \prod_{i=1}^m \sum_{C_i} \prod_{O_j \in \mathbf{B}_i} P(O_j \mid C_i) P(C_i)\end{aligned}$$

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# Citation matching

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[Lashkari et al 94] Collaborative Interface Agents, Yezdi Lashkari, Max Metral, and Pattie Maes, Proceedings of the Twelfth National Conference on Artificial Intelligence, MIT Press, Cambridge, MA, 1994.

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Are these descriptions of the same object?

This problem is ubiquitous with real data sources, hence the *record linkage* industry

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# Large databases: CiteSeer

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Unavailability of exact key matches can make large databases useless

Russell w/4 Norvig

# Large databases: CiteSeer

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Unavailability of exact key matches can make large databases useless

Russell w/4 Norvig

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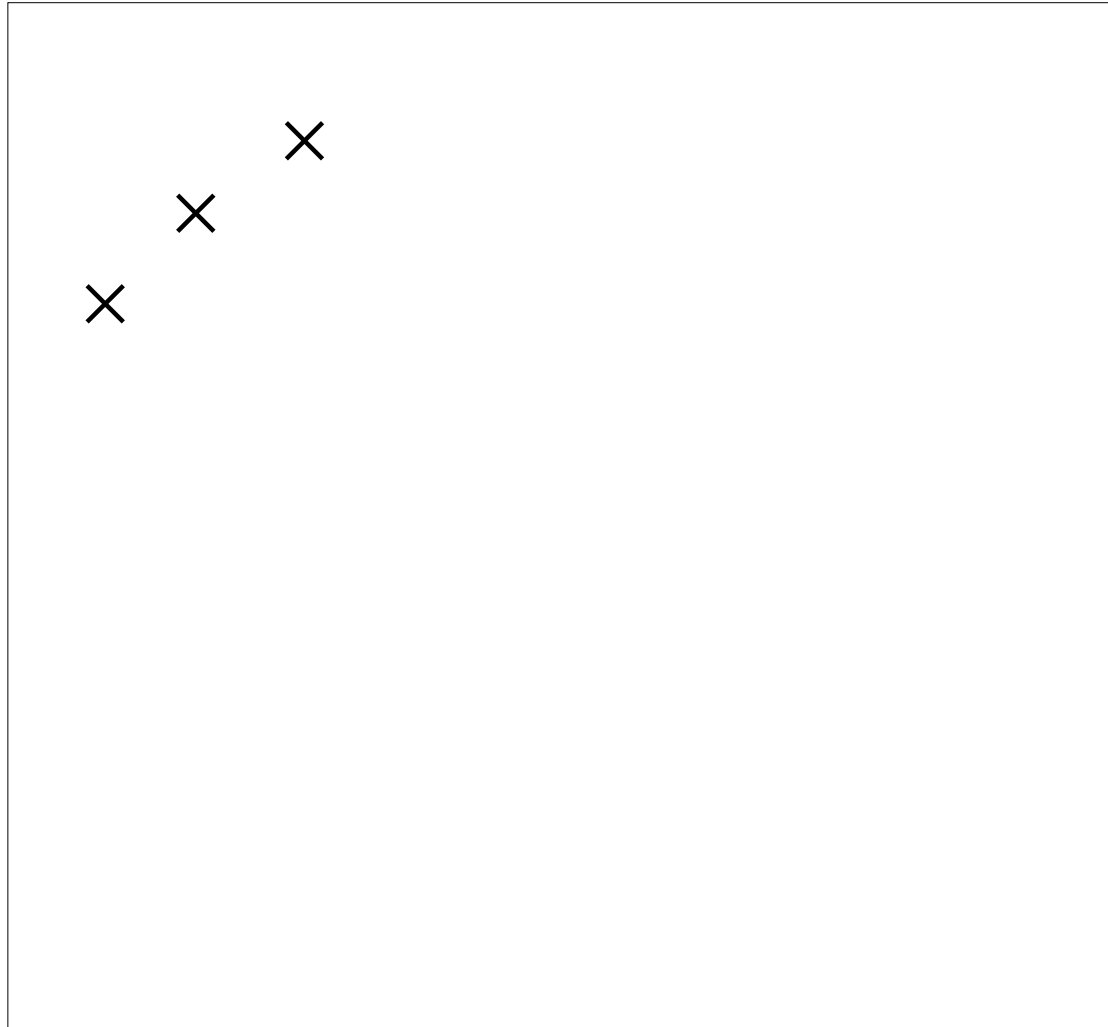
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# Data association: classical

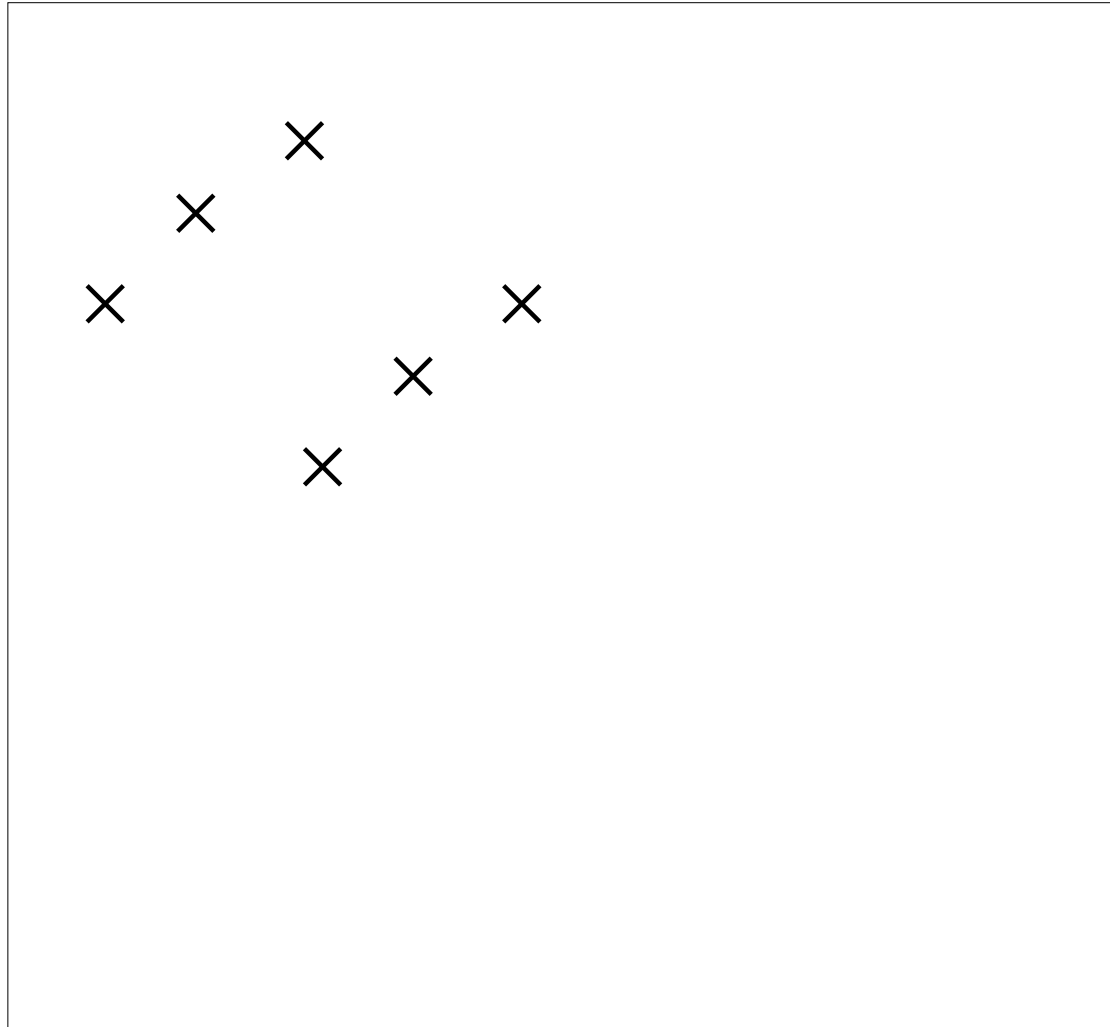
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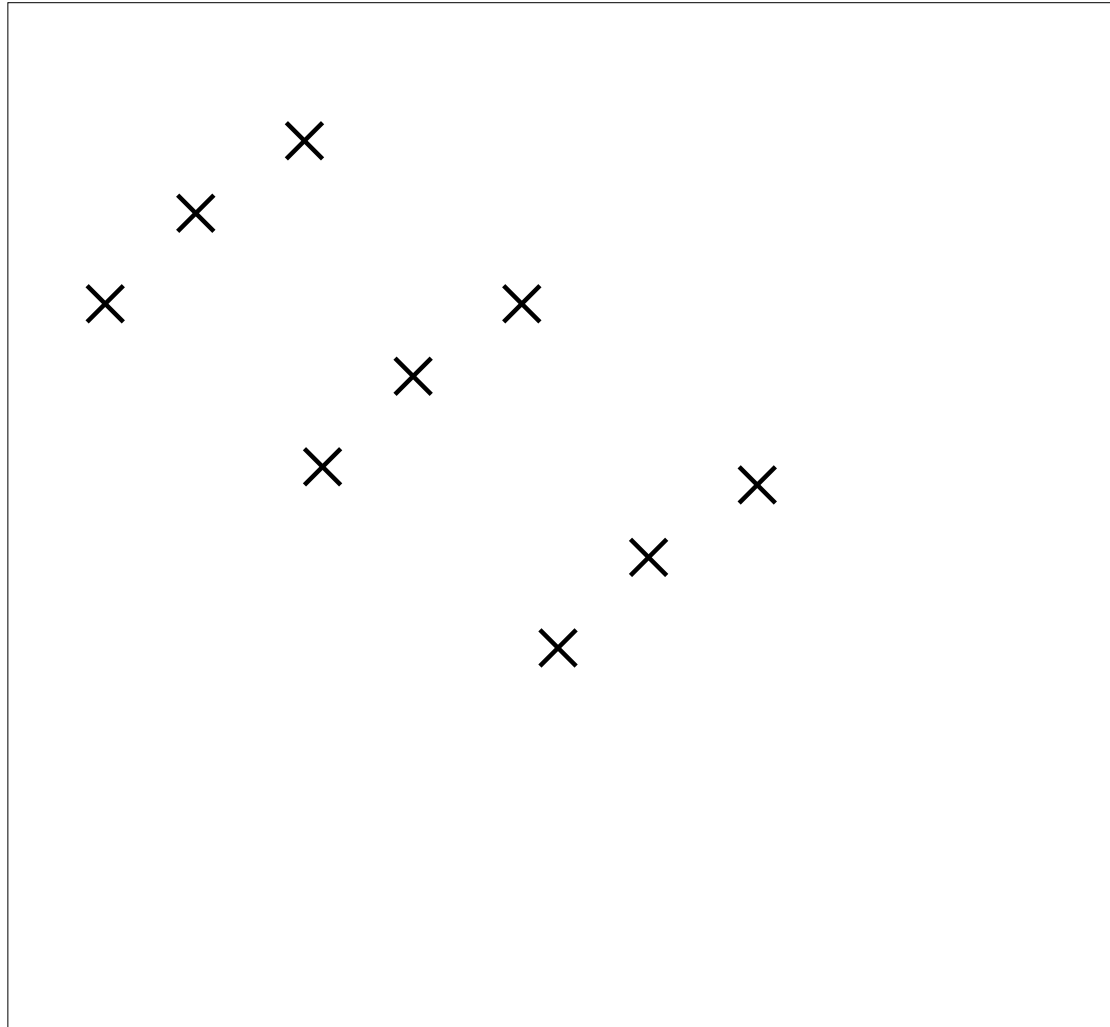
# Data association: classical

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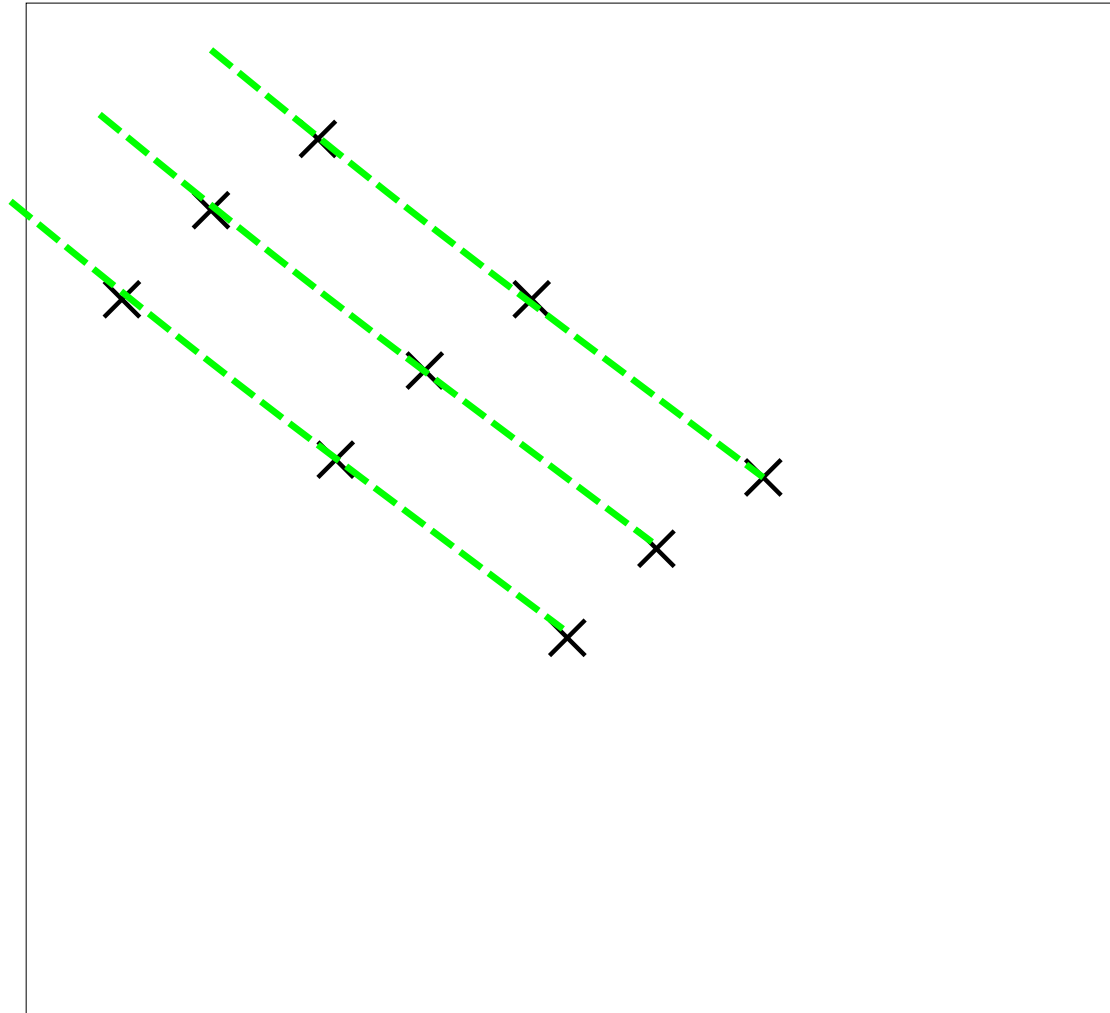
# Data association: classical

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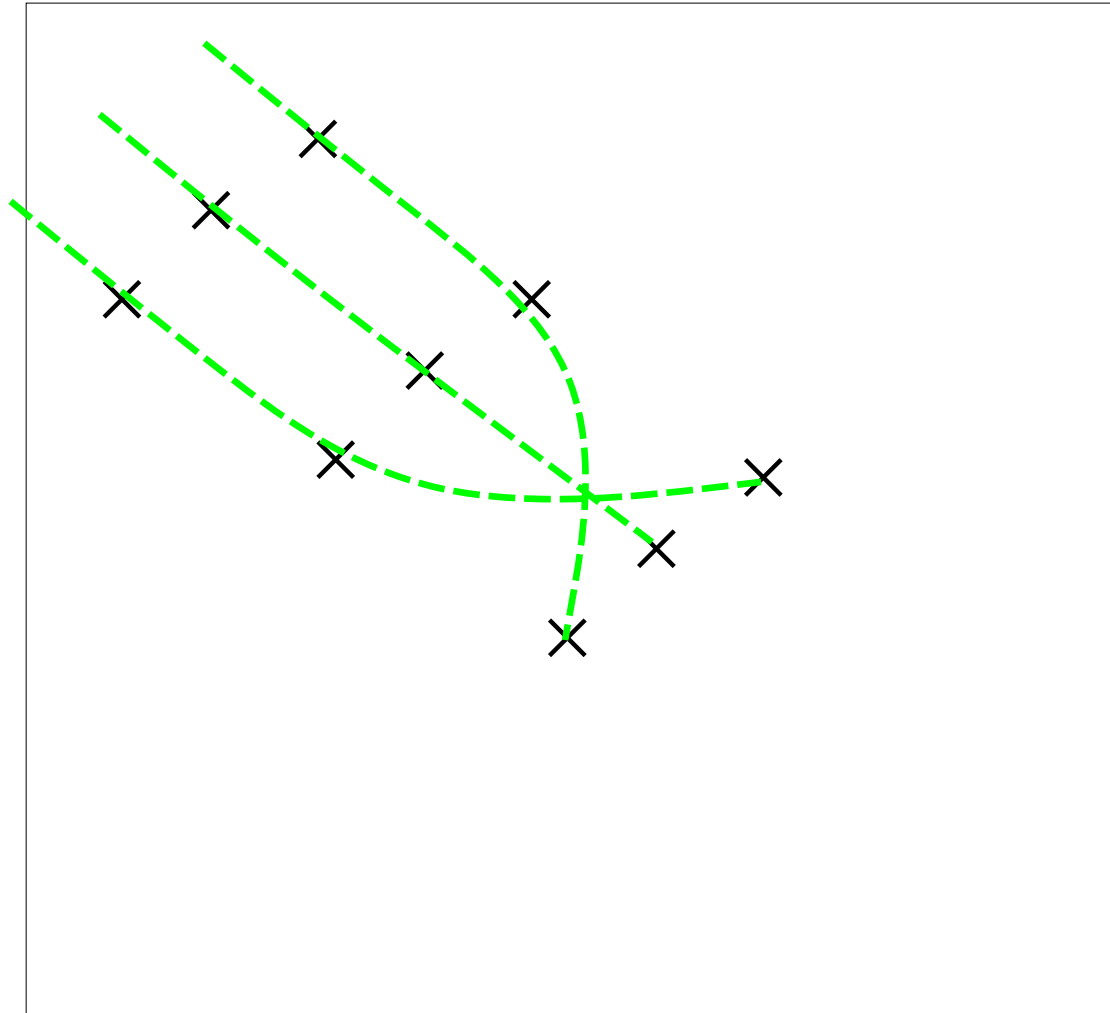
# Data association: classical

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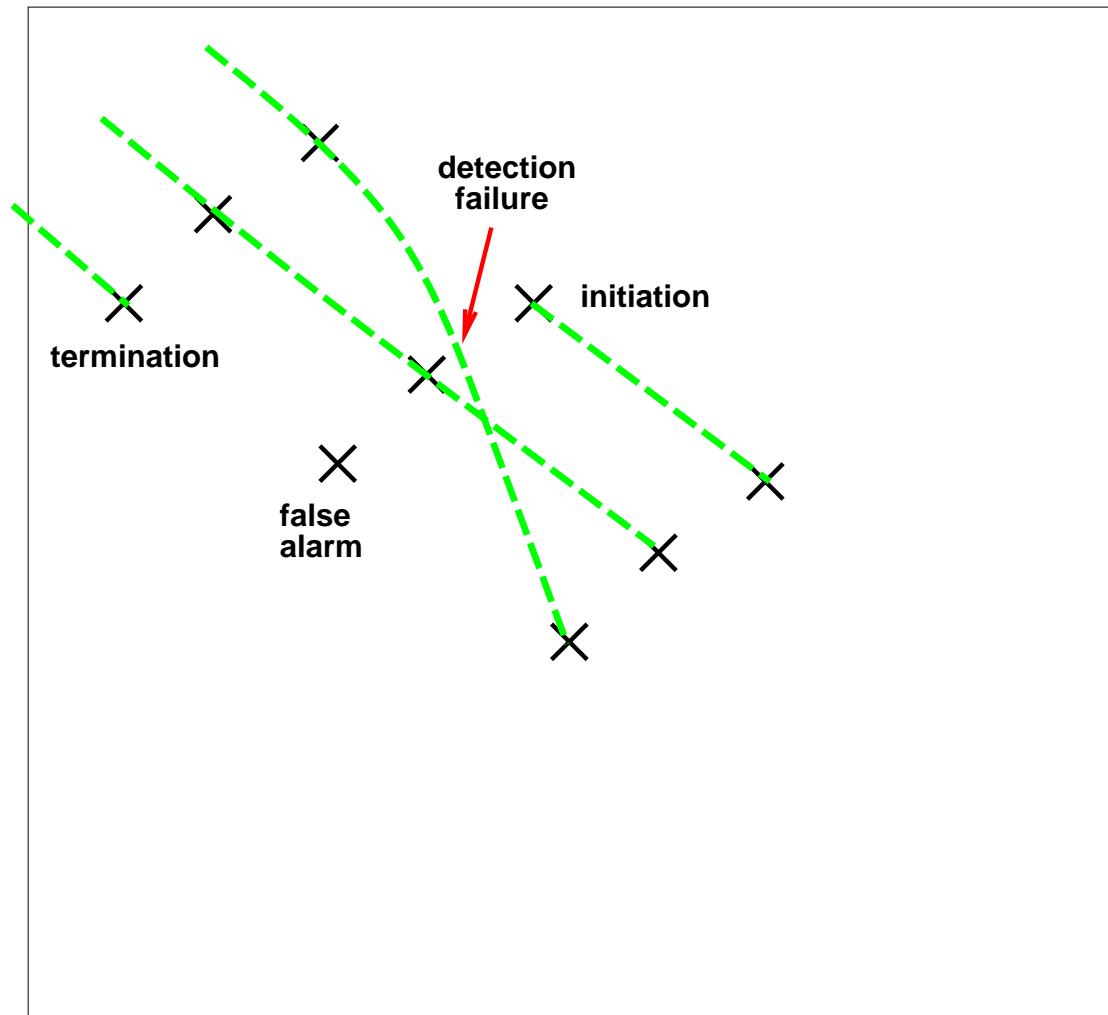
# Data association: classical

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# Data association: classical

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# First-order probabilistic languages

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(Gaifman, 1964; Halpern, 1990; lots of recent papers)

Idea: KB defines probability measure  $\mu$  over all possible logical worlds

Idea [PR 01]: FOPL inference by sampling possible logical worlds

- ◇ Not easy to define consistent and complete theories
  - ◇ Most FOPLs assume unique names and domain closure:  
*possible world = Herbrand model on fixed object set*
  - ◇ Real world violates unique names and domain closure
  - ◇ BLOG [MMR 04] for open worlds:  
*possible world = object sets + relation structure + symbol mapping*
-

# BLOG models

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*Guaranteed objects* are known to exist:

$\{\text{Color } c\} : = \{\text{Red, Blue}\}$

Also includes built-in types (integers, strings, reals, etc.)

*Number statements* specify distributions for objects that might exist:

$\#\{\text{Ball } b\} : \sim \text{Uniform}(\{1, \dots, 8\})$

Can also depend on existence of other objects

*Dependency statements* specify conditional distributions for predicates and functions

$\text{TrueColor}(b) : \sim \text{Uniform}(\{\text{Color } c\})$

$\text{BallDrawn}(d) : \sim \text{Uniform}(\{\text{Ball } b\})$

$\text{ObservedColor}(d) : \sim \text{ColorSensorModel}(\text{TrueColor}(\text{BallDrawn}(d)))$

---

# BLOG model for citations

---

$\#\{\text{Researcher } r\}$ :

$\sim \text{NumResearchersDistrib}()$

$\text{Name}(r)$ :

$\sim \text{NamePrior}()$

$\#\{\text{Publication } p\}$ :

$\sim \text{NumPubsDistrib}(\{\text{Researcher } r\})$

$\text{NumAuthors}(p)$ :

$\sim \text{NumAuthorsDistrib}()$

$\text{Author}(p, i)$ :

if  $i < \text{NumAuthors}(p)$

then  $\sim \text{SampleUnused}(\{\text{Researcher } r\},$   
 $\{\text{Author}(p, j) : j < i\})$

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# BLOG model for citations, contd.

---

Title( $p$ ):

$\sim TitlePrior()$

PubCited( $c$ ):

$\sim Uniform(\{Publication\ p\})$

NameAsCited( $c, i$ ):

if  $i < NumAuthors(PubCited(c))$

then  $\sim NameObs(Name(Author(PubCited(c), i)))$

TitleAsCited( $c$ ):

$\sim TitleObs(Title(PubCited(c)))$

CitString( $c$ ):

$\sim CitDistrib(\{NameAsCited(c, i) : i < NumAuthors(PubCited(c))\},$   
TitleAsCited( $c$ ))

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# BLOG model for aircraft tracking

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$\#\{\text{AirBase}\}$ :

$\sim \text{NumBasesDistrib}()$

$\text{Location}(b)$ :

$\sim \text{UniformLocation}()$

$\#\{\text{Aircraft} : \text{HomeBase} \mapsto b\}$ :

$\sim \text{NumAircraftDistrib}()$

$\text{TakesOff}(a, t)$ :

if  $t > 0 \wedge \neg \text{InFlight}(a, t - 1)$   
then  $\sim \text{TakeoffBernoulli}()$

$\text{Lands}(a, t)$ :

if  $t > 0 \wedge \text{InFlight}(a, t - 1)$   
then  $\sim \text{LandingDistrib}(\text{State}(a, t - 1),$   
 $\text{Location}(\text{Dest}(a, t - 1)))$

---

# BLOG model for aircraft contd.

---

CurBase( $a, t$ ):

```
if  $t = 0$  then = HomeBase( $a$ )
elseif TakesOff( $a, t$ ) then = null
elseif Lands( $a, t$ ) then = Dest( $a, t - 1$ )
else = CurBase( $a, t - 1$ )
```

InFlight( $a, t$ ):

```
= (CurBase( $a, t$ ) = null)
```

State( $a, t$ ):

```
if TakesOff( $a, t$ )
    then  $\sim$  InitState(Location(CurBase( $a, t - 1$ )))
elseif InFlight( $a, t$ )
    then  $\sim$  StateTransition(State( $a, t - 1$ ),
                               Location(Dest( $a, t$ )))
```

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# BLOG model for aircraft contd.

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Dest( $a, t$ ):

```
if TakesOff( $a, t$ )
  then  $\sim$  UniformChoice({AirBase  $a$ })
elseif InFlight( $a, t$ )
  then = Dest( $a, t - 1$ )
```

#{RadarBlip : BlipSource  $\mapsto a$ , BlipTime  $\mapsto t$ }:

```
if InFlight( $a, t$ ) then  $\sim$  NumDetectionsDistrib()
```

#{RadarBlip : BlipSource  $\mapsto$  null, BlipTime  $\mapsto t$ }:

```
 $\sim$  NumFalseAlarmsDistrib()
```

ApparentPos( $r$ ):

```
if BlipSource( $r$ ) = null
```

```
  then  $\sim$  FalseDetectionDistrib()
```

```
else  $\sim$  ObsDistrib(State(BlipSource( $r$ ), BlipTime( $r$ )))
```

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# Semantics

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*Possible worlds* defined by

- possibly infinite sets of objects for each type, each tagged by generation record (if any)  
e.g., *Publication<sub>12</sub> from Researcher<sub>3</sub>*
- a relation over the objects for each random predicate symbol
- a function over the objects for each random function symbol
- an object for each random constant symbol

*Theorem*: every well-formed BLOG KB defines a unique measure over possible worlds

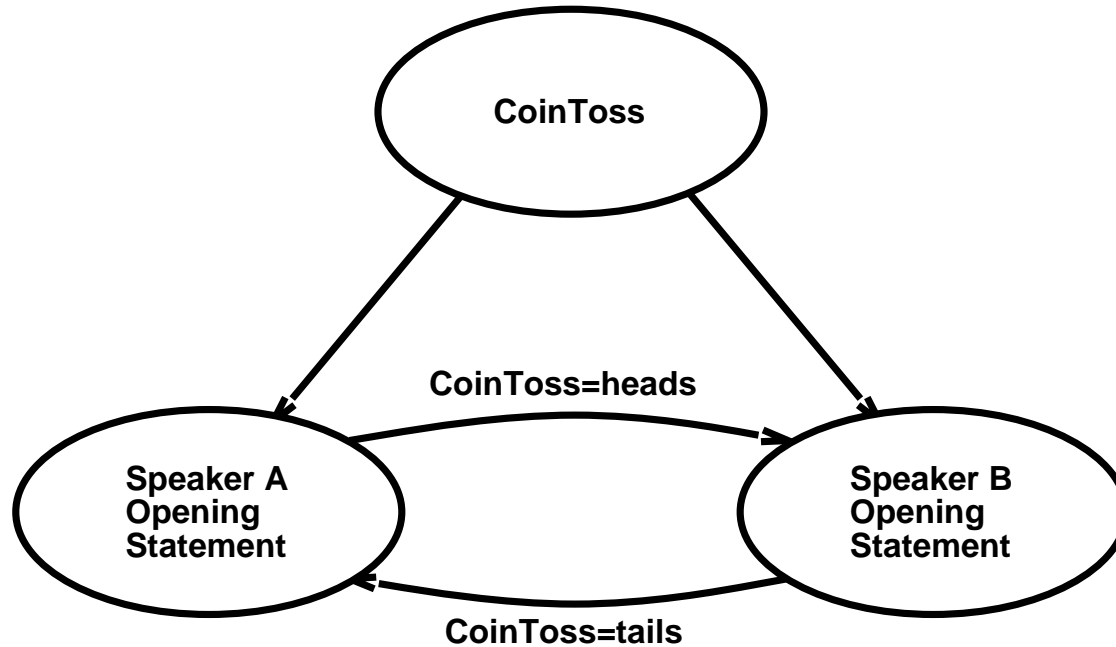
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# Well-formed BLOG models

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Dependency structure specified by BLOG model must

- have no infinite receding chains
- have finite parent contexts (but may have infinite parent sets)
- be *conditionally acyclic*

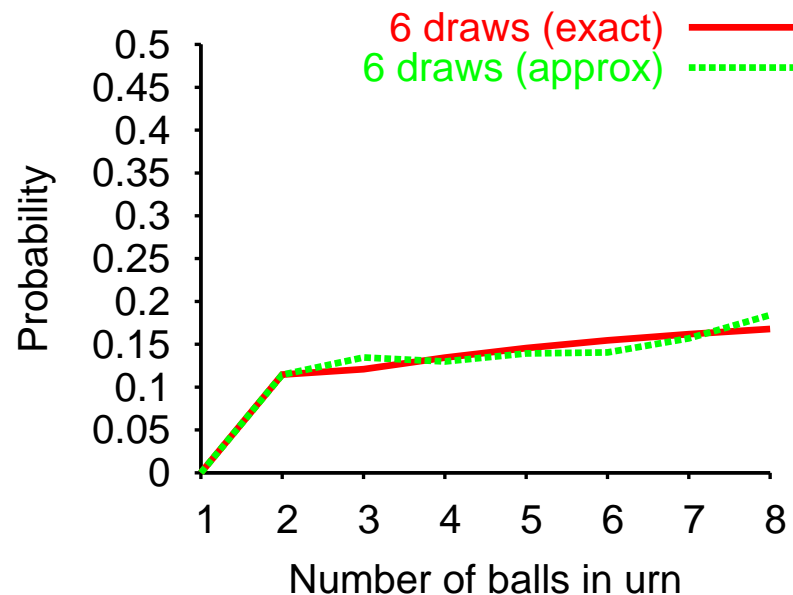


# Inference

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Completely generic importance sampling and MCMC algorithms based on query/evidence ancestor search

*Theorem:* Algorithms are consistent and have finite time per sample, for any well-formed BLOG model



# Application of MCMC to FOPLs

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Markov chain states are possible worlds

Proposals are modifications to worlds  $\omega \longrightarrow \omega'$

e.g., change relations between objects, merge objects, etc.

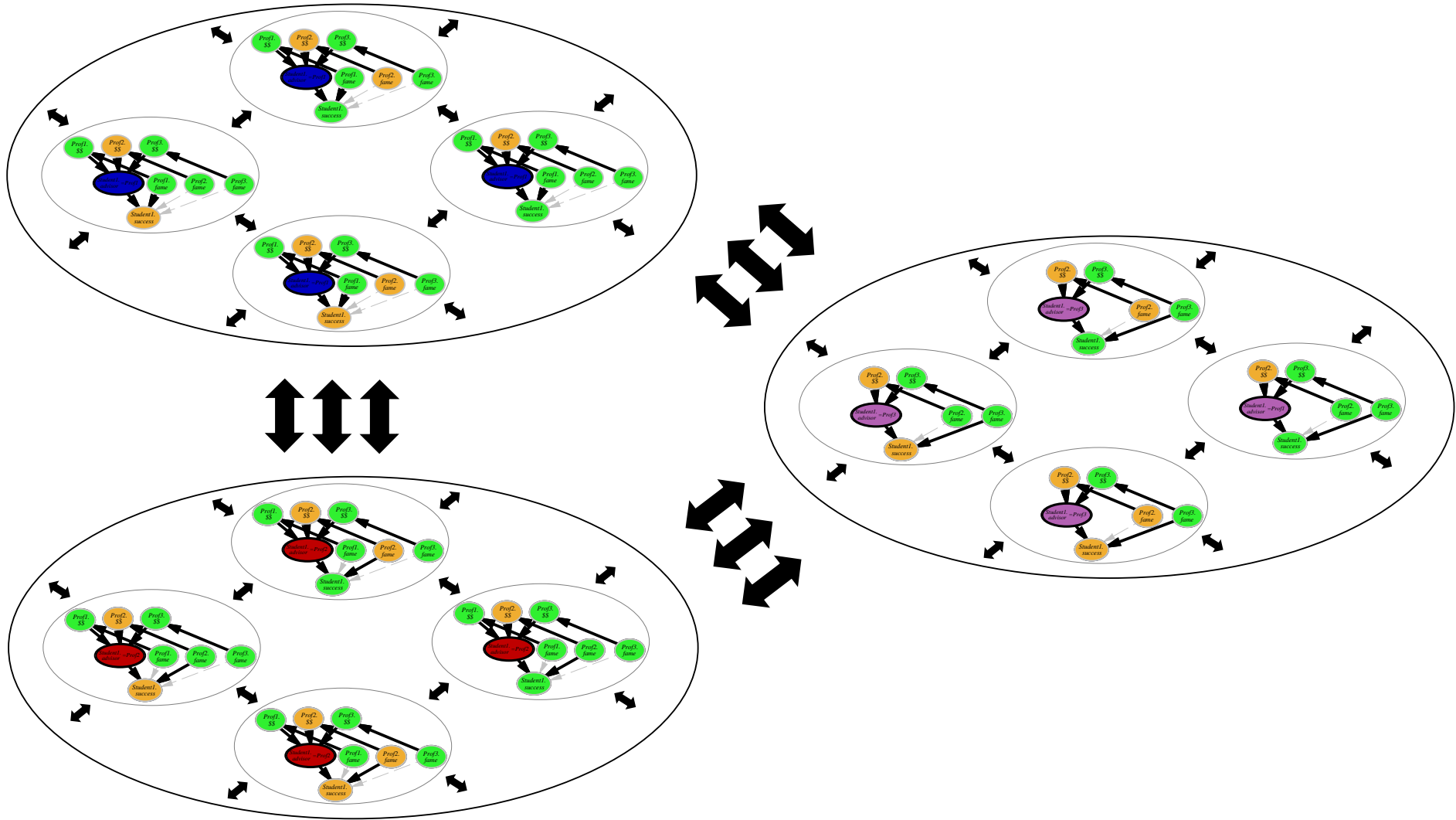
Transition ratio  $\pi(\omega')/\pi(\omega)$  computable from KB,  
ideally by incremental modification

Computing  $f(\omega)$  = evaluating arbitrary query sentence on a world,  
ideally by incremental modification

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# MCMC on possible worlds



# Citation matching

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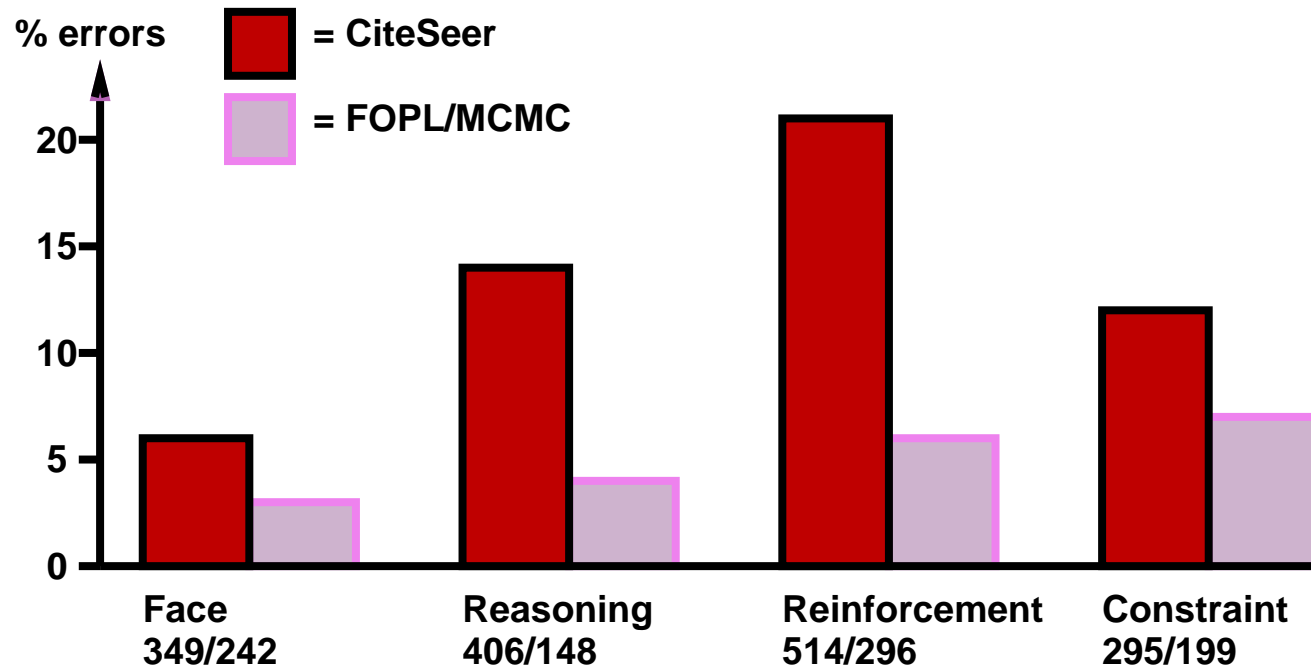
[PMMRS 02]: MCMC state is a complete publication database

Transitions (these all happen automatically via generic inference):

- change cited publication
  - change authorship
  - change true title, true author names
  - change citation parsing decisions
  - add/remove papers, researchers
-

# Citation results

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# Integrated Parsing and Extraction

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Citation parsing is nontrivial: HMM gets 31% correct

Wauchope, K. Eucalyptus: Integrating Natural Language Input with a Graphical User Interface. NRL Report NRL/FR/5510-94-9711 (1994).

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# Integrated Parsing and Extraction

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Citation parsing is nontrivial: HMM gets 31% correct

Wauchope, K. Eucalyptus: Integrating Natural Language Input with a Graphical User Interface. NRL Report NRL/FR/5510-94-9711 (1994).

Adducing other evidence helps:

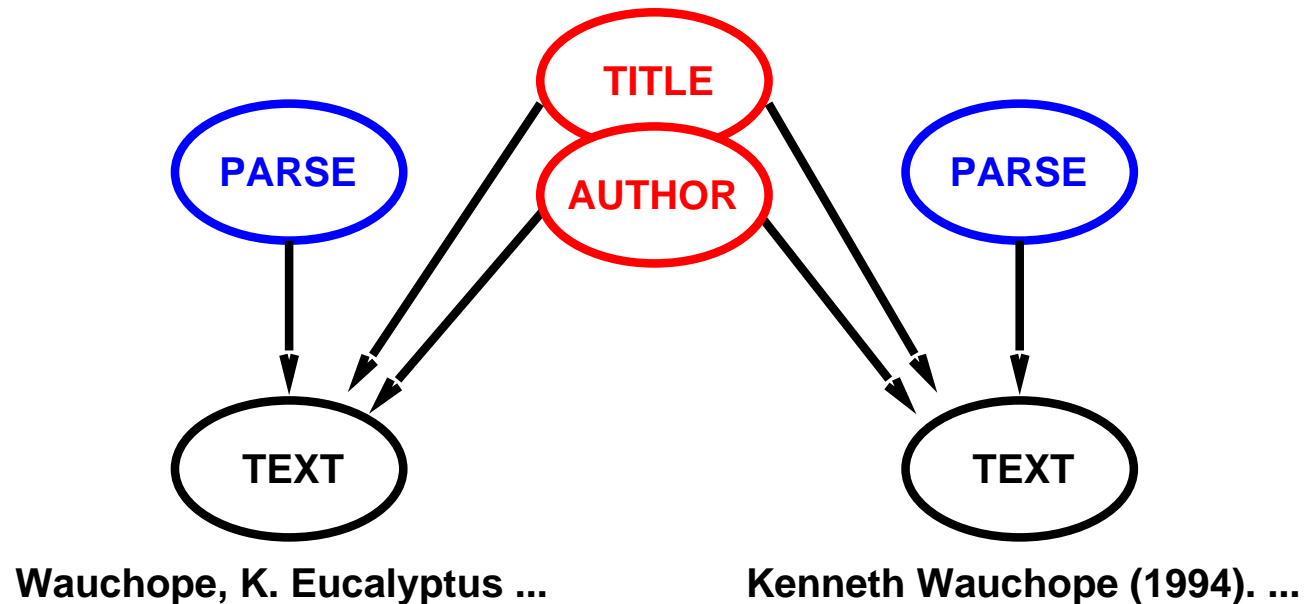
Kenneth Wauchope (1994). Eucalyptus: Integrating natural language input with a graphical user interface. Technical Report, Naval Research Laboratory, Washington, DC, 39pp.

64% correct parsing by combining two citations

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# Knowledge and Parsing

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Knowledge directly affects MCMC parsing decisions

Transfer of information depends on paper identity assumption  
i.e., combining top-down and bottom-up processing

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# Summary

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Probability models for full FOL model structures—unknown worlds

Inference currently slow except for application-specific proposals

Needs a generic adaptive proposal mechanism

Parametric learning easy via stochastic EM; structural learning harder

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