

# Routing and Peering in a Competitive Internet

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# Peering

- Multiple network providers: AT&T, Sprint, etc.
- *Peering points*: connection points between network providers
- Key issue: What is the value of interdomain routing?

# Outline

- Provider objectives
- Routing in a competitive internet
- Future directions

# Provider objectives

Assume we are given two providers with following goals:

- The sending network  $S$ : Outgoing traffic should exit as cheaply as possible
- The receiving network  $R$ : Incoming traffic should be sent to destination at minimum cost

Sender's strategy: *nearest exit* or "hot potato" routing.

# Routing in a competitive Internet

Henceforth: Assume peering point locations are fixed.

- Optimal routing and nearest exit routing
- Game theoretic models

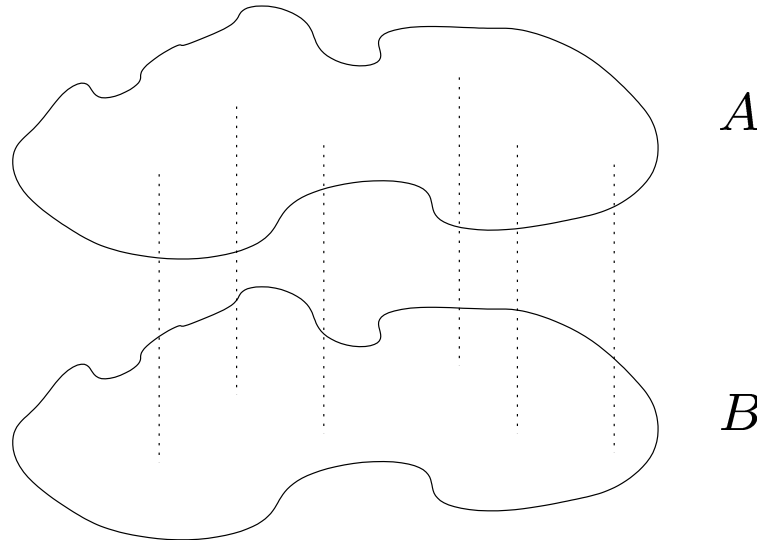
# Optimal routing: the traditional framework

- Flow on link  $(i, j)$ :  $f_{ij}$
- Cost incurred on link  $(i, j)$ :  $C_{ij}(f_{ij})$
- Minimize  $\sum_{(i,j)} C_{ij}(f_{ij})$   
subject to source-destination flow constraints

Note: *As if* only one network provider exists.

# “Nearest exit” routing: the competitive Internet

- Two network providers connected by peering points



- Each minimizes cost only within their own network

# Optimal vs. nearest exit routing

- All costs linear:  $C_{ij}(f_{ij}) = d_{ij}f_{ij}$
- Peering points:  $p_1, \dots, p_n \in N$  (zero cost)

*Optimal routing:*

Shortest path between  $s$  and  $d$ .

*Nearest exit routing:*

Provider 1 sends from  $s$  to nearest peering point  $p_i$ .

Provider 2 uses shortest path from  $p_i$  to  $d$ .



# Comparison

How much worse than optimal routing is nearest exit routing?

*Theorem:*

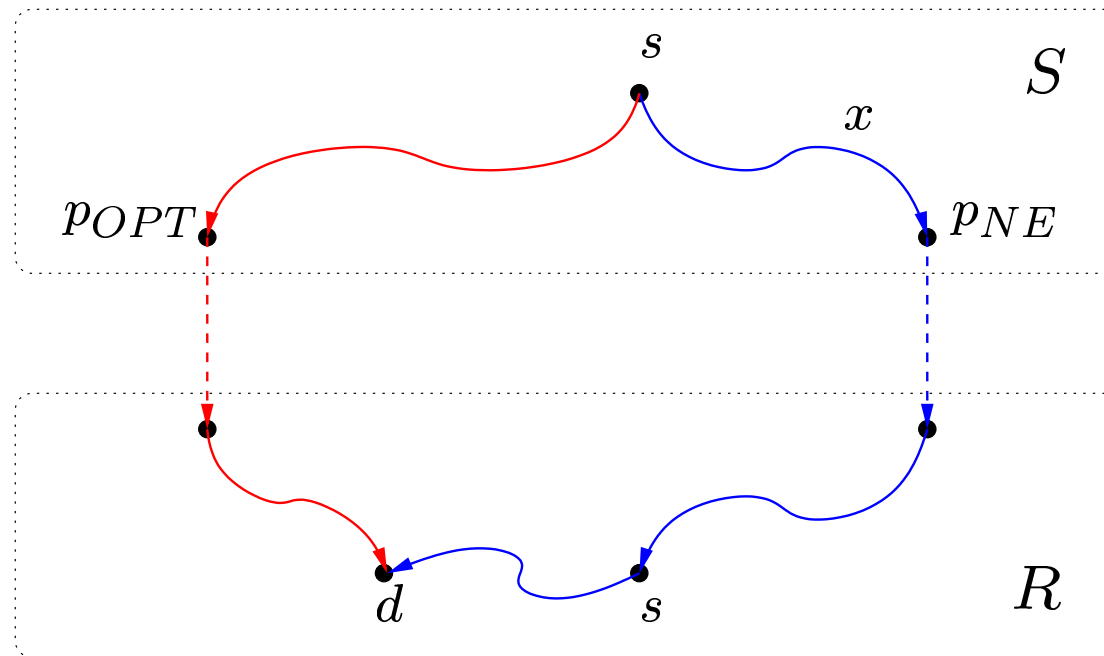
If:

- All costs are linear, and
- $S = R$

Then:

Nearest exit routing cost  $\leq 3 \times$  optimal routing cost

# Proof of bound



**Blue:** Nearest exit routing

**Red:** Shortest path routing (cost =  $r$ )

## Proof of bound

Note:  $x \leq r$  by definition of nearest exit routing.

One possible receiver route from  $p_{NE}$  to  $d$ :

$$p_{NE} \rightarrow s \in R: \text{cost } x \leq r$$

$$s \rightarrow d \in R: \text{cost } \leq r$$

So total nearest exit cost is  $\leq 3r$ .

## In general?

In general, nearest exit cost is arbitrarily worse than optimal.

Competitive routing as a two-stage game:

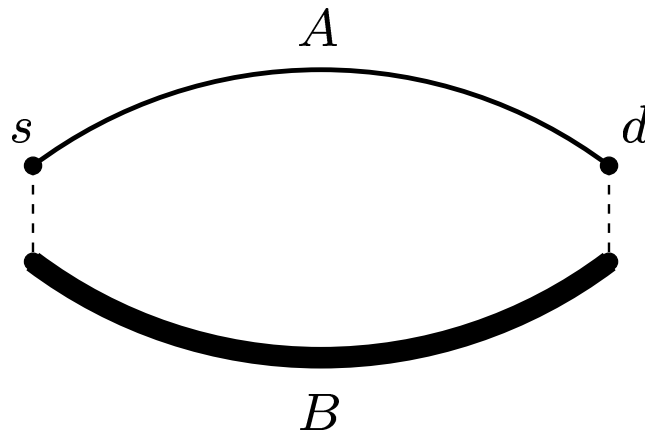
1. Providers choose prices for use of their links
2. *Given prices*, providers determine how best to route flow

Is the optimal routing solution, with:

$$\text{price of link} = \text{marginal cost of link}$$

an equilibrium of this game?

# Game theoretic models: example



Provider  $A$ : Wants to send  $x_A$  from  $s$  to  $d$ .

Provider  $B$ : Wants to send  $x_B \ll x_A$  from  $s$  to  $d$ .

At optimal routing solution, marginal costs are low.

But at these prices, provider  $B$  has an incentive to raise his price.

# Game theoretic models

Objective for provider  $A$ :

Minimize:

*Cost of total flow on  $A$ 's link:  $C_A(f_A)$*

+

*Payment to provider  $B$ :  $p_B \times (A$ 's flow sent on  $B$ 's link)*

—

*Payment from provider  $B$ :  $p_A \times (B$ 's flow sent on  $A$ 's link)*

Subject to:

$A$  sends  $x_A$  from  $s$  to  $d$

# Game theoretic models

We can analyze the optimal routing solution, which yields:

- flow  $f_i$  on link  $i$
- price  $p_i = C'_i(f_i)$  (marginal cost) on link  $i$

Except in a completely symmetric situation,  
the optimal routing solution is *never* an equilibrium of the two-stage game.

## Future directions

Moral: We must not assume that the predictions of a global static optimization model will hold up in a competitive Internet.

Future research questions:

- Game theoretic analysis of routing for arbitrary networks
- Optimal strategies for individual providers



## **Future directions**

- Pricing mechanisms to encourage optimal routing
- Protocol design to encourage optimal routing