Evaluating forecasts with observations across time scales

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Observing the system in situ

To evaluate the models we need to have relevant measurements

State variables are momentum (winds), energy (temperature), and tracer masses

The most important tracer is water, divided among various states including two(+) flavors of condensate

Climate-relevant observations are long term, geographically diverse, with well-understood sampling

Observing the system in situ

Go outside.

30.2 Rain Rising 80-4 ഷം 80-8 Risin Dul - 450 Thick Orarcast SNOOTH 470 SNOOTH Dull 49' Overcast Cissi SLIGHT SWELL ಲಂ Fine 43° Clear

The dotted lines indicate the gradations of barometric pressure The variations of the temperature are marked by figures, the state of the sea and sky by descriptive words, and the direction of the wind by arrows—barbed and feathered according to its force. O denotes calm.

Image: http://galton.org

WEATHER CHART, MARCH 31, 1875.



Radiosonde locations, I Dec 2006, 6 hr window around 12Z





If you want to measure more of the atmosphere you look at it i.e. sense it remotely using electromagnetic radiation

$$\begin{aligned} \mathbf{\Omega} \cdot \nabla I(\mathbf{x}, \mathbf{\Omega}) &= -\sigma(\mathbf{x}) I(\mathbf{x}, \mathbf{\Omega}) \\ &+ \sigma(\mathbf{x}) \frac{\omega_0(\mathbf{x})}{4\pi} \int_{4\pi} I(\mathbf{x}, \mathbf{\Omega}) P(\mathbf{x}, \mathbf{\Omega}' \to \mathbf{\Omega}) d\mathbf{\Omega}' \\ &+ \sigma(\mathbf{x}) (1 - \omega_0(\mathbf{x})) B(T(\mathbf{x})) \end{aligned}$$

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$$\mu \frac{dI_{\lambda}(\tau,\mu,\phi)}{d\tau} = -I_{\lambda}(\tau,\mu,\phi) + \frac{\omega_0}{4\pi} \int_0^{2\pi} \int_{-1}^1 P_{\lambda}(\mu',\phi'\to\mu,\phi) I_{\lambda}(\tau,\mu',\phi') d\phi' d\mu' + (1-\omega_0) B_{\lambda}(T(\tau))$$

Three main characteristics

Passive vs. active remote sensing

Emission vs. scattering regimes

View from above or below

Observing the system remotely (emission/absorption)

In the infrared and microwave scattering is small

At nadir (looking straight down)

$$\mu \frac{dI_{\lambda}(\tau,\mu,\phi)}{d\tau} = -I_{\lambda}(\tau,\mu,\phi) + (1-\omega_0)B_{\lambda}(T(\tau))$$

In an absorbing atmosphere of total thickness au^*

$$I_{\lambda}(0) = I_{\lambda}(\tau^*)e^{-\tau^*} + \int_{\tau^*}^0 e^{-\tau'}B_{\lambda}(\tau')d\tau'$$



Dave Turner, U. Wisconsin



Dave Turner, U. Wisconsin

Observing the system remotely (scattering)

Scattering dominates in the visible and near-infrared in clouds (emission is negligible)

Solutions are costly to compute

Parameters vary significantly with wavelength, particle size, shape, ...



SWIR composite



Cloud Mask overall confidence

Thermodynamic phase Cloud_Phase_Optical_Properties



clear

probably cloudy



undetermined

Optical thickness

Particle size (µm)



Radiosonde locations, I Dec 2006, 6 hr window around 12Z



What's the likelihood of a given state given our forecast and observations?

$$p(\mathbf{x}|\mathbf{y}, \mathbf{x}_{\mathbf{b}}) = \frac{p(\mathbf{y}, \mathbf{x}_{\mathbf{b}}|\mathbf{x}) p(\mathbf{x})}{p(\mathbf{y}, \mathbf{x}_{\mathbf{b}})}$$

Introduce a cost function

$$J(\mathbf{x}) = -\log(p(\mathbf{x}|\mathbf{y}, \mathbf{x}_{\mathbf{b}})) + c$$

Assume no correlation between forecast and observation errors

$$p(\mathbf{y}, \mathbf{x}_{\mathbf{b}} | \mathbf{x}) = p(\mathbf{y} | \mathbf{x}) p(\mathbf{x}_{\mathbf{b}} | \mathbf{x})$$
$$J(\mathbf{x}) = -\log(p(\mathbf{x} | \mathbf{x}_{\mathbf{b}})) - \log(p(\mathbf{x} | \mathbf{y})) + c$$

Assume Gaussian distributions of forecast and observations errors

$$J(\mathbf{x}) = \frac{1}{2} (\mathbf{x}_{\mathbf{b}} - \mathbf{x})^T \mathbf{P}_{\mathbf{b}}^{-1} (\mathbf{x}_{\mathbf{b}} - \mathbf{x}) + \frac{1}{2} (\mathbf{y} - \mathcal{H}(\mathbf{x}))^T \mathbf{R}^{-1} (\mathbf{y} - \mathcal{H}(\mathbf{x}))$$

Our cost function minimum is at

$$\nabla J(\mathbf{x}) = \mathbf{P}_{\mathbf{b}}^{-1}(\mathbf{x}_{\mathbf{b}} - \mathbf{x}) + \mathbf{H}^{T}\mathbf{R}^{-1}(\mathbf{y} - \mathcal{H}(\mathbf{x})) = 0$$

Assuming linear observation operator

$$\mathcal{H}(\mathbf{x}) = \mathcal{H}(\mathbf{x}_{\mathbf{b}}) + \mathbf{H}(\mathbf{x} - \mathbf{x}_{\mathbf{b}})$$

So the most likely solution is given by

$$\mathbf{P}_{\mathbf{b}}^{-1}(\mathbf{x} - \mathbf{x}_{\mathbf{b}}) + \mathbf{H}^{T}\mathbf{R}^{-1}(\mathcal{H}(\mathbf{x}_{\mathbf{b}}) + \mathbf{H}(\mathbf{x} - \mathbf{x}_{\mathbf{b}}) - \mathbf{y}) = 0$$

Rearranging gives something more familiar

$$\mathbf{x}_{\mathbf{a}} = \mathbf{x}_{\mathbf{b}} + \mathbf{K}(\mathbf{y} - \mathcal{H}(\mathbf{x}_{\mathbf{b}}))$$

with

$$\mathbf{K} = [\mathbf{P}_{\mathbf{b}}^{-1} + \mathbf{H}^T \mathbf{R}^{-1} \mathbf{H}]^{-1} \mathbf{H}^T \mathbf{R}^{-1}$$

This is the Kalman filter equation

Data assimilation for weather forecasting

There are two main classes of implementation of the Kalman filter in the atmospheric sciences

Variational methods minimize the cost function iteratively

"3D-Var" minimizes cost function at a single time; "4D-Var" minimizes cost function over some extended time window

Variational methods need tangent-linear and adjoint models

Ensemble methods use Monte Carlo integration of Bayes's formula; take sample covariance matrices from a finite ensemble

Ensemble data assimilation recipe (for Brian Mapes)

For each observation in turn

compute the prior/background observation PDF

fit the ensemble of expected observations with a Gaussian

find the product of the background and observation PDFs

find the increment needed for each ensemble member

update "each" element in the state vector in each member

regress the expected observation against the element using the ensemble

apply (observation increment) * (correlation coefficient) * (localization)

Data assimilation is model evaluation

Analysis quality is measured by quality of fit to observations

"Observation biases" make this complicated

Forecast skill is measured against verifying analysis

Note: Forecast skill includes errors in forecast model and initial conditions (including errors in assimilation)

Standard deterministic verification metrics are boring

Geographic regions:

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Tropics (20S - 20N), extratropics (20-90 S, N)
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Grid: 2.5° lat-lon

Quantities:

Sea-level pressure, geopotential height, winds, temperature Heights: 850 hPa, 250 hPa (+ sea level in extratropics) Statistics:

bias, root-mean-square error, anomaly correlation, S1 skill (measures magnitude of gradients)

Anomaly correlation of ECMWF 500hPa height forecasts



Simmons and Hollingsworth, 2001

Deterministic forecast evaluation

A lot of effort goes into analyses - best estimates of the state of the atmosphere

Verification against those analyses is straightforward

Tests large-scale circulation, which is not so sensitive to model details

But evaluation is routine - 2-4 times each day, year after year

Probabilistic evaluation is more fun

Ensembles of forecasts

produce sample distributions

are expressed as the probability of some discrete event (e.g. "chance of rain > 1 mm")

Verification is binary

Brier score is discrete analog to mean-squared error

Includes sharpness (differentiation of forecasts) and reliability (forecast frequencies matching observations)



Tom Hamill, notes for Short Course on Ensemble Forecasting From weather forecasting to climate projections

Weather forecasting and climate modeling communities (and codes) are mostly distinct

Few climate models are able to make weather forecasts

Retrospective simulations are loosely coupled to historical state of the atmosphere

The most sought-after forecasts by climate models (e.g. "climate sensitivity") can't be verified

Observing the climate system: data reduction

How are all those observations summarized?

Univariate averaging on regular grids, for the most part

Maybe histograms, joint histograms, linear regressions

Life without time correspondence (evaluating "climate")

Choose a variable ϕ

Build a composite season cycle

$$\hat{\phi}(x, y; m) = \frac{1}{Y} \sum_{y=1}^{Y} \phi(x, y; m, y)$$

Compute the mean squared error

$$e^2 = \frac{1}{T} \int_T \frac{1}{A} \int_A (\hat{\phi}_m - \hat{\phi}_o)^2 \, da \, dt$$

Invoke

$$e^{2} = \overline{e}^{2} + e^{\prime 2}$$
$$= \overline{e}^{2} + \sigma_{o}^{2}(1 + s^{2} - 2sr)$$



K.E. Taylor, 200 I (c.f. Pincus et al., 2008)





There are three more broad classes of evaluation based on

relationships among variables (e.g. Bony et al., 2003; Bennhold and Sherwood, 2008; Clement et al., 2009)

characteristics of emergent behavior (e.g. Williams and Tselioudis, 2008; see also phenomena-based metrics)

information theoretic (e.g. Shukla et al., 2005, Majda and Gershgorin 2010)

There may be an infinity of ways in which the models are wrong



Shukla el al., 2005

The climate model evaluation conundrum

Models are evaluated during development

Each group, each individual has their own set of metrics

Centers trade-off skill in mean vs. skill in variability

Community metrics are being developed

But there is no basis on which to select or prefer a given metric

Weak-to-no observational basis linking historical skill with climate change response

Relationships in existing ensembles may be fortuitous and/or have simple causes