



Deconvolutional Networks

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Overview

- “Generative” image model
- Convolutional form of sparse coding
- Pooling with latent variables (what/where)
 - Integrated into cost function (differentiable)
- Learn features for object recognition

Talk Overview

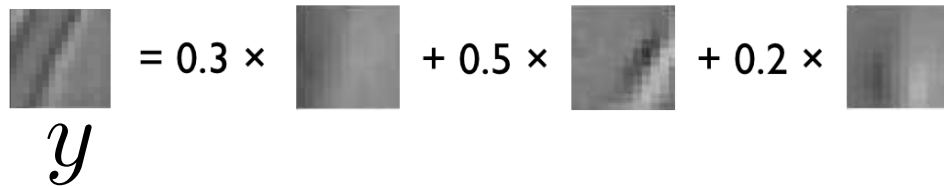
- Single layer
 - Convolutional Sparse Coding
 - Gaussian Pooling
- Multiple layers
 - Multi-layer inference
 - Filter learning
- Related work
- Experiments

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Recap: Sparse Coding (Patch-based)

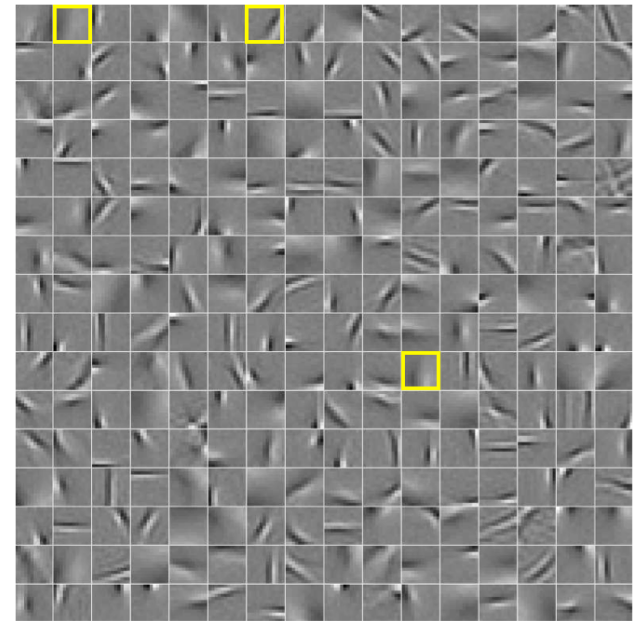
- Over-complete linear decomposition of input y using dictionary D


$$y = 0.3 \times \text{patch}_1 + 0.5 \times \text{patch}_2 + 0.2 \times \text{patch}_3$$

$$C(y, D) = \underset{p}{\operatorname{argmin}} \frac{\lambda}{2} \|Dp - y\|_2^2 + |p|_1$$

- ℓ_1 regularization yields solutions with few non-zero elements:

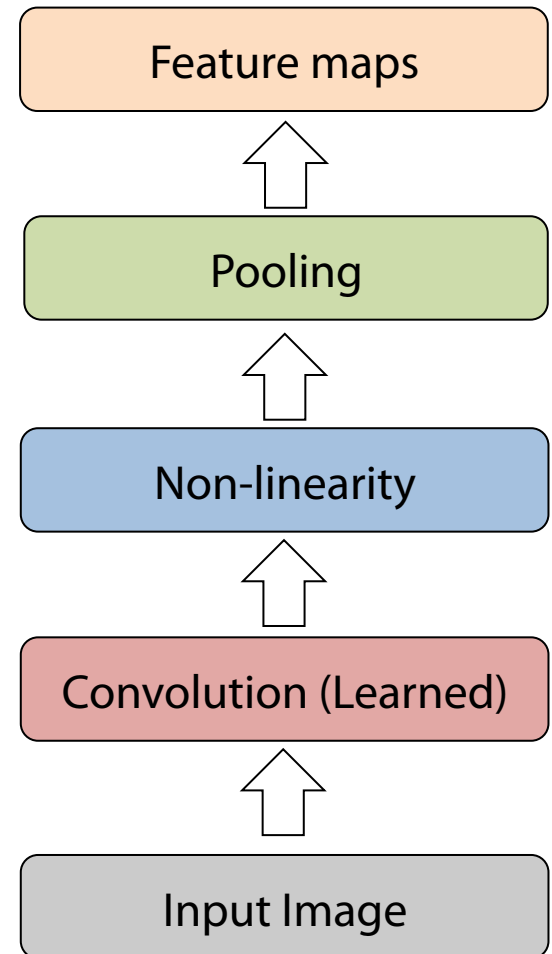
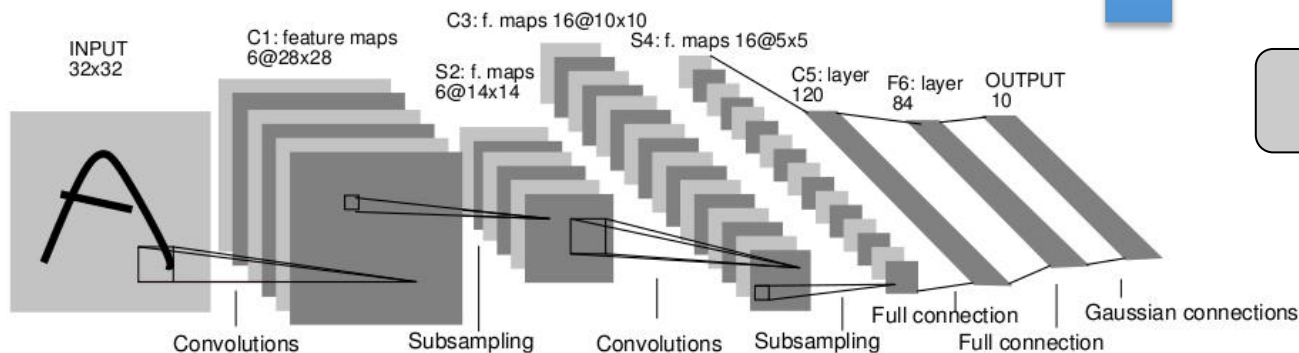
$$p = [0, 0.3, 0, \dots, 0.5, \dots, 0.2, \dots, 0]$$



Dictionary D

Convolutional Networks

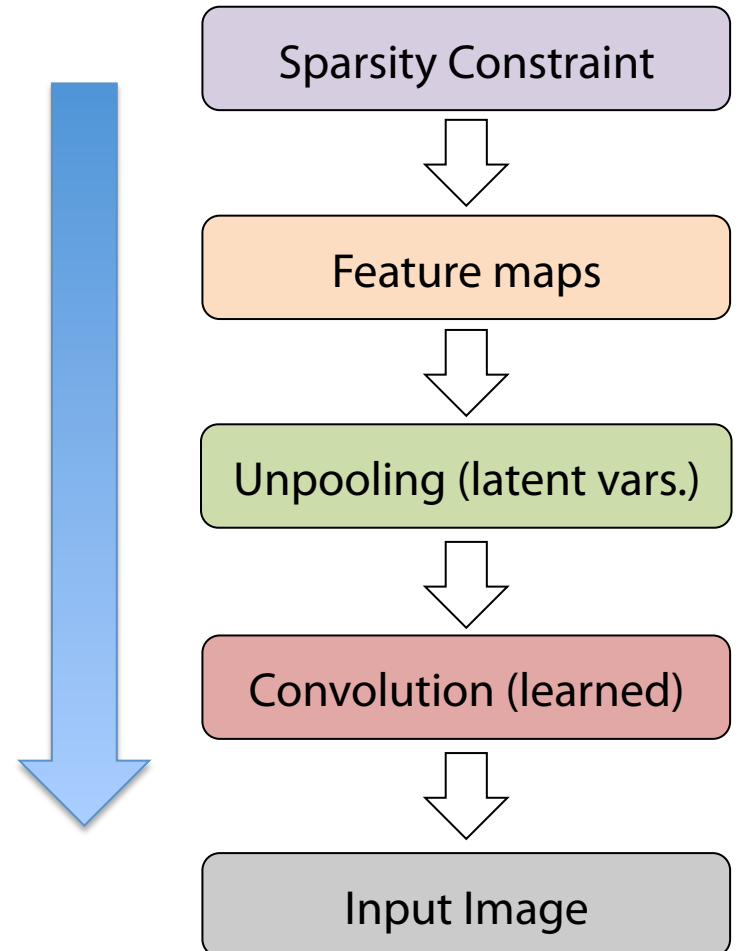
- Feed-forward:
 - Convolve input
 - Non-linearity
 - Pooling
- Supervised
- Encoder-only



Deconvolutional Networks

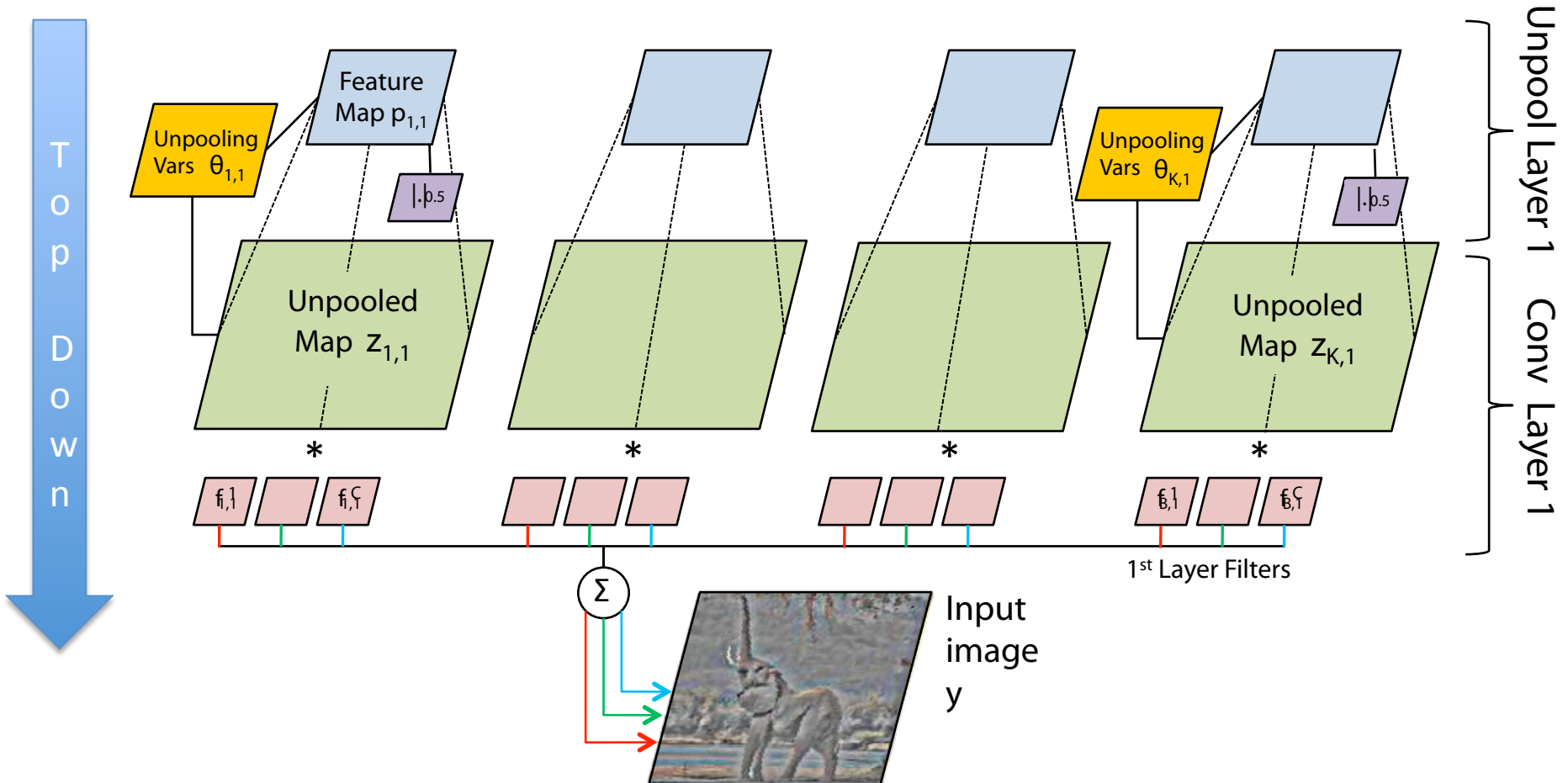
[Zeiler et al. CVPR'10, ICCV'11]

- Feed-back:
 - Unpool feature maps
 - Using inferred latent variables
 - Convolve unpooled maps
 - Learned filters
- Unsupervised
 - Must reconstruct input
 - Sparsity constraint
- Decoder-only
 - Have to infer features



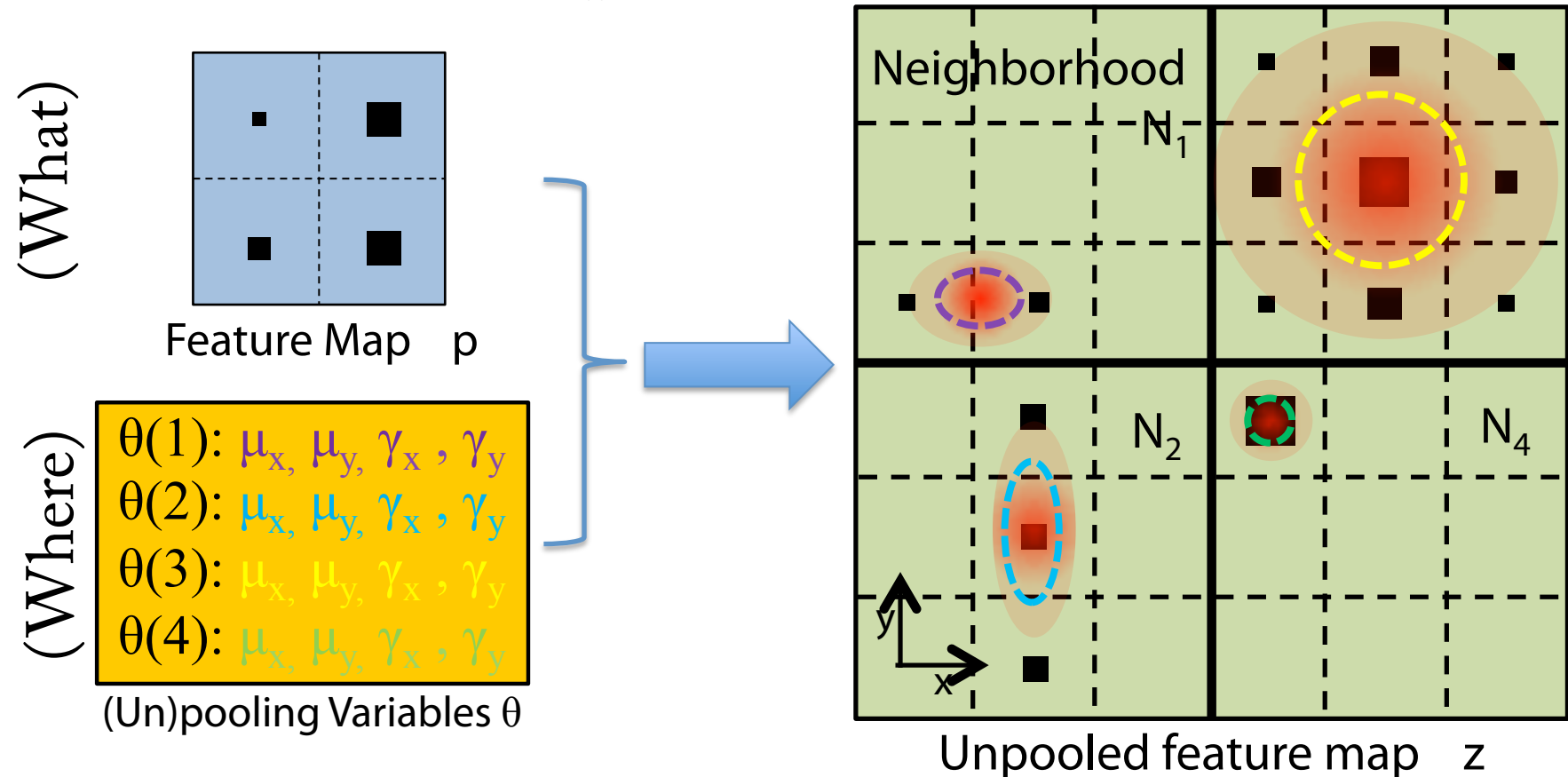
Single Layer Architecture

- Decomposition of input image
 - Over-complete $\rightarrow$ per-element sparsity constraint

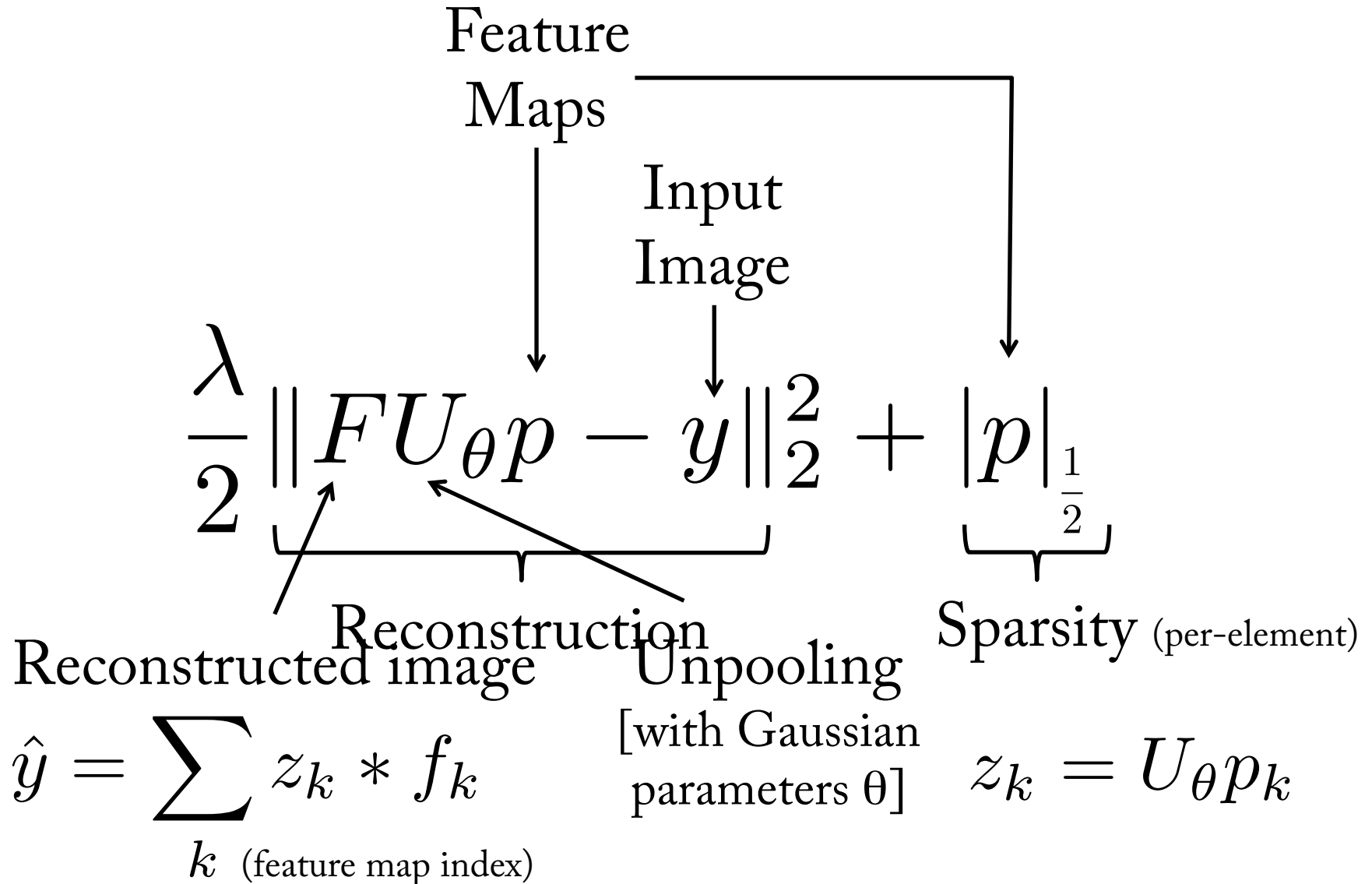


Gaussian Unpooling

- Each unpooling region has its own 2D Gaussian
- Gaussian weights scaled by feature map activation
- Differentiable representation



Single Layer Cost Function



Single Layer Cost Function

Learned
(share across
all images)

Feature
Maps

Input
Image

Infer for
each image

$$\frac{\lambda}{2} \| \textcolor{green}{F} U_{\textcolor{red}{\theta}} \textcolor{red}{p} - y \|_2^2 + |\textcolor{red}{p}|_{\frac{1}{2}}$$

Reconstructed image

$$\hat{y} = \sum_k \textcolor{red}{z}_k * \textcolor{green}{f}_k$$

k (feature map index)

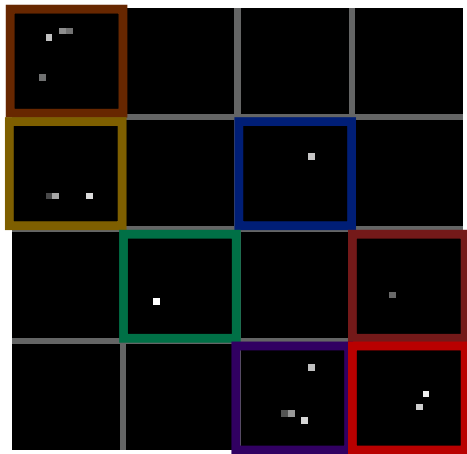
Unpooling
[with **Gaussian**
parameters θ]

$$\textcolor{red}{z}_k = U_{\textcolor{red}{\theta}} \textcolor{red}{p}_k$$

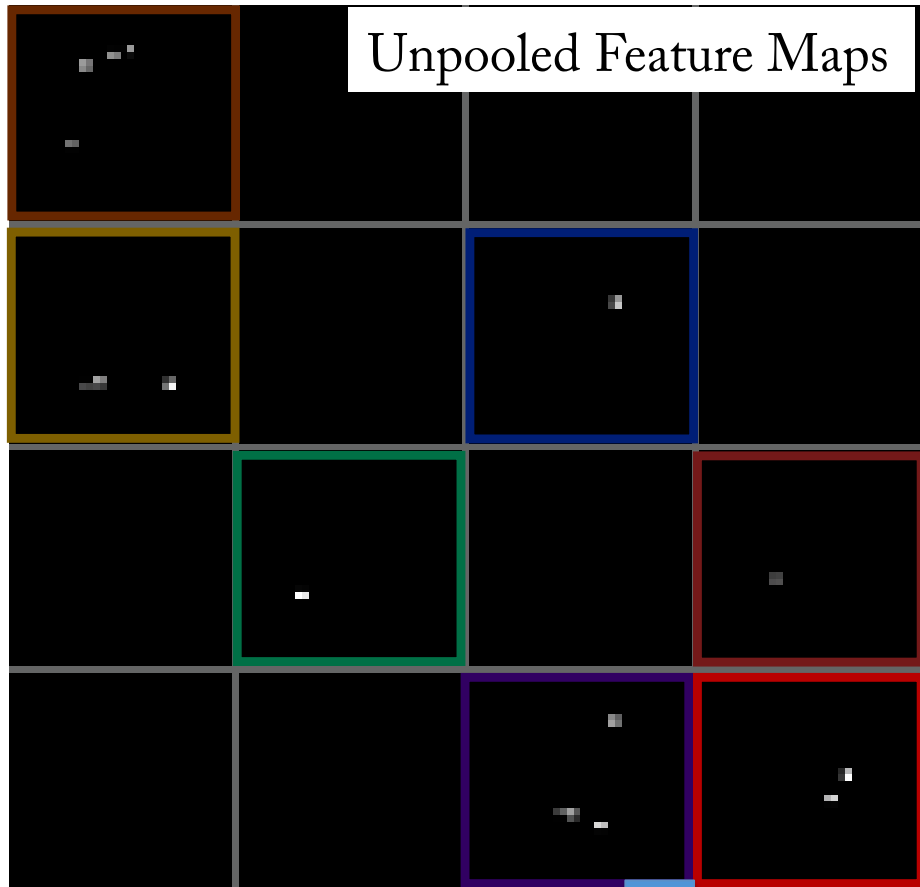
Single Layer Inference

- Feature Maps $\mathbf{p}$ (What)
 - Fix convolution filters $\mathbf{f}$ and pooling variables θ
 - Convolutional form of sparse coding
 - Use ISTA [Beck & Teboulle SIAM J. Imaging Sciences 2009]:
 - Gradient step on reconstruction term (Quadratic)
 - Gradient step on sparsity term
 - Project to be non-negative
- Pooling variables θ (Where)
 - Fix convolution filters $\mathbf{f}$ and feature maps $\mathbf{p}$
 - Chain rule of derivatives to update mean & precision of each Gaussian pooling neighborhood

Single Layer Example



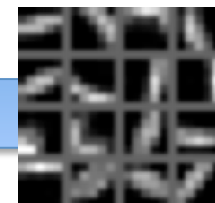
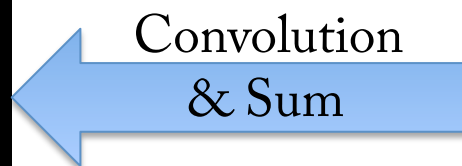
16 Feature Maps



Input Image



Reconstruction



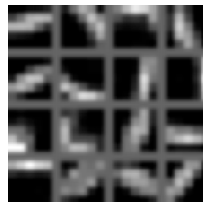
Filters

Effect of Pooling Variables

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Pixel-space projections of
sample feature map activations



Filter
coefficients



Reconstruction Examples

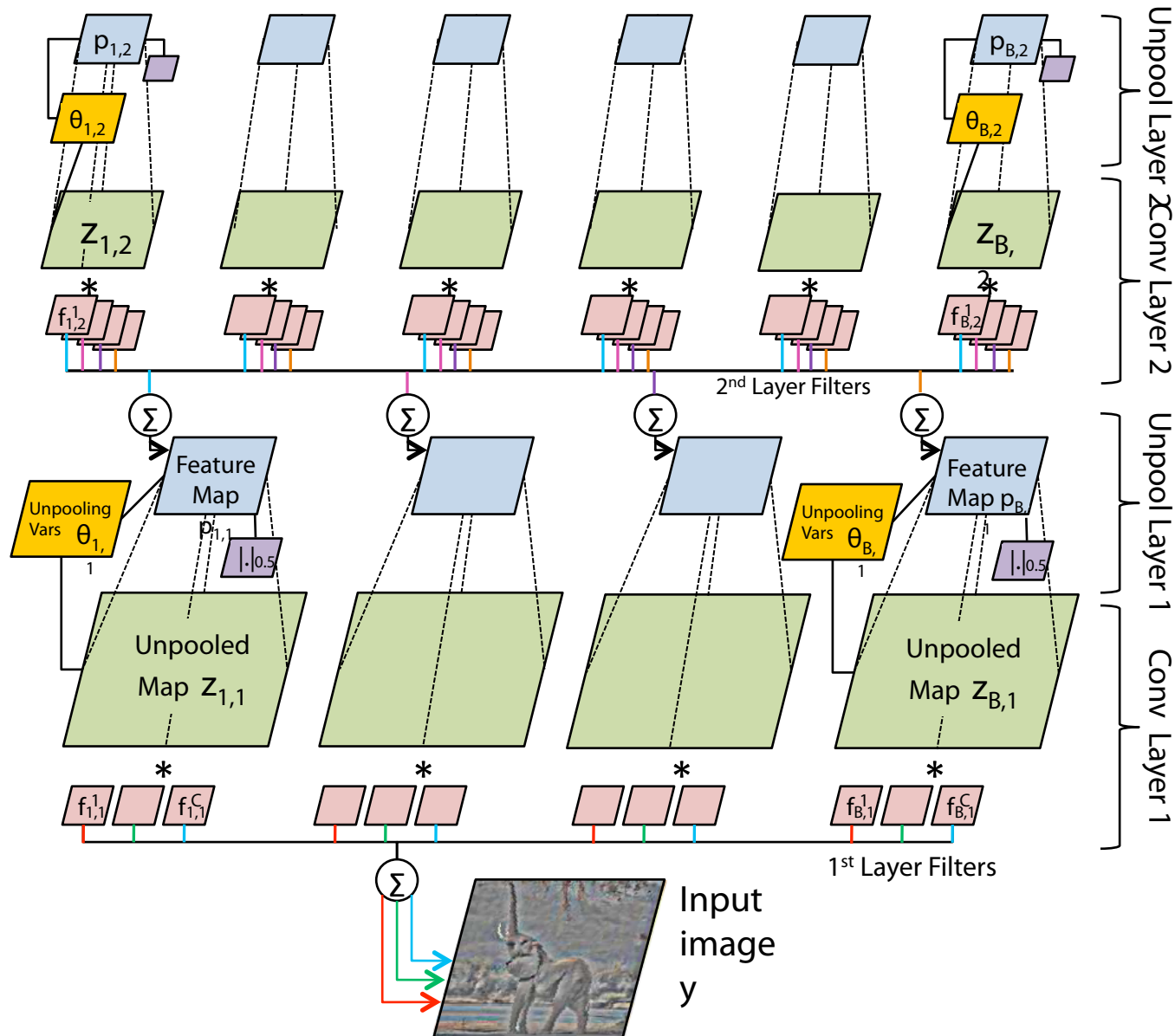
Talk Overview

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Stacking the Layers

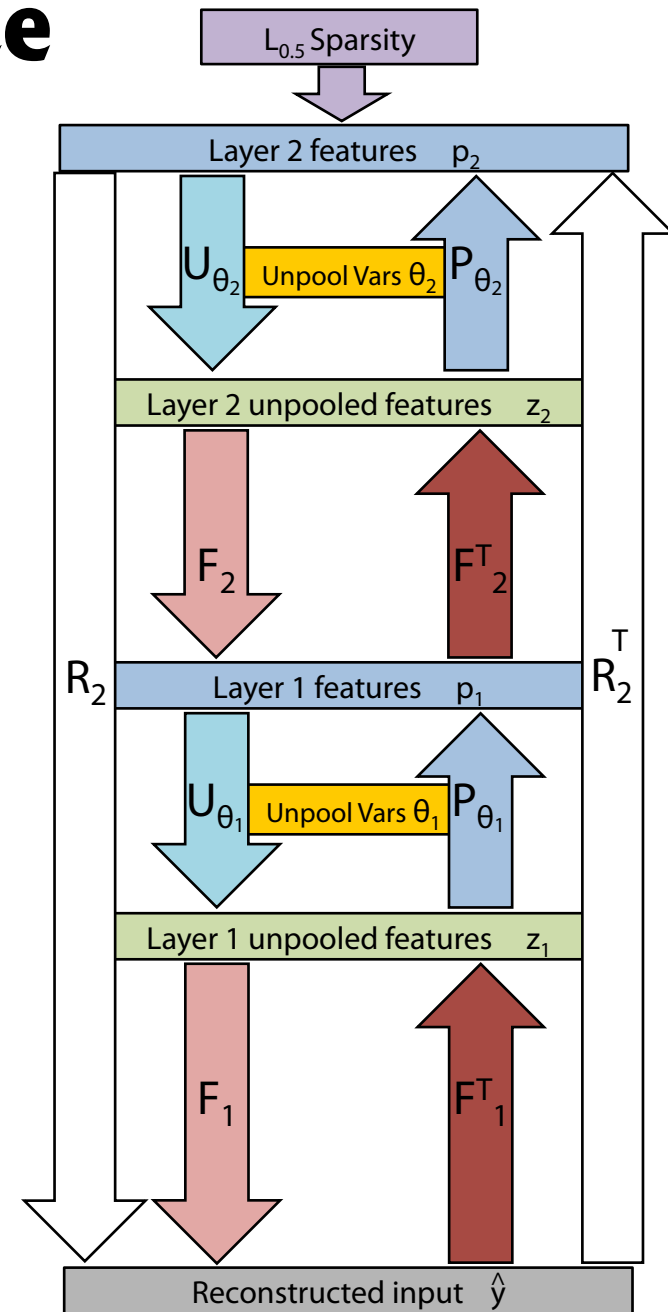
- Take pooled maps as input to next layer
- Joint inference over all layers
 - Only possible with differentiable pooling
- Objective is reconstruction error of input image
 - Not layer below, like most deep models
- Sparsity & pooling make model non-linear
 - No explicit non-linearities (e.g. sigmoid)

Overall Architecture (2 layers)



Multi-layer Joint Inference

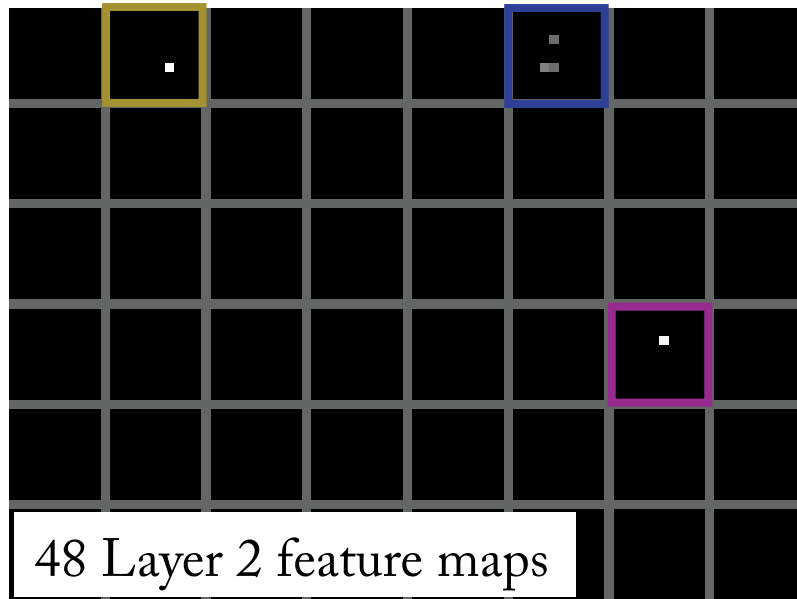
- Consider layer 2 inference:
 - Want to minimize reconstruction error of **input image** $\|\hat{y} - y\|_2^2$, subject to sparsity.
 - Update feature maps at top (p_2) and pooling variables (θ_1, θ_2) from both layers



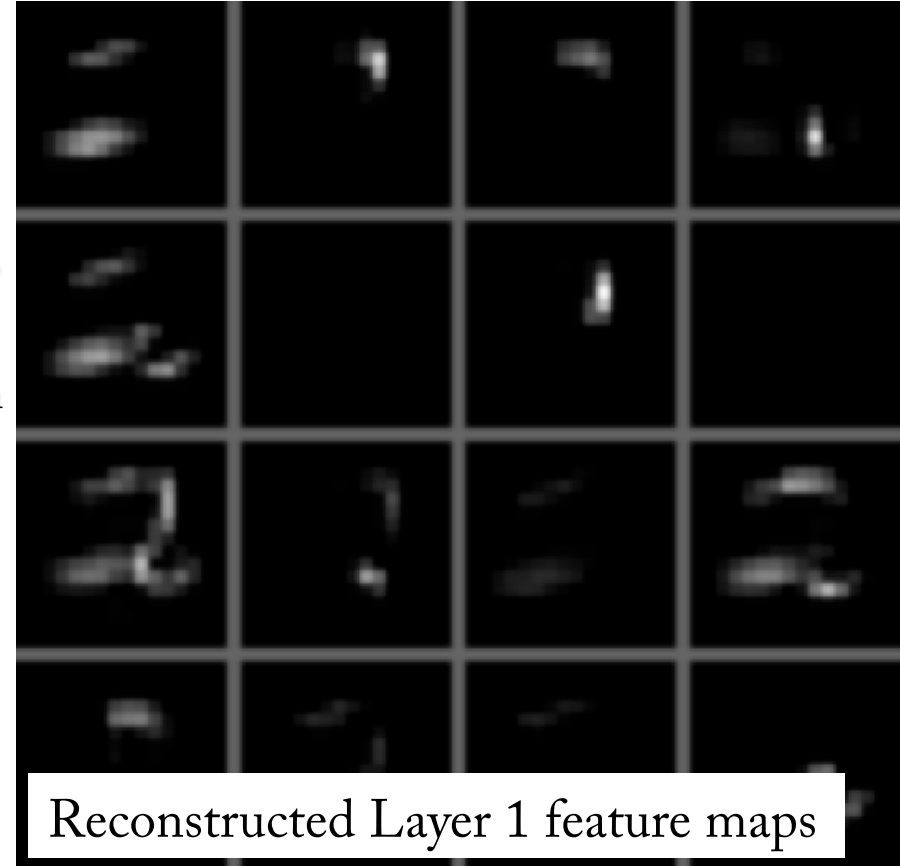
Filter Learning

- Goal: update convolutional filters f
- Fixed feature maps p & pooling variables θ
 - from inference on all training images
- Over-constrained least-squares problem
- Use Conjugate Gradients
- Normalize to unit L2 length & project positive
- Learn filters layer-by-layer
 - Joint training doesn't seem to work

Two Layer Example



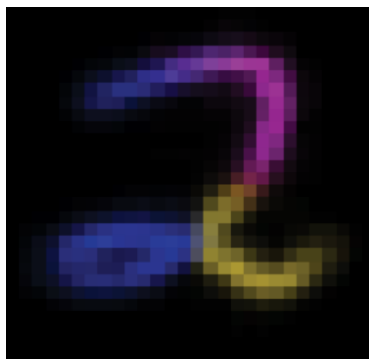
Unpool &
Convolution
with
Layer 2
filters



Input Image



Reconstruction



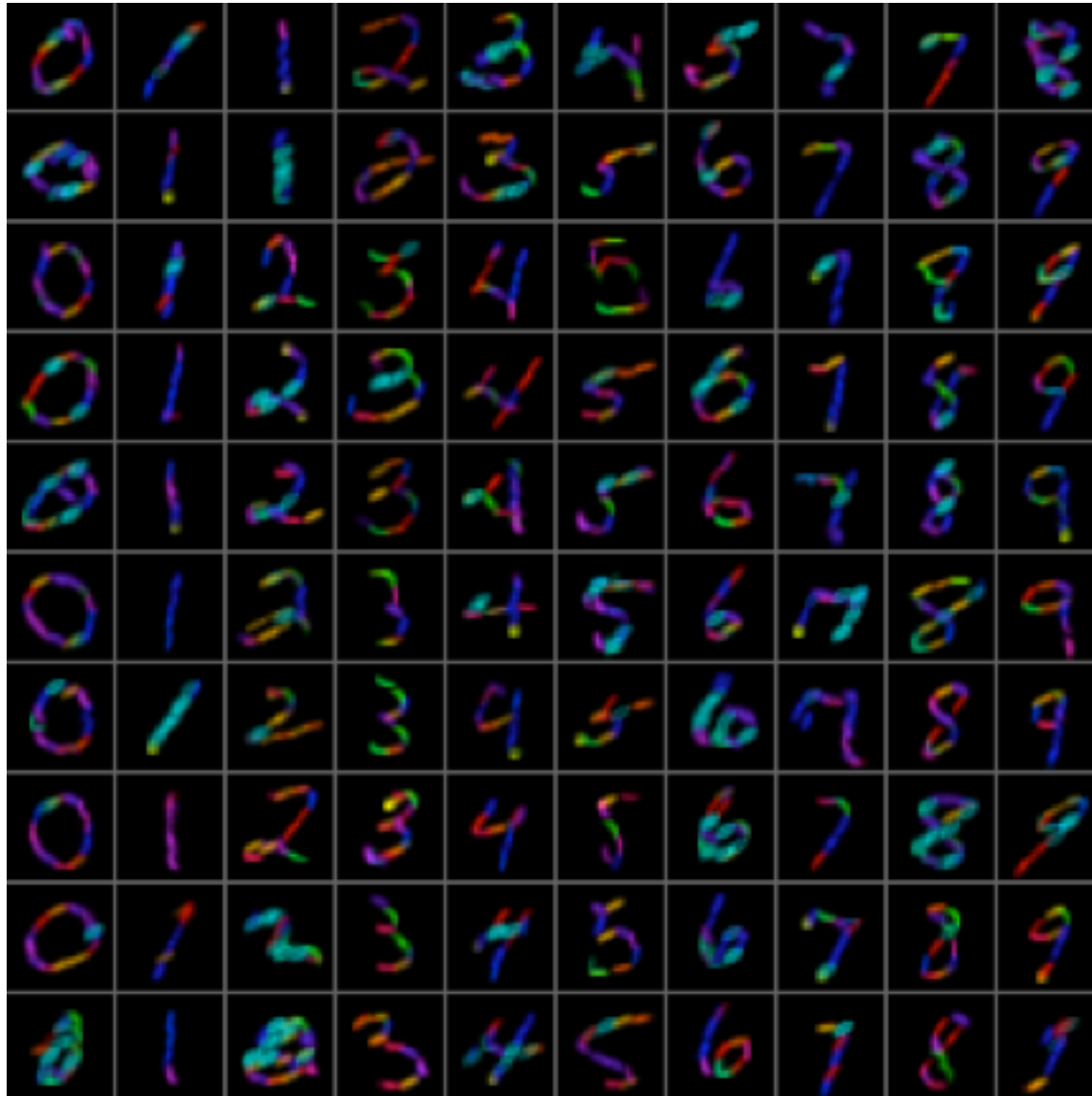
Unpool &
Convolution
with
Layer 1
filters

Reconstructions from 2 layer model

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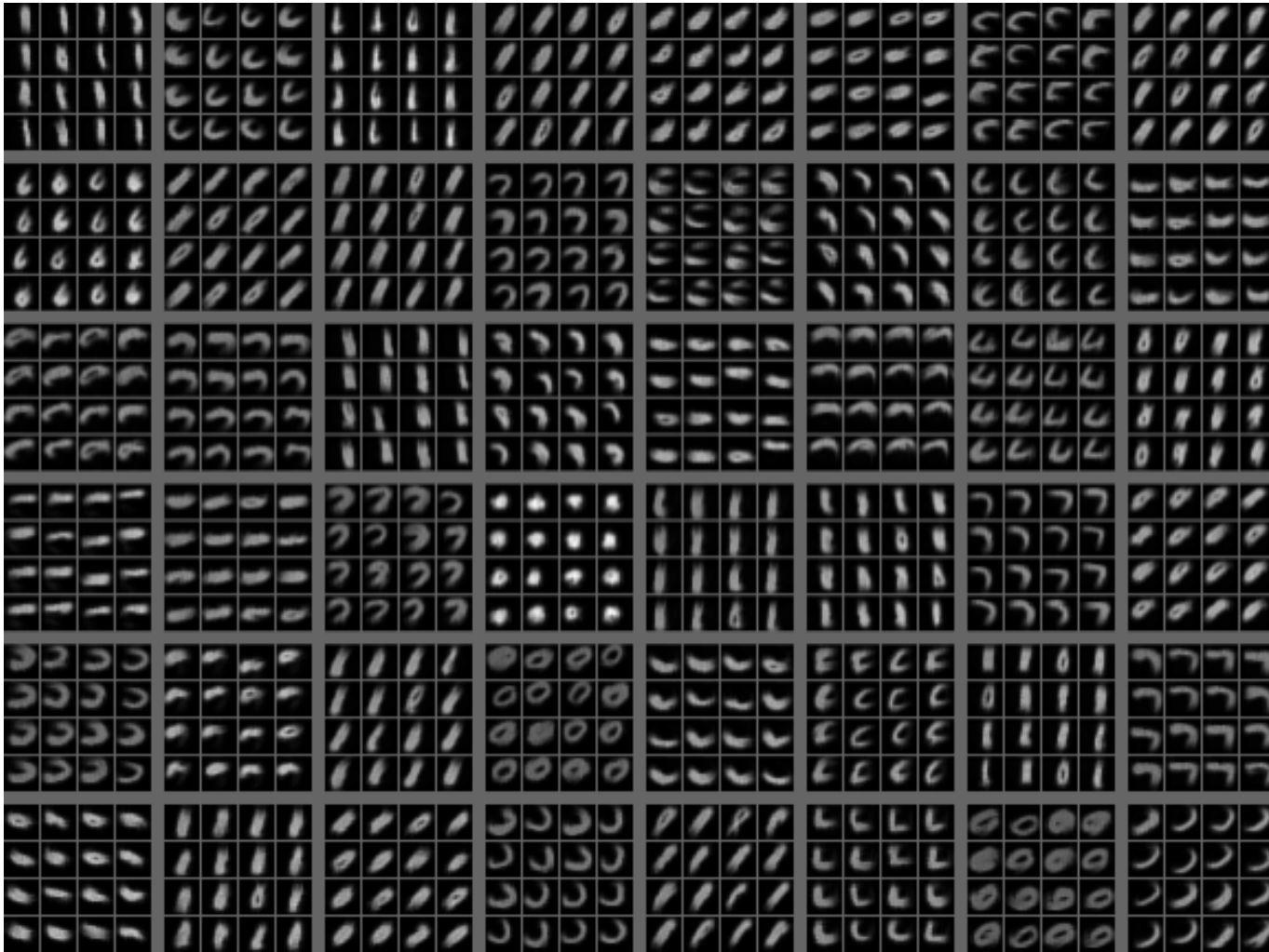


.....



Gaussian Pooling in 2 layer model

- Projection of 2nd layer features activations down to pixels, using inferred pooling variables



Algorithm 1 Learning with Differentiable Pooling in Deconvolutional Networks

Require: Training set Y , # layers L , # epochs E , # ISTA steps T

Require: Regularization coefficients λ_l , # feature maps B_l

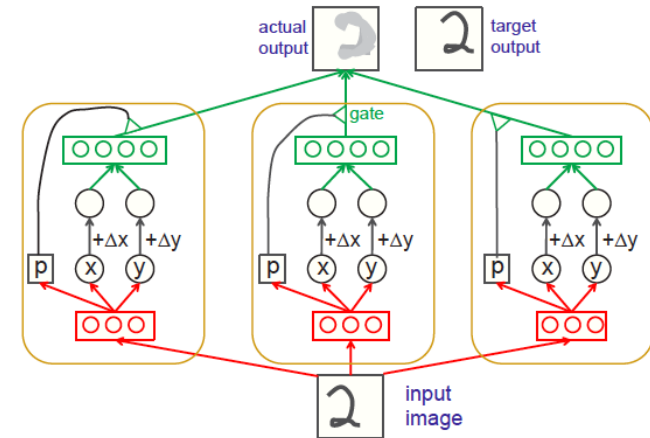
Require: Pooling step sizes β_{U_l}

```
1: for  $l = 1 : L$  do %% Loop over layers
2:   Init. features/filters:  $p_l^i \sim 0, f_l \sim \mathcal{N}(0, \epsilon)$ 
3:   Init. switches:  $\theta_l^i = Fit(R_l^T y_i) \quad \forall i$ 
4:   for epoch = 1 :  $E$  do %% Epoch iteration
5:     for  $i = 1 : N$  do %% Loop over images
6:       for  $t = 1 : T$  do %% ISTA iteration
7:         Reconstruct input:  $\hat{v}_l^i = R_l p_l^i$ 
8:         Compute reconstruction error:  $e = \hat{v}_l^i - v^i$ 
9:         Propagate error up to layer  $l$ :  $\nabla p_l = R_l^T e$ 
10:        Estimate step size  $\beta_{p_l}$  as in Eqn. 15
11:        Take gradient step on  $p$ :  $p_l^i = p_l^i - \lambda_l \beta_{p_l} \nabla p_l$ 
12:        Perform shrink:  $p_l^i = \max(|p_l^i| - \beta_{p_l}, 0) \text{sign}(p_l^i)$ 
13:        Project to positive:  $p_l^i = \max(p_l^i, 0)$ 
14:        for  $k = 1 : l$  do %% Loop over lower layers
15:          Take gradient step on  $\theta$ :  $\theta_k^i = \theta_k^i - \lambda_l \beta_{U_k} \nabla \theta_k$ 
16:        end for
17:      end for
18:    end for
19:    Update  $f_l$  by solving Eqn. 26 using CG
20:    Project  $f_l$  to positive and unit length
21:  end for
22: end for
23: Output: filters  $f$ , feature maps  $p$  and pooling variables  $\theta$ .
```

Related Work

- What / Where Separation

- Transforming Auto-Encoders [Hinton et al. ICANN'11]
- Gregor & LeCun [<http://arxiv.org/pdf/1006.0448v1.pdf>]
- [Ranzato et al. CVPR'07]

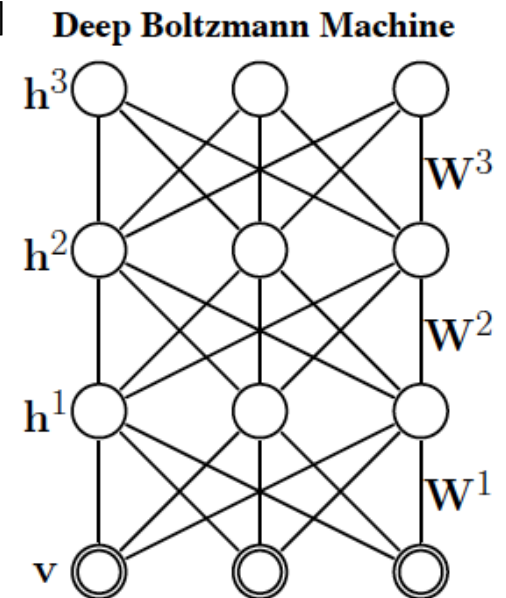


- Convolutional Sparse Coding

- Zeiler, Krishnan, Taylor & Fergus [CVPR '10]
- Kavukcuoglu, Sermanet, Boureau, Gregor, Mathieu & LeCun [NIPS '10]
- Chen, Spario, Dunson & Carin [JMLR submitted]
- Only 2 layer models

- Reconstruct all the way down to input

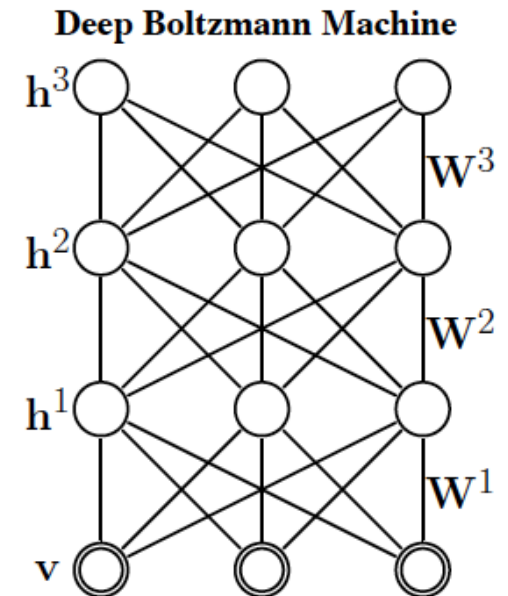
- Deep Boltzmann Machines
 - Salakhutdinov & Hinton [AISTATS'09]
- Deep Energy Models
 - Ngiam et al. [ICML'11]



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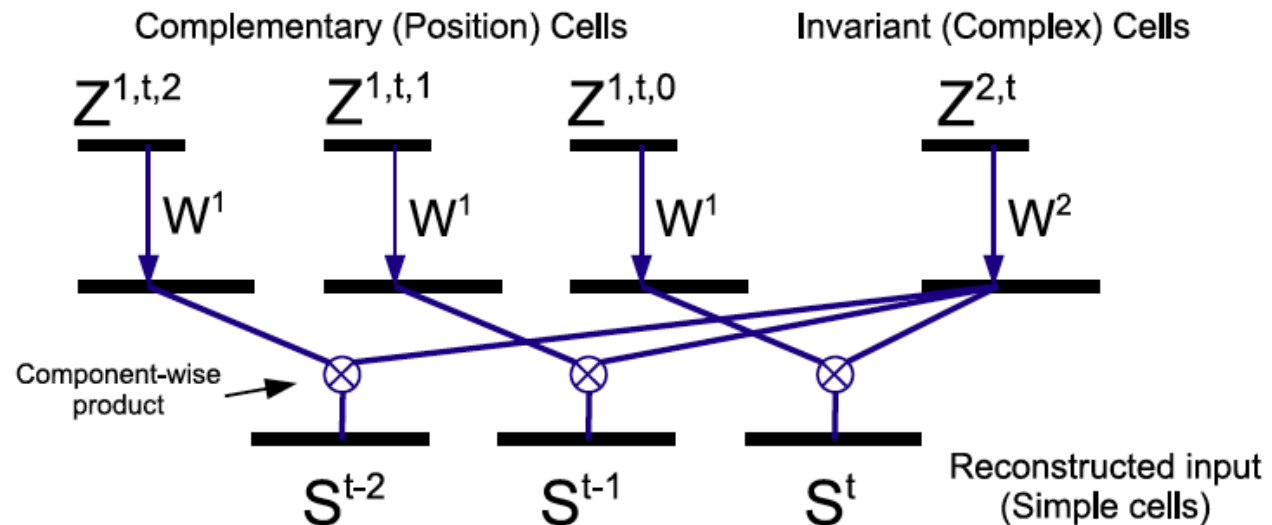
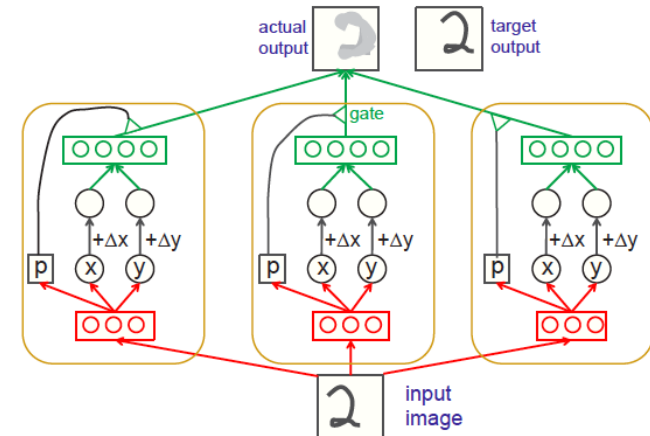
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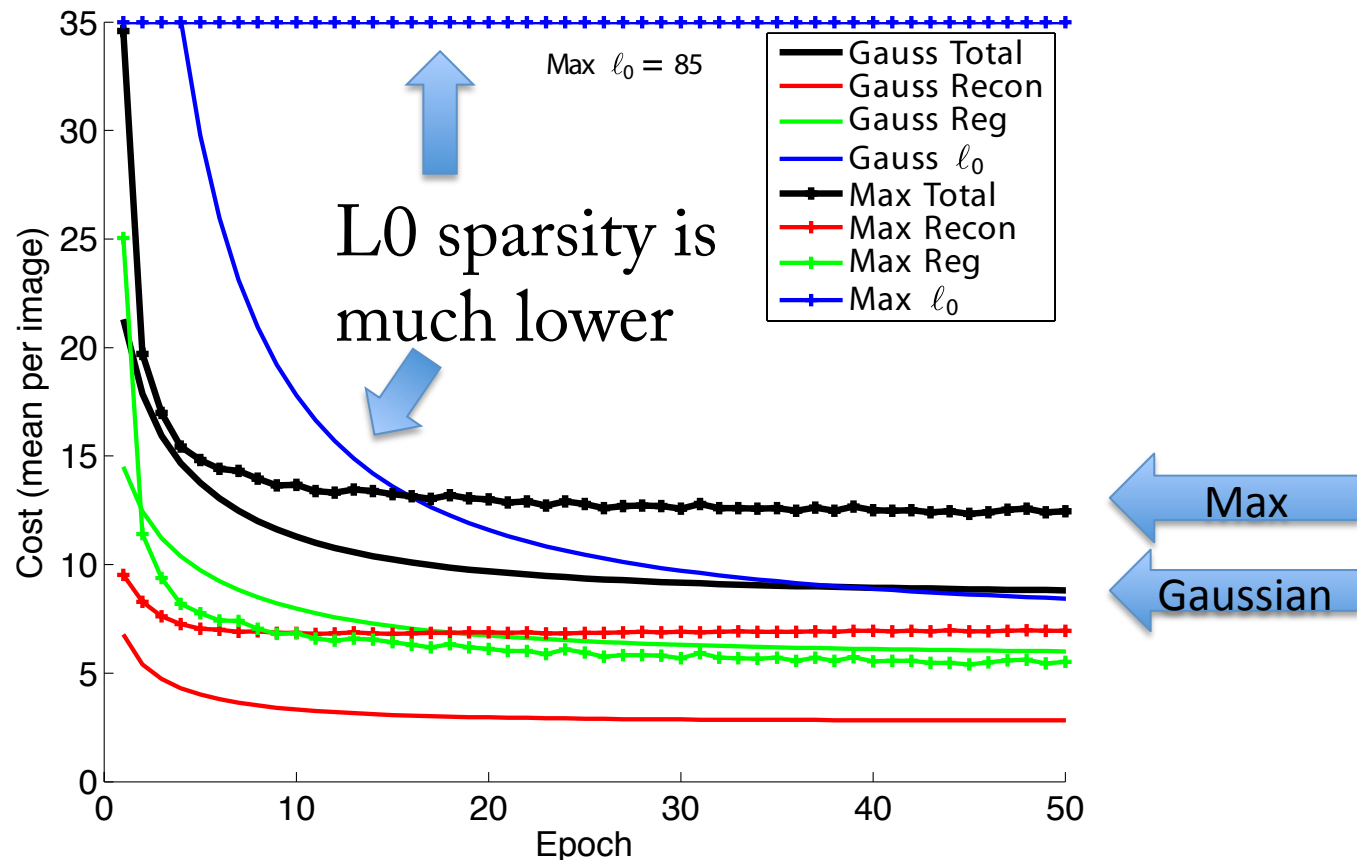
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MNIST Experiments

- 2 layers:
 - Layer 1: 16 filters (5x5 pixels)
 - Layer 2: 48 filters (5x5 pixels)
 - 2x2 (Un)pooling at each layer
- 50 inference iterations per image
 - 100 frames/sec on GPU
- Unsupervised training
 - No fine tuning
- Classification: patchify feature maps → linear SVM

Gaussian vs Max Pooling

- Compare objective cost to conventional max pooling



Classification:

	Layer 1	Layer 2
Max Pooling	1.30%	1.25%
Gaussian Pooling	1.38%	0.84%

Joint vs Separate Inference

Separate inference (2 phases):

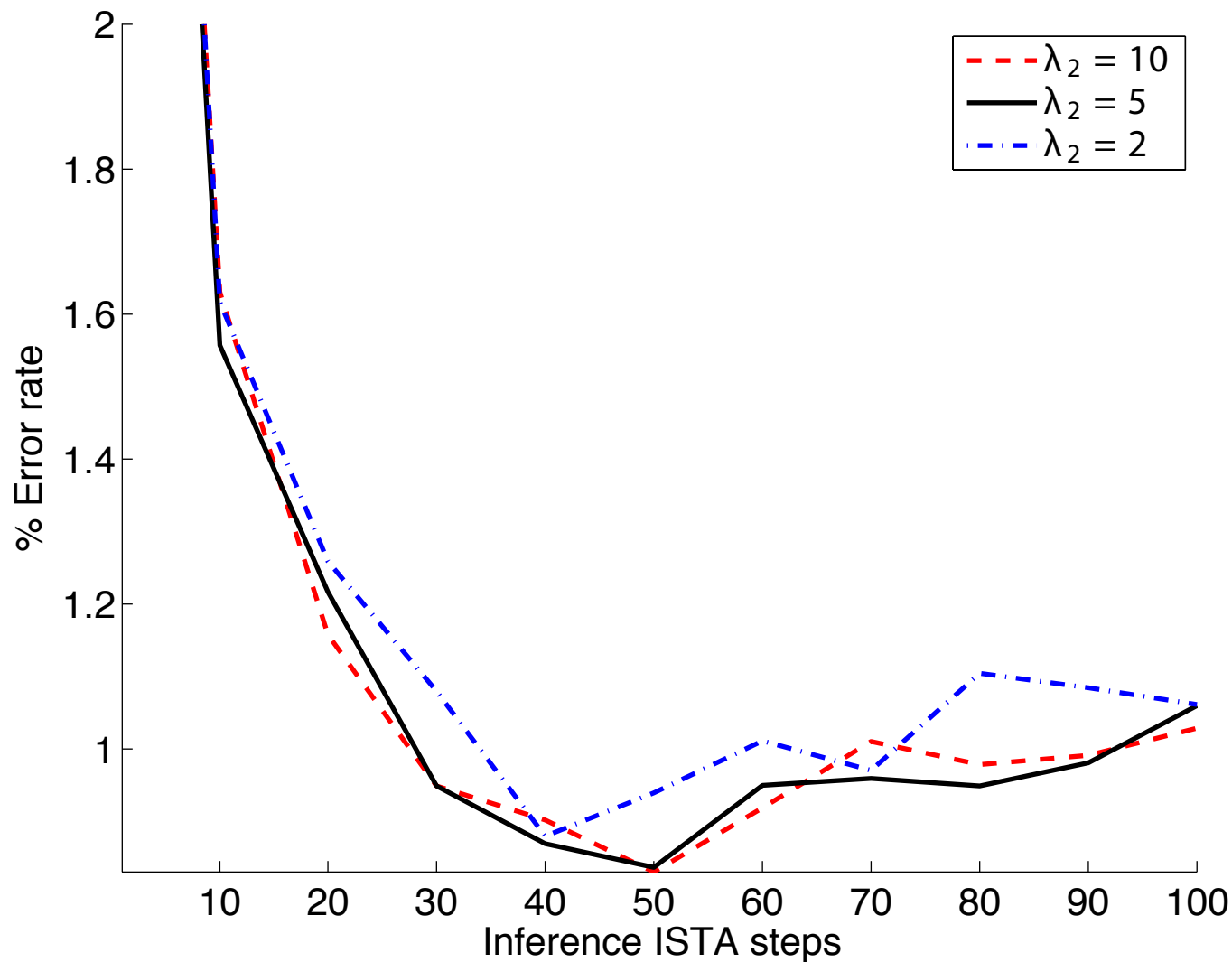
- (i): Layer 1 infer (θ_1, p_1) then fix θ_1 1.39% error
- (ii): Layer 2 infer (θ_2, p_2)

Joint Inference (1 phase):

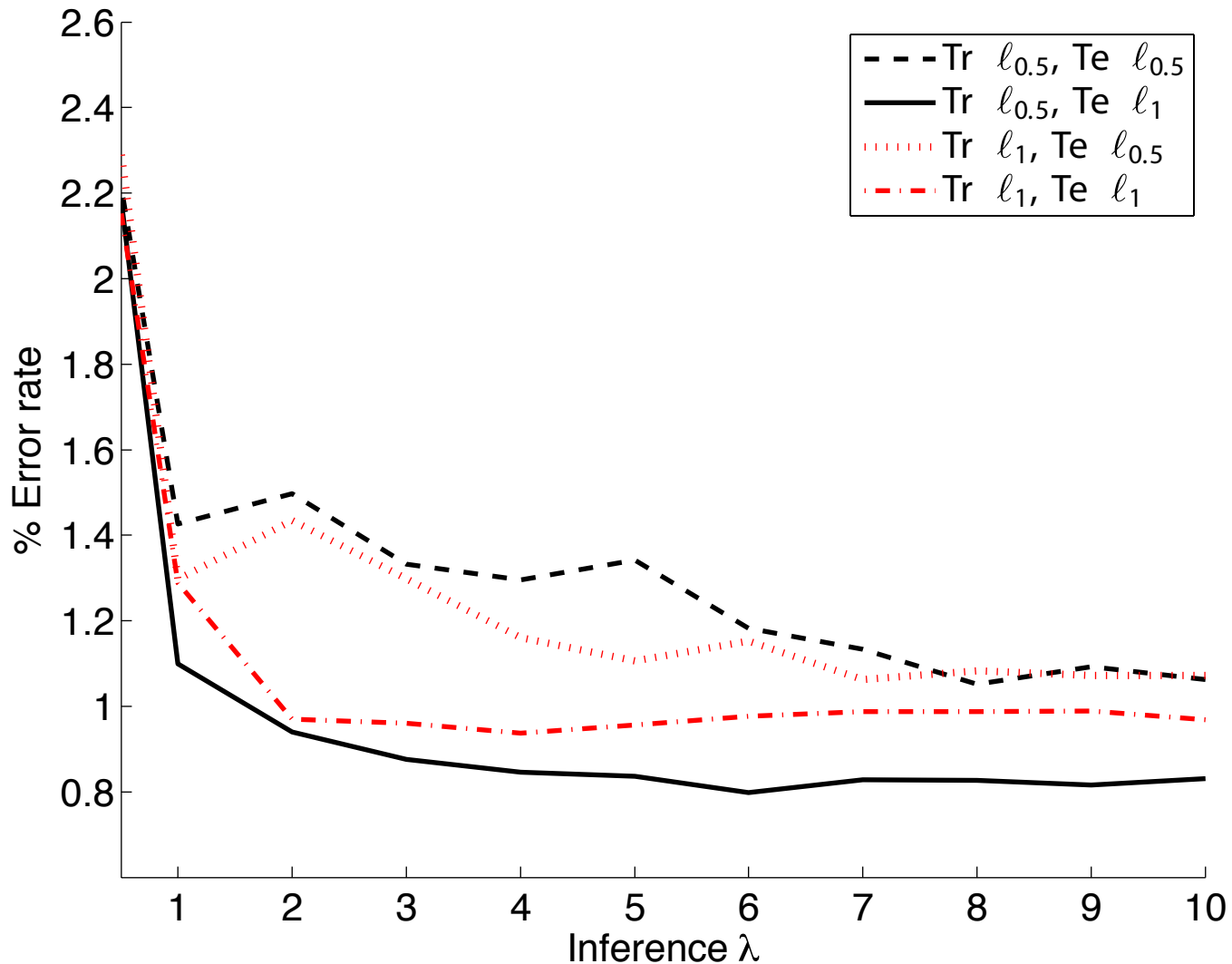
- (i): Layer 1 & 2 infer (θ_1, θ_2, p_2) 0.84% error

Using top-down information to set
lower pooling variables: 40% reduction in error

Number of ISTA Iterations (Test)



L0.5 vs L1 Sparsity in Train/Test



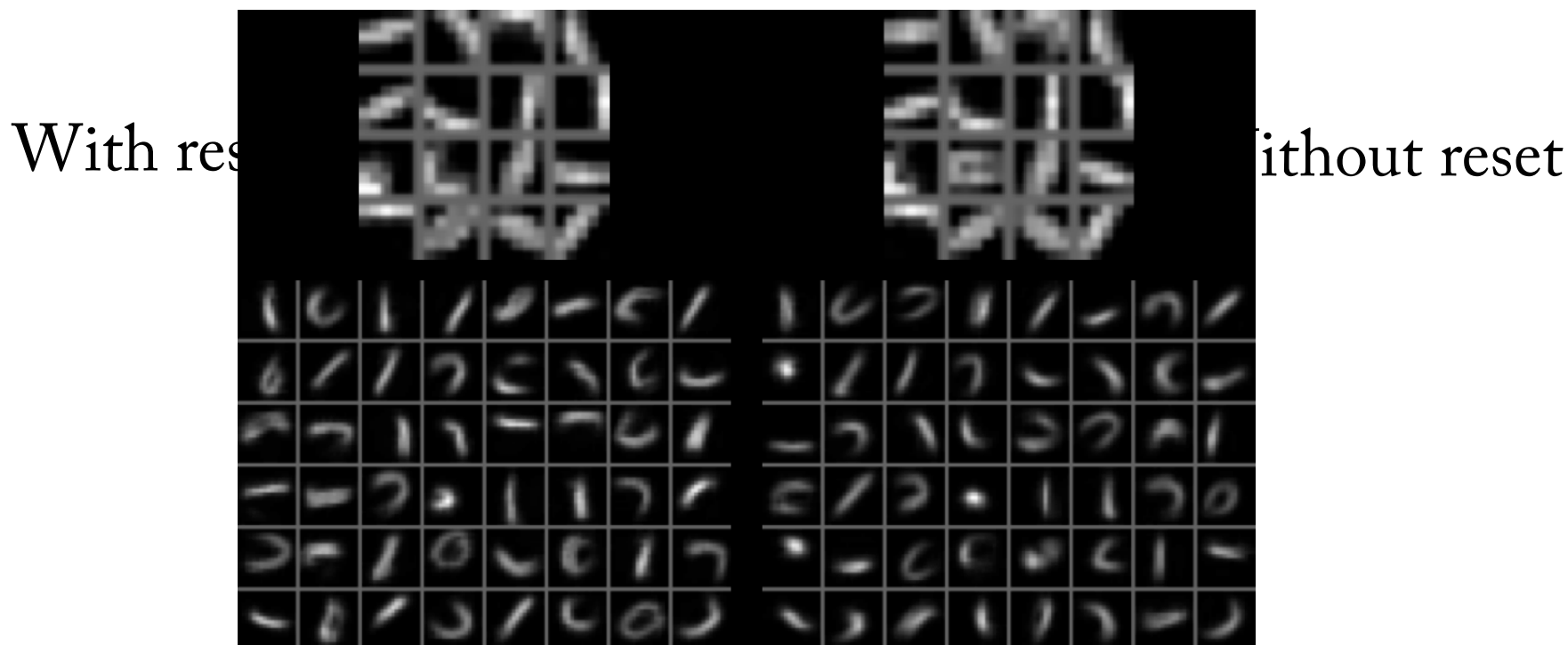
Non-Negativity Results

	Positive/Negative	Non-negative
Max Pooling	2.04%	1.25%
Gaussian Pooling	2.32%	0.84%

Table 3. MNIST error rate for Max and Gaussian models trained with and without the non-negativity constraint.

Resetting Trick

- Periodically set feature maps to zero during training



Trained with No Reset	Trained with Reset
1.00%	0.84%

Table 4. MNIST error rates for 2 layer models trained with and without resetting the feature maps.

MNIST Results Comparison

.....

	Pre-training	Fine-tuning
Our Method	0.84%	-
Convolutional RBM [Lee et al. ICML'09]	0.82%	-
Deep Belief Net [Hinton et al. 2006]	2.5%	1.18%
Deep Boltzmann Machine [S & H AISTATS'09]	-	0.95%

Caltech 101 Experiments

- Experiment using older model (from Zeiler et al. ICCV'11) using Max pooling NOT Gaussian pooling
- Unsupervised training on 3060 images from Caltech 101
- Resized/padded to 150x150 gray-scale
- Subtractive & divisive contrast normalization

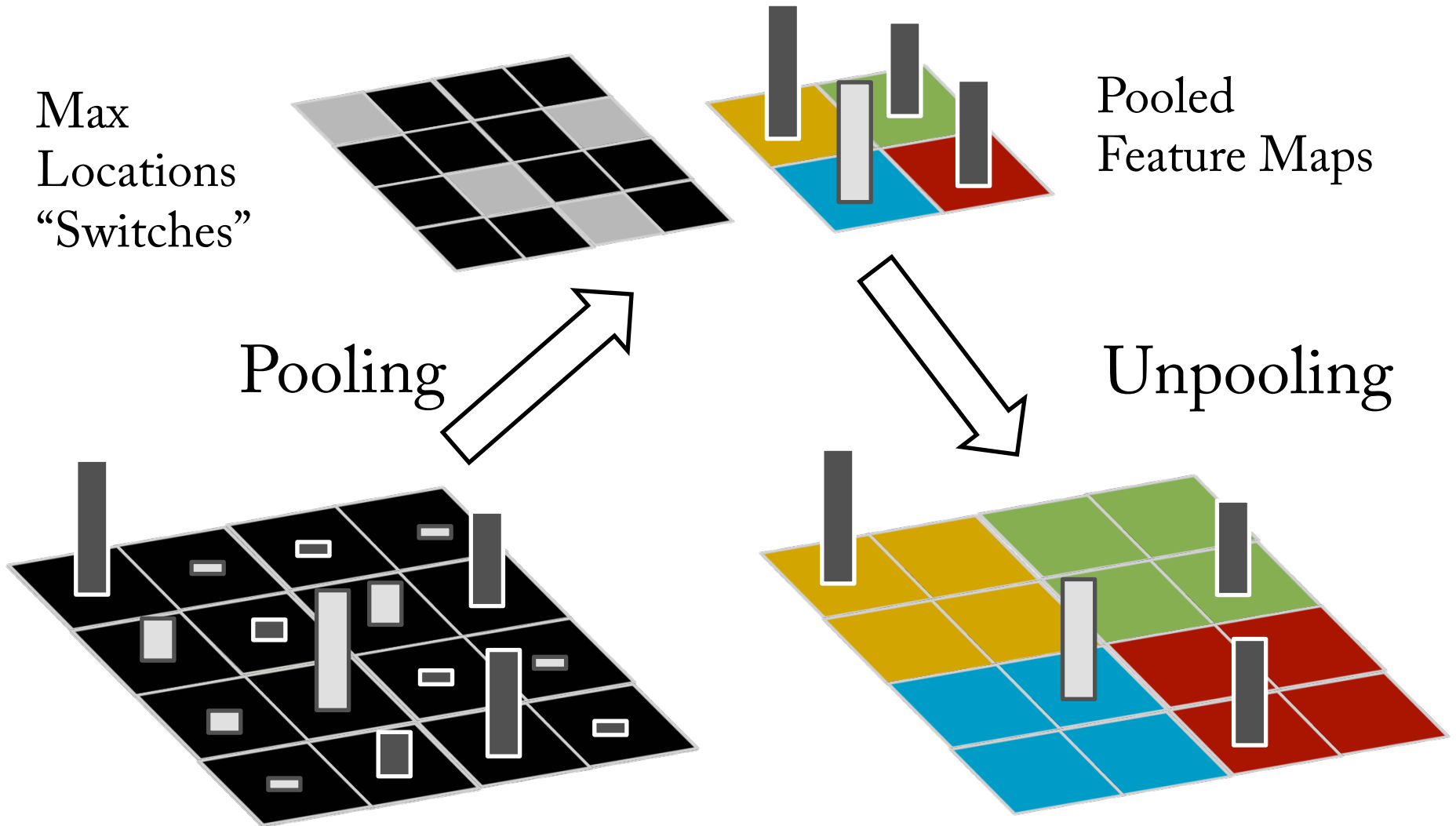
Reversible Max Pooling

Max
Locations
“Switches”

Pooling

Pooled
Feature Maps

Unpooling



Model Parameters/Statistics

Property	Layer 1	Layer 2	Layer 3	Layer 4
# Feature maps K_l	15	50	100	150
Pooling size	3x3x3	3x3x2	3x3x2	3x3x2
λ_l	2	0.1	0.005	0.001

- 7x7 filters at all layers

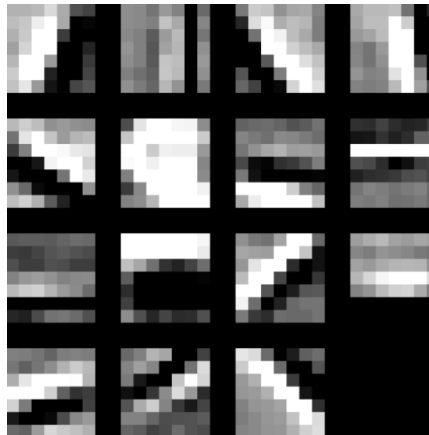
Model Reconstructions

Input



Layer 1 Filters

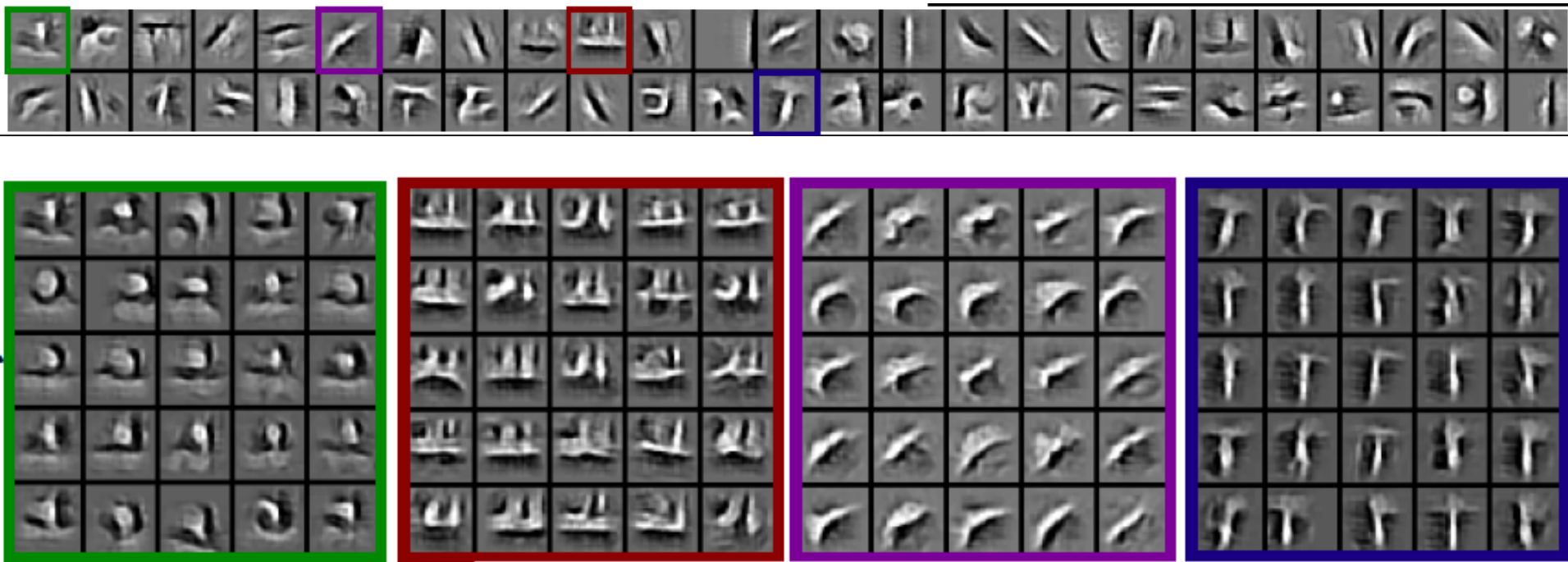
- 15 filters/feature maps



Layer 2 Filters

.....

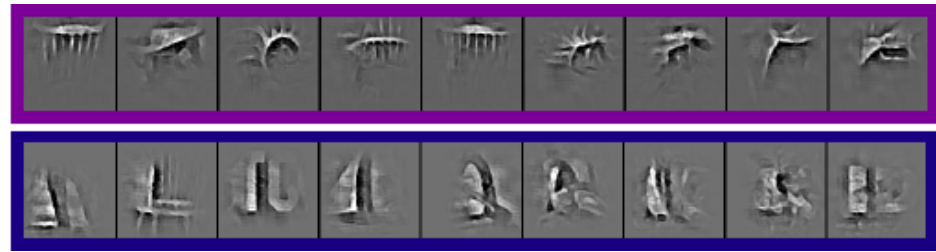
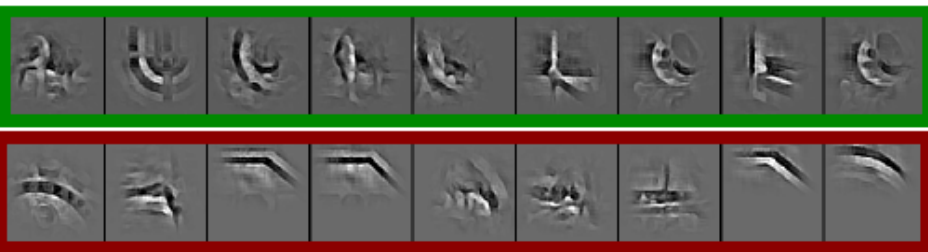
- 50 filters/feature maps, showing max for each map projected down to image



Layer 3 filters

.....

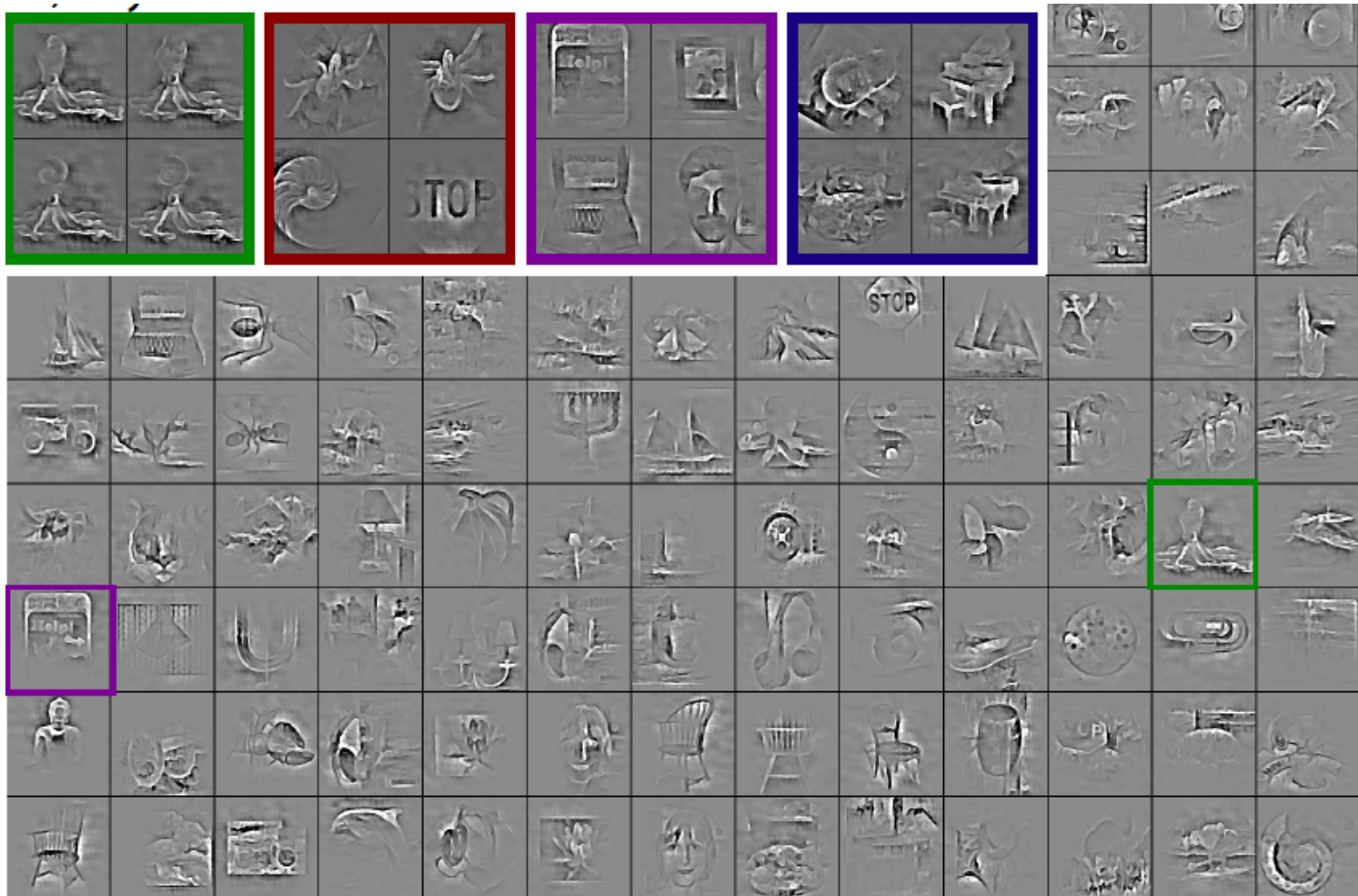
- 100 filters/feature maps, showing max for each map



Layer 4 filters

.....

- 150 in total; receptive field is entire image



Largest 5 activations at top layer

.....

Max 1

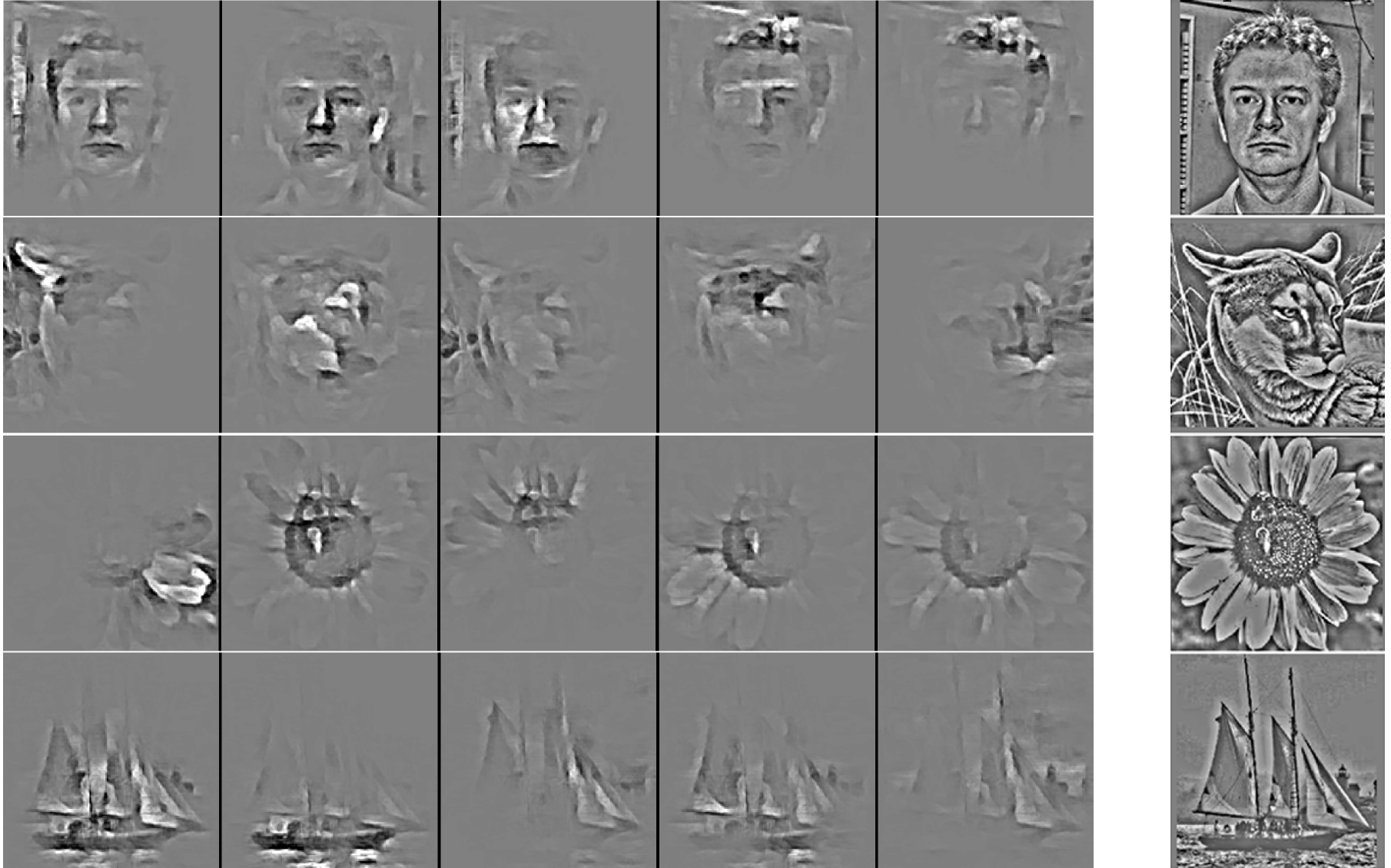
Max 2

Max 3

Max 4

Max 5

Input Image



Classification Results: Caltech 101

.....

- Use features as input to Spatial Pyramid Matching (SPM) of Lazebnik et al. [CVPR'06]

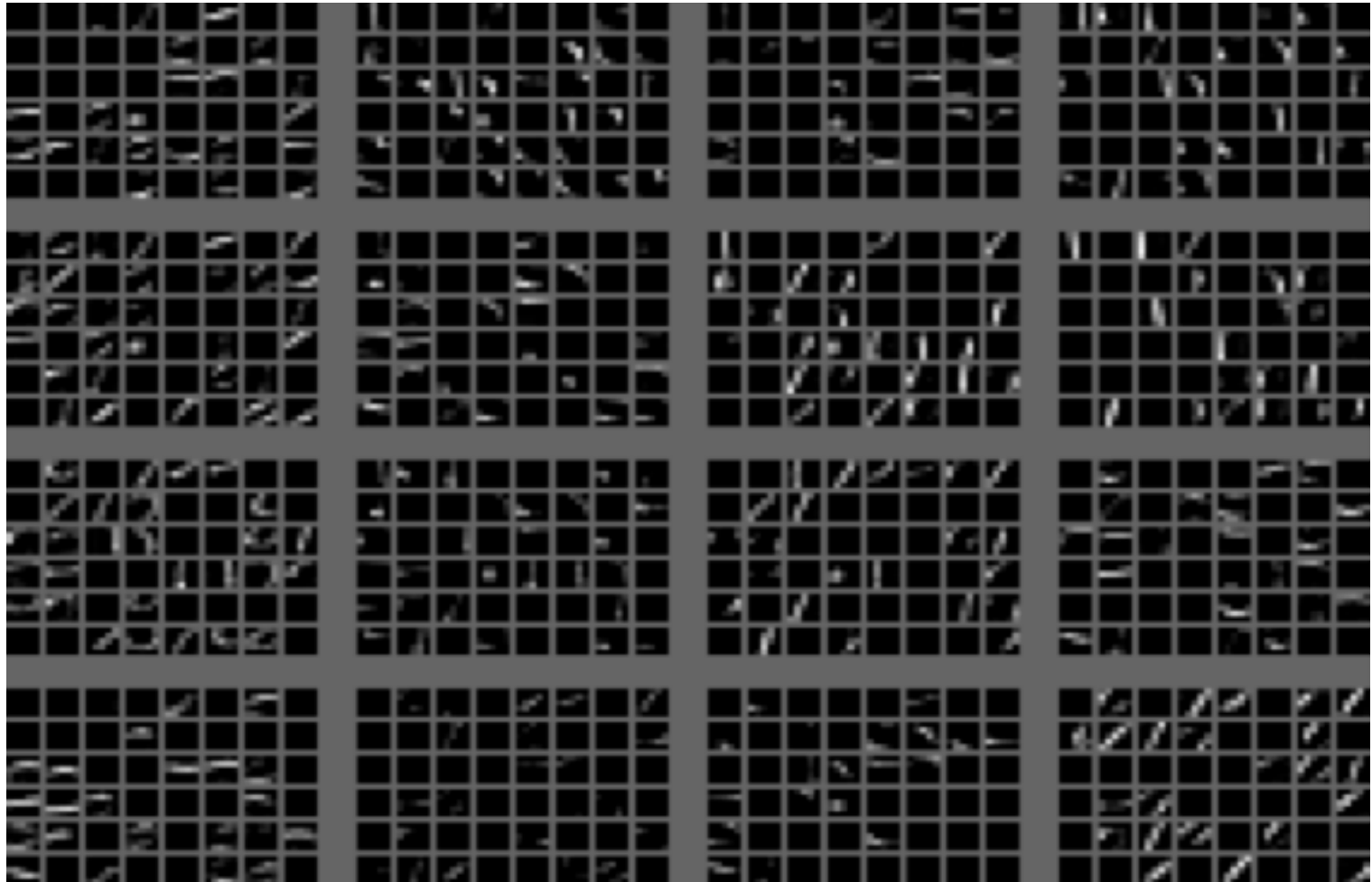
Our model - layer 1	$67.8 \pm 1.2\%$	
Chen <i>et al.</i> [3] layer-1+2 (ConvFA)	$65.7 \pm 0.7\%$	Convolutional Sparse Coding
Kavukcuoglu <i>et al.</i> [8] (ConvSC)	$65.7 \pm 0.7\%$	
Zeiler <i>et al.</i> [20] layer-1+2 (DN)	$66.9 \pm 1.1\%$	
Boureau <i>et al.</i> [2] (Macrofeatures)	$70.9 \pm 1.0\%$	Other approaches using SPM with Hard quantization
Jarrett <i>et al.</i> [7] (PSD)	$65.6 \pm 1.0\%$	
Lazebnik <i>et al.</i> [9] (SPM)	$64.6 \pm 0.7\%$	
Lee <i>et al.</i> [11] layer-1+2 (CDBN)	$65.4 \pm 0.5\%$	

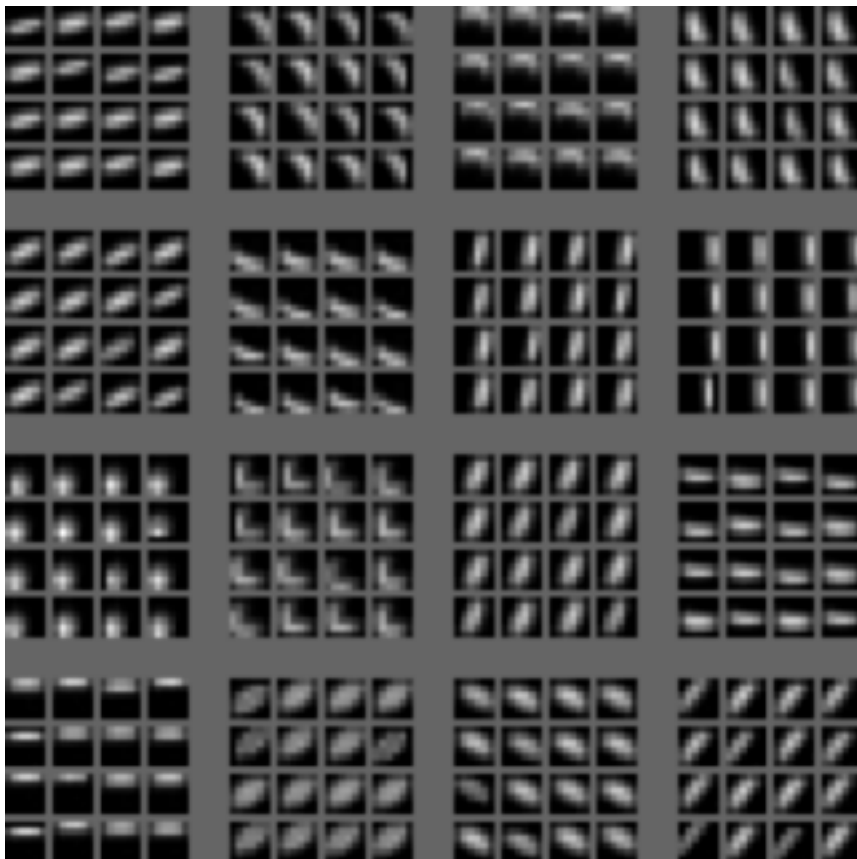
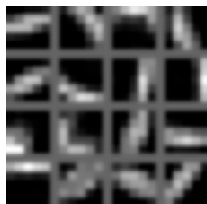
But some way below SOA for single feature ($\sim 78\%$)

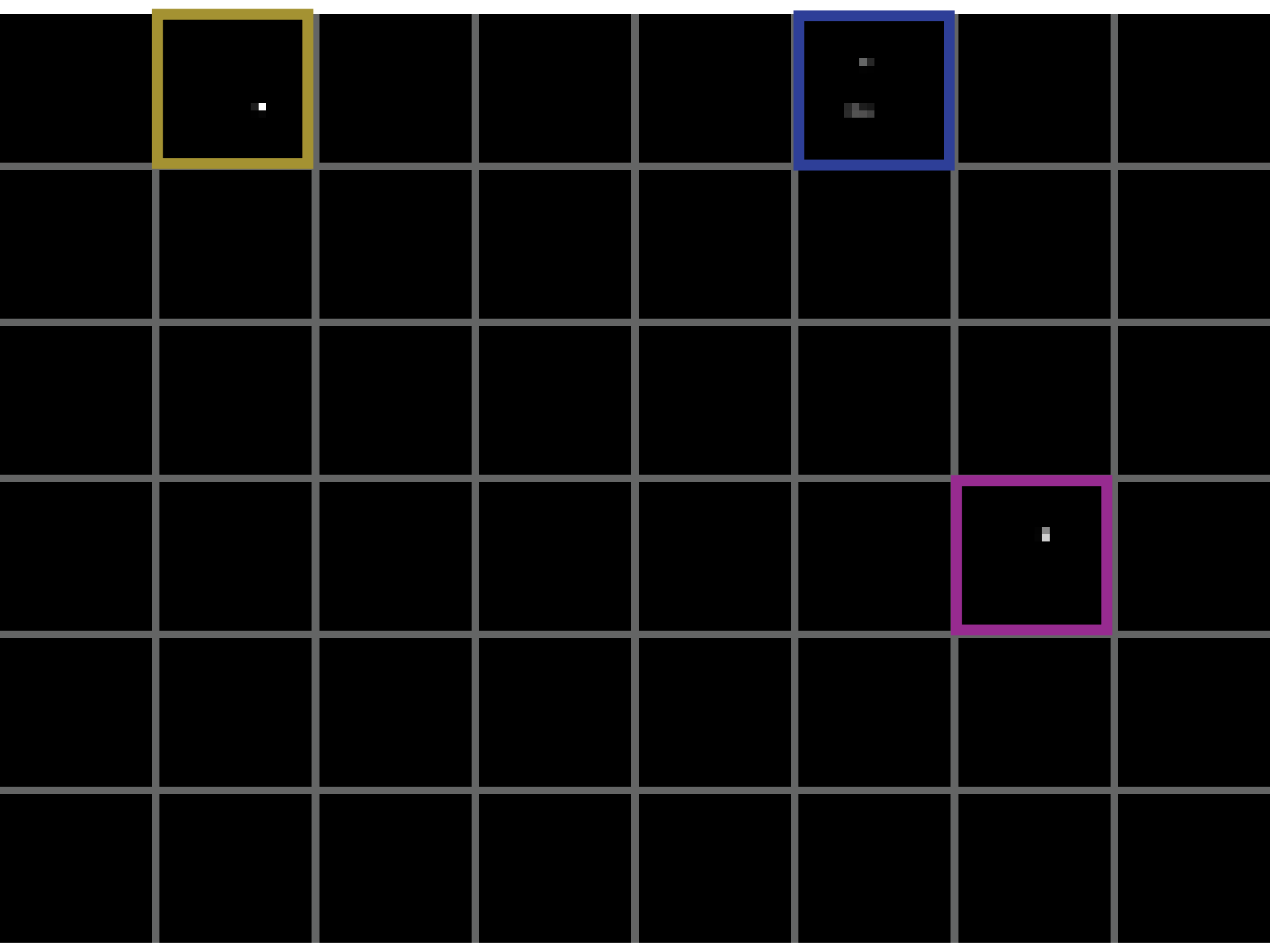
Summary

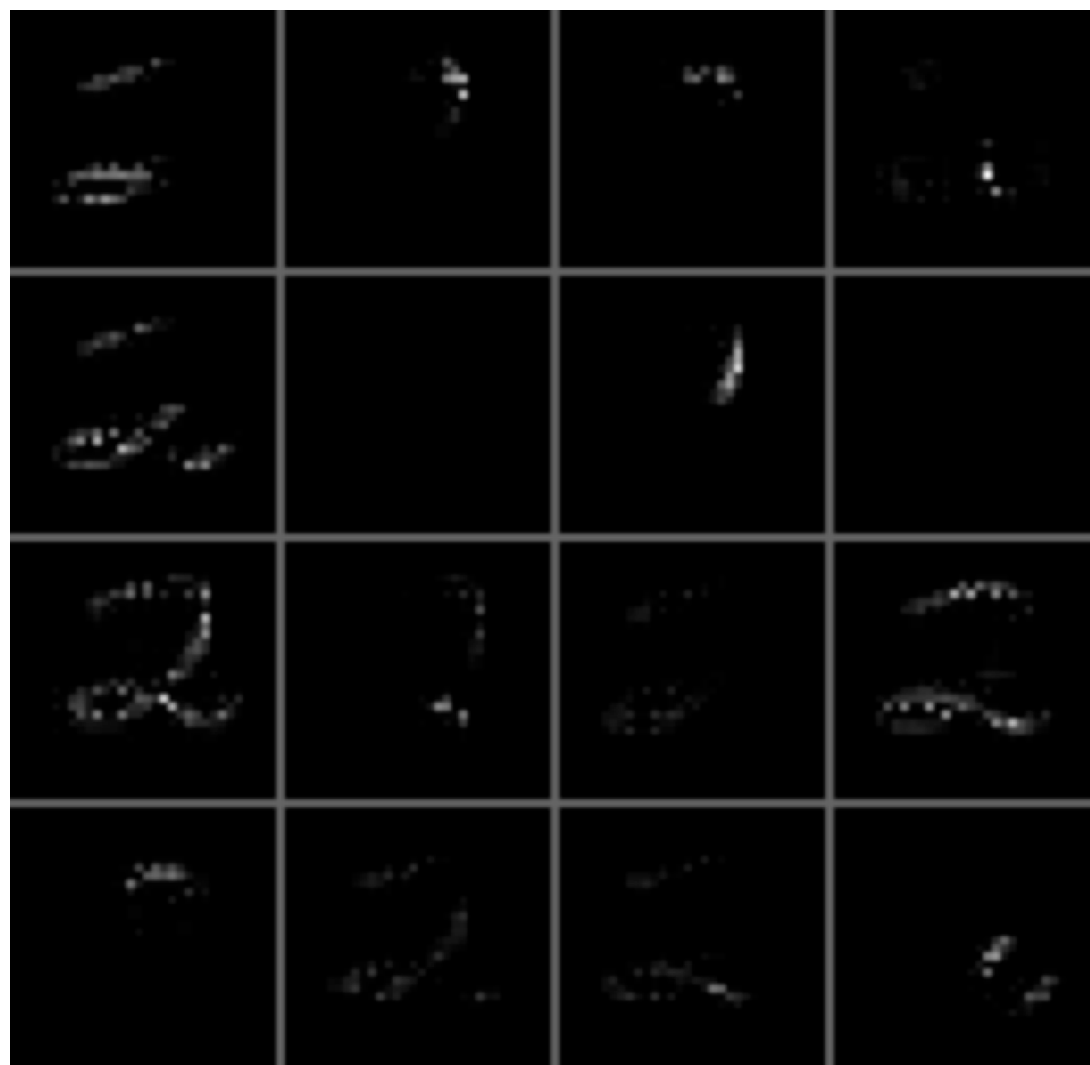
- Variant of sparse coding with novel Gaussian pooling
- Integrating pooling into cost function gives better & sparser features
- Joint inference: top-down influence on lower levels helps performance
- Code & papers on Matt Zeiler's webpage
 - <http://www.matthewzeiler.com/pubs/arxiv2012/arxiv2012.pdf>

Layer 2 Filter Coefficients

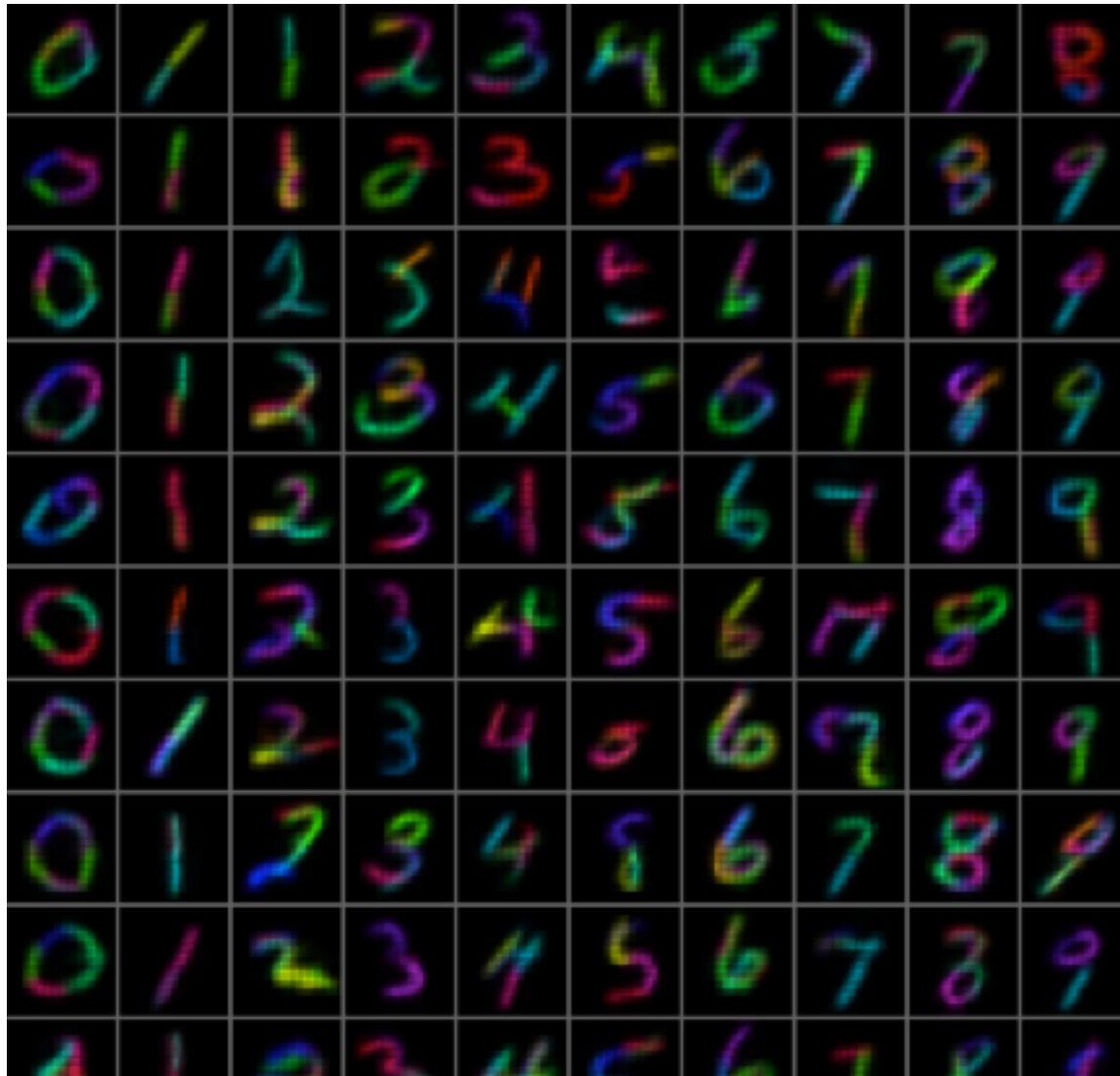








Max Pooling Projections (Aliasing)

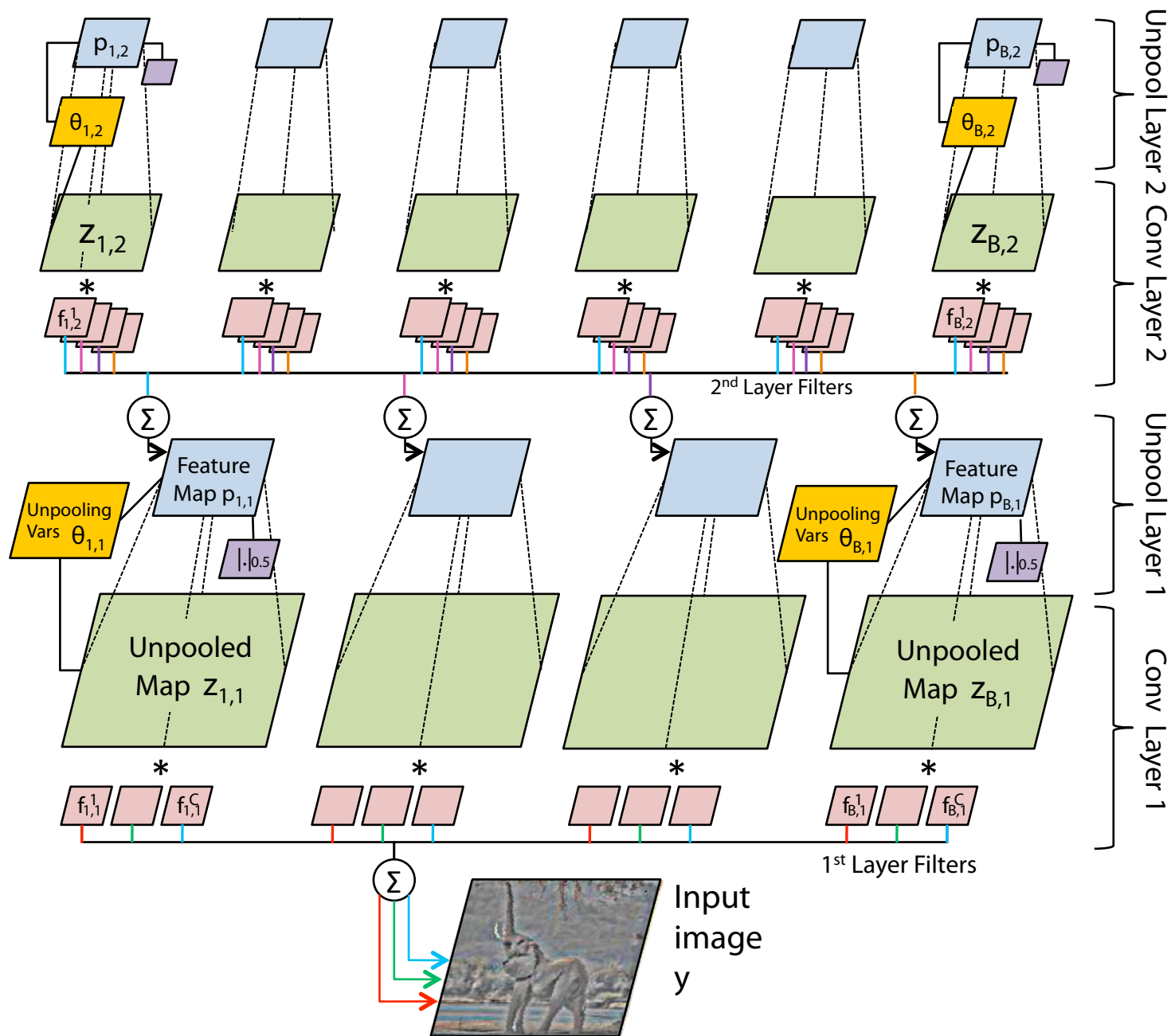


Joint vs Separate Inference

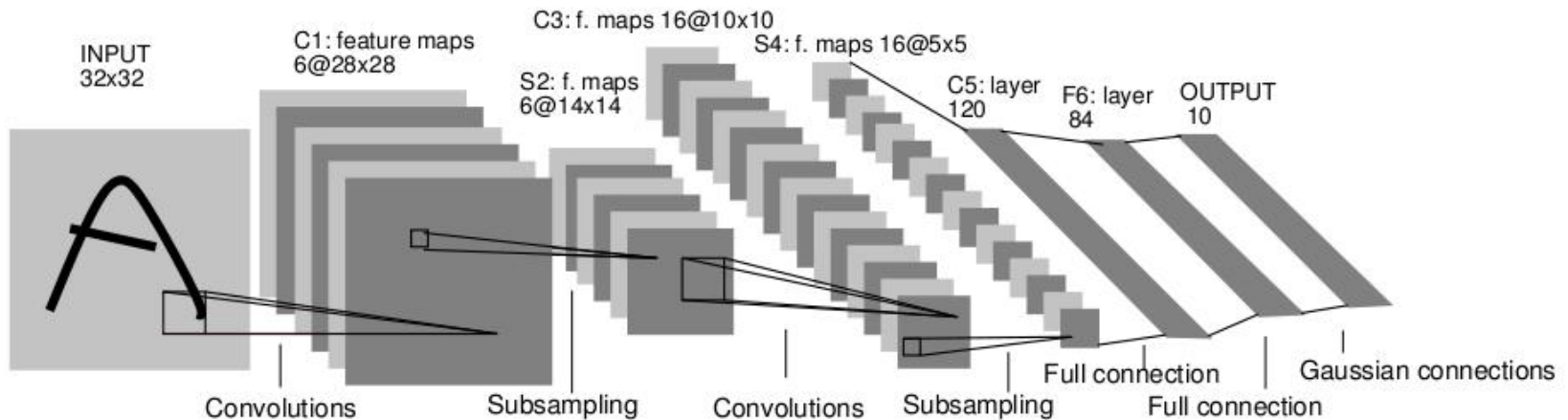
.....

Training	Infer 2 phases	Infer 1 phase (no U_1)	Infer 1 phase
Updating F_1 U_{w_1}	1.79%	1.63%	1.40%
Updating F_1	1.71%	1.21%	1.10%
Updating U_{w_1}	1.39%	1.04%	0.84%
No Layer 1 Updates	1.46%	0.99%	1.03%

Table 2. Comparison of joint training techniques. Each row is a trained two layer model that updates select variables in layer 1 during training (in addition to F_2 and U_{w_2}). The three columns use these models but run inference at test time in 2 phases, 1 phase without updating U_1 , and 1 phase with all updates respectively.



Comparison: Convolutional Nets



LeCun *et al.* 1989

Convolutional Networks

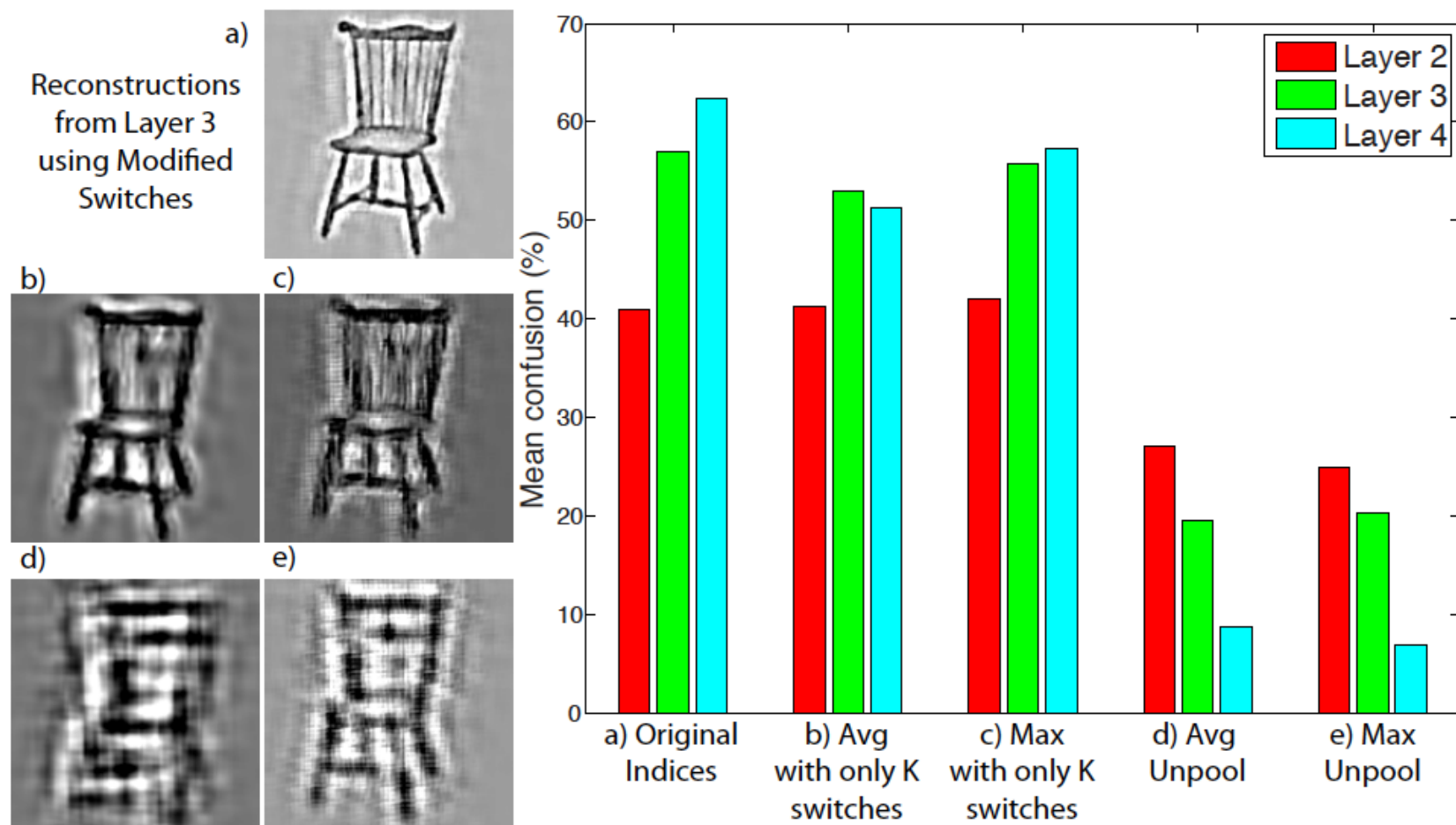
- Bottom-up filtering with convolutions in image space.
- Trained supervised requiring labeled data.

Deconvolutional Networks

- Top-down decomposition with convolutions in feature space.
- Non-trivial unsupervised optimization procedure involving sparsity.

Analysis of Switch Settings

- Recons. and classification with various unpooling.



Related Work

- Convolutional Sparse Coding
 - Zeiler, Krishnan, Taylor & Fergus [CVPR '10]
 - Kavukcuoglu, Sermanet, Boureau, Gregor, Mathieu & LeCun [NIPS '10]
 - Chen, Spario, Dunson & Carin [JMLR submitted]
 - Only 2 layer models
- Deep Learning
 - Hinton & Salakhutdinov [Science '06]
 - Ranzato, Poultney, Chopra & LeCun [NIPS '06]
 - Bengio, Lamblin, Popovici & Larochelle [NIPS '05]
 - Vincent, Larochelle, Bengio & Manzagol [ICML '08]
 - Lee, Grosse, Ranganth & Ng [ICML '09]
 - Jarrett, Kavukcuoglu, Ranzato & LeCun [ICCV '09]
 - Ranzato, Mnih, Hinton [CVPR'11]
 - Reconstruct layer below, not input
- Deep Boltzmann Machines
 - Salakhutdinov & Hinton [AISTATS '09]

Related Work

- Hierarchical vision models
 - Zhu & Mumford [F&T '06]
 - Tu & Zhu [IJCV '06]
 - Serre, Wolf & Poggio [CVPR '05]

