

An optimal trading problem in intraday electricity markets

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René Aïd Pierre Gruet Huyên Pham
EDF R&D - Finance for Energy Market Research Centre
LPMA, University Paris Diderot



Agenda

- 1 Trading in the intraday market
 - Intraday market
 - A problem of optimal trading
- 2 Optimal trading model
 - No jumps, no delay
 - Jumps in the residual demand forecast
 - Delay in generation
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Disclaimer

Disclaimer

Any views or opinions presented in this presentation are solely those of the author and do not necessarily represent those of the EDF group.

Trading in the intraday market

A bit of context

Development of renewable energy in continental Europe

- windfarm: Germany 31 GW of 177 GW total installed capacity, Spain 22 GW of 105 GW
- solar power: Germany 32 GW, Italy 16 GW of 124 GW of installed capacity.
- source: Department Of Energy, Energy Information Agency

Effects on generation management and trading

- Increasing forecasting error on short time horizon
- root mean square error (RMSE) of the error forecast for the production of a wind farm in six hours can reach 20% of its installed capacity (Giebel et al. (2011))
- Producers / retailers endure imbalance costs. Imbalance: difference between generation (plus purchases) and consumption (plus sales).
- They are penalised for their imbalances because the TSO has to buy energy from someone else to insure the equilibrium of the system.
- Increasing need for producers to find ways to balance their short-term position.
- Development of intraday electricity market

Intraday market

Intraday market

- Operated by a market operator
- Market for next hours where firms
 - exchange power to balance their position
 - minimize the cost of their imbalances
- Exchanged volume in EpeX intraday market in Germany has grown from 2 TWh (2008) to 25 TWh (2013).

EPEX Intraday market

- Continuous trading
- Opens at 15:00 the day before.
- Possibility to buy/sell physical delivery contracts for the 24 periods 0:00 – 1:00, ..., 23:00 – 24:00.
- Closes 45 minutes before beginning of delivery.

Example of the quotation of a given hour of delivery

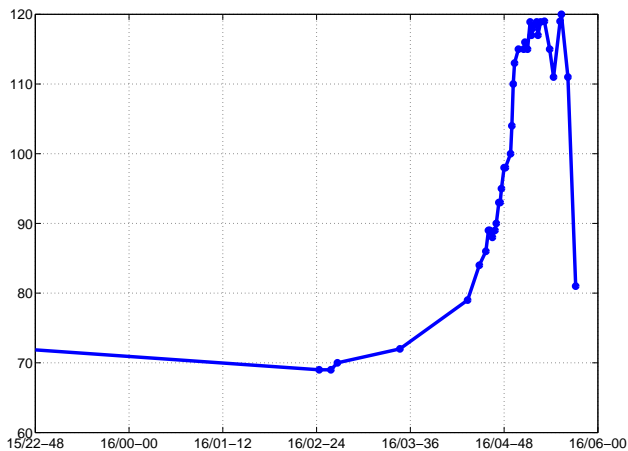


Figure: Epex intraday Germany market december 16th 2010, 7 a.m.

Relation between intraday and dayahead prices

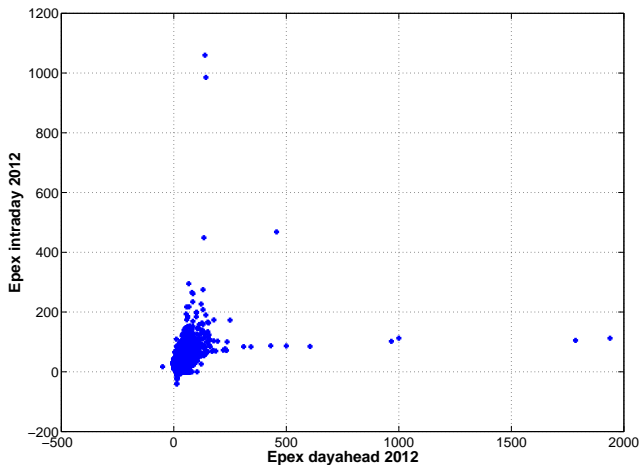


Figure: Epex intraday and dayahead hourly prices during 2012.

Liquidity and players

EpexSpot - for a given hour (2014)

- Total exchanged volumes can reach 3.000 MW
- Average buy/sell volume \approx 350 MW
- Exchanges are cut in orders \approx 20 MW

EpexSpot - members (2014)

- \approx 100 actors on the French intraday market
- \approx 240 actors on the all Epex intraday markets (France, Germany, Austria, Switzerland)
- Power utilities (EDF, E.On, Enel...), oil companies (BP), agregators (Voltalis), banks and financial institutions (Morgan Stanley, JP Morgan, CitiGroup, Barklays, Merrill Lynch Commodities Ltd...)

Problem

Settings

- Demand and renewable production forecasts are frequently updated (every 2 hours for demand, every 4 hours for wind production)
- Shocks in forecast happens.
- Short-term generation management involves many complex constraints of power plants and many different technology costs.
- Mainly, it takes time to mobilize generation.

Questions

- Knowing that the objectif of a power producer is to minimize the total cost of production and trading, what can be the optimal trading strategy?
- Knowing that shocks may happen, should traders take anticipated precautionary positions?
- Dilemma between waiting for a possible better price and closing immediatly an imbalanced position.

Previous works

References

- Henriot (2014): discrete time model with wind production error forecast as only source of randomness
- Garnier and Madlener (2014): continuous time model analysing the trade-off between entering into a deal right now and waiting for a better quote. Wind follows a arithmetic Brownian motion and intraday prices a geometric Brownian motion.

This talk

Analysis of the problem with a stylised model simplifying the generation side and yet preserving the main feature of the dilemma, **the information structure**

- The producer minimises the expected total cost of production using
 - Thermal plants (oil, gas, nuclear): can be dispatched with anticipation (delay)
- + trading costs
- + Penalization of the imbalance with residual demand.
- Model inspired by Almgren-Chriss (2000) optimal execution model with market impact
- Here, random target, as we only have a forecast of final **residual demand**
- **Residual demand**: total final demand minus renewable energy production.

Optimal trading model

Trading

- X_t : net sale/buy position (inventory) on the intraday market with trading rate control $q_t = \dot{X}_t$

$$X_t = X_0 + \int_0^t q_s ds,$$

- Transactions occur at price

$$P_t(\mathbf{q}) = \underbrace{\hat{P}_t + \int_0^t \nu q_s ds}_{Y_t := \text{observable quoted price}} + \gamma q_t,$$

- \hat{P}_t : unaffected price on $(\Omega, \mathcal{F}, (\mathcal{F}_t)_t, \mathbb{P})$
- ν permanent impact factor, γ : instantaneous impact factor.

Demand, generation and penalization

- D_T residual demand at time T . Continuously updated forecast $(D_t)_{0 \leq t \leq T}$.
- Thermal production ξ is chosen at time $T - h$. Length h is the **delay in production**.
- cost function $c(\xi) = \frac{\beta}{2}\xi^2$, $\beta > 0$.

Objective function of the agent

Minimize over trading rates $\mathbf{q} \in \mathcal{A}$: \mathbb{F} -adapted and generation $\xi \in L_+^0(\mathcal{F}_{T-h})$

$$\mathbf{E} \left(\underbrace{\int_0^T q_s P_s(\mathbf{q}) ds}_{\text{trading cost}} + \underbrace{\frac{\beta}{2} \xi^2}_{\text{generation cost}} + \underbrace{\frac{\eta}{2} (D_T - X_T - \xi)^2}_{\text{imbalance penalization}} \right)$$

where

- $C(D_T - X_T, \xi) := \frac{\beta}{2} \xi^2 + \frac{\eta}{2} (D_T - X_T - \xi)^2$ is the cost of holding X_T while the final demand is D_T and the production ξ has been chosen.

Case with no jumps and no delay

- We assume that thermal production can be decided instantaneously. The production decision has to be made at final time T .
- The unaffected price process is

$$\hat{P}_t = \hat{P}_0 + \sigma_0 W_t, \text{ thus } dY_t = \nu q_t dt + \sigma_0 dW_t,$$

- the residual demand forecast has dynamics

$$dD_t = \mu dt + \sigma_d dB_t,$$

with $\mu \in \mathbf{R}$, $\sigma_0 > 0$, $\sigma_d > 0$ and $d < W, B \rangle_t = \rho dt$, $\rho \in [-1, 1]$.

Dynamical formulation

Value function:

$$v(t, x, y, d) = \inf_{\substack{\mathbf{q} \in \mathcal{A}_t \\ \xi \in L_+^0(\mathcal{F}_T)}} J(t, x, y, d; \mathbf{q}, \xi)$$

where

$$J(t, x, y, d; \mathbf{q}, \xi) = \mathbf{E} \left(\int_t^T q_s (Y_s^{t,y} + \gamma q_s) ds + C(D_T^{t,d} - X_T^{t,x}, \xi) \right),$$

\mathcal{A}_t being the set of adapted processes \mathbf{q} such that $\mathbf{E} \left(\int_t^T q_s^2 ds \right) < +\infty$.

Note: The production quantity ξ is chosen at time T , after the choice of the whole trajectory \mathbf{q} .

Solving the problem

$$v(t, x, y, d) = \inf_{\mathbf{q} \in \mathcal{A}_t} \mathbf{E} \left(\int_t^T q_s (Y_s^{t,y} + \gamma q_s) ds + \inf_{\xi \in L_+^0(\mathcal{F}_T)} C(D_T^{t,d} - X_T^{t,x}, \xi) \right)$$

Optimal generation:

$$\begin{aligned} \xi_T^* &= \frac{\eta}{\eta + \beta} (D_T^{t,d} - X_T^{t,x}) \mathbf{1}_{D_T^{t,d} - X_T^{t,x} \geq 0} \\ &=: \hat{\xi}^+(D_T^{t,d} - X_T^{t,x}) \end{aligned}$$

Thus:

$$\begin{aligned} v(t, x, y, d) &= \inf_{\mathbf{q} \in \mathcal{A}_t} \mathbf{E} \left(\int_t^T q_s (Y_s^{t,y} + \gamma q_s) ds + \frac{\beta}{2} \hat{\xi}^+(D_T^{t,d} - X_T^{t,x})^2 \right. \\ &\quad \left. + \frac{\eta}{2} (D_T^{t,d} - X_T^{t,x} - \hat{\xi}^+(D_T^{t,d} - X_T^{t,x}))^2 \right) \end{aligned}$$

We do not expect to get an explicit formula, due to the indicator function.

Auxiliary relaxed problem

Relax the positivity constraint on the production ξ :

$$\tilde{v}(t, x, y, d) = \inf_{\substack{\mathbf{q} \in \mathcal{A}_t \\ \xi \in L^0(\mathcal{F}_T)}} J(t, x, y, d; \mathbf{q}, \xi).$$

Optimal generation level:

$$\hat{\xi}(D_T^{t,d} - X_T^{t,x}) = \frac{\eta}{\eta + \beta} (D_T^{t,d} - X_T^{t,x})$$

New value function expression:

$$\tilde{v}(t, x, y, d) = \inf_{\mathbf{q} \in \mathcal{A}_t} \mathbf{E} \left(\int_t^T q_s (Y_s^{t,y} + \gamma q_s) ds + \frac{1}{2} \frac{\eta \beta}{\eta + \beta} (D_T^{t,d} - X_T^{t,x})^2 \right).$$

Linear-quadratic problem. Value function is quadratic.

⇒ Straightforward but tedious computations.

Optimal strategy in the auxiliary problem

Optimal trading rate

$$\hat{q}_t = \frac{r(\eta, \beta)(D_t + \mu(T - t) - \hat{X}_t) - \hat{Y}_t}{(r(\eta, \beta) + \nu)(T - t) + 2\gamma}$$

where $r(\eta, \beta) := \frac{\eta\beta}{\eta+\beta}$ and \hat{X}_t, \hat{Y}_t designate the inventory and price trajectory with \hat{q}_t as a control.

Interpretation

- Define the forecast final production seen from time $t \leq s \leq T$:

$$\hat{\xi}_s = \frac{\eta}{\eta + \beta} (D_s + \mu(T - s) - \hat{q}_s(T - s) - \hat{X}_s)$$

- The optimal trading rate satisfies:

$$\hat{Y}_s + \nu \hat{q}_s(T - s) + 2\gamma \hat{q}_s = c'(\hat{\xi}_s).$$

- The optimal trading strategy consists in making the forecast marginal costs equal to the forecast price.
- Close to the operational strategy.

Interpretation

Consequence

- Suppose that at time 0, the intraday price is equal to the day-ahead spot price and the producer is balanced.
- Thus $\hat{Y}_0 = c'(D_0 + \mu T - \hat{X}_0)$
- Thus the initial trading rate is null \Rightarrow No anticipated precautionary position is needed.

A nice property of the optimal trading rate in the auxiliary problem

Property

The optimal trading rate is a martingale.

Proof

Itô's lemma applied to $\hat{q}_s = \hat{q}(T - s, D_s - \hat{X}_s, \hat{Y}_s)$ gives:

$$d\hat{q}_s = (D_2\hat{q})\sigma_d dB_s + (D_3\hat{q})\sigma_0 dW_s.$$

Consequence

- The expected inventory is thus a linear function of time: $\mathbf{E}(\hat{X}_s) = X_0 + \hat{q}_0 s$.
- Constant trading rate in Almgren and Chriss (2000).
- Previous “forecasts keeping the same control” are thus pertinent.

Quality of the approximation of the original problem

- The production ξ has to be positive.
- Suggested strategy:
 - 1 First follow strategy $(\hat{q}_s)_{t \leq s \leq T}$ of the auxiliary problem.
 - 2 Then choose production level $\hat{\xi}^+ (= \hat{\xi} \mathbf{1}_{\hat{\xi} \geq 0})$.
- Denote

$$\mathcal{E}_1(t, x, y, d) = J(t, x, y, d; \hat{\mathbf{q}}, \hat{\xi}^+) - v(t, x, y, d),$$

$$\mathcal{E}_2(t, x, y, d) = v(t, x, y, d) - \tilde{v}(t, x, y, d).$$

- Bounds of \mathcal{E}_i show very low error.

Incorporation of jumps on demand

- Add a compound Poisson process $(N_t^+, N_t^-)_t$ with intensity λ , counting positive and negative jumps, to the residual demand forecast.
- At each jump time t ,
 - with probability p^+ , $(N_t^+)_t$ has a jump.
 - with probability $p^- = 1 - p^+$, $(N_t^-)_t$ has a jump.
- New dynamics of demand:

$$dD_t = \mu dt + \sigma_d dB_t + \delta^+ dN_t^+ + \delta^- dN_t^-$$

with $\delta^+ > 0$ and $\delta^- < 0$

- Impact on intraday price:

$$dY_t = \nu q_t dt + \sigma_0 dW_t + \pi^+ dN_t^+ + \pi^- dN_t^-$$

with $\pi^+ > 0$ and $\pi^- < 0$.

Let $\delta := p^+ \delta^+ + p^- \delta^-$ and $\pi := p^+ \pi^+ + p^- \pi^-$.

Value function and auxiliary problem

- Value function:

$$v^{(\lambda)}(t, x, y, d) = \inf_{\substack{\mathbf{q}^{(\lambda)} \in \mathcal{A}_t \\ \xi \in L_+^0(\mathcal{F}_T)}} J(t, x, y, d; \mathbf{q}, \xi).$$

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- Auxiliary problem, relaxing the constraint of positivity of the production:

$$\tilde{v}^{(\lambda)}(t, x, y, d) = \inf_{\substack{\mathbf{q}^{(\lambda)} \in \mathcal{A}_t \\ \xi \in L^0(\mathcal{F}_T)}} J(t, x, y, d; \mathbf{q}, \xi).$$

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- The solution to that problem is **again** explicit.

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- Yet straightforward but (much more) tedious computations.

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- The solution to that problem is **again** explicit.
- Yet straightforward but (much more) tedious computations.
- Tedious?

Pierre Gruet's handmade computation



Handwritten mathematical derivations and notes on a grid background. The text includes various equations, definitions, and step-by-step calculations. Key elements include:

- Top left: Definitions of variables like X, Y, Z and a function f .
- Top middle: A complex equation involving E and f .
- Top right: A series of equations involving λ and μ .
- Middle left: A large equation with multiple terms and a summation.
- Middle right: A series of equations involving λ and μ .
- Bottom left: A series of equations involving λ and μ .
- Bottom middle: A series of equations involving λ and μ .
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Handwritten mathematical derivations and notes on a grid background, continuing from the top section. The text includes various equations, definitions, and step-by-step calculations. Key elements include:

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Optimal control in the auxiliary problem

Optimal trading rate

$$\hat{q}_s^{(\lambda)} = \hat{q}_s^{(0)} + \lambda \frac{r(\eta, \beta) \delta(T - s) + \frac{\pi}{4\gamma} (r(\eta, \beta) + \nu)(T - s)^2}{(r(\eta, \beta) + \nu)(T - s) + 2\gamma}$$

Property

$$\bar{q}_s^{(\lambda)} := \left(\hat{q}_s^{(\lambda)} + \frac{\lambda\pi}{2\gamma} (s - t) \right)_{t \leq s \leq T}$$

is a martingale:

- if $\pi > 0$, then $(q_s^{(\lambda)})_s$ is a supermartingale.
- if $\pi < 0$, then $(q_s^{(\lambda)})_s$ is a submartingale.

Interpretation

- Expected demand at final time T seen at time t is

$$\bar{D}_t := D_t + \mu(T - t) + \lambda\delta(T - t),$$

- Expectation of \hat{X}_T seen at time t is

$$\bar{X}_t := X_t + \hat{q}_t^{(\lambda)}(T - t) - \frac{\lambda\pi}{4\gamma}(T - t)^2$$

- Expectation of the final "price plus marginal cost of getting $\hat{q}_T^{(\lambda)}$ " is

$$\bar{Y}_t := Y_t + \lambda\pi(T - t) + \nu(\hat{q}_t^{(\lambda)}(T - t) - \frac{\lambda\pi}{4\gamma}(T - t)^2) + 2\gamma(\hat{q}_t^{(\lambda)} - \frac{\lambda\pi}{2\gamma}(T - t))$$

- Thus,

$$\bar{Y}_t = c'(\bar{D}_t - \bar{X}_t)$$

- Optimal trading strategy is still to make the forecast marginal cost equal to the forecast price.

Interpretation

Consequence

- Suppose that at time 0, the intraday price is equal to the day-ahead spot price and the producer is balanced.
- Here, balanced means:

$$Y_0 + \lambda\pi T = c'(\widehat{D}_0 - \widehat{X}_0)$$

- Thus, at time 0 should be taken the precautionary position:

$$\bar{q}_0^{(\lambda)} = \frac{\lambda\pi T + \frac{\lambda\pi}{4\gamma}(r(\eta, \beta) + \nu)T^2}{(r(\eta, \beta) + \nu)T + 2\gamma}$$

Delay h in generation

- Consider the auxiliary relaxed problem without jumps.
- It is always better to wait until $T - h$ to take the generation decision.
- Between $T - h$ and T , we face an optimal trading problem with no generation and with inventory $X_{T-h} + \xi$.
- Knowing the optimal trading rate as function of ξ , it is possible to compute the optimal generation level.
- Knowing the optimal generation level to be applied at time $T - h$ and the optimal trading rate between $T - h$ and T , we are brought back to an instance of our problem between 0 and $T - h$ with a (slightly) more complex terminal cost function.

Consequences

After tedious computations, we found that:

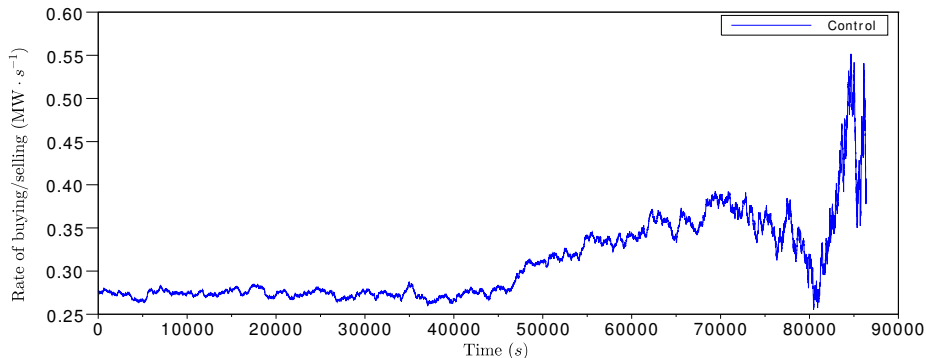
- Between 0 and $T - h$, the control with and without delay is the same.
- Only the value functions differ.

Numerical applications and simulations

Parameter values for nice simulations

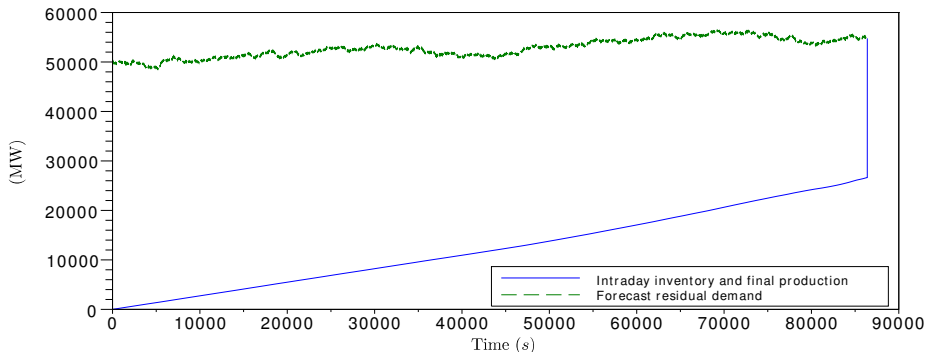
Time period	$T = 24$	h
Initial inventory level	$X_0 = 0$	MWh
Initial demand forecast	$D_0 = 50,000$	MWh
Initial intraday price	$Y_0 = 50$	$\text{€} \cdot (\text{MWh})^{-1}$
Demand forecast trend	$\mu = 0$	$\text{MWh} \cdot \text{s}^{-1}$
Intraday price volatility	$\sigma_0 = 1/60$	$\text{€} \cdot (\text{MWh})^{-1} \cdot \text{s}^{-1/2}$
Demand forecast volatility	$\sigma_d = 1000/60$	$\text{MWh} \cdot \text{s}^{-1/2}$
Correlation	$\rho = 0.8$	
Cost function parameter	$\beta = 0.002$	$\text{€} \cdot (\text{MWh})^{-2}$
Inbalance penalty	$\eta = 200$	$\text{€} \cdot (\text{MWh})^{-2}$
Permanent impact	$\nu = 4.00 \cdot 10^{-5}$	$\text{€} \cdot (\text{MWh})^{-2}$
Instantaneous impact	$\gamma = 2.22$	$\text{€} \cdot \text{s} \cdot (\text{MWh})^{-2}$
Probability of positive jumps	$p^+ = 1$	
Intensity of jump	$\lambda = 1.5 / (3600 \cdot 24)$	s^{-1}
Size of the price jump	$\pi^+ = 10$	$\text{€} \cdot (\text{MWh})^{-1}$
Size of the demand forecast jump	$\delta^+ = 1500$	MWh

No jumps, no delay — Optimal trading rate



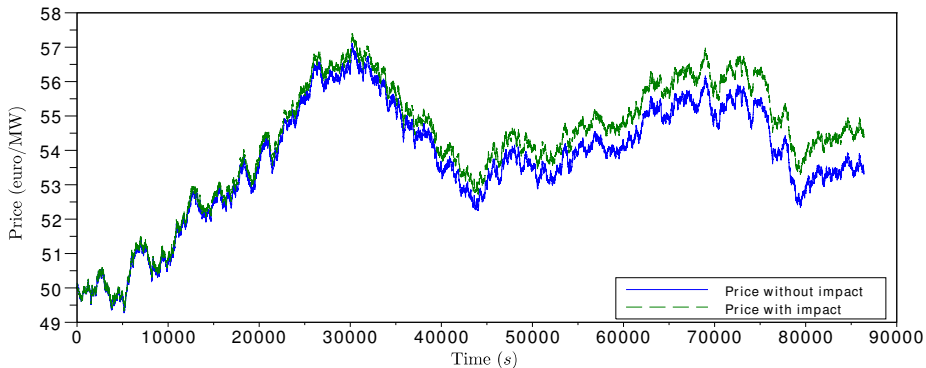
Final oscillation to adjust production and demand.

No jumps, no delay — Inventory



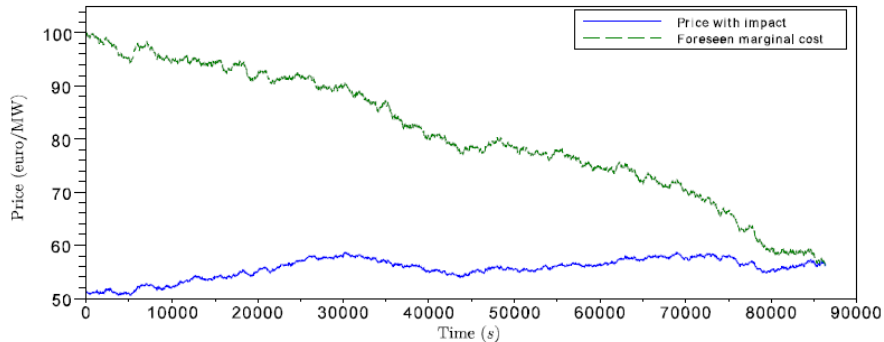
Linear growth of the inventory with final generation to adjust to demand.

No jumps, no delay — Prices



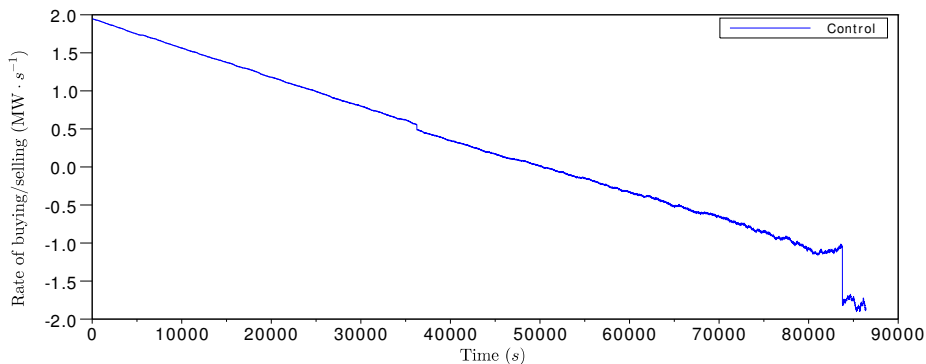
Small yet persistent impact on prices.

No jumps, no delay — Marginal cost and price



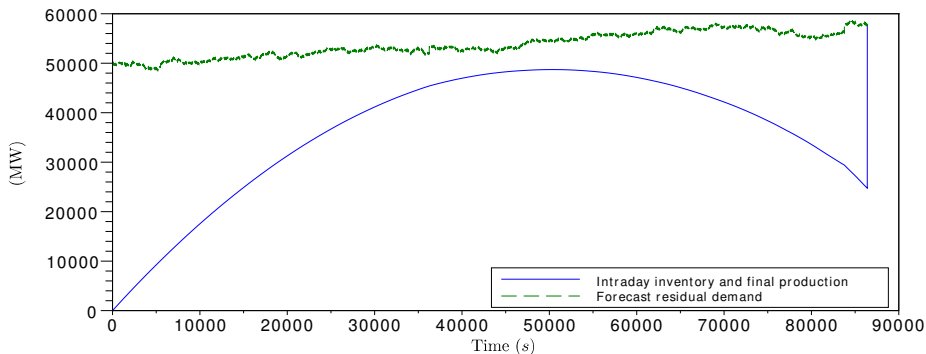
The marginal cost decreases until it reaches the increasing price.

Jumps $\pi > 0$, no delay — Optimal trading rate



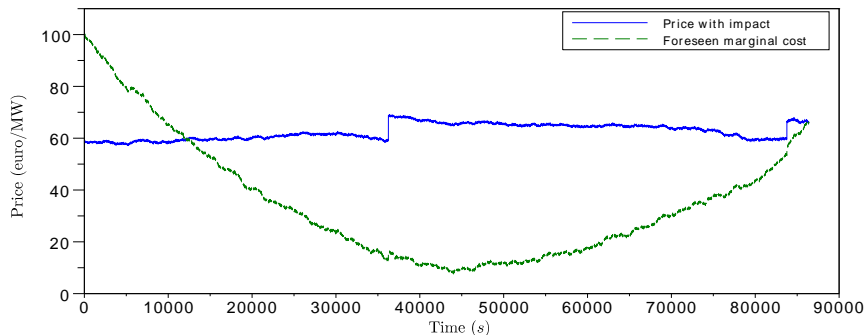
Decreasing trading rate. Starts with positive value (buy), at some point in time, becomes negative (sell).

Jumps $\pi > 0$, no delay — Inventory



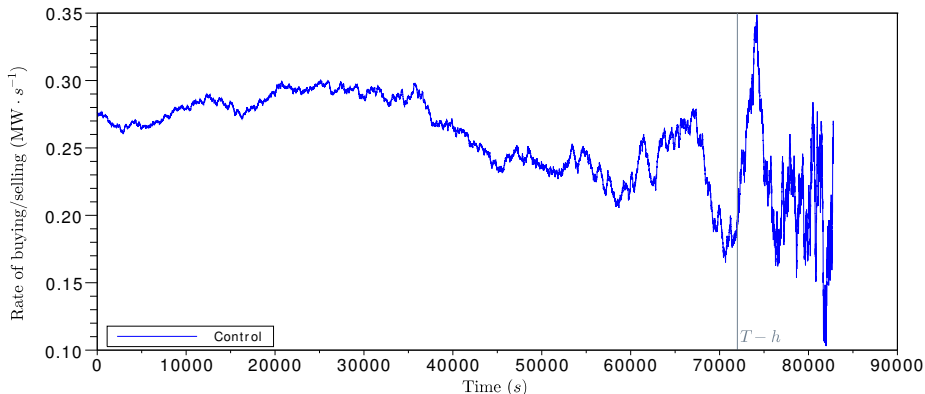
First, increasing inventory, then decreasing inventory, and final generation to adjust to demand.

Jumps, no delay — Marginal cost and price



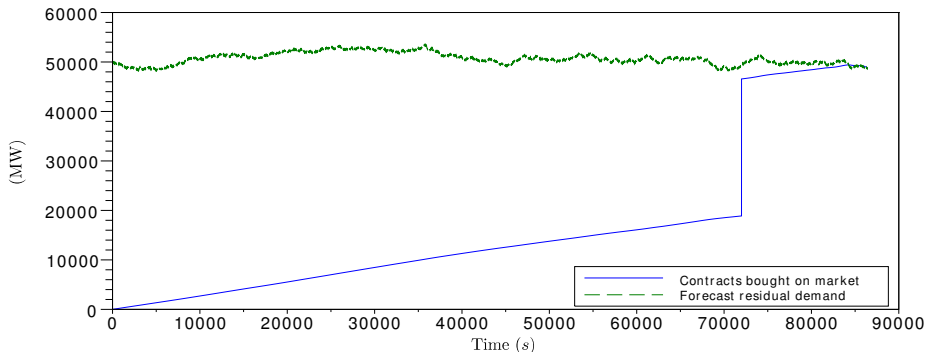
First decreasing forecast marginal cost (positive large inventory means less to be produced at maturity) then, increasing forecast marginal cost.

Delay $h = 4$ hours — Optimal trading rate



Trading rate after time $T - h$ is the only tool to fit the demand. Thus becomes more volatile.

Delay $h = 4$ hours — Inventory



At $T - h$, the rate at which the inventory increases suddenly changes.

Application — Precautionary position

Question

What is the size of the anticipated precautionary position that should be taken in the case of jumps in the residual demand forecast?

Answer

$$\bar{q}_0^{(\lambda)} = \frac{\lambda\pi T + \frac{\lambda\pi}{4\gamma}(r(\eta, \beta) + \nu)T^2}{(r(\eta, \beta) + \nu)T + 2\gamma}$$

with reasonable parameter values:

$\lambda = 1.5 \cdot 10^{-5}$ (1 jump per month), $\gamma = 2 \text{ €}\cdot\text{h}\cdot(\text{MWh})^{-2}$, $\nu = 0.1 \text{ €}\cdot(\text{MWh})^{-2}$,
 $\pi = 500 \text{ €}/\text{MWh}$, $\eta = 200 \text{ €}/\text{MWh}$, $\beta = 2.0 \cdot 10^{-3} \text{ €}/\text{MW}^2$, $T = 24$ hours.

$$\bar{q}_0^{(\lambda)} \approx 3.6 \text{ MWh}/\text{h}$$

For one jump per week, the precautionary position is $\approx 14 \text{ MWh}/\text{h}$.

Conclusion

Conclusion

- Analysis of electricity intraday trading with a small and tractable stochastic control model.
- Extension of Almgren and Chriss (2000) optimal execution model with linear impact to stochastic target.
- Confort the operational strategy.
- Jumps in the residual demand process lead to non-zero yet small precautionary initial position.

Perspective

- Intraday prices models.
- Statistical arbitrage.
- Risk management.

References

- Talk based on paper "An optimal trading problem in intraday electricity market" available on arXiv and to appear in *Mathematical and Financial Economics*.
- All presented data on intraday electricity markets are available on demand at EpexSpot website www.epexspot.com.
- R. Almgren and N. Chriss. Optimal execution of portfolio transactions. *Journal of Risk*. 2000.
- E. Garnier and R. Madlener. Balancing forecast errors in continuous-trade intraday markets. FCN WP 2/2014, RWTH Aachen University School of Business and Economics, 2014.
- G. Giebel, G. Kariniotakis, R. Brownsword, M. Denhard and C. Draxl. The state-of-the-art in short-term prediction of wind power. A literature overview. 2nd Edition. In Deliverable Report D1.2 of the Anemos Project (ENK5-CT-2002-00665), 2011.
- A. Henriot. Market design with centralised wind power management: handling low-predictability in intraday markets. *The Energy Journal*. 2014.