

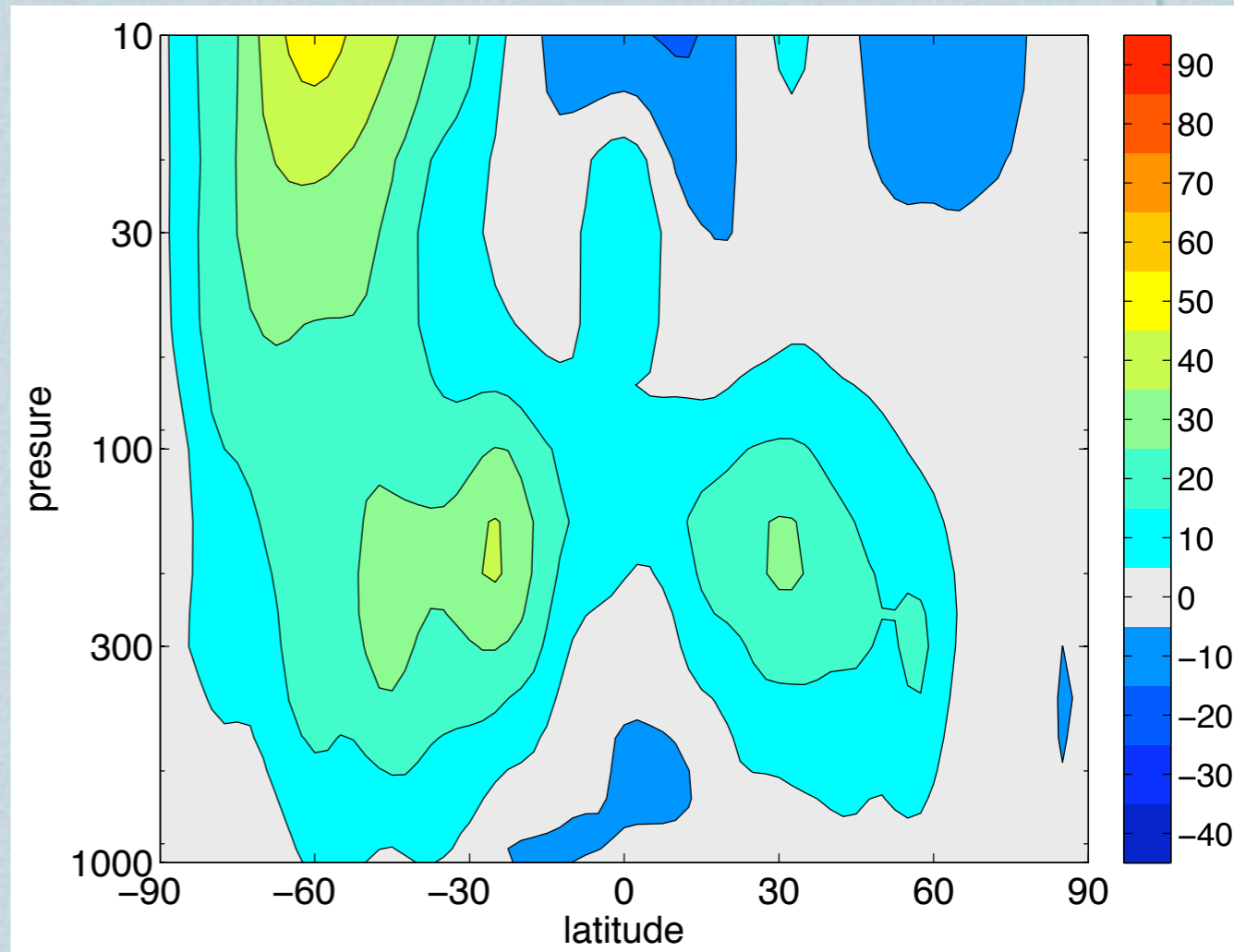
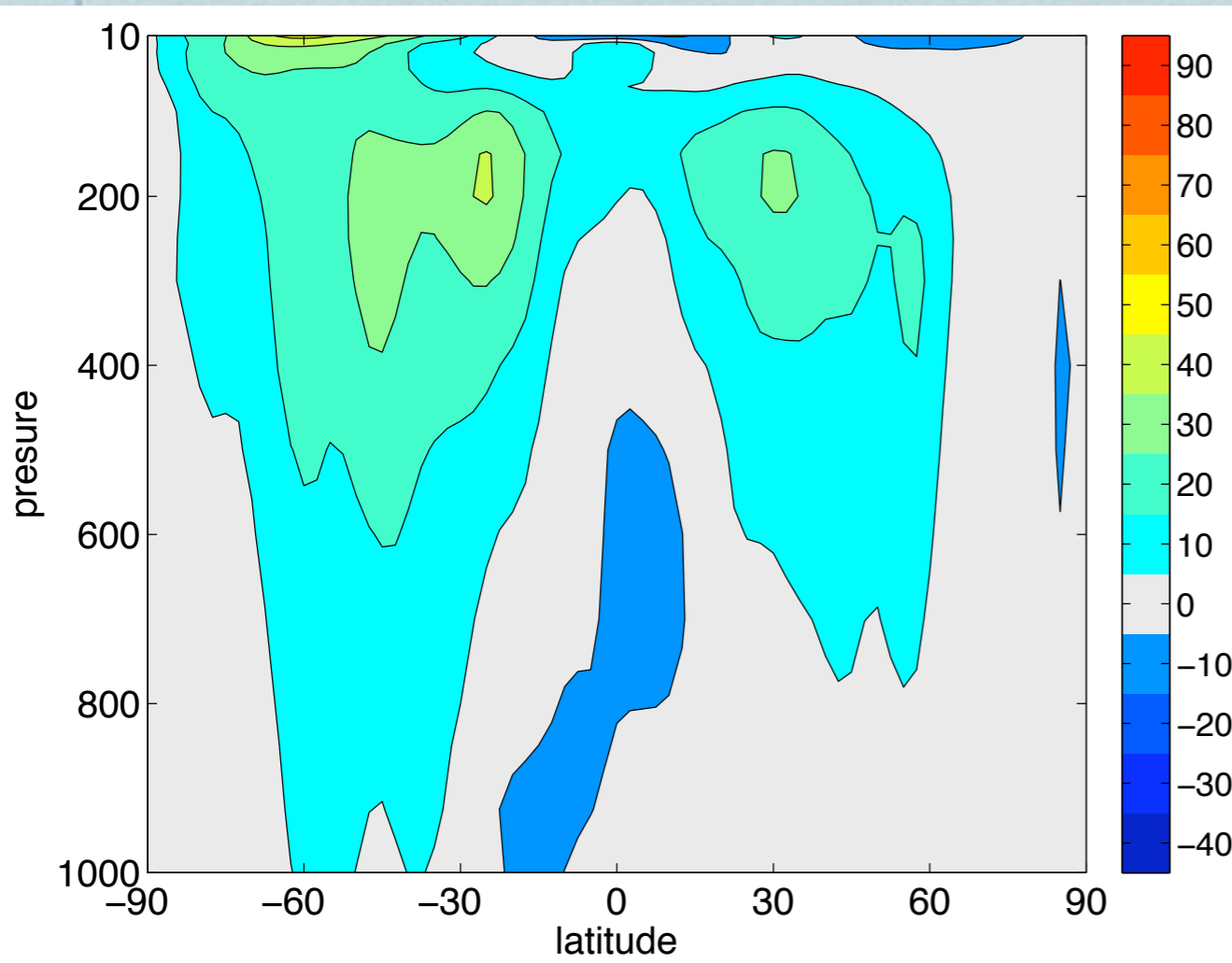
On the time scales of midlatitude
atmospheric variability:
Eddy-mean flow interactions and
coupling from on high

Edwin P. Gerber

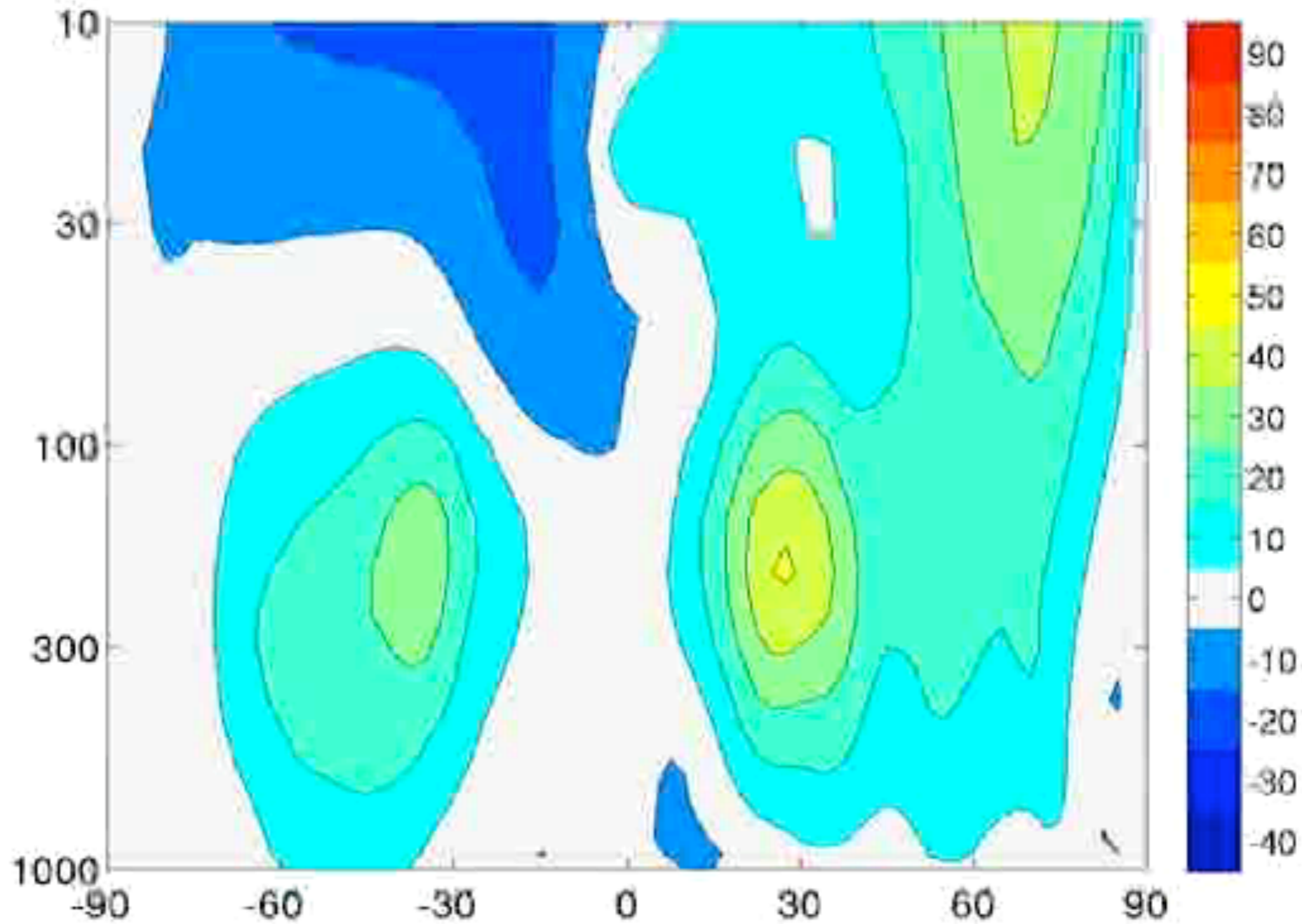
Center for Atmosphere Ocean Science
Courant Institute, New York University



Zonal Mean Zonal Winds: Jets



NCEP-NCAR Reanalyses for 5/18/78



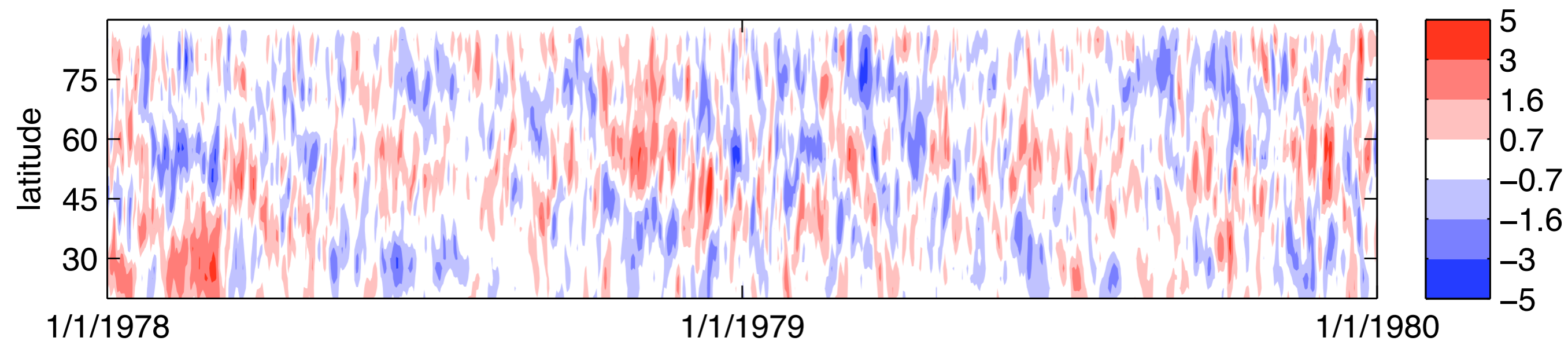
Jan
1978

Jan
1979

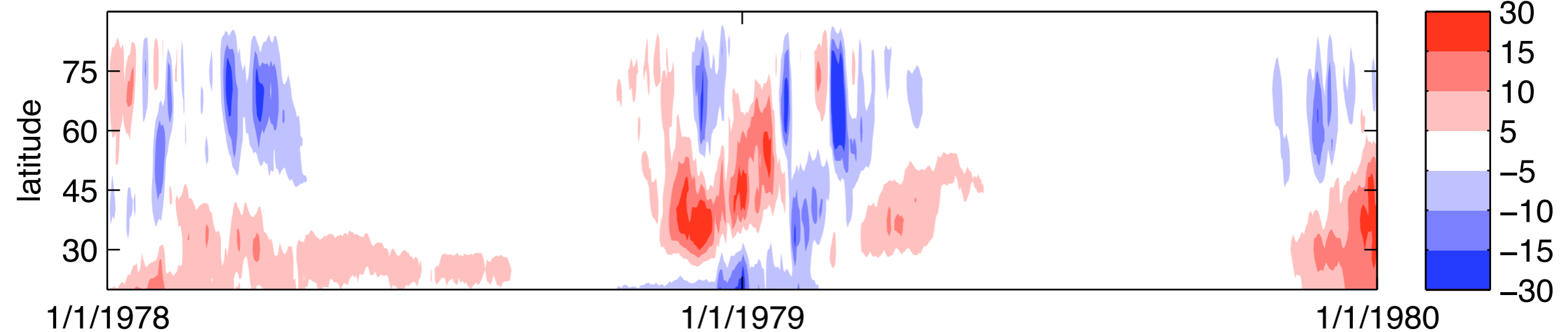
Jan
1980

Variations of the Jets

zonal mean zonal wind anomalies at 1000 hPa



zonal mean zonal wind anomalies at 10 hPa

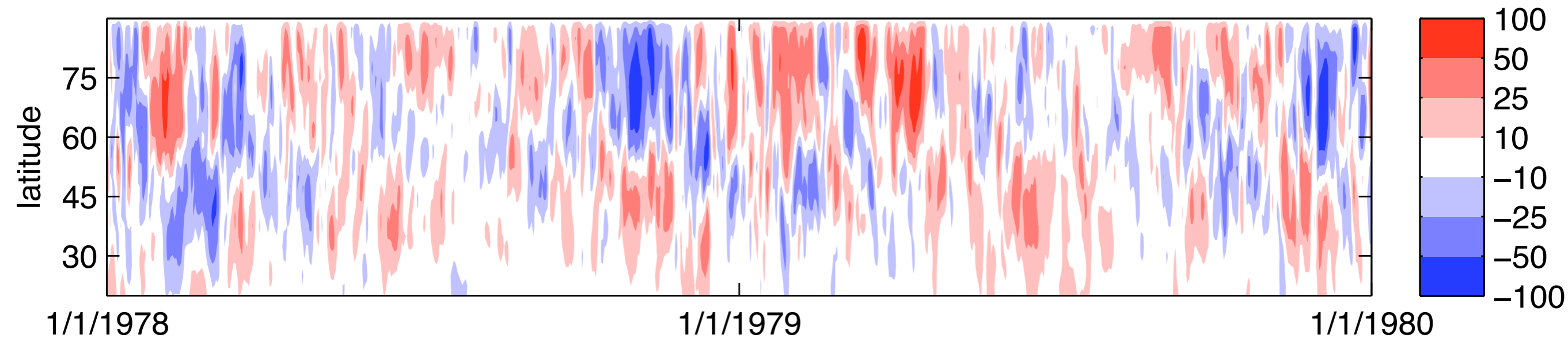


[$\cos^{1/2}(\text{lat})$ weighted, NCEP-NCAR reanalyses]

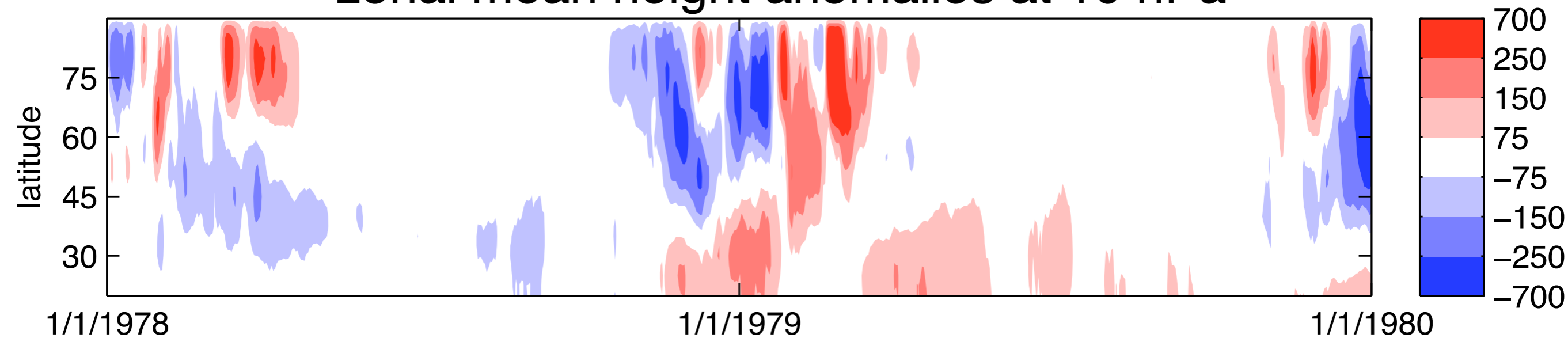
Variations of the Jets

(viewed through height anomalies!)

zonal mean height anomalies at 1000 hPa

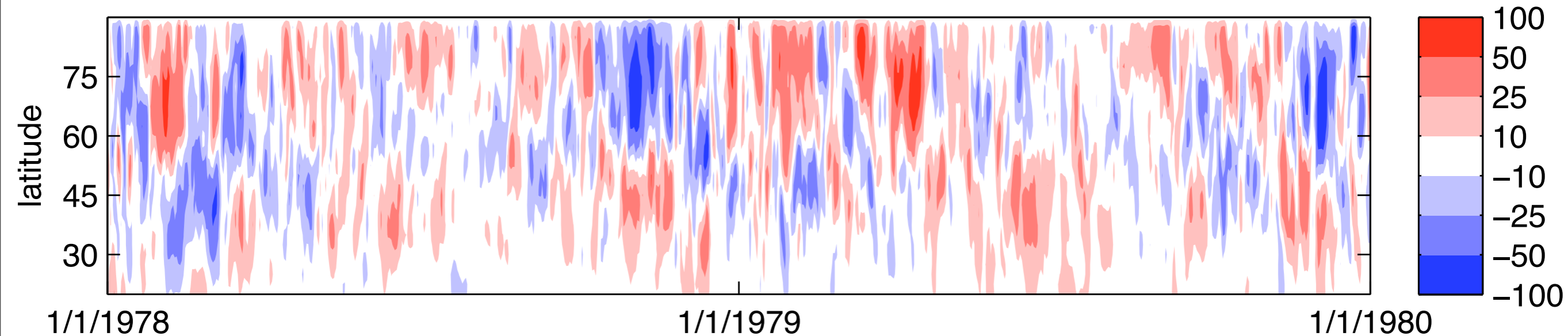


zonal mean height anomalies at 10 hPa



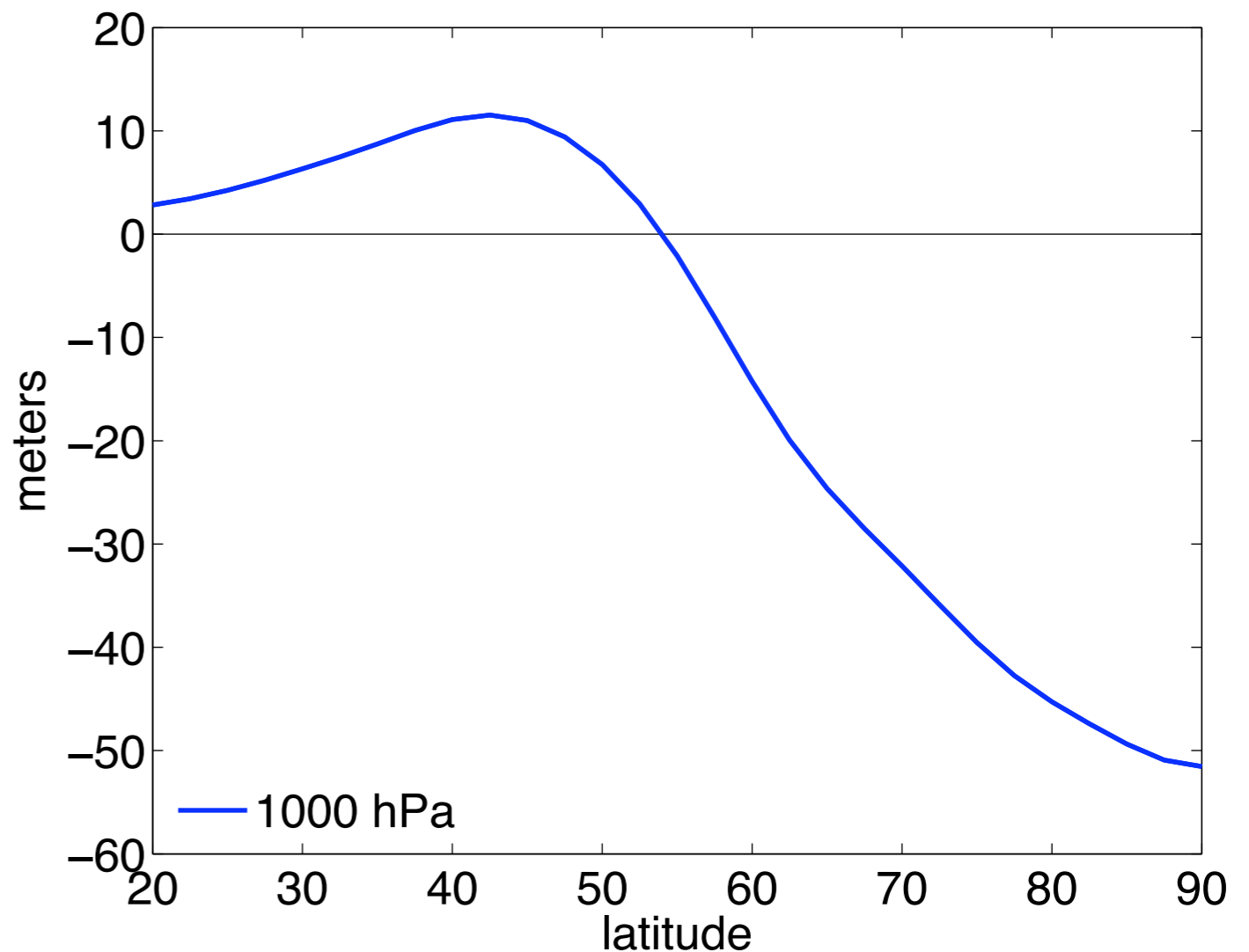
[$\cos^{1/2}(\text{lat})$ weighted, NCEP-NCAR reanalyses]

The Annular Mode (AM)

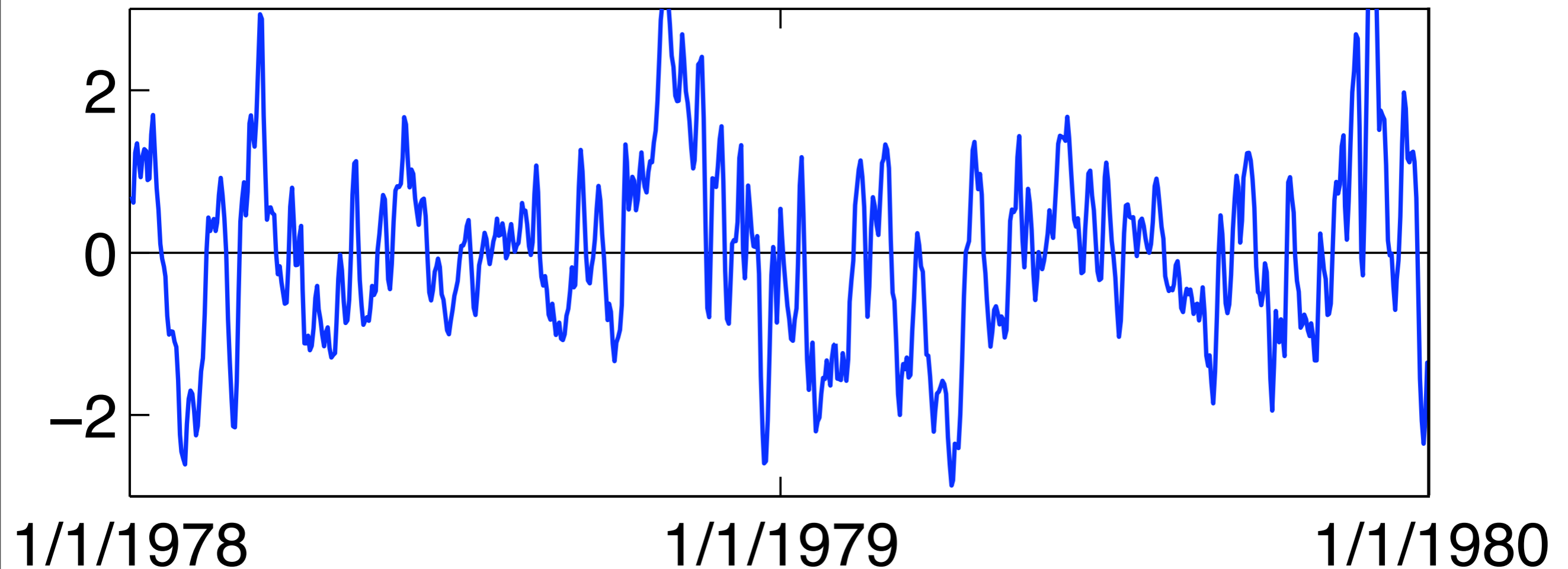
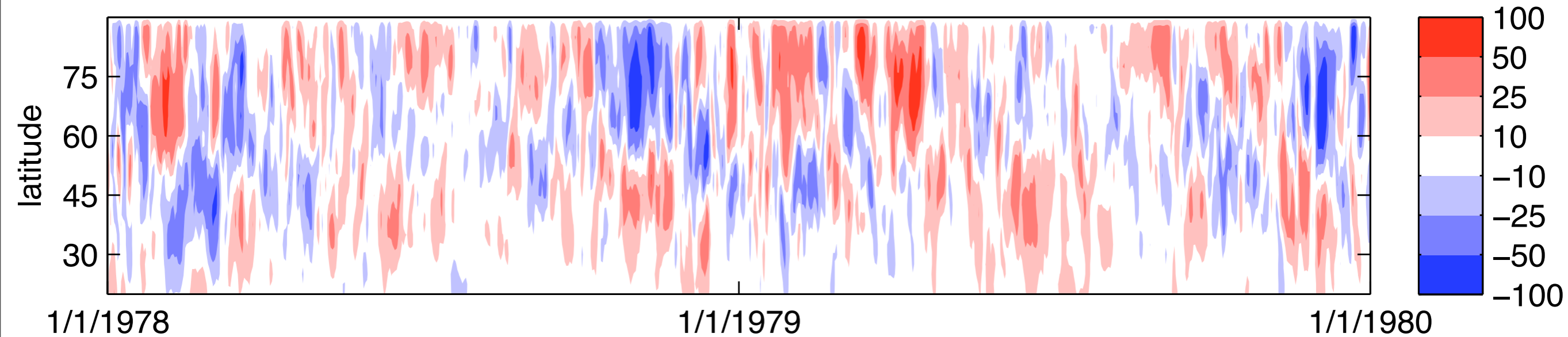


first Empirical Orthogonal
Function (EOF) of zonal
mean geopotential height

Thompson and Wallace 1998,
Baldwin and Thompson 2009



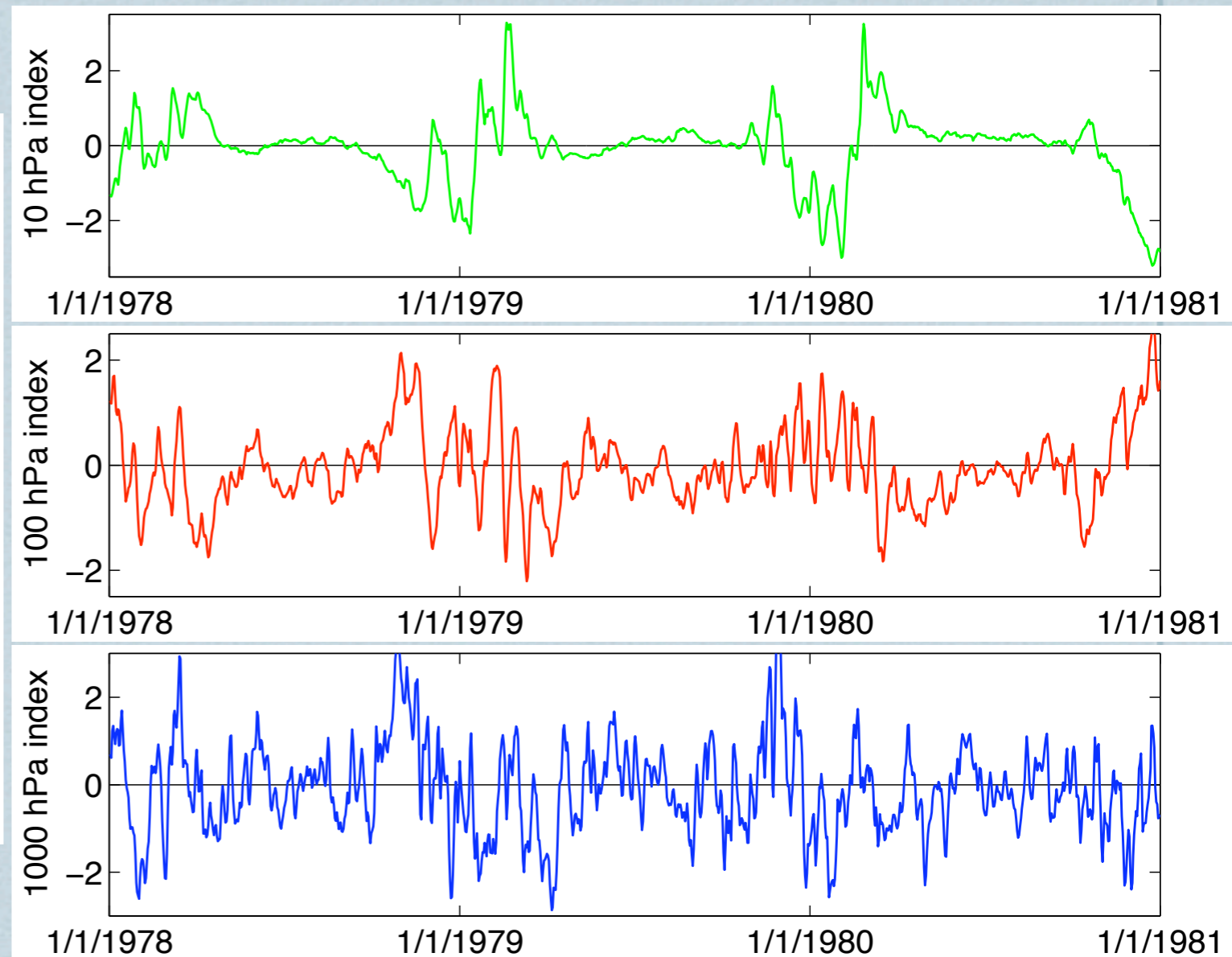
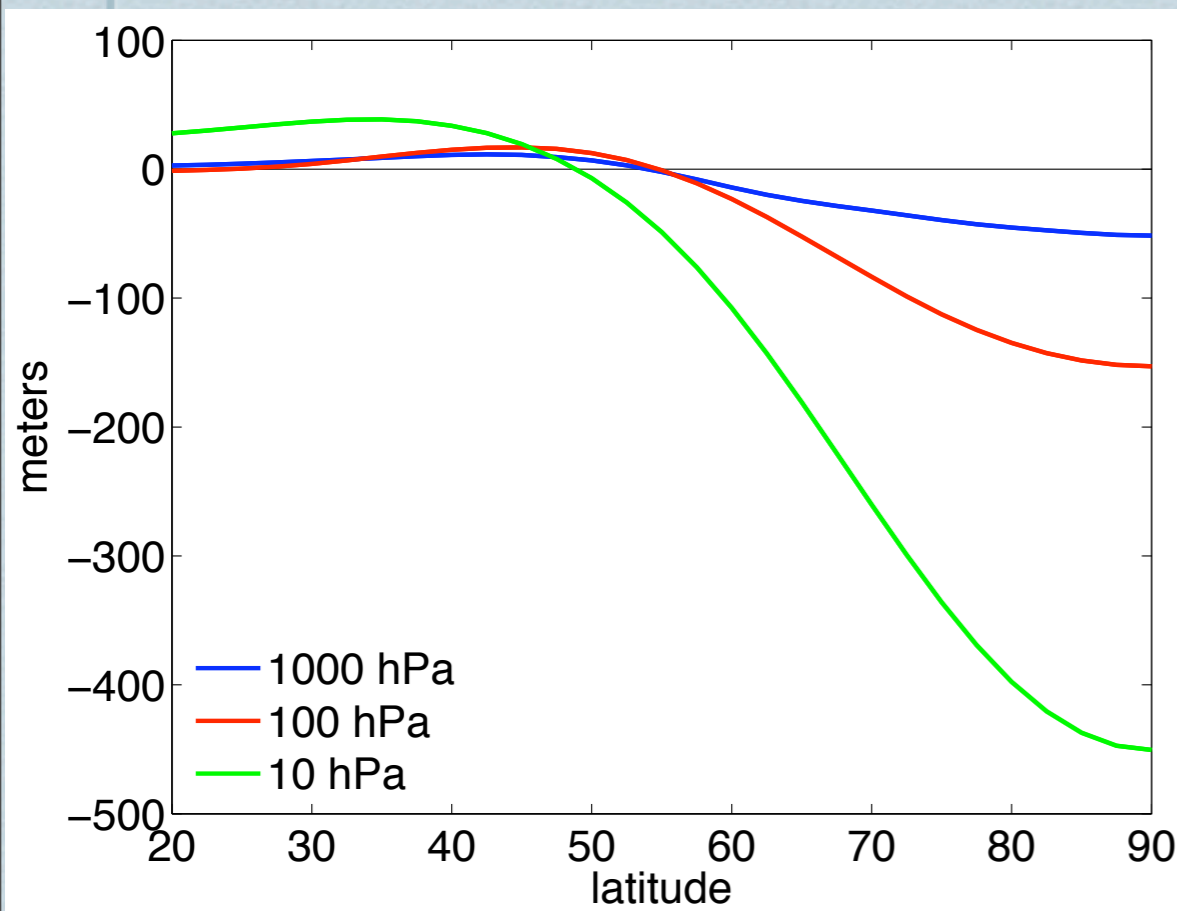
The Annular Mode Index



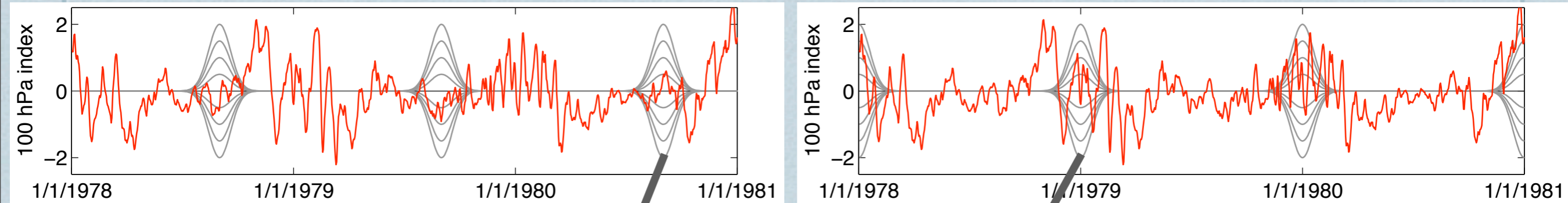
The Annular Mode (AM): as a function of height

AM Indices

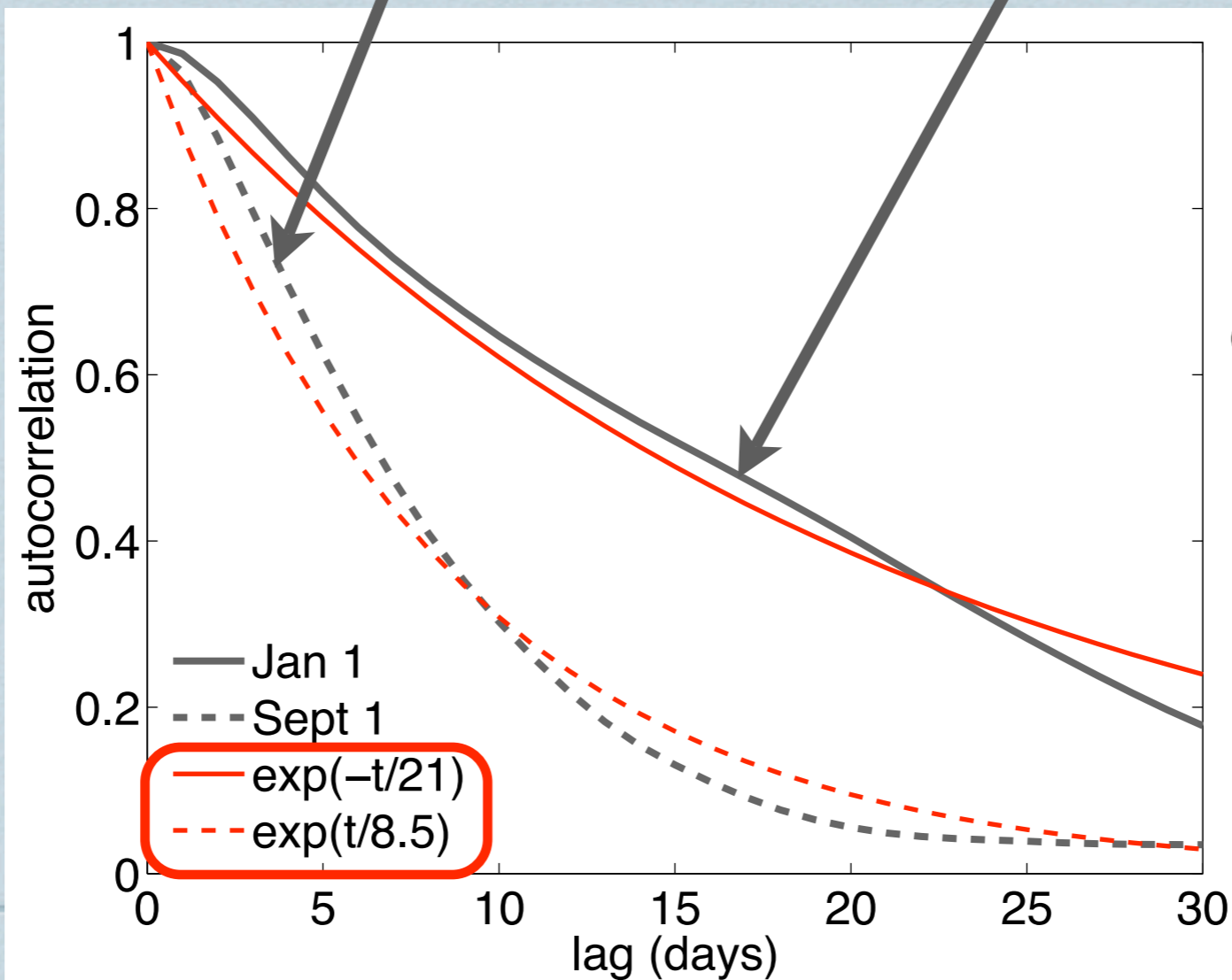
AM patterns



Quantify the correlation: the e-folding time scale



Sept. weather
changes each
week!

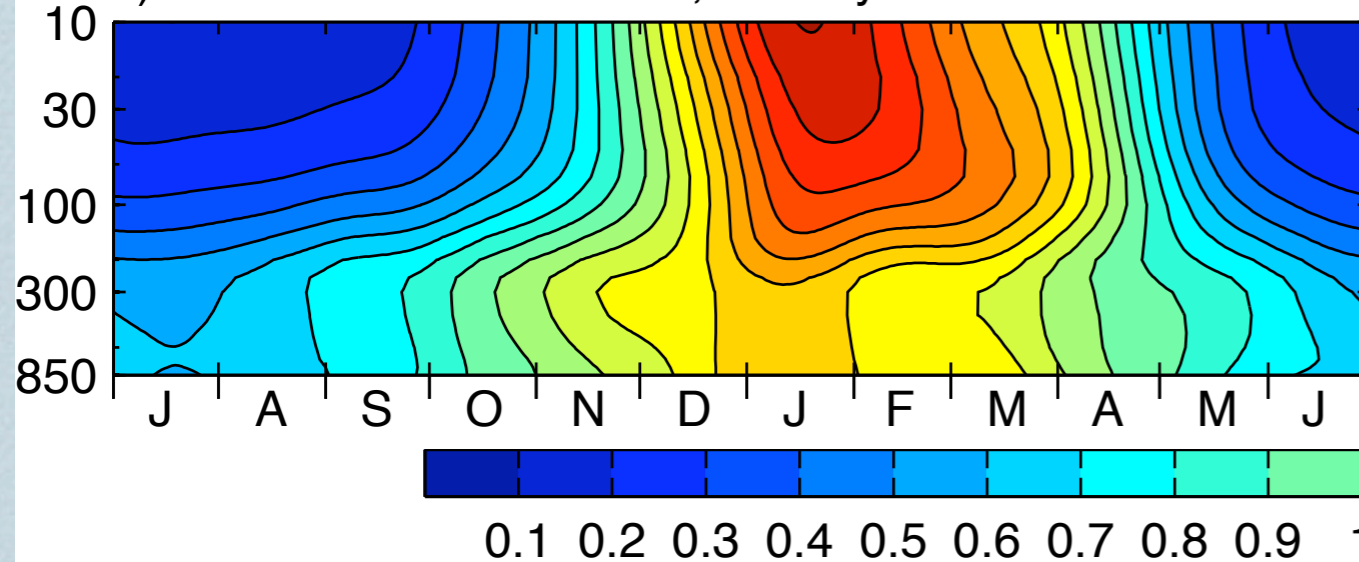


Jan. weather
changes every
three weeks!

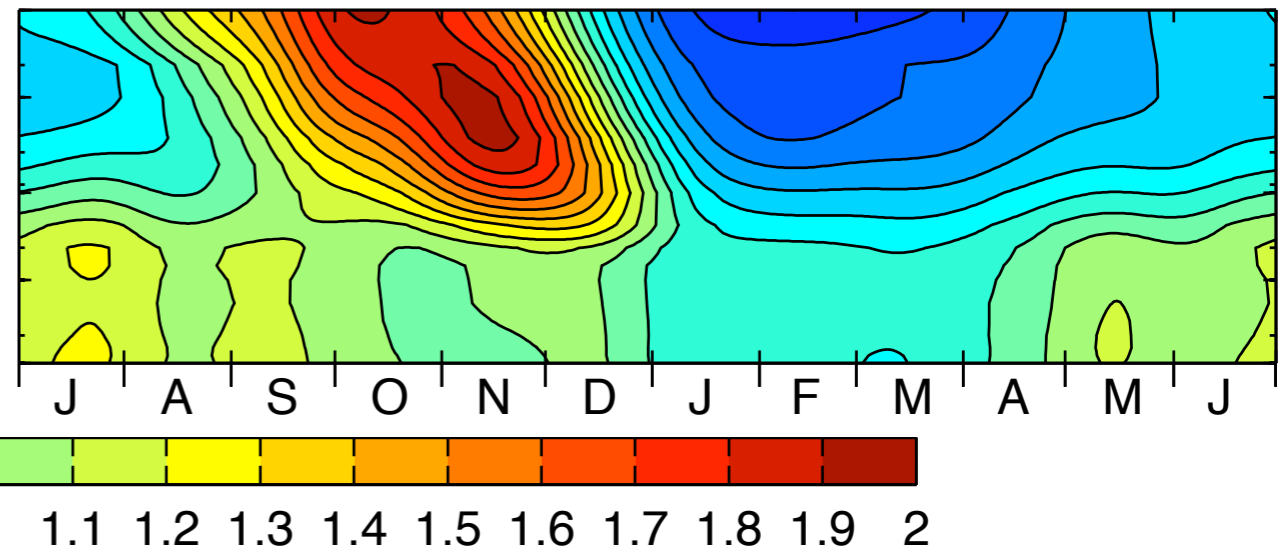
Baldwin
et al. 2003

Observed Annular Mode Amplitude and Time Scale

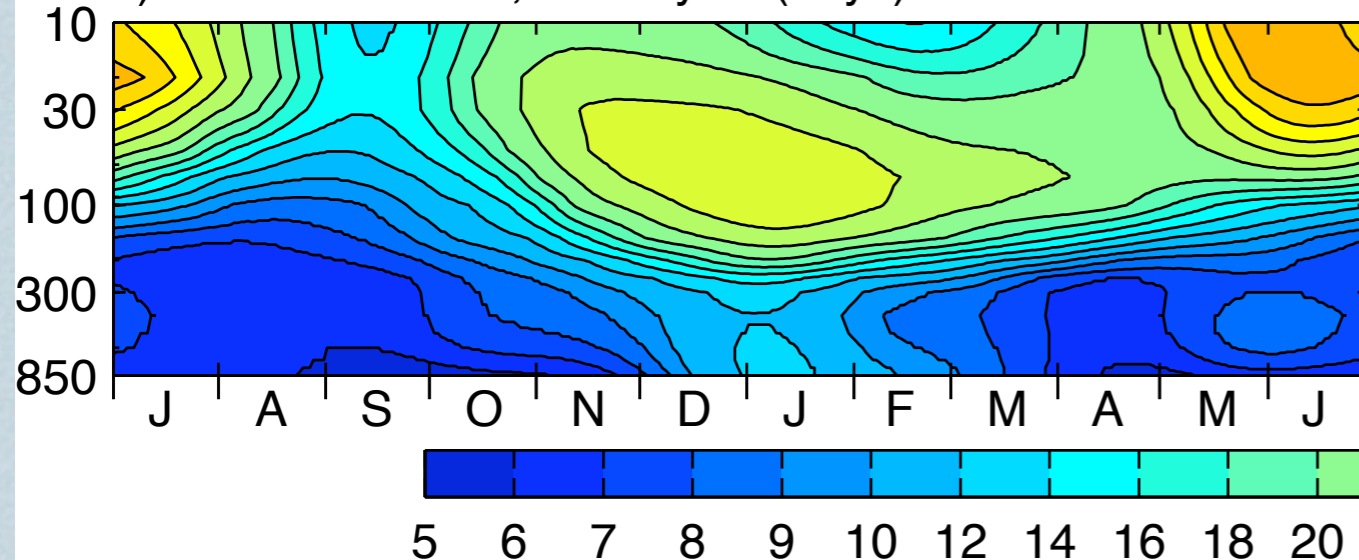
a) NAM standard deviation, reanalysis



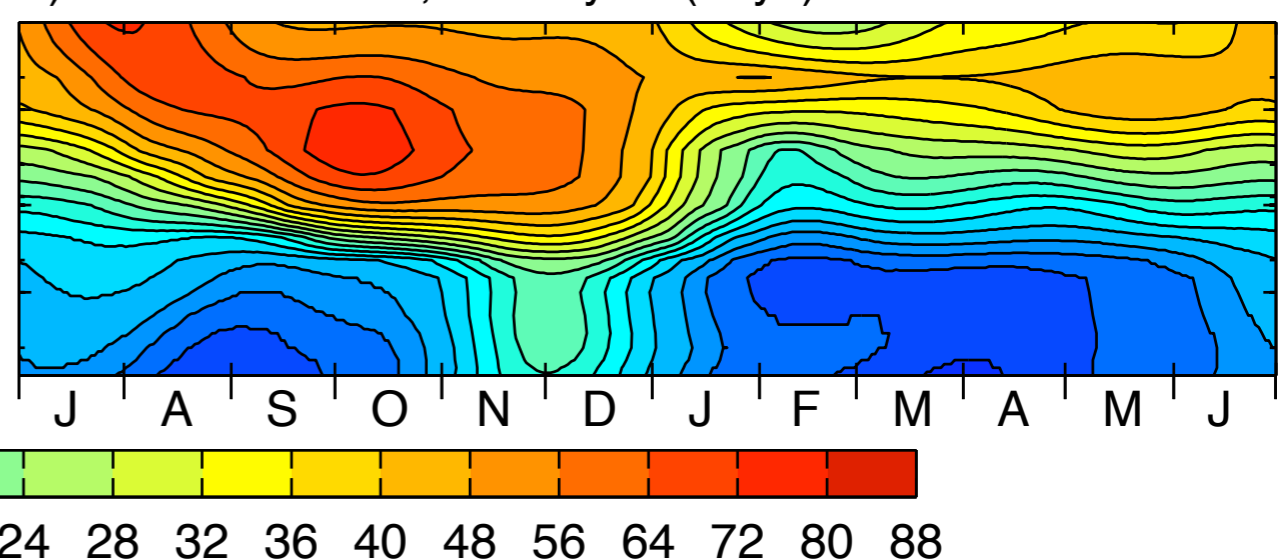
b) SAM standard deviation, reanalysis



a) NAM time scale, reanalysis (days)



b) SAM time scale, reanalysis (days)



Questions

1. What sets the time scales of internal variability?
2. What is the role of the stratosphere (if any) in tropospheric variability?
3. Why is internal variability important? Connection to climate change.

PLAYBILL[®]

Portola Plaza Theatre

(cast, in order of appearance)

- ❖ The barotropic vorticity equation on the sphere
 - stirred with random vorticity perturbations
- ❖ Dry dynamical core (primitive eqns on sphere, “self stirring”)
 - *Held and Suarez* (1994) forcing: troposphere climate
 - *Polvani and Kushner* (2002): add stratospheric polar vortex
- ❖ CMIP₃ coupled atmosphere-ocean climate models, used in the IPCC Fourth Assessment Report
- ❖ Chemistry Climate Models (CCMs)
 - simulate interactive stratospheric ozone chemistry
 - well resolved stratosphere + comparable horizontal resolution to CMIP₃, but forced with specified SSTs

The Simplest Model:

Barotropic Vorticity Dynamics on the Sphere

2D zonal momentum:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} - f v = -\frac{\partial \phi}{\partial x} + \underset{\substack{\uparrow \\ \text{forcing}}}{F_u} - \underset{\substack{\uparrow \\ \text{dissipation}}}{D_u}$$

take zonal mean, and note that
eddy momentum flux
divergence = the vorticity flux

$$\overline{v' \zeta'} = -\frac{\overline{\partial u' v'}}{\partial y}$$

↓

$$\frac{\partial \bar{u}}{\partial t} = \overline{v' \zeta'} + \bar{F}_u - \bar{D}_u \rightarrow$$

($\bar{\quad}$ is zonal mean, $'$ deviation therefrom)

assume no direct momentum forcing, and Rayleigh friction

$$\frac{\partial \bar{u}}{\partial t} = \overline{v' \zeta'} - r \bar{u}$$

The Simplest Model:

Barotropic Vorticity Dynamics on the Sphere

to understand $\overline{v'\zeta'}$
 start with the linearized
 barotropic vorticity eqn.

$$\frac{\partial \zeta'}{\partial t} + \bar{u} \frac{\partial \zeta'}{\partial x} + \gamma v = F'_\zeta - D'_\zeta$$

$$\gamma = \beta - \partial^2 \bar{u} / \partial y^2$$

divide by γ , multiply
 by ζ , take zonal mean
 to get pseudo-
 momentum eqn.

is the meridional gradient in abs. vorticity

$$\frac{\partial M}{\partial t} - \overline{v'\zeta'} = -\frac{1}{\gamma} (\overline{\zeta' F'_\zeta} - \overline{\zeta' D'_\zeta})$$

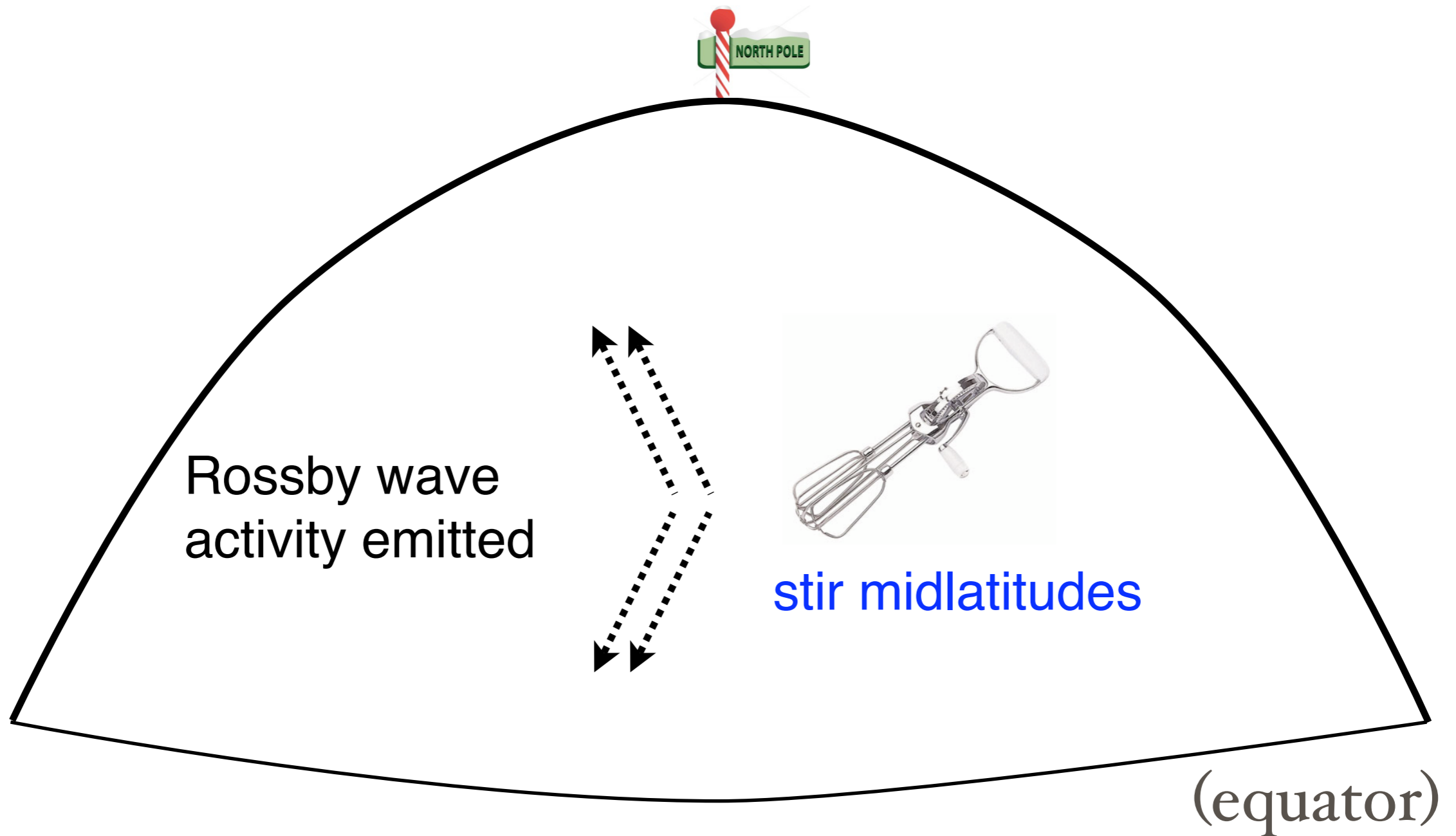
$$M = -\overline{\zeta'^2} / 2\gamma$$

Lastly, combine w/ the momentum equation:

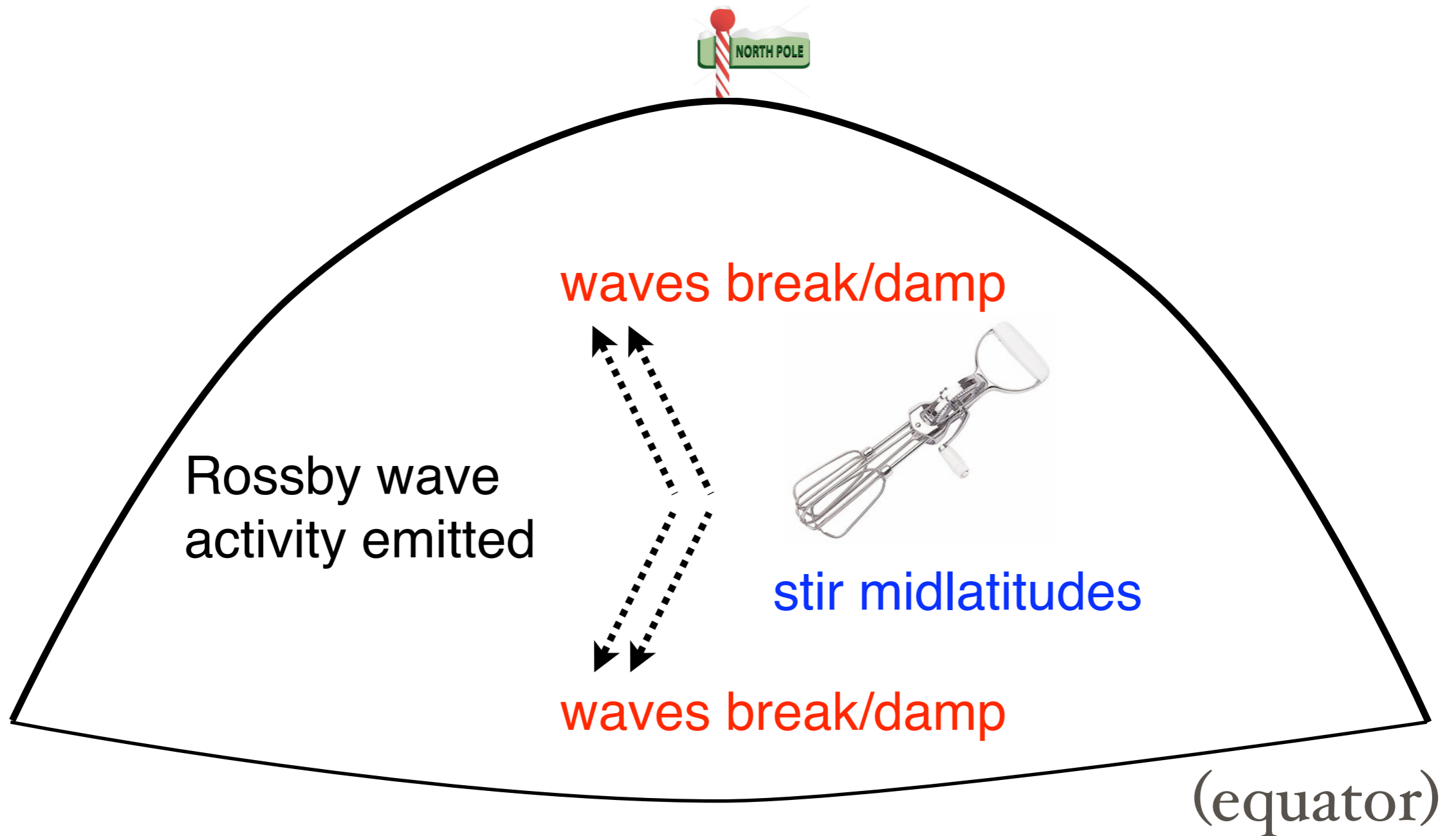
$$\frac{\partial \bar{u}}{\partial t} - \frac{\partial M}{\partial t} = -r\bar{u} + \frac{1}{\gamma} \overline{\zeta' F'_\zeta} - \overline{\zeta' D'_\zeta}$$

stirring
damping

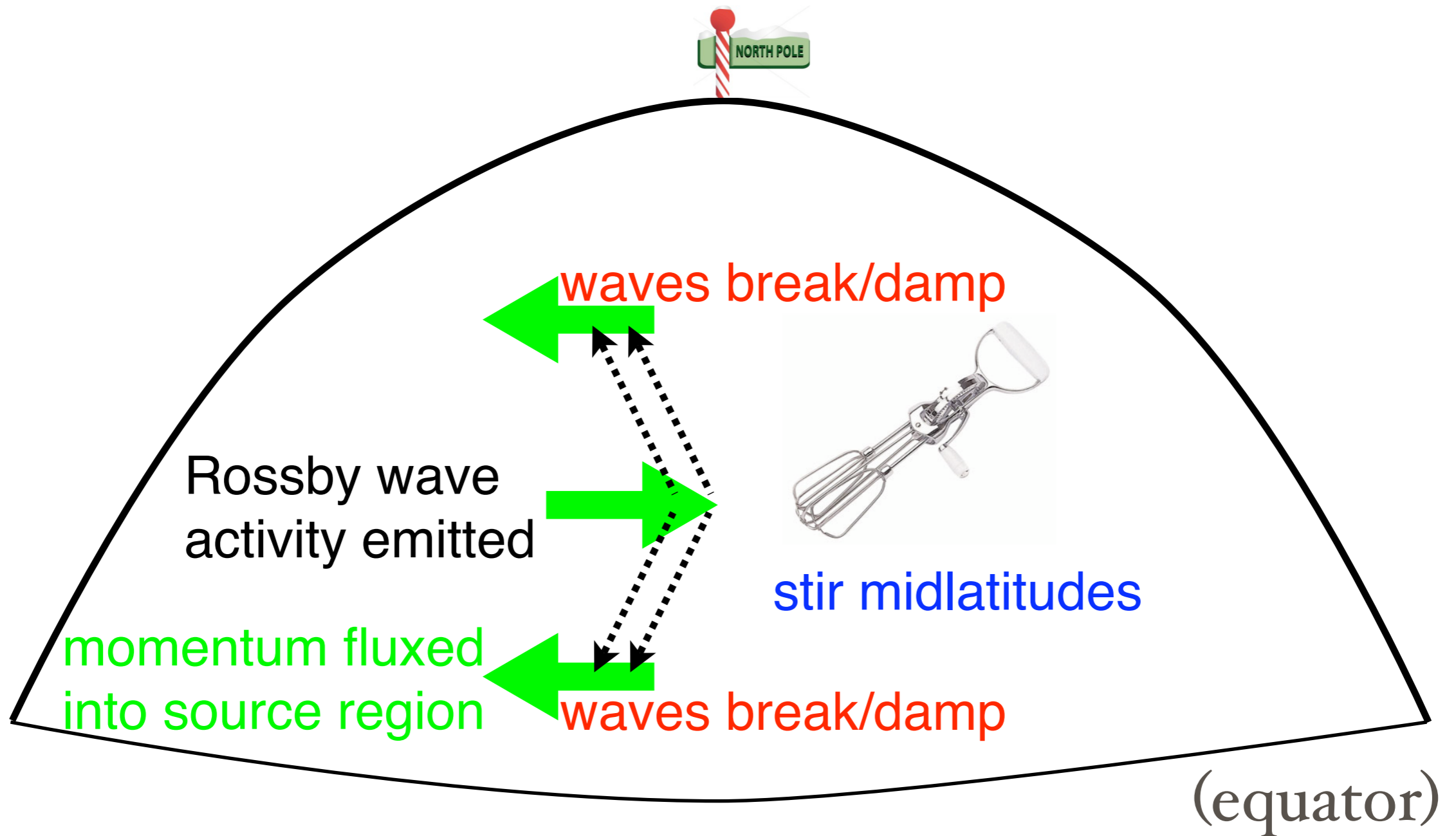
A Physical Picture



A Physical Picture

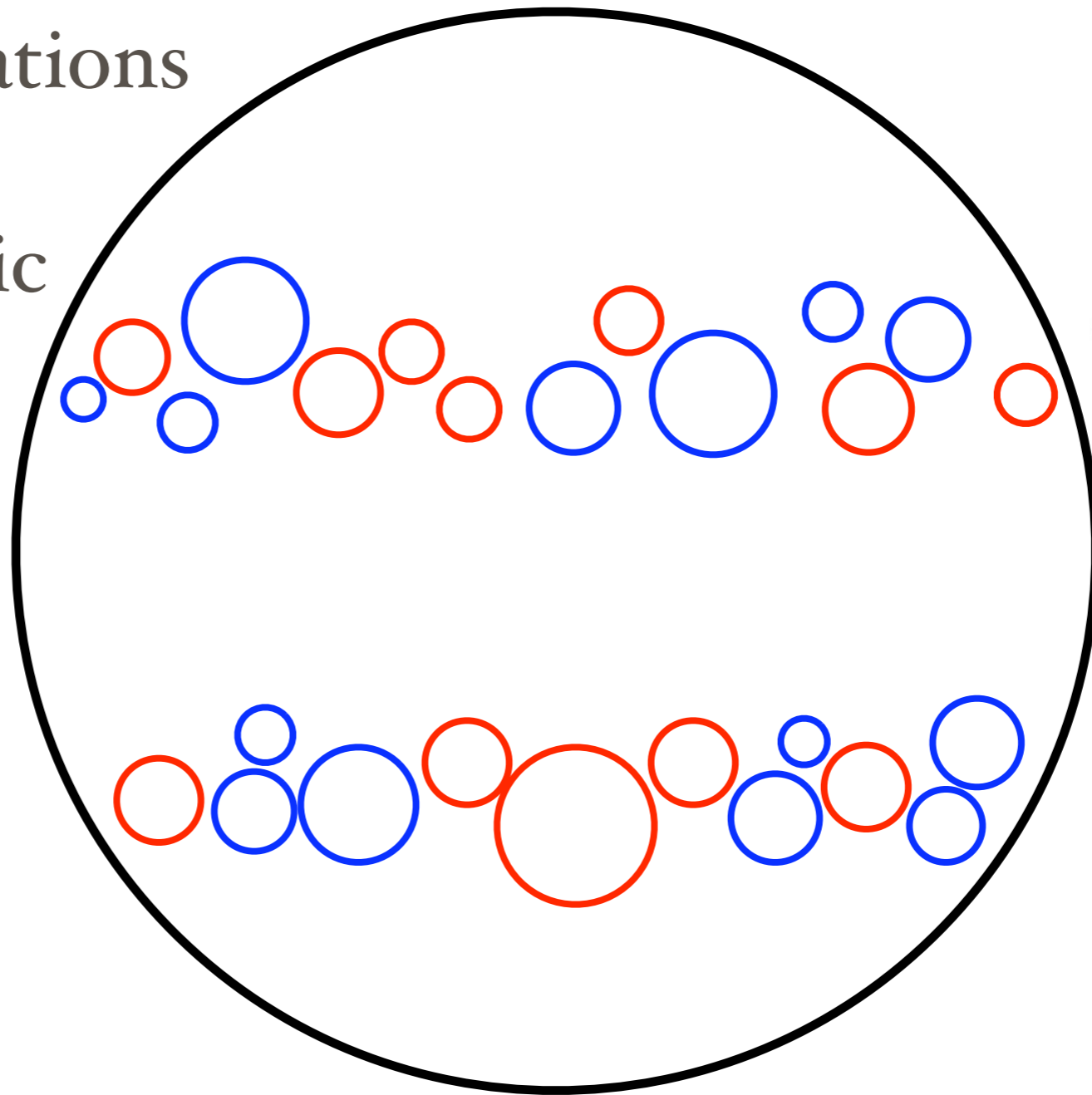


A Physical Picture

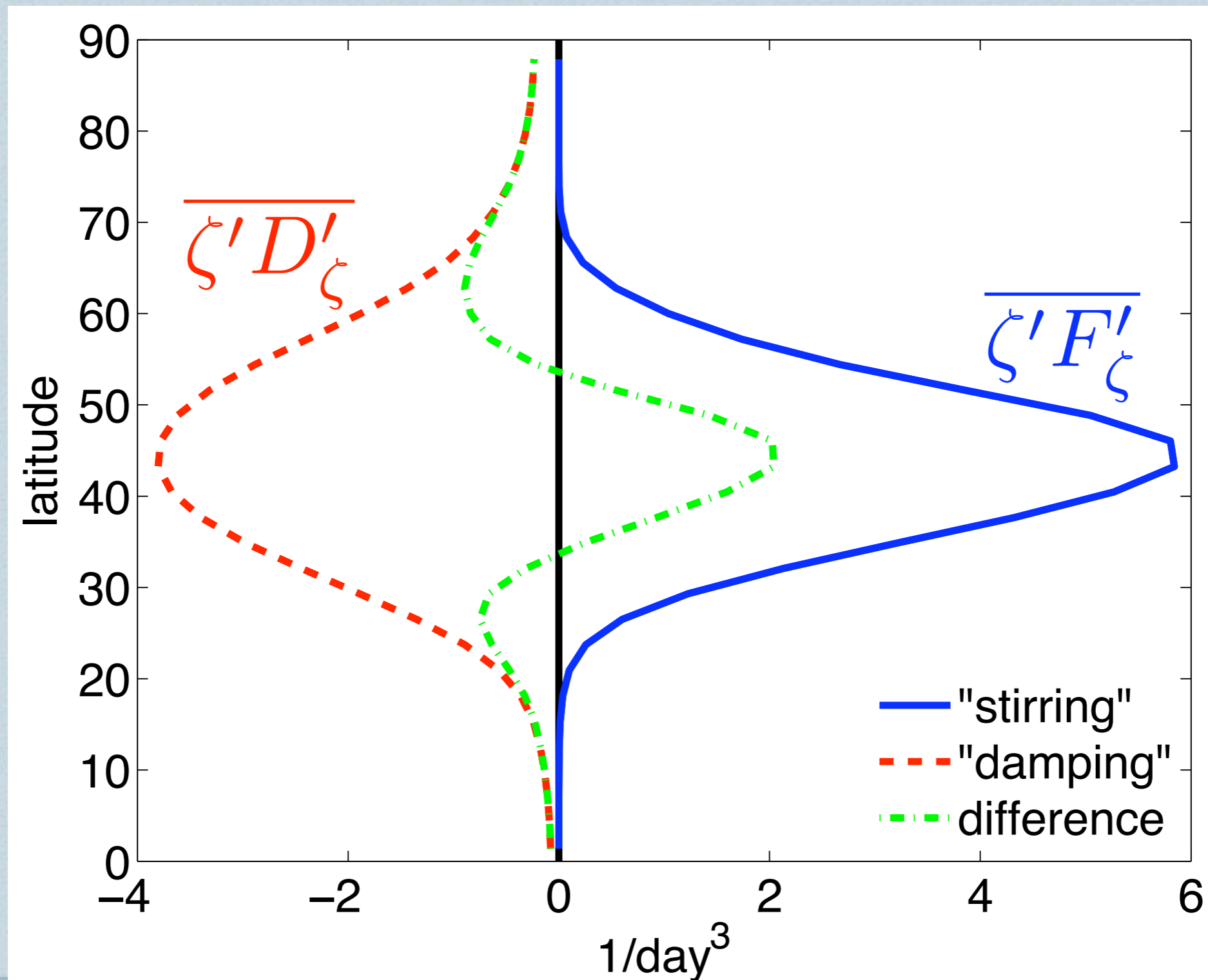


Numerical Experiments on the Sphere

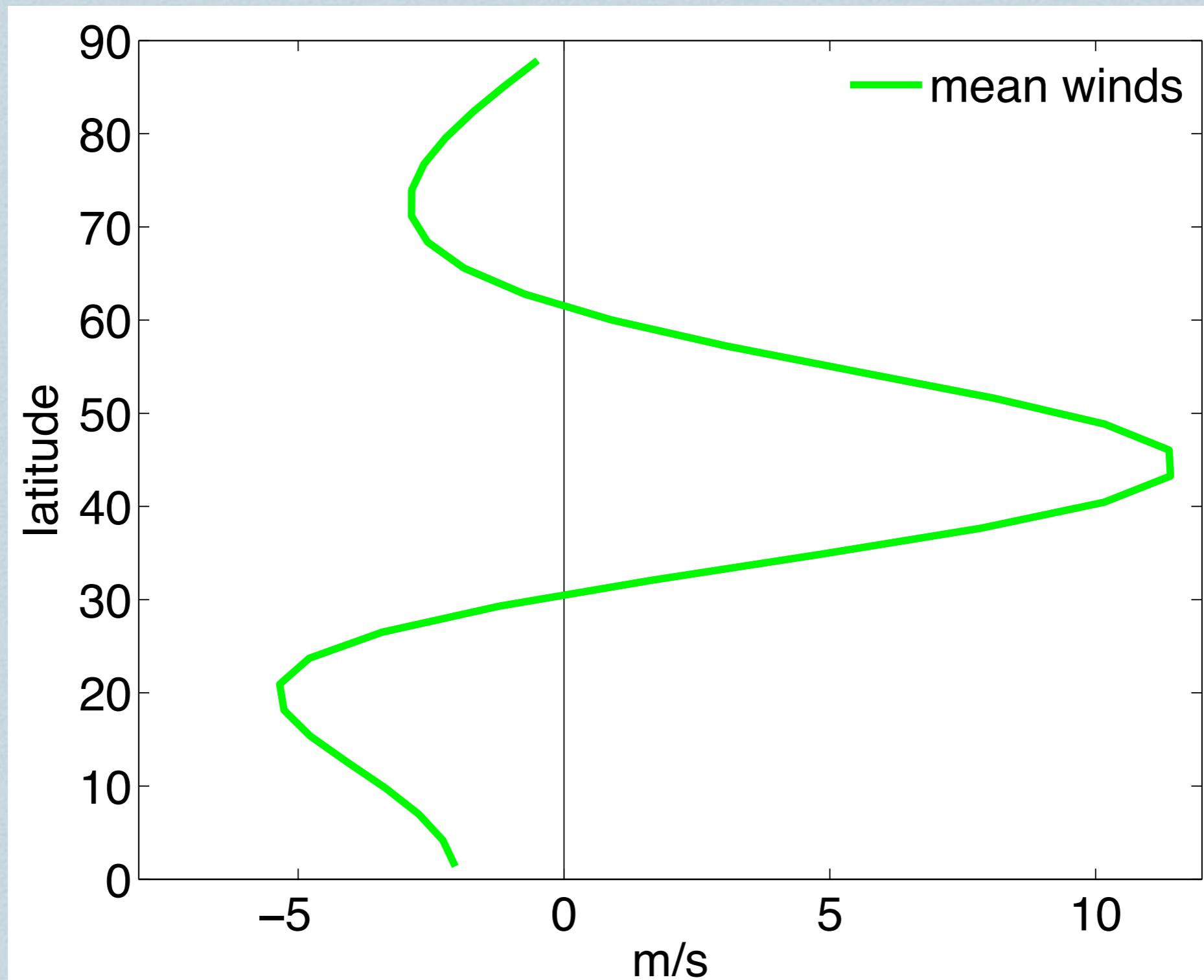
random perturbations
to the vorticity
forced in synoptic
wave numbers
in midlatitude
band;
perturbations
have no net
vorticity



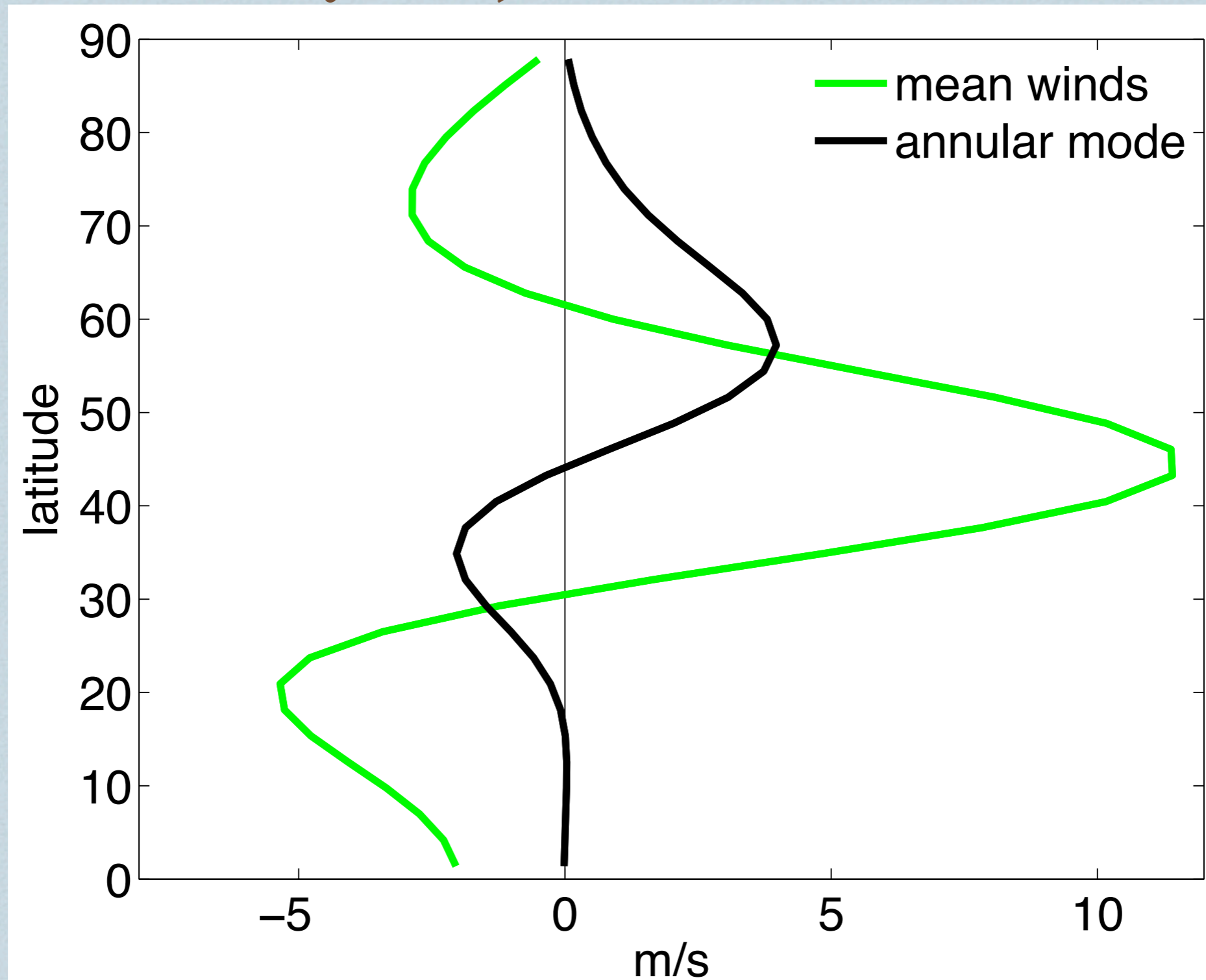
Numerical Simulations



Prototype Midlatitude Jet



Variability in stirring → Variability in jet (Annular Mode)



Simple Model of Annular Mode Time Scales

variations in zonal mean driven by variations in vorticity fluxes

$$\frac{\partial \bar{u}}{\partial t} = \overline{v' \zeta'} - r \bar{u}$$

project \bar{u} anomalies onto AM, approx. forcing as white noise: looks like Ornstein-Uhlenbeck process (discrete analog AR-1)

$$\frac{dx}{dt} = \dot{W} - rx$$

Anomalies of zonal mean winds are the integral of the vorticity fluxes created by baroclinic eddies, hence will have **redder spectrum** of variability!

Simple Model of Annular Mode Time Scales

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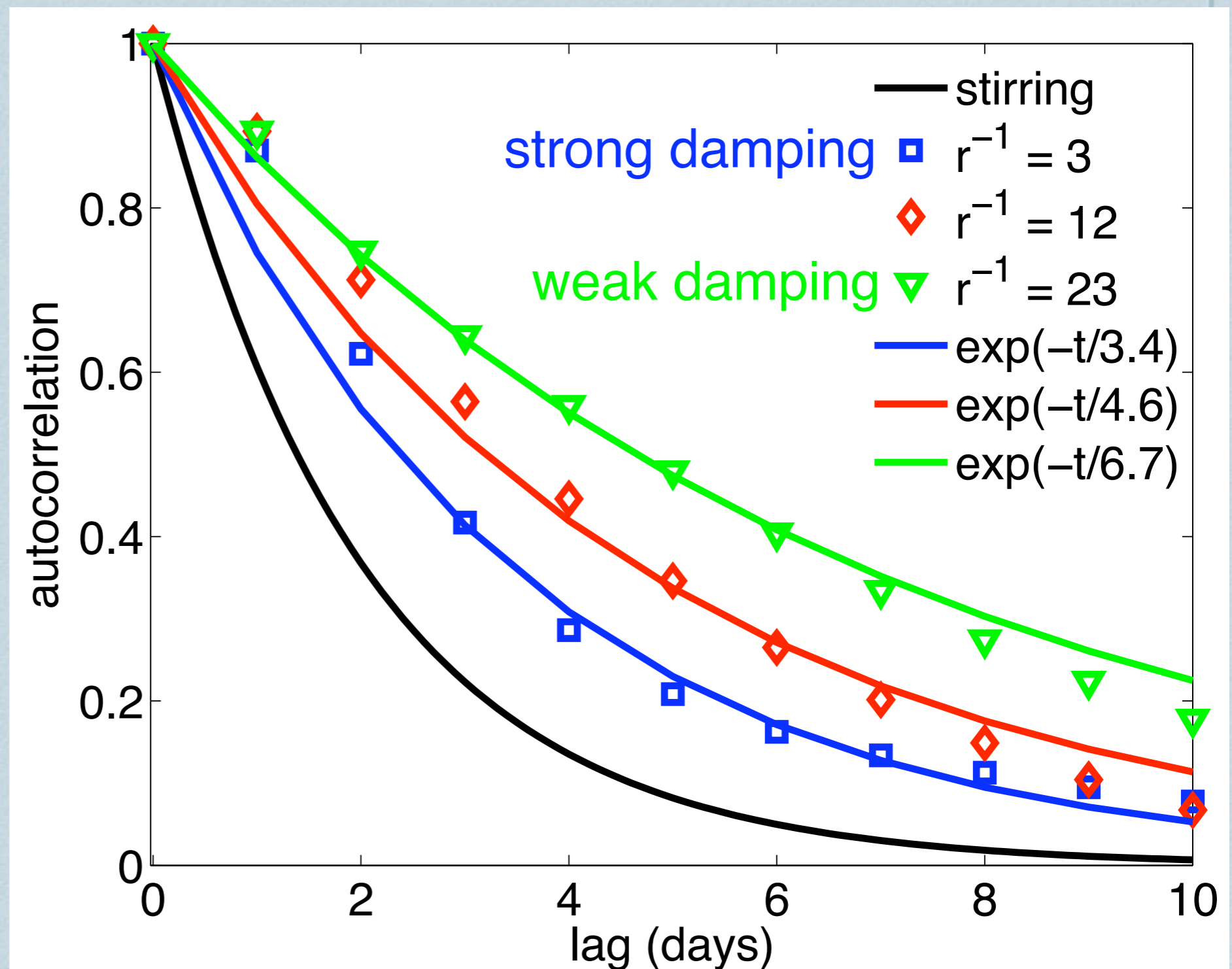
$$\frac{dx}{dt} = \dot{W} - rx$$

Anomalies of zonal mean winds are the integral of the vorticity fluxes created by baroclinic eddies, hence will have **redder spectrum** of variability! Friction will bound variability on low frequencies.

Model Results: Exponential-ish Decay, like AR-1 Process

decrease the
damping,
increase the
time scales

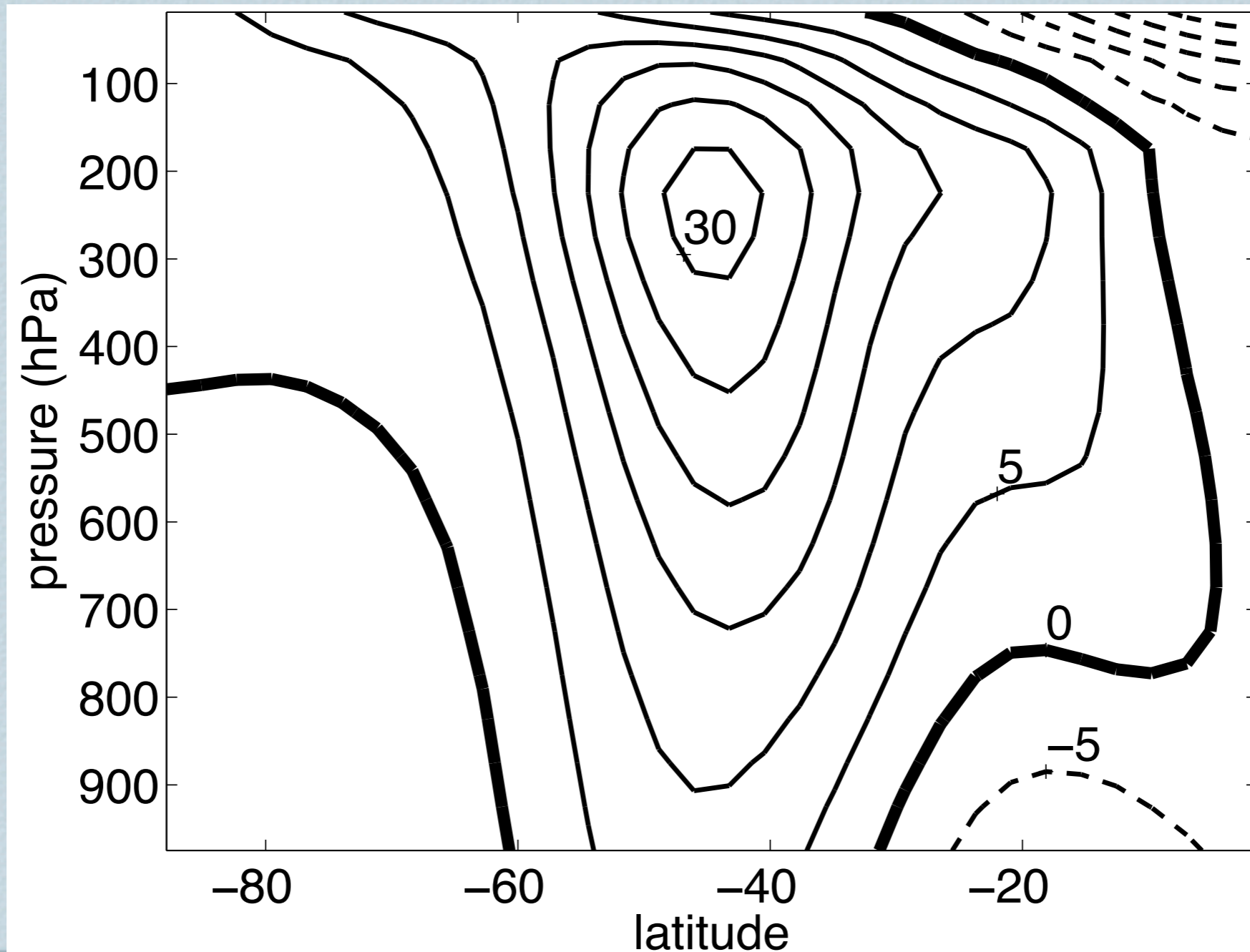
non-linear
interactions
limit time
scales



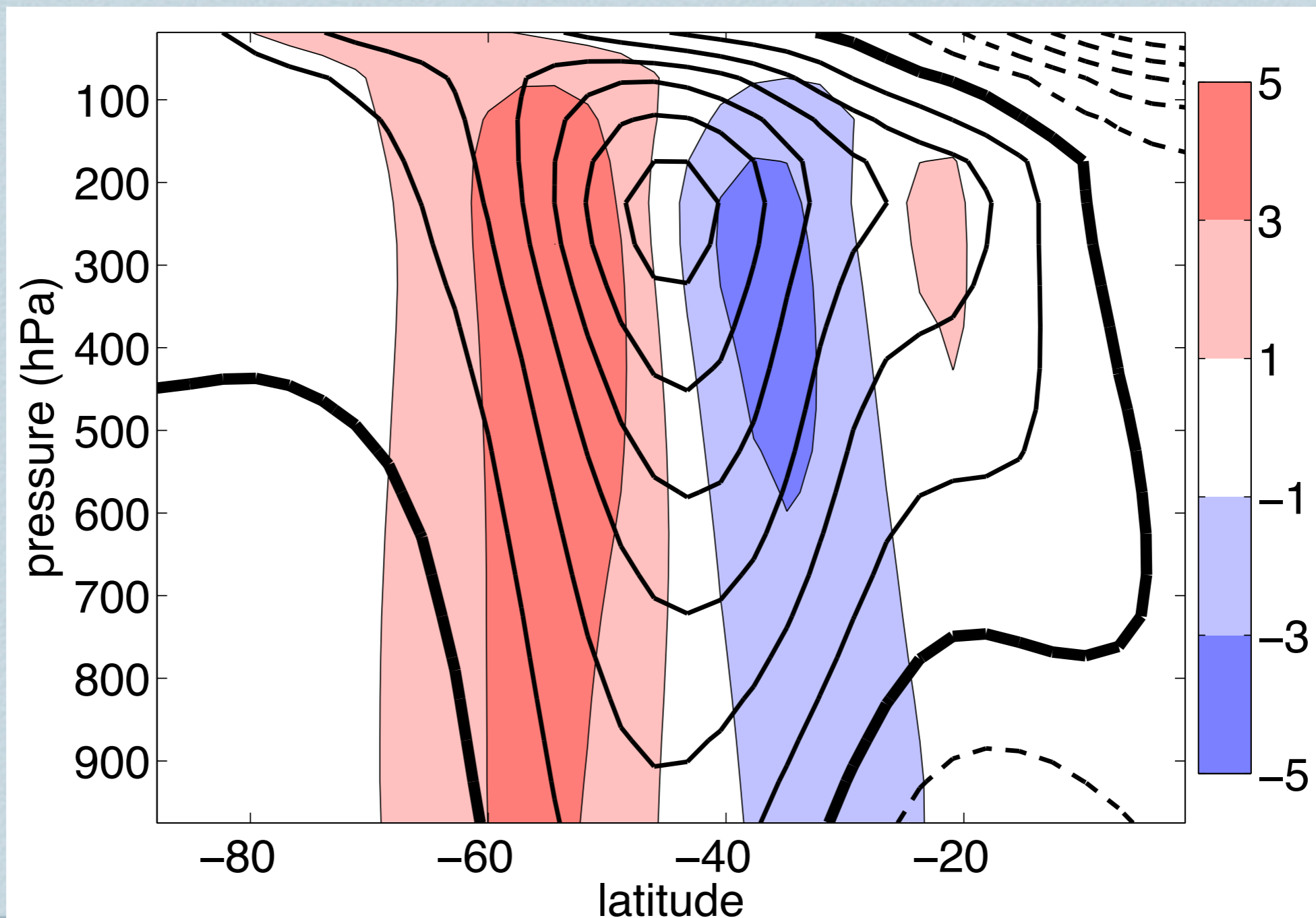
Interactive Stirring: Dynamical Core

- ❖ Vorticity “stirring” is generated by baroclinic instability, which is a function of jet structure. **Potential for positive feedbacks!**
(Lorenz and Hartmann 2001, 2003)
- ❖ Dynamical core integrates 3-D primitive equations, captures baroclinic instability
- ❖ Forced by Held-Suarez simplified physics (Newtonian relaxation to radiative-convective equilibrium)

Held-Suarez Jet Structure



Held-Suarez Jet Structure and Annular Mode

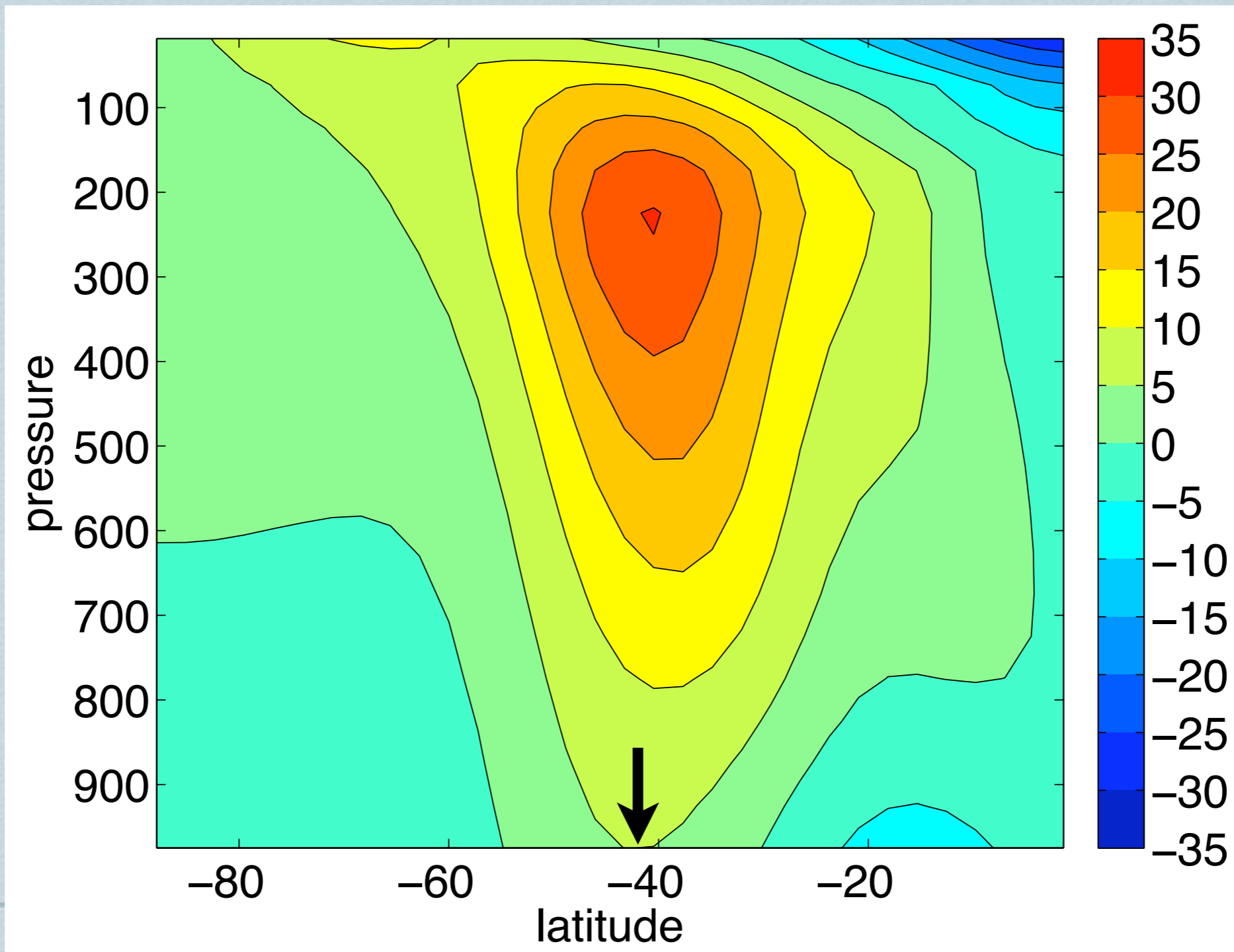


What determines time scale of Annular Mode in this system?

- ❖ First, systematically vary Held-Suarez forcing parameters
 - ❖ Thermal restoring time scale $k_a^{-1}=40$ days: $\frac{dT}{dt} = \dots - k_a(T - T_{eq})$
 - ❖ Surface friction $k_f^{-1}=1$ day: $\frac{du}{dt} = \dots - k_f \frac{p/p_s - 0.7}{0.3} u, p/p_s > 0.7$
 - ❖ baroclinic growth of eddies (heat fluxes) effect vertical momentum transport on synoptic time scale of 6-8 days; to modulate baroclinicity, vary equator-to-pole temperature gradient of equilibrium profile: ΔT_{eq}
- ❖ Second, investigate impact of zonal asymmetries (more appropriate for the NH)

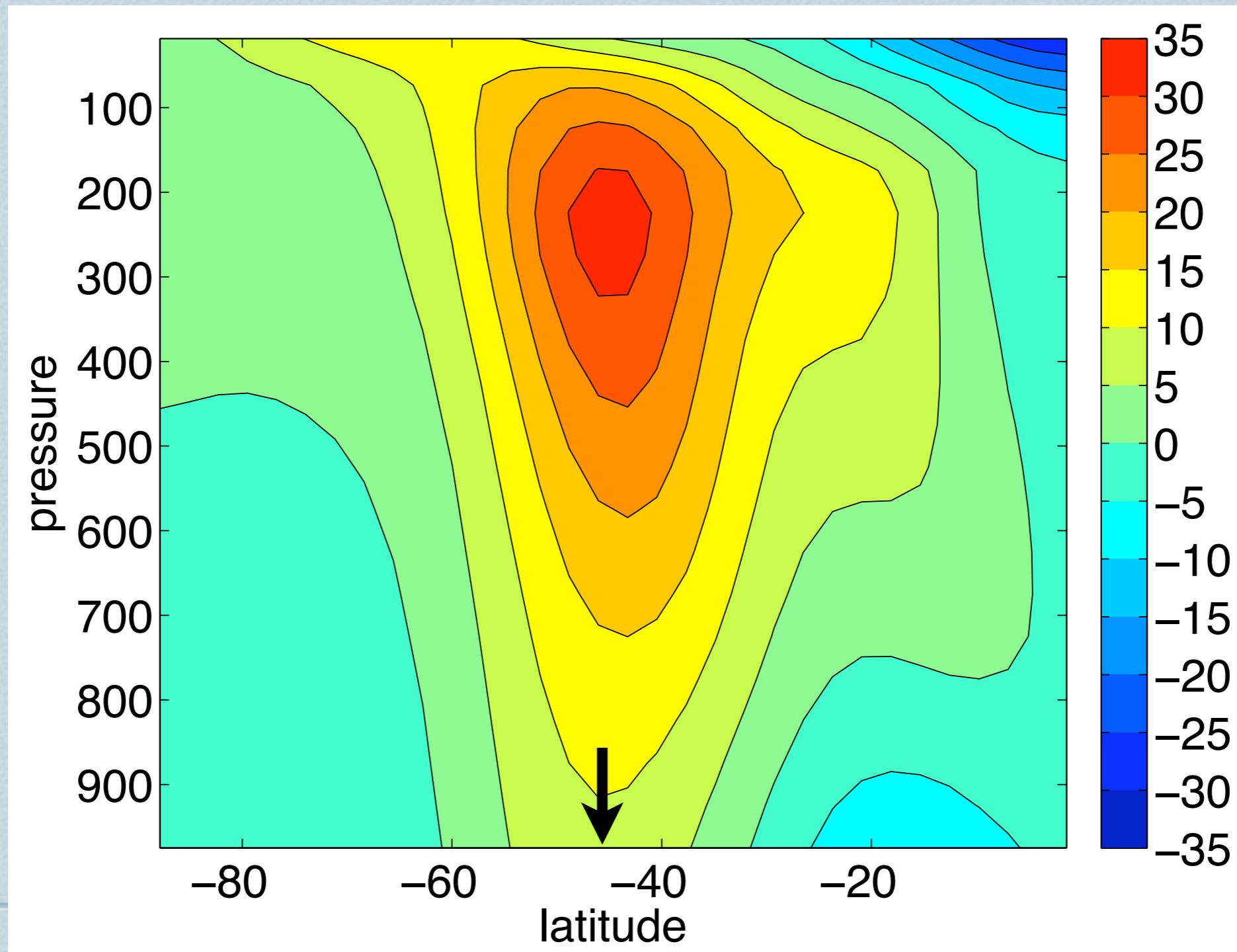
Vary Surface Friction

$$k_f = 4/3 \text{ day}^{-1}$$



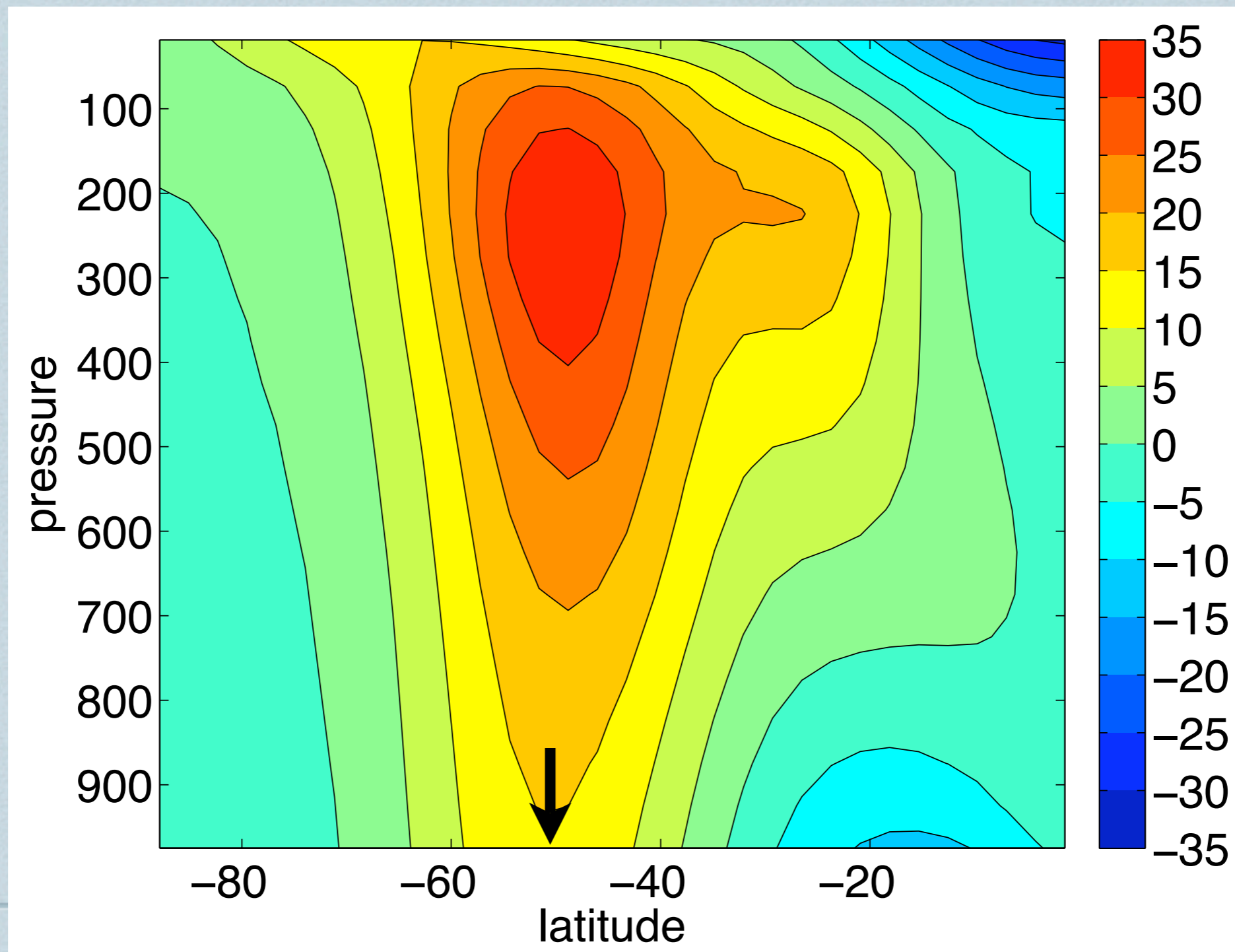
Vary Surface Friction

$$k_f = 1 \text{ day}^{-1}$$

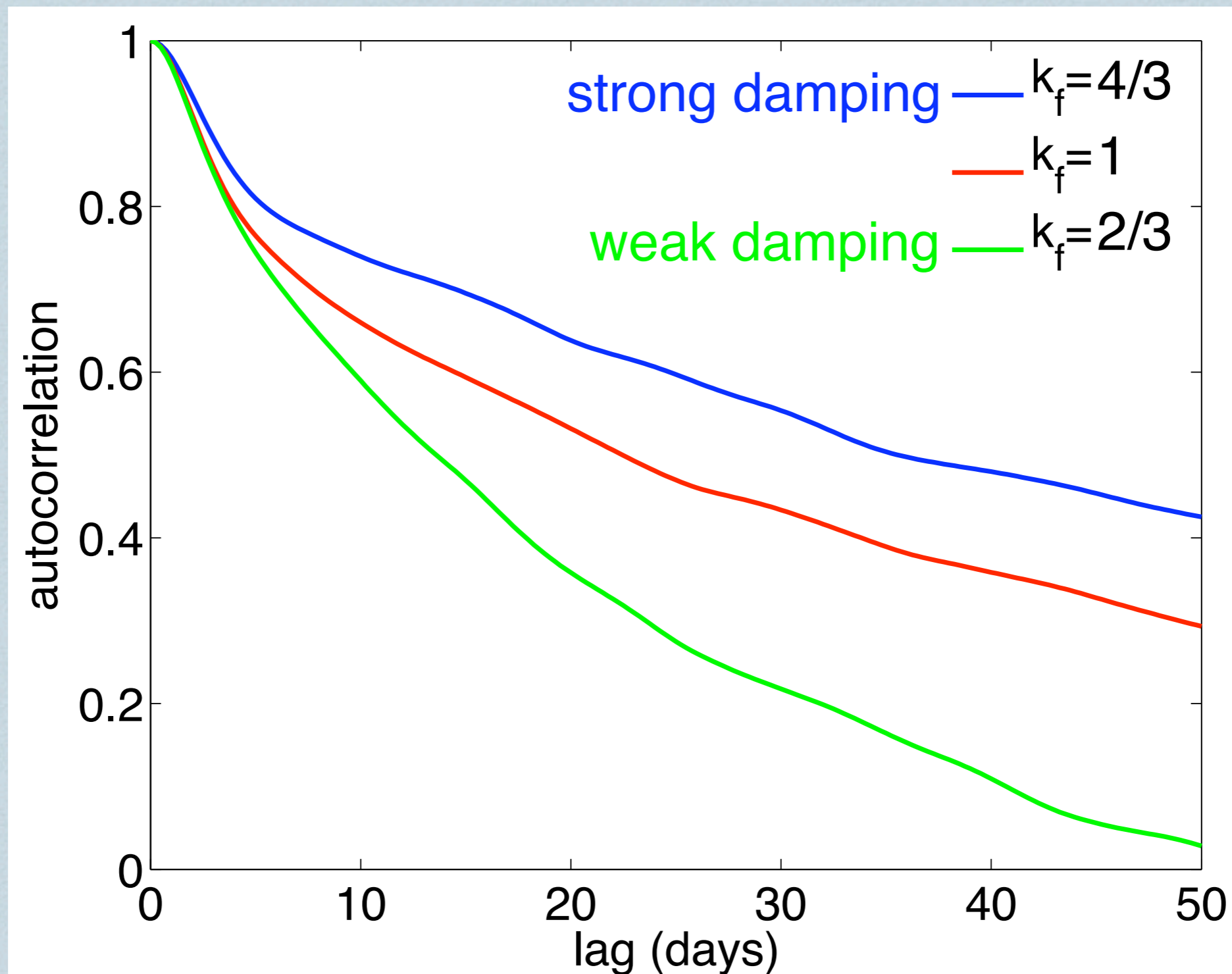


Vary Surface Friction

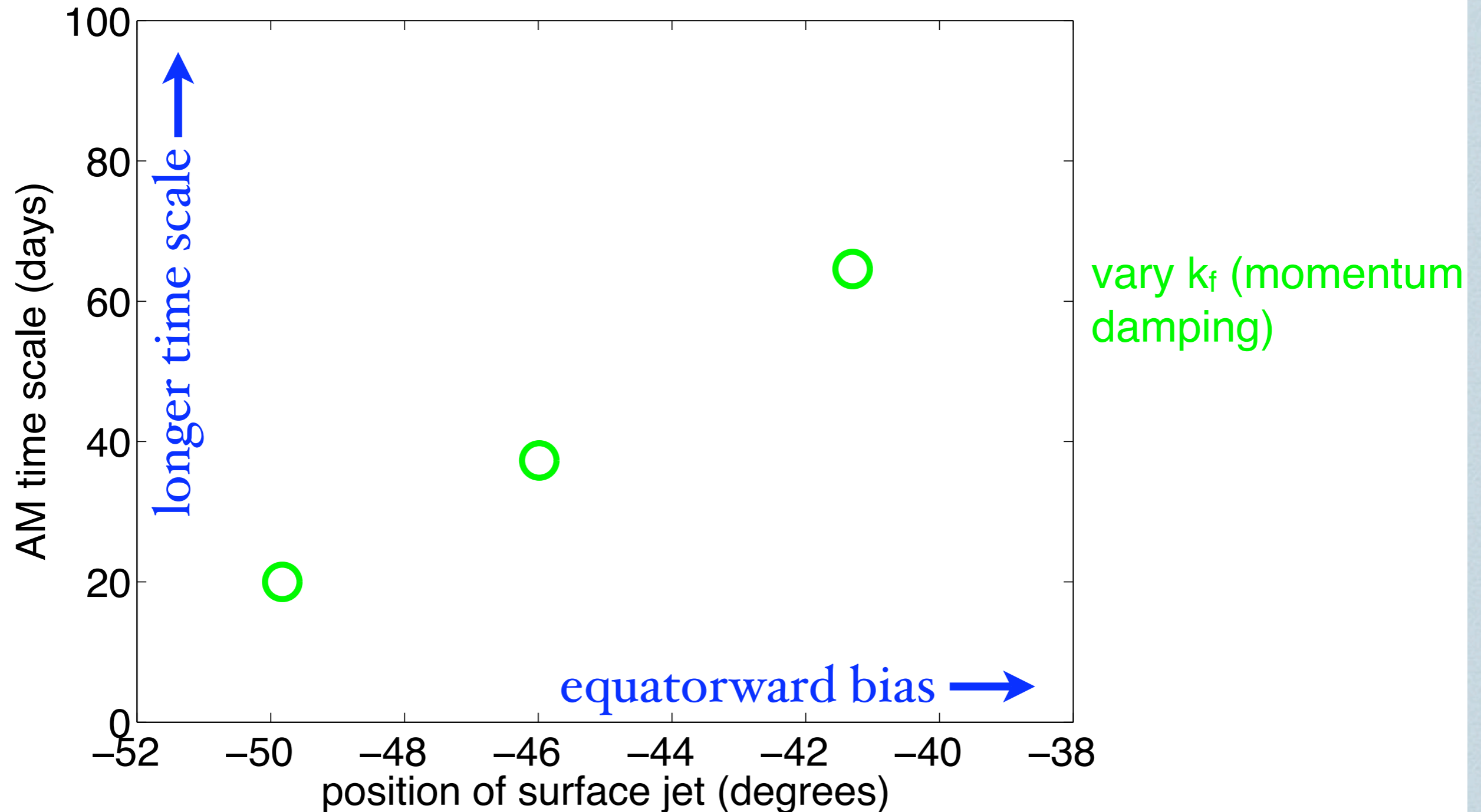
$$k_f = 2/3 \text{ day}^{-1}$$



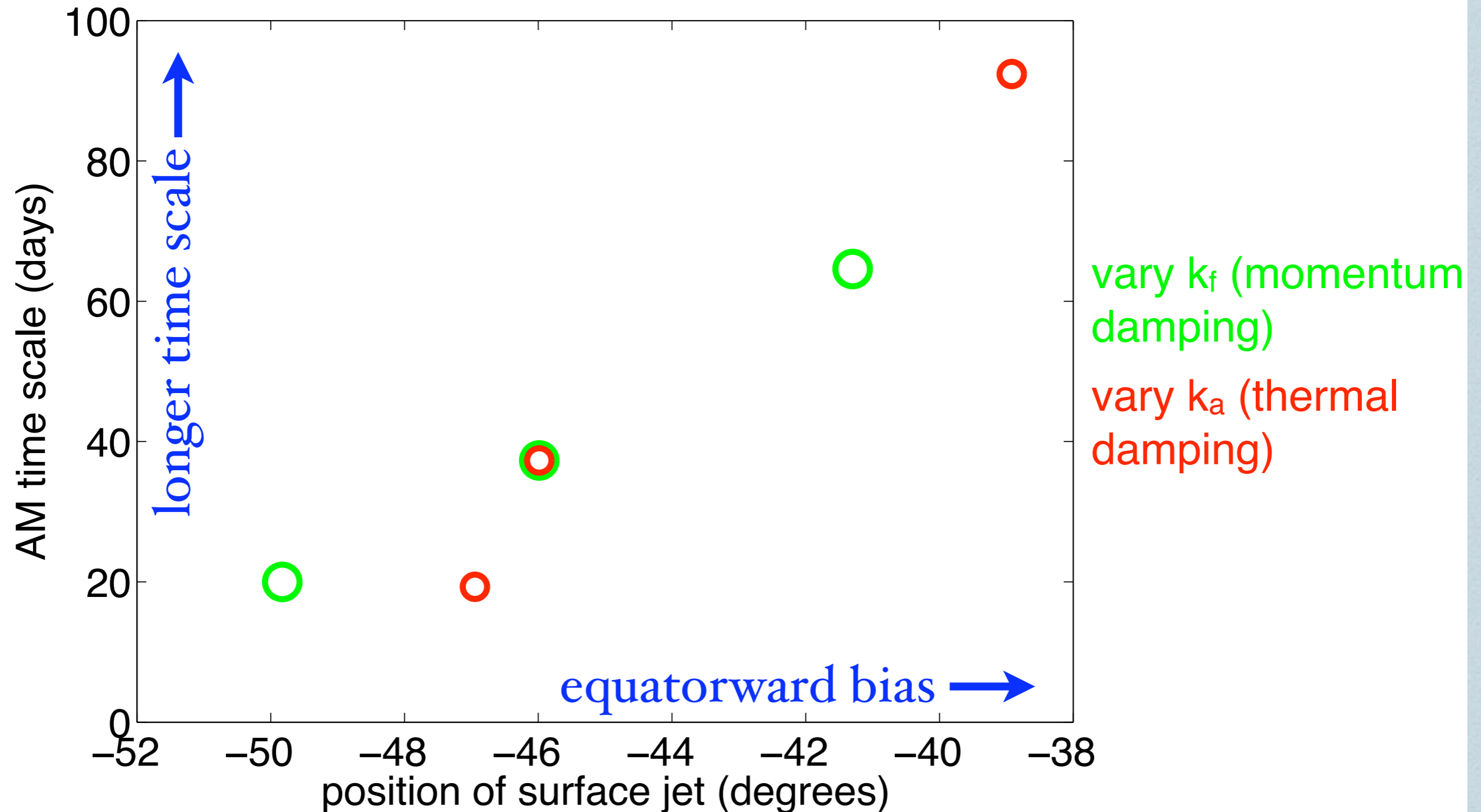
AM autocorrelation structure: stronger damping = greater persistence!



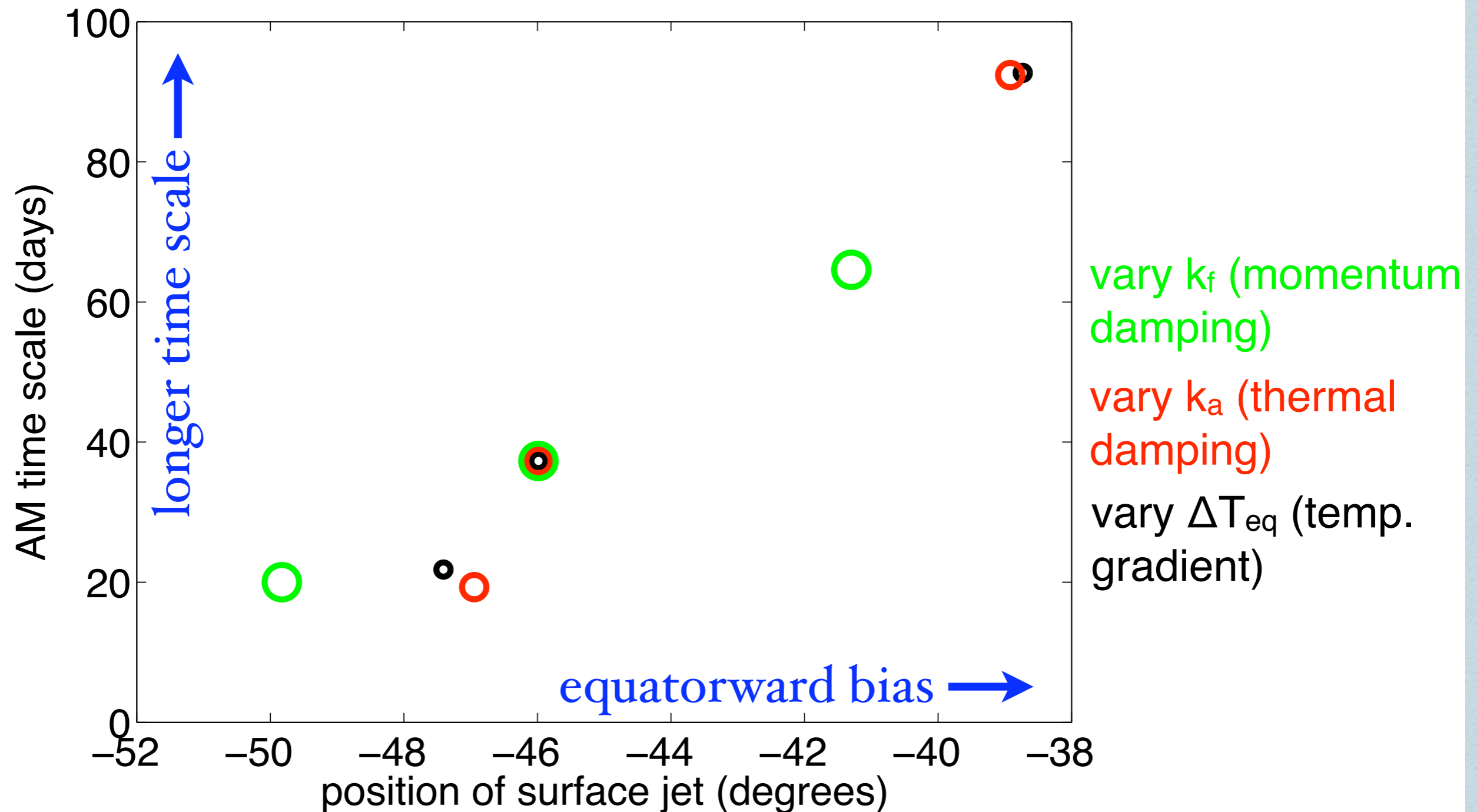
Annular Mode Time Scale - Jet Latitude Connection



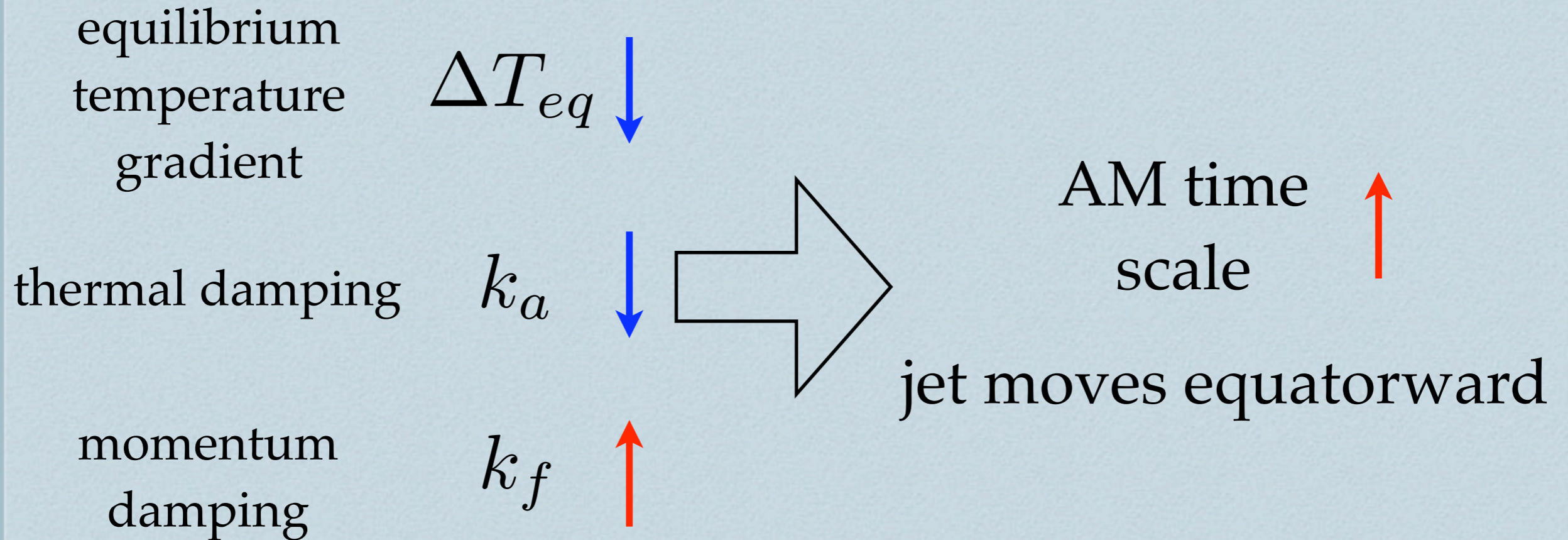
Annular Mode Time Scale - Jet Latitude Connection



Annular Mode Time Scale - Jet Latitude Connection



Summary of Parameter Impacts



Implications:

- 1) AM time scale is distinct from the imposed time scales, rather a product of eddy-mean flow interactions
- 2) processes that set jet location also set AM time scale

Simple Model of Feedback

(after Lorenz and Hartmann 2001)

variation in
annular mode
index $z(t)$

$$\frac{dz}{dt} = \dot{W} - \frac{z}{\tau} + bz$$

stochastic
"eddy" forcing

frictional
damping

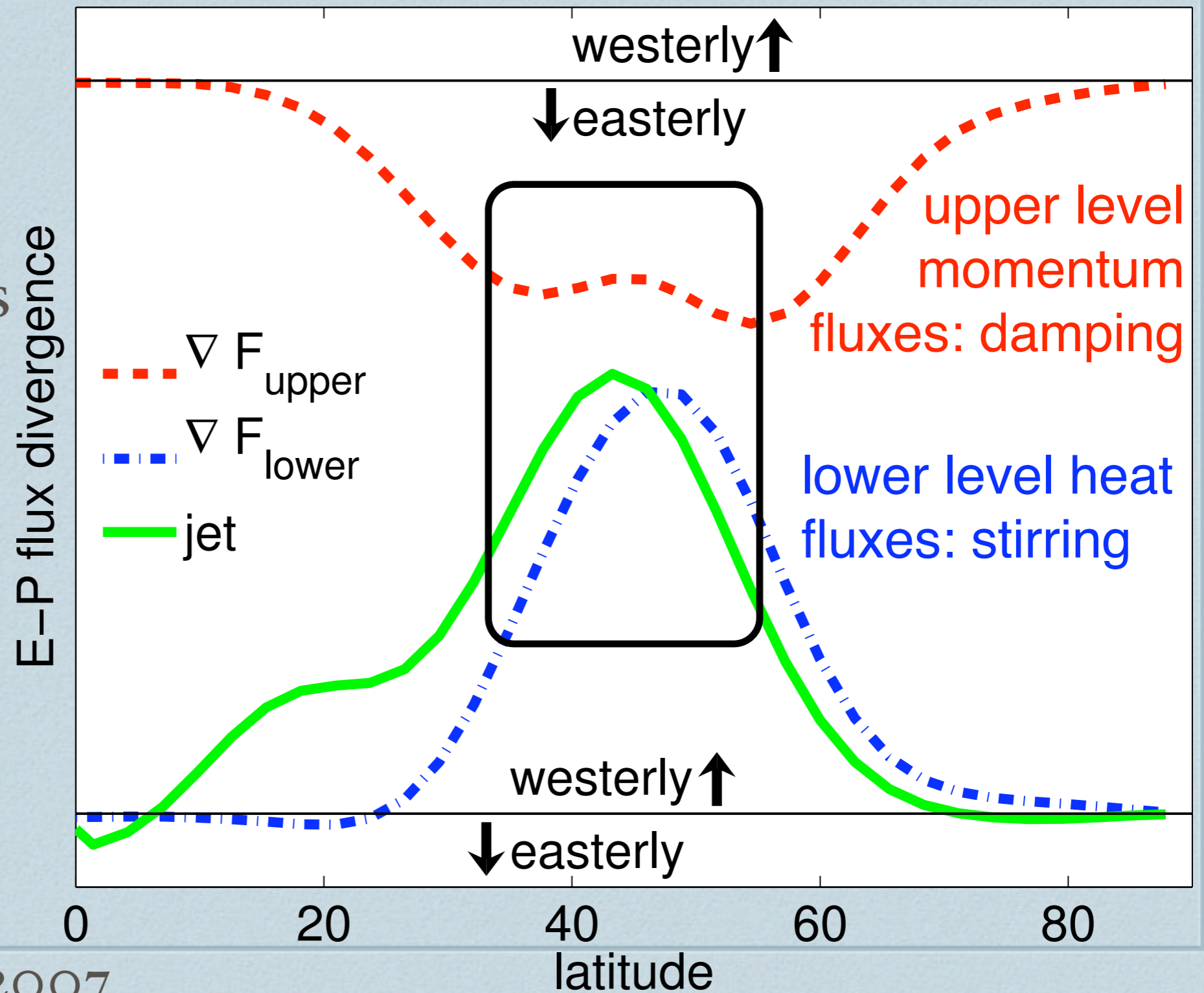
positive feedback
btw jet and eddies

Net effect of
feedback is new
time scale τ_2

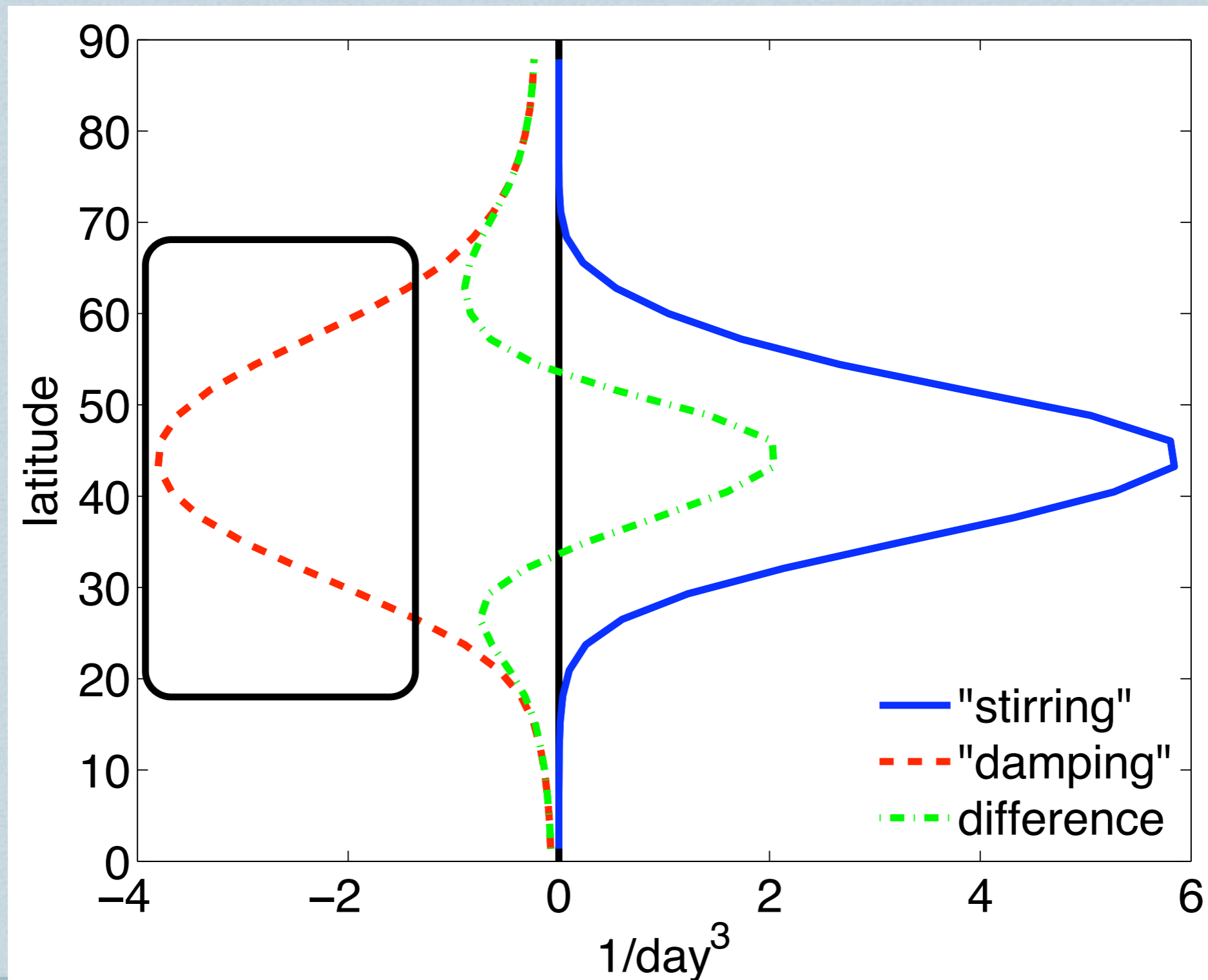
$$\frac{dz}{dt} = \dot{W} - \frac{z}{\tau_2}, \quad \tau_2 = (\tau^{-1} - b)^{-1}$$

Schematic of the Feedback: “Self Maintaining jet” (Robinson 2006)

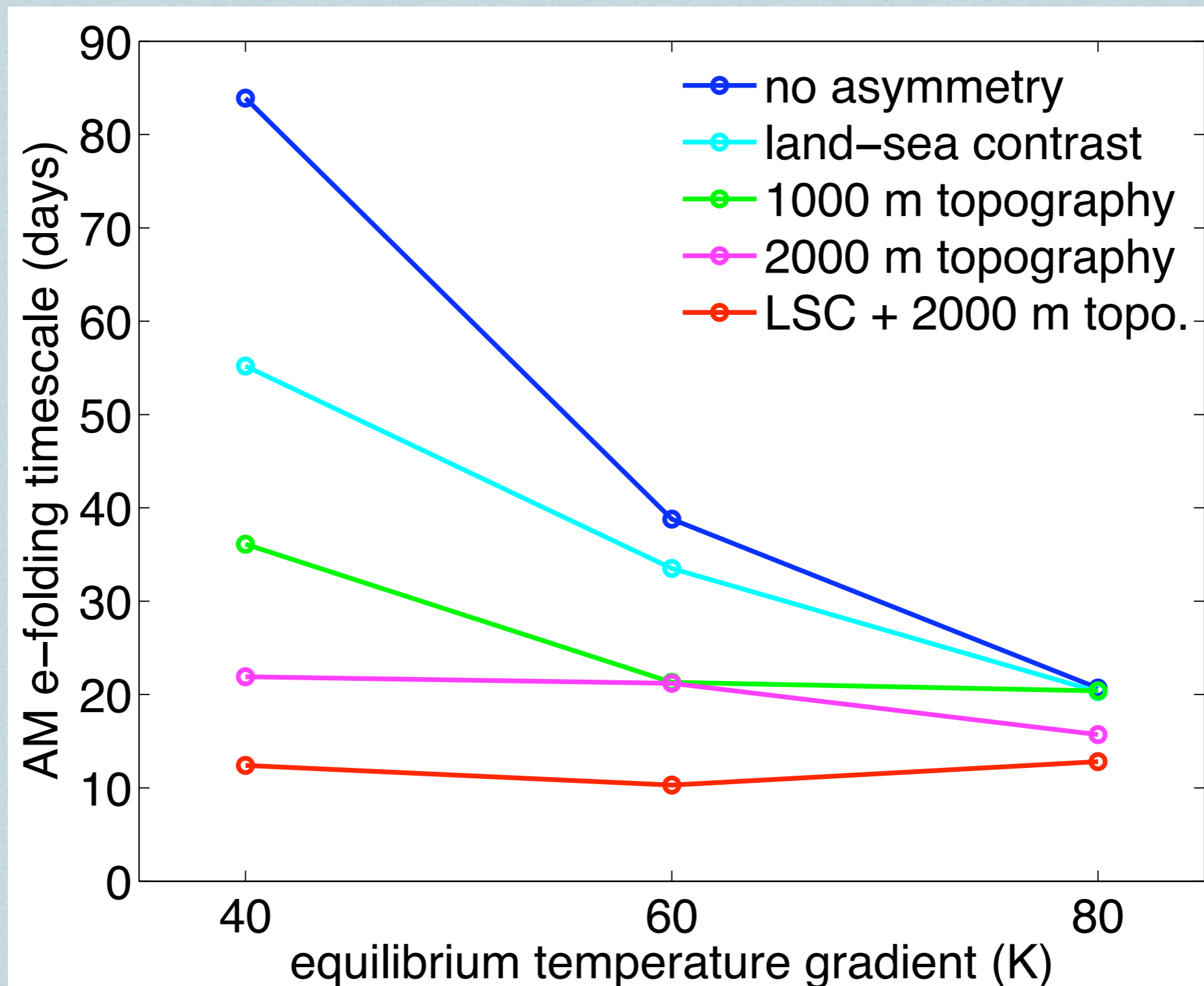
Key to feedback:
upper level winds
steer Rossby
waves out of the
jet core, thus
maintaining the
baroclinicity



Barotropic Vorticity Dynamics



Zonal Asymmetries Eliminate Parameter Sensitivity (Destroy Feedbacks!)

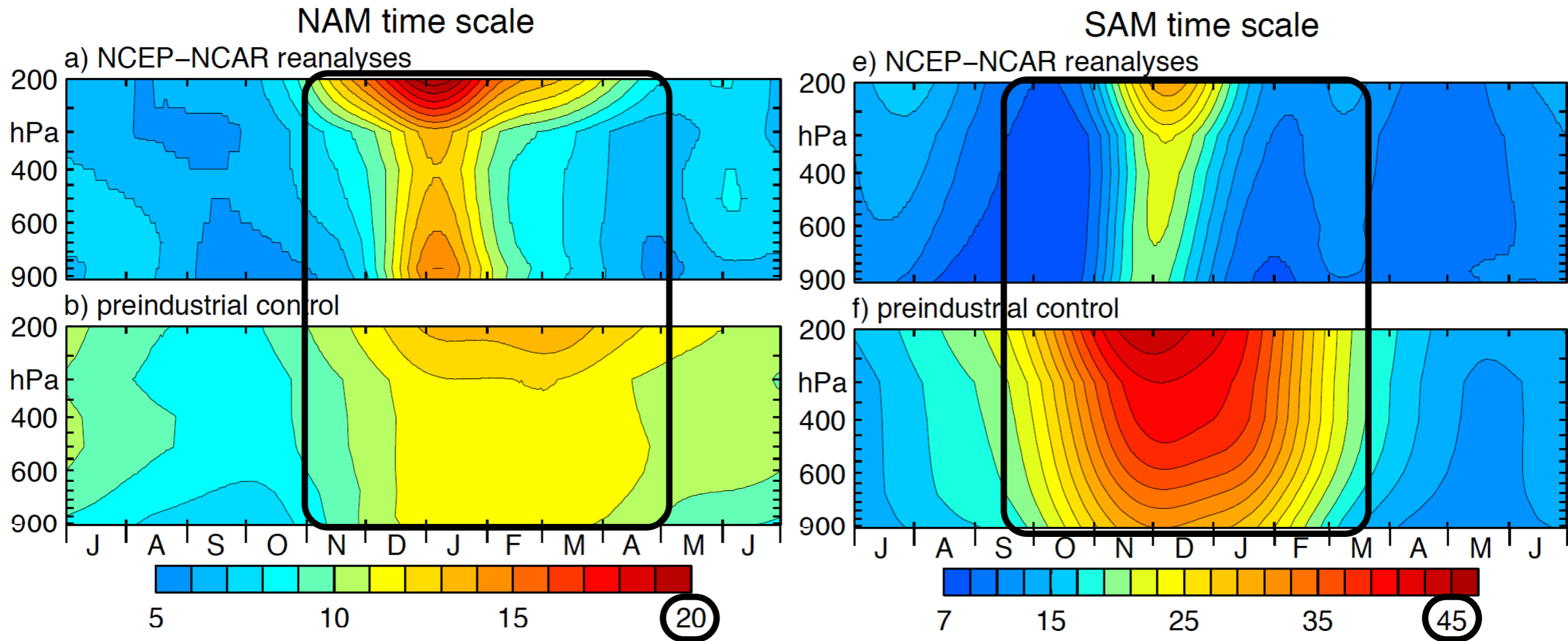


How does this relate to the real atmosphere?

- ❖ Simple model time scales very sensitive to many things
- ❖ Zonal asymmetries (as found in “real” world) seem to take away these problems

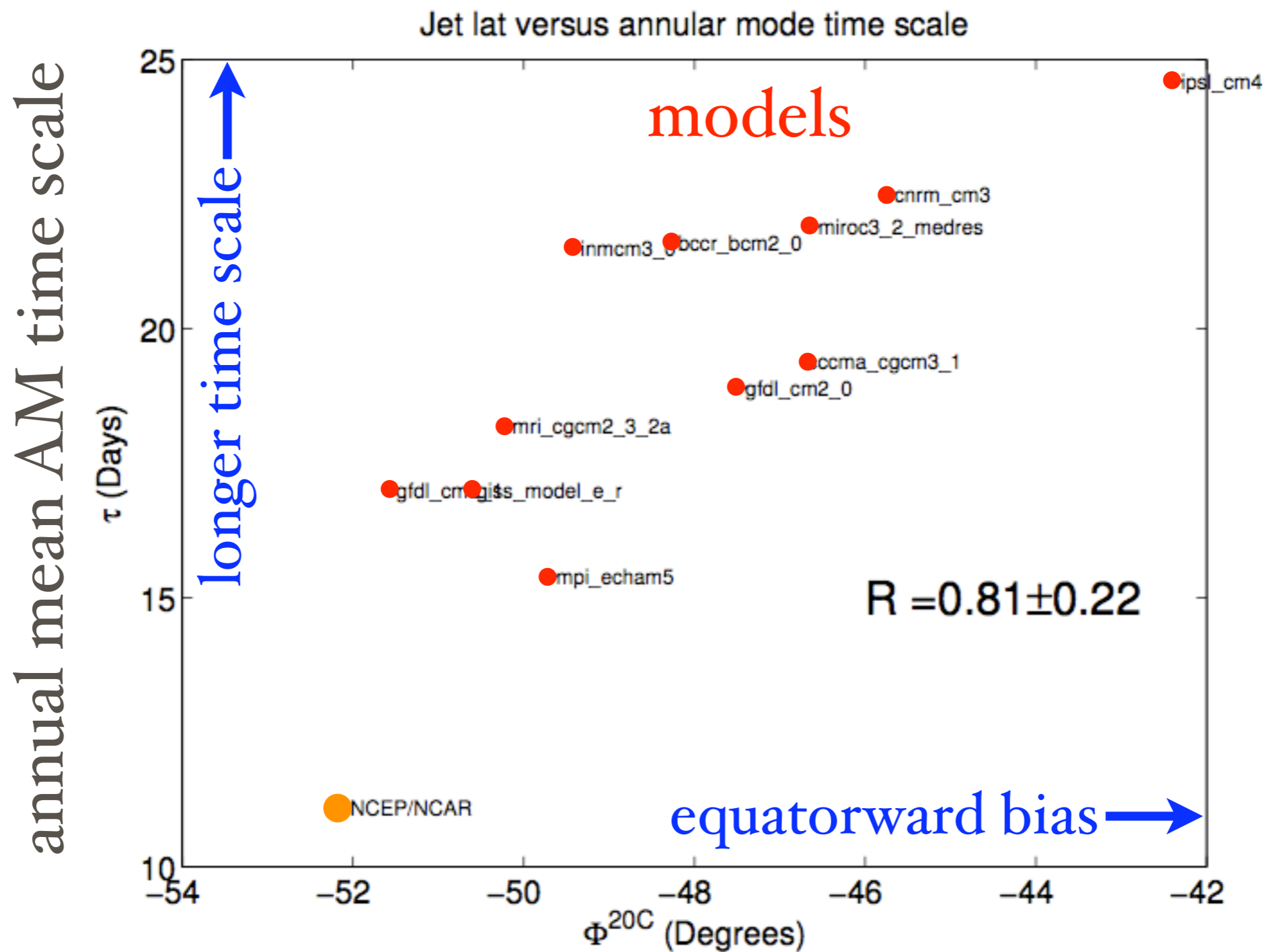
Move to comprehensive climate models

IPCC AR₄ Models: Ensemble Mean Performance



- 1) models have trouble with amplitude of SH time scales
- 2) models have trouble with sharpness of seasonal cycle

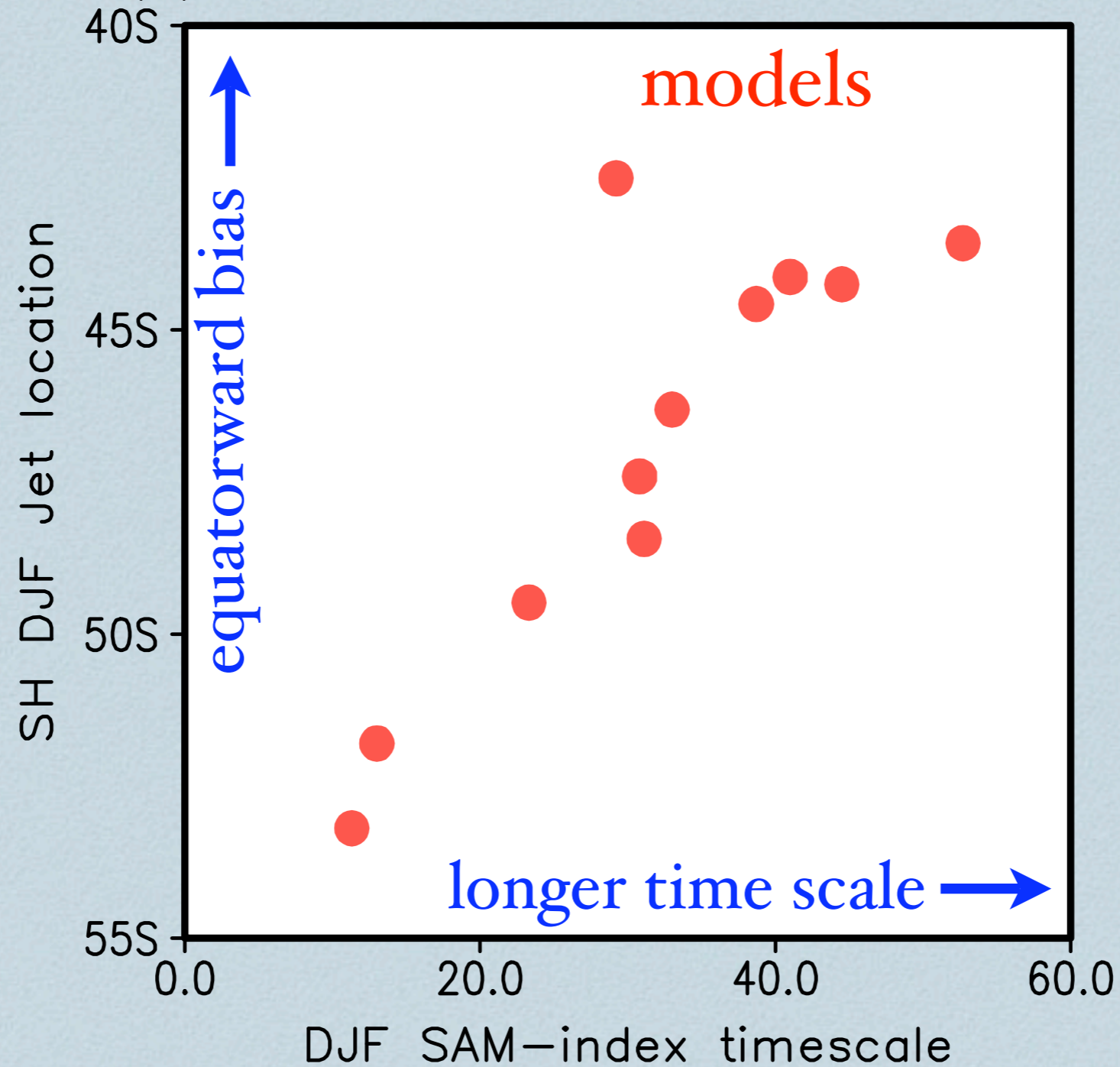
IPCC: Time scale - Jet lat. Connection



position of jet in 20th century control runs

Chemistry Climate Models

(b) SAM timescale vs. Jet location



(axes flipped)

Why are SH time scales so hard to simulate?

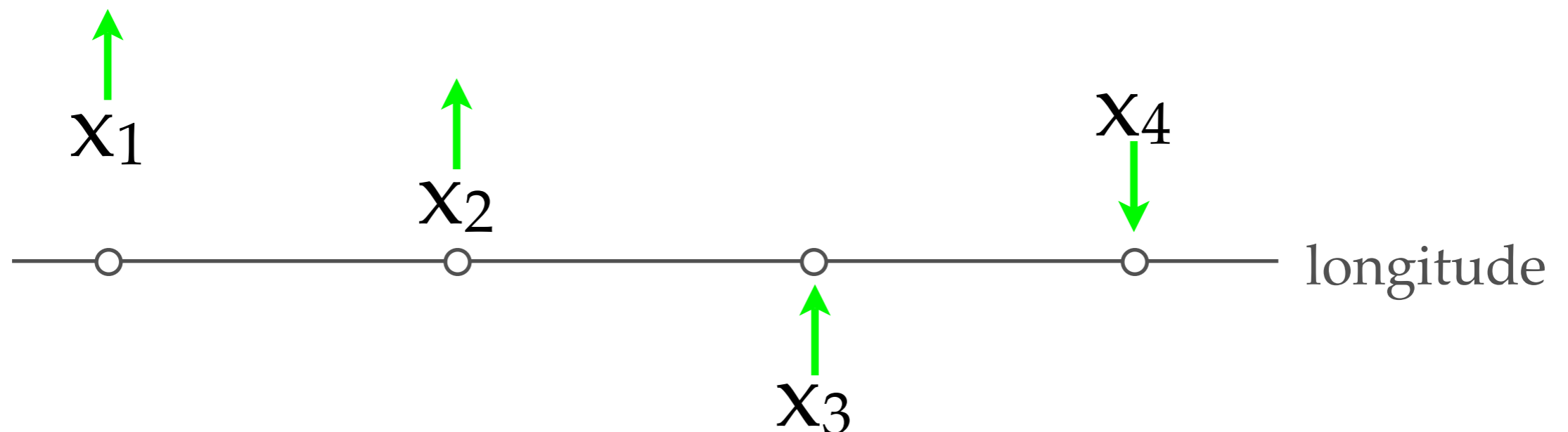
- ❖ In idealized GCMs w/ little zonal asymmetry and full model integrations of SH, feedbacks can lead to long time scales and large biases in jet location. Very sensitive to resolution, forcing, numerics, ...
- ❖ Increased zonal asymmetries appear very effective at reducing time scales in models (and constraining the location of the jet)

How do Zonal Asymmetries Prevent Strong Feedbacks?

Let x_i , the state of the zonal flow at $i=1, \dots, n$ representative longitudes, be determined by coupled stochastic oscillators. (Similar to Lorenz and Hartmann feedback, but spread in longitude.)

$$\frac{d}{dt} x_i = \dot{W}_i - \frac{x_i}{\tau} + b x_{i-1}$$

stochastic "eddy" forcing linear damping coupling with upstream flow

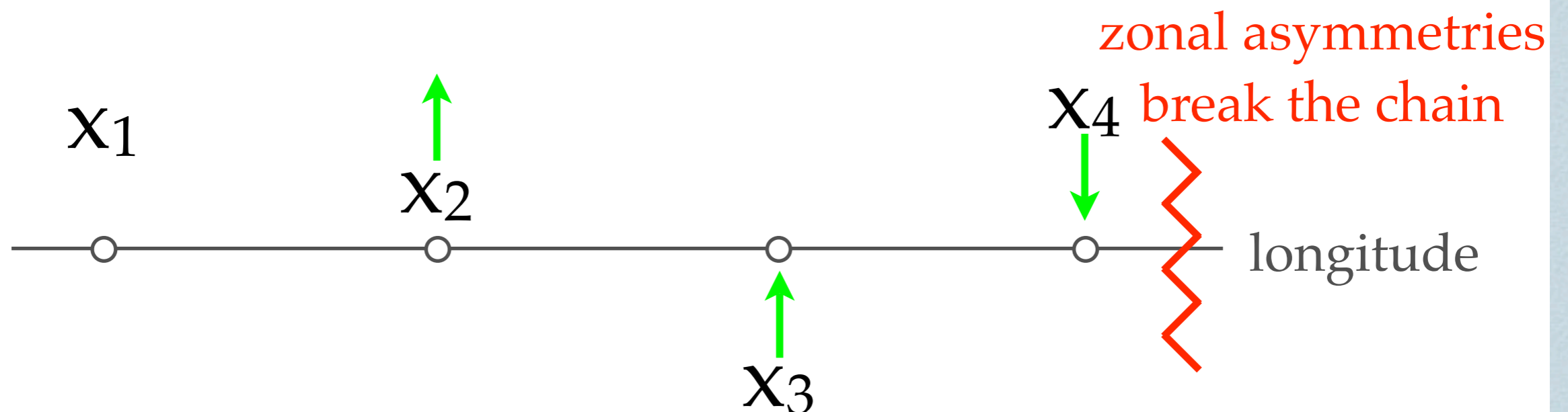


How do Zonal Asymmetries Prevent Strong Feedbacks?

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$$\frac{d}{dt} x_i = \dot{W}_i - \frac{x_i}{\tau} + b x_{i-1}$$

stochastic "eddy" forcing linear damping coupling with upstream flow



Time Scale of the Zonal Average

How does the short range feedback influence the “zonal average” signal?

$$z = \frac{1}{n} \sum_i x_i$$

In the zonally symmetric case, the spread of the interaction in longitude has no impact on the total persistence.

$$\begin{aligned} \frac{dz}{dt} &= \frac{1}{\sqrt{n}} \dot{W} - \frac{z}{\tau} + b z \\ &= \frac{1}{\sqrt{n}} \dot{W} - \frac{z}{\tau_2} \end{aligned}$$

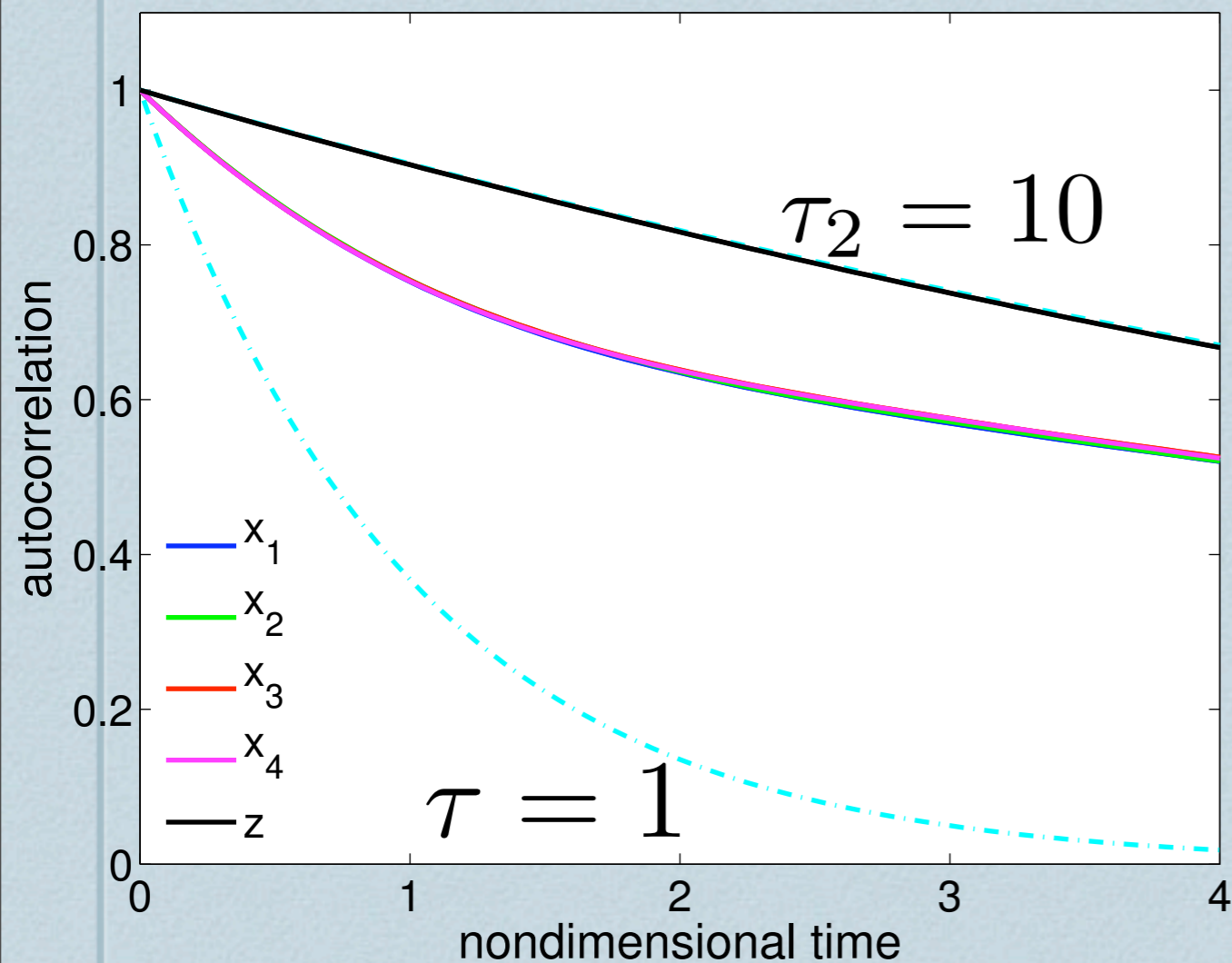
$$\tau_2 = (\tau^{-1} - b)^{-1}$$

What happens when the interaction is broken at one link? Simulations with $n=4$, $\tau = 1$, $\tau_2 = 10$.

Simulation Without Break

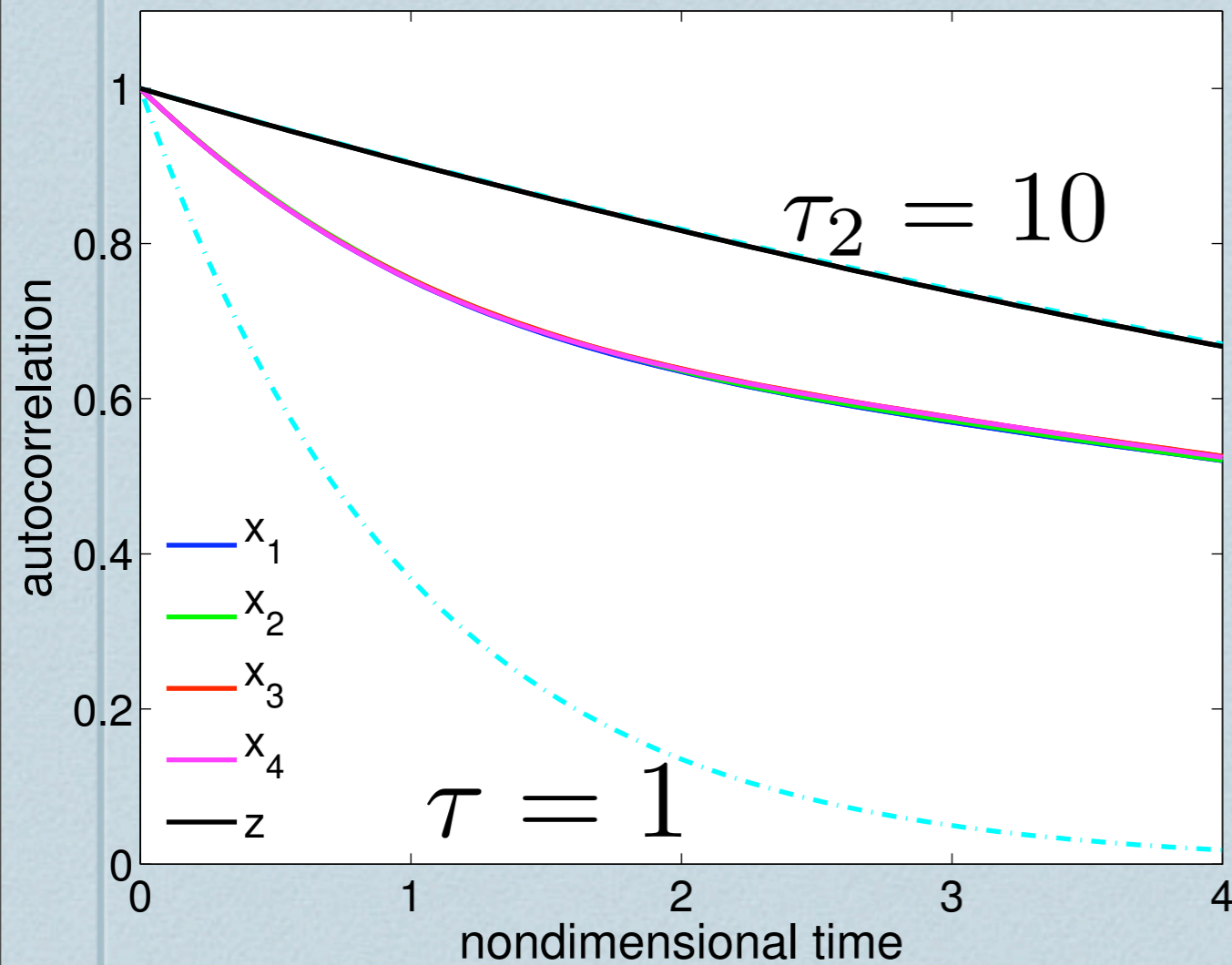
(verify the analytic result)

zonally symmetric model:
unbroken chain

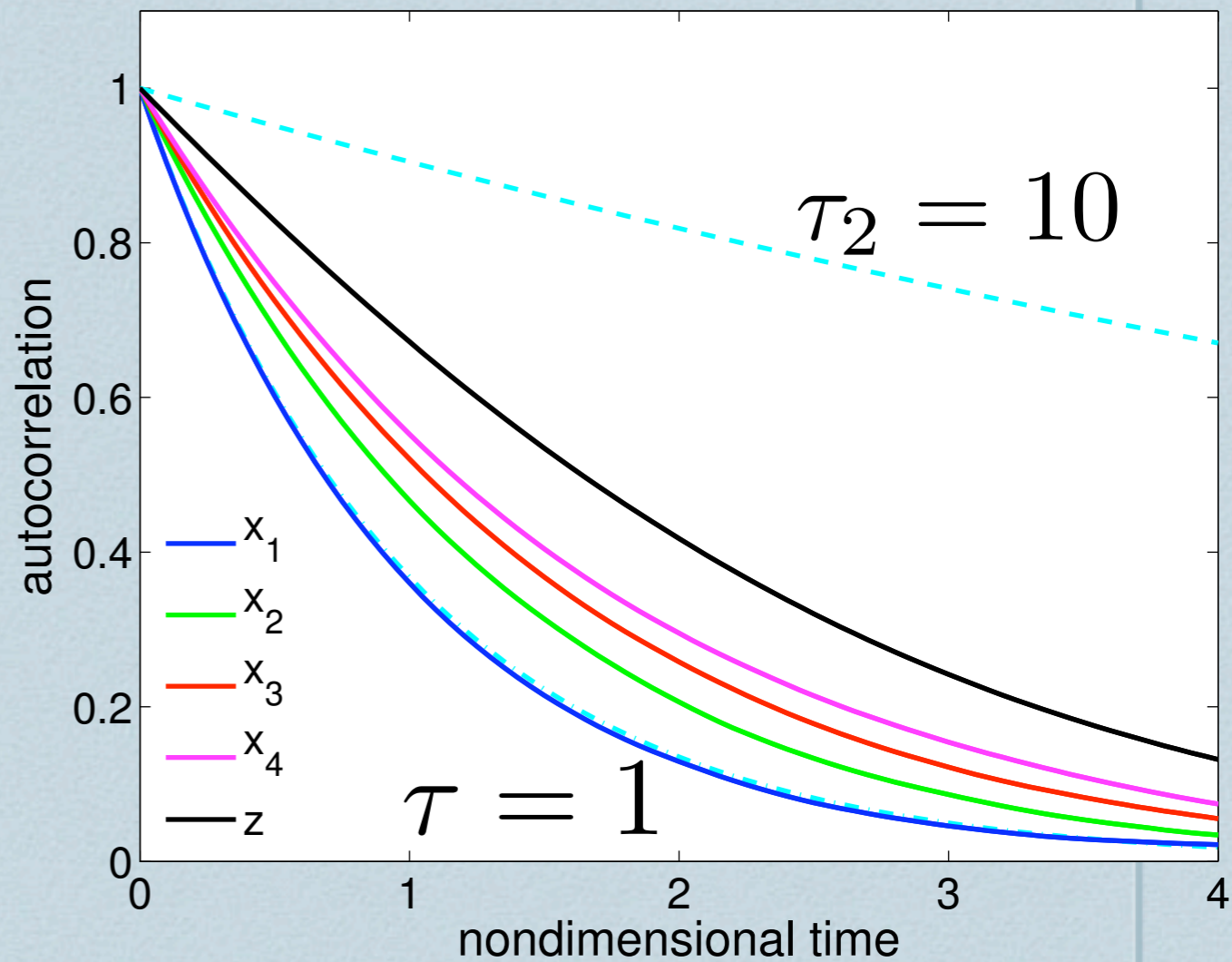


Break in Chain Kills Feedback

zonally symmetric model:
unbroken chain



no interaction between x_4
and x_1 : broken chain



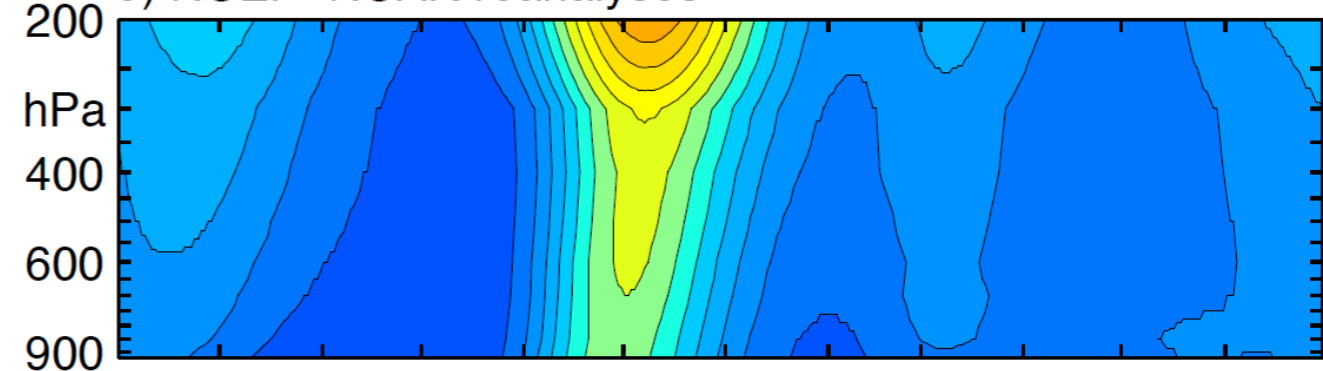
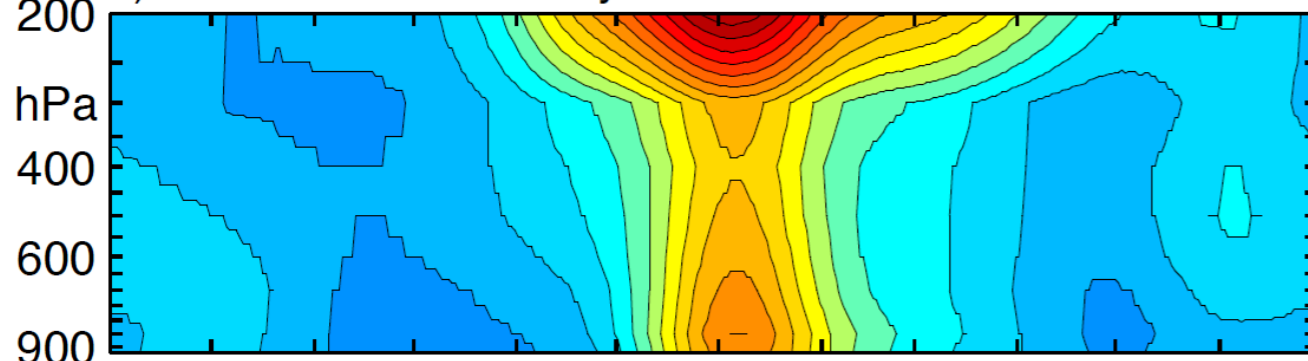
SH Much Harder to Simulate due to Potential for Positive Feedbacks

NAM time scale

SAM time scale

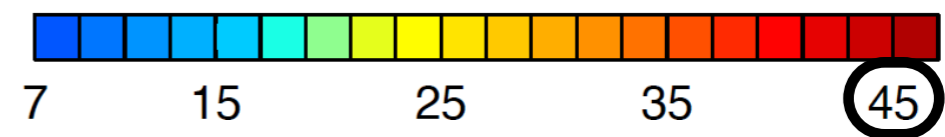
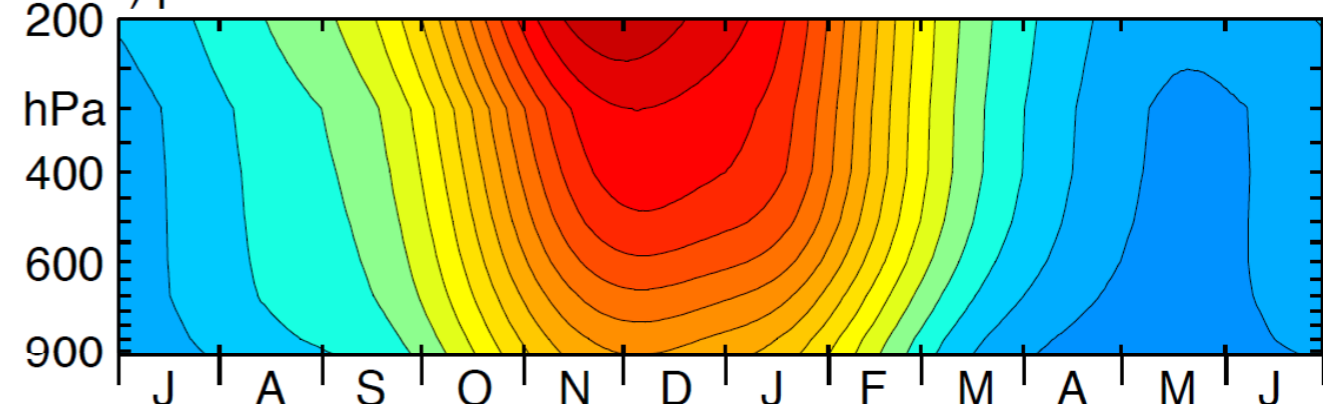
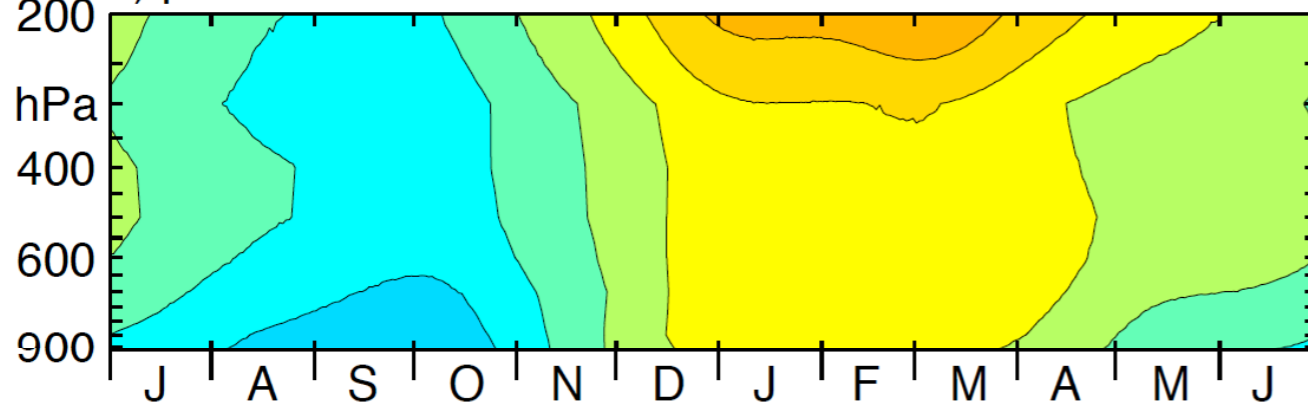
a) NCEP-NCAR reanalyses

e) NCEP-NCAR reanalyses



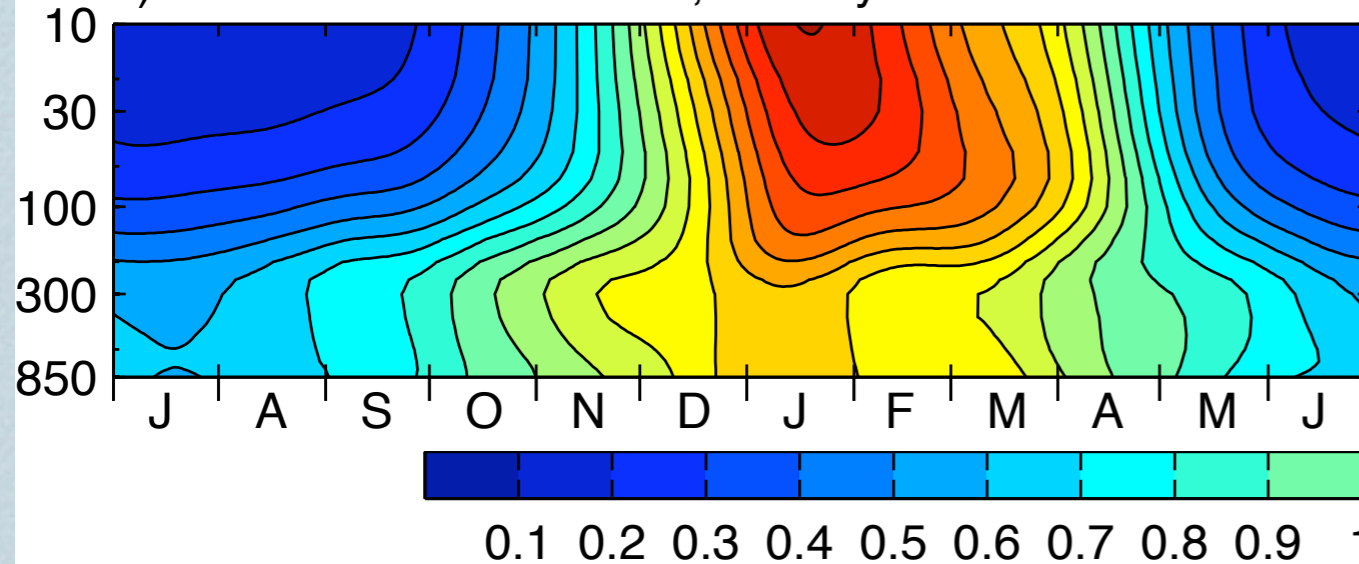
b) preindustrial control

f) preindustrial control

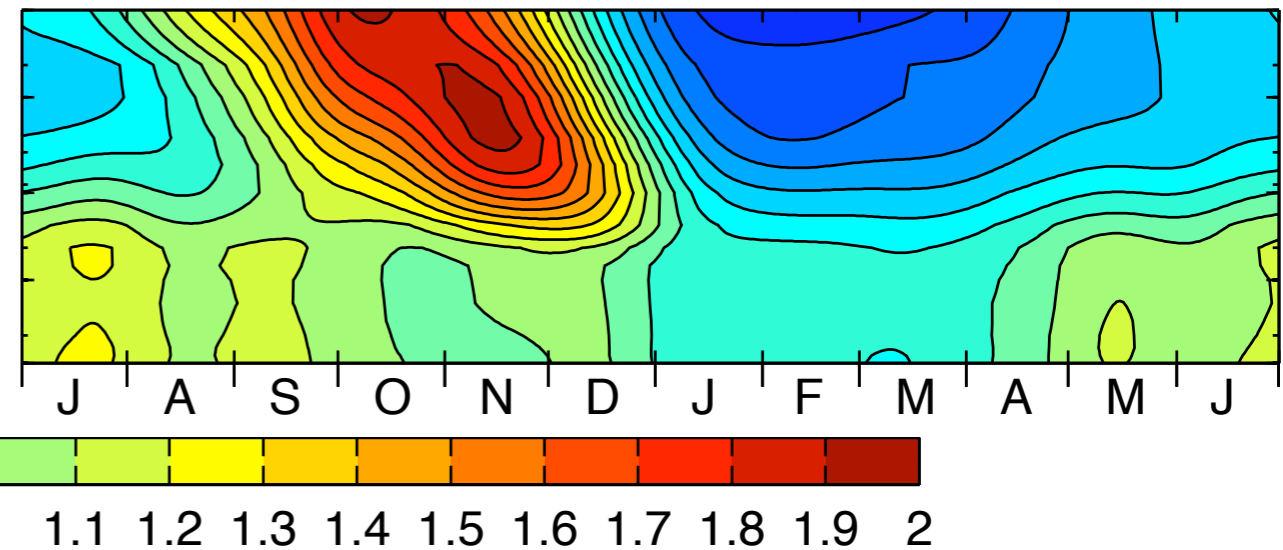


(2) Seasonal Cycle: Stratospheric Variability and Tropospheric Persistence

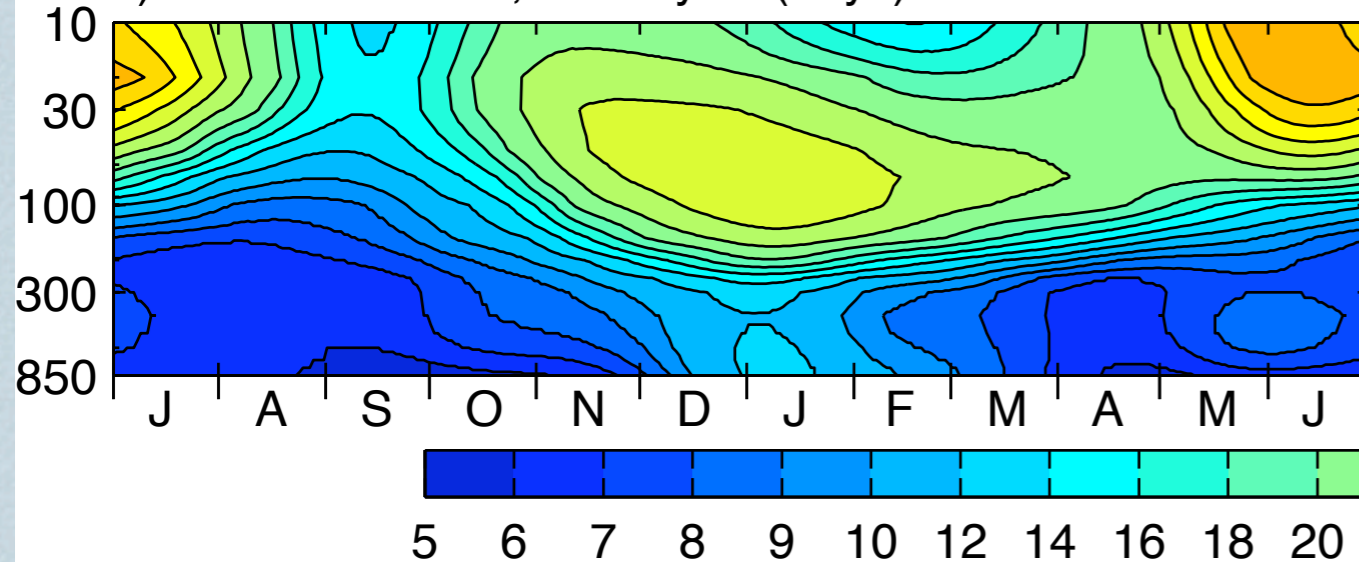
a) NAM standard deviation, reanalysis



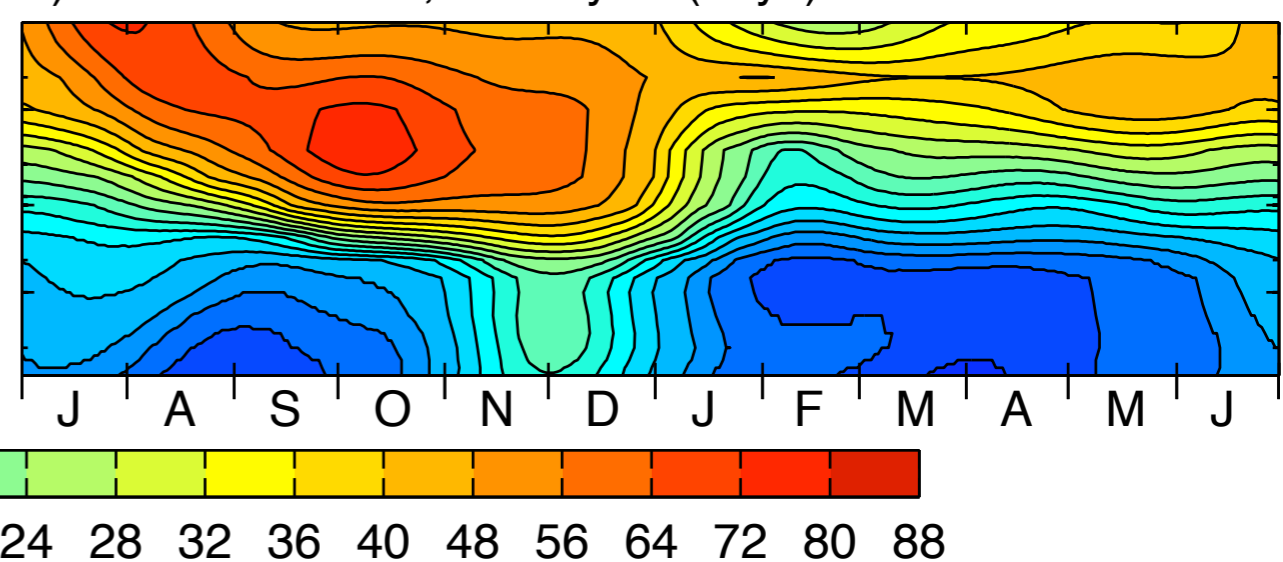
b) SAM standard deviation, reanalysis



a) NAM time scale, reanalysis (days)

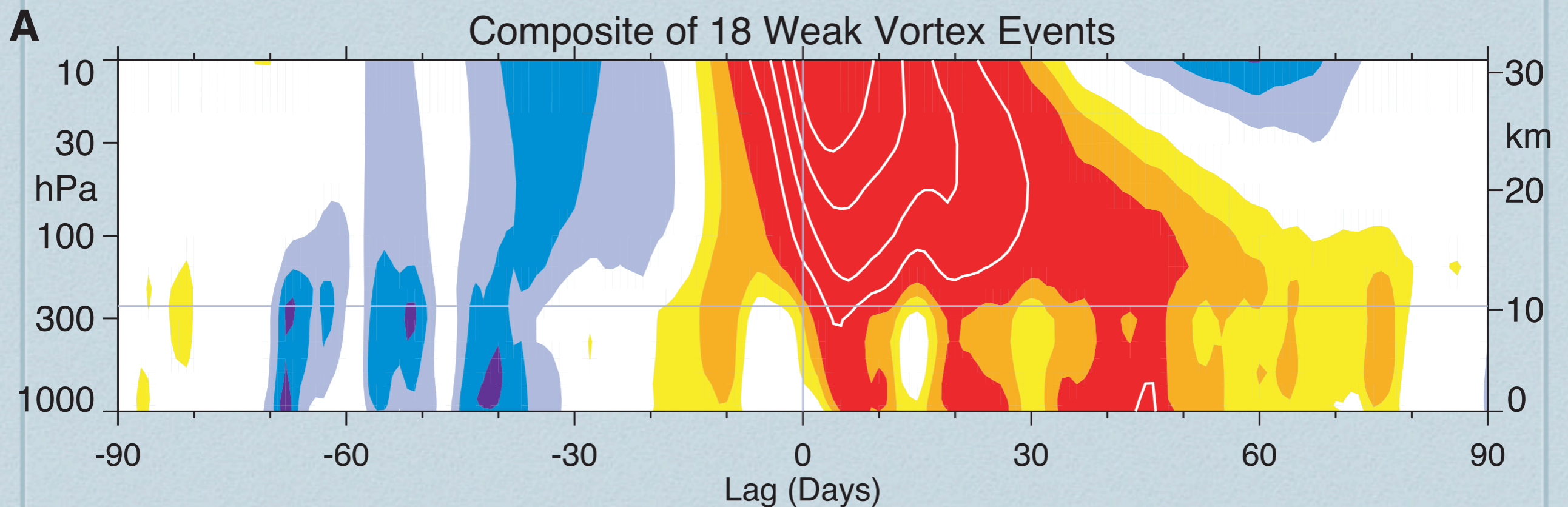


b) SAM time scale, reanalysis (days)



Downward influence from Stratosphere

composite of AM index formed about instances
when the stratospheric vortex is very weak - negative AM
(Stratospheric Sudden Warmings)

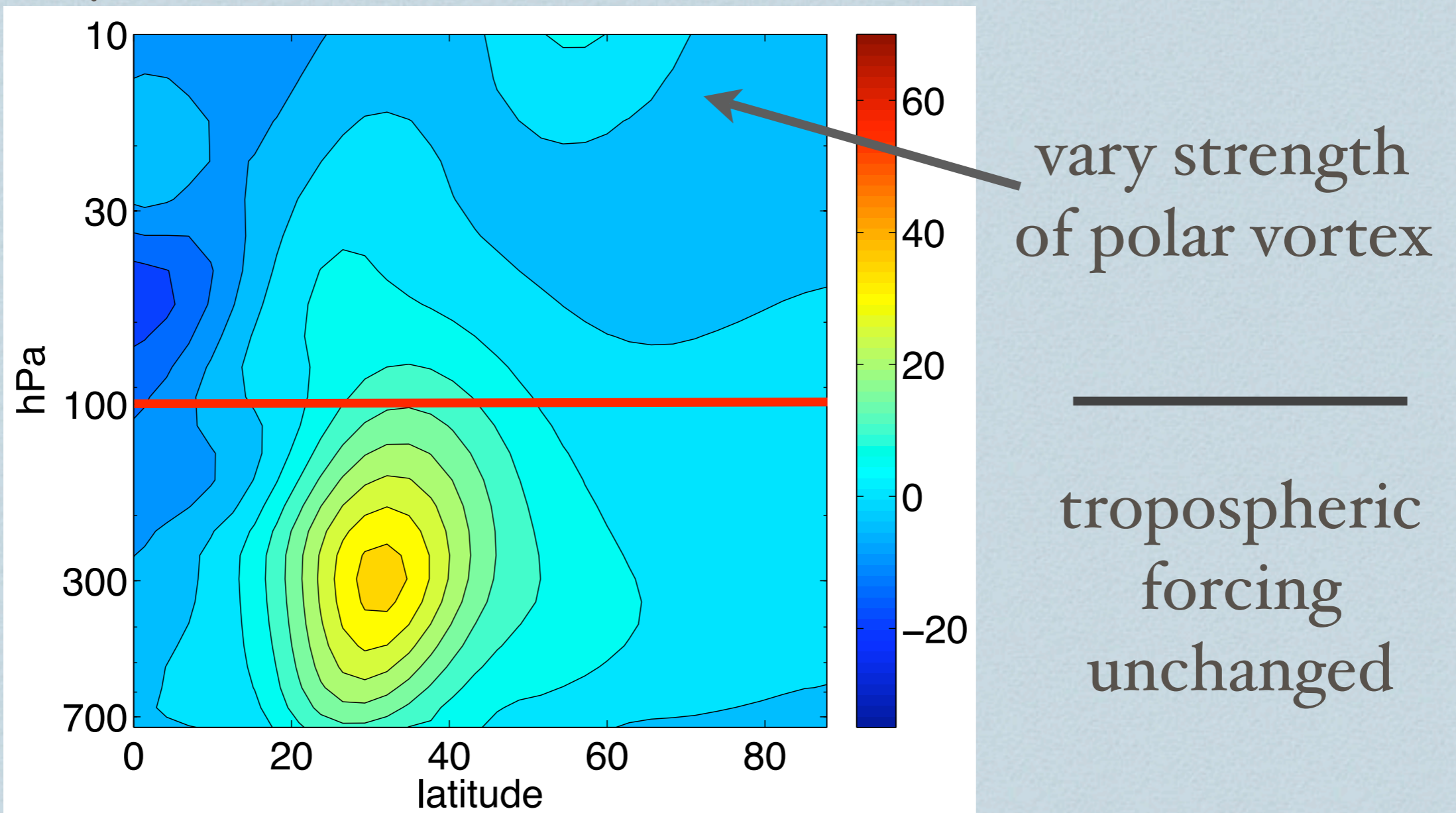


Clean test: Vary only the Stratosphere

- ❖ Gerber and Polvani (2009) idealized GCM
 - ❖ forced by Polvani and Kushner 2002 forcing (Held Suarez troposphere + a stratospheric polar vortex)
 - ❖ includes simple wavenumber 2 topography (needed to produce stratospheric variability)
 - ❖ Experiment: compare time slice runs where only the stratospheric vortex is varied

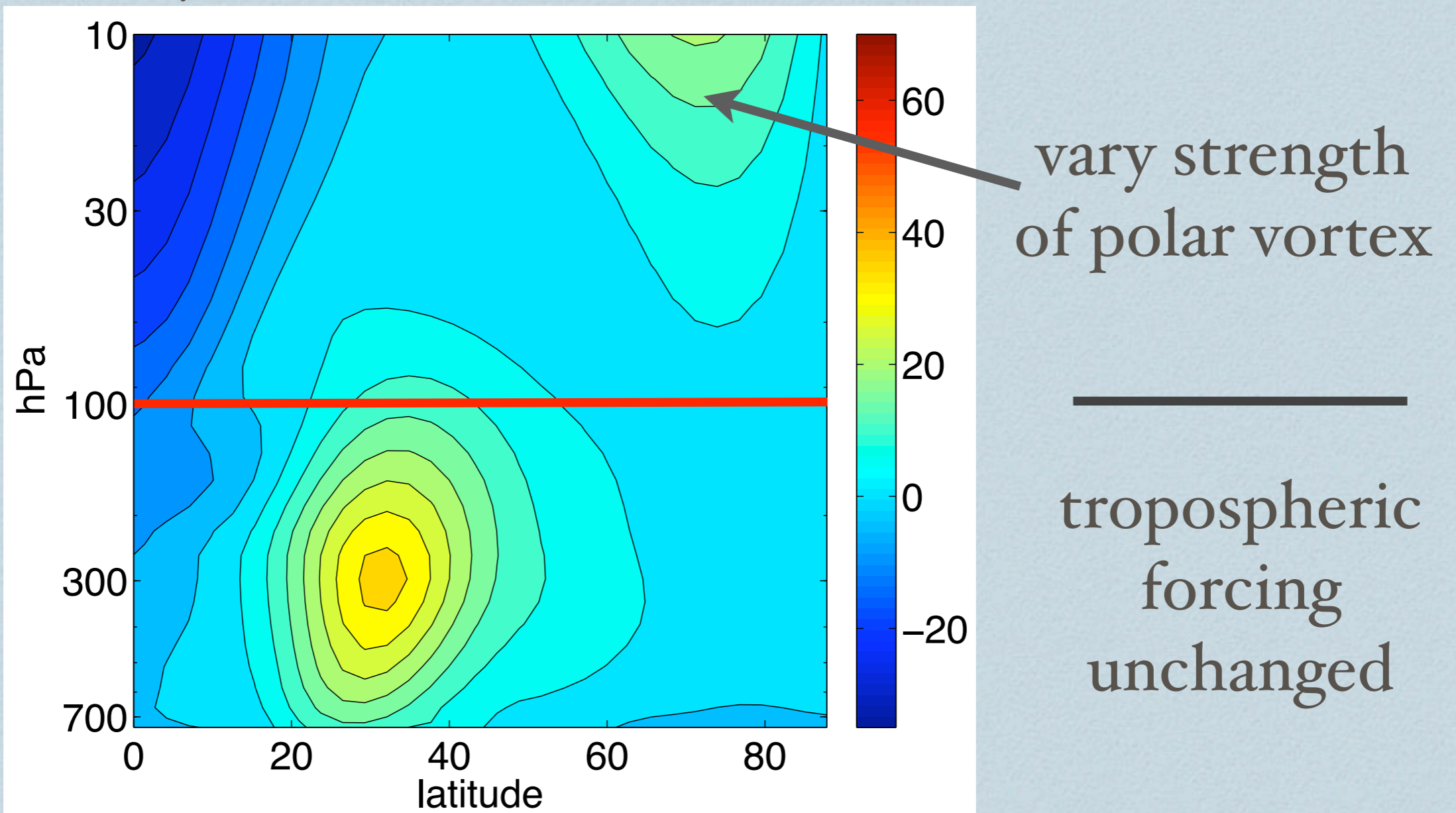
Impact of Seasonal Variations of Stratosphere Alone

$\gamma = 0$: no vortex (summer-ish)



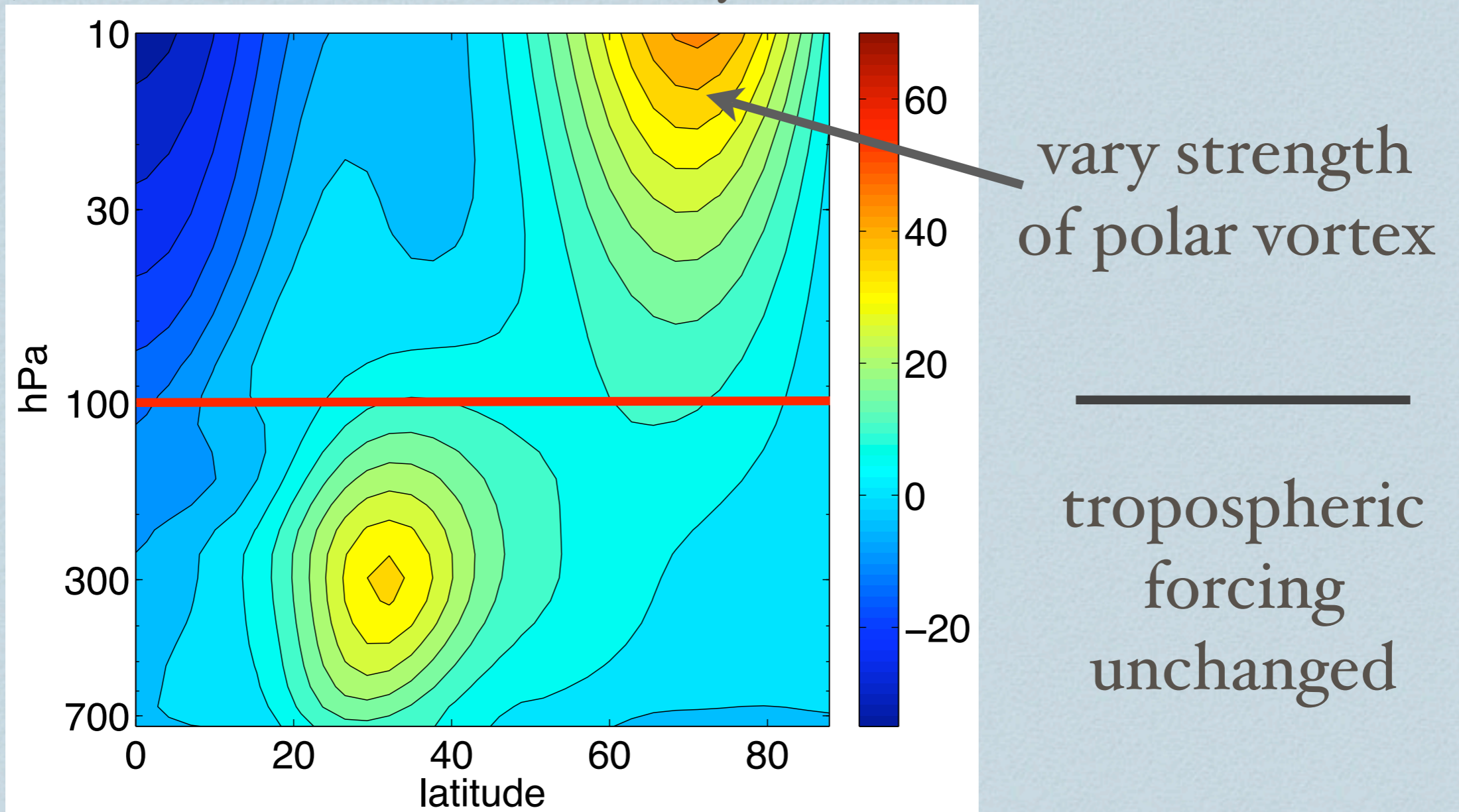
Impact of Seasonal Variations of Stratosphere Alone

$\gamma = 2$: weak vortex (fall)



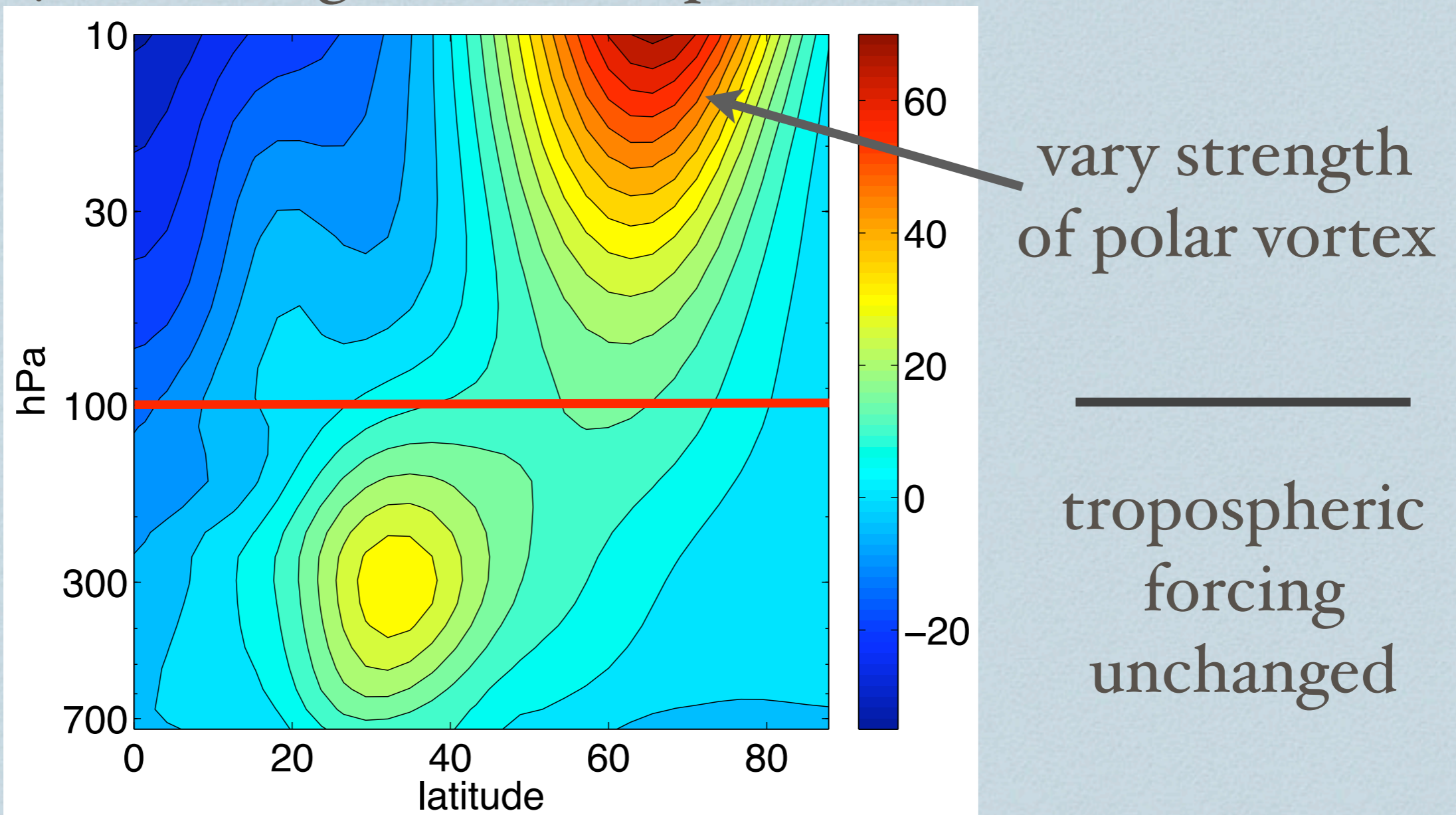
Impact of Seasonal Variations of Stratosphere Alone

$\gamma = 4$: medium vortex (early winter)

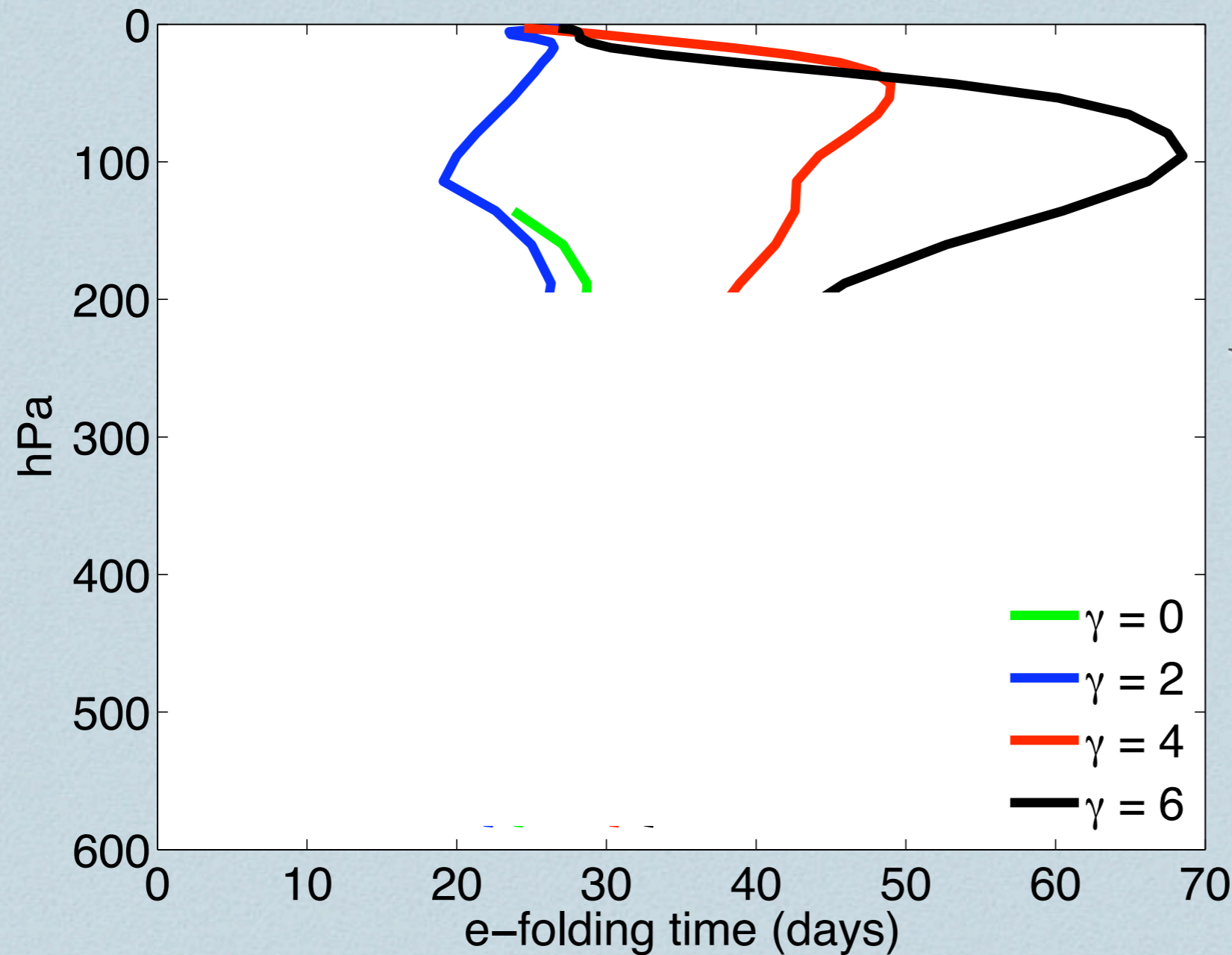


Impact of Seasonal Variations of Stratosphere Alone

$\gamma = 6$: strong vortex (deep winter)

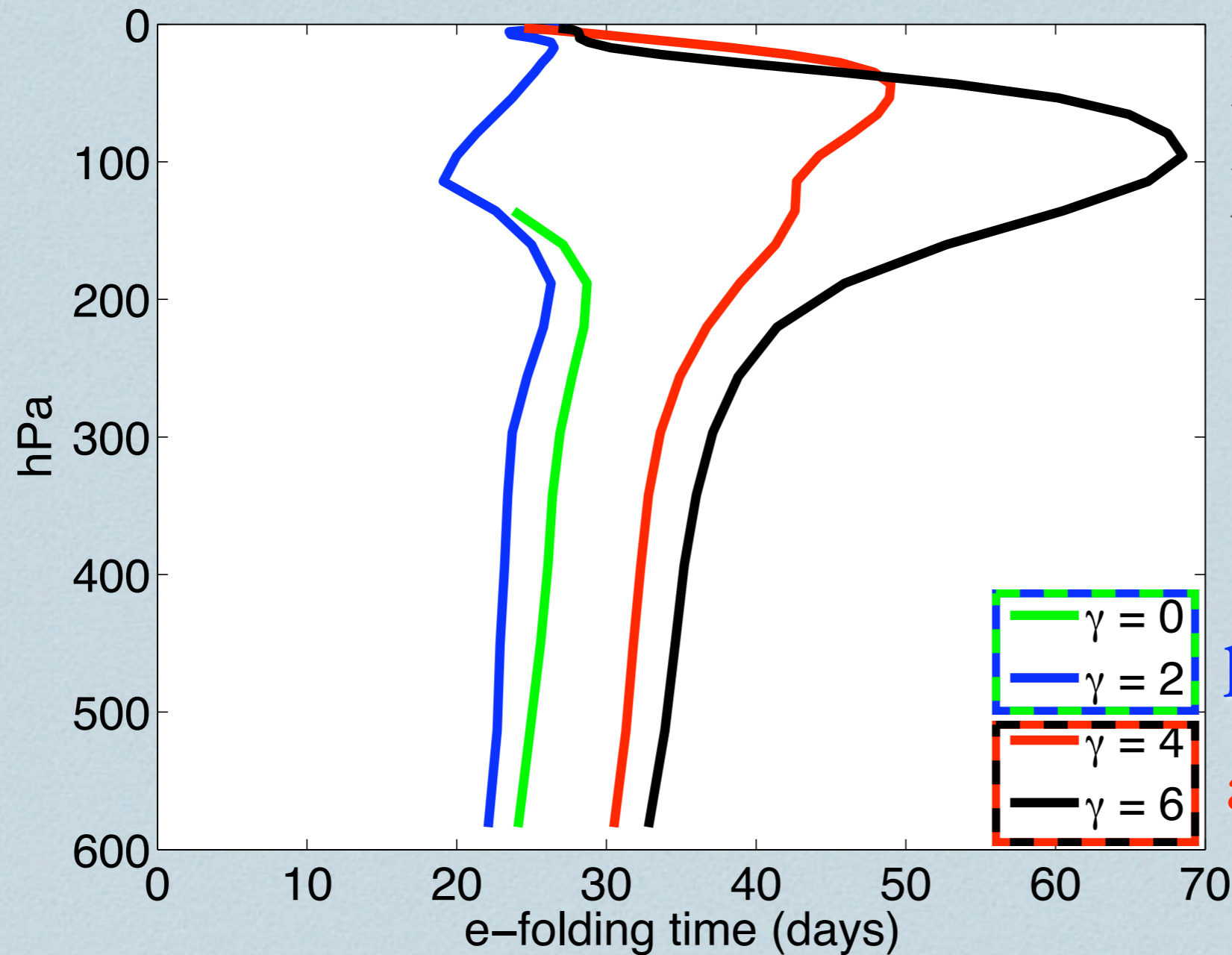


Stratosphere-Troposphere Coupling Enhances Tropospheric Persistence



stratosphere is
active only when
there are sufficient
westerly winds

Stratosphere-Troposphere Coupling Enhances Tropospheric Persistence



lower stratosphere
provides extended
memory to
troposphere

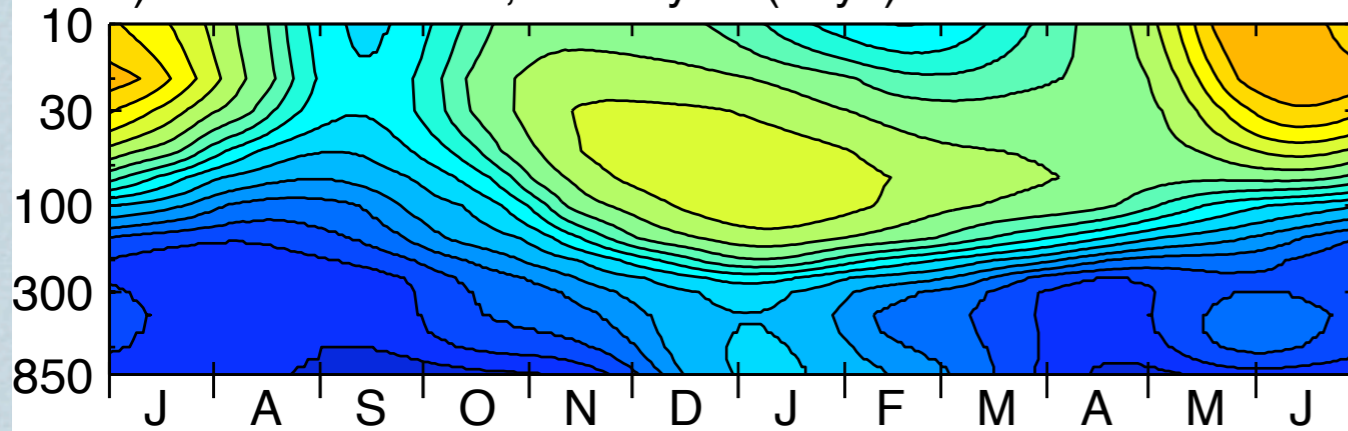
passive strat.

active strat.

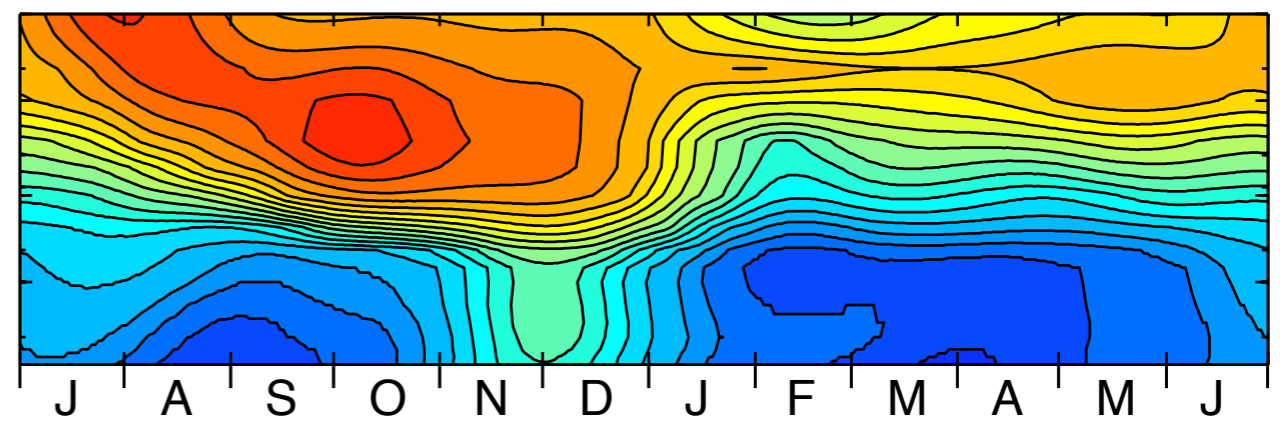
(Some) Chemistry Climate Models capture tighter seasonal structure!

Reanalyses

a) NAM time scale, reanalysis (days)

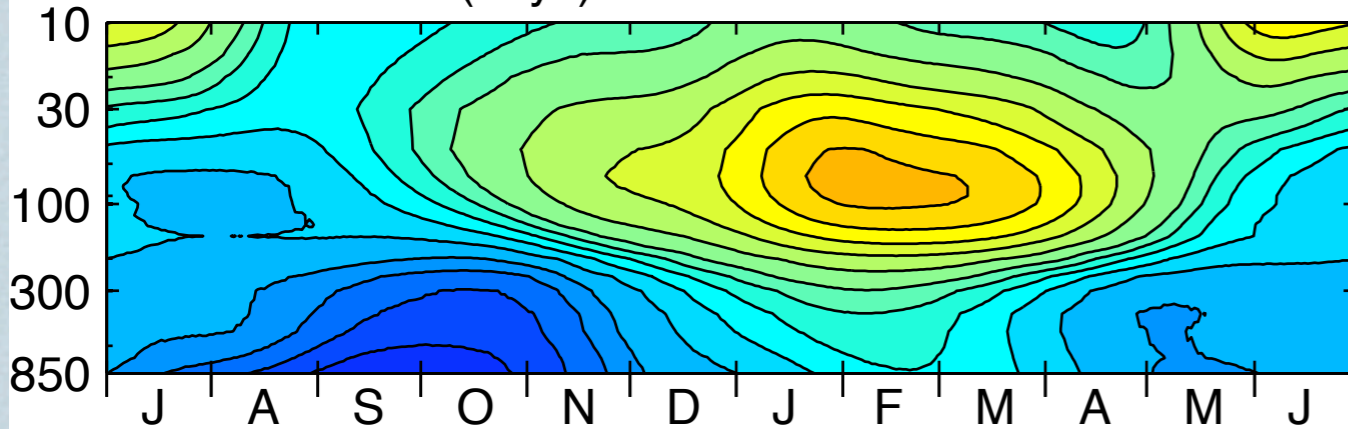


b) SAM time scale, reanalysis (days)

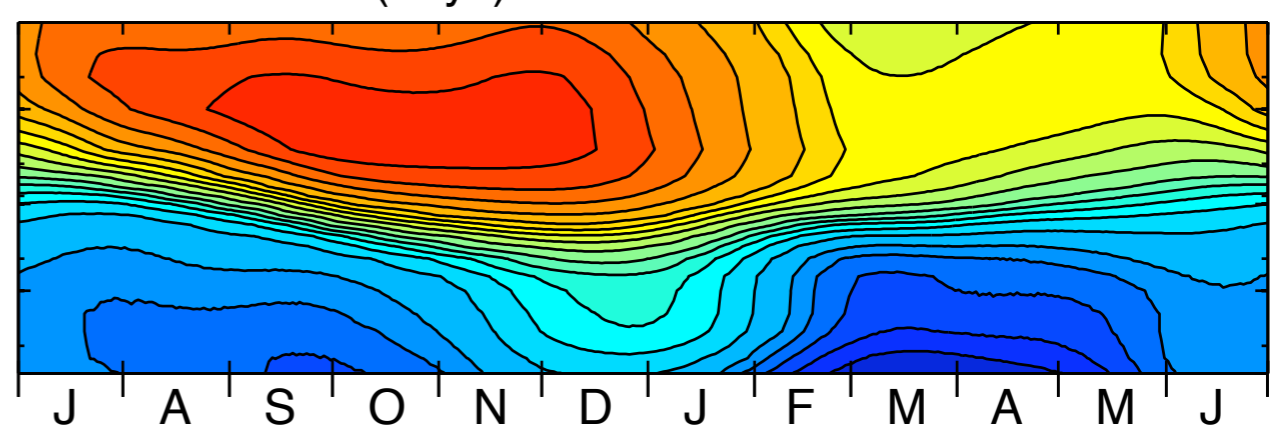


GEOSCCM [Pawson, Stolarski et al.]

NAM time scale (days)



SAM time scale (days)



5 6 7 8 9 10 12 14 16 18 20 24 28 32 36 40 48 56 64 72 80 88

(3) Internal Variability - Climate Response Connection

- ❖ Fluctuation-dissipation theory relates connects the response of a system to external forcing with the time scales of its internal, unforced variability
- ❖ Proper application requires knowledge of correlations between all modes of variability to compute the proper response operator (Gritsun and Branstator 2008, Majda et al. 2010)
- ❖ If climate modes are roughly uncorrelated with others, autocorrelation function may provide rough estimate (Leith 1975)

Experiment with Idealized GCM (Held-Suarez)

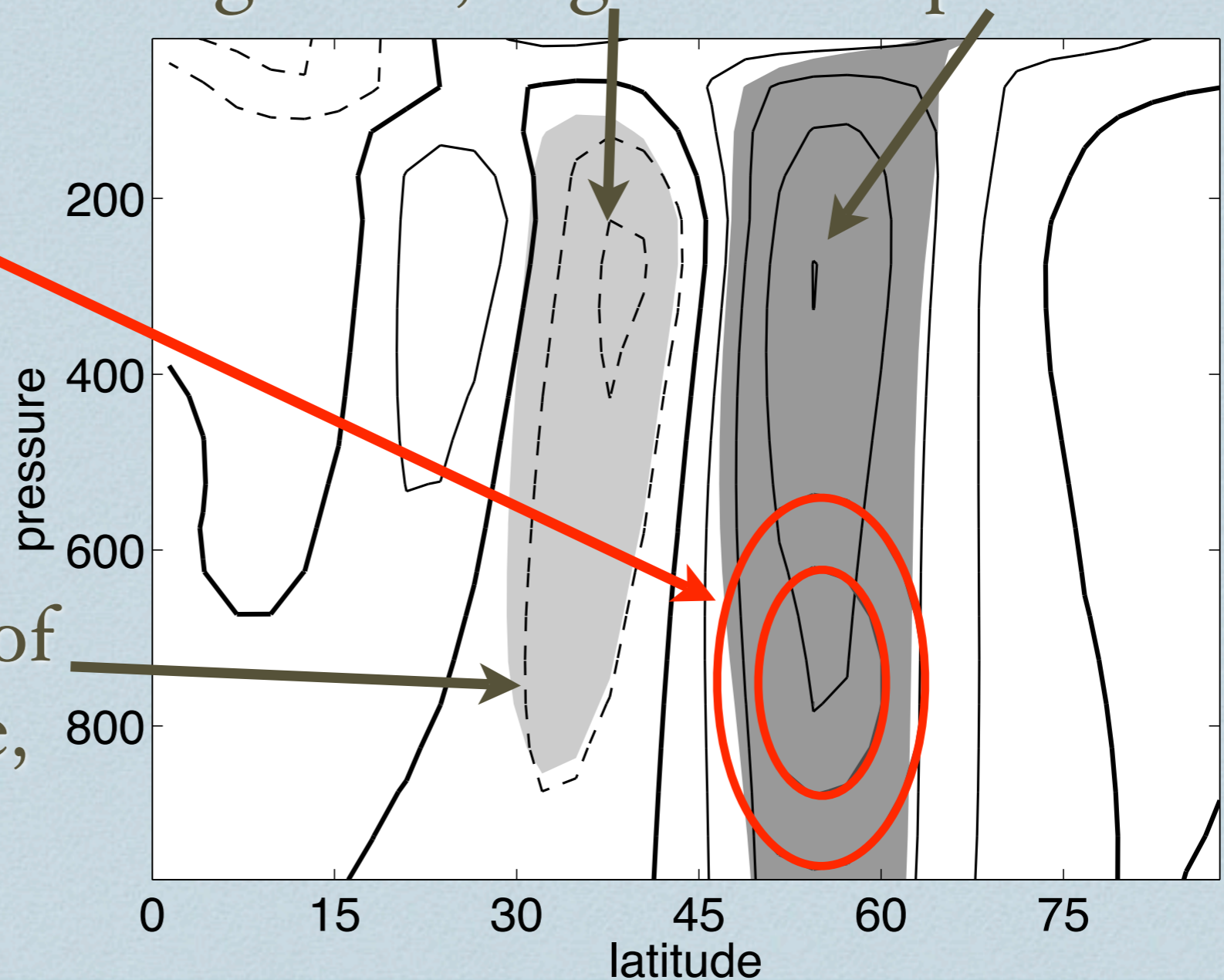
- ❖ Consider two models with very different AM time scales: 33 days versus 96 days
- ❖ Apply torque the projects well onto the AM pattern (Ring and Plumb 2008)
- ❖ Compare model response (shift in jet stream): F-D suggests that model with longer time scales will be more sensitive to the the torque.

Response of Annular mode to External Forcing (Torque)

shading: first EOF of u from control integration, negative and positive

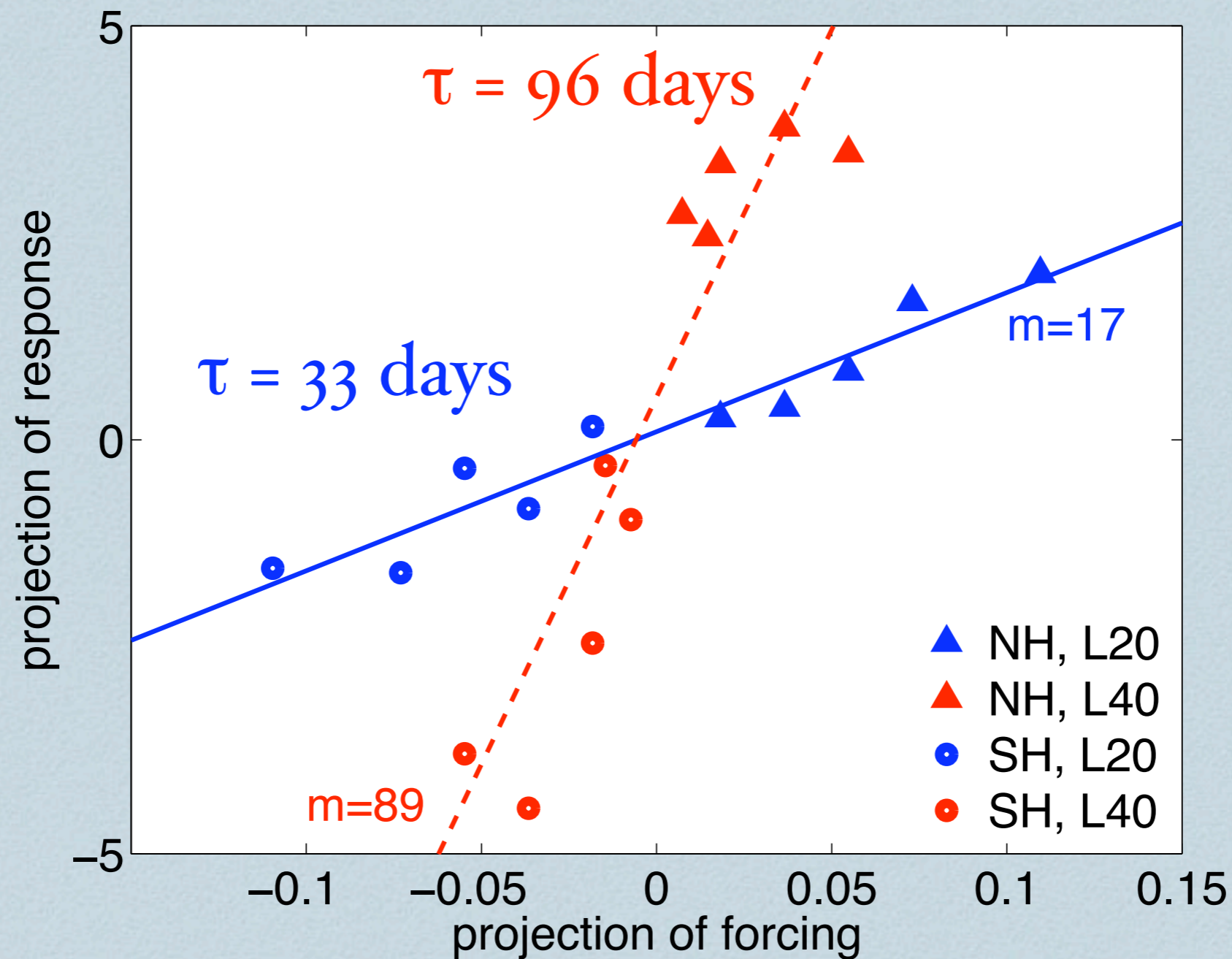
apply a torque that projects onto the EOF

contours: response of model to the torque, $\bar{u}_{\text{forced}} - \bar{u}_{\text{control}}$ (negative dashed)



after Ring and Plumb 2008

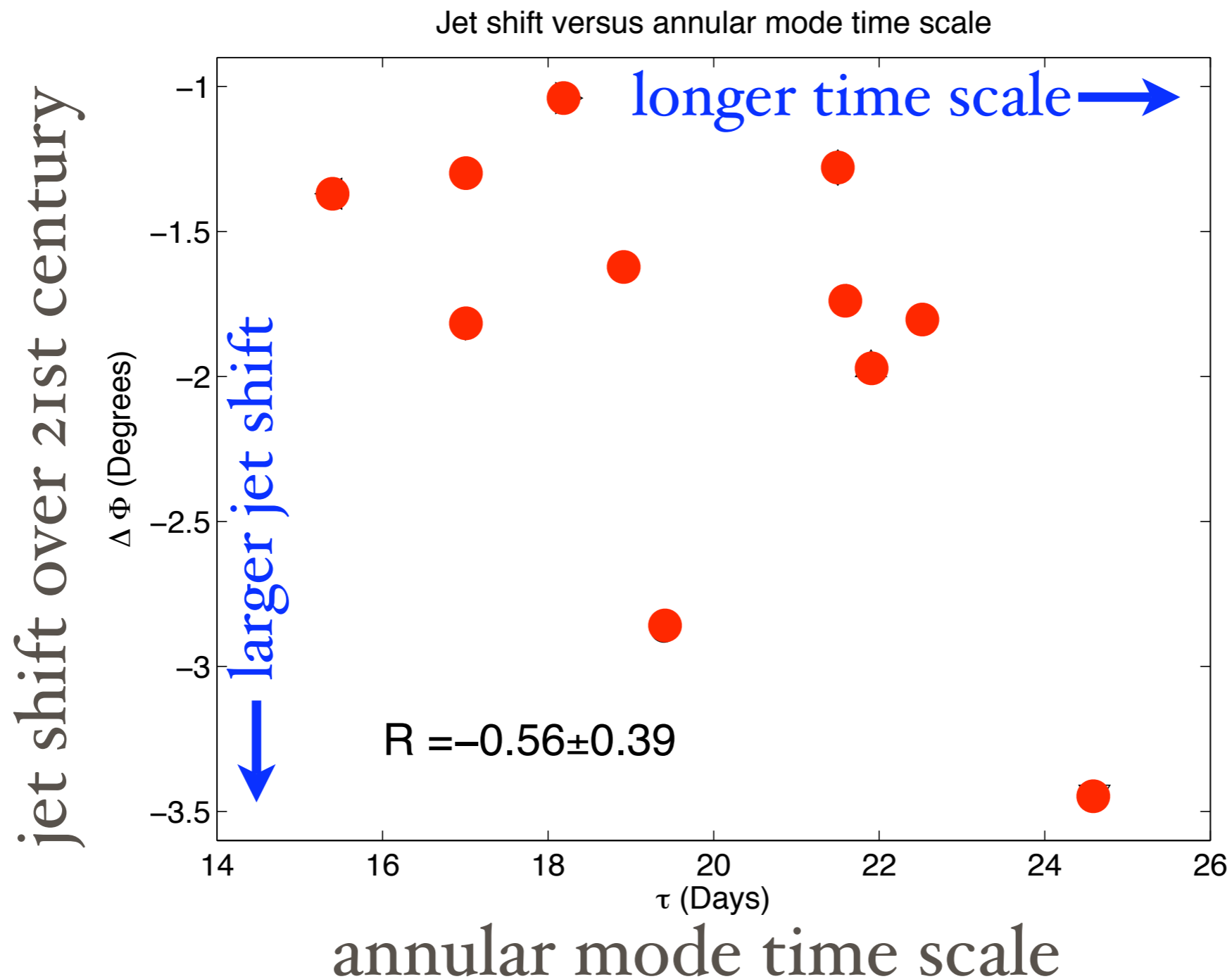
Model with longer time scale more sensitive to external



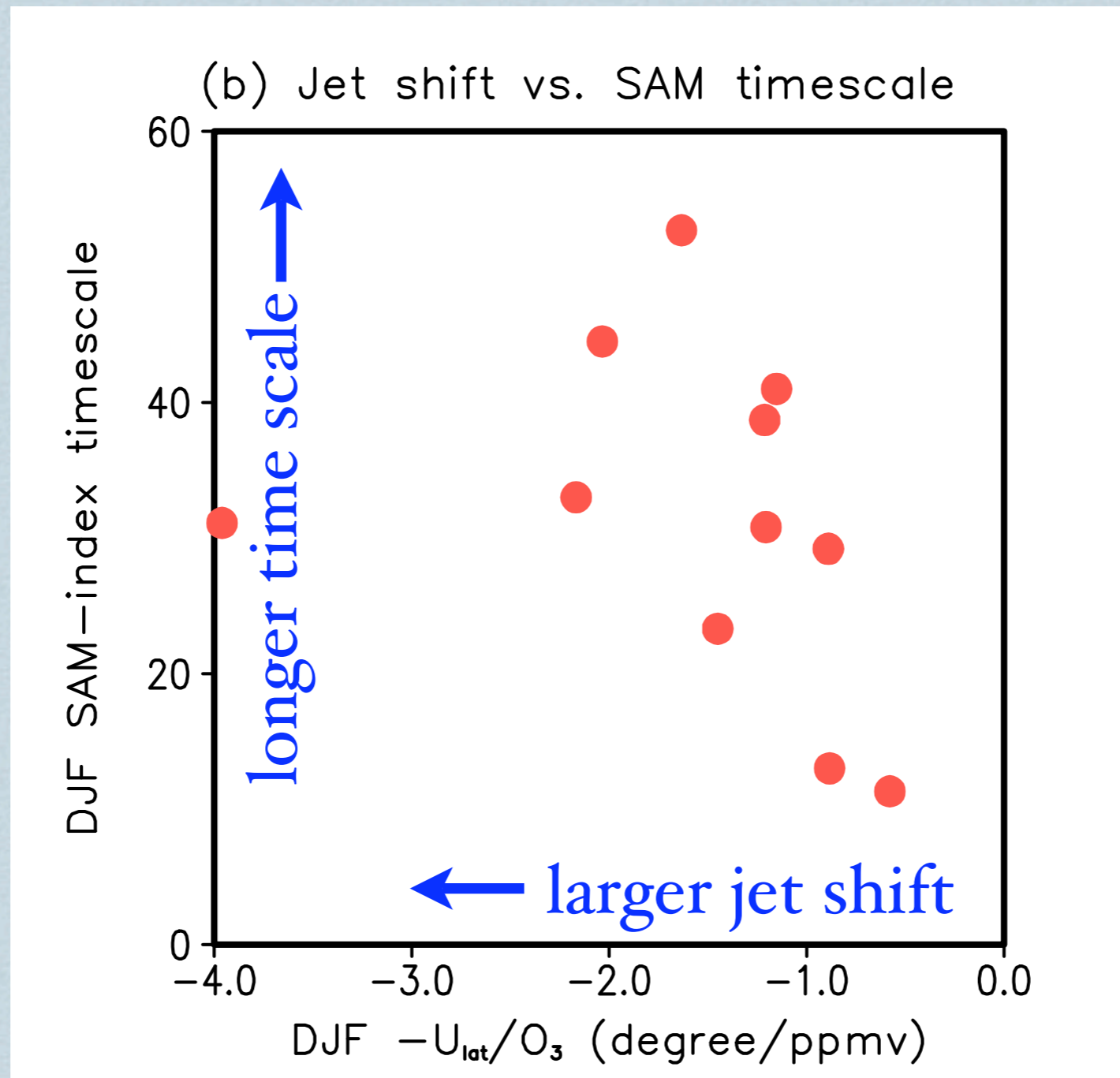
Comprehensive GCMs

- ❖ IPCC model time scales vary by a factor of 2, CCM model time scales vary by factor of 4
- ❖ If projection of anthropogenic forcing in the A2 / REF-B2 scenarios models is roughly the same, one might expect models with longer time scales to exhibit a larger response.

IPCC Model Climate Response Sensitivity to AM Time Scale



CCM Climate Response Sensitivity to AM Time Scale



(axes flipped)

Conclusions

- ❖ Simplified models help us understand the key features of annular mode variability
 - ❖ zonal mean variability is integral of eddy forcing: hence increased power on lower frequencies
 - ❖ eddy-mean flow feedbacks create distinct time scale
- ❖ zonal asymmetries (e.g. topography) shorten time scales: variability in NH is less persistent than SH
- ❖ stratosphere increases persistence of tropospheric variability during active seasons (NH winter, SH spring)
- ❖ SH harder to simulate (stronger eddy-mean flow feedbacks)
 - ❖ biases in mean state: equatorward jet \Leftrightarrow long time scales
 - ❖ climate change: long time scales \Leftrightarrow enhanced response to anthropogenic forcing

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