

Conflict analysis for decision making and control of connected automated vehicles

Gábor Orosz

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Motivation

Connectivity and **automation** of road vehicles may improve **safety, energy efficiency,** and **mobility**

Categorization (Michigan)



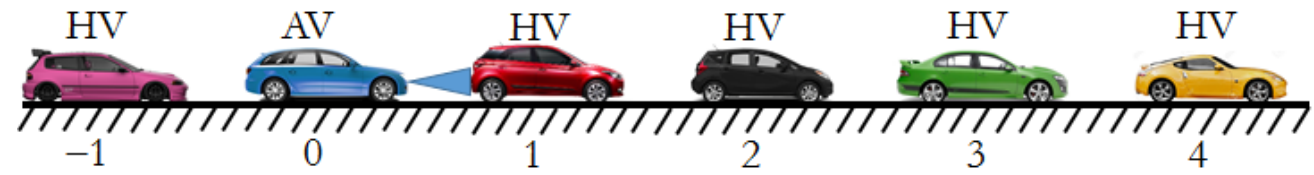
Connected and automated road vehicles: state of the art and future challenges

Tulga Ersal ^a, Ilya Kolmanovsky ^b, Neda Masoud ^c, Necmiye Ozay ^d,
Jeffrey Scruggs ^c, Ram Vasudevan ^a and Gábor Orosz ^{a,c}

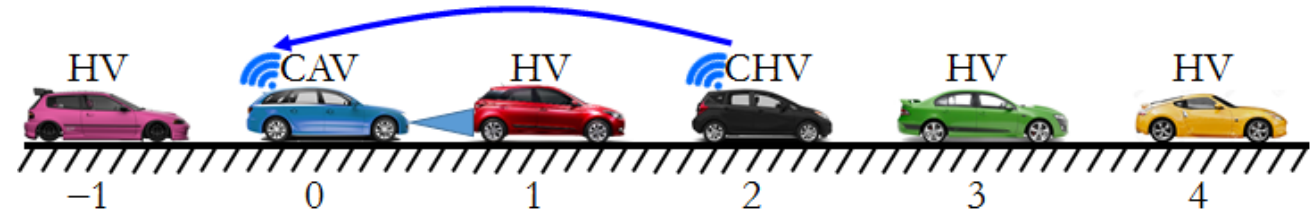
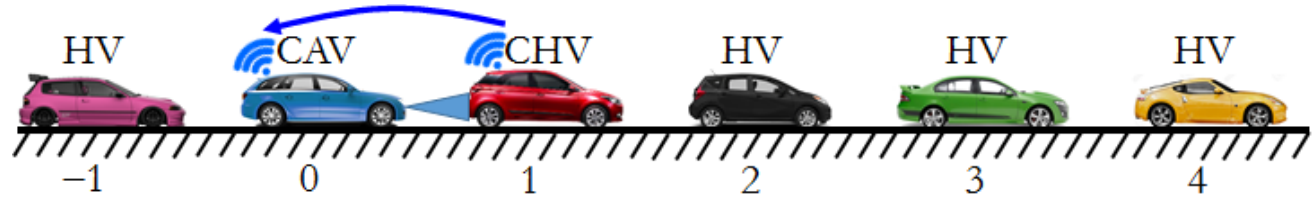
^aDepartment of Mechanical Engineering, University of Michigan, Ann Arbor, MI, USA; ^bDepartment of Aerospace Engineering, University of Michigan, Ann Arbor, MI, USA; ^cDepartment of Civil and Environmental Engineering, University of Michigan, Ann Arbor, MI, USA; ^dDepartment of Electrical Engineering and Computer Science, University of Michigan, Ann Arbor, MI, USA

		without V2X	with V2X
controlled by	human driver	Human-driven Vehicle (HV)	Connected Human-driven Vehicle (CHV)
	computer	Automated Vehicle (AV)	Connected Automated Vehicle (CAV)

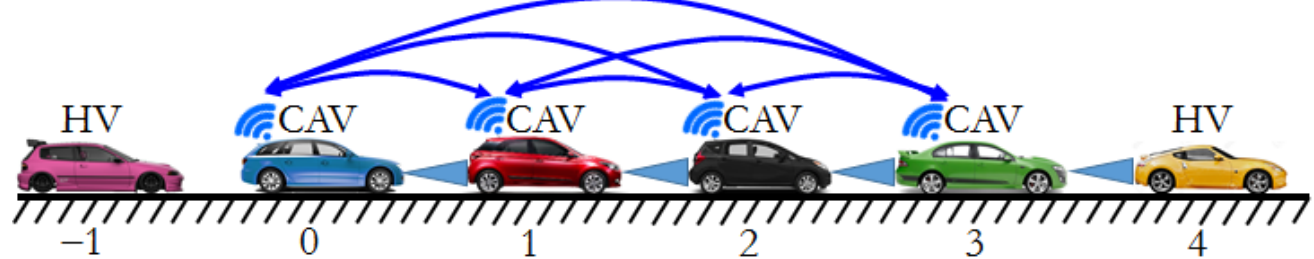
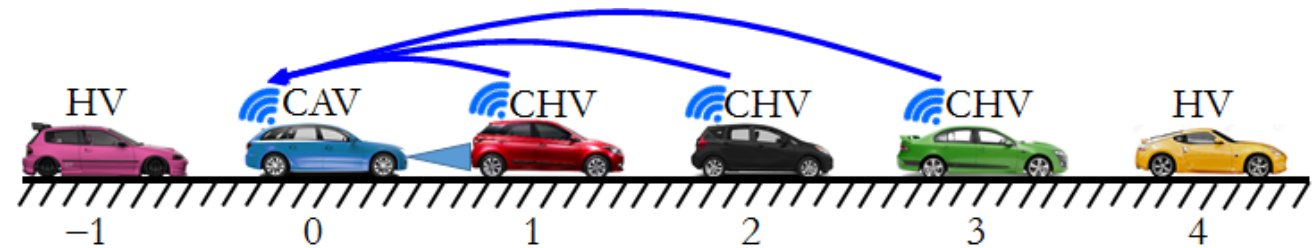
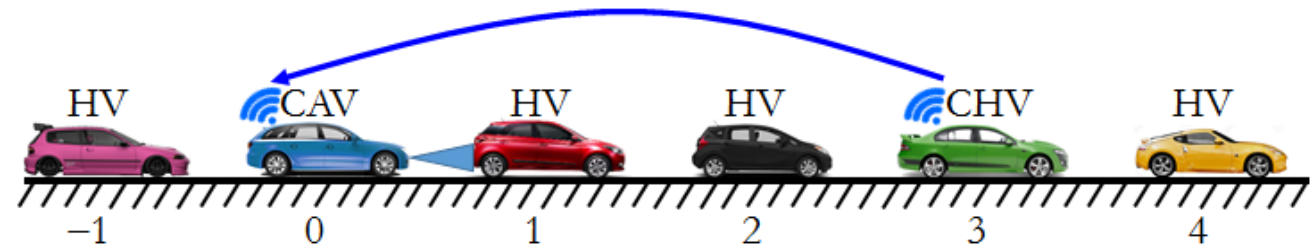
Adaptive
Cruise
Control
(ACC)



Connected
Cruise
Control
(CCC)



Cooperative
Adaptive
Cruise
Control
(CACC)



Mixed Traffic

Connected Cruise Control (theory)

Transportation Research Part C 46 (2014) 46–64



Contents lists available at [ScienceDirect](#)

Transportation Research Part C

journal homepage: www.elsevier.com/locate/trc



VEHICLE SYSTEM DYNAMICS, 2016
VOL. 54, NO. 8, 1147–1176
<http://dx.doi.org/10.1080/00423114.2016.1193209>



Dynamics of connected vehicle systems with delayed acceleration feedback



Connected cruise control: modelling, delay effects, and nonlinear behaviour

1638

IEEE TRANSACTIONS ON INTELLIGENT TRANSPORTATION SYSTEMS, VOL. 17, NO. 6, JUNE 2016 5Z

Department of Mechanical Engineering, University of Michigan, Ann Arbor, MI, USA

Motif-Based Design for Connected Vehicle Systems in Presence of Heterogeneous Connectivity Structures and Time Delays

2056

IEEE TRANSACTIONS ON INTELLIGENT TRANSPORTATION SYSTEMS, VOL. 18, NO. 8, AUGUST 2017

Optimal Control of Connected Vehicle Systems With Communication Delay and Driver Reaction Time

INTERNATIONAL JOURNAL OF ROBUST AND NONLINEAR CONTROL

Int. J. Robust Nonlinear Control 2017; **27**:781–803

Published online 10 August 2016 in Wiley Online Library (wileyonlinelibrary.com). DOI: 10.1002/rnc.3600

IEEE TRANSACTIONS ON INTELLIGENT TRANSPORTATION SYSTEMS, VOL. 19, NO. 2, FEBRUARY 2018

545

Application of Predictor Feedback to Compensate Time Delays in Connected Cruise Control

Consensus and disturbance attenuation in multi-agent chains with nonlinear control and time delays

Linjun Zhang^{*,†} and Gábor Orosz

Department of Mechanical Engineering, University of Michigan, Ann Arbor, MI 48105, USA

Tamás G. Molnár, Wubing B. Qin, Tamás Insperger, and Gábor Orosz

Connected Cruise Control (practice)

Transportation Research Part C 91 (2018) 335–352



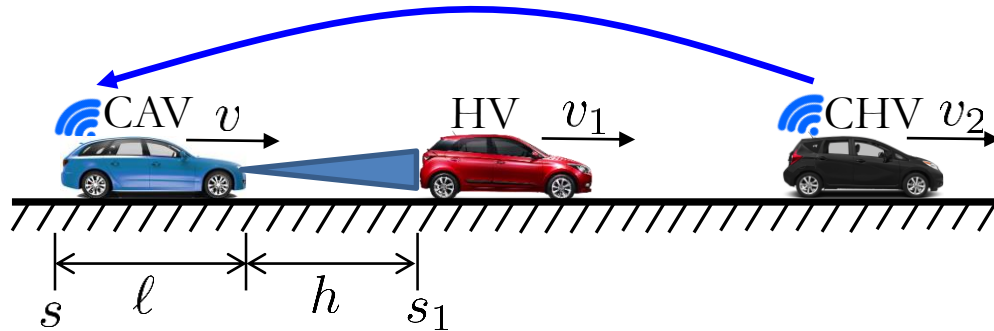
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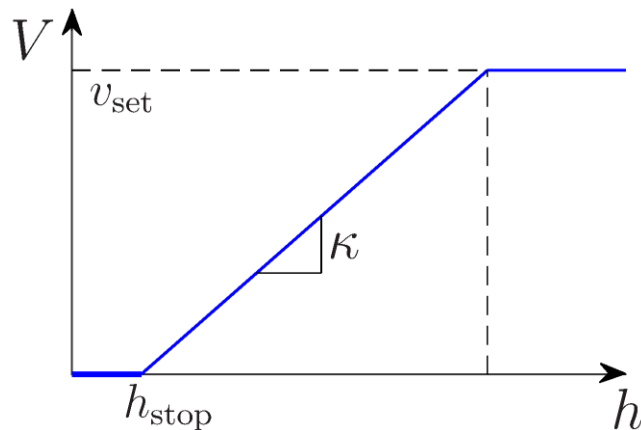
journal homepage: www.elsevier.com/locate/trc



Experimental validation of connected automated vehicle design among human-driven vehicles



$$u = \alpha (V(h) - v) + \beta_1 (v_1 - v) + \beta_2 (v_2 - v)$$



Connected Cruise Control (practice)

Transportation Research Part C 91 (2018) 335–352



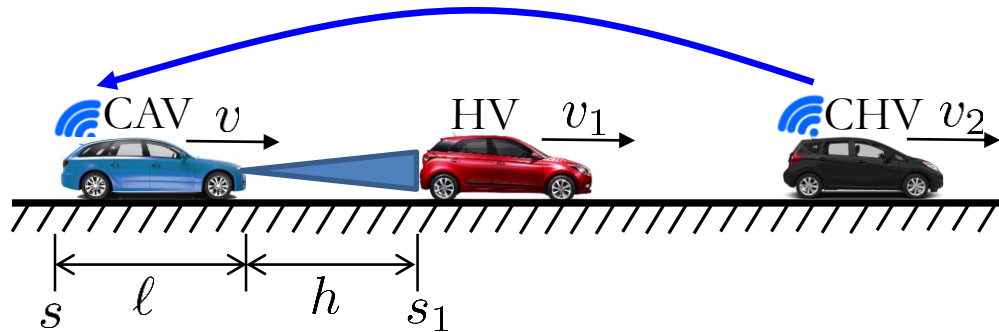
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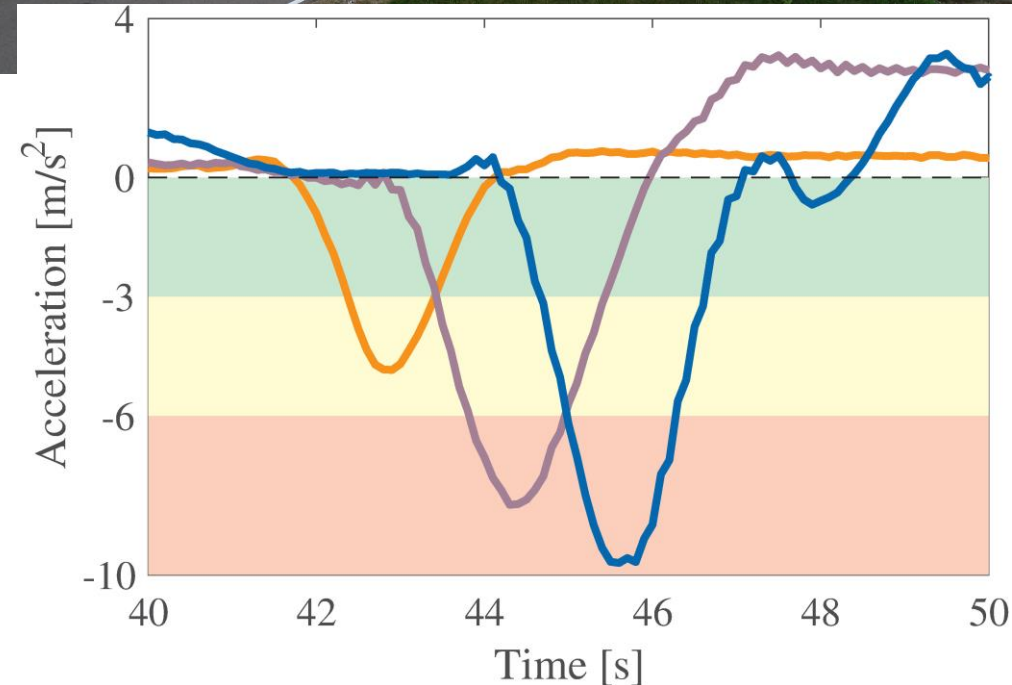
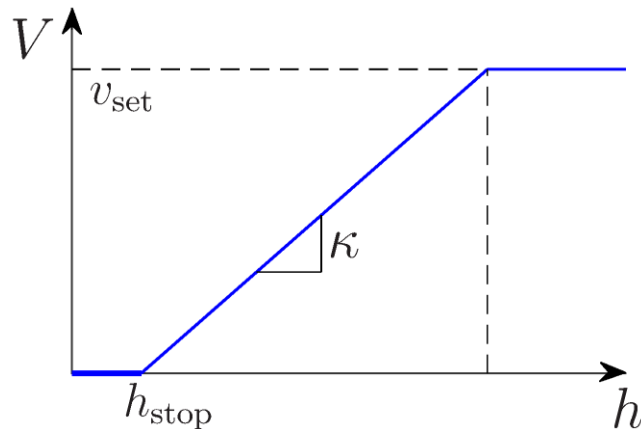
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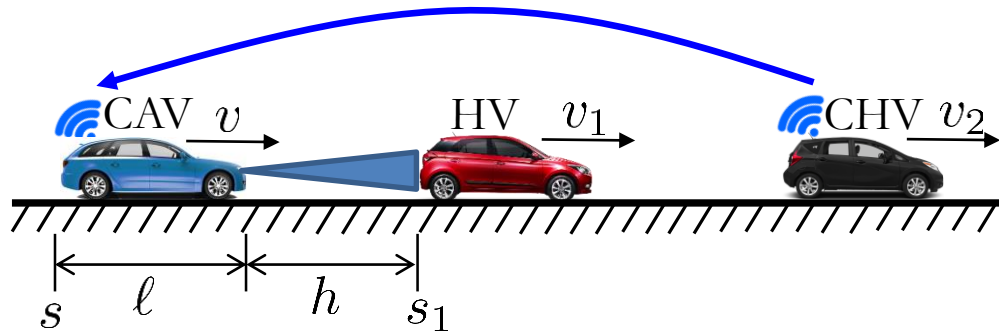
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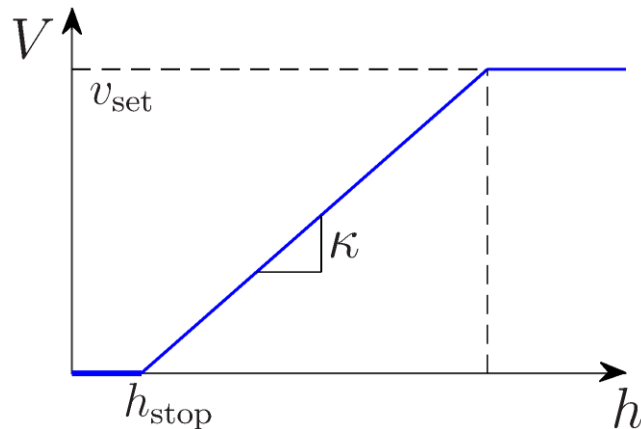
journal homepage: www.elsevier.com/locate/trc



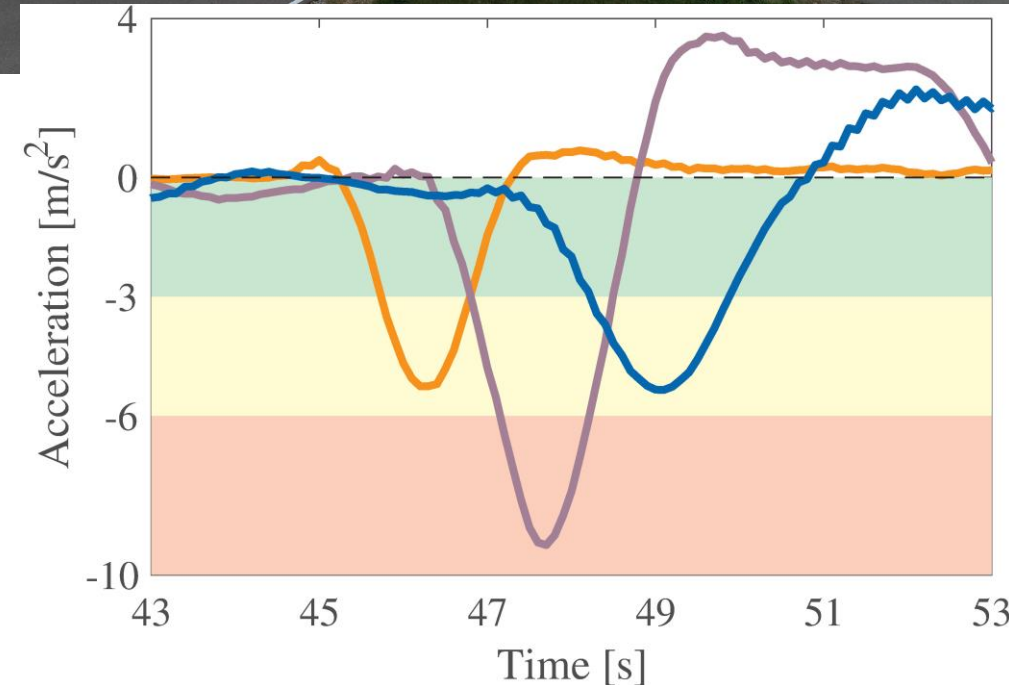
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Automated Vehicle



Connected Cruise Control (practice)

Transportation Research Part C 91 (2018) 335–352



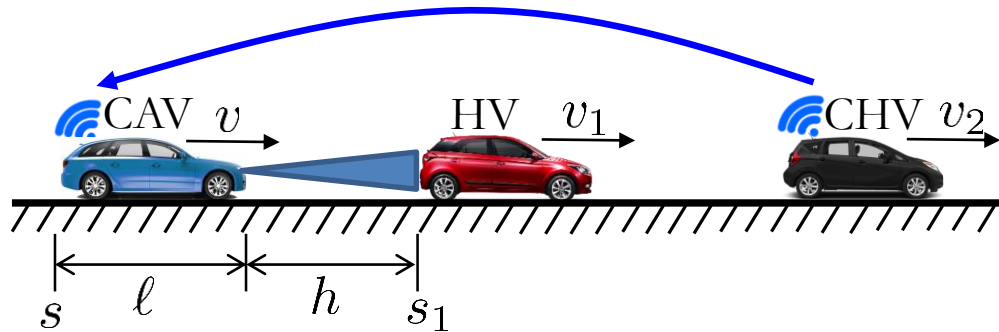
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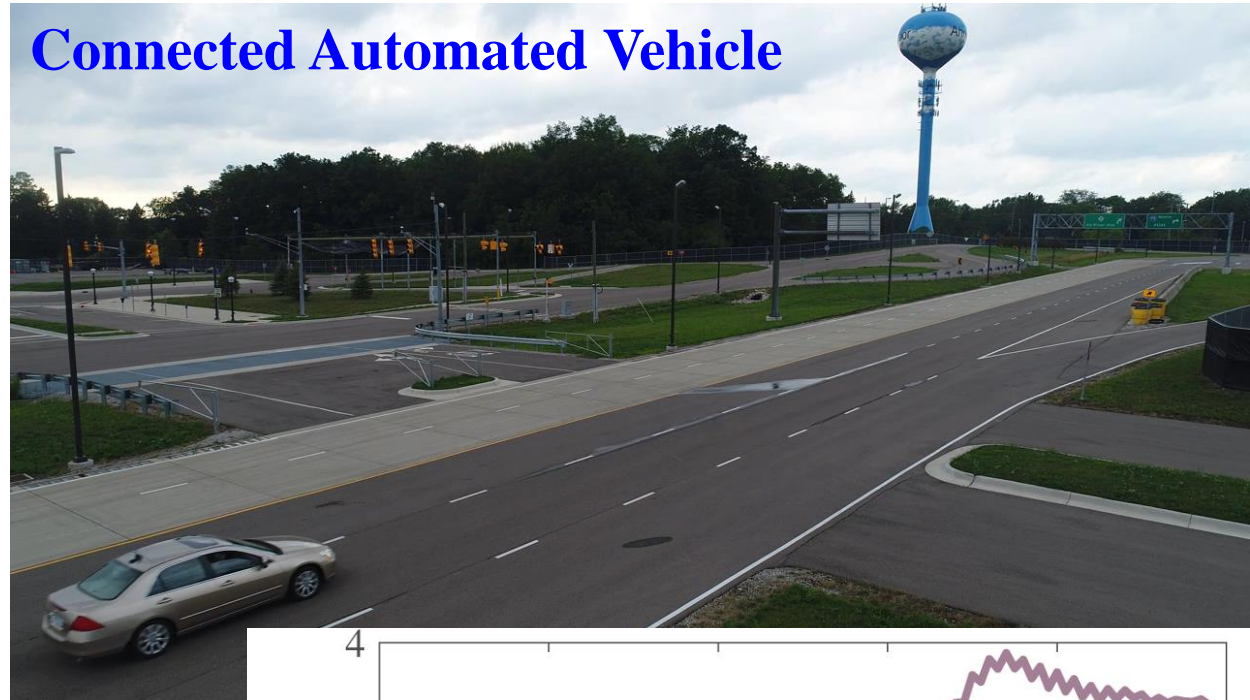
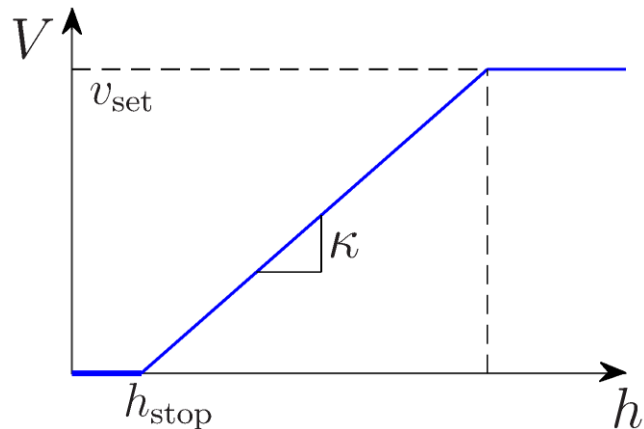
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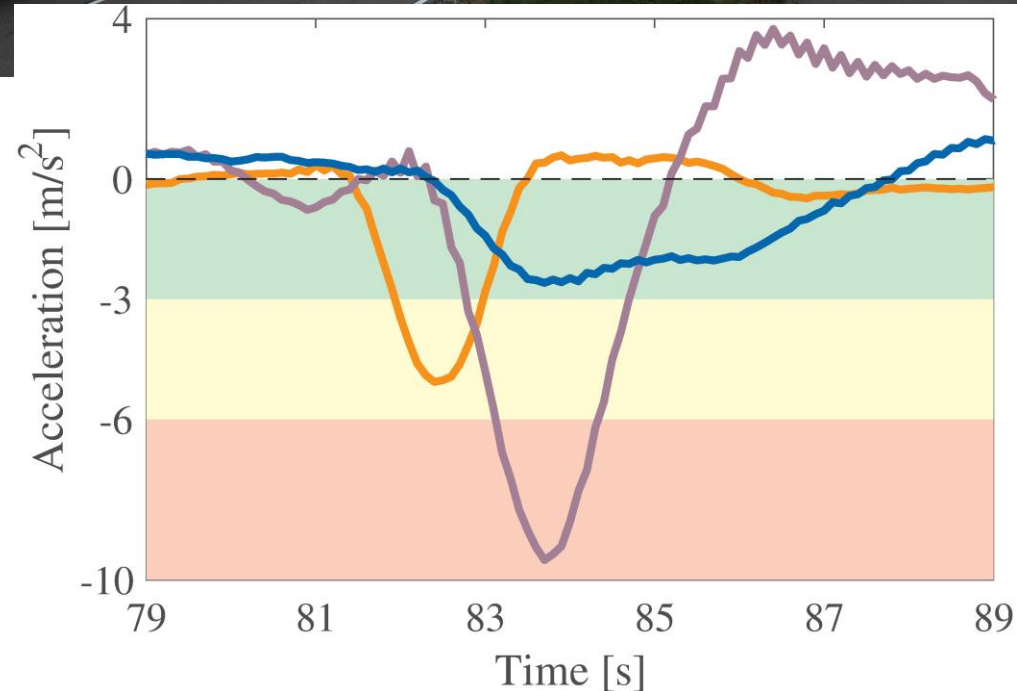
Experimental validation of connected automated vehicle design among human-driven vehicles



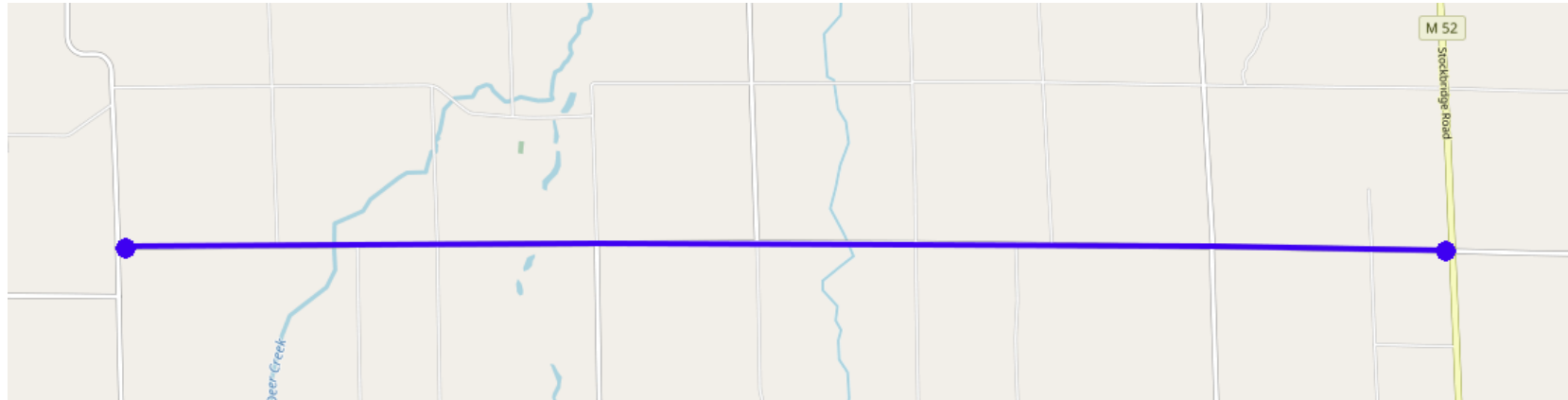
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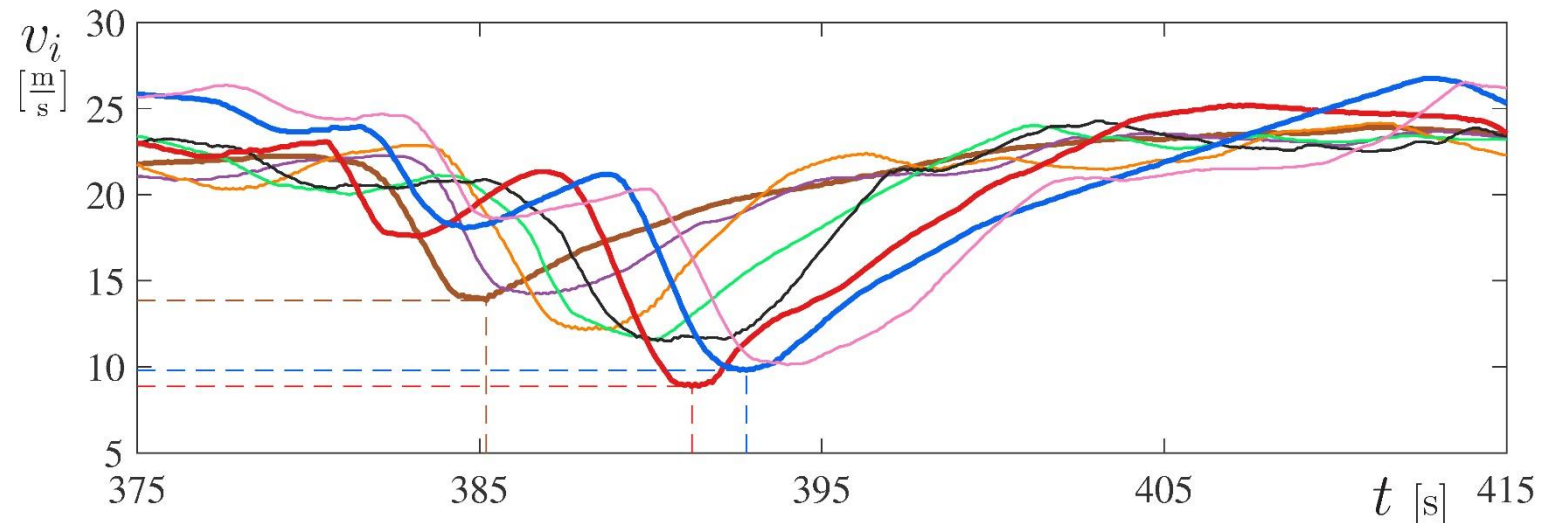
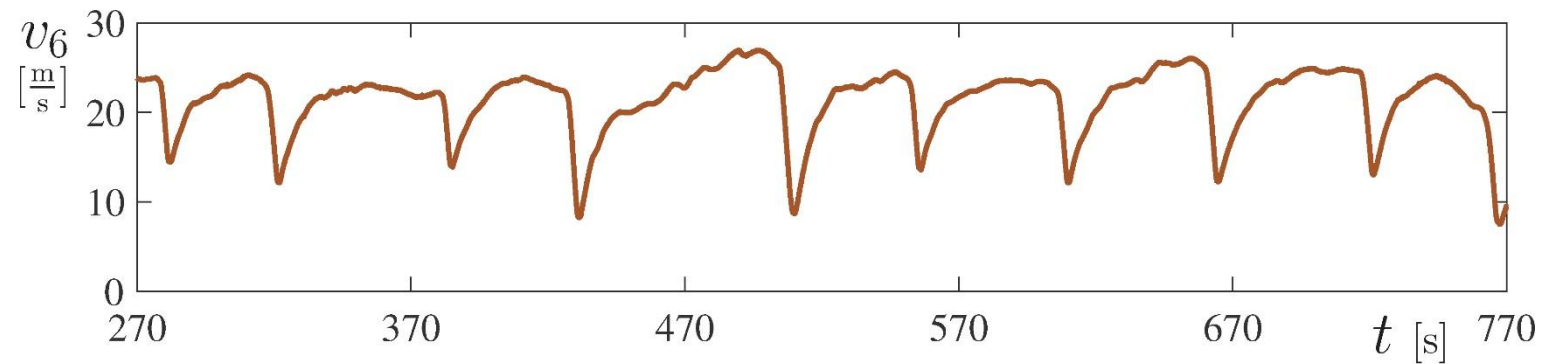
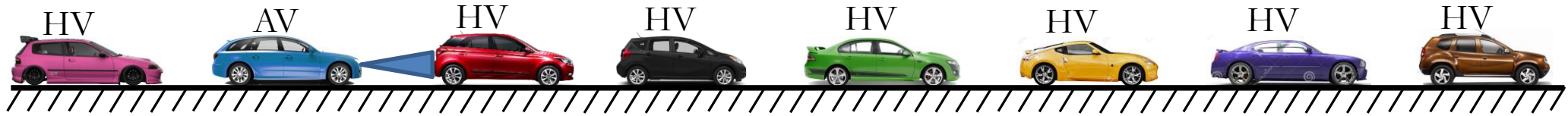
Connected Automated Vehicle



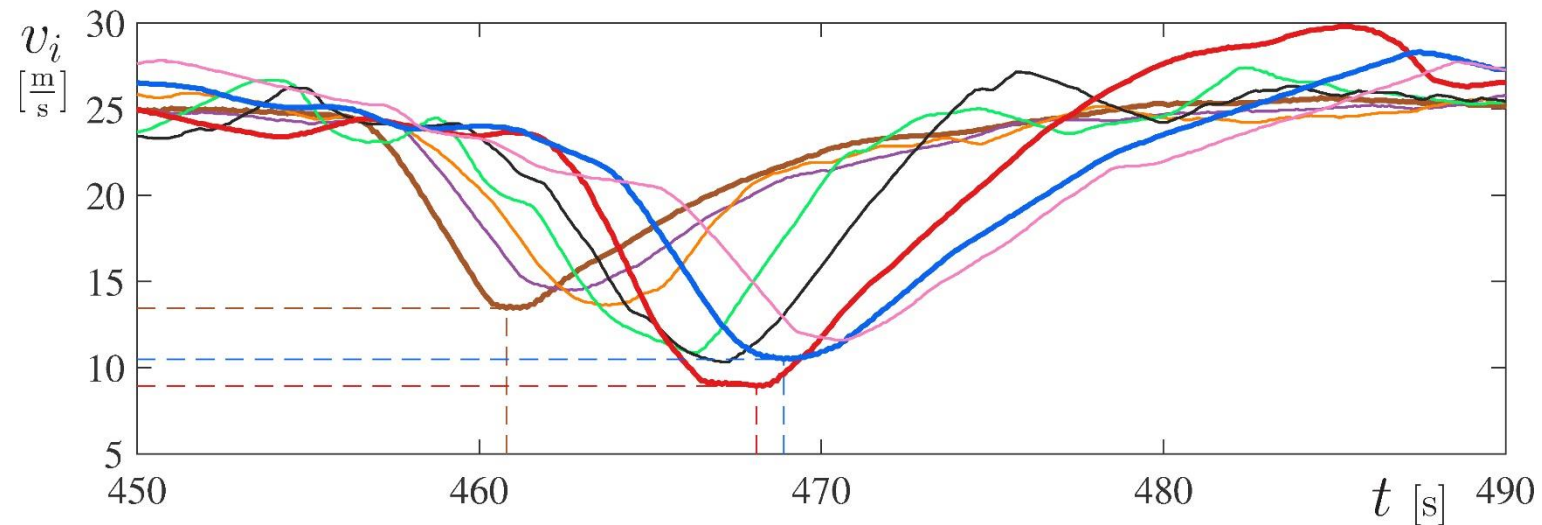
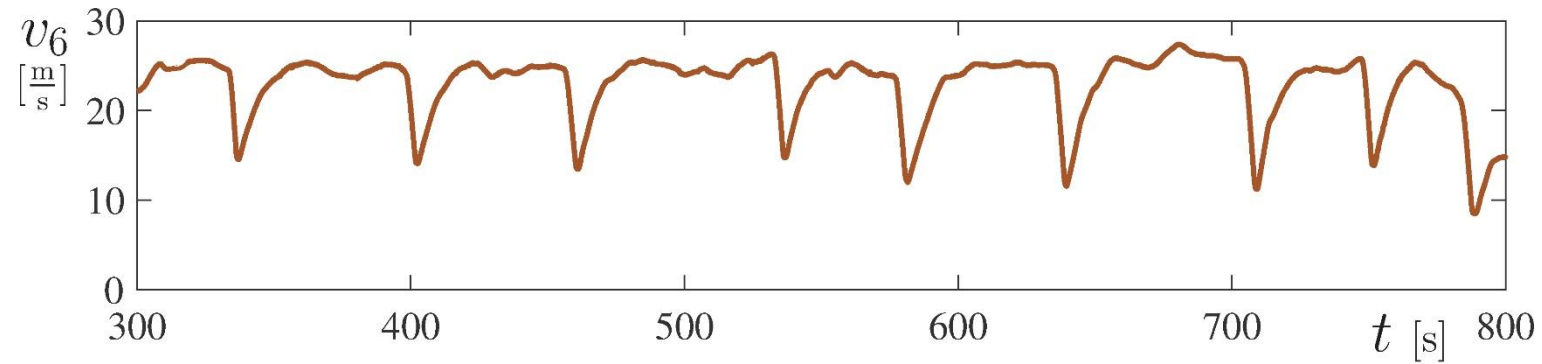
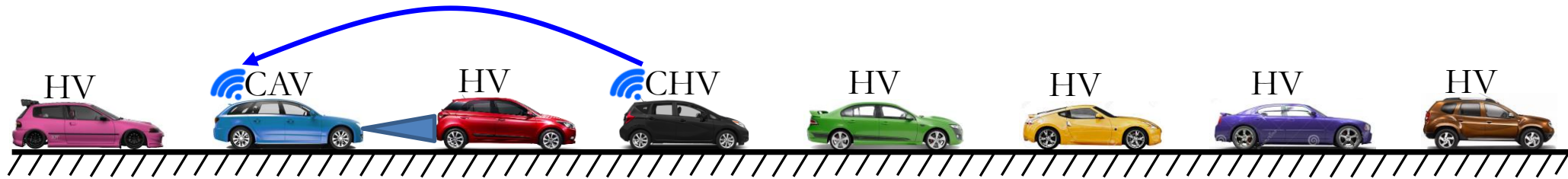
Connected Cruise Control (public road)



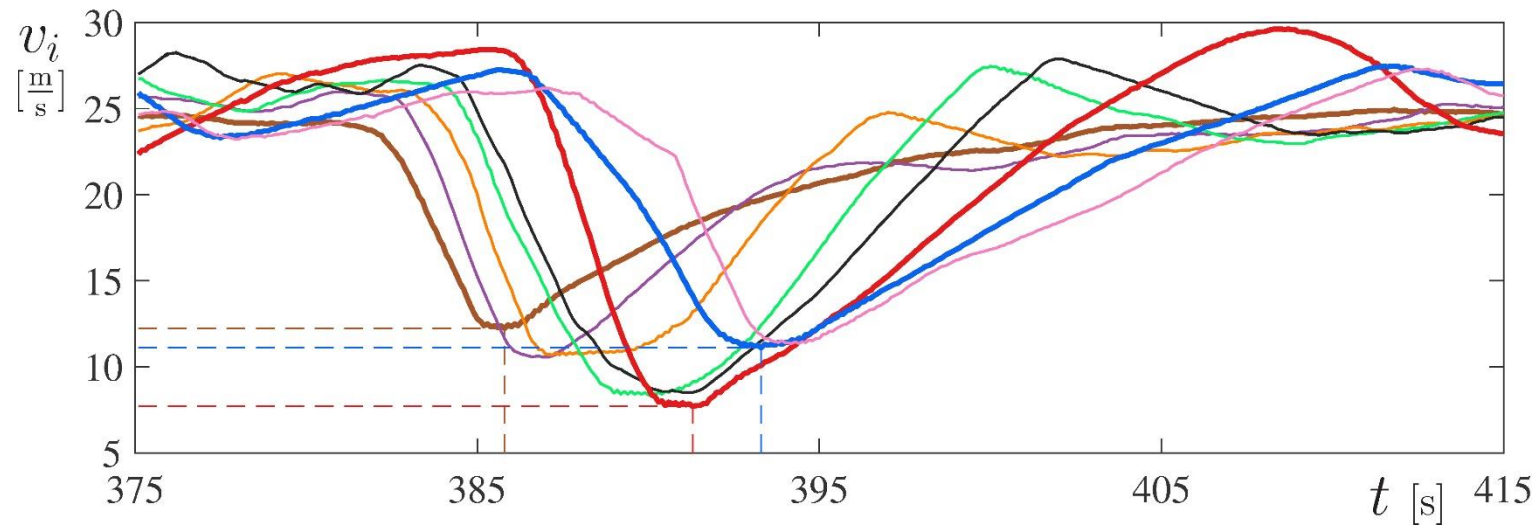
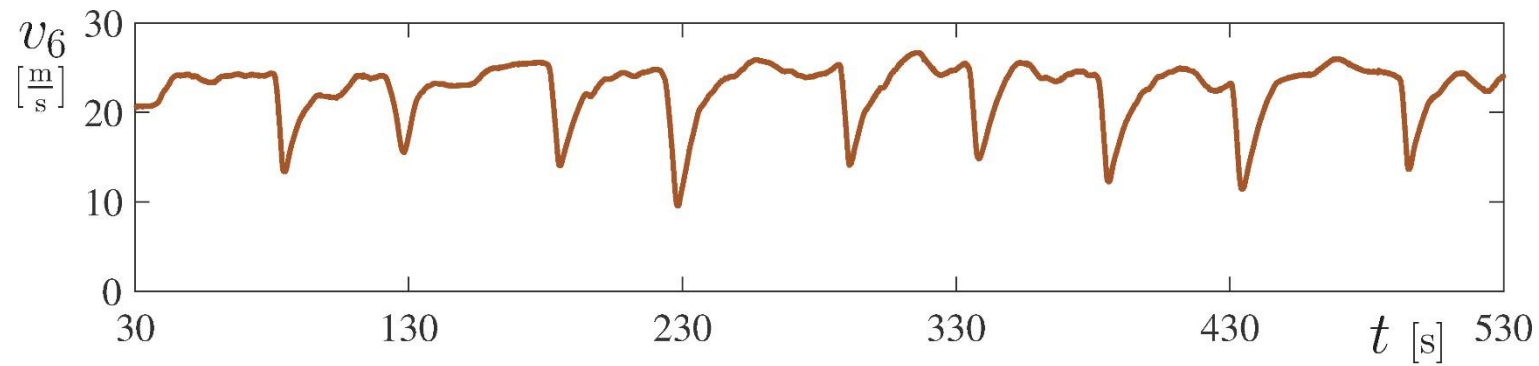
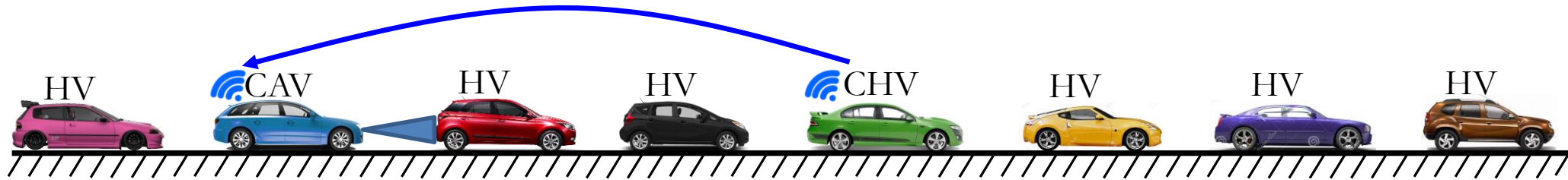
Connected Cruise Control (public road) Adaptive



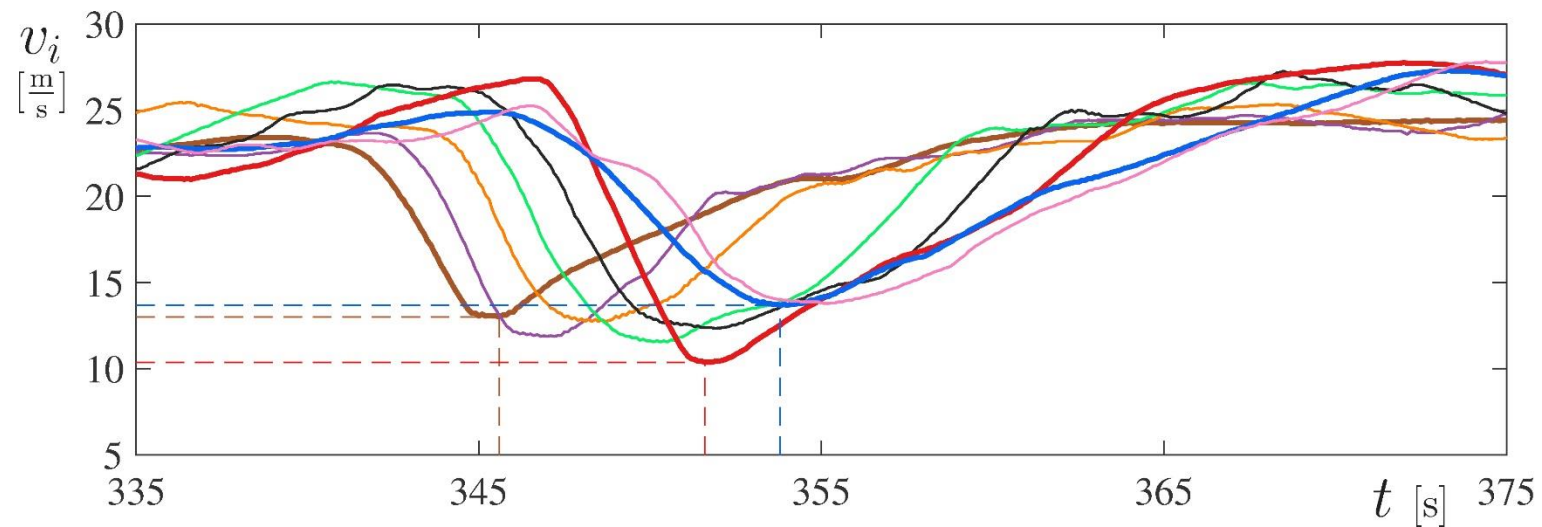
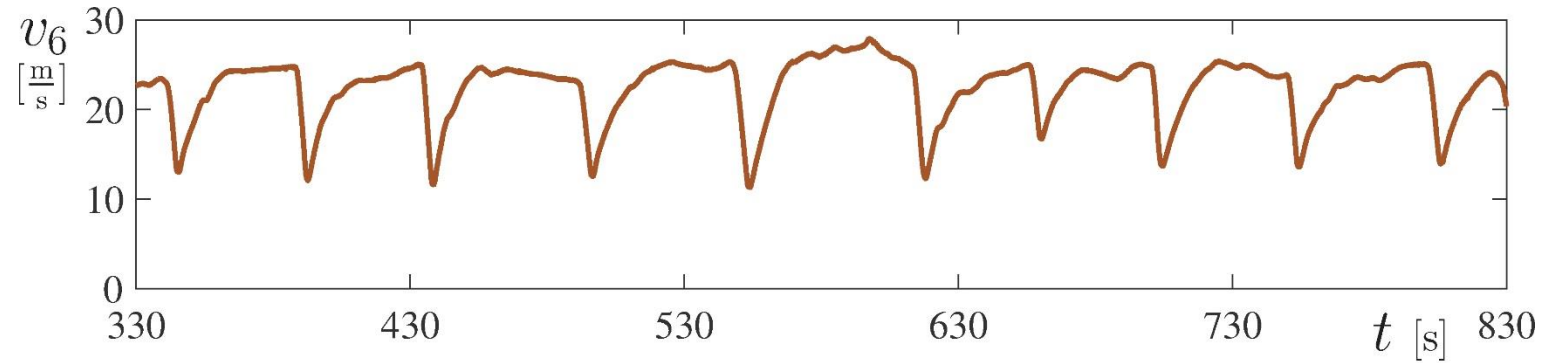
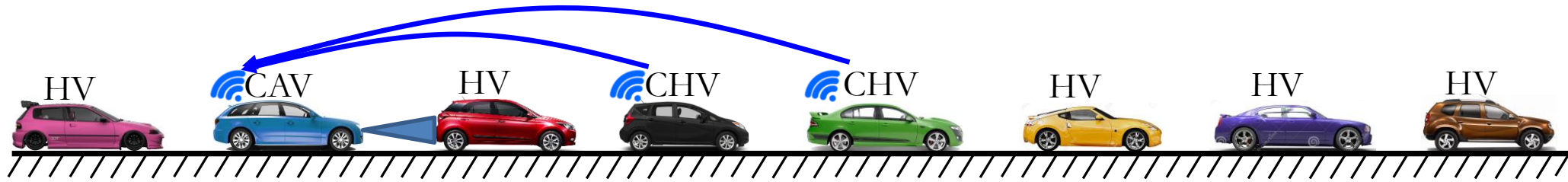
Connected Cruise Control (public road)



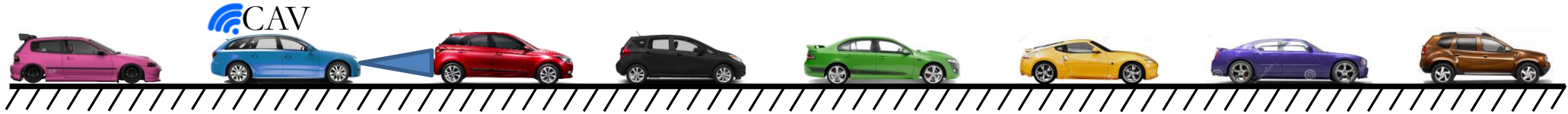
Connected Cruise Control (public road)



Connected Cruise Control (public road)

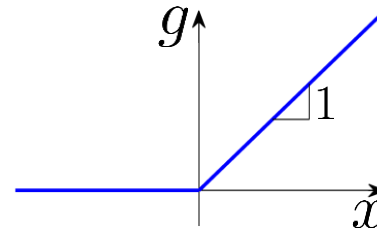


Energy Efficiency



Energy consumption (per unit mass)

$$w_i = \int_0^T g(\dot{v}_i(\theta)) v_i(\theta) d\theta$$



	w_{-1} [J/kg]	w_0 [J/kg]	w_1 [J/kg]	w_2 [J/kg]	w_3 [J/kg]	w_4 [J/kg]	w_5 [J/kg]	w_6 [J/kg]
Exp #1	86	93	100	79	77	72	66	63
Exp #2	90	88	97	100	96	87	83	81
Exp #3	83	84	100	94	91	81	77	73
Exp #4	80	76	100	84	85	77	71	65

7%
energy
saving
by
conne
ctivity

19%
energy
saving
by
conne
ctivity

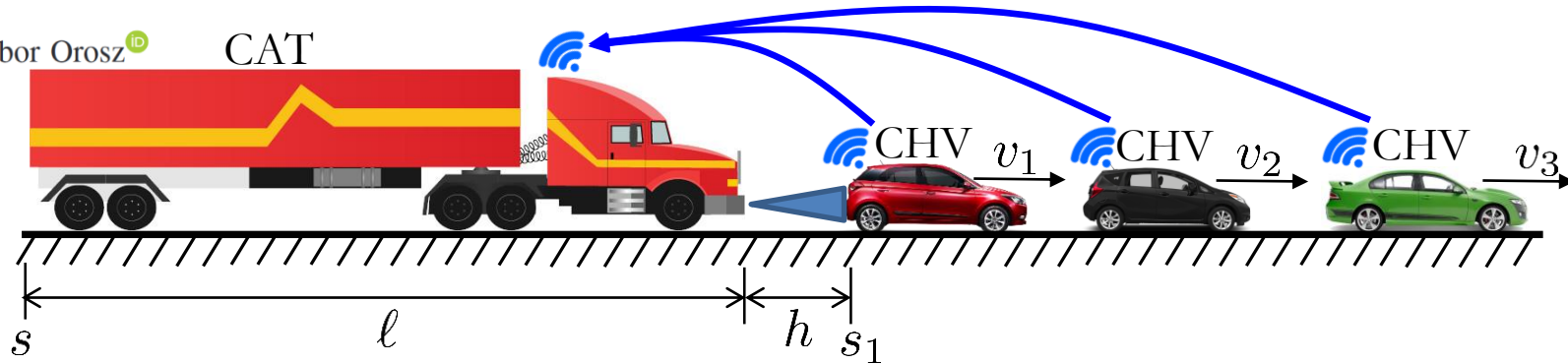
Energy Efficiency for Class-8 Trucks



Energy Efficiency of Class-8 Trucks

Fuel Efficient Connected Cruise Control for Heavy-Duty Trucks in Real Traffic

Chaozhe R. He^{ID}, Jin I. Ge^{ID}, and Gábor Orosz^{ID}



Independent of the control design:

Theorem:

$$\alpha_1(J) \leq w \leq \alpha_2(J)$$

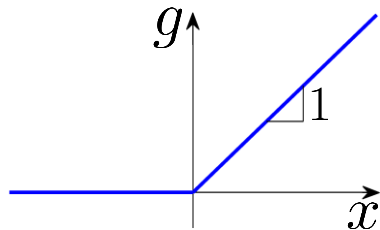
where

$$w = \int_0^T g(\dot{v}(\theta))v(\theta)d\theta$$

$$J = \sum_{k=0}^M \omega_k^2 D_k^2$$

$$\omega_k = k \frac{2\pi}{T}$$

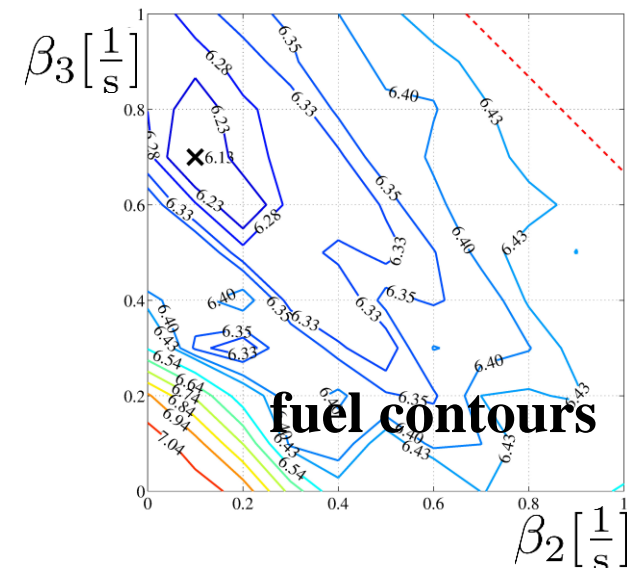
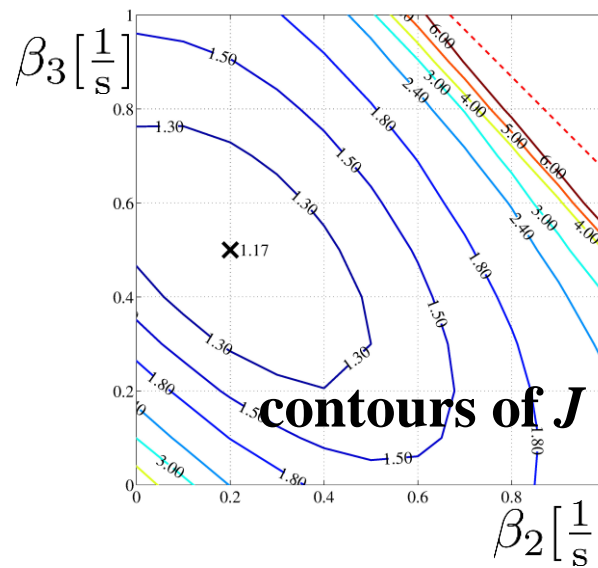
class \mathcal{K} functions



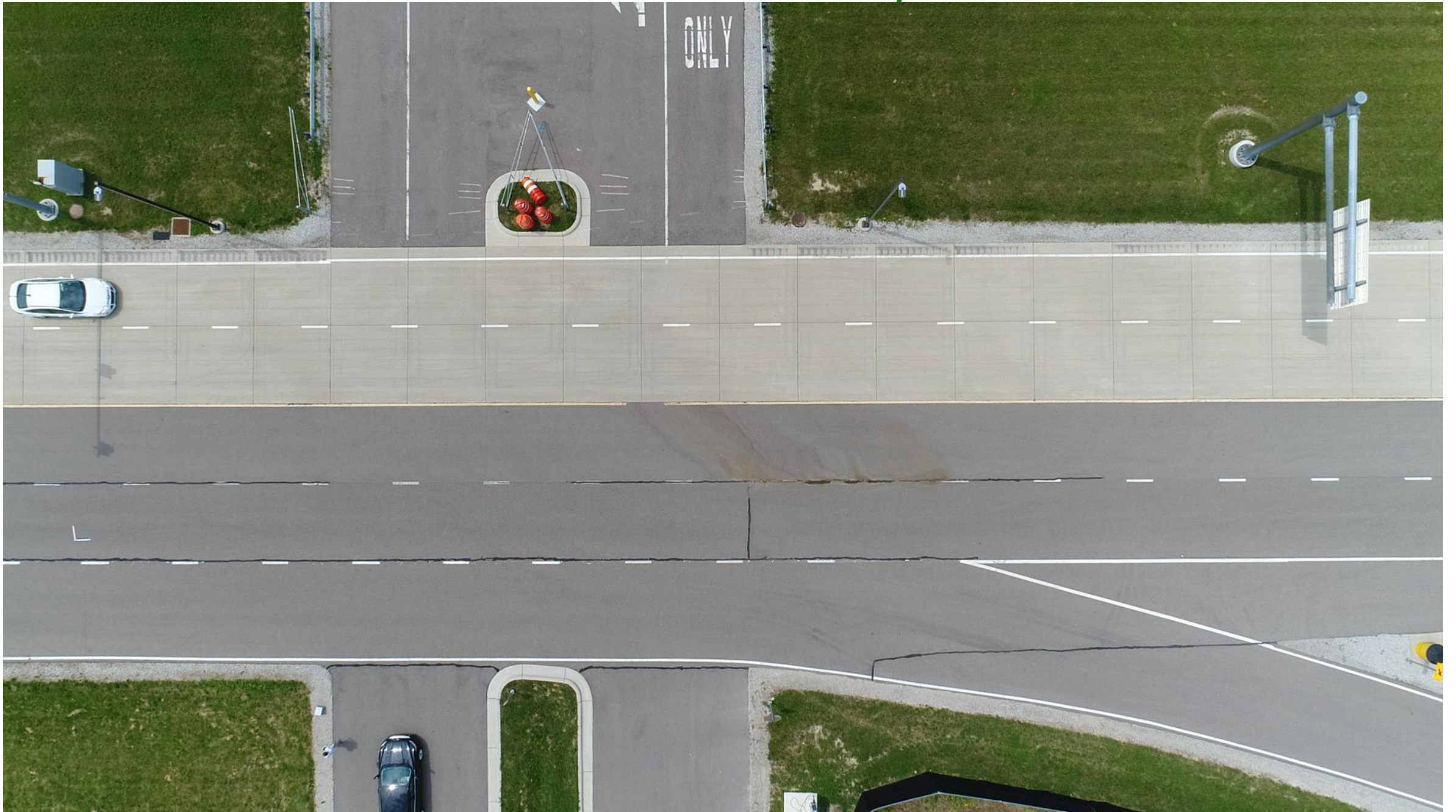
Fourier components

Applying this to the controller

$$u = \alpha (V(h) - v) + \beta_1(v_1 - v) + \beta_2(v_2 - v) + \beta_3(v_3 - v)$$



What about safety?



Verifying / Synthetizing Safe Controllers

Barrier functions

- based on Lyapunov approach
- provide sufficient conditions on user defined safety region

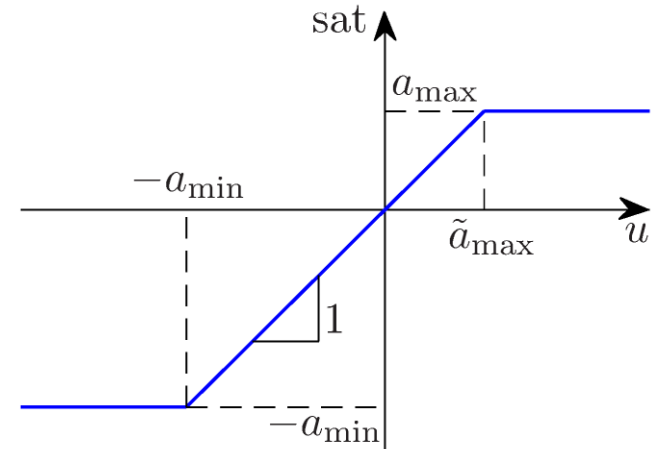
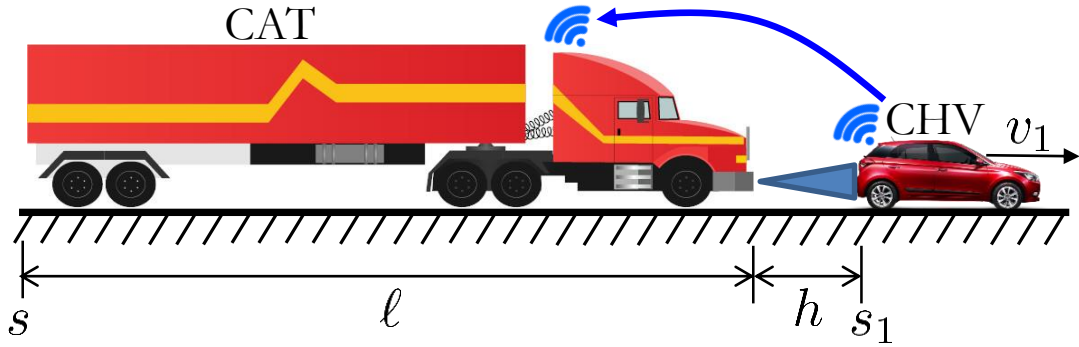
Formal methods

- based on linear temporal logic \wedge (and), \vee (or), \rightarrow (implies)
 \square (always), \diamond (eventually), $\square\diamond$
- discretizes time and quantizes state space and utilizes games
- give exact results but suffer from curse of dimensionality

Reachability calculations

- based on Hamilton-Jacobi PDEs
- utilizes differential games
- give exact results but suffer from curse of dimensionality

Barrier functions



Longitudinal dynamics

$$\dot{h} = v_1 - v$$

$$\dot{v} = \text{sat}(u)$$

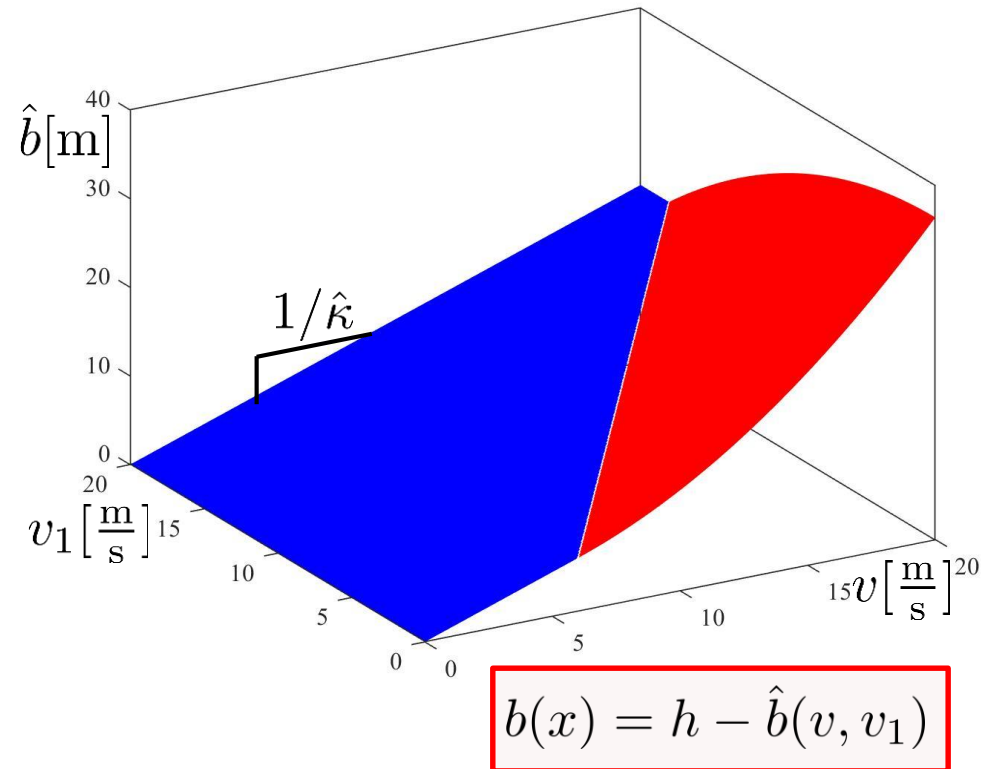
$$\dot{v}_1 = a_1 \longleftarrow -a_{1,\min} < a_1 < a_{1,\max}$$

Safety \Leftrightarrow Invariant set in state space $x = [h \quad v \quad v_1]^T$

$$\mathcal{S} = \{x \in \mathbb{R}^n : b(x) \geq 0\}$$

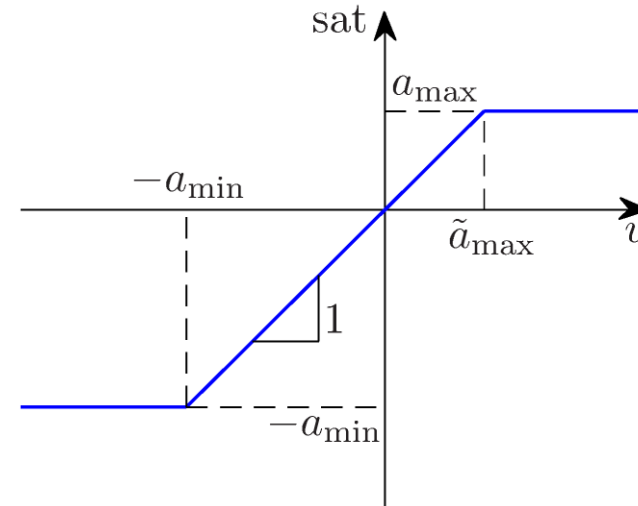
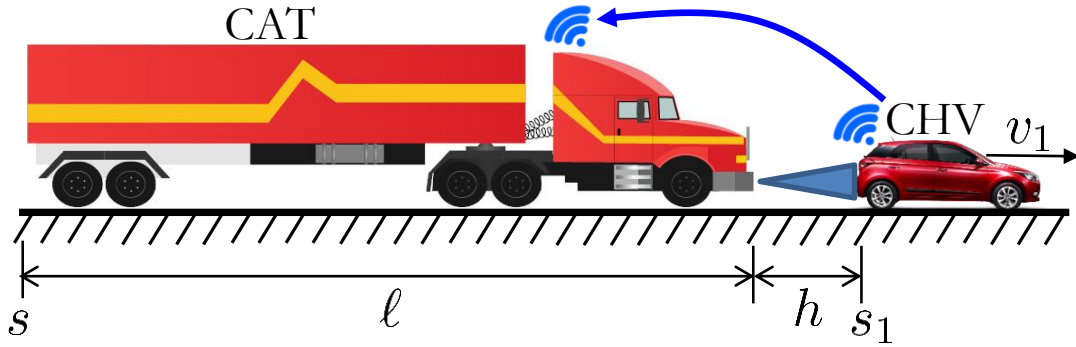
Theorem \mathcal{S} is invariant is $\exists \eta > 0$ s.t.

$$\sup_u \left[\dot{b}(x) + \eta b(x) \right] \geq 0, \quad \forall x \in \mathcal{S}$$



$$b(x) = h - \hat{b}(v, v_1)$$

Barrier functions



Longitudinal dynamics

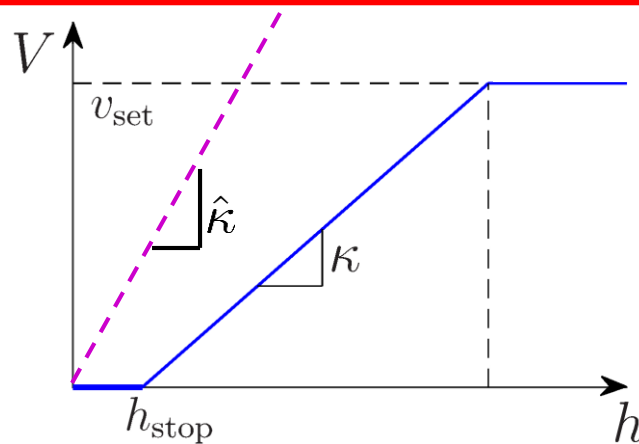
$$\dot{h} = v_1 - v$$

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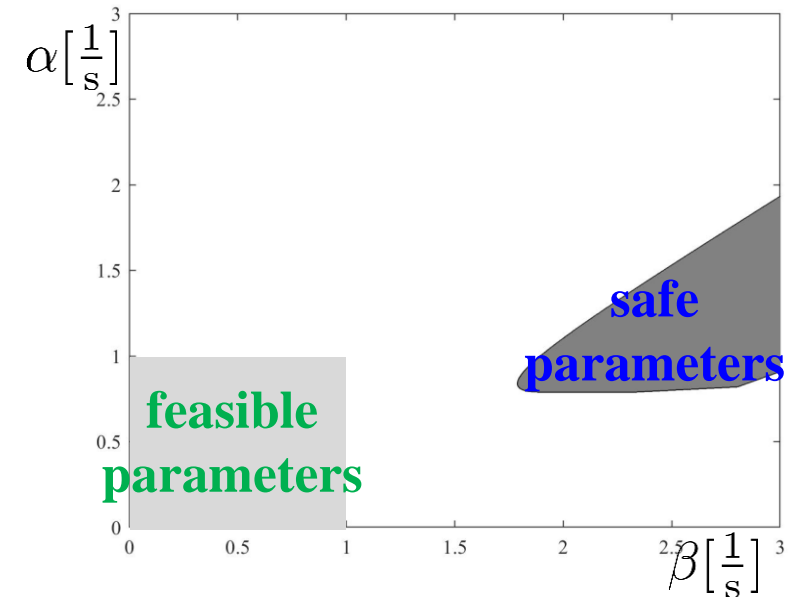
$$\dot{v}_1 = a_1 \longleftarrow -a_{1,\min} < a_1 < a_{1,\max}$$

Nominal controller

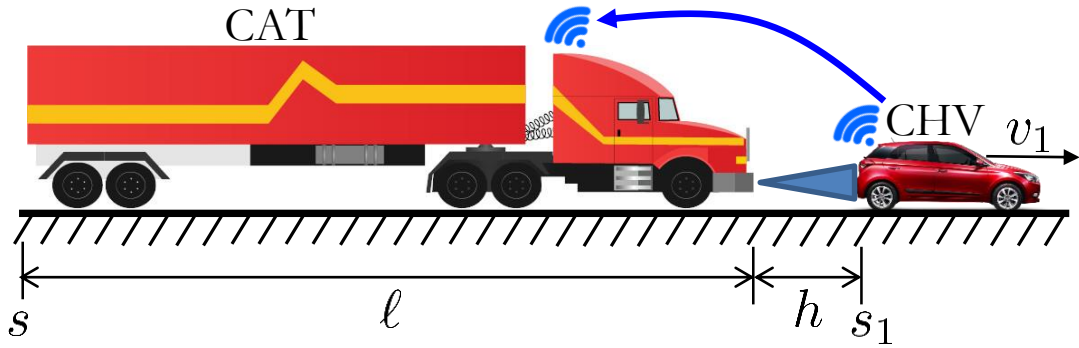
$$u = \alpha (V(h) - v) + \beta (v_1 - v)$$



Safety chart



Barrier functions



Longitudinal dynamics

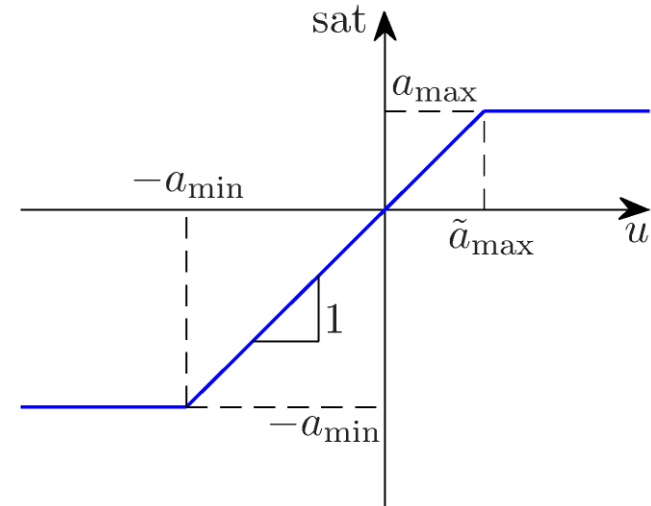
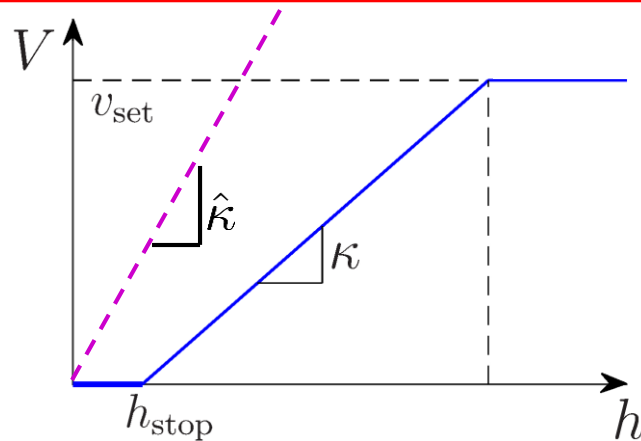
$$\dot{h} = v_1 - v$$

$$\dot{v} = \text{sat}(u)$$

$$\dot{v}_1 = a_1 \longleftarrow -a_{1,\min} < a_1 < a_{1,\max}$$

Nominal controller

$$u = \alpha (V(h) - v) + \beta (v_1 - v)$$

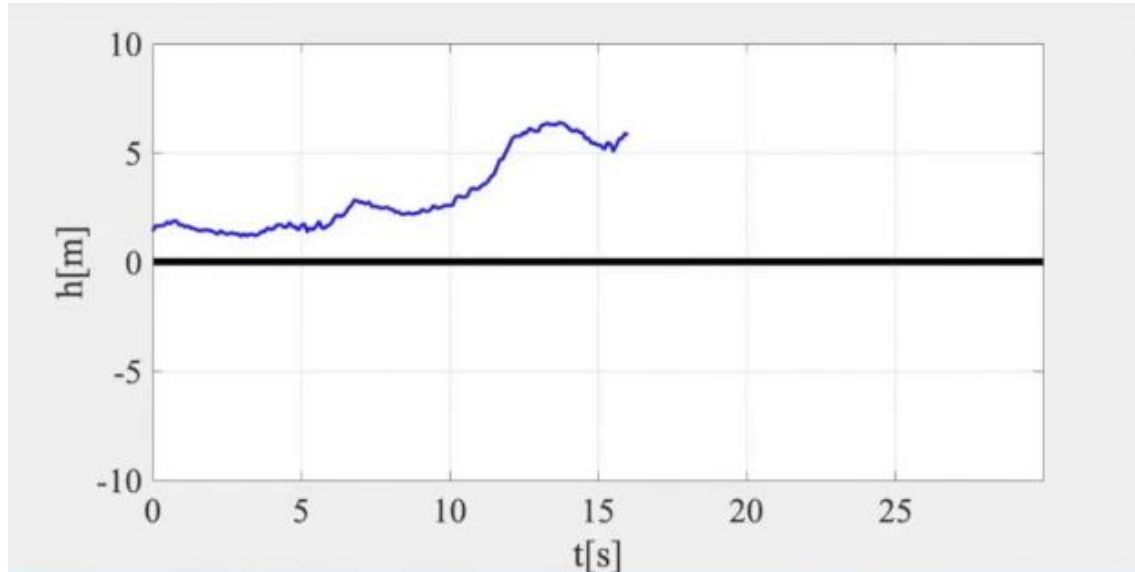


Intervening control $\min\{u, \hat{u}\}$

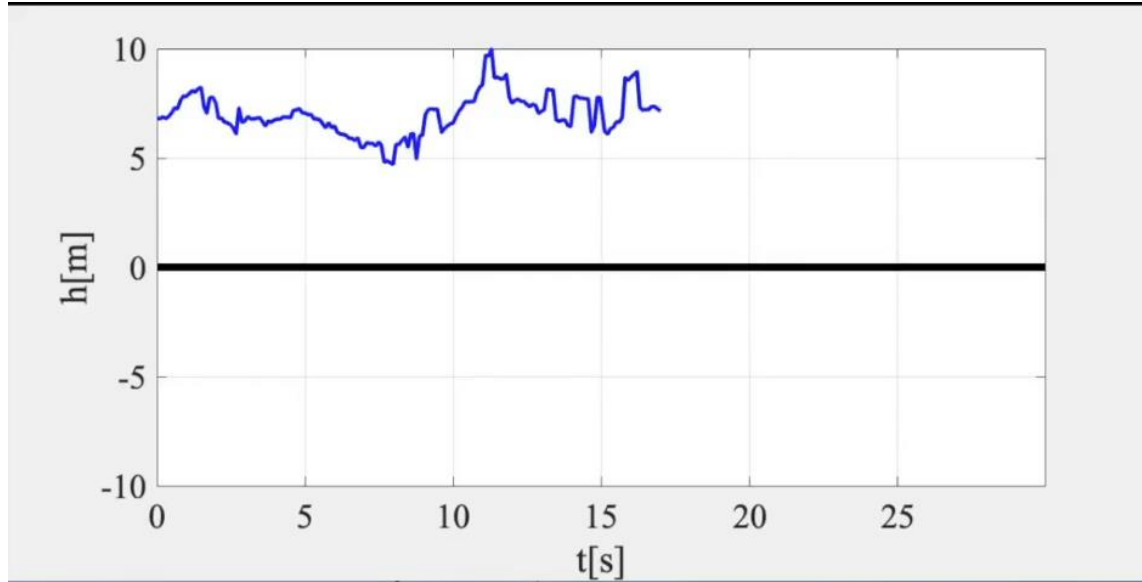
$$\hat{u} = \left(\frac{\partial \hat{b}}{\partial v} \right)^{-1} \left(v_1 - v - \frac{\partial \hat{b}}{\partial v_1} a_1 + \eta (h - \hat{b}) \right)$$

via connectivity

Without barrier function



With barrier function



Is there any way to resolve conflicts earlier?



Is there any way to resolve conflicts?



Conflicts Analysis

Longitudinal dynamics

$$\begin{aligned}\dot{r}_1 &= -v_1, \\ \dot{v}_1 &= \text{sat}(u_1), \\ \dot{r}_2 &= -v_2, \\ \dot{v}_2 &= \text{sat}(u_2),\end{aligned}$$

Conflict

$$C := \{\exists t, r_1(t) \in [-s, 0] \wedge r_2(t) \in [-s, 0]\} \quad s = L + l$$

Vehicle 2 merges ahead

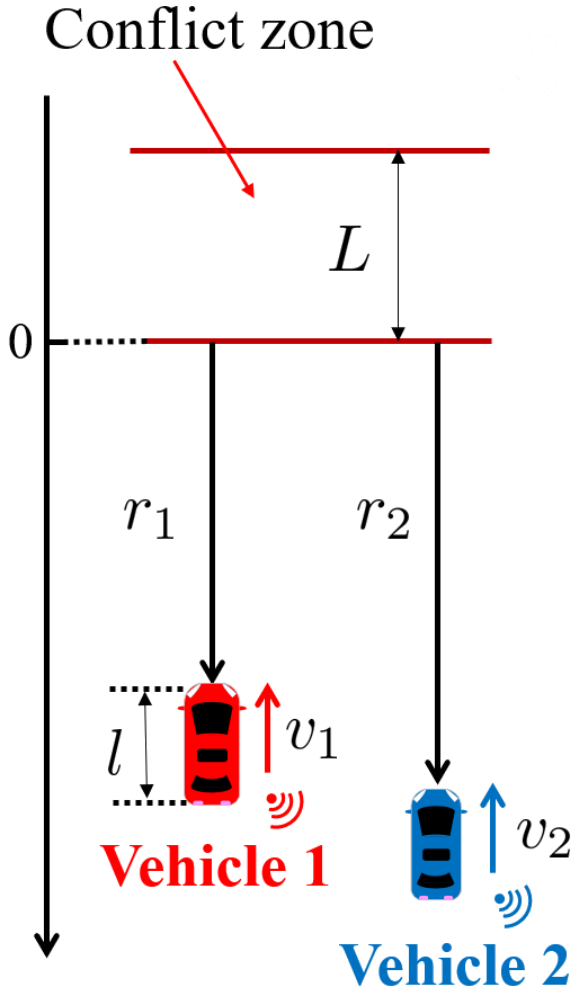
$$P := \{\exists t, r_1(t) = 0 \wedge r_2(t) < -s\}$$

Vehicle 2 merges behind

$$Q := \{\exists t, r_1(t) = -s \wedge r_2(t) > 0\}$$

Theorem

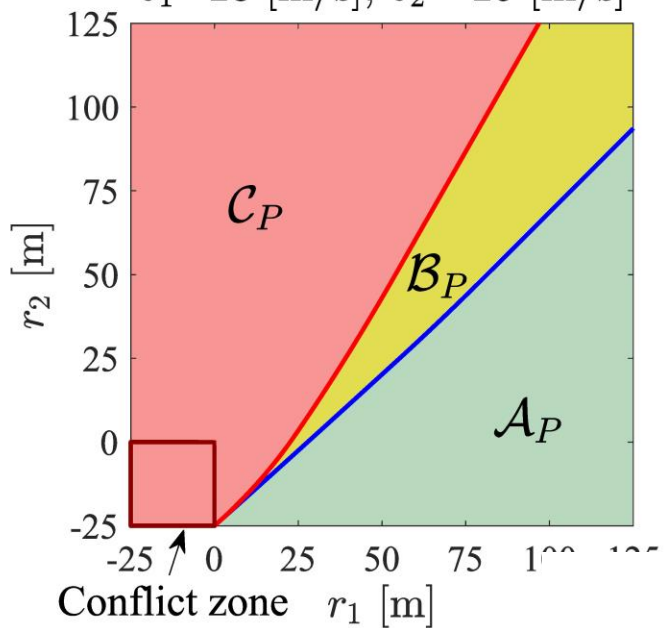
$$P \vee Q \iff \neg C$$



Conflicts Analysis

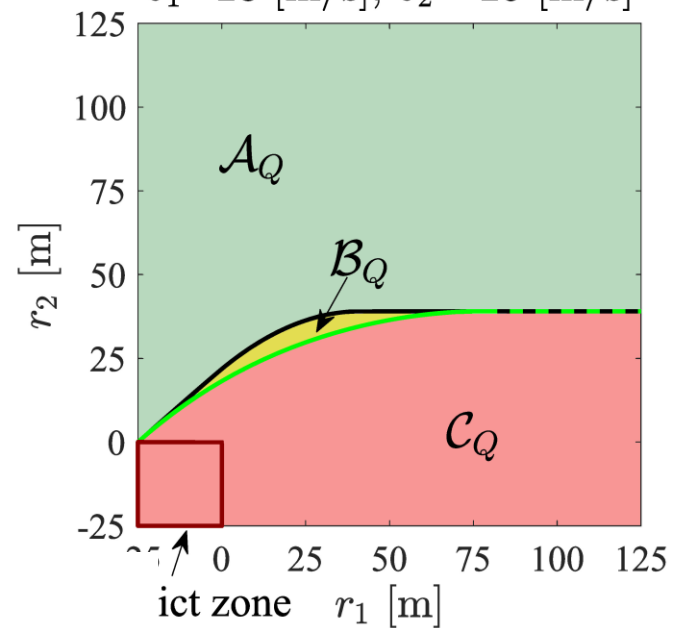
Vehicle 2 merges ahead

$v_1=28$ [m/s], $v_2=25$ [m/s]



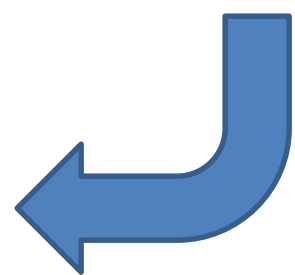
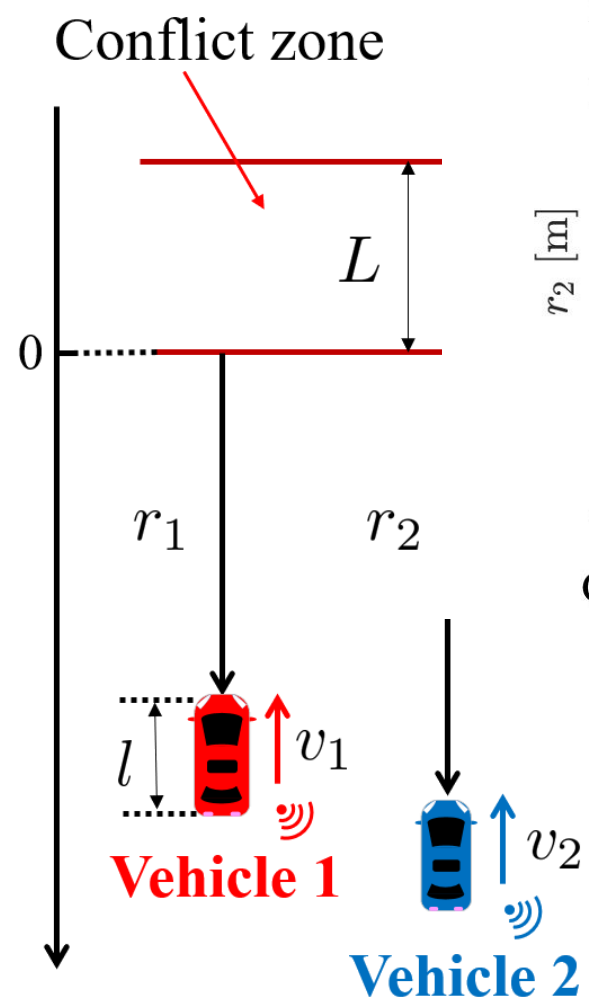
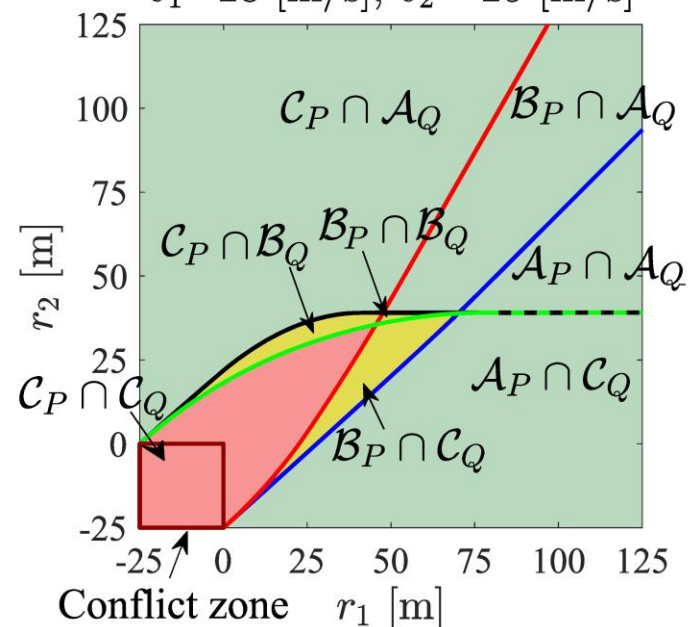
Vehicle 2 merges behind

$v_1=28$ [m/s], $v_2=25$ [m/s]



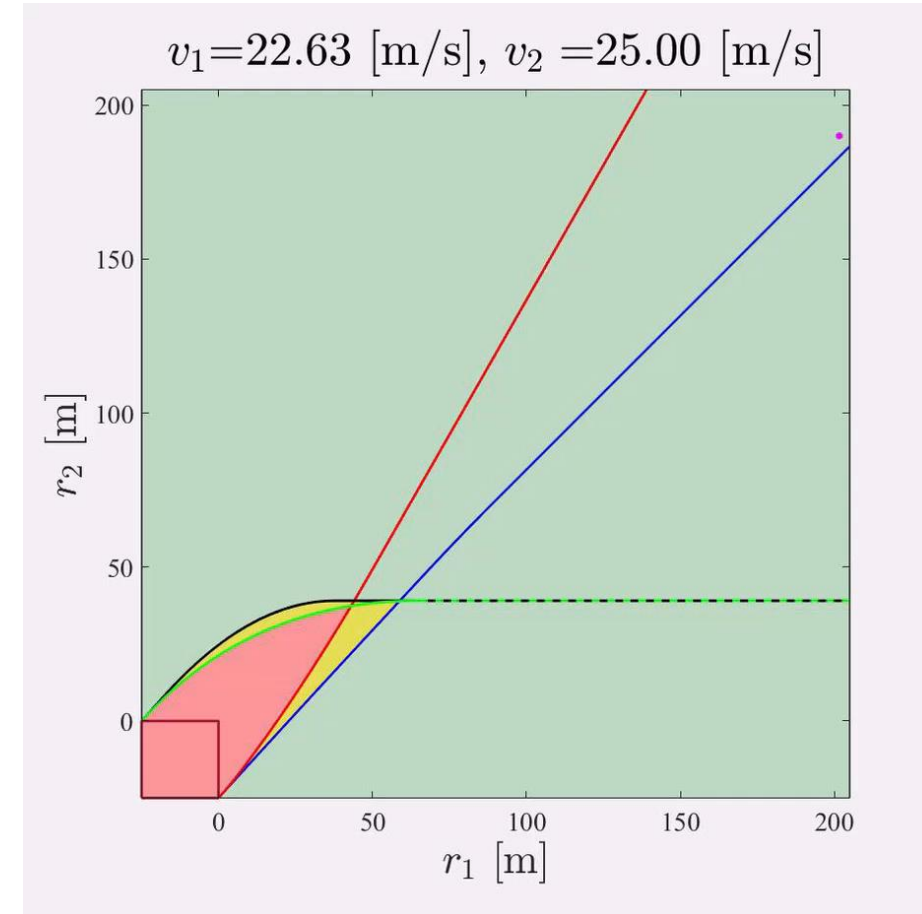
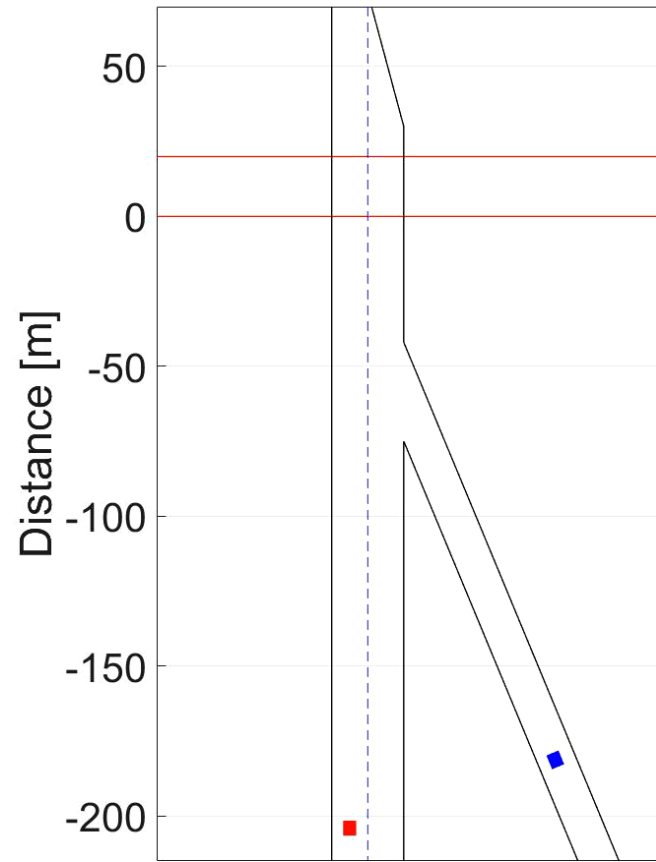
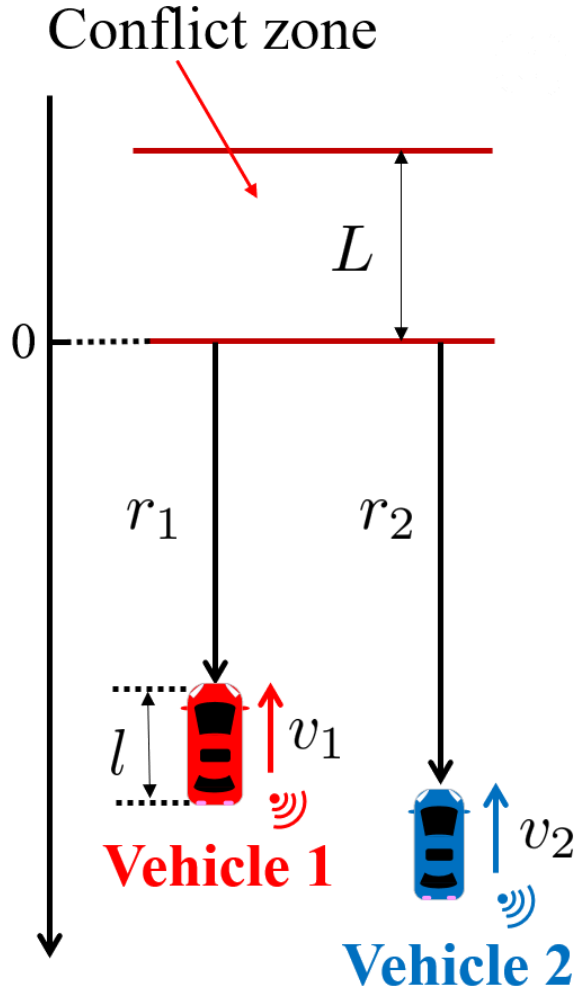
Conflict Chart

$v_1=28$ [m/s], $v_2=25$ [m/s]



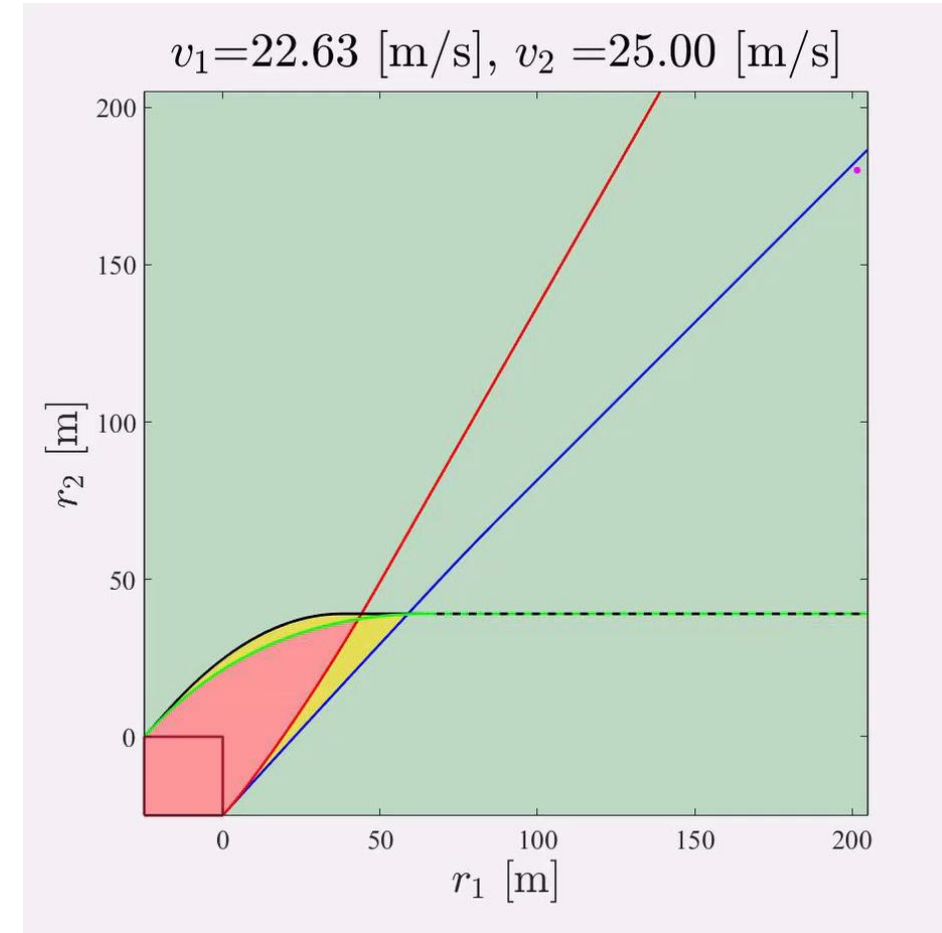
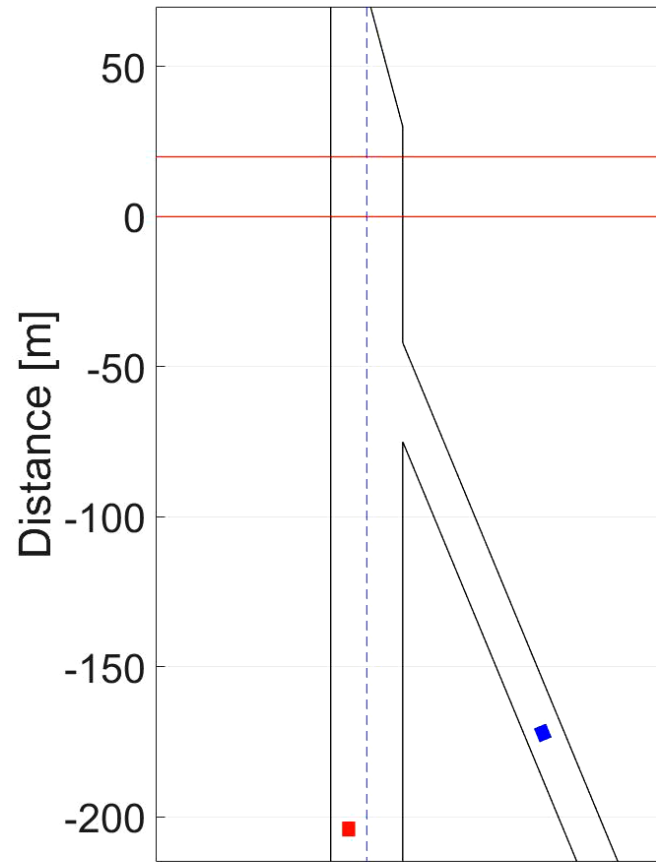
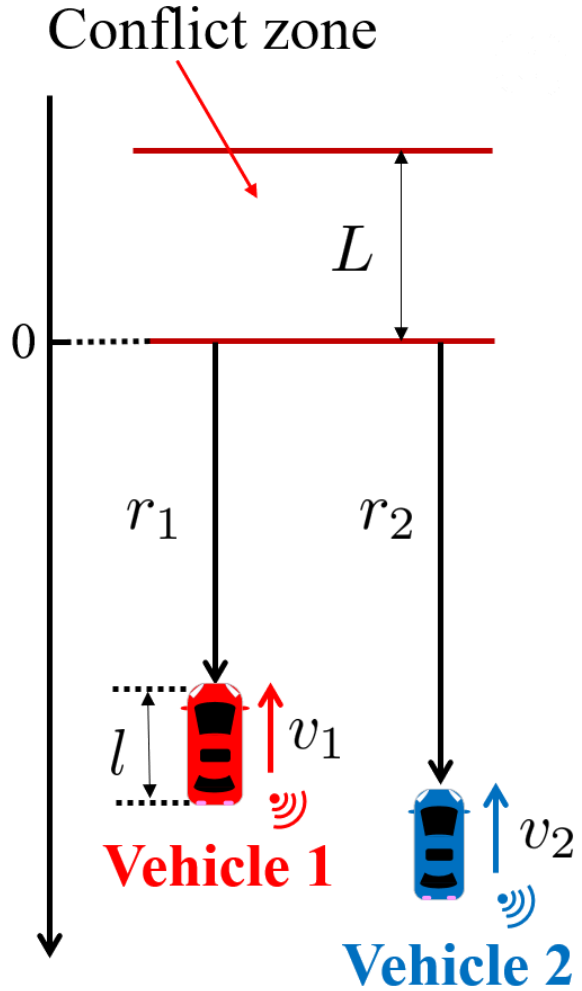
Connectivity Enabled Decision Making

Vehicle 2 merges behind



Connectivity Enabled Decision Making

Vehicle 2 merges ahead



Conclusions

- High level **societal goals** can be turned into **control objectives for CAVs**
- **Connectivity may help** CAVs to achieve better **performance and efficiency**
- **Safety** may be ensured using **barrier functions** and **conflict analysis**

Collaborators



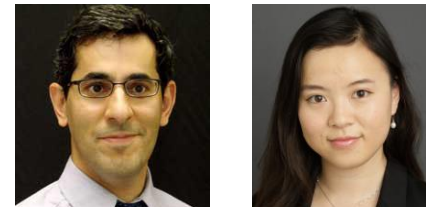
Caltech



Richard Murray Aaron Ames Joel Burdick



Gábor Stépán Tamás Insperger Dani Bachrathy Dénes Takács



Ardalan Vahidi Rose Yu



Jim Yan
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Matt Hunkler



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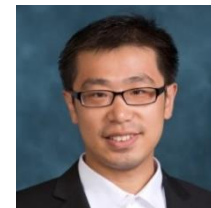
Onur Altintas
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John Kenney



Sergei Avedisov



Eric Tseng
Wayne Williams
Helen Kouros
Mike Hopka
Devesh Upadhyay
Michiel van Nieuwstadt



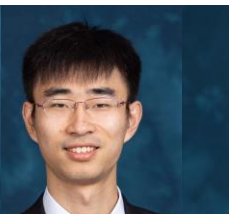
Linjun Zhang



Tamás Molnár



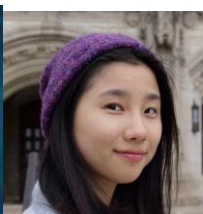
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Johaann Chacko Mathew
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Ilya Kolmanovsky



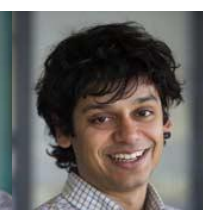
Neda Masoud



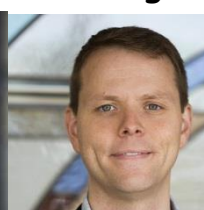
Necmiye Ozay



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Ram Vasudevan



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